

29-30 January 2020, Archamps

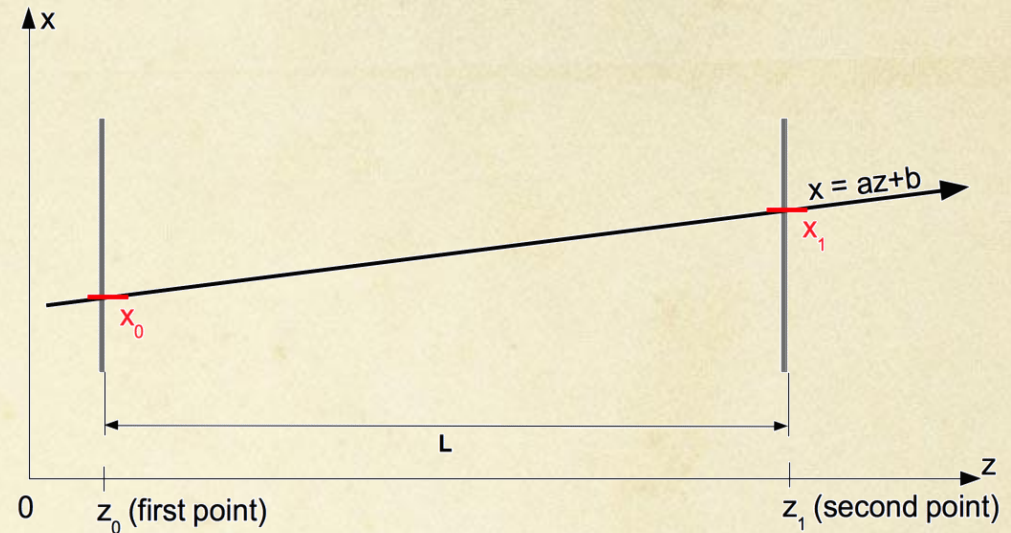


Jérôme Baudot  
([baudot@in2p3.fr](mailto:baudot@in2p3.fr))



### ○ Hypothesis:

- Two sensors
  - perfect positions
  - Infinitely thin
- 1 straight tracks
  - 2 parameters (a,b)



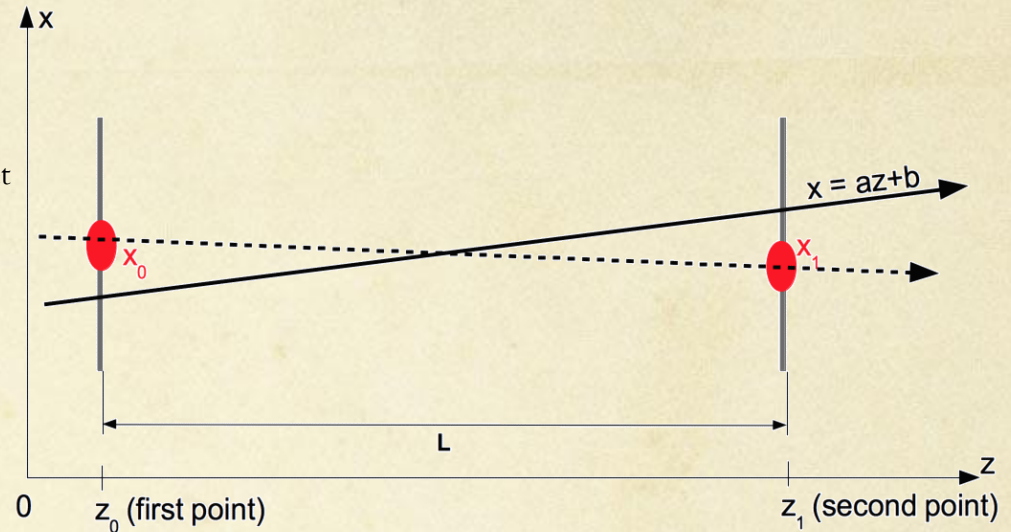
### ○ Estimation of track parameters

- Assuming track model is straight
- No uncertainty !

$$a = \frac{x_1 - x_0}{z_1 - z_0}, \quad b = \frac{x_0 z_1 - x_1 z_0}{z_1 - z_0}$$

### ○ Hypothesis:

- Two sensors
  - Positions with UNCERTAINTY  $\sigma_{\text{det}}$
  - Infinitely thin
- 1 straight tracks
  - 2 parameters (a,b)



### ○ Estimation of track parameters

- Assuming track model is straight
- Uncertainties from error propagation

$$a = \frac{x_1 - x_0}{z_1 - z_0}, \quad b = \frac{x_0 z_1 - x_1 z_0}{z_1 - z_0}$$

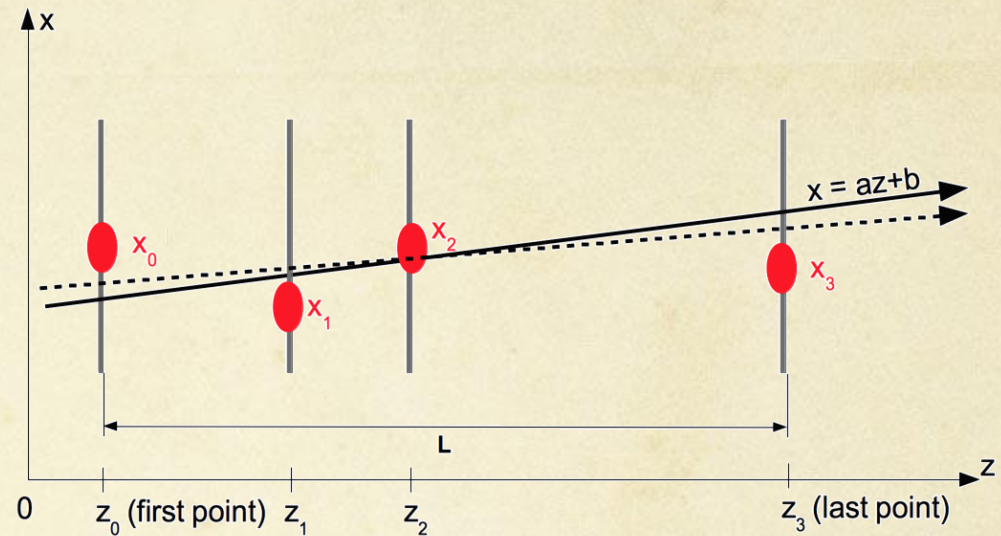
$$S_a = \frac{\sqrt{2}}{z_1 - z_0} S_{\text{det}}, \quad S_b = \frac{\sqrt{z_1^2 + z_0^2}}{z_1 - z_0} S_{\text{det}}$$

$$\text{COV}_{a,b} = -\frac{\sqrt{z_1 + z_0}}{z_1 - z_0} S_{\text{det}}$$



### ○ Hypothesis:

- More than two sensors
  - Positions with uncertainty  $\sigma_{\text{det}}$
  - Infinitely thin
- 1 straight tracks
  - 2 parameters (a,b)



### ○ Estimation of track parameters

- Assuming track model is straight
  - Need **FITTING PROCEDURE** least square
  - Need covariance matrix of measurements (here diagonal)
- Uncertainties from error propagation
  - Detail depends on geometry

➔ Both estimation & uncertainties improve

$$a = \frac{S_1 S_{xz} - S_x S_z}{S_1 S_{z^2} - (S_z)^2}, \quad b = \frac{S_x S_{z^2} - S_z S_{xz}}{S_1 S_{z^2} - (S_z)^2}$$

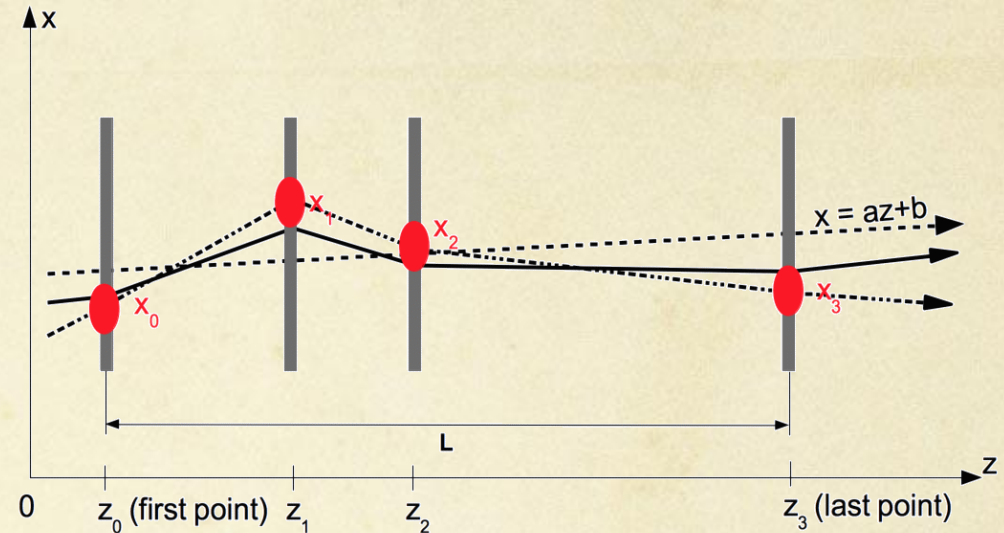
$$S_a^2 = \frac{S_1}{S_1 S_{z^2} - (S_z)^2}, \quad S_b^2 = \frac{S_{z^2}}{S_1 S_{z^2} - (S_z)^2}$$

$$\text{COV}_{a,b} = \frac{-S_z}{S_1 S_{z^2} - (S_z)^2}$$

See LSM on  
straight tracks  
later

### ○ Hypothesis:

- More than two sensors
  - Positions with uncertainty  $\sigma_{\text{det}}$
  - With some THICKNESS  
→ physics effect
- 1 straight tracks
  - 2 parameters (a,b)



### ○ Estimation of track parameters

- Assuming track model is straight
  - Need fitting procedure least square
  - Need covariance matrix of measurements  
physics effect → **NON DIAGONAL** terms
- Uncertainties from error propagation

→ same estimators but increased uncertainties

$$a = \frac{S_1 S_{xz} - S_x S_z}{S_1 S_{z^2} - (S_z)^2}, \quad b = \frac{S_x S_{z^2} - S_z S_{xz}}{S_1 S_{z^2} - (S_z)^2}$$

### Complex covariant matrix expression

- correlation between sensors
- Various implemetations possible



# What are we talking about?

## ○ Hypothesis:

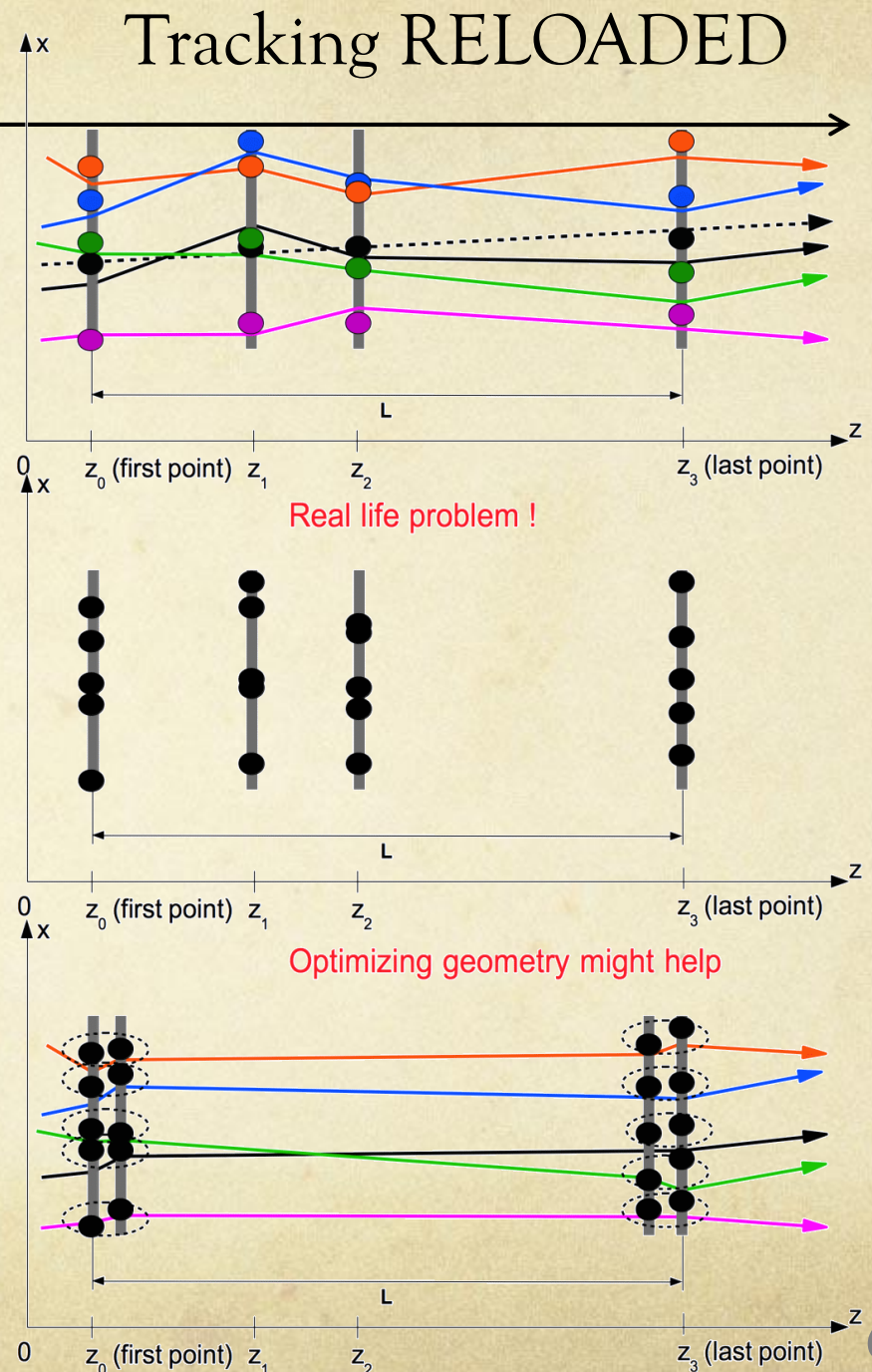
- More than two sensors
  - Positions with uncertainty  $\sigma_{\text{det}}$
  - With some thickness
- MANY straight tracks
  - Still 2 parameters (a,b)...per track!
  - But may change along track path

## ○ New step = FINDING

- Which hits to which tracks ?
- Strongly depends on geometry

## ○ Estimation of track parameters

- Happens after finder
- Uncertainties involve correlation



# Lecture outline

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1. Basic concepts
2. Position sensitive detectors
3. Standard algorithms
4. Advanced algorithms
5. Optimizing a tracking system
6. References

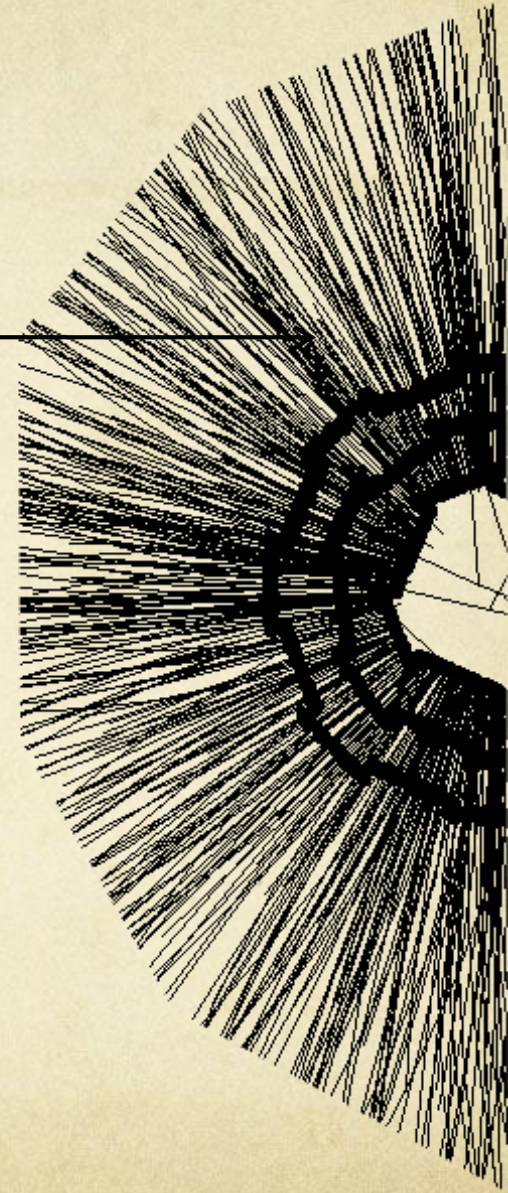
first lecture

second lecture

third lecture



practice

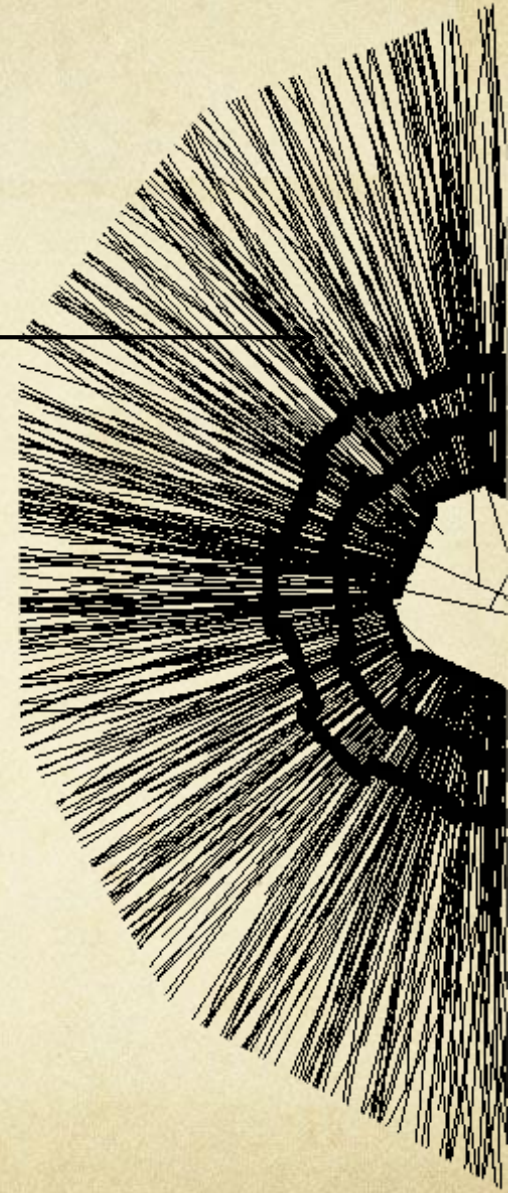




# 1. Motivations & basic concepts

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- Motivations
- Types of measurements
- The 2 main tasks
- Environmental considerations
- Figures of merit





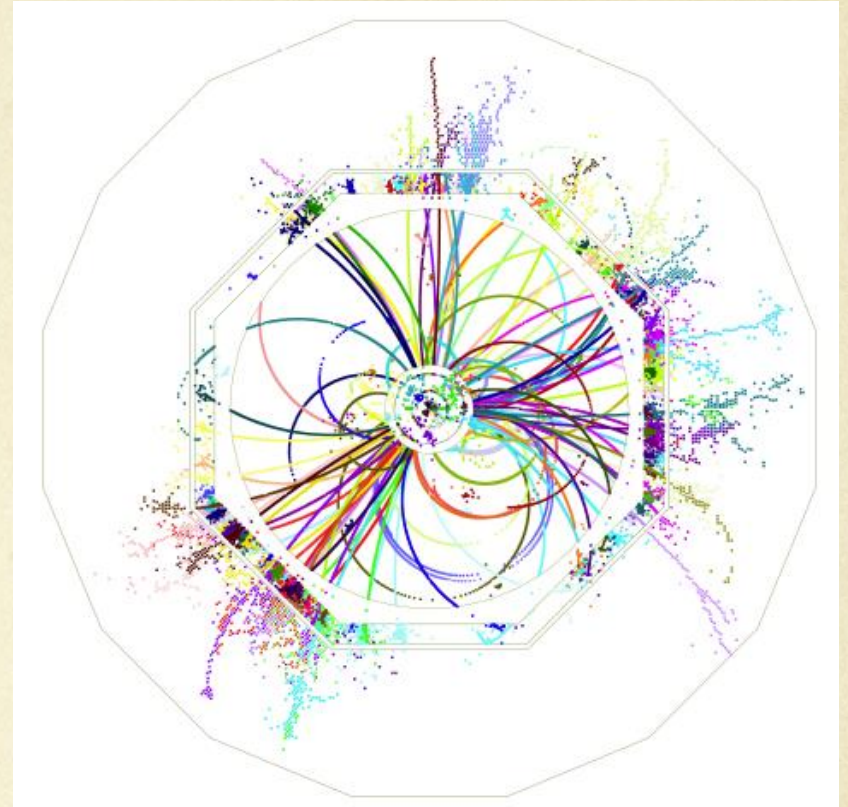


### ○ Understanding an event

- Individualize tracks  $\simeq$  particles
- Measure their properties
- LHC:  $\sim 1000$  particles per 25 ns “event”

### ○ Track properties

- **Momentum**  $\Leftrightarrow$  curvature in B field
  - Reconstruct invariant masses
  - Contribute to jet energy estimation
- **Energy**  $\Leftrightarrow$  range measurement
  - Limited to low penetrating particle
- **Mass**  $\Leftrightarrow$  dE/dx measurement
- **Origin**  $\Leftrightarrow$  vertexing (connecting track)
  - Identify decays
  - Measure flight distance
- **Extension**  $\Leftrightarrow$  particle flow algorithm (pfa)
  - Association with calorimetric shower



8 jets event ( $t\bar{t}h$ ) @ 1 TeV ILC

# 1. Motivations & Basic Concepts

## Momentum measurement

### ○ Magnetic field curves trajectories

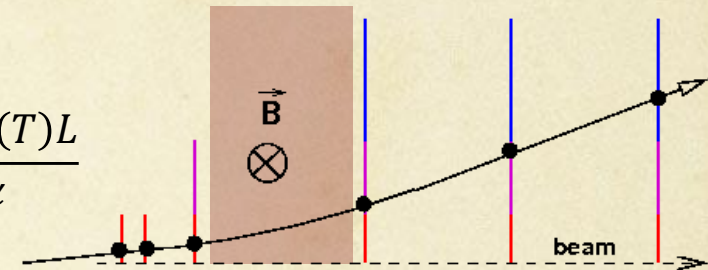
$$\frac{d\vec{p}}{dt} = q\vec{v} \times \vec{B}$$

- In B=4T a 10 GeV/c particle will get a sagitta of 1.5 cm @ 1m

### ○ Fixed-target experiments

- Dipole magnet on a restricted path segment
- Measurement of deflection (angle variation)

$$\frac{p_T}{q} = \frac{0.3 \cdot B(T)L}{\Delta\alpha}$$



### ○ Collider experiment

- Barrel-type with axial B over the whole path
- Measurement of curvature (sagitta)

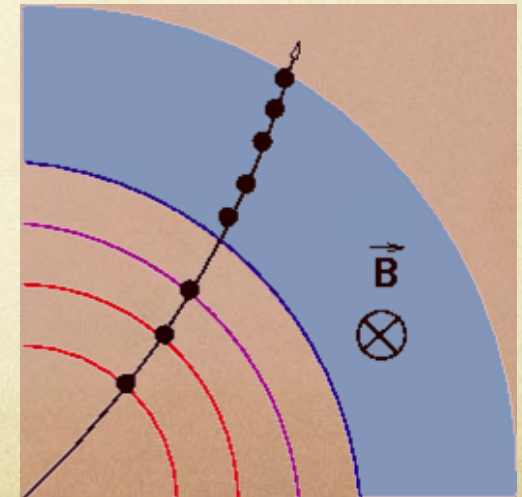
$$\frac{p_T(\text{GeV}/c)}{q} = 0.3 \times B(T) \times R(m)$$

### ○ Other arrangements

- Toroidal B... not covered

### ○ Two consequences

- Position sensitive detectors needed
- Perturbation effects on trajectories limit precision on track parameters





### ○ Identifying through topology

#### → Short-lived weakly decaying particles

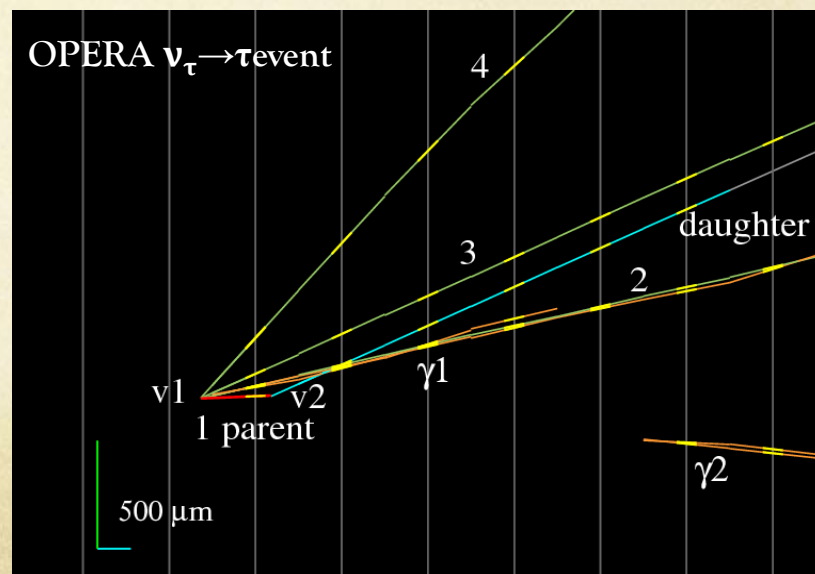
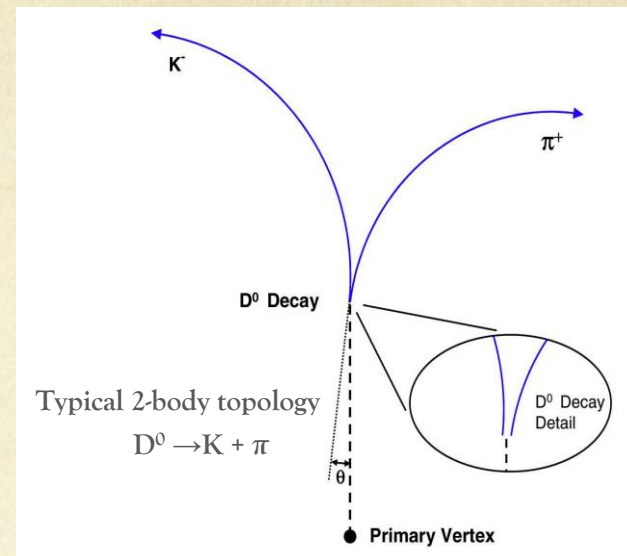
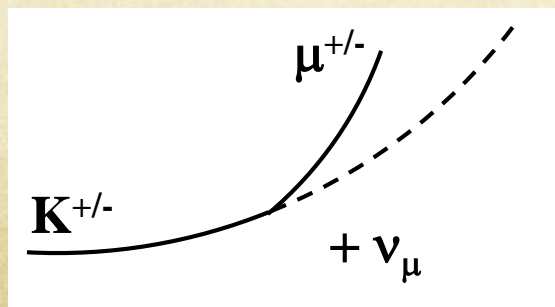
- Charm  $c\tau \sim 120 \mu\text{m}$
- Beauty  $c\tau \sim 470 \mu\text{m}$
- $\tau$ , strange ( $K_S, \Lambda$ )/charmed (D)/beauty (B) particles

### ○ Exclusive reconstruction

- Decay topology with secondary vertex
- Exclusive = all particles in decay associated

### ○ Inclusive “kink” reconstruction

- Some particles are invisible ( $\nu$ )

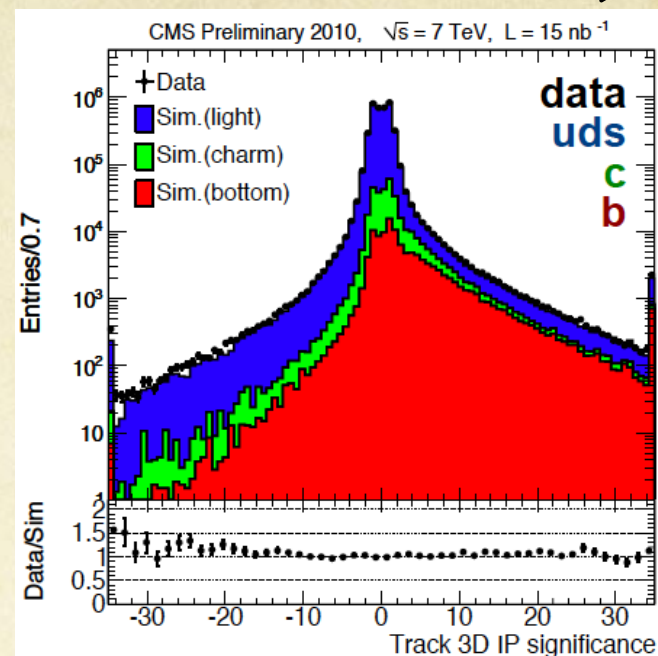


### ○ Inclusive reconstruction

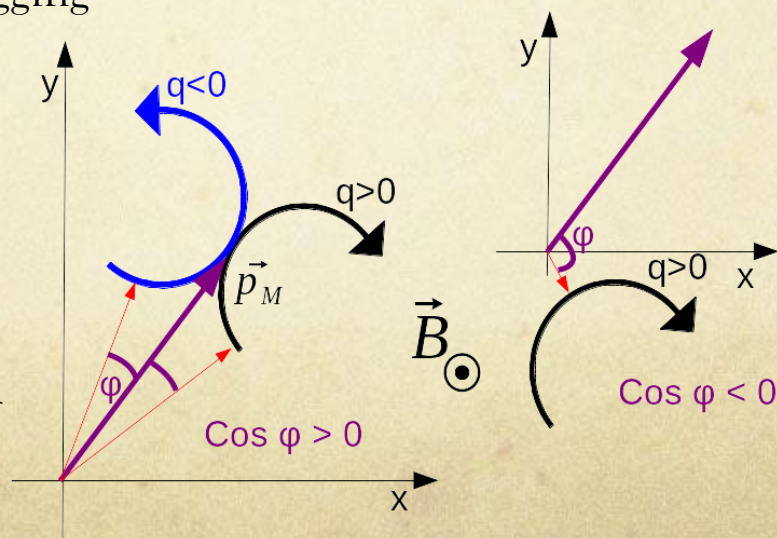
- Selecting parts of the daughter particles  
= flavor tagging for high energy colliders
- based on impact parameter (IP)
- $\sigma_{IP} \sim 20\text{-}100 \mu\text{m}$  requested

### ○ Definition of impact parameter (IP)

- Also **DCA = distance of closest approach**  
from the trajectory to the primary vertex
- Full 3D or 2D (transverse plane  $d_p$ ) + 1D (beam axis  $z$ )
- Sign extremely useful for flavor-tagging



