

SMEFT at NLO  
Celine Degrande

# Plan

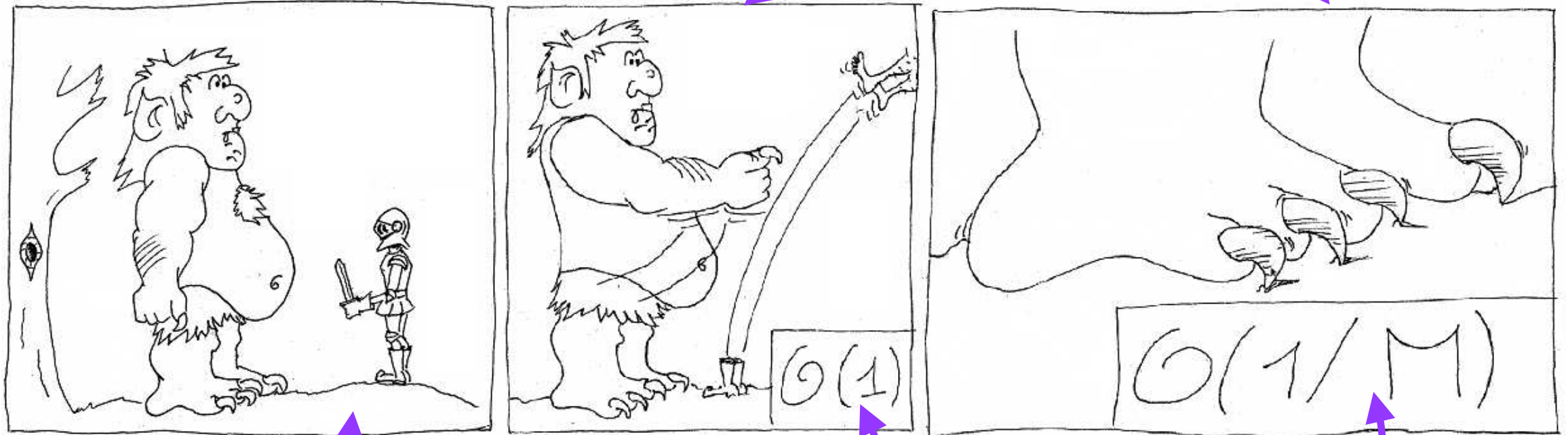
- Introduction
- Challenges
- Status
- Outlook

In collaboration with G. Durieux, F. Maltoni, K. Mimasu, A. Vasquez, E. Vryonidou,  
C. Zhang

# Introduction

# EFT and NLO

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{d>4} \sum_i \frac{C_i}{\Lambda^{d-4}} \mathcal{O}_i^d$$



$$\frac{d\sigma}{dX} = \alpha_s^2 \frac{d\sigma^{LO}}{dX} + \alpha_s^3 \frac{d\sigma^{NLO}}{dX} + \alpha_s^4 \frac{d\sigma^{NNLO}}{dX} + \dots$$

$$\frac{d\sigma}{dX} = \alpha_s^2 0 + \alpha_s^3 \frac{d\sigma^{LO}}{dX} + \alpha_s^4 \frac{d\sigma^{NLO}}{dX} + \dots$$

Tree-level
One-loop
Two-loop

Automation of one-loop for SMEFT

# Precision era at the LHC

## Standard Model Total Production Cross Section Measurements

Status:  
July 2018

$\int \mathcal{L} dt$   
[fb<sup>-1</sup>]

Reference

+jets

- pp
- W
- Z
- t $\bar{t}$
- t $\bar{t}$ -char
- WW
- H
- Wt
- WZ
- ZZ
- t $\bar{t}$ -char
- ttW
- t $\bar{t}$ Z
- tZj