Sign defined by  
angle dca / jet momentum

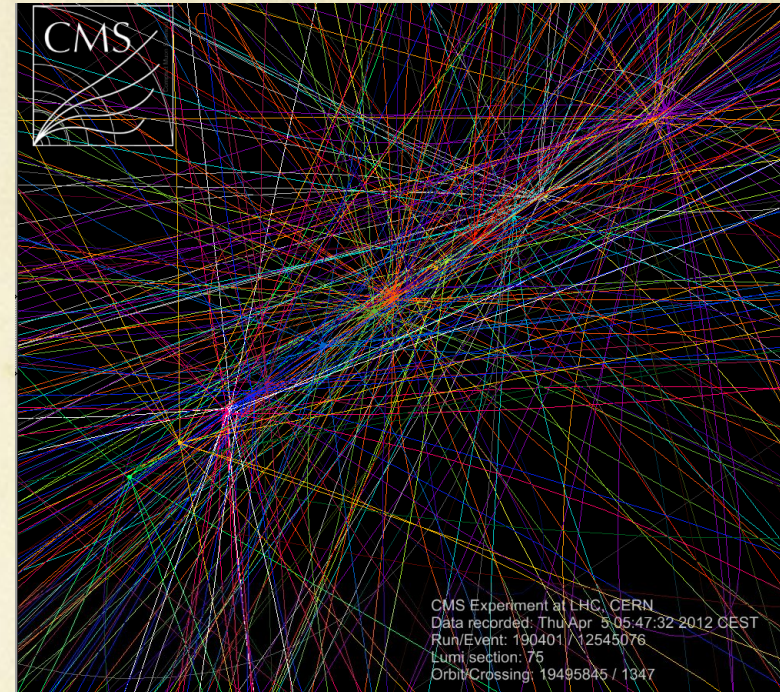






### ○ Finding the event origin

- Where did the collision did occur?
  - = Primary vertex
- (life)Time dependent measurements
  - CP-asymmetries @ B factories ( $\Delta z \simeq 60\text{-}120\text{ }\mu\text{m}$ )
- Case of multiple collisions / event
  - $\gg 10$  (100) vertex @ LHC (HL-LHC)



### ○ Remarks for collider

- Usually no measurement below 1-2 cm / primary vertex
  - Due to beam-pipe maintaining vacuum
- Requires **extrapolation** → expect “unreducible” uncertainties



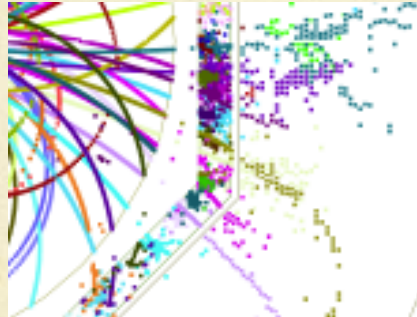


### ○ Usually not a tracker task

- CALORIMETERs (see dedicated lecture)
- Indeed calorimeters gather material to stop particles while trackers try to avoid material (multiple scattering)
- however...calorimetry tries to improve granularity  $\Rightarrow$  track-cal are “trendy”

### ○ Particle flow algorithm

- Colliders (pp and ee)



### ○ Energy evaluation by counting particles

- Clearly heretic for calorimetry experts
- Requires to separate  $E_{\text{deposit}}$  in dense environment

### ○ Range measurement for low energy particles

- Stack of tracking layers
- Modern version of nuclear emulsion

**NOT COVERED**



### ○ Reminder on the physics (see other courses)

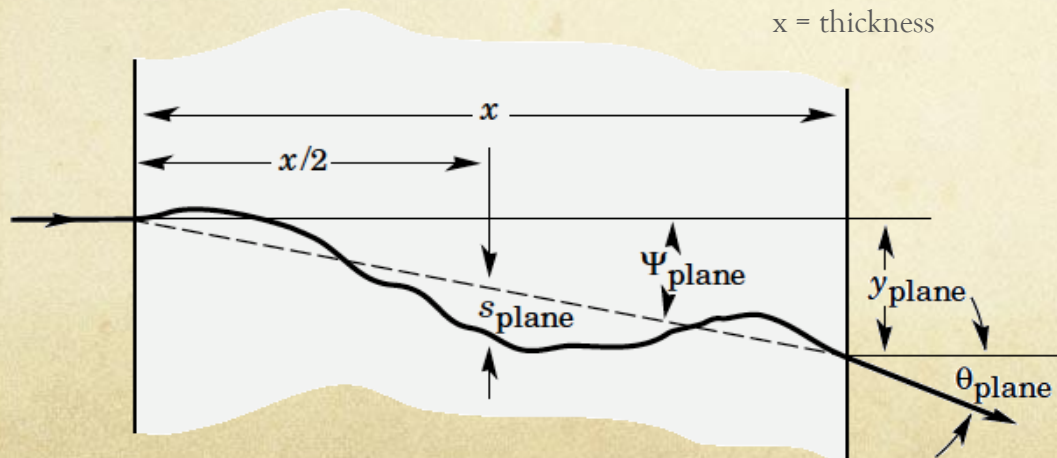
- Coulomb scattering mostly on nuclei
- Molière theory description as a **centered** gaussian process
  - the thinner the material, the less true → large tails

### ○ In-plane description (defined by vectors $\mathbf{p}_{in}$ , $\mathbf{p}_{out}$ )

- Corresponds to  $(\varphi, \theta = \theta_{plane})$  with  $\mathbf{p}_{in} = \mathbf{p}_z$  and  $p_{out}^2 = p_{out,z}^2 + p_{out,T}^2$ 

$$\begin{cases} p_{out} \cos \theta \approx p_{out,z} \\ p_{out,T} = p_{out} \sin \theta \approx p_{out} \theta \end{cases}$$

Highland formula: 
$$S_q = \frac{13.6 \text{ (MeV/c)}}{bp} \cdot z \cdot \sqrt{\frac{\text{thickness}}{X_0}} \cdot \left[ 1 + 0.038 \ln\left(\frac{\text{thickness}}{X_0}\right) \right]$$
(note:  $f \hat{=} [0, 2\rho]$  uniform)  
 $z$  = particle charge)



$X_0$  = radiation length

Same definition as in calorimetry  
 ... though this is accidental

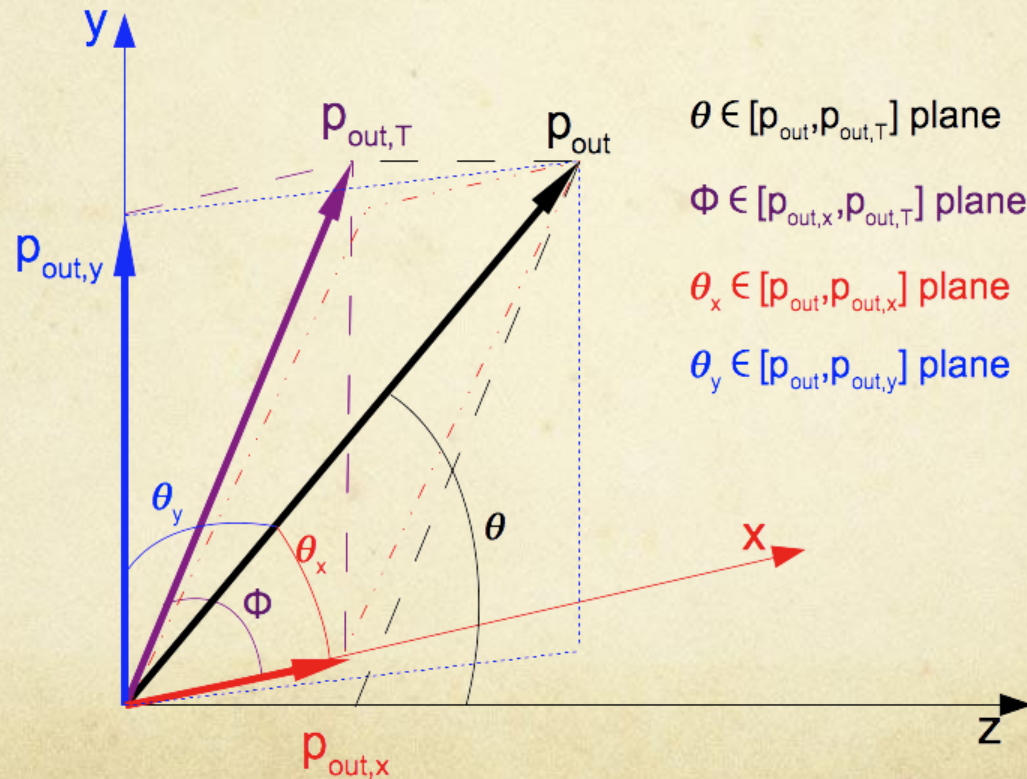
### ○ In-space description (defined by fixed x/y axes)

→ Corresponds to  $(\theta_x, \theta_y)$  with

$$p_{out,T}^2 = p_{out,x}^2 + p_{out,y}^2 \quad \begin{cases} p_{out} \sin \theta_x \approx p_{out} \theta_x \\ p_{out} \sin \theta_y \approx p_{out} \theta_y \end{cases} \quad \theta_{plane}^2 = \theta_x^2 + \theta_y^2$$

→  $\theta_x$  and  $\theta_y$  are independent gaussian processes

$$\sigma_{\theta_x} = \sigma_{\theta_y} = \frac{\sigma_{\theta_{plane}}}{\sqrt{2}}$$





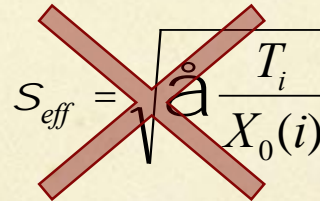
### ○ Important remark when combining materials

→ Total thickness  $T = \sum T_i$ , each material (i) with  $X_0(i)$

→ Definition of effective radiation length →  $X_{0,eff} = \frac{\sum T_i \cdot X_0(i)}{T}$

→ Consider **single gaussian** process  $s_{eff} \propto \sqrt{\frac{T}{X_{0,eff}}}$

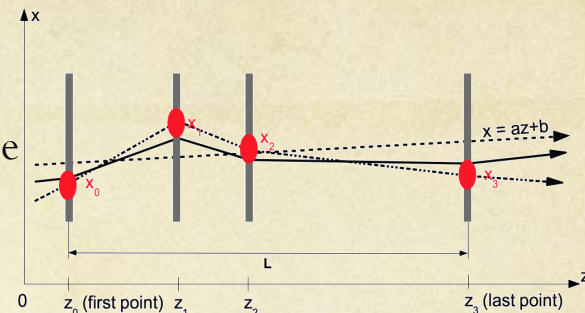
and never do variance addition  
(which minimize deviation)


$$s_{eff} = \sqrt{\sum \frac{T_i}{X_0(i)}}$$

### ○ Impact on tracking algorithm

- The track **parameters evolves** along the track !
- May drive choice of reconstruction method

Remember this simple case



### ○ Photon conversion

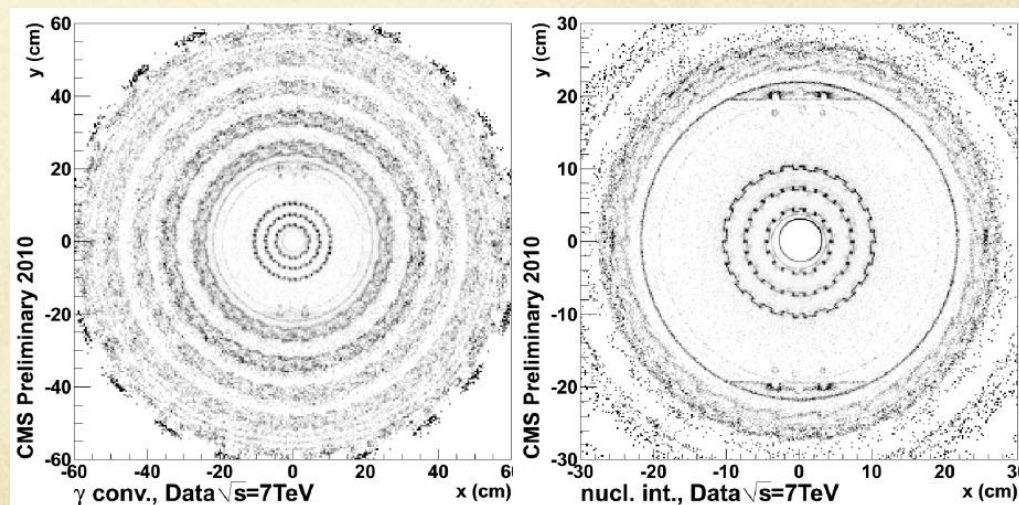
- Alternative definition of radiation length  
probability for a high-energy photon to generate a pair over a path  $dx$ :

$$\text{Prob} = \frac{dx}{\frac{9}{7} X_0}$$

- $\gamma \rightarrow e^+e^-$  = conversion vertex

- Generate troubles :

- Additional unwanted tracks
- Decrease statistics for electromagnetic calorimeter



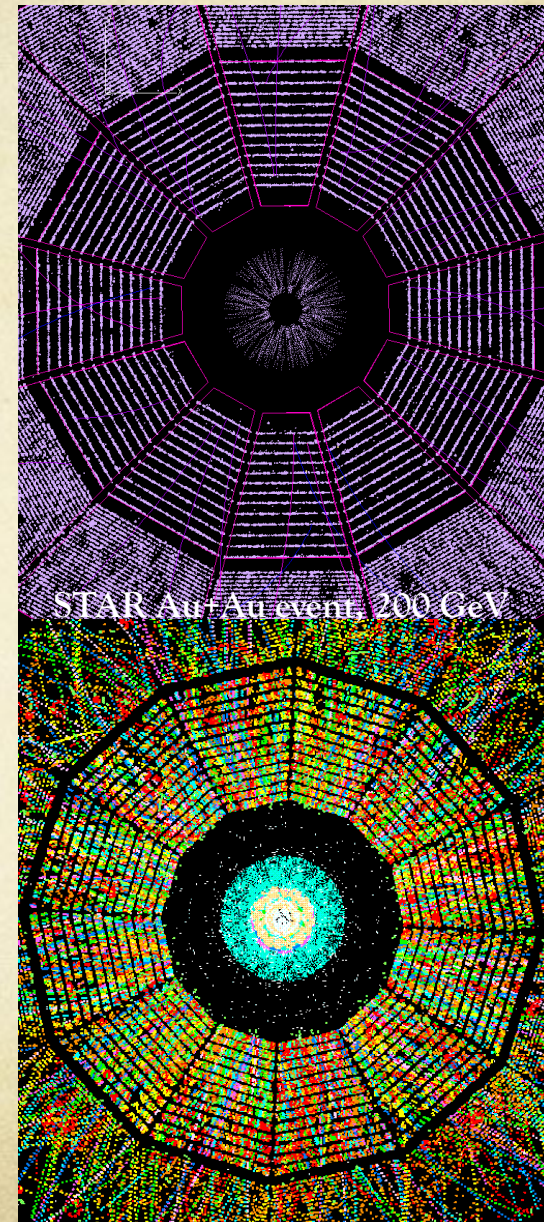
CMS “picture” of material budget  
through photon conversion vertices  
(silicon tracker only)





### The collider paradigm

- Basic inputs from detectors
  - Succession of 2D or 3D points (or track segments)
    - Who's who ?
- 2 steps process
  - Step 1: track identification = **finding** = pattern recognition
    - Associating a set of points to a track
  - Step 2: track **fitting**
    - Estimating trajectory parameters → momentum
- Both steps require
  - **Track model** (signal, background)
  - Knowledge of **measurement uncertainties**
  - Knowledge of **materials traversed** (Eloss, mult. scattering)
- Vertexing needs same 2 steps
  - Identifying tracks belonging to same vertex
  - Estimating vertex properties (position + 4-vector)







### The Telescope mode

#### ○ Beam test

- Single particle at a time
  - Sole nuisances = noise and material budget
- Trigger from beam
  - Often synchronous
- Goal = get the particle incoming direction



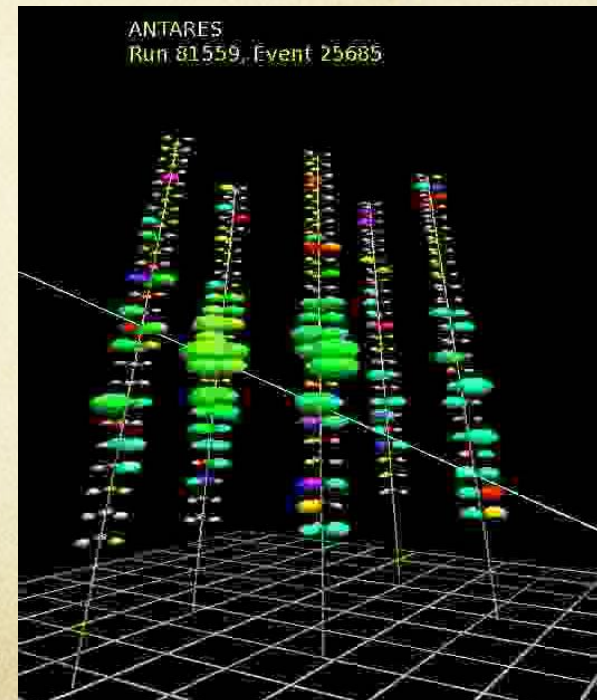
EUDET beam telescope

#### ○ The astroparticle way

- Similar to telescope mode
- No synchronous timing
- Ex: deep-water  $\nu$  telescopes

=> For 2 last cases: mostly a fitting problem

- Usually with straight track model







### ○ Life in a real experiment is tough (*for detectors of course, students are welcome!*)

- Chasing small cross-sections → large luminosity and/or energy
  - Short interval between beam crossing (LHC: 25 ns)
  - Pile-up of events (HL-LHC >100 collisions / crossing)
  - **Large amount of particles** (could be >  $10^8$  part/cm<sup>2</sup>/s)
    - background, radiation
  - Vacuum could be required (space, very low momentum particles (CBM, LHCb))
- } → Finding more complicated!  
→ Requirements on detectors:  
• Fast timing  
• High granularity

### ○ Radiation tolerance

- Two types of energy loss
  - **Ionizing** (generate charges): dose in Gy = 100 Rad
  - **Non-ionizing** (generate defects in solid): fluence in  $n_{eq}(1\text{MeV})/\text{cm}^2$
- The innermost the detection layer, the harder the radiation (radius<sup>2</sup> effect)
- Examples for most inner layers:
  - LHC:  $10^{15}$  to  $<10^{17}$   $n_{eq}(1\text{MeV})/\text{cm}^2$  with 50 to 1 MGy
  - ILC:  $<10^{12}$   $n_{eq}(1\text{MeV})/\text{cm}^2$  with 5 kGy

### ○ Timing consideration

- **Integration time** drives occupancy level (important for finding algorithm)
- **Time resolution** offers time-stamping of tracks
  - Tracks in one “acquisition event” could be associated to their proper collision event if several have piled-up
- Key question = triggered or not-triggered experiment?

### ○ Heat concerns

- Spatial resolution → segmentation → many channels  
Readout speed → power dissipation/channel
  - Efficient cooling techniques exist BUT  
add material budget and may not work everywhere (space)
- } Hot cocktail!

### ○ Summary

- Tracker technology driven by environmental conditions: hadron colliders (LHC)
- Tracker technology driven by physics performances: lepton colliders (B factories, ILC), heavy-ion colliders (RHIC, LHC)
- Of course, some intermediate cases: superB factories, CLIC



# 1. Motivations & Basic Concepts:

## Figures of Merit

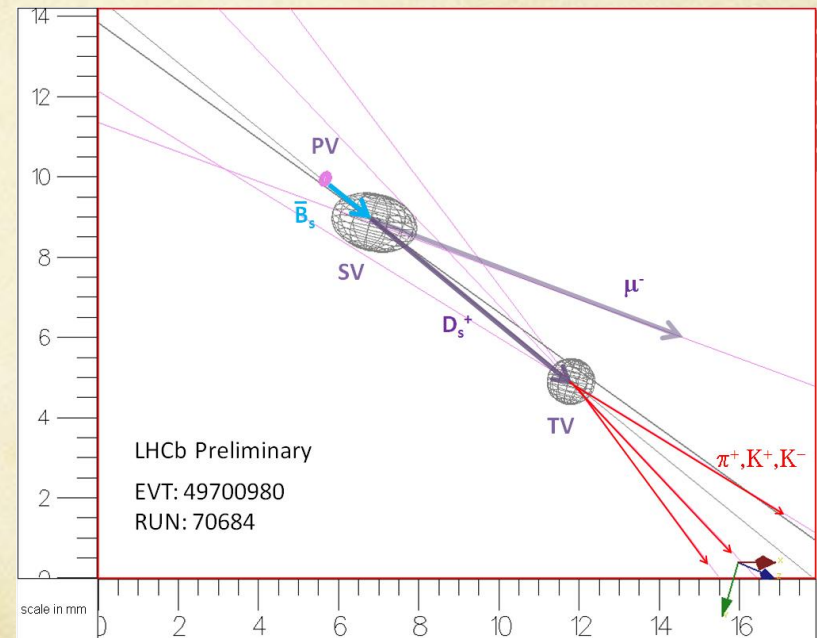
### ○ For detection layer

- **Detection efficiency**
  - Mostly driven by Signal/Noise
  - Note: Noise = signal fluctuation  $\oplus$  readout (electronic) noise
- **Intrinsic spatial resolution**
  - Driven by segmentation (not only)
  - Useful tracking domain  $\sigma < 1\text{mm}$
- Linearity and resolution on  $dE/dx$  for PID
- **Material budget**

### ○ For detection systems (multi-layers)

- **Track finding efficiency & purity**
- **Two-track resolution**
  - Ability to distinguish two nearby trajectories
  - Mostly governed by signal spread / segments
- **Momentum resolution**
- **Impact parameter resolution**
  - Sometimes called “distance of closest approach” to a vertex

- **“Speed”** (time resolution, hit rate)
- **Radiation tolerance**



# 1. Motivations & Basic Concepts:

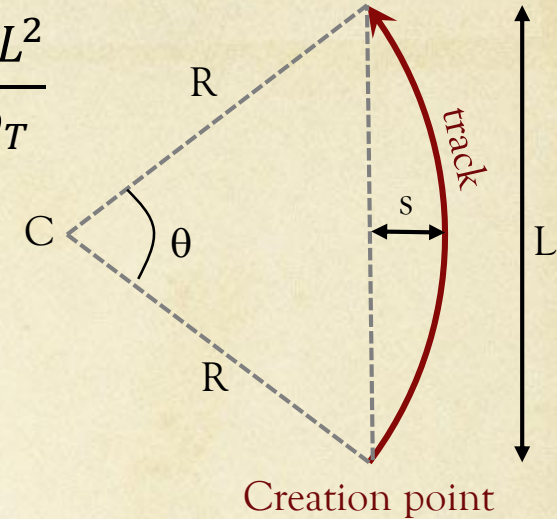
## Figures of Merit: initial estimates

### ○ Momentum resolution

- Based on sagitta ( $s$ ) measurement in collider geometry
- $L$  = lever arm of measurements
- $R$  = curvature radius  $p_T/0.3B \gg L$

$$s \approx \frac{L^2}{8R} = 0.038 \frac{BL^2}{p_T}$$

$$\frac{\sigma_{p_T}}{p_T} = \frac{\sigma_s}{s}$$



### ○ Impact parameter resolution

- Based on two layers measurements
- assume track straight over small distance:  $R_{\text{ext}} \ll \text{curvature}$
- Each layer with spatial resolution:  $\sigma_{\text{int}}, \sigma_{\text{ext}}$
- Material budget  $\rightarrow \sigma_\theta$
- Telescope equation:

$$\sigma_{IP} \propto \frac{\sqrt{R_{\text{ext}}^2 \sigma_{\text{int}}^2 + R_{\text{int}}^2 \sigma_{\text{ext}}^2}}{R_{\text{ext}} - R_{\text{int}}} \oplus \frac{R_{\text{int}} \sigma_{\vartheta(\text{ms})}}{p \sin^{3/2}(\theta)}$$

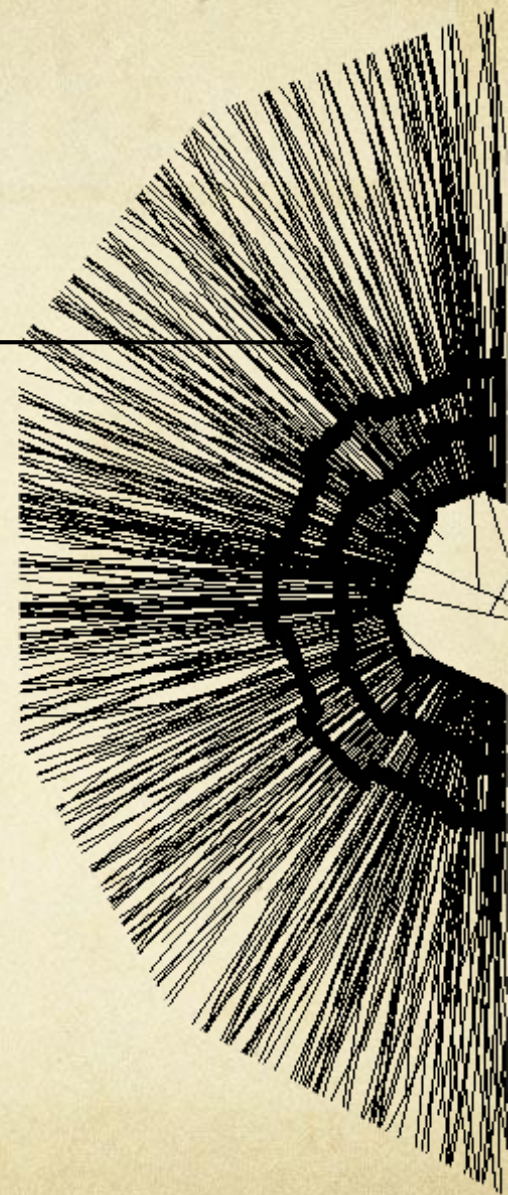




## 2. Detection technologies

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- Spatial resolution
- Single layer systems
  - Silicon & gas sensors, scintillators
- Multi-layer systems
  - Drift chambers and Time projection chambers
- Tentative simplistic comparison
- Magnets
- Practical considerations
- Leftovers



## 2. Detector Technologies:

## Spatial resolution

### ○ Position measurement comes from segmentation

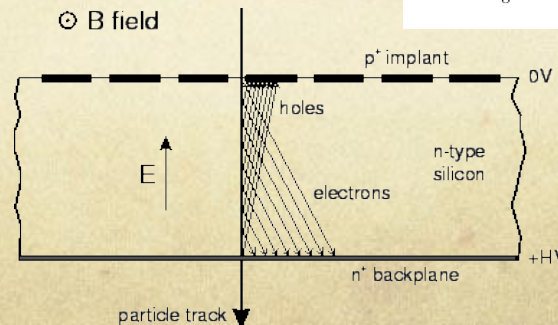
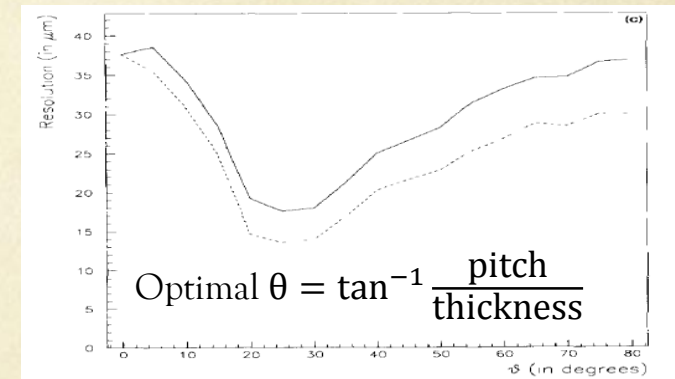
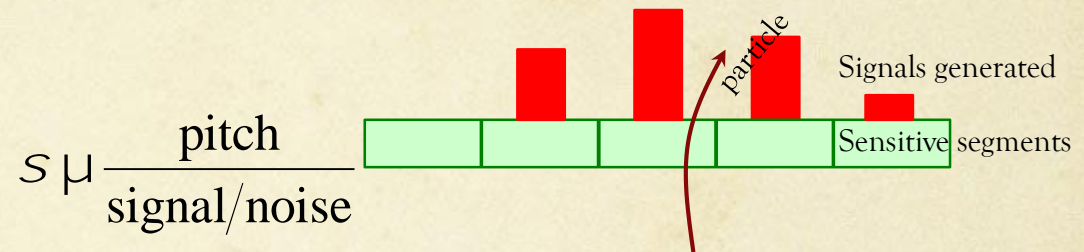
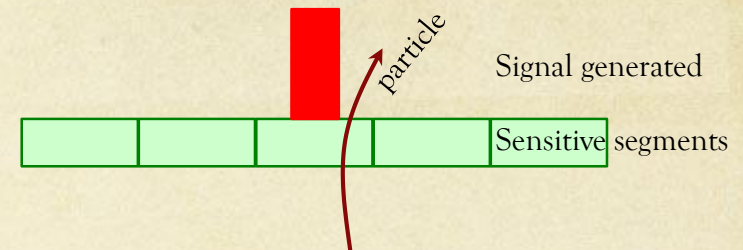
- Pitch

### ○ Digital resolution

$$S = \frac{\text{pitch}}{\sqrt{12}}$$

### ○ Improvement from signal sharing

- Position = charge center of gravity
- Effects generated by
  - Secondary charges spread inside volume
  - Inclined tracks (however, resol. limited at large angles)
- Potential optimization of segmentation / sharing
  - Work like signal sampling theory (Fourier transform)
- Warnings:
  - Lorentz force from B mimic the effect
  - counterproductive / 2-track resolution

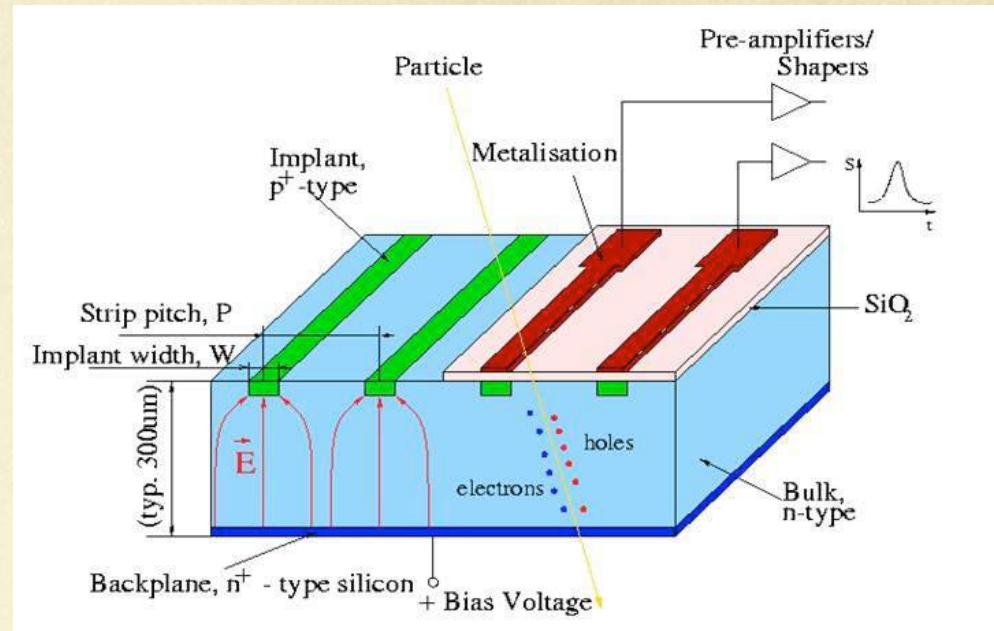




### ○ Signal generation

- e-h pairs are generated by ionization in silicon
  - Average energy needed / e-h pair = 3.6 eV
  - 300  $\mu\text{m}$  thick Si generates  $\sim 22000$  charges for MIP  
BUT beware of Landau fluctuation
- Collection: P-N junction = diode
  - **Full depletion** (10 to 0.5 kV) generates a drift field ( $10^4$  V/cm)
  - Collection time  $\sim 15$  ps/ $\mu\text{m}$

$$\text{depth}_{\text{depleted}} \propto \sqrt{\text{resistivity} \times V_{\text{bias}}}$$



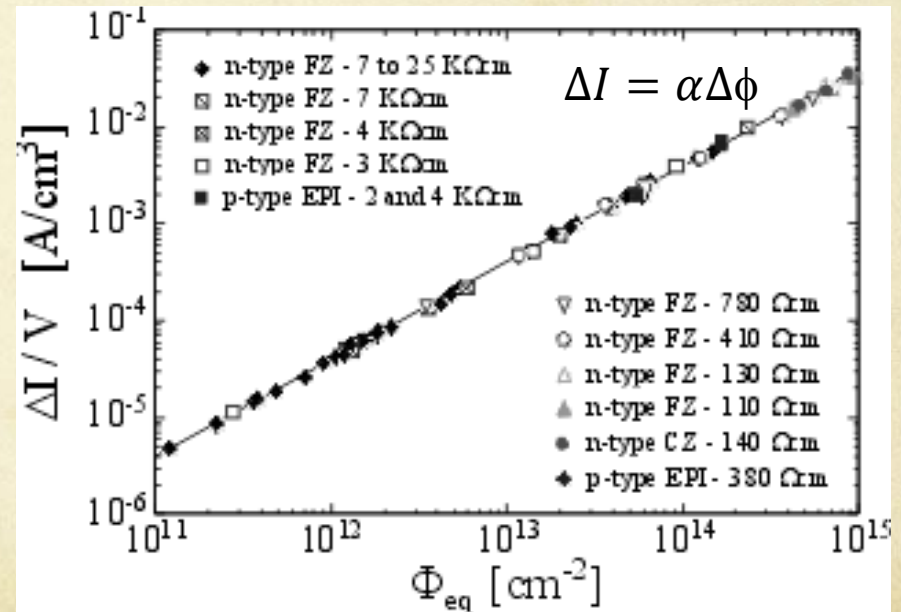
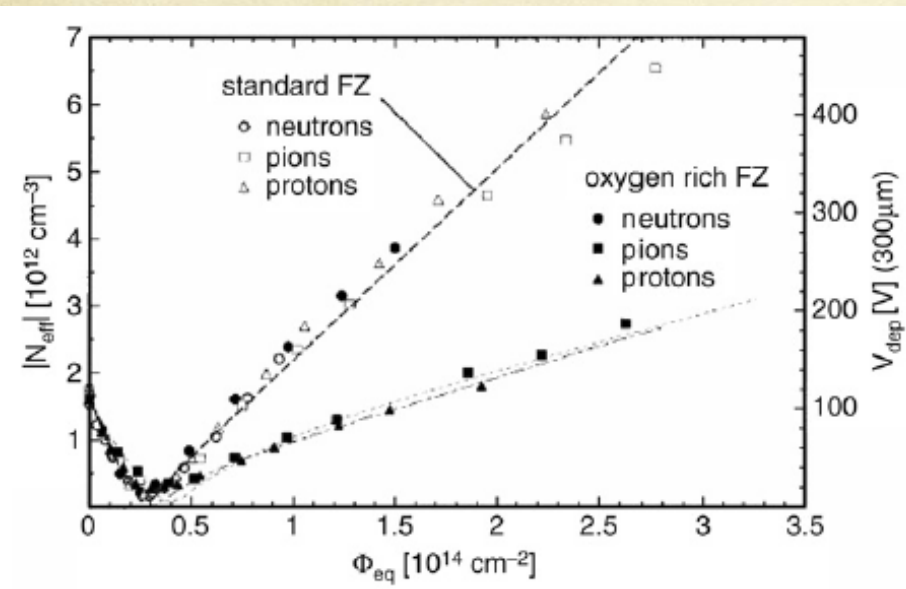


### ○ Non-ionizing energy loss

- Damage crystal network
  - Generates higher leakage current (noise)
  - Generates charge traps (lower signal)
- Modifies doping

### ○ Cumulated ionizing dose

- Parasitic charges trapped at interface with oxides
  - Released randomly  $\Rightarrow$  Noise !



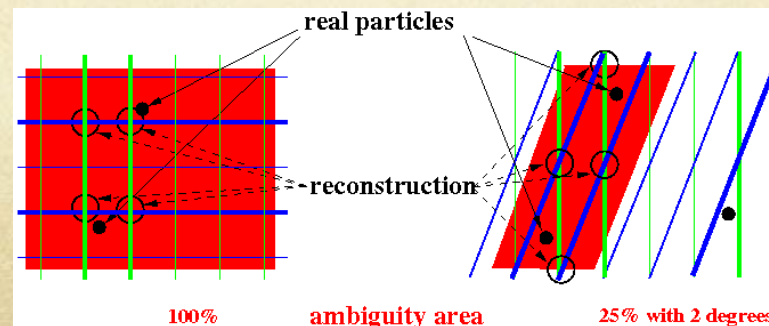
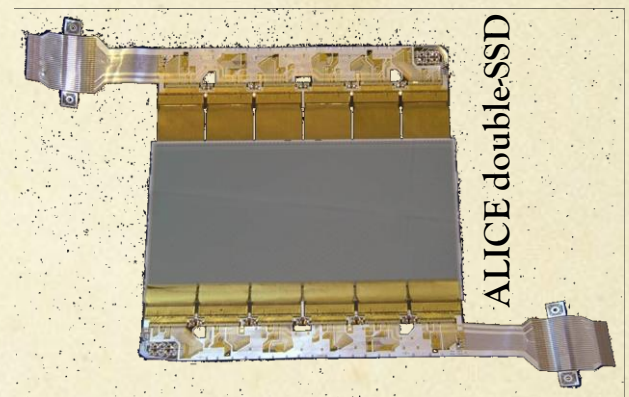
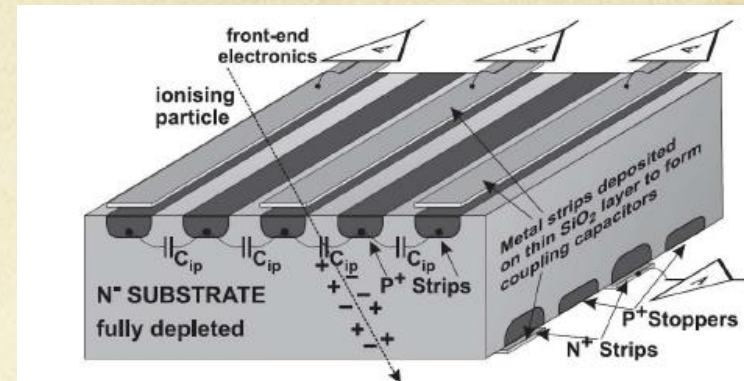


### ○ Concept

- Pattern P-N junction as collection electrodes
- Exploit silicon industry lithographic technique

### ○ Silicon strip detectors

- Sensors “easily” manufactured with pitch down to  $\sim 25 \mu\text{m}$
- 1D if single sided
- Pseudo-2D if double-sided
  - Stereo-angle useful against ambiguities
- Difficult to go below  $100 \mu\text{m}$  thickness (low SNR)
- Speed and radiation hardness: LHC-grade

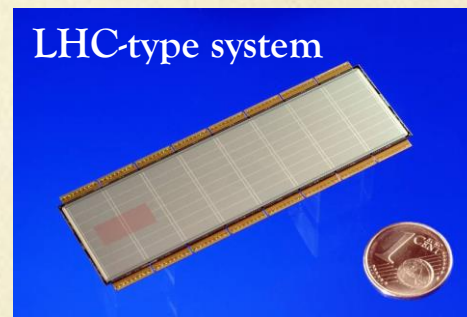
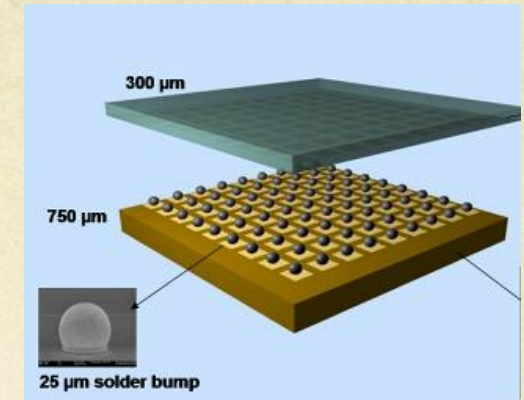
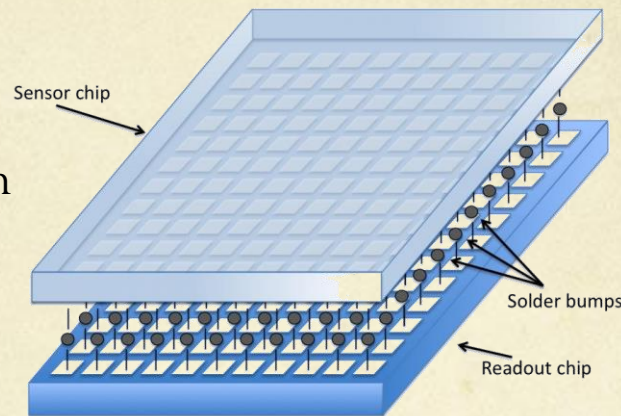


### ○ Concept

- Strips → pixels on sensor
- One to one connection from electronic channels to pixels

### ○ Performances

- Real 2D detector  
& keep performances of strips
  - Can cope with LHC rate (speed & radiation)
- Pitch size limited by physical connection and #transistors for treatment
  - minimal (today):  $50 \times 50 \mu\text{m}^2$
  - typical:  $100 \times 150 / 400 \mu\text{m}^2$
  - spatial resolution about  $10 \mu\text{m}$
- Material budget
  - Minimal(today):  $100(\text{sensor}) + 100(\text{elec.}) \mu\text{m}$
- Power budget:  $10 \mu\text{W}/\text{pixel}$

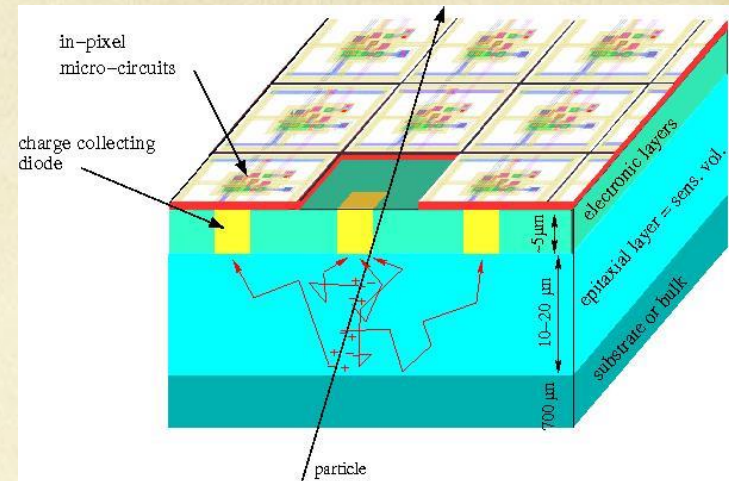


Currently the only technology surviving LHC innermost layers environment



### ○ Concept

- Use industrial CMOS process
  - Implement an array of sensing diode
  - Amplify the signal with transistors near the diode
- Benefit to
  - granularity: pixel pitch down to  $\sim 10 \mu\text{m}$
  - material: sensitive layer thickness as low as  $10\text{-}20 \mu\text{m}$
- Known as Monolithic Active Pixel Sensors (MAPS)



### ○ Sensitive layer

- If undepleted & thin ( $10\text{-}20 \mu\text{m}$ )
  - Slow (100 ns) thermal drift of charges
  - non-ionizing rad. tolerance  $\lesssim 10^{13} n_{\text{eq}(1\text{MeV})}/\text{cm}^2$
- If fully depleted (from 10 to  $100 \mu\text{m}$ )
  - Fast (few ns) field-driven drift of charges
  - non-ionizing rad. tolerance  $> 10^{15} n_{\text{eq}(1\text{MeV})}/\text{cm}^2$

## 2. Detector Technologies:

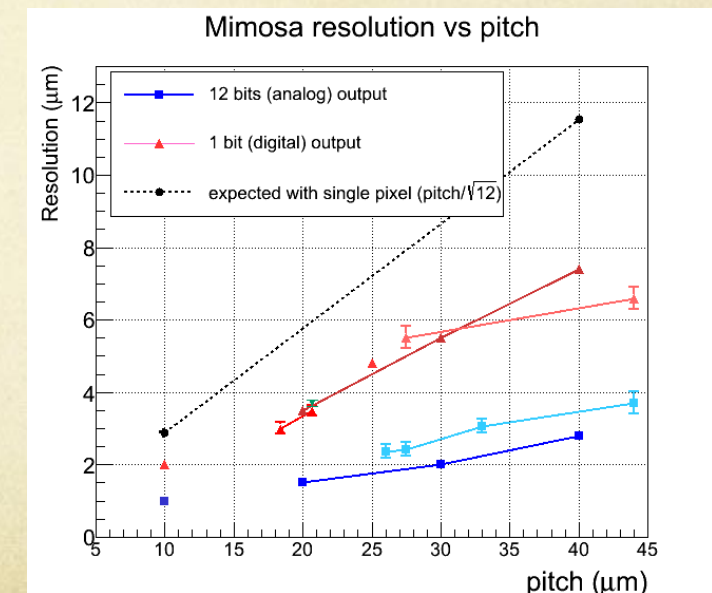
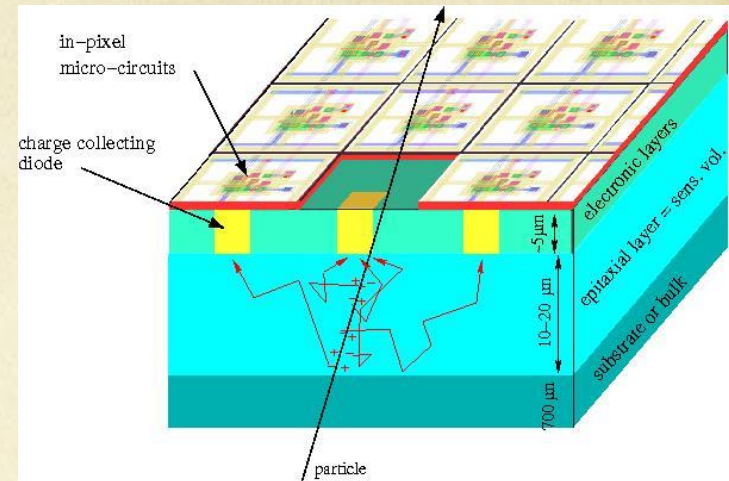
# CMOS Pixel Sensor

### ○ Concept

- Use industrial CMOS process
  - Implement an array of sensing diode
  - Amplify the signal with transistors near the diode
- Gain in granularity: pitch down to  $\sim 10 \mu\text{m}$
- Gain in sensitive layer thickness  $\sim 10\text{-}20 \mu\text{m}$
- For undepleted thin sensitive layer
  - Slow (100 ns) thermal drift of charges
  - non-ionizing rad. tolerance  $\lesssim 10^{13} n_{\text{eq}(1\text{MeV})}/\text{cm}^2$
- For fully depleted thin to thick sensitive layer
  - Fast (few ns) field-driven drift of charges
  - non-ionizing rad. tolerance  $> 10^{15} n_{\text{eq}(1\text{MeV})}/\text{cm}^2$

### ○ Performances

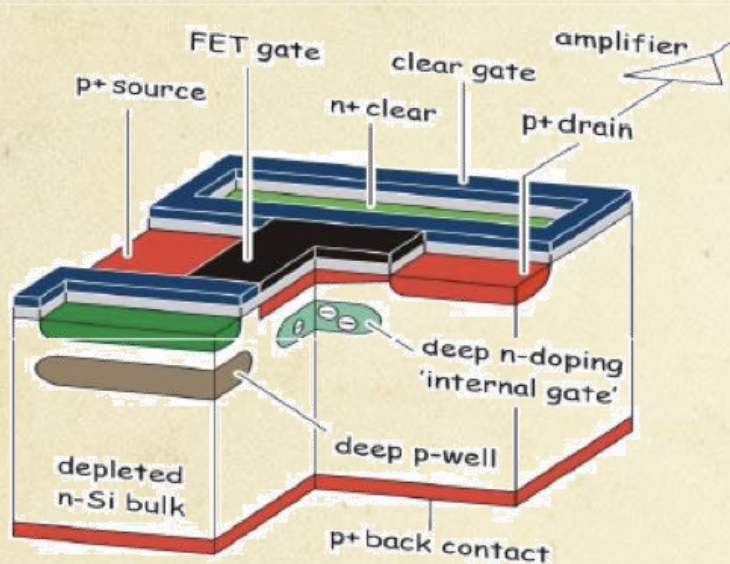
- Spatial resolution 1-10  $\mu\text{m}$  (in 2 dimensions)
- Material budget:  $\lesssim 50 \mu\text{m}$
- Power budget:  $< \mu\text{W}/\text{pixel}$
- Integration time  $\approx 5\text{-}100 \mu\text{s}$  demonstrated
  - $\sim 1 \mu\text{s}$  in development
- Timestamping @ ns level in development





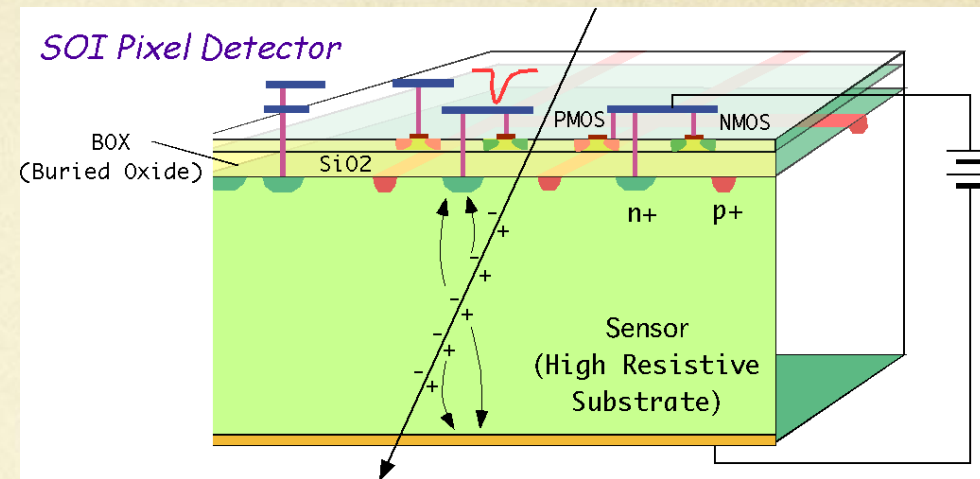
### ○ DEPFET

- Depleted p-channel FET



- Fully depleted sensitive layer
- Large amplification
- Still require some read-out circuits
  - Not fully monolithic
  - Possibly limited in read-out speed

### ○ Silicon On Insulator (SOI)

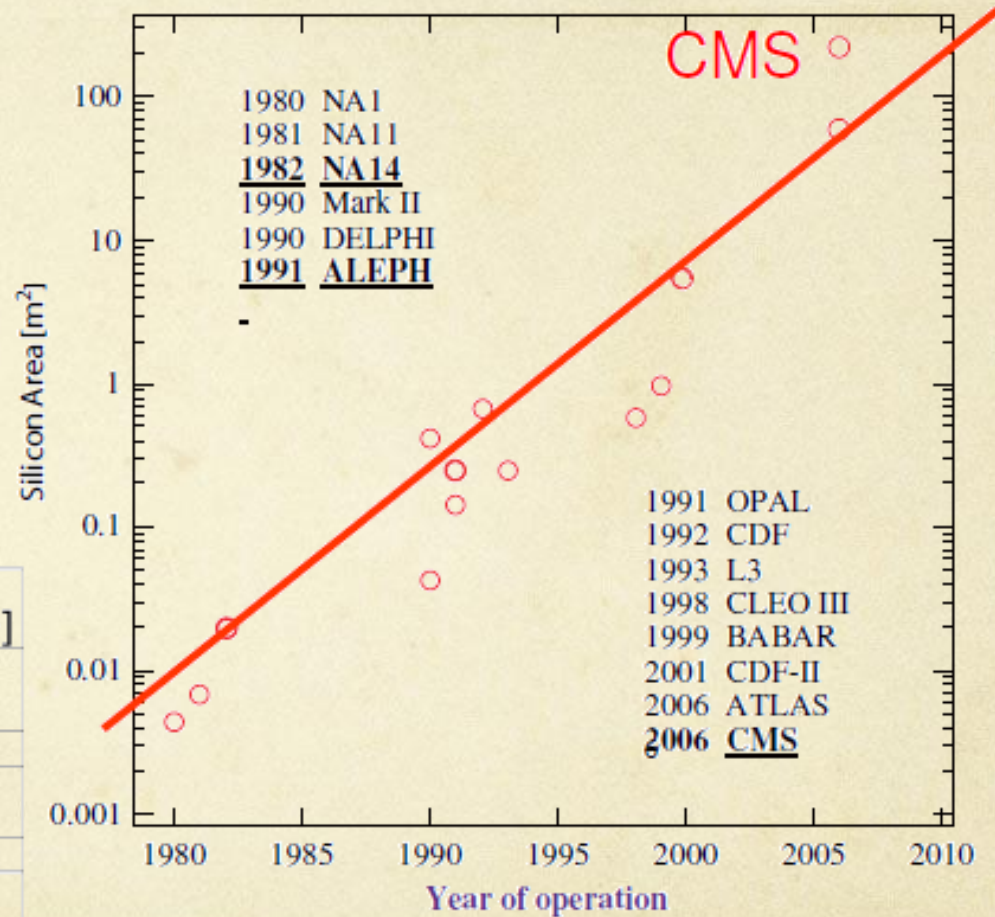


- Fully depleted sensitive layer
- Fully monolithic
- Electronics similar to MAPS

### ○ Increasing popularity

- Initially restricted to vertexing
  - LEP, B-factories
- Gradually introduced for tracking
  - LHC
  - Possible due to dvpmnt of integration techniques (bonding, ...)

experiment	nb. of detectors	nb. of channels	silicon area [m <sup>2</sup> ]
CMS	15.95 k	$10 \times 10^6$	223
ATLAS	16.0/2 k	$6.15 \times 10^6$	60
AMS 2	2.3 k	196 k	6.5
DO 2		793 k	4.7
CDF SVX II	720	405 k	1.9
Babar		140 k	0.95
Aleph	144	95 k	0.49
L3	96	86 k	0.23



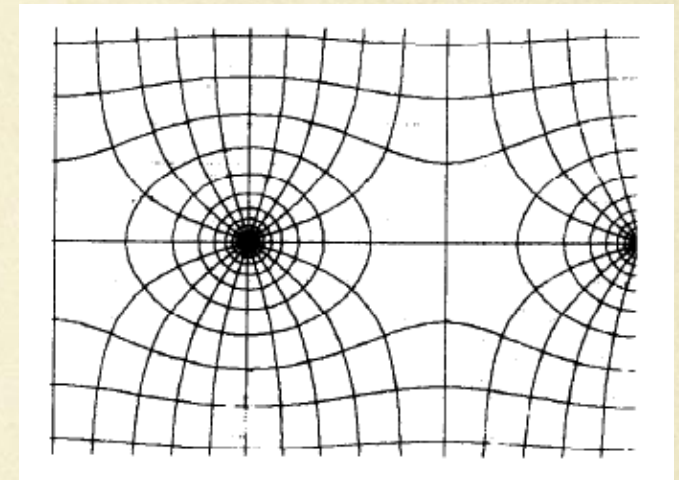
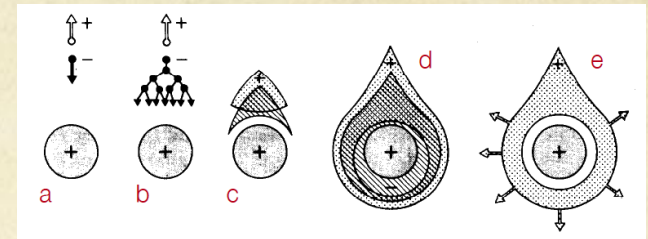


### ○ Basic sensitive element

- Metallic wire,  $1/r$  effect generated an avalanche
- Signal depends on gain (proportional mode) typically  $10^4$
- Signal is fast, a few ns

### ○ Gas proportional counters

- Multi-Wire Proportional Chamber
  - Array of wires
  - 1 or 2D positioning depending on readout
  - Wire spacing (pitch) limited to 1-2 mm
- Straw or drift tube
  - One wire in One tube
  - Extremely fast (compared to Drift Chamber)
  - Handle high rate
  - Spatial resolution  $< 200 \mu\text{m}$
  - Left/right ambiguity



Electric fields line  
around anode wires

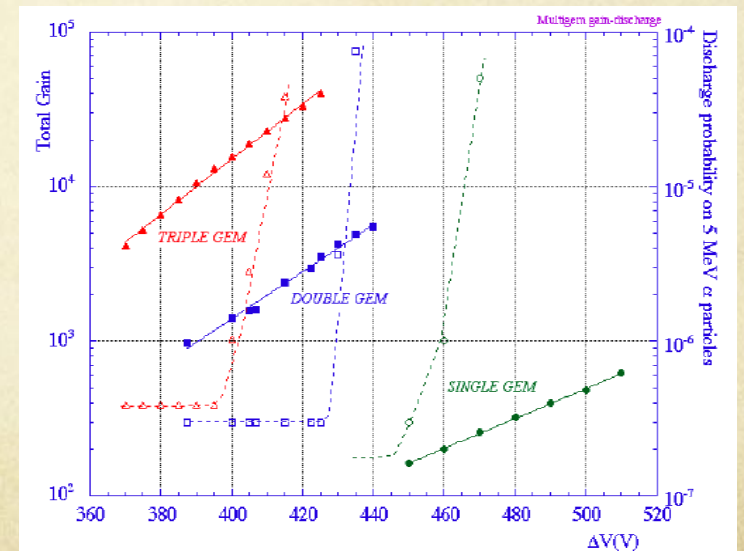
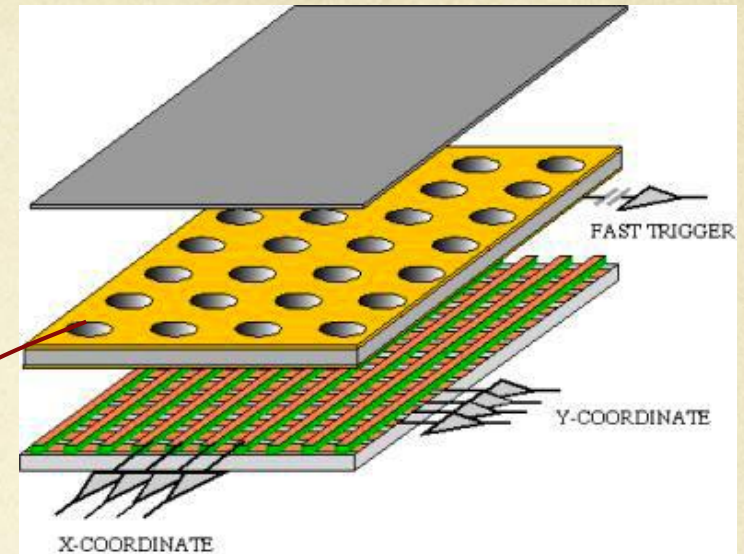
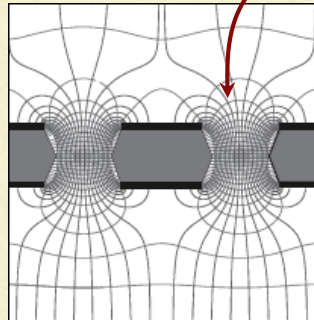
### ○ Micro-pattern gas multipliers

#### → MSGC

- Replace wires with lithography micro-structures
- Smaller anodes pitch 100-200  $\mu\text{m}$
- BUT Ageing difficulties due to high voltage and manufacturing not so easy

#### → GEM

- Gain  $10^5$
- Hit rate  $10^6 \text{ Hz/cm}^2$





### ○ Micro-pattern gas multipliers

#### → MSGC

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- BUT Ageing difficulties due to high voltage and manufacturing not so easy

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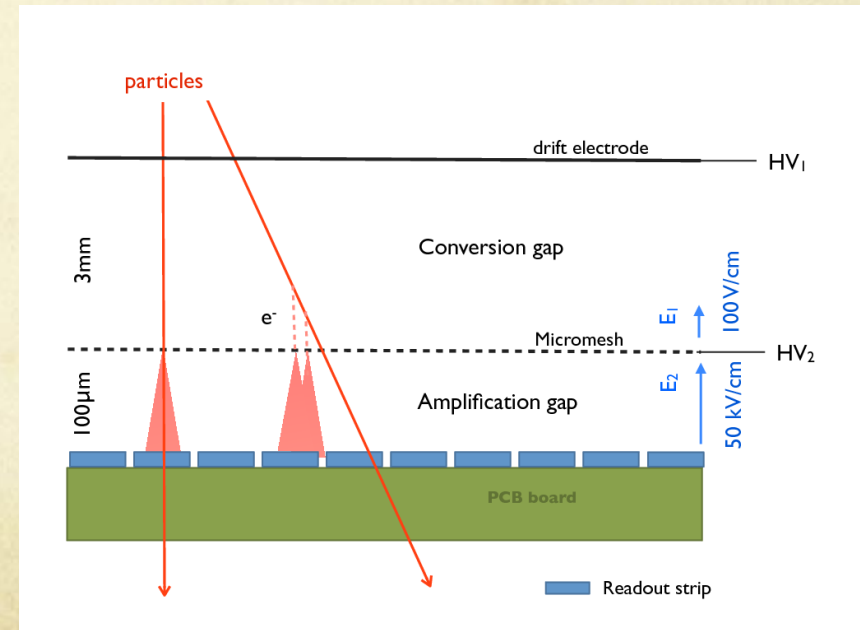
- Gain  $10^5$
- Hit rate  $10^6 \text{ Hz/cm}^2$

#### → MICROMEAS

- Even smaller distance anode-grid
- Hit rate  $10^9 \text{ Hz/cm}^2$

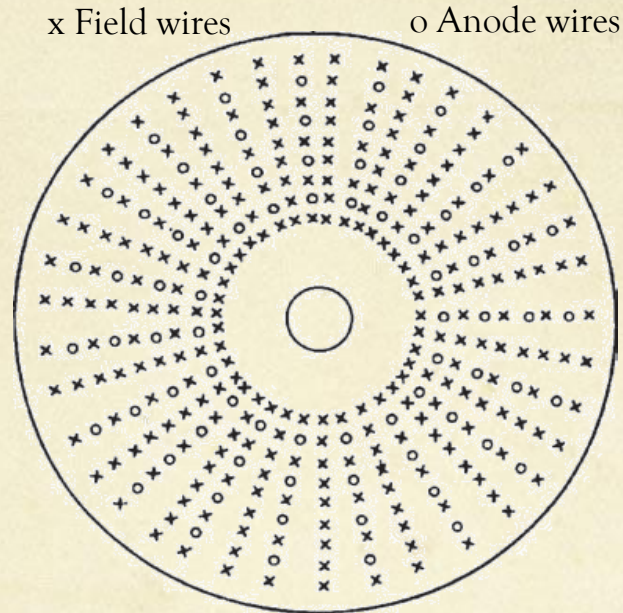
#### → More development

- Electron emitting foil working in vacuum!