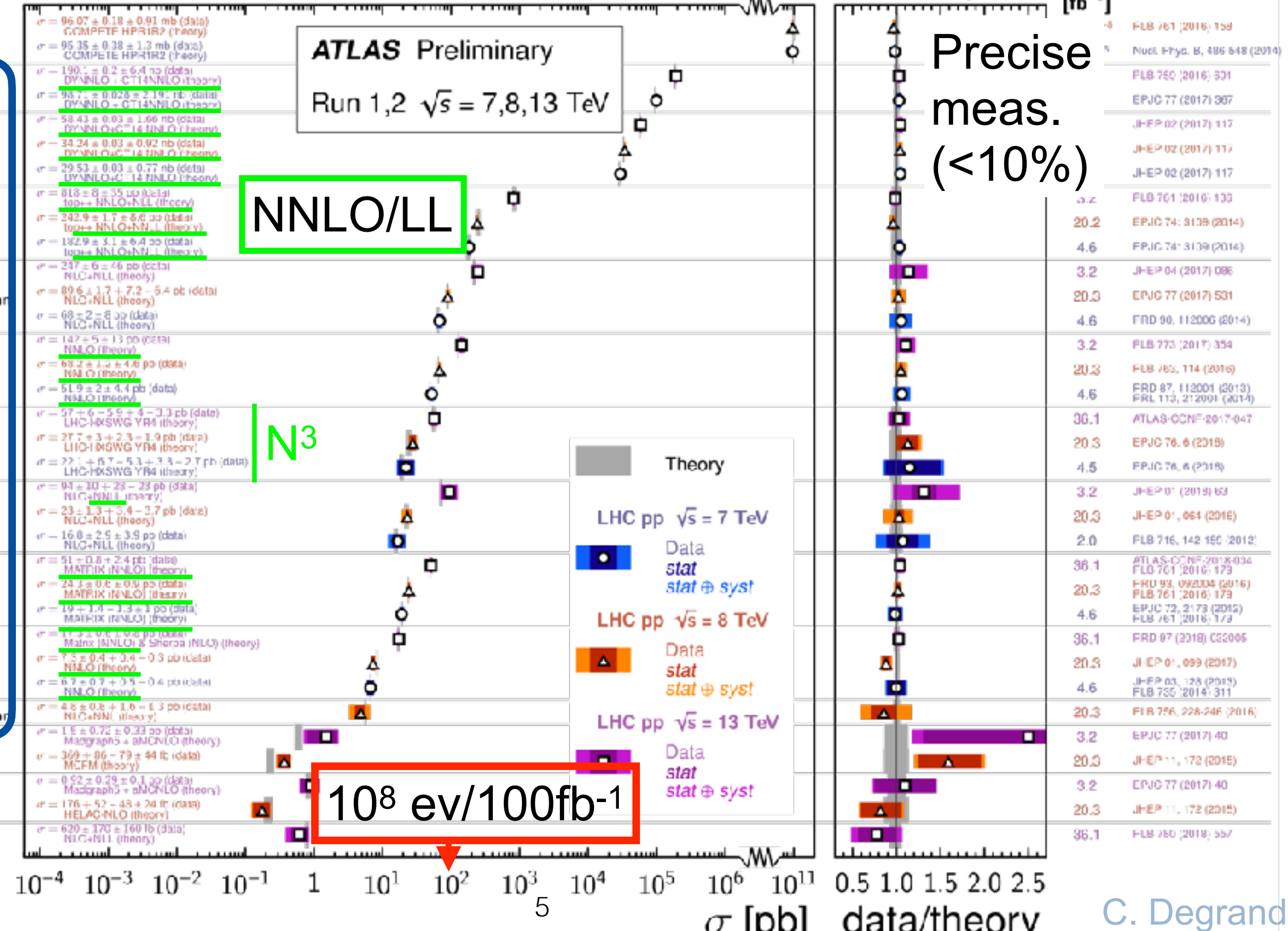
ATLAS Preliminary  
Run 1,2  $\sqrt{s} = 7,8,13$  TeV