### ○ Basic principle

- Mix field and anode wires
  - Generate a drift
- Pressurize gas to increase charge velocity (few atm)
- 3D detector
  - 2D from wire position
  - 1D from charge sharing at both ends



Belle II drift Chamber

### ○ Spatial Resolution

- Related to drift path

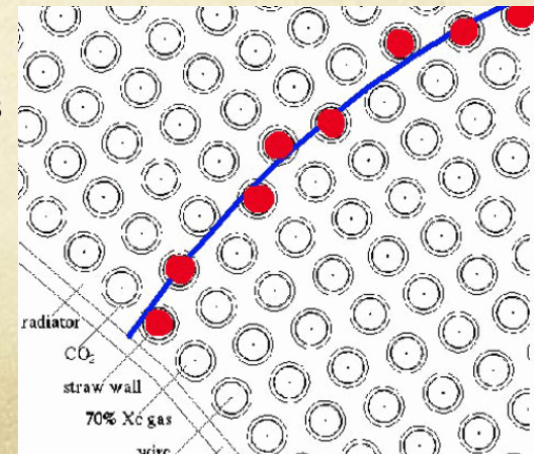
$$S \propto \sqrt{\text{drift length}}$$

- Typically 100-200  $\mu\text{m}$

### ○ Remarks

- Could not go to very small radius

Same principle  
with straw tubes



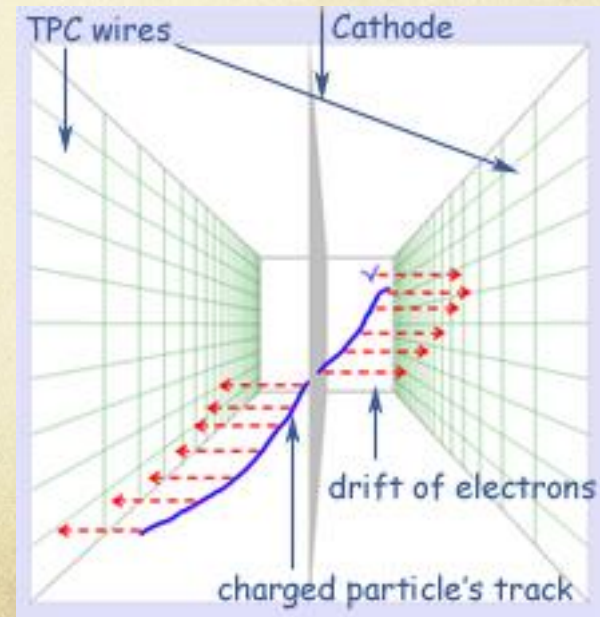
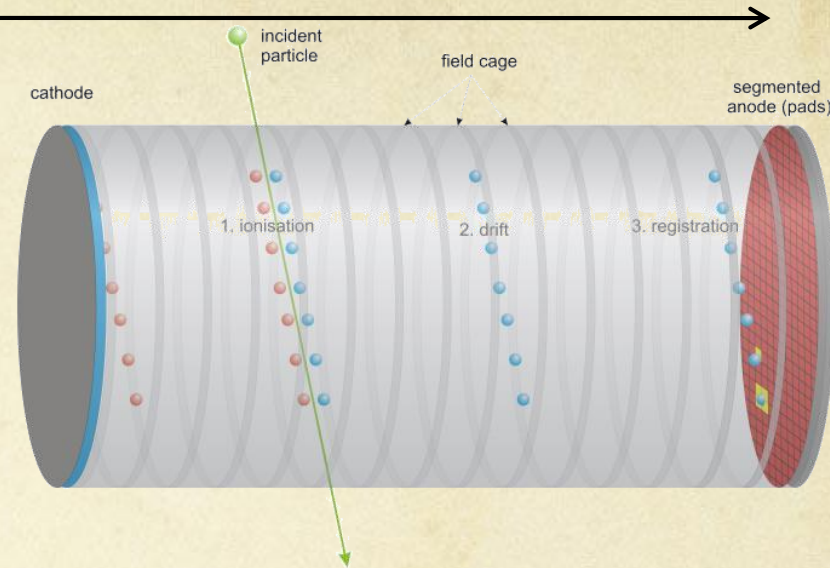


### ○ Benefits

- Large volume available
- Multi-task: tracking + Part. Identification

### ○ Basic operation principle

- Gas ionization → charges
- Electric field → charge drift along straight path
- Information collected
  - 2D position of charges at end-cap
  - 3rd dimension from drift time
  - Energy deposited from #charges
- Different shapes:
  - rectangles (ICARUS)
  - Cylinders (colliders)
  - Volumes can be small or very large



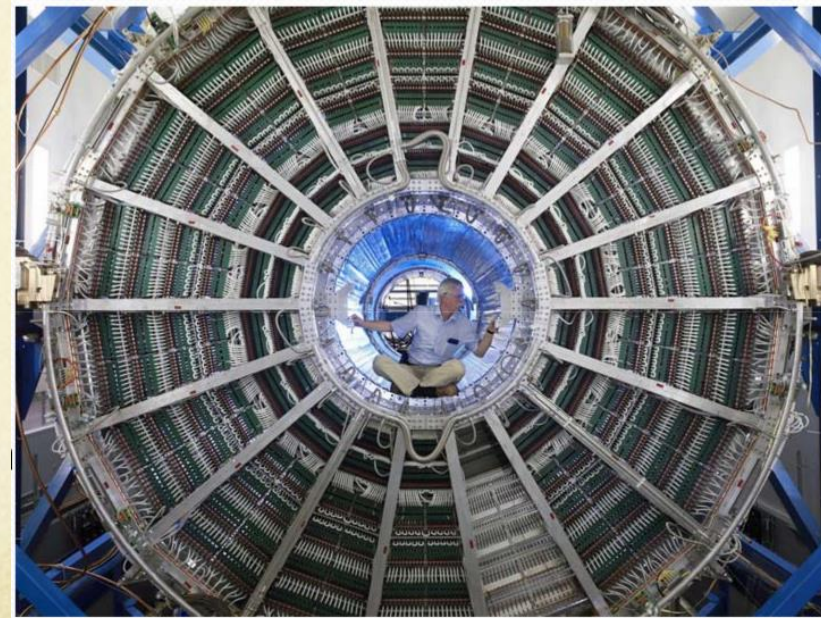
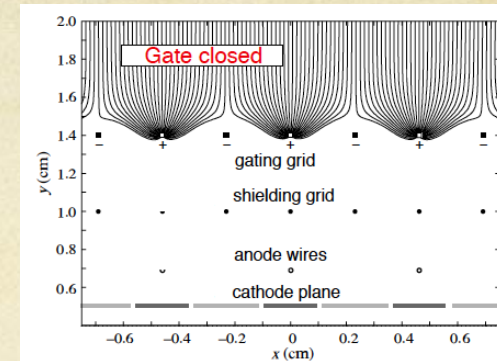
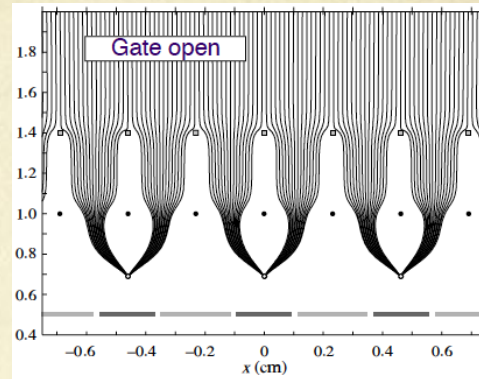


### ○ End cap readout

- Gas proportional counters
  - Wires+pads, GEM, Micromegas

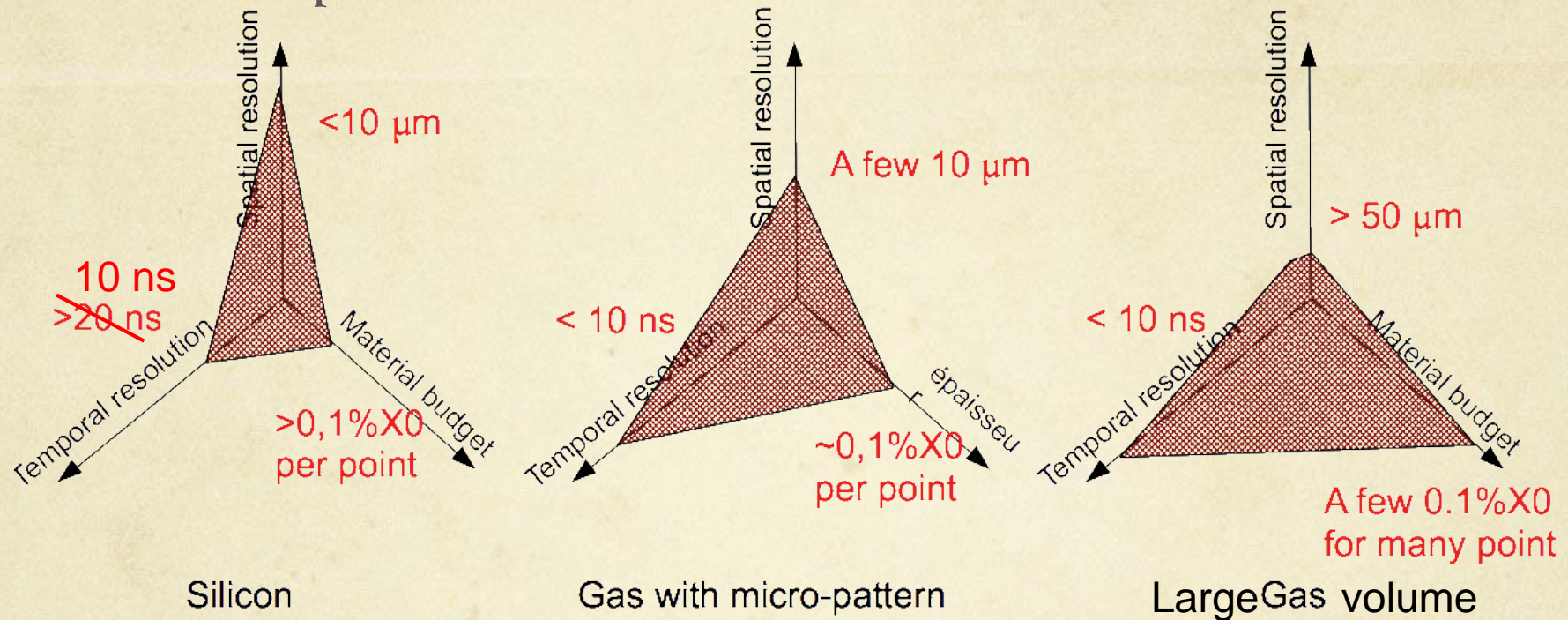
### ○ Performances

- Two-track resolution  $\sim 1\text{cm}$
- Transverse spatial resolution  $\sim 100 - 200\ \mu\text{m}$
- Longitudinal spatial resolution  $\sim 0.2 - 1\ \text{mm}$
- Longitudinal drift velocity: 5 to 7 cm/ $\mu\text{s}$ 
  - ALICE TPC (5m long): 92  $\mu\text{s}$  drift time
- Pros
  - Nice continuously spaced points along trajectory
  - Minimal multiple scattering (inside the vessel)
- Cons
  - Limiting usage with respect to collision rate





### ○ Tentative Comparison



### ○ Trend

- Faster collision rates and higher particle multiplicities favour
  - Fast silicon sensors and micro-pattern gas chambers
  - pixelisation
  - Still large gas ensemble for  
BelleII (SuperKEKB) → CDC and ILD (ILC) → TPC

### ○ Solenoid

- Field depends on current  $I$ , length  $L$ , # turns  $N$ 
  - on the axis  $B = \frac{\mu_0 NI}{\sqrt{L^2 + 4R^2}}$
  - Typically: 1 T needs 4 to 8 kA
    - **superconducting** metal to limit heat
- Field uniformity needs flux return (iron structure)
  - Mapping is required for fitting (remember  $B(\mathbf{x})$ ?)
  - Usually performed with numerical integration
- Calorimetry outside ➤ limited material ➤ **superconducting**
- Fringe field calls for compensation



	Field (T)	Radius (m)	Length (m)	Energy (MJ)
ALICE	0.5	6		150
ATLAS	2	2.5	5.3	700
CMS	4	5.9	12.5	2700
ILC	4	3.5	7.5	2000

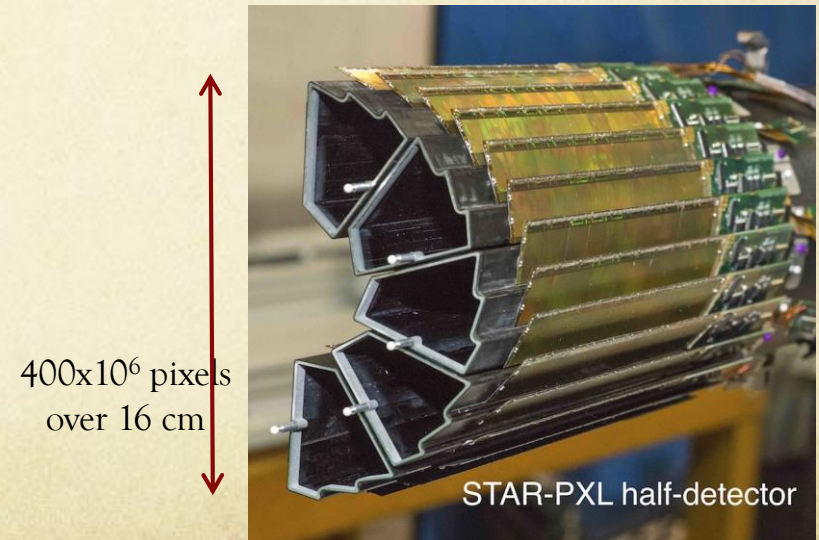
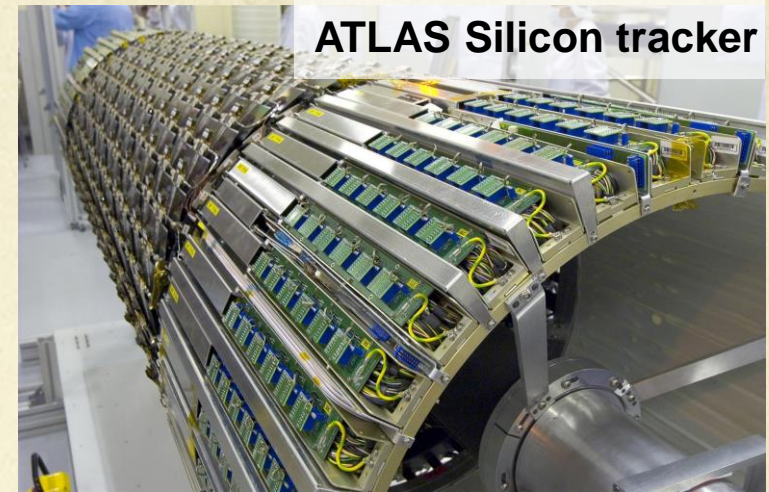
### ○ Superconduction

- cryo-operation ➤ quenching possible !
- Magnetic field induces energy:  $E \propto B^2 R^2 L$ 
  - Cold mass necessary to dissipate heat in case of quench



### ○ From a detection principle to a detector

- Build large size or many elements
  - Manufacture infrastructures
  - Characterization capabilities
  - Production monitoring
  - New monolithic silicon pixel detector tend to replace silicon strip technology
- Integration in the experiment
  - Mechanical support
  - Electrical services (powering & data transmission)
  - Cooling (signal treatment dissipates power)
- Specific to trackers
  - Internal parts of multi-detectors experiment → limited space
  - Material budget is ALWAYS a concern
  - ⇒ trade-offs required







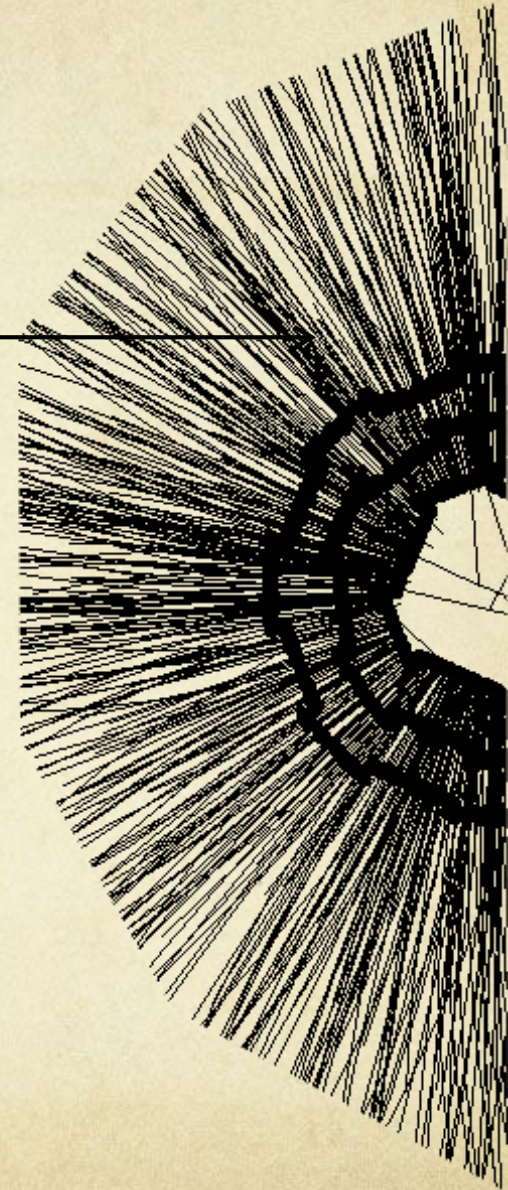
- Signal generation
  - see Ramo's theorem
- Silicon drift detectors
  - Real 2D detectors made of strips
  - 1D is given by drift time
- Diamond detectors
  - Could replace silicon for hybrid pixel detectors
  - Very interesting for radiation tolerance
- Charge Coupled Devices (CCD)
  - Fragile/ radiation tolerance
- Nuclear emulsions
  - One of the most precise  $\sim 1\mu\text{m}$
  - No timing information  $\rightarrow$  very specific applications
- Scintillators
  - Extremely fast (100 ps)
  - Could be arranged like straw tubes
  - But quite thick ( $X_0 \sim 2\text{ cm}$ )



# 3. Standard algorithms

---

- Finders
- First evaluation of momentum resolution
- Fitters
- Alignment



#### ○ Global methods

- Transform the coordinate space into **pattern space**
  - “pattern” = parameters used in track model
- Identify the “best” solutions in the new phase space
- Use all points at a time
  - No history effect
- Well adapted to evenly distributed points with same accuracy

#### ○ Local methods

- Start with a **track seed** = restricted set of points
  - Could require good accuracy from the beginning
- Then extrapolate to next layer-point
  - And so on...**iterative procedure**
- “Wrong” solutions discarded at each iteration
- Possibly sensitive to “starting point”
- Well adapted to redundant information

**FINDING drives  
tracking efficiency  
fake track rate**



#### ○ A simple example

- Straight line in 2D: model is  $x = a^*z + b$
- Track parameters (a,b); N measurements  $x_i$  at  $z_i$  ( $i=1..N$ )

#### ○ A more complex example

- Helix in 3D with magnetic field
- Track parameters ( $\gamma_0, z_0, D, \tan\lambda, C=R$ )
- Measurements ( $r, \varphi, z$ )

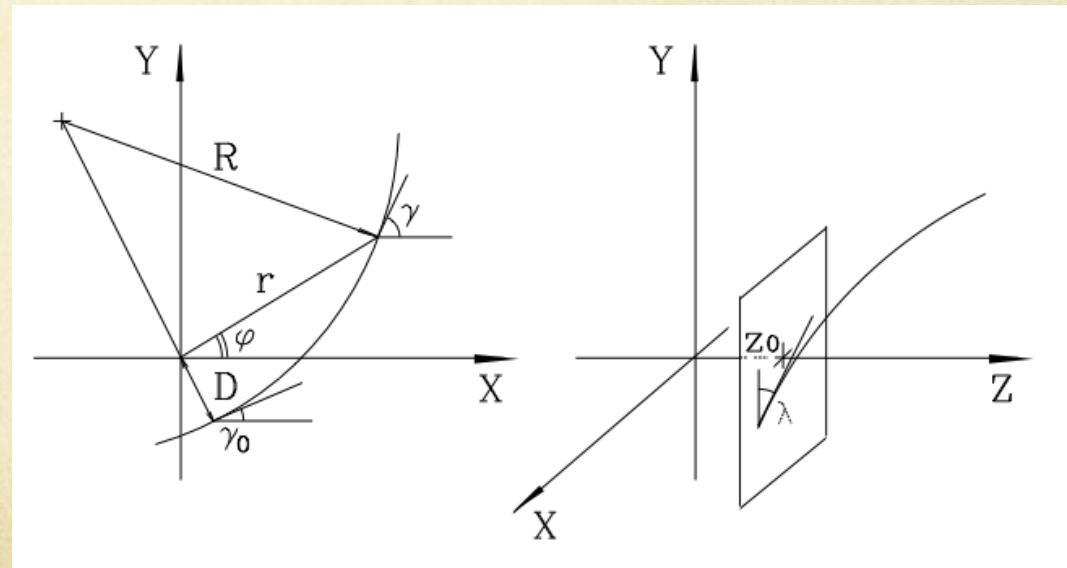
$$\varphi(r) = \gamma_0 + a \sin \frac{C r (1 + CD) D / r}{1 + 2CD}$$

$$z(r) = z_0 + \frac{\tan\lambda}{C} a \sin \left( C \sqrt{\frac{r^2 - D^2}{1 + 2CD}} \right)$$

#### ○ Generalization

- Parameters: P-vector  $\mathbf{p}$
- Measurements: N-vector  $\mathbf{c}$
- Model: function  $f(\mathcal{R}^P \rightarrow \mathcal{R}^N)$

$$f(\mathbf{p}) = \mathbf{c} \leftrightarrow \text{propagation}$$





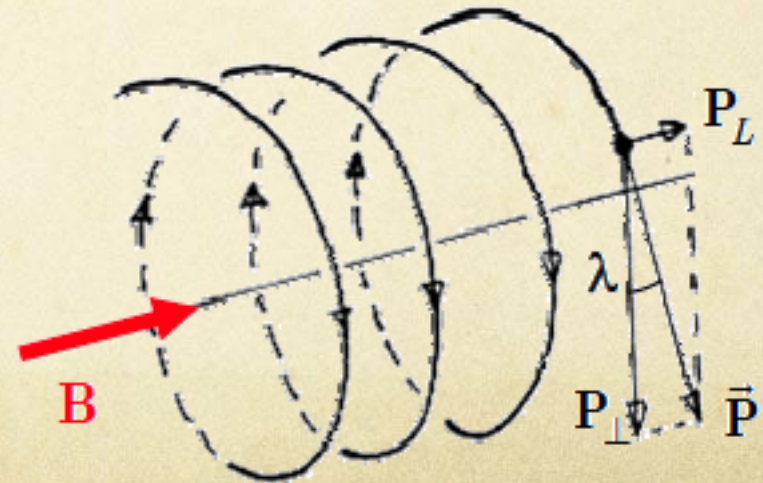
### ○ Another view of the helix

- $s$  = track length
- $h$  = rotation direction
- $\lambda$  = dip angle
- Pivot point ( $s=0$ ):
  - position  $(x_0, y_0, z_0)$
  - orientation  $\varphi_0$

$$x(s) = x_0 + R \left[ \cos \left( \Phi_0 + \frac{hs \cos \lambda}{R} \right) - \cos \Phi_0 \right]$$

$$y(s) = y_0 + R \left[ \sin \left( \Phi_0 + \frac{hs \cos \lambda}{R} \right) - \sin \Phi_0 \right]$$

$$z(s) = z_0 + s \sin \lambda$$





### 3. Standard algorithms:

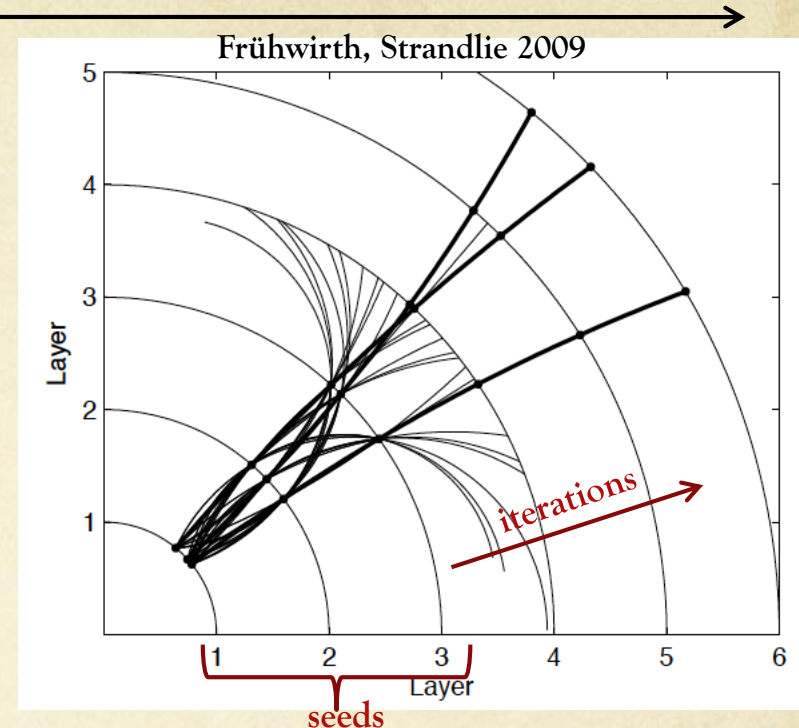
## Local method 1/2

#### ○ Track seed = initial segment

- Made of few (2 to 4) points
  - One point could be the expected primary vtx
- Allows to initialize parameter for track model
- Choose most precise layers first
  - usually inner layers
- But if high hit density
  - Start farther from primary interaction @ lowest density
  - Limit mixing points from different tracks

#### ○ Extrapolation step

- Out or inward (=toward primary vtx) onto the next layer
- Not necessarily very precise, especially **only local model** needed
  - Extrapolation uncertainty  $\lesssim$  layer point uncertainty
  - Computation speed important
- Match (associate) nearest point on the new layer
  - Might skip the layer if point missing
  - Might reject a point: if worst track-fit or if fits better with another track



#### ○ Variant with track segments

- First build “tracklets” on natural segments
  - Sub-detectors, or subparts with same resolution
- Then match segments together
- Typical application:
  - Segments large tracker (TPC) with vertex detector (Si)
    - layers dedicated to matching

#### ○ Variant with track roads

- Full track model used from start

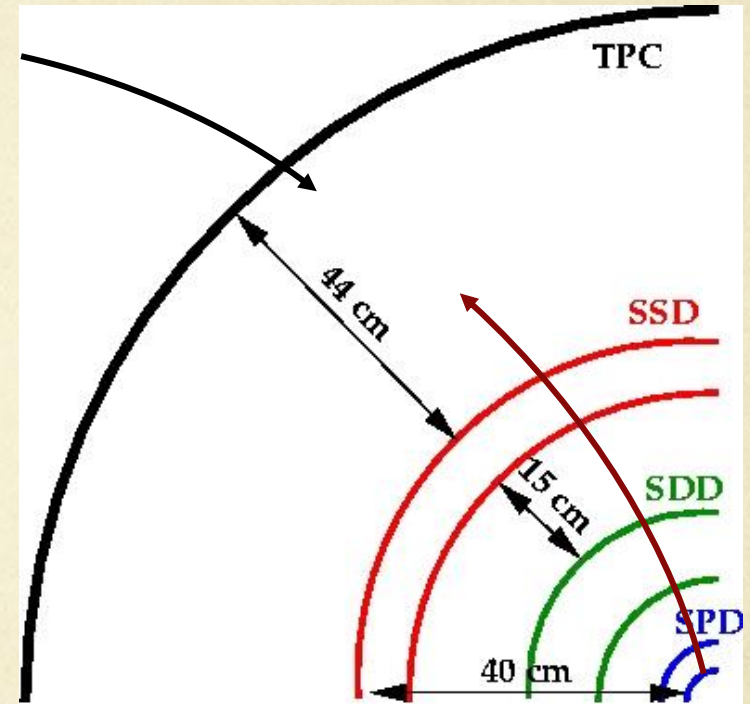
#### ○ Variant with Kalman filter

- See later

#### ○ Figure of merit

$$S_{eff,f} \sim S_{eff,z} \sim r_{bckgrnd}$$

- $\sigma_{eff} = \sigma(\text{sensor}) \oplus \sigma(\text{track extrapolation})$  = effective spatial resolution
- $\rho$  = background hit density





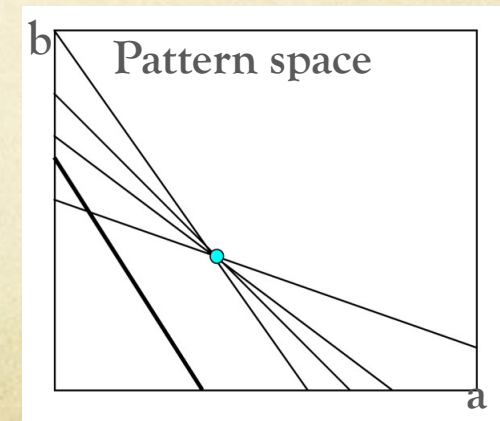
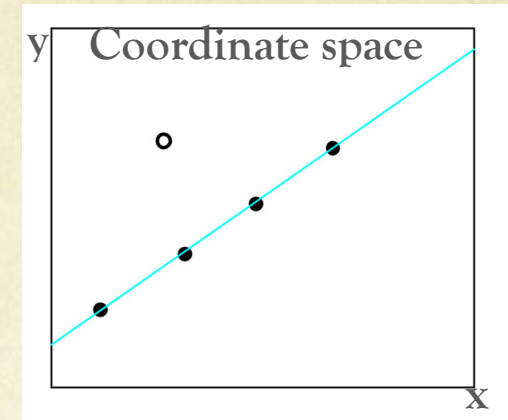
#### ○ Brute force = combinatorial way

- Consider all possible combination of points to make a track
- Keep only those compatible with model
- Usually too time consuming...

#### ○ Hough transform

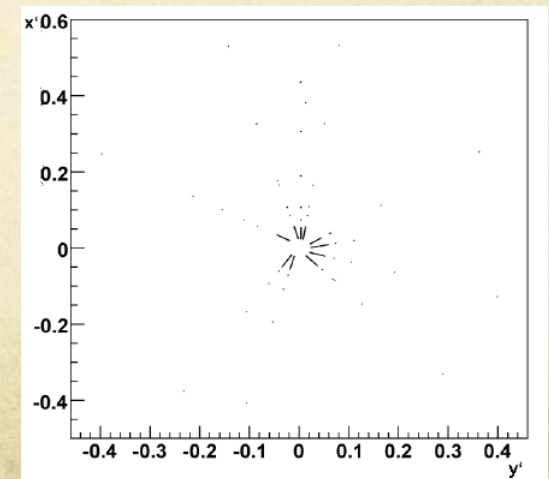
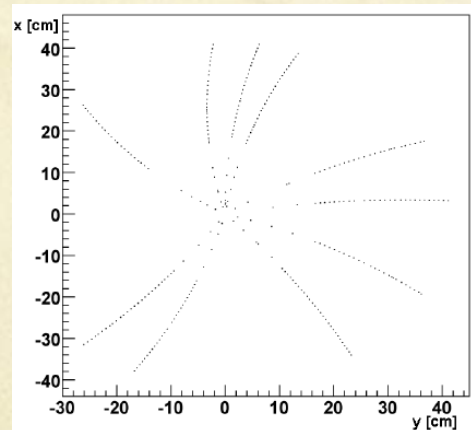
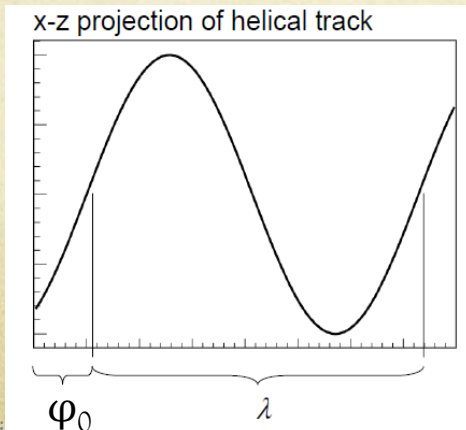
- Example straight track:

- Coord. space  $y = a \cdot x + b \Leftrightarrow$  pattern space  $b = y - x \cdot a$
- Each point  $(y,x)$  defines a line in pattern space
- All lines, from points belonging to same straight-track, cross at same point  $(a,b)$
- In practice:  
discretize pattern space and search for maximum
- Applicable to circle finder
  - needs two parameters as well  $(r, \varphi$  of center)
  - if track is assumed to originate from  $(0,0)$
- More difficult for more than 2 parameters...



### ○ Conformal mapping for helix

- $(x_0, y_0, z_0)$  a (pivot) point on the helix with  $(a, b)$  the center of the projected circle of radius  $r$ 
  - $(x-a)^2 + (y-b)^2 = r^2$
- Transforming to  $x' = \frac{x-x_0}{r^2}, y' = \frac{y-y_0}{r^2}$  leads to  $y' = -\frac{a}{b}x' + \frac{1}{2b}$  i.e. a line!
  - So all measured points  $(x, y)$  in circles are aligned in  $(x', y')$  plane
- Use Hough transform  $(x', y') \rightarrow (r, \theta)$  so that  $r = x' \cos \theta + y' \sin \theta$ 
  - To find the lines corresponding to true circles with  $a = r \cos \theta$  and  $b = r \sin \theta$
- Repeat for different  $z_0$ 
  - New Hough transforms
  - $\lambda$  = dip angle
  - $\varphi_0$  = orientation of pivot point



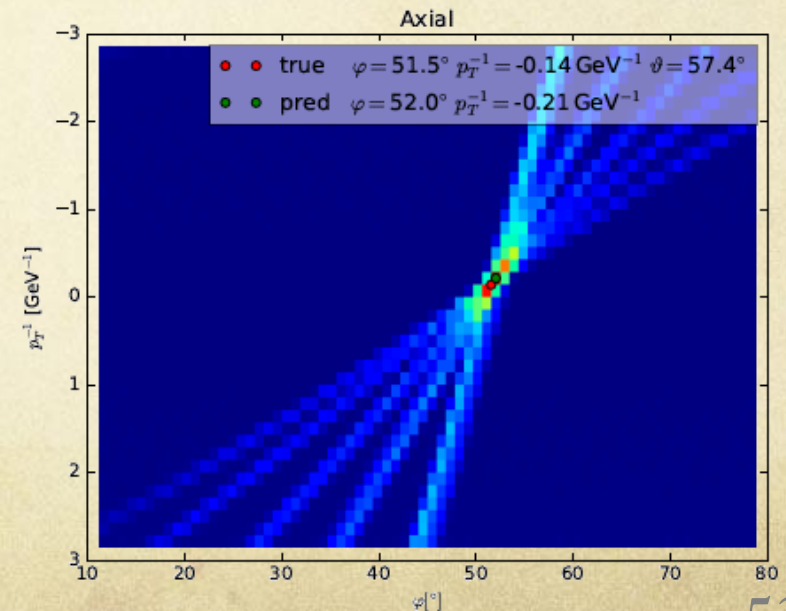




### ○ Figure of merit

- Search precision in pattern space depends on bin-size in the pattern space
  - Such bin-size  $\sim$  uncertainty on the measurements

$$S_f(sensor) \cdot S_z(sensor) \cdot r_{bckgrnd}$$



#### ○ Why do we need to fit?

- Measurement error
- Multiple scattering error

#### ○ Global fit

- Assume knowledge of:
  - all track points
  - full correlation matrix
    - difficult if  $\sigma_{\text{mult. scatt.}} \gtrsim \sigma_{\text{meas.}}$
- Least square method

#### ○ Iterative (local) fit

- Iterative process:
  - points included in the fit one by one
  - could be merged with finder step
- Kalman filter

**FITTING drives  
track extrapolation  
& momentum res.**



#### ○ The rule

- For the fit: nb of constraints  $>$  nb of free parameters in the track model

#### ○ Measurements

- 1 point in 2D = 1 constraint ( $x \leftrightarrow y$ ) or ( $r \leftrightarrow \phi$ )
- 1 point in 3D = 2 constraints ( $x \leftrightarrow z$  &  $y \leftrightarrow z$ )

#### ○ Models

- Straight track in 2D = 2 parameters
  - 1 position @ origin ( $z=0$ ) , 1 slope
- Straight track in 3D = 4 parameters
  - 2 positions @ origin, 2 slopes
- Circle in 2D = 3 parameters
  - 2 position for center, 1 radius
- Helix in 3D = 5 parameters
  - , 1 radius, 1 dip angle

#### ○ Minimal #points needed

$\Leftarrow$  2 points in 2D

$\Leftarrow$  2 points in 3D

$\Leftarrow$  3 points in 2D

$\Leftarrow$  3 points in 3D

#### ○ Linear model hypothesis

- P track parameters  $\mathbf{p}$ , with N measurements  $\mathbf{c}$

$$\vec{c} = \vec{c}_s + A(\vec{p} - \vec{p}_s) + \vec{\epsilon}$$

- $\mathbf{p}_s$  = known starting point (pivot),  $\mathbf{A}$  = **track model** NxP matrix,  $\vec{\epsilon}$  = error vector corresponding to  $\mathbf{V}$  = covariance NxN matrix

“N measurements” means:

- K points (or layers)
- D coordinates at each point
- $N = K \times D$

#### ○ Sum of squares:

$$\hat{a} \frac{(\text{model} - \text{measure})^2}{\text{uncertainty}^2} \quad \Rightarrow \quad S(\vec{p}) = \left( \vec{c}_s + A(\vec{p} - \vec{p}_s) - \vec{c} \right)^T V^{-1} \left( \vec{c}_s + A(\vec{p} - \vec{p}_s) - \vec{c} \right)$$

#### ○ Best estimator (minimizing variance)

$$\frac{dS}{d\vec{p}}(\underline{\vec{p}}) = 0 \quad \Rightarrow \quad \underline{\vec{p}} = \vec{p}_s + \left( A^T V^{-1} A \right)^{-1} A^T V^{-1} (\vec{c} - \vec{c}_s)$$

- Variance (= uncertainty) of the estimator:

$$\underline{V}_{\vec{p}} = \left( A^T V^{-1} A \right)^{-1}$$

- Estimator p follows a  $\chi^2$  law with N-P degrees of freedom

#### ○ Problem $\Leftrightarrow$ inversion of a PxP matrix ( $A^T V^{-1} A$ )

- **But real difficulty could be computing V (NxN matrix)**

← layer correlations if multiple scattering non-negligible if  $\sigma_{\text{mult. scatt.}} \gtrsim \sigma_{\text{meas}}$



### 3. Standard algorithms:

## LSM on straight tracks

#### ○ Straight line model

- 2D case → D=2 coordinates (z,x)
- 2 parameters: a = slope, b = intercept at z=0

#### ○ General case

- K+1 detection planes (i=0...k)
  - located at  $z_i$
  - Spatial resolution  $\sigma_i$

- Useful definitions

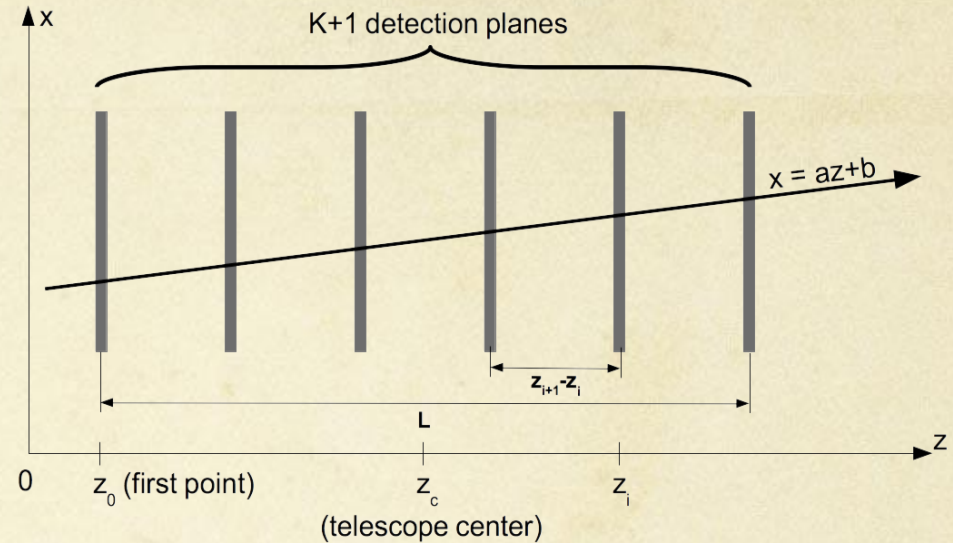
$$S_1 = \frac{\sum_{i=0}^K \frac{1}{S_i^2}}{\sum_{i=0}^K \frac{1}{S_i^2}}, S_z = \frac{\sum_{i=0}^K \frac{z_i}{S_i^2}}{\sum_{i=0}^K \frac{1}{S_i^2}}, S_{xz} = \frac{\sum_{i=0}^K \frac{x_i z_i}{S_i^2}}{\sum_{i=0}^K \frac{1}{S_i^2}}, S_{z^2} = \frac{\sum_{i=0}^K \frac{z_i^2}{S_i^2}}{\sum_{i=0}^K \frac{1}{S_i^2}}$$

→ Solutions 
$$a = \frac{S_1 S_{xz} - S_x S_z}{S_1 S_{z^2} - (S_z)^2}, b = \frac{S_x S_{z^2} - S_z S_{xz}}{S_1 S_{z^2} - (S_z)^2}$$

- Uncertainties

$$S_a^2 = \frac{S_1}{S_1 S_{z^2} - (S_z)^2}, S_b^2 = \frac{S_{z^2}}{S_1 S_{z^2} - (S_z)^2}$$

**! correlation** 
$$\text{cov}_{a,b} = \frac{-S_z}{S_1 S_{z^2} - (S_z)^2}$$



#### ○ Case of uniformly distributed (K+1) planes

- $z_{i+1} - z_i = L/K$  et  $\sigma_i = \sigma \quad \forall i$

- $S_z = 0 \rightarrow a, b$  uncorrelated

$$S_a^2 = \frac{12K}{(K+2)L^2} \frac{S^2}{K+1}, S_b^2 = \left( 1 + 12 \frac{K}{K+2} \frac{z_c^2}{L^2} \right) \frac{S^2}{K+1}$$

- Uncertainties :

- $\sigma_a$  and  $\sigma_b$  improve with  $1/\sqrt{(K+1)}$
- $\sigma_a$  and  $\sigma_b$  improve with  $1/L$
- $\sigma_b$  improve with  $z_c$

### 3. Standard algorithms:

## LSM on fixed target geometry

#### ○ Hypothesis

- K detectors, each with  $\sigma$  single point accuracy

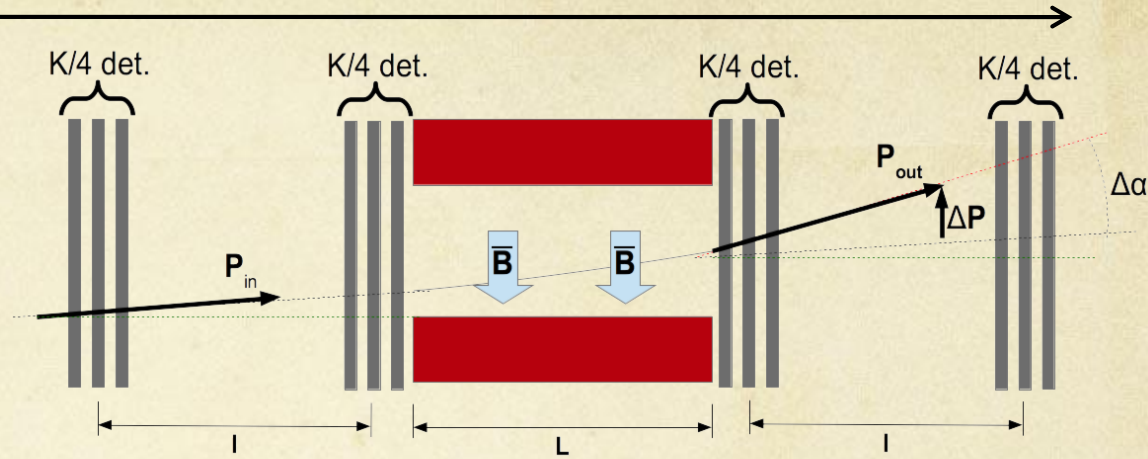
- Uniform field over L from dipole

- Trajectory:  $\Delta\alpha = \left| \frac{0.3qBL}{p} \right|$

- Bending:  $\Delta p = p \Delta\alpha$

- Geometrical arrangement optimized for resolution

- Angular determination on input and output angle:  $S_a^2 = \frac{16 S^2}{K l^2}$



#### ○ Without multiple scattering

- Uncertainty on momentum

$$\frac{S_p}{p} = \frac{8}{0.3q} \frac{1}{BL} \frac{S}{l\sqrt{K}} p$$

- Note proportionality to  $p$ !

#### ○ Multiple scattering contribution

- Bring additive term proportional to K and  $\sigma_\theta = \frac{13.6 \text{ (MeV/c)}}{\beta p} \sqrt{\frac{\text{thickness}}{X_0}}$



### 3. Standard algorithms:

## LSM on collider geometry

#### ○ Hypothesis

- K detectors uniformly distributed each with  $\sigma$  single point accuracy
- Uniform field over path length L

#### ○ Without multiple scattering

- Uncertainty on transverse momentum (Glückstern formula)

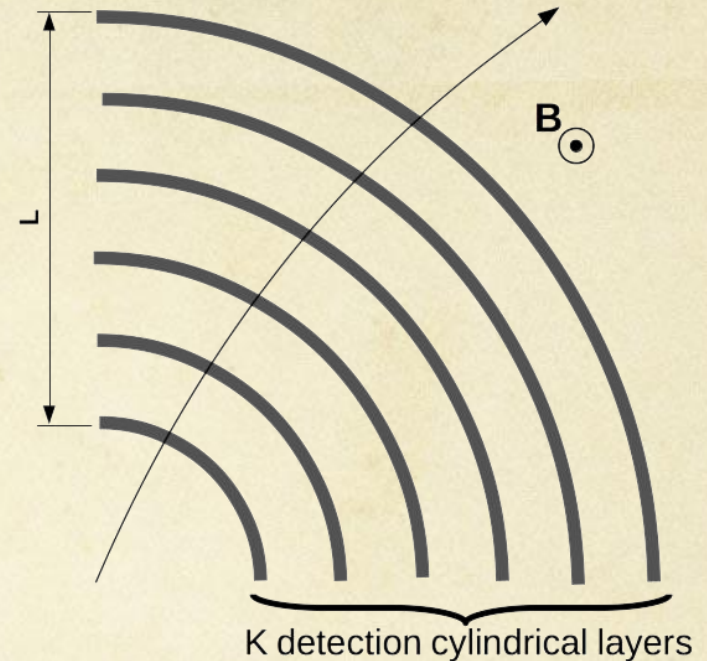
$$\frac{S_{p_T}}{p_T} = \frac{\sqrt{720}}{0.3q} \frac{1}{BL^2} \frac{S}{\sqrt{K+6}} p_T$$

- Works well with large  $K > 20$

#### ○ Multiple scattering contribution

- Brings additive contribution

$$\frac{\sigma_{p_T}}{p_T} = \frac{1.43}{0.3q} \frac{1}{BL} \frac{13.6 \text{ (MeV/c)}}{\beta p} \sqrt{\frac{\text{thickness}}{X_0}}$$



### 3. Standard algorithms:

## Kalman filter 1/2

#### ○ Dimensions

- P parameters for track model
- D “coordinates” measured at each point (usually  $D < P$ )
- K measurement points (# total measures:  $N = K \times D$ )

#### ○ Starting point

- Initial set of parameters: first measurements
- With large uncertainties if unknowns

#### ○ Iterative method

- Propagate to next layer = prediction

- Using the **system equation**  $\vec{p}_k = G \vec{p}_{k-1} + \vec{\omega}_k$
- $G$  = P x P matrix,  $\omega$  = perturbation associated with covariance P x P matrix  $V_\omega$

- Update the covariance matrix with additional uncertainties (ex: material budget between layers)

$$V_{k|k-1} = V_{k-1} + V_{W_k}$$

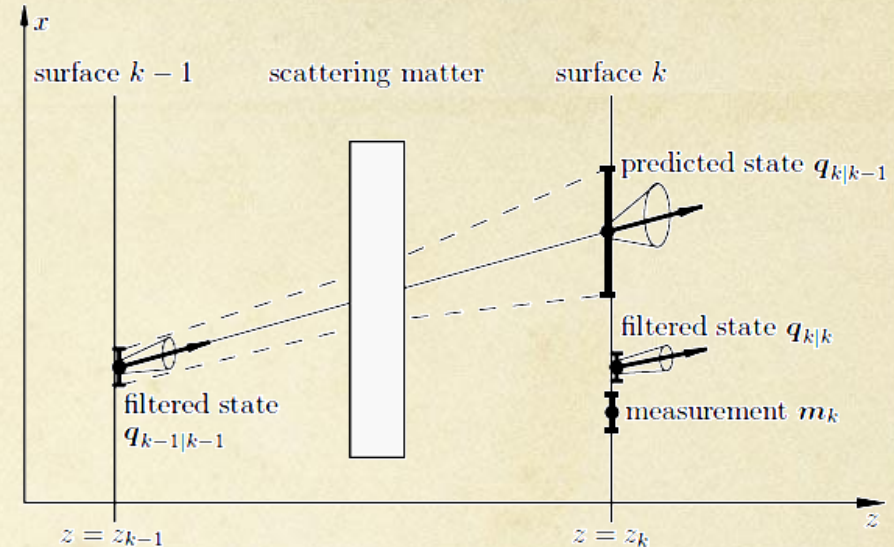
- Add new point to update parameters and covariance, using the **measure equation**

$$\vec{m}_k = H \vec{p}_k + \vec{\varepsilon}_k$$

- $H$  = D x P matrix,  $\varepsilon$  = measure error associated with **diagonal** covariance D x D matrix  $V_m$
- Weighted means of prediction and measurement using variance  $\Leftrightarrow \chi^2$  fit

- Iterate...

$$\vec{p}_k = \left( V_{k|k-1}^{-1} \vec{p}_{k|k-1} + H^T V_{m_k}^{-1} \vec{m}_k \right) \cdot \left( V_{k|k-1}^{-1} + H^T V_{m_k}^{-1} H \right)^{-1}$$







### ○ Forward and backward filters

- Forward estimate of  $\vec{p}_k$  from 1 → k-1 measurements
- Backward estimate of  $\vec{p}_k$  from k+1 → K measurements
- Independent estimates → combination with weighted mean = smoother step

### ○ Computation complexity

- only PxP, DxP or DxD matrices computation ( $\ll N \times N$ )

### ○ Mixing with finder

- After propagation step: local finder
- Some points can be discarded if considered as outliers in the fit (use  $\chi^2$  value)

### ○ Include exogenous measurements

- Like dE/dx, correlated to momentum
- Additional measurement equation

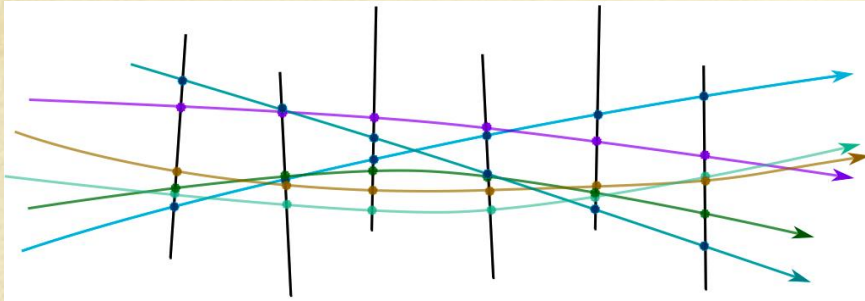
$$\vec{m}'_k = H' \vec{p}_k + \vec{\varepsilon}'_k$$

$$\vec{p}_k = \left( V_{k|k-1}^{-1} \vec{p}_{k|k-1} + H^T V_{m_k}^{-1} \vec{m}_k + H'^T V_{m'_k}^{-1} \vec{m}'_k \right) \cdot \left( V_{k|k-1}^{-1} + H^T V_{m_k}^{-1} H + H'^T V_{m'_k}^{-1} H' \right)^{-1}$$

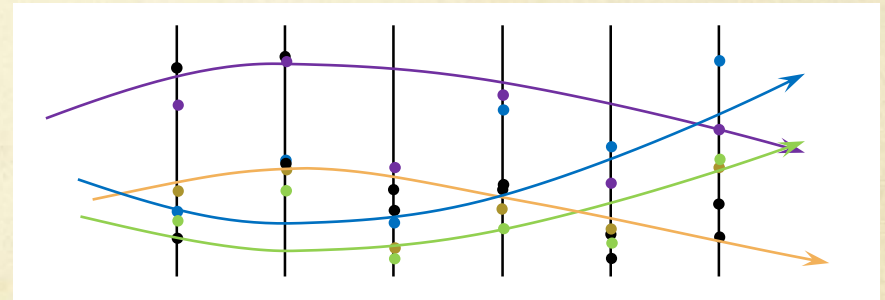
#### ○ Let's come back to one initial & implicit hypothesis

- “We know where the point are located.”
- True to the extent we know where the detector is!
- BUT, mechanical instability (magnetic field, temperature, air flow...) and also drift speed variation (temperature, pressure, field inhomogeneity...) limit our knowledge
- Periodic determination of positions and deformations needed = alignment

True tracks & True detector positions



Initial assumption for detector positions  
& tracks built from these assumptions



Note hit position relative to detector are the same  
tracks reconstructed are not even close to reality...  
and this assuming hits can be properly associated  
together!



#### ○ Alignment parameters

- Track model depends on additional “free” parameters, i.e. the sensor positions

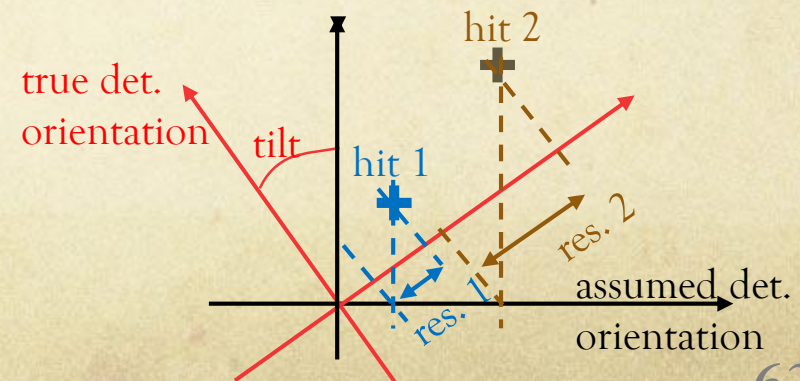
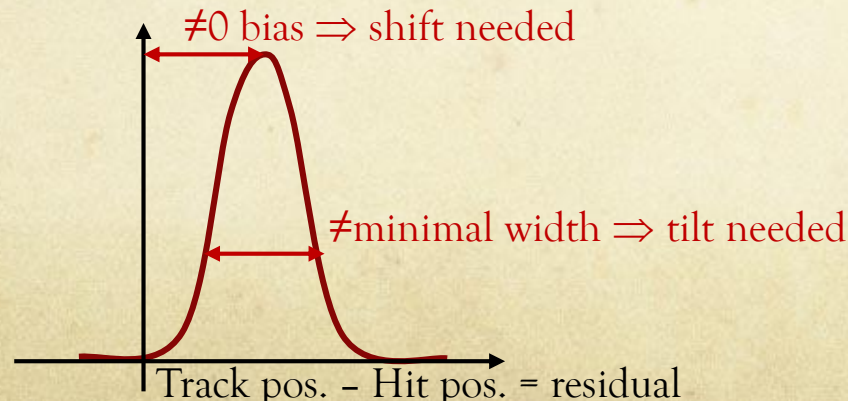
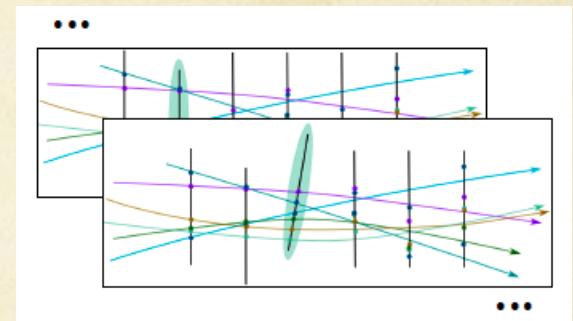
#### ○ Methods to find the relative position of individual sensors

##### → Global alignment:

- Fit the new params. to minimize the overall  $\chi^2$  of a set of tracks
- Beware: many parameters could be involved (few  $10^3$  can easily be reached) → Millepede algo.

##### → Local alignment:

- Use tracks reconstructed with reference detectors
- Align other detectors by minimizing the “residual” (track-hit distance) width

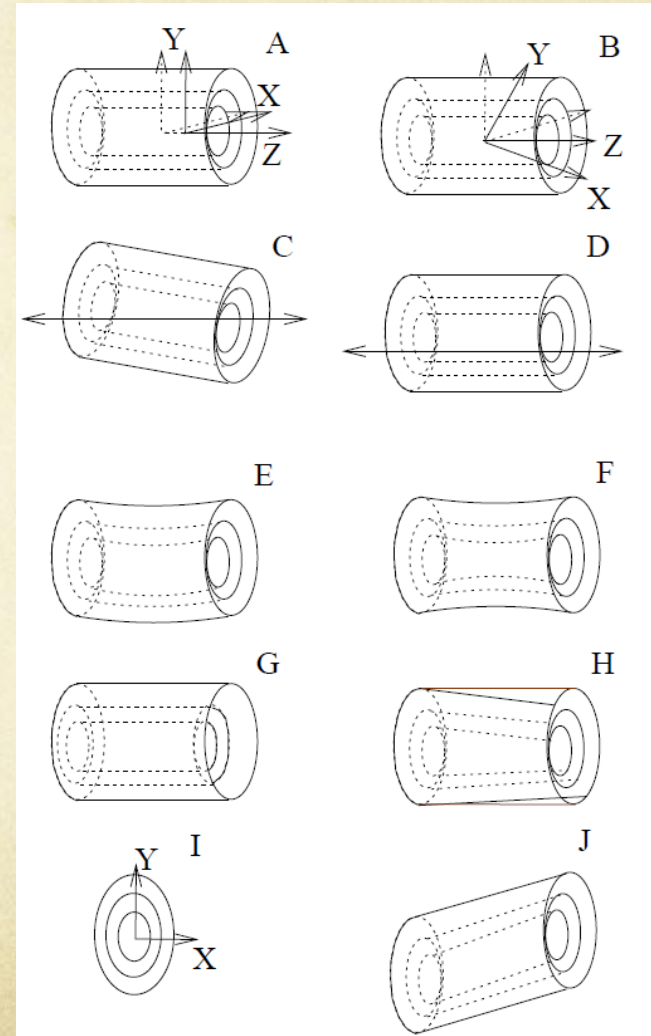


#### ○ In both methods (global or local alignment)

- Use a set of well know tracks and tracking-"friendly" environment to avoid bias
  - Muons (very traversing) and no magnetic field
  - Low multiplicity events

#### ○ Global deformations also possible

- affect overall positions & momentum
- Corrected through observing
  - Mass peak positions
  - Systematic differences at various track angles or detector positions



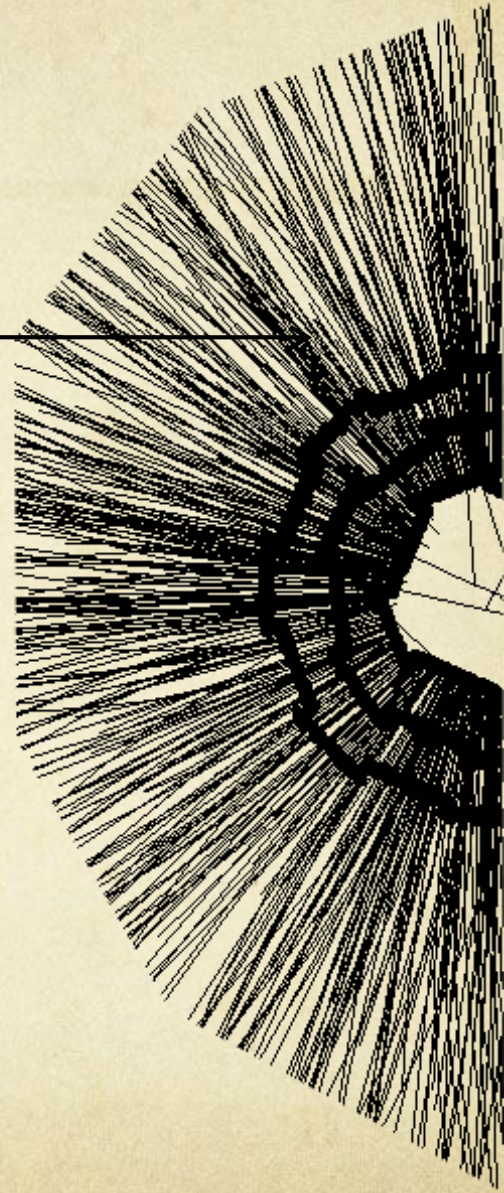


# 4. Advanced methods

## (brief illustrations)

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- Why ?
- Neural network
- Cellular automaton



### ○ Shall we do better?

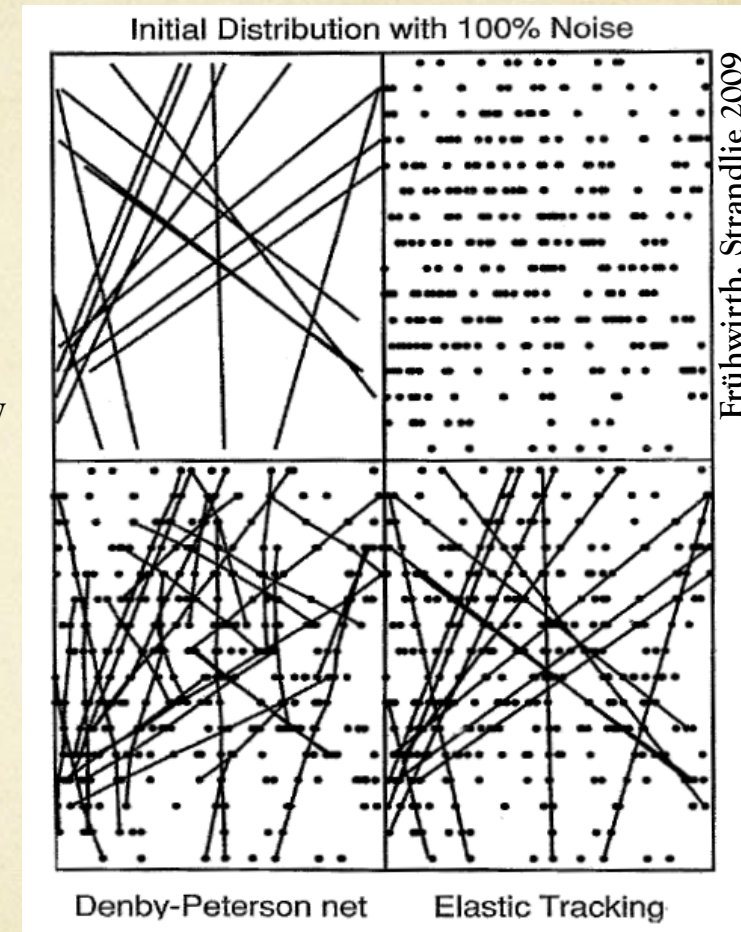
- Higher track/vertex density, less efficient the classical method
- Allows for many options and best choice

### ○ Adaptive features

- **Dynamic change** of track parameters during finding/fitting
- Measurements are weighted according to their uncertainty
  - Allows to take into account several “normally excluded” info
- **Many hypothesis are handled simultaneously**
  - But their number decrease with iterations (annealing like behavior)
- Non-linearity
- Often CPU-time costly (is that still a problem?)