NNLO/LL

N<sup>3</sup>

10<sup>8</sup> ev/100fb<sup>-1</sup>

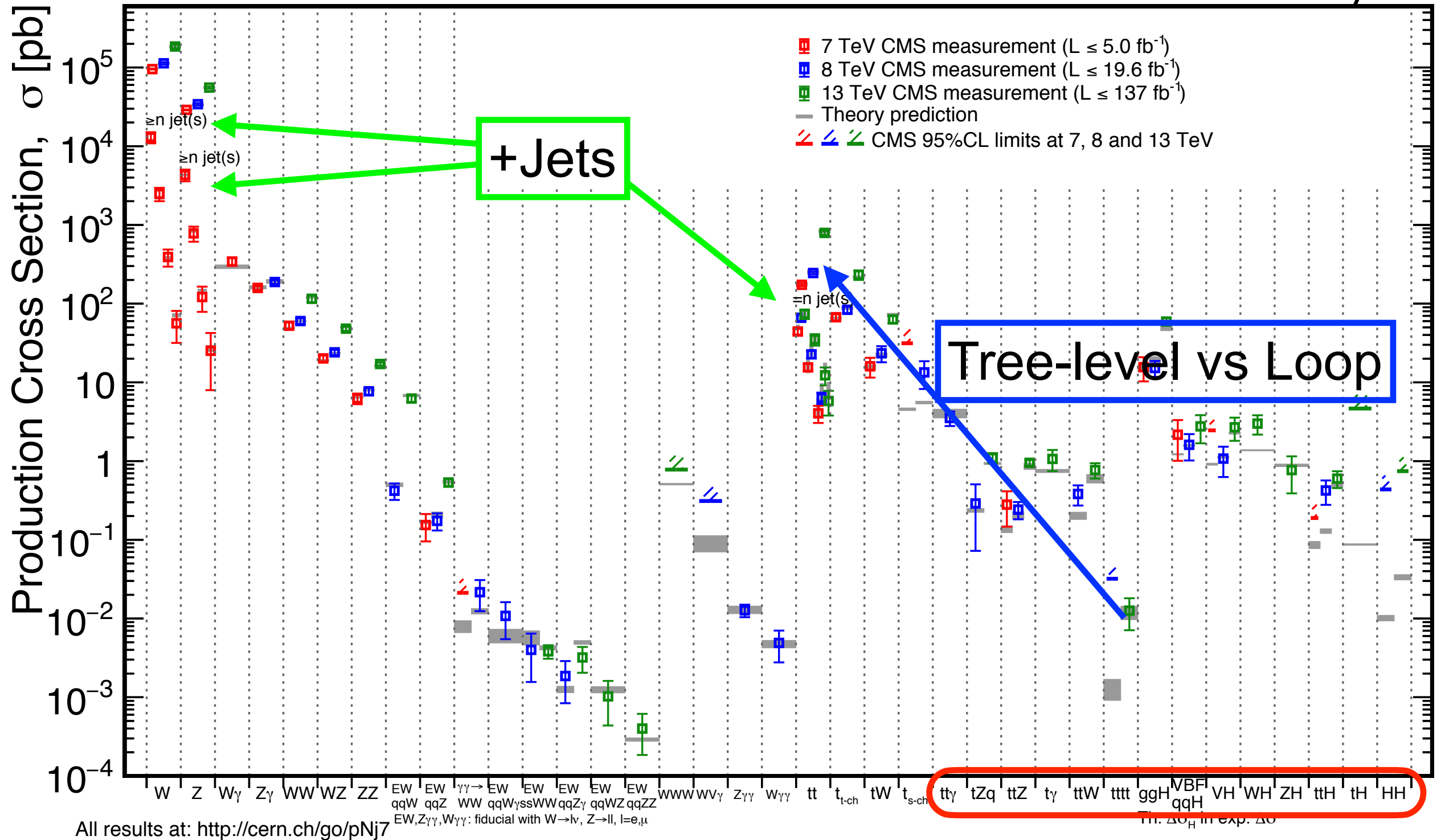
Precise meas.  
(<10%)



# Precision era at the LHC

September 2019

CMS Preliminary



# Challenges

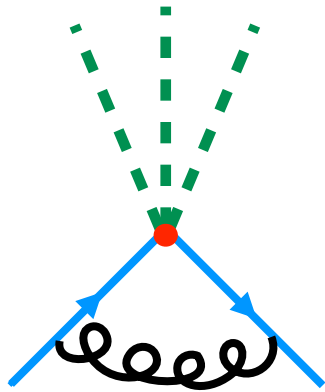
# EFT at NLO (QCD)