### ○ Examples

- Neural network, Elastic nets, Gaussian-sum filters, Deterministic annealing, Cellular automaton

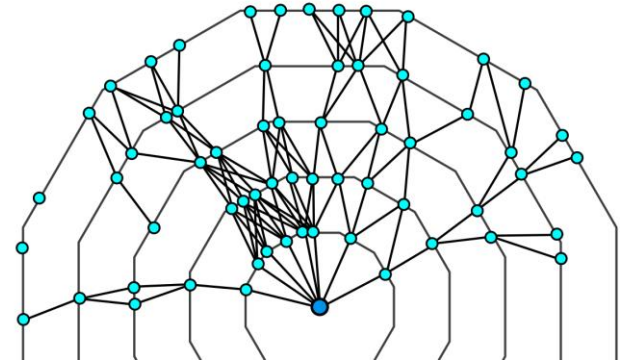




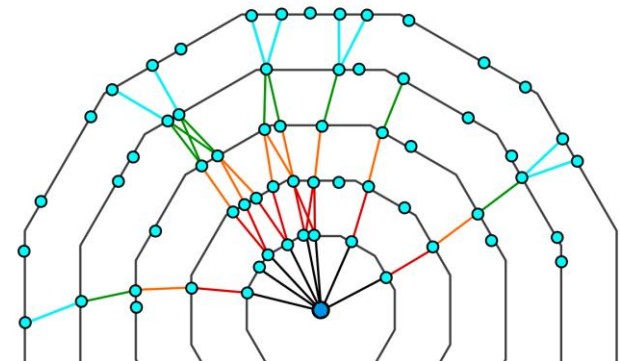
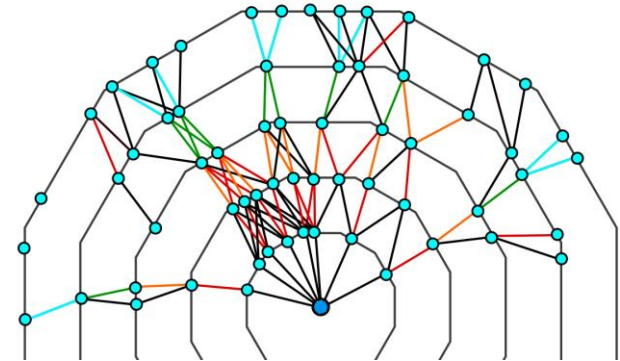
### ○ Cellular automaton

- Initialization
  - built any cell (= segment of 2 points)
- Iterative step
  - associate neighbour cells (more inner)
  - Raise “state” with associated cells
  - Kill lowest state cells

J. Lettenbichler *et al.*, 2013



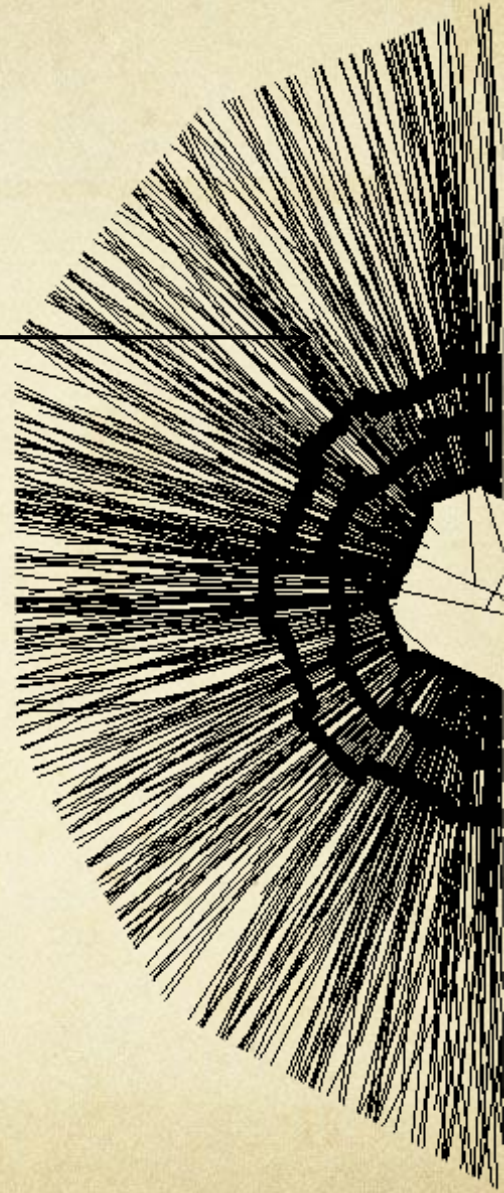
0 (black), 1 (red), 2 (orange), 3 (green), 4 (cyan)



# 5. Deconstructing some tracking systems

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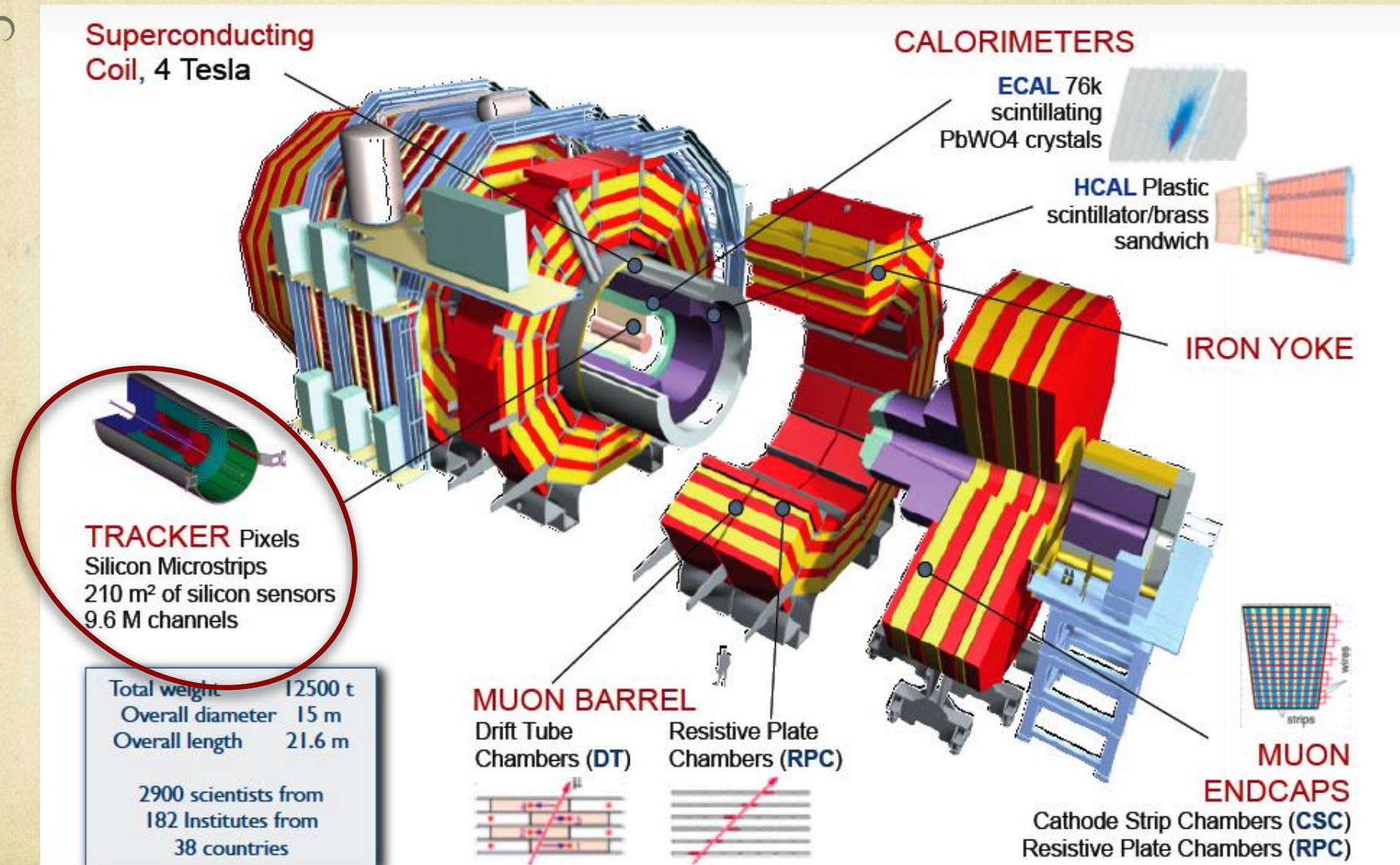
- CMS (colliders)
- AMS, ANTARES (telescopes)





## 5. Some tracking systems:

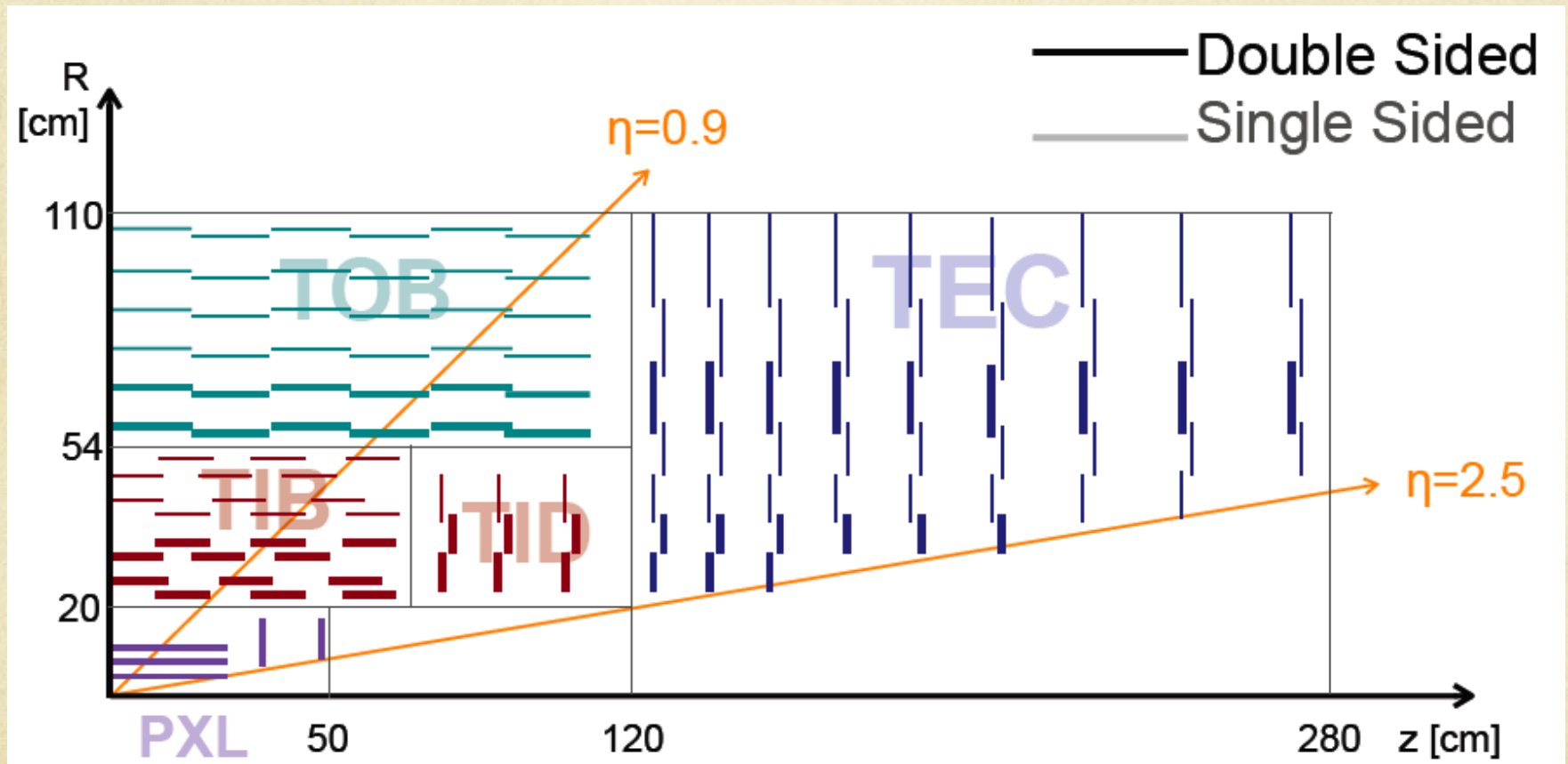
CMS



## 5. Some tracking systems:

CMS

### ○ The trackerS



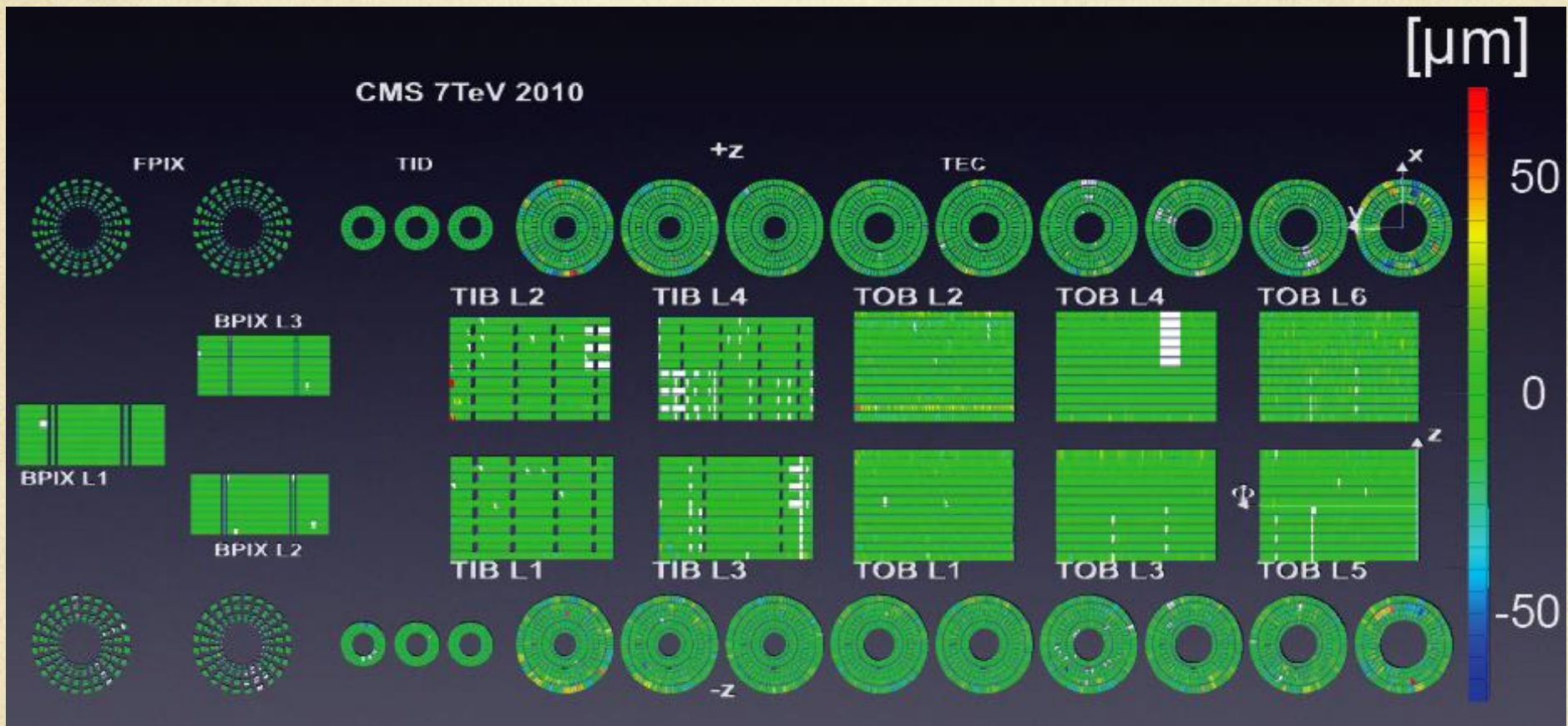


## 5. Some tracking systems:

CMS



### ○ Alignment residual width



## 5. Some tracking systems:

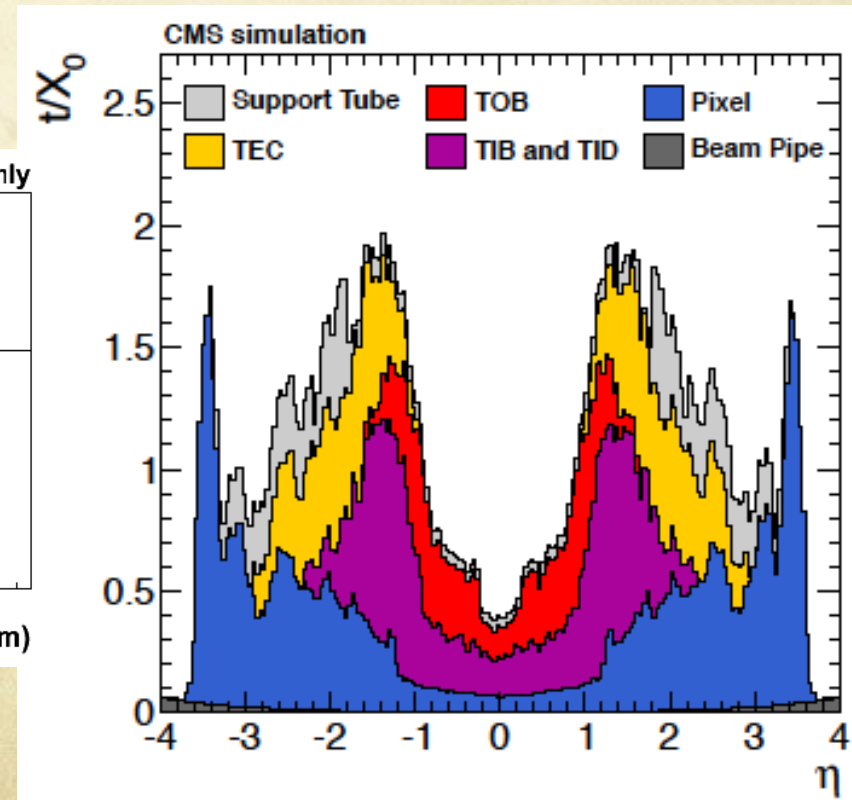
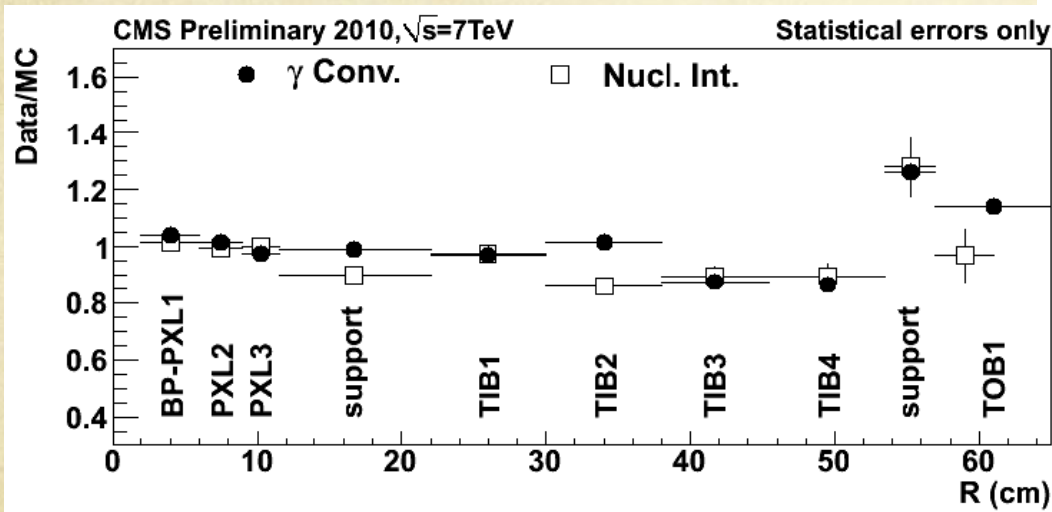
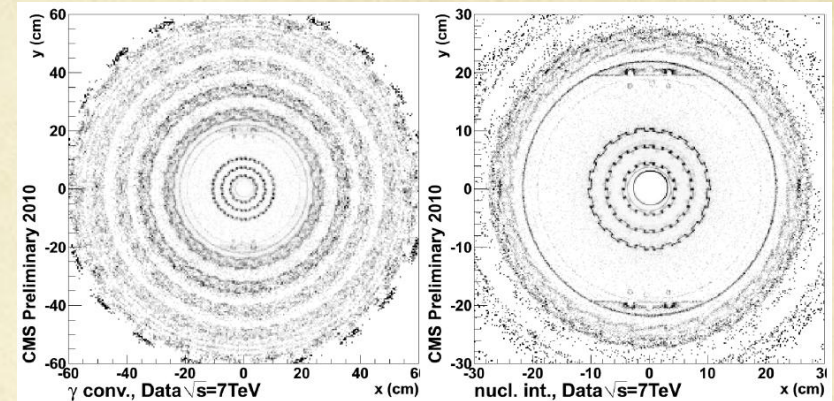
CMS



### ○ Taking a picture of the material budget

- Using secondary vertices from  $\gamma \rightarrow e^+e^-$

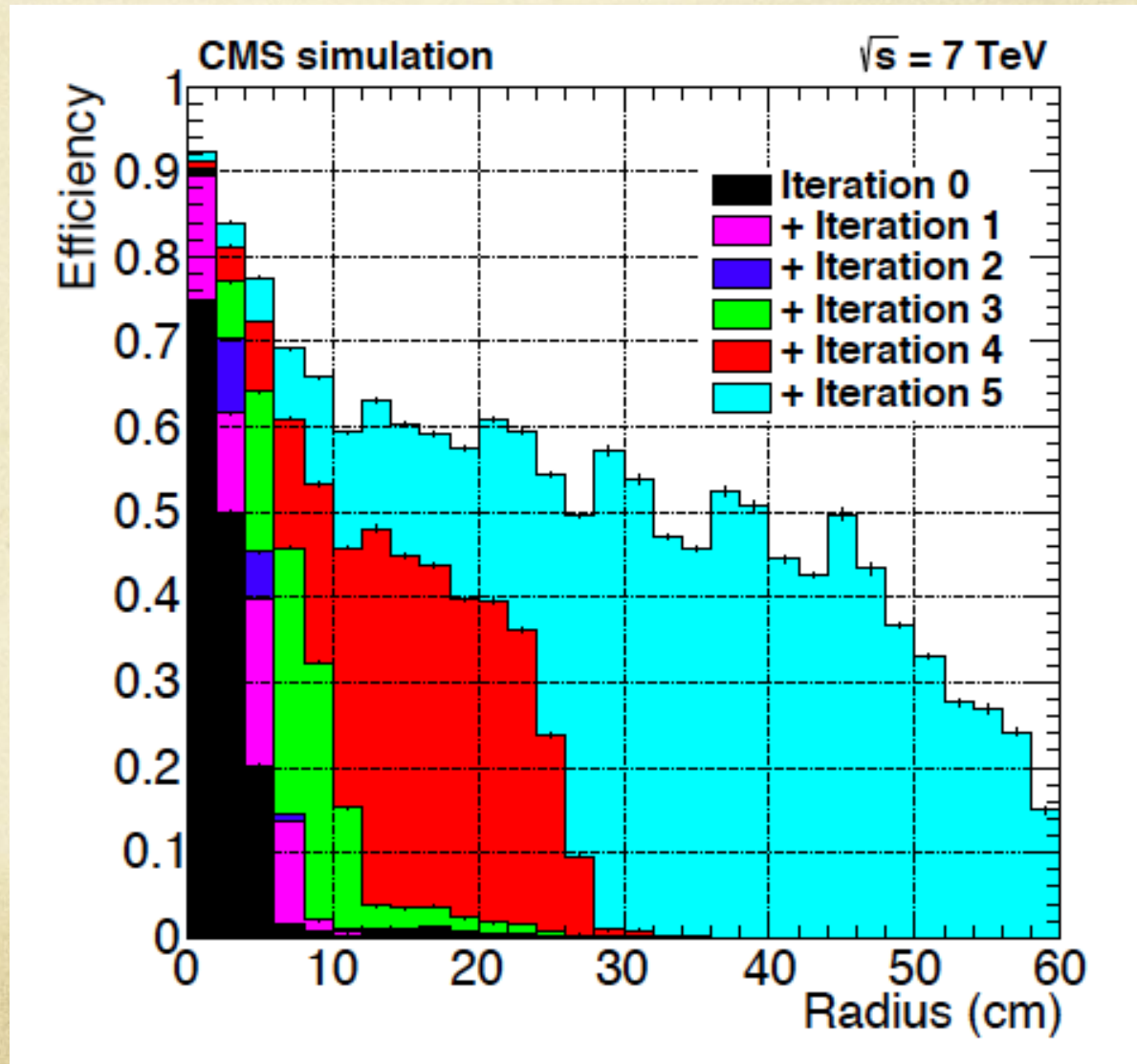
### ○ Measuring it by data/simulation comparison







- Tracking algorithm = multi-iteration process

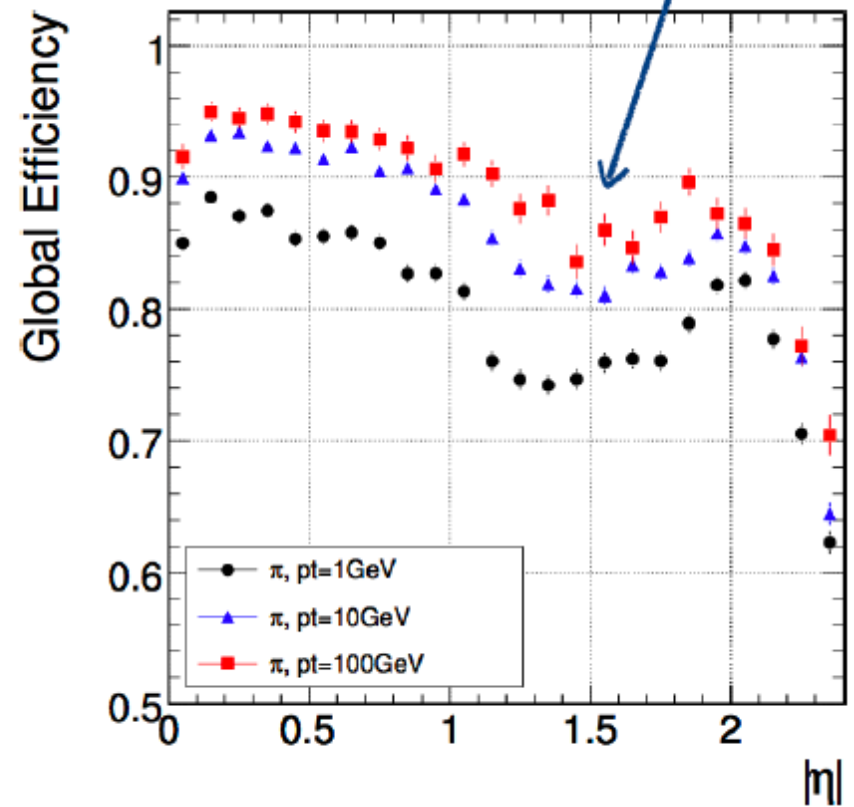
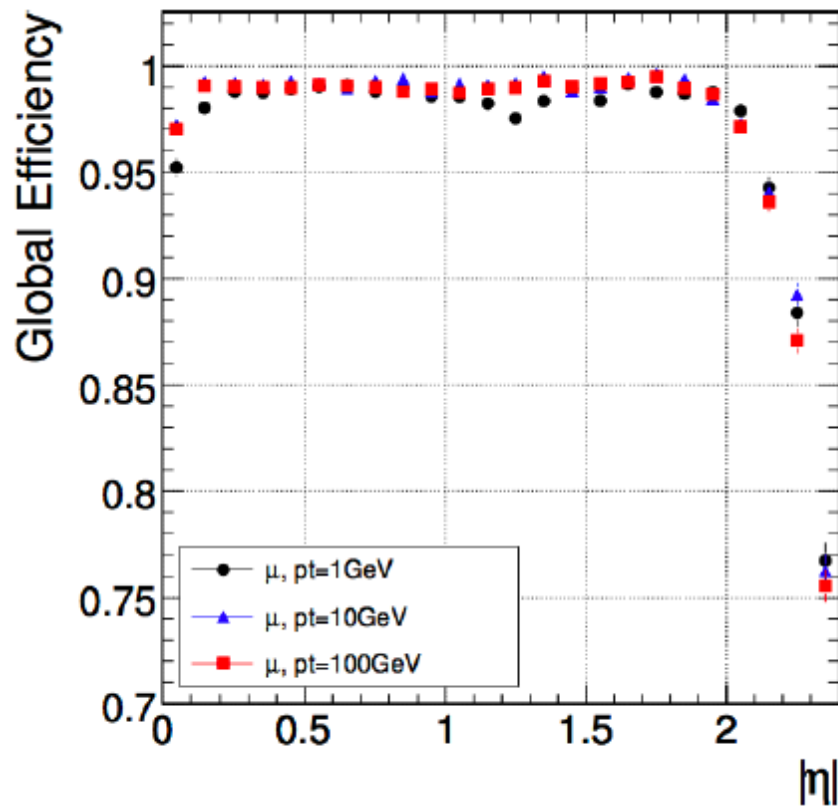


## 5. Some tracking systems:

CMS



### ○ Tracking efficiency

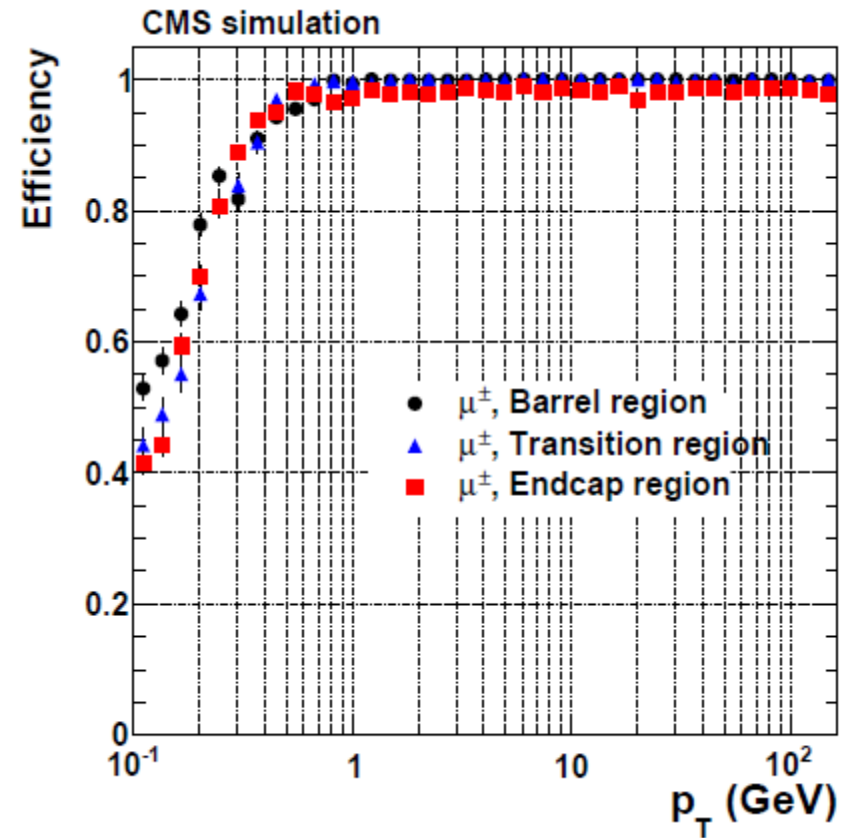
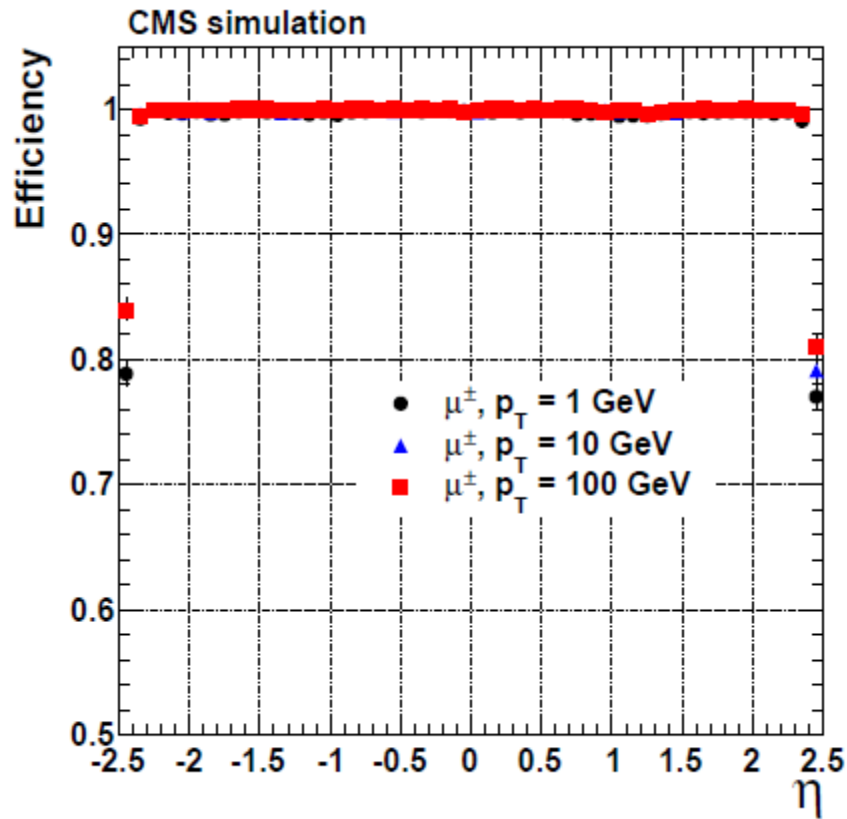