B. Grzadkowski et al, JHEP 1010 (2010) 085

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi}$	<del><math>(\varphi^{\dagger} \varphi)^3</math></del>	$Q_{e\varphi}$	<del><math>(\varphi^{\dagger} \varphi)(\bar{l}_p e_r \varphi)</math></del>
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi\Box}$	<del><math>(\varphi^{\dagger} \varphi)\Box(\varphi^{\dagger} \varphi)</math></del>	$Q_{u\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	<del><math>\epsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}</math></del>	$Q_{\varphi D}$	<del><math>(\varphi^{\dagger} D^{\mu} \varphi)^* (\varphi^{\dagger} D_{\mu} \varphi)</math></del>	$Q_{d\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	<del><math>\epsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}</math></del>				
				<b>No QCD particle</b>	
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^{\dagger} \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	<del><math>(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I</math></del>	$Q_{\varphi l}^{(1)}$	<del><math>(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{l}_p \gamma^{\mu} l_r)</math></del>
$Q_{\varphi \tilde{G}}$	$\varphi^{\dagger} \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	<del><math>(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}</math></del>	$Q_{\varphi l}^{(3)}$	<del><math>(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{l}_p \tau^I \gamma^{\mu} l_r)</math></del>
$Q_{\varphi W}$	<del><math>\varphi^{\dagger} \varphi W_{\mu\nu}^I W^{I\mu\nu}</math></del>	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	<del><math>(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{e}_p \gamma^{\mu} e_r)</math></del>
$Q_{\varphi \tilde{W}}$	<del><math>\varphi^{\dagger} \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}</math></del>	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{q}_p \gamma^{\mu} q_r)$
$Q_{\varphi B}$	<del><math>\varphi^{\dagger} \varphi B_{\mu\nu} B^{\mu\nu}</math></del>	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	<del><math>(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{q}_p \tau^I \gamma^{\mu} q_r)</math></del>
$Q_{\varphi \tilde{B}}$	<del><math>\varphi^{\dagger} \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}</math></del>	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} u_r)$
$Q_{\varphi WB}$	<del><math>\varphi^{\dagger} \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}</math></del>	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{d}_p \gamma^{\mu} d_r)$
$Q_{\varphi \tilde{W}B}$	<del><math>\varphi^{\dagger} \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}</math></del>	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^{\dagger} D_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} d_r)$



# EFT at NLO



In the loop: same as SM  
 +axial anomaly  $(\varphi^\dagger \varphi) (\bar{q}_p u_r \tilde{\varphi})$   
 $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{q}_p \gamma^\mu q_r)$

$$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$$

$$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$$

More momenta: higher rank of the integral numerator

Additional gamma and colour algebra

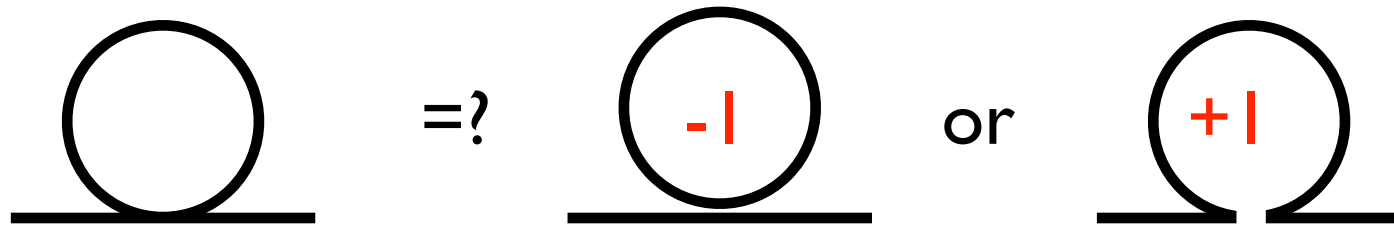
$$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$$

# EFT at NLO

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	<del><math>(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)</math></del>	$Q_{ee}$	<del><math>(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)</math></del>	$Q_{le}$	<del><math>(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)</math></del>
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

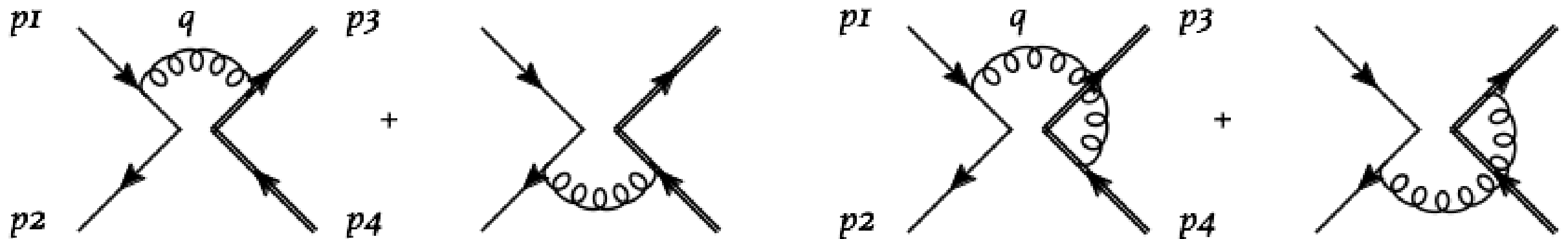
Same as SM but axial anomaly!

# EFT at NLO



Evanescent operators:

$$O_{ut}^{(8)} = (\bar{u}\gamma^\mu T^A u) (\bar{t}\gamma_\mu T^A t)$$

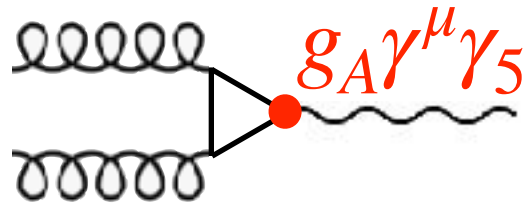


$$\gamma^\mu \gamma^\nu \gamma^\rho P_R \otimes \gamma_\mu \gamma_\nu \gamma_\rho P_R = E + (16 - 4a\varepsilon) \gamma^\mu P_R \otimes \gamma_\mu P_R$$

$$\gamma^\mu \gamma^\nu \gamma^\rho P_R \otimes \gamma_\rho \gamma_\nu \gamma_\mu P_R = -E + [4 - (12 - 4a)\varepsilon] \gamma^\mu P_R \otimes \gamma_\mu P_R$$

**Extra R2 (gauge invariant)**  
**Change the UV matching**

# Axial anomaly



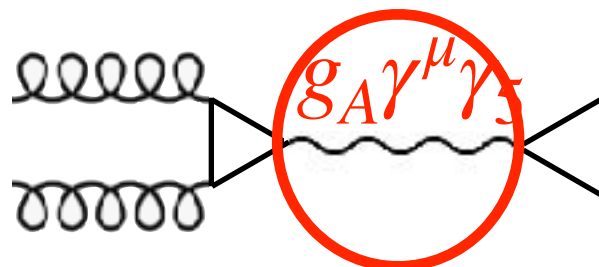
SM:

$$g_A^u = g_A^c = g_A^t = -g_A^d = -g_A^s = -g_A^b$$

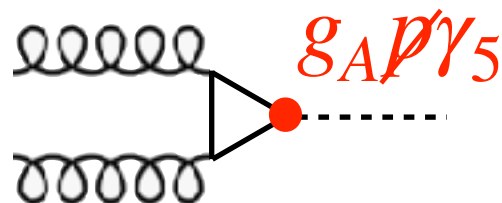
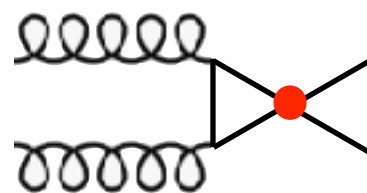
SMEFT:

$$g_A^u \neq g_A^c \neq g_A^t \neq -g_A^d \neq -g_A^s \neq -g_A^b$$

+ modification of quarks-gluon vertex (chromo)



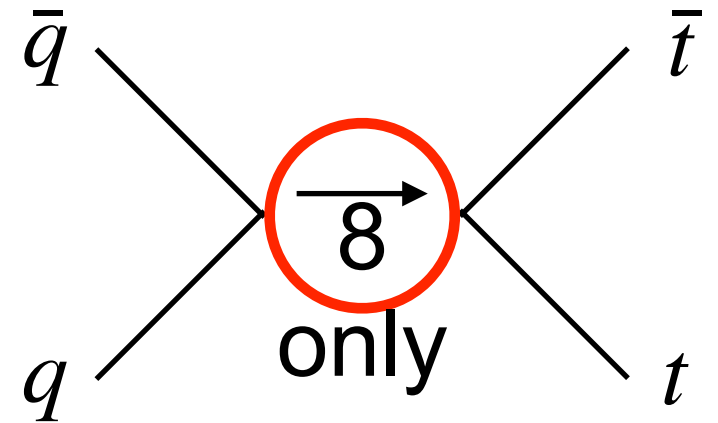
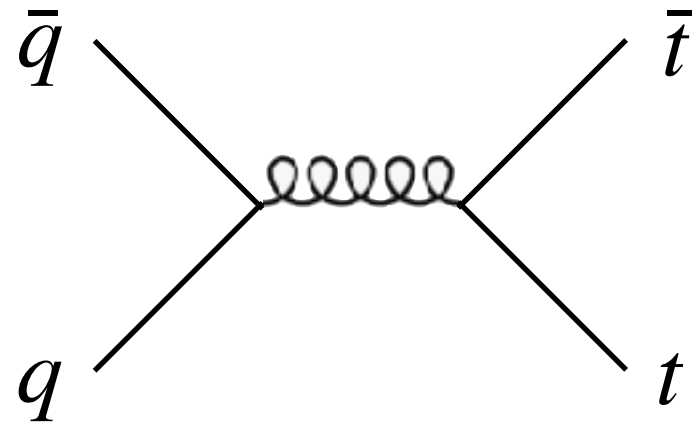
=