## ○ Tracking efficiency

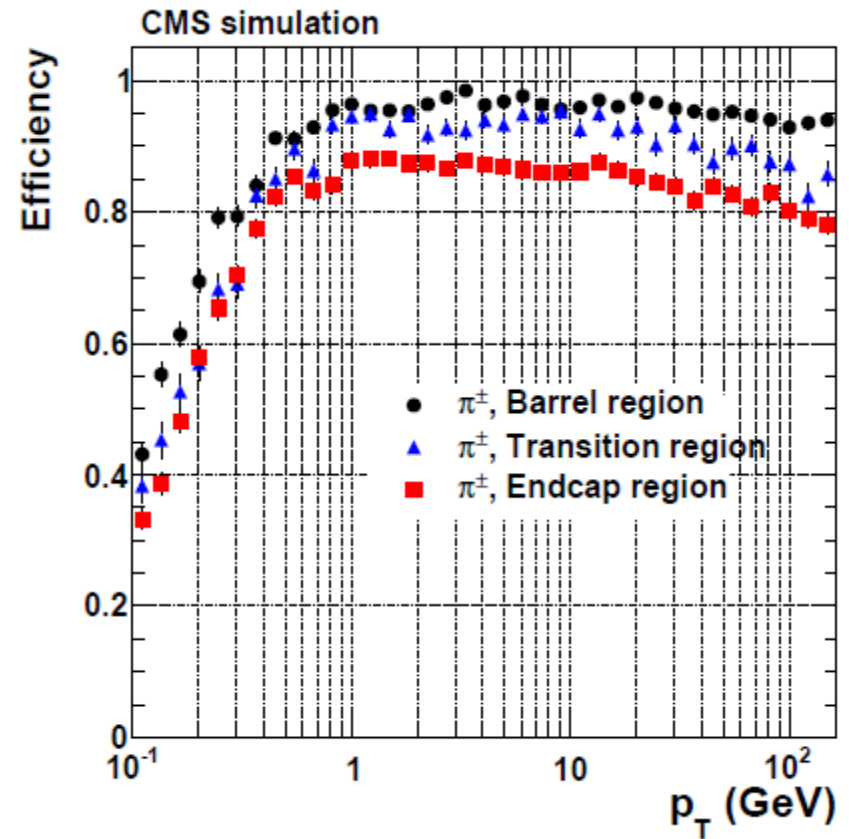
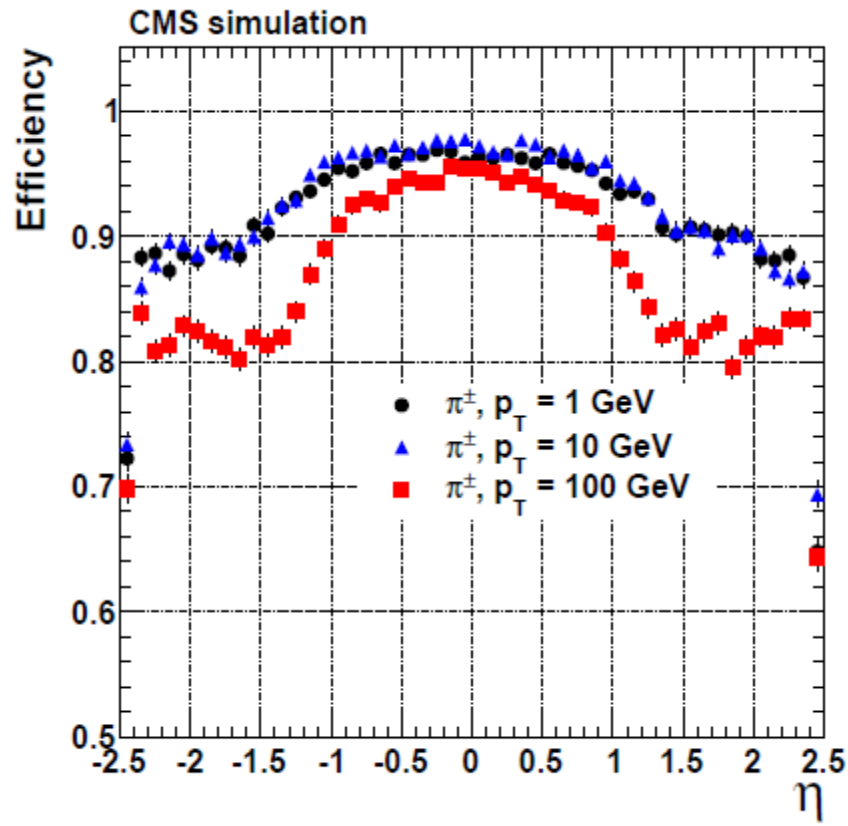
- Single, isolated muons





## ○ Tracking efficiency

→ All pions

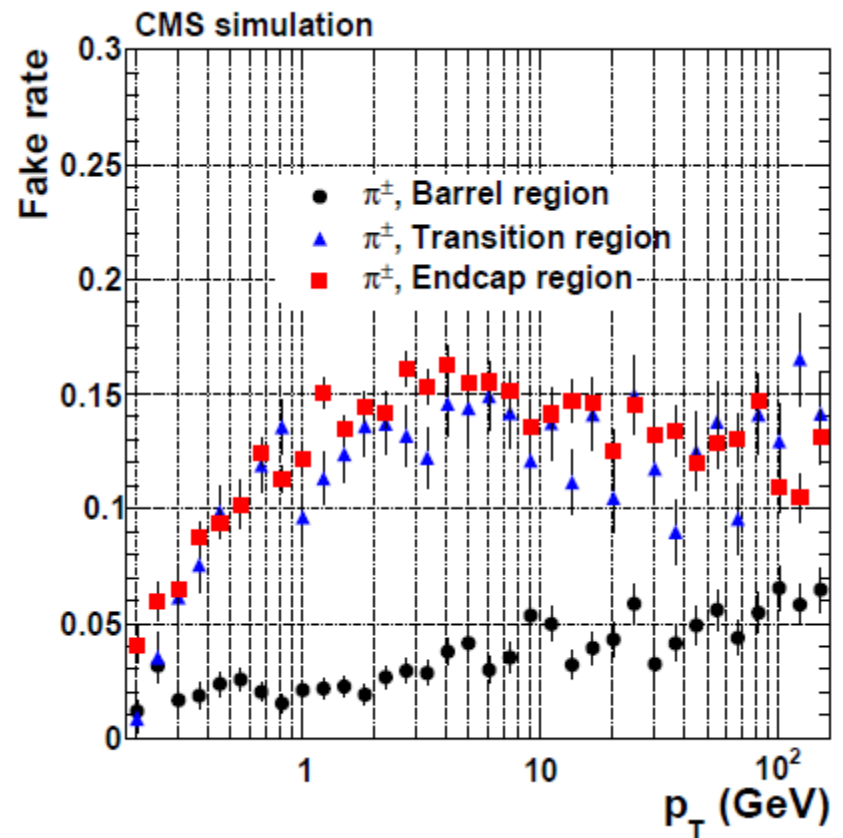
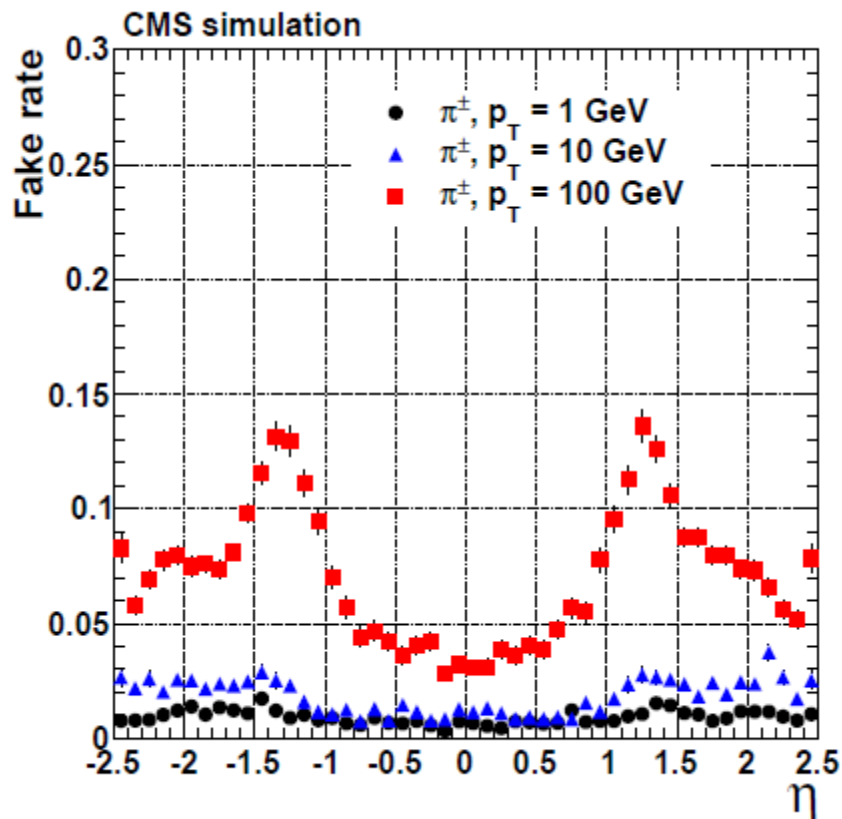






## ○ Tracking purity

→ All pions



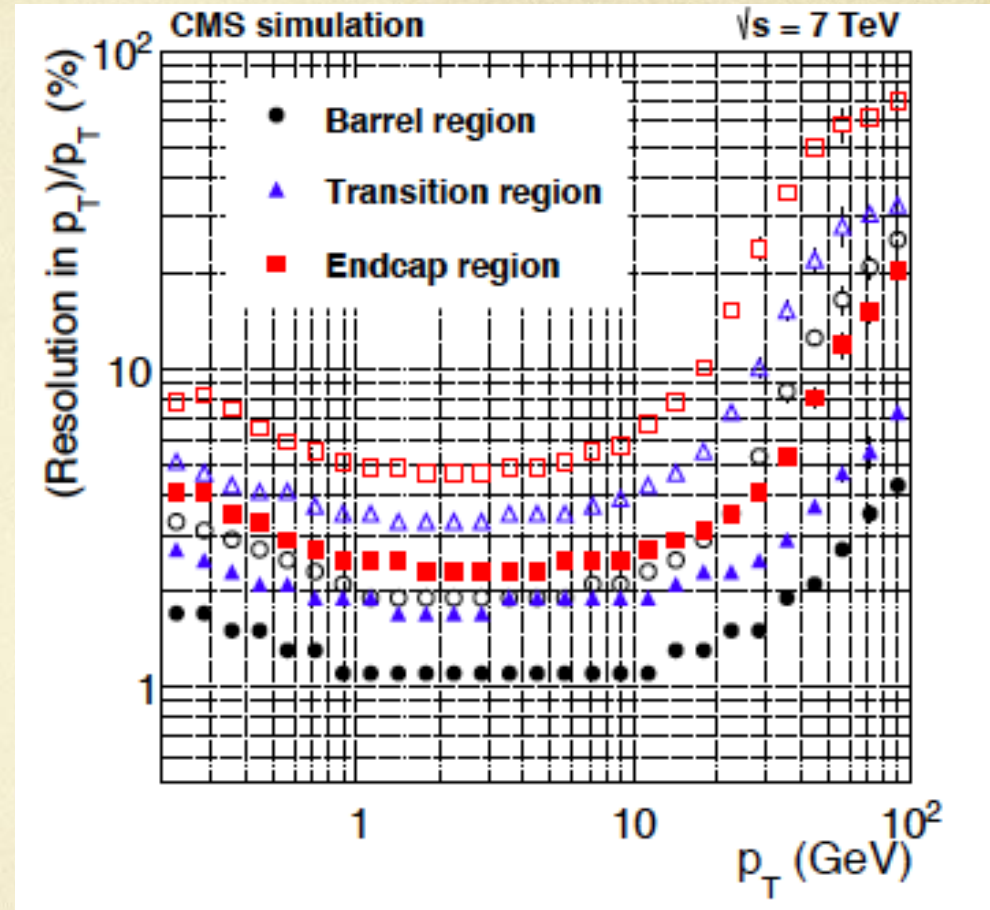
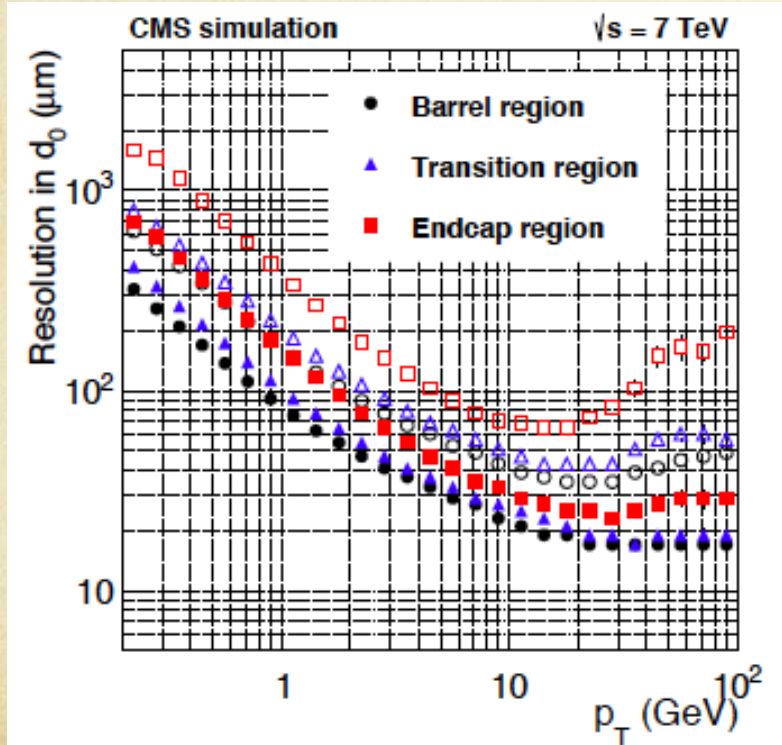
## 5. Some tracking systems:

CMS



### ○ Tracking resolution

$d_0$  = transverse impact parameter



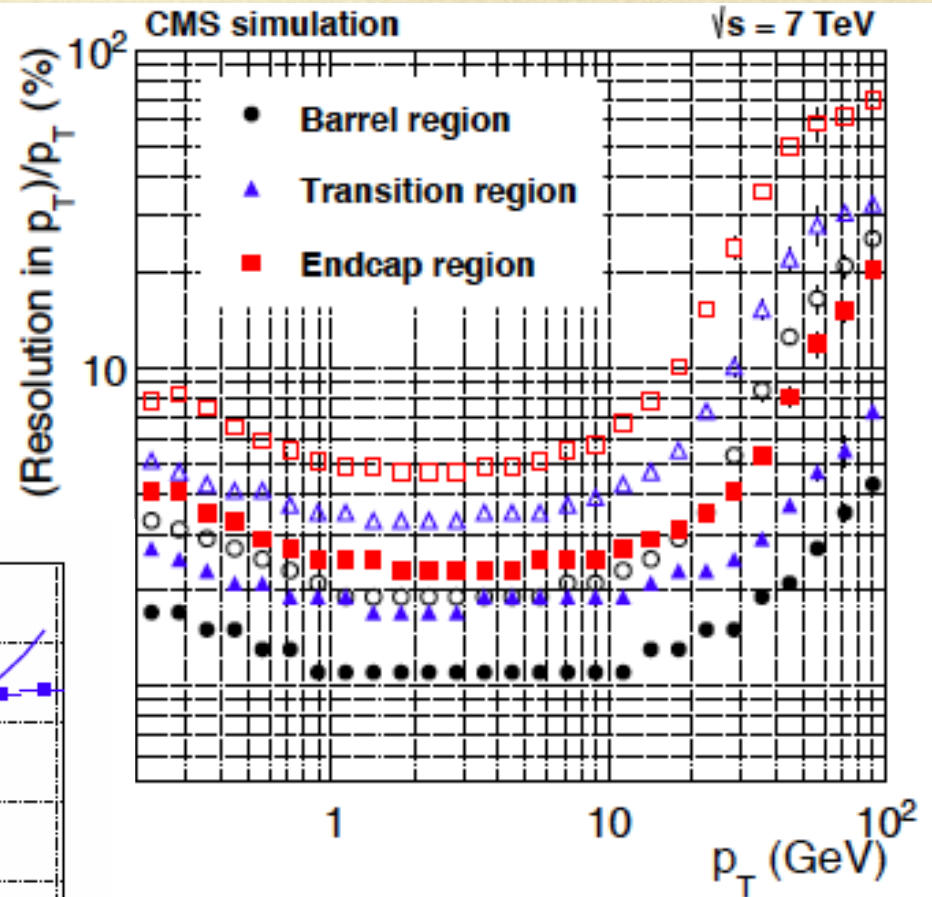
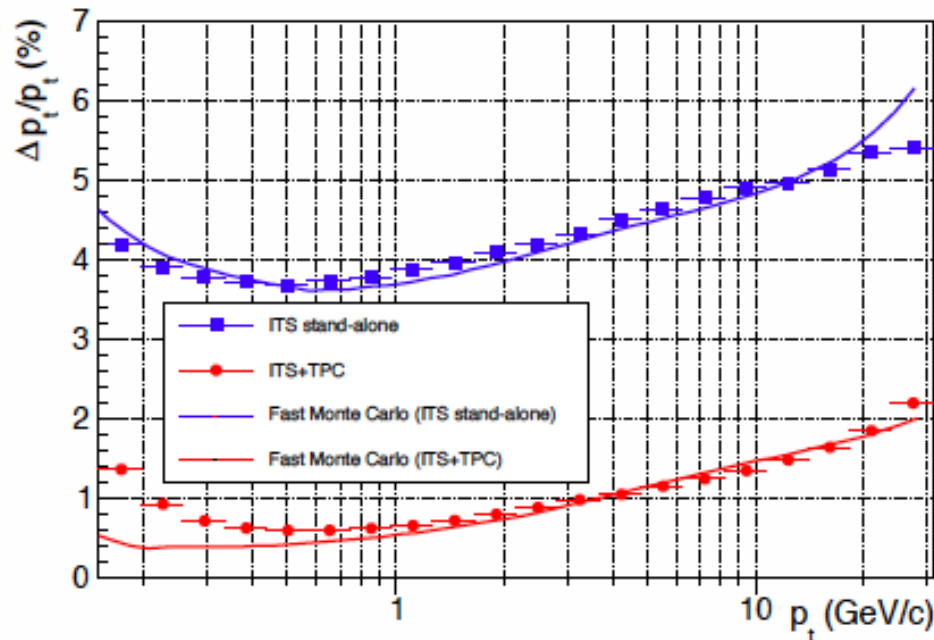


## 5. Some tracking systems:

CMS

### ○ Tracking resolution

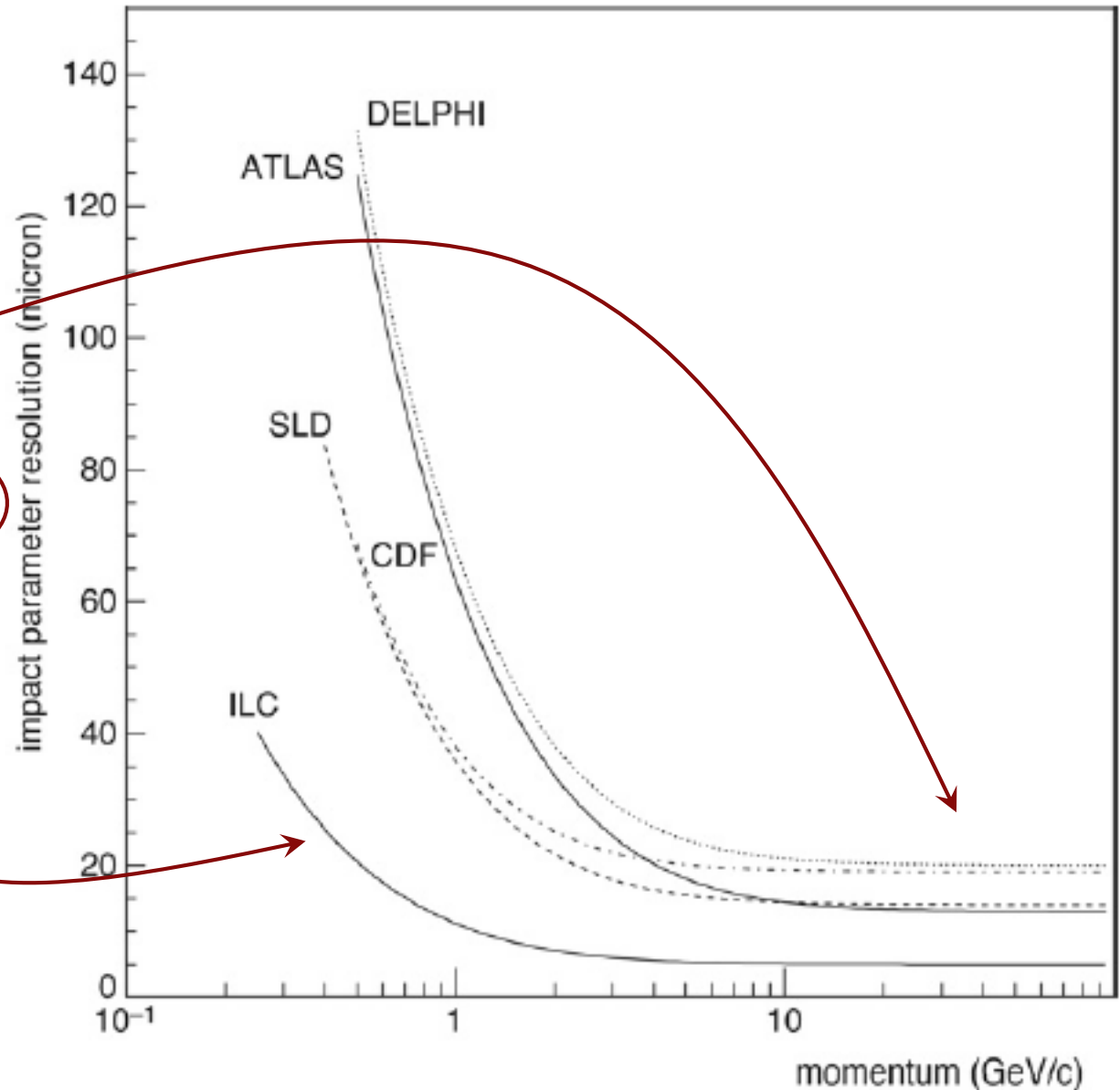
ALICE figure



## 5. Some tracking systems:

## Impact parameter resolution

$$\sigma_{IP} \propto \frac{\sqrt{R_{\text{ext}}^2 \sigma_{\text{int}}^2 + R_{\text{int}}^2 \sigma_{\text{ext}}^2}}{R_{\text{ext}} - R_{\text{int}}} \oplus \frac{R_{\text{int}} \sigma_{\vartheta(\text{ms})}}{p \sin^{3/2}(\theta)}$$







# AMS: A TeV precision, multipurpose particle physics spectrometer in space.

**TRD**  
Identify  $e^+$ ,  $e^-$



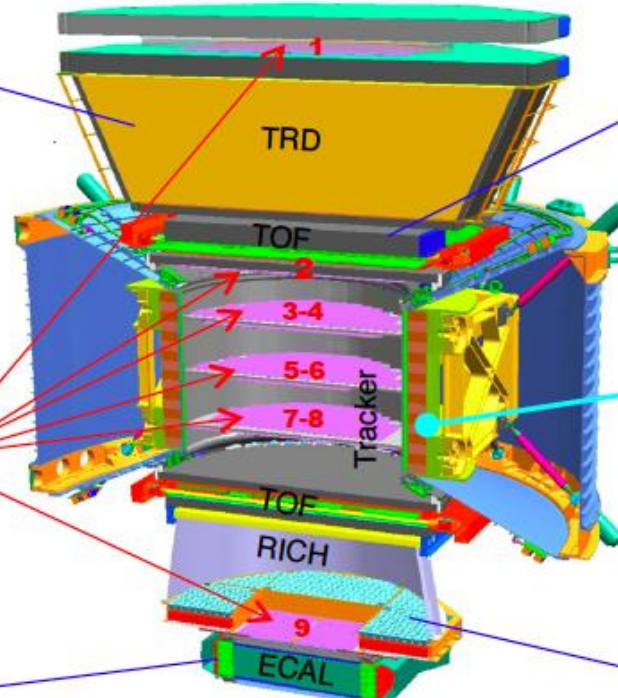
**Silicon Tracker**  
 $Z, P$



**ECAL**  
 $E$  of  $e^+$ ,  $e^-$ ,  $\gamma$



Particles and nuclei are defined by their charge ( $Z$ ) and energy ( $E \sim P$ )



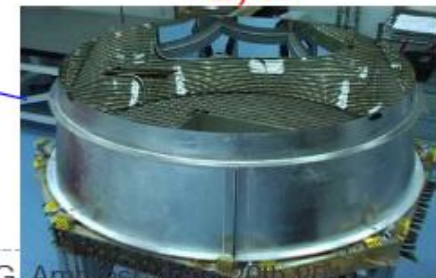
**TOF**  
 $Z, E$



**Magnet**  
 $\pm Z$



**RICH**  
 $Z, E$

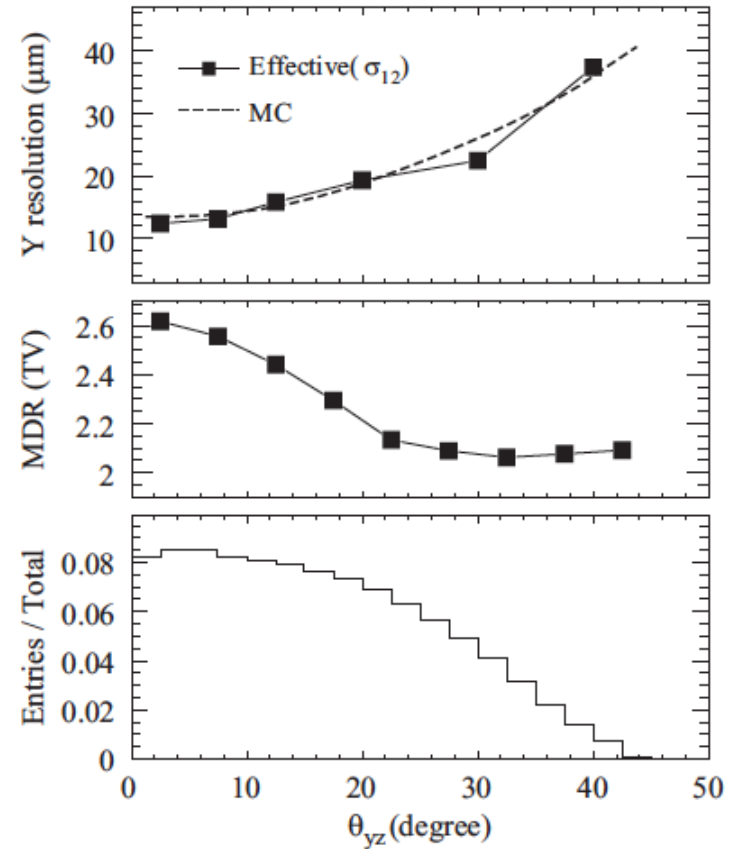
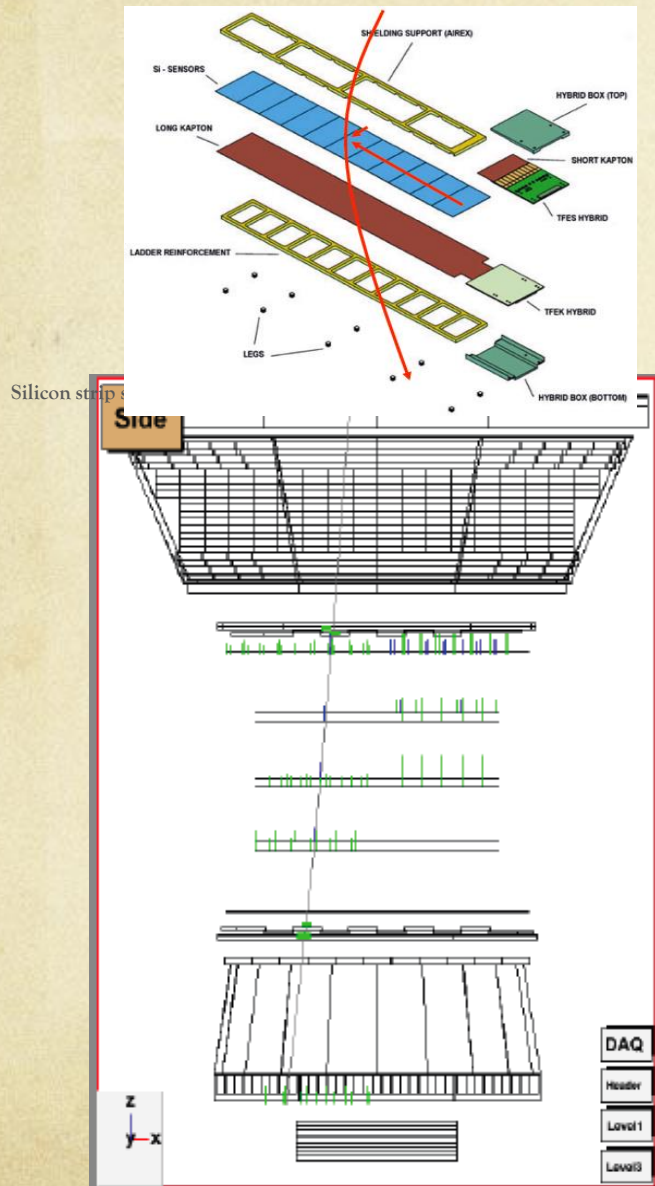