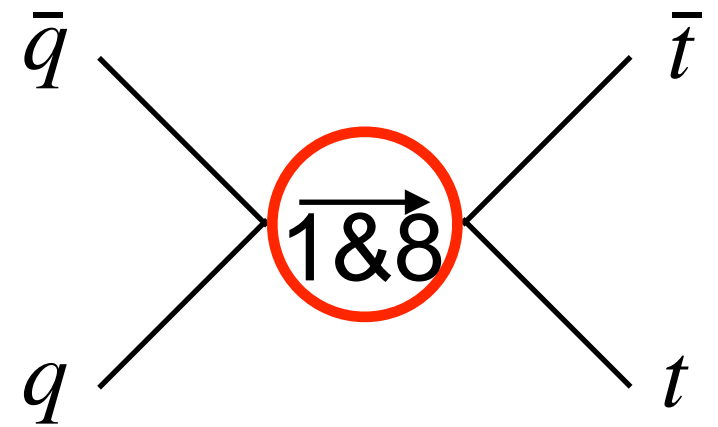
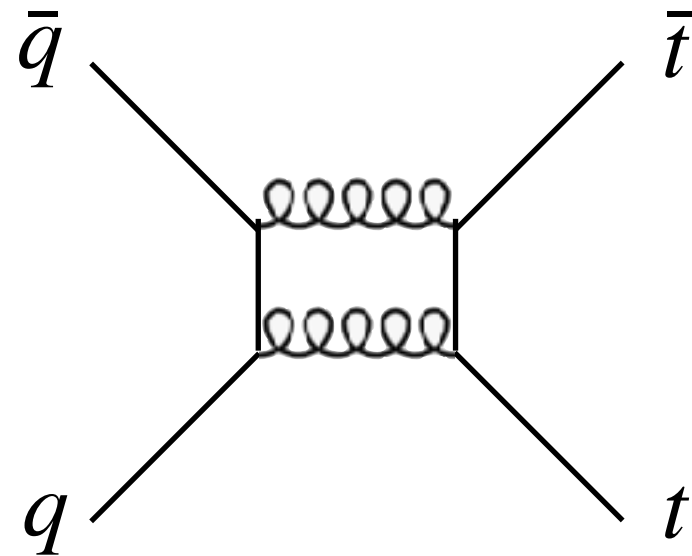
$$\propto \epsilon^{p_1 p_2 \mu_1 \mu_2}$$

# More operators/process

LO:



NLO:

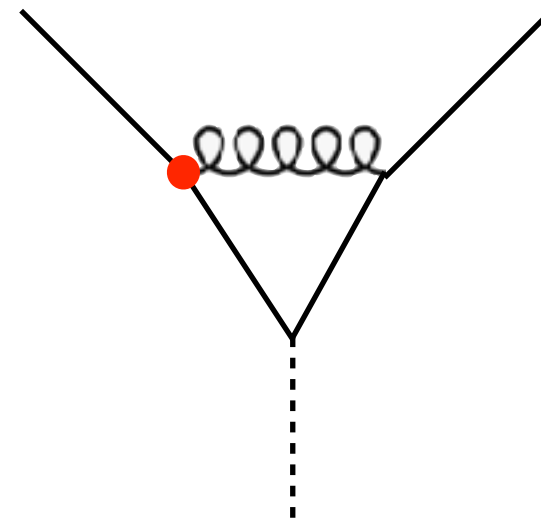


- 4-tops to top pair prod.,....
- Fit & correlations

# Running and mixing

$C_{uG}^{(13)}$ ,  $C_{uW}^{(13)}$ ,  $C_{uB}^{(13)}$  and  $C_{u\varphi}^{(13)}$

$$\gamma = \frac{\alpha_S}{\pi} \begin{pmatrix} \frac{1}{3} & 0 & 0 & 0 \\ \frac{2}{3} & 0 & 0 & 0 \\ \frac{10}{9} & 0 & \frac{2}{3} & 0 \\ 4y_t^2 & 0 & 0 & -2 \end{pmatrix}$$

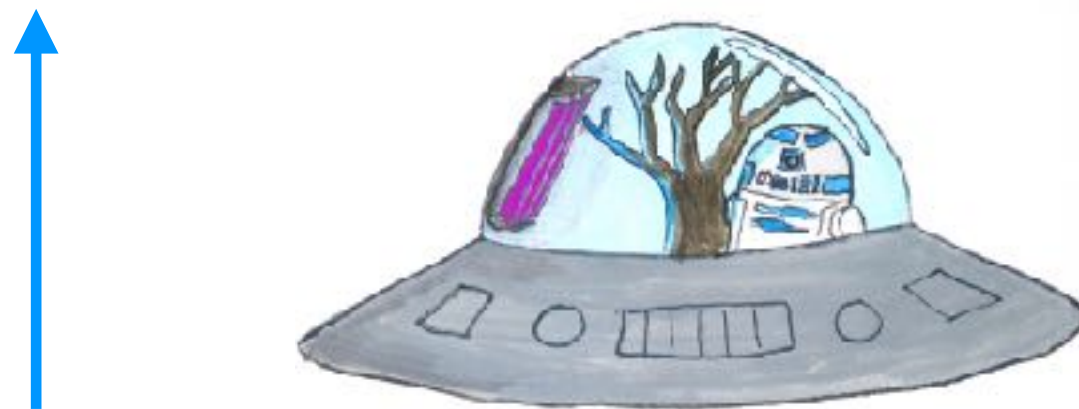


R. Alonso, E. Jenkins, A. Manohar, M. Trott, *JHEP* 10 (2013) 087, *JHEP* 01 (2014) 035, *JHEP* 04 (2014) 159

Status

# Automated BSM at one-loop

- NLO for tree-level processes/LO for loop-induced
- dimension-4 BSM at first
- MadGraph5\_aMC@NLO: one-loop computation + PS



- FeynRules: Model tree-level vertices and UV/R2 counterterms
  - UV+basis reduction, check R. Alonso, E. E. Jenkins, A. V. Manohar, M. Trott, JHEP 1404 (2014) 159



- SM counterterms for EW
- Anomalous gluon interaction:
  - V. Hirschi, F. Maltoni, I. Tsinikos, E. Vryonidou, *JHEP* 07 (2018) 093
- Higgs gluon interaction: like SM heavy top limit for H prod but for HH (A. Buchalla et al, *JHEP* 09 (2018) 057), ...

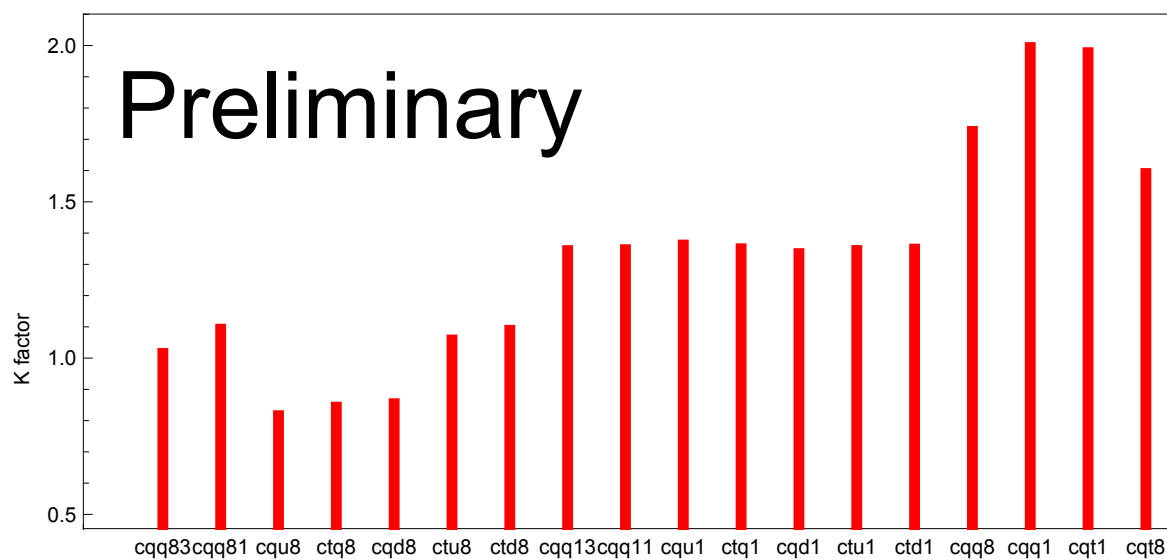
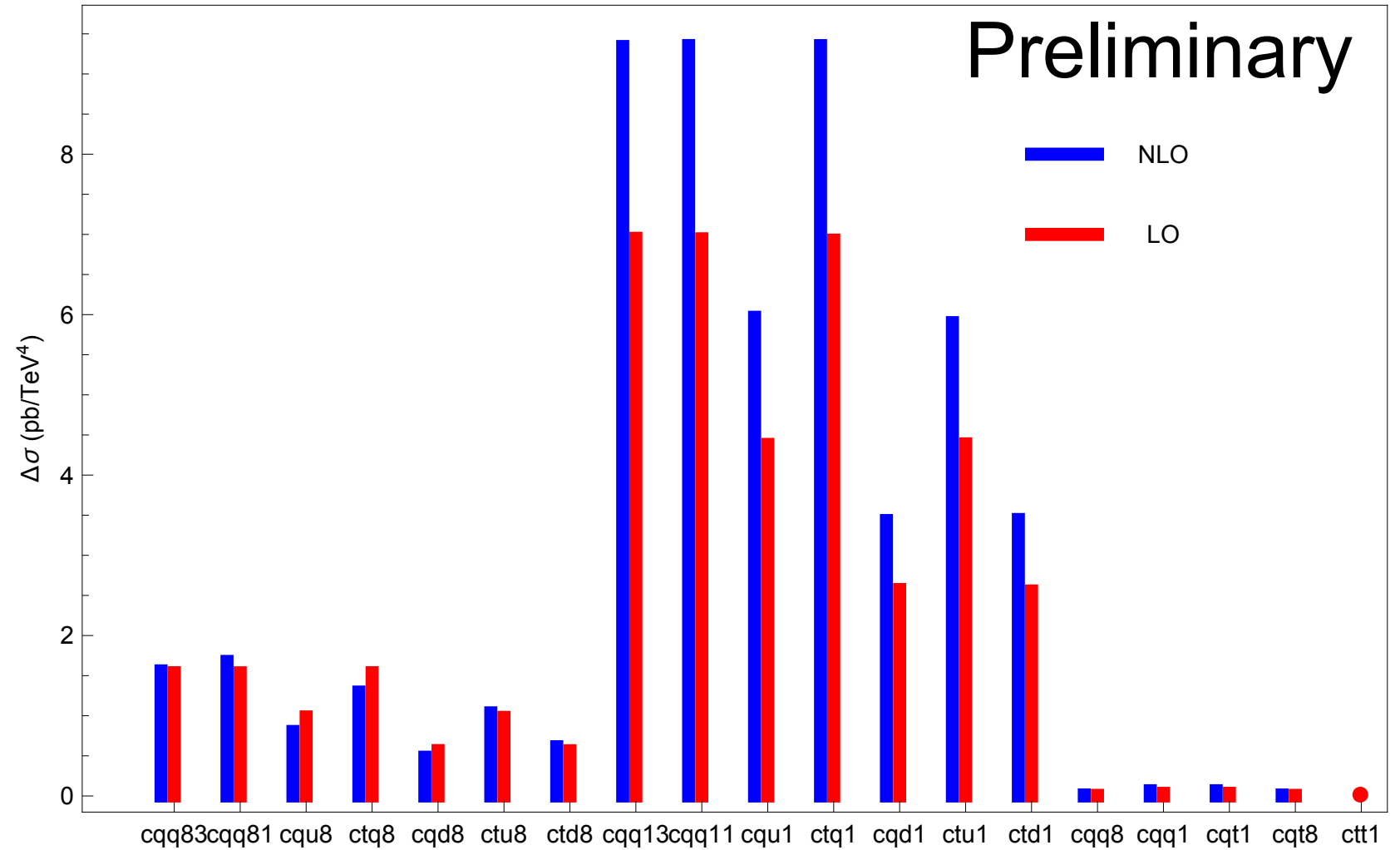
CD et al. (*Phys.Rev.D* 91 (2015) 034024) (FCNC)

- Non-trivial: Chromomagnetic
- $\psi^2\varphi^3$  like SM
- $\psi^2\varphi^2 D$  like SM but
- axial anomaly :  $gg > Z > tt, gg > gz, uu > gz, \dots$  few fb/TeV<sup>4</sup> but larger when not properly taken into account

# 4F

Full UFO for top  
SMEFT being tested

dim6<sup>2</sup>



# 5F

# Outlook

# Outlook

- LHC is entering the precision era
- EFT is multi-channel/observable (even more at one-loop)
- Global fit with a large number of parameters/multiple data
- Interplay between PDF and EFT
- Interplay between EFT and SM parameters

# Outlook