$Z, P$  are measured independently by the Tracker, RICH, TOF and ECAL

G. Ambrosi, June 20th 2011

## 5. Some tracking systems:

AMS

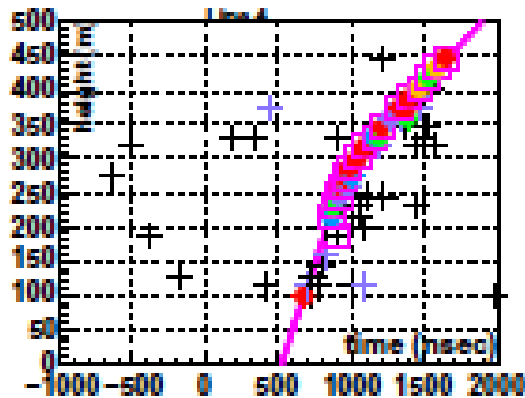
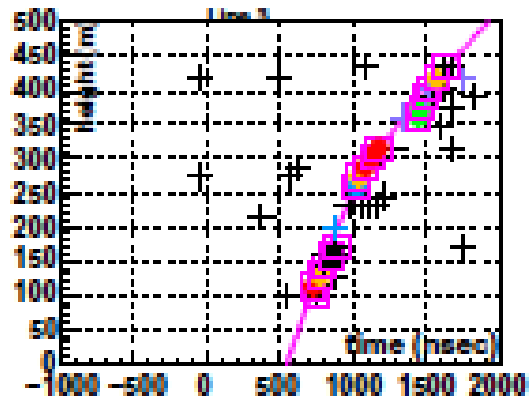
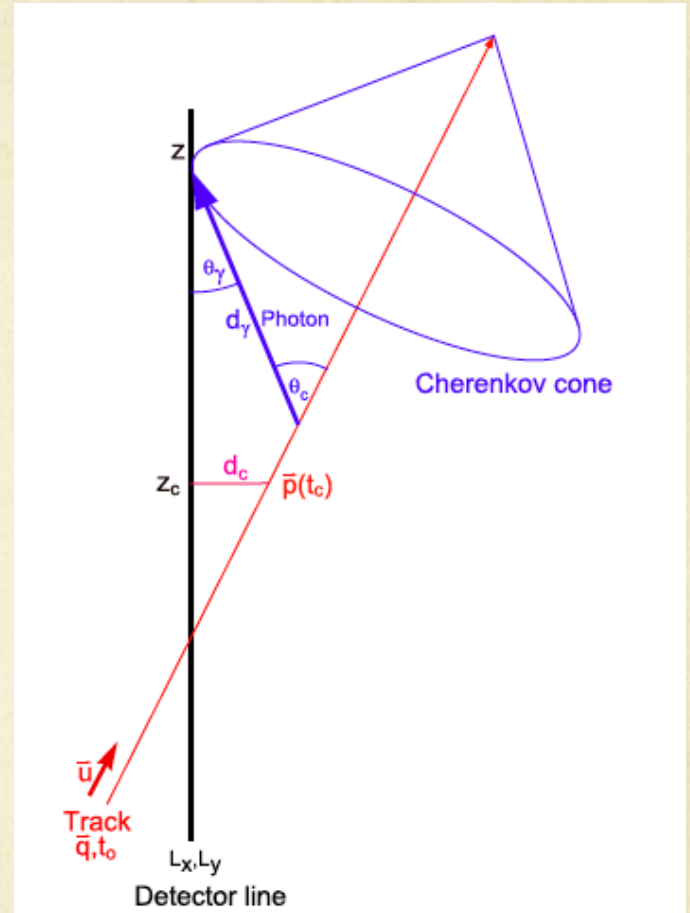
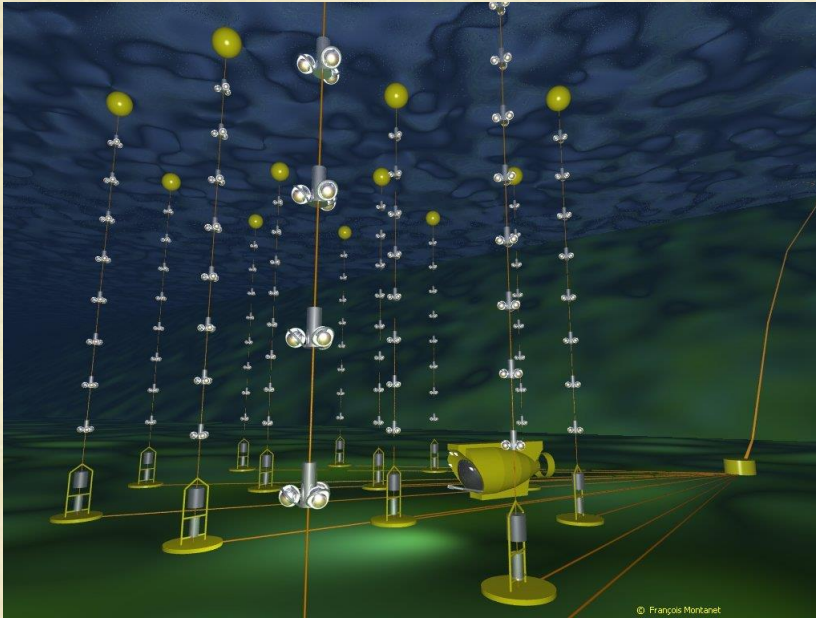


**Fig. 5.** The effective position resolution (weighted average of two Gaussian widths) in the y-coordinate for different inclination angles (top), the Maximum Detectable Rigidity (MDR, 100% rigidity measurement error) as a function of the inclination angle estimated for 1TV proton incidence with the simulation (middle), and the inclination angle distribution in the geometric acceptance of the tracker (bottom).



## 5. Some tracking systems:

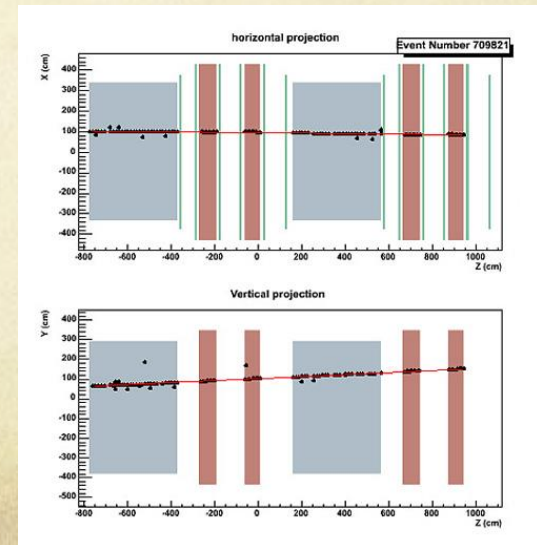
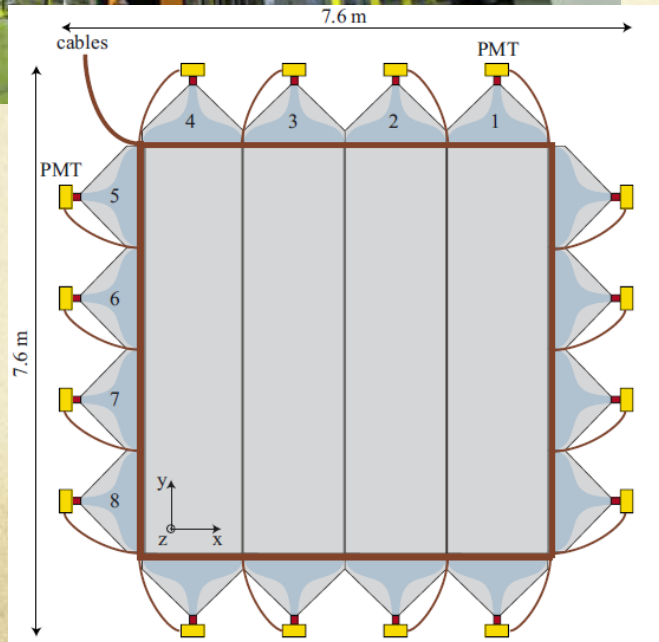
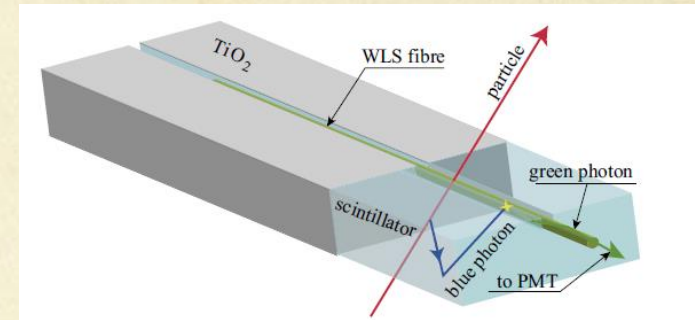
# ANTARES



## 5. Some tracking systems:

# OPERA

**Target Tracker** with scintillator strips:  
1 strip = 6.86m long,  
10.6mm thick, 26.3mm wide



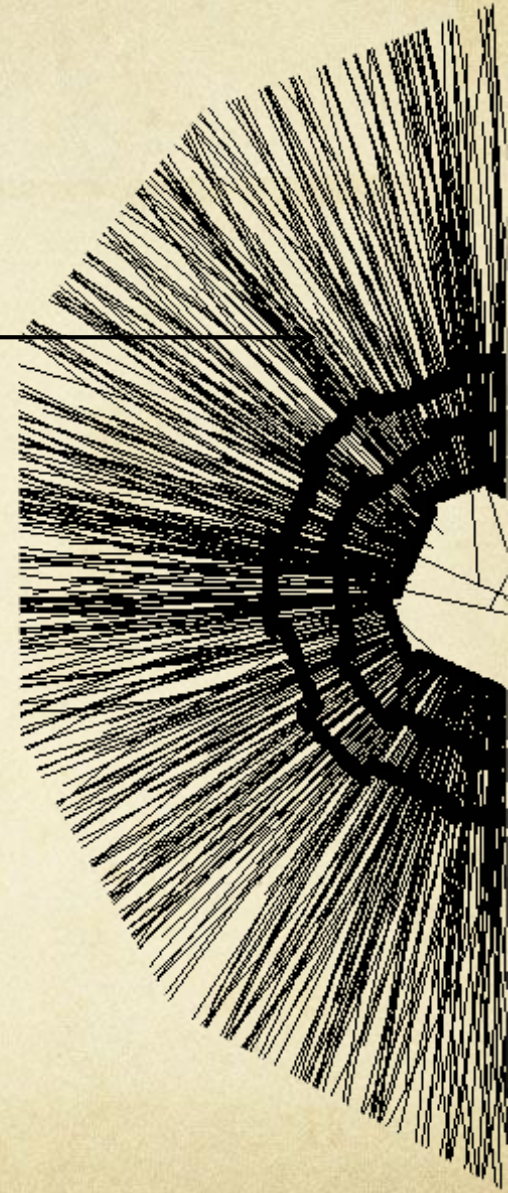


- **Fundamental characteristics of any tracking & vertexing device:**
  - (efficiency), granularity, material budget, power dissipation, “timing”, radiation tolerance
  - All those figures are intricated: each technology has its own limits
- **Many technologies available**
  - None is adapted to all projects (physics + environment choose, in principle)
  - Developments are ongoing for upgrades & future experiments
    - Goal is to extent limits of each techno. → convergence to a single one?
- **Reconstruction algorithms**
  - Enormous boost (variety and performances) in the last 10 years
  - Each tracking system has its optimal algorithm
- **Development trend**
  - Always higher hit rates call for more data reduction
  - Tracking info in trigger → high quality online tracking/vertexing
- **Link with:**
  - PID: obvious with TPC, TRD, topological reco.
  - Calorimetry: Particle flow algorithm, granular calo. using position sensors

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<http://pdg.web.cern.ch>, “Reviews, Tables, Plots” section
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**The Physics of Particle Detectors**  
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(some sections describing tracking)





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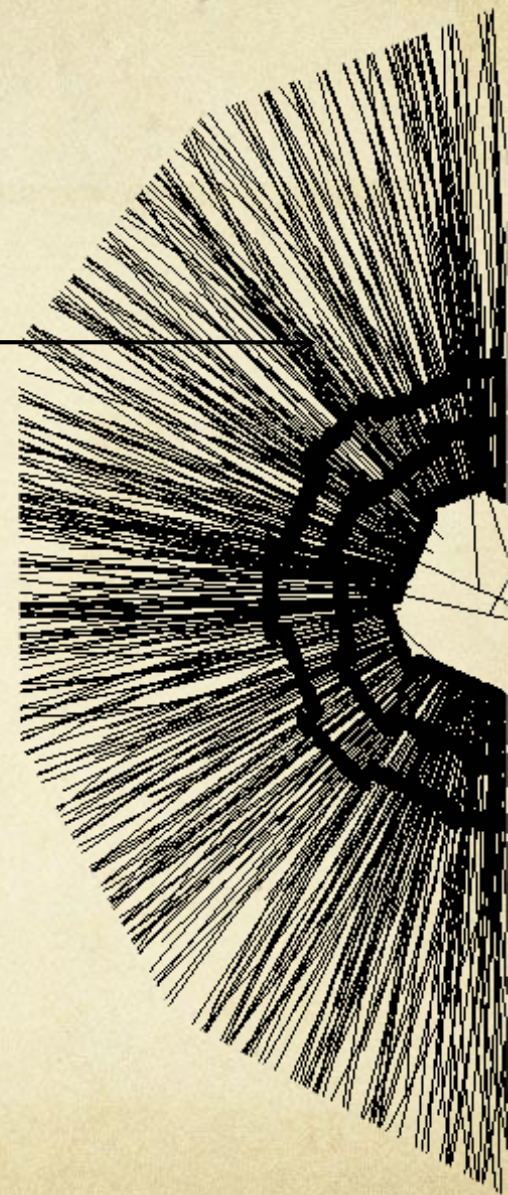
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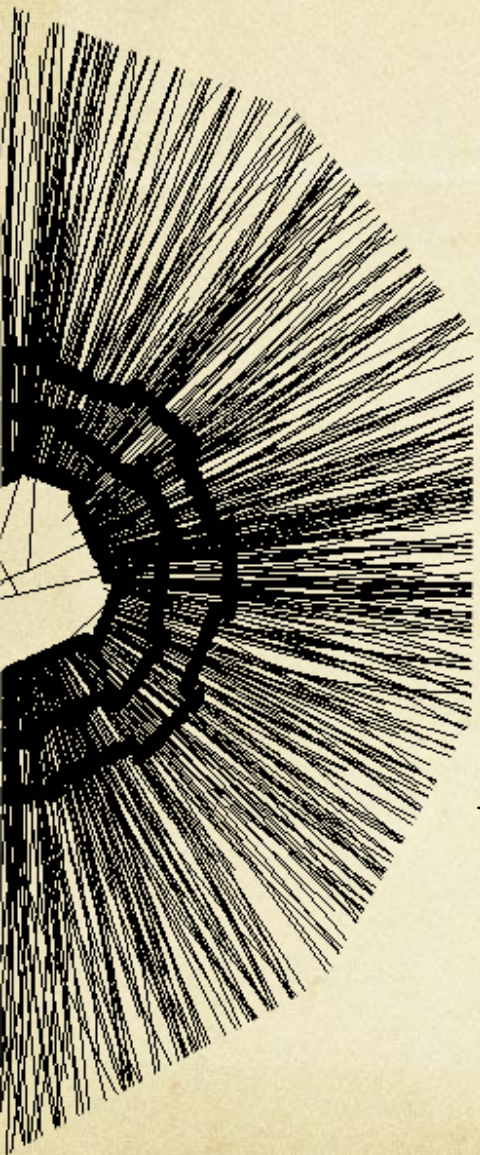
# Was not discussed

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- Particle interaction with matter
- The readout electronics
- Cooling systems
- Triggering
- Vertexing



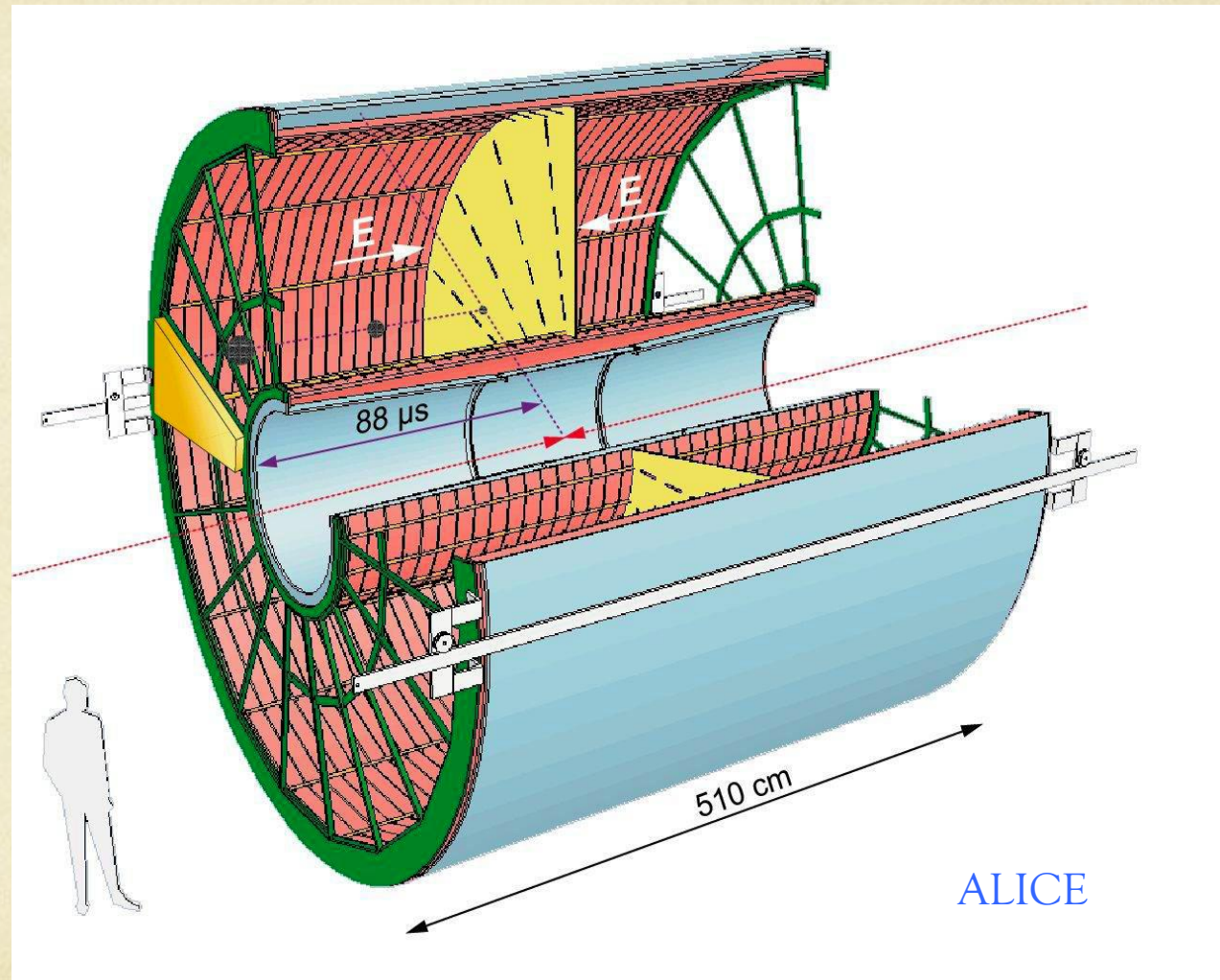




# Backups



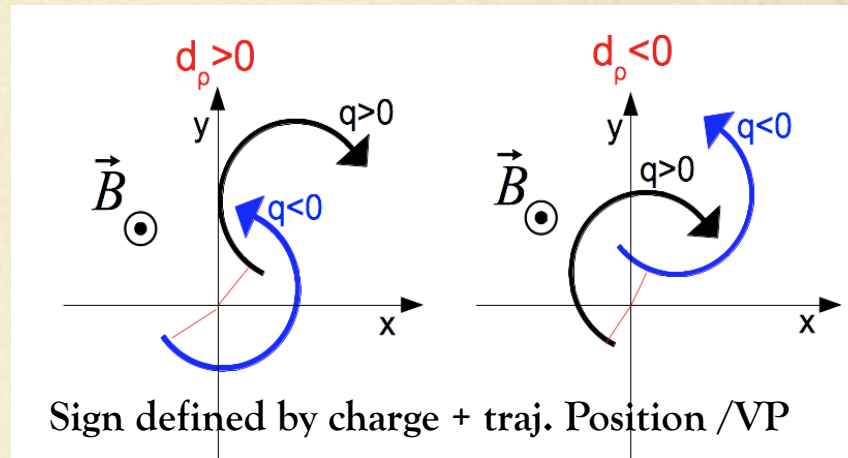




# Sign of Impact Parameter

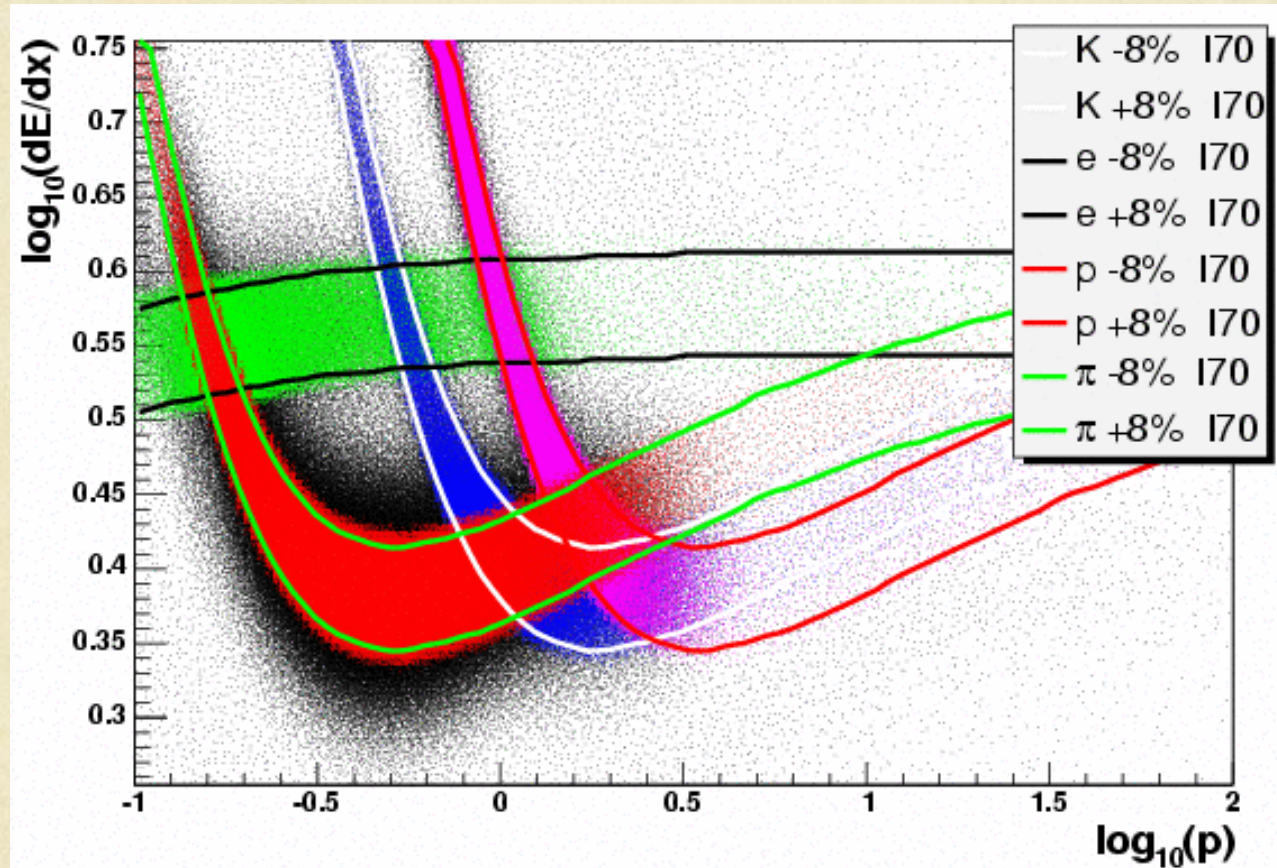
## ○ Geometrical sign

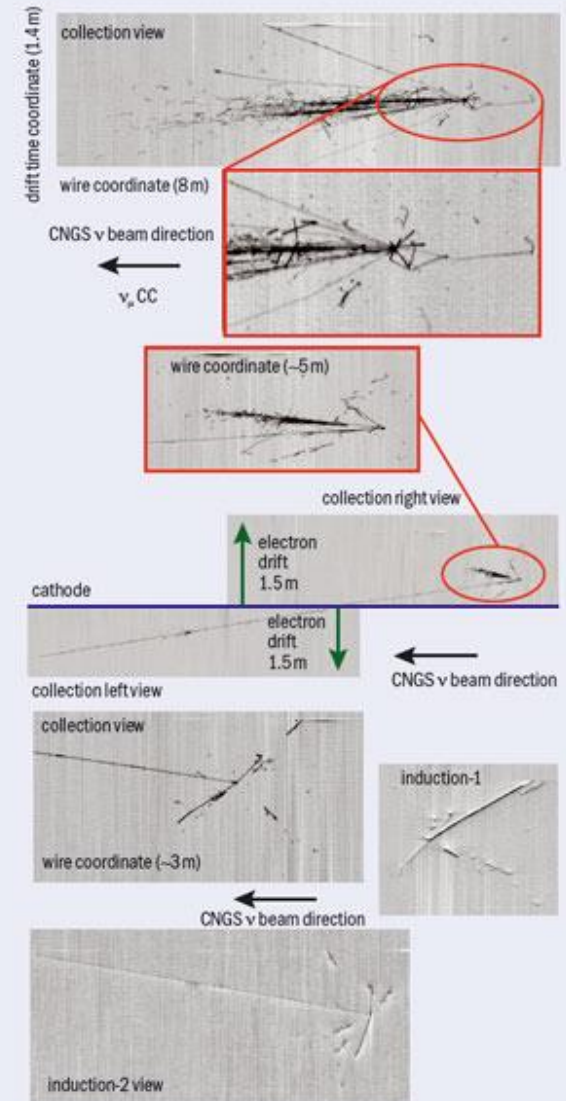
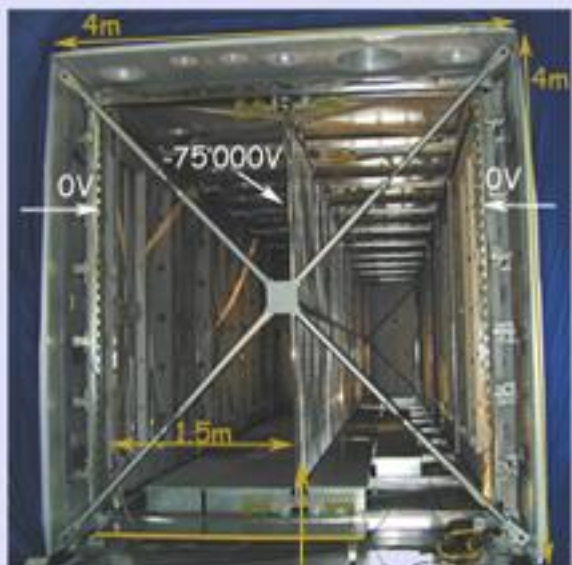
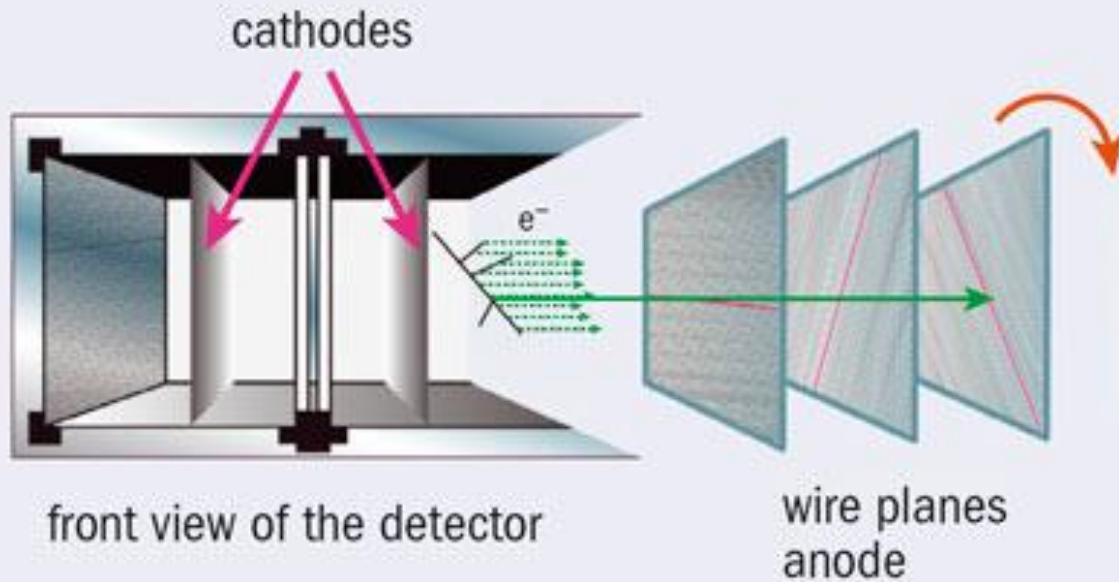
- Not helpful for b-tagging long-lived particles



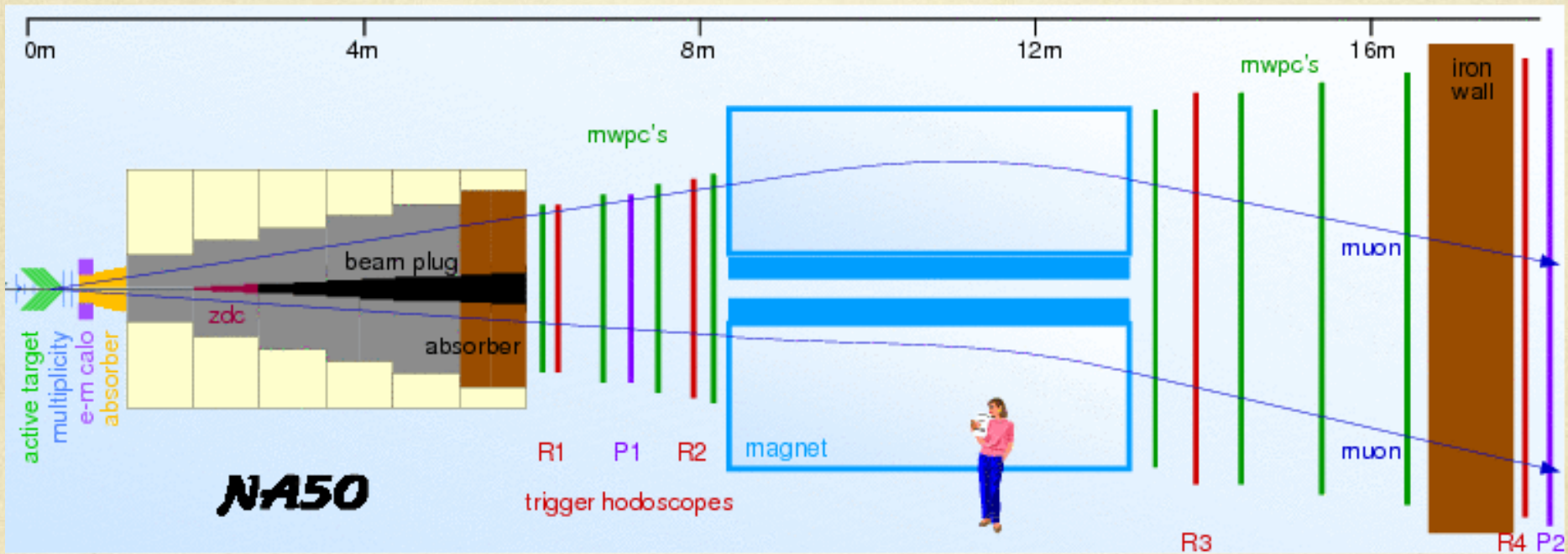


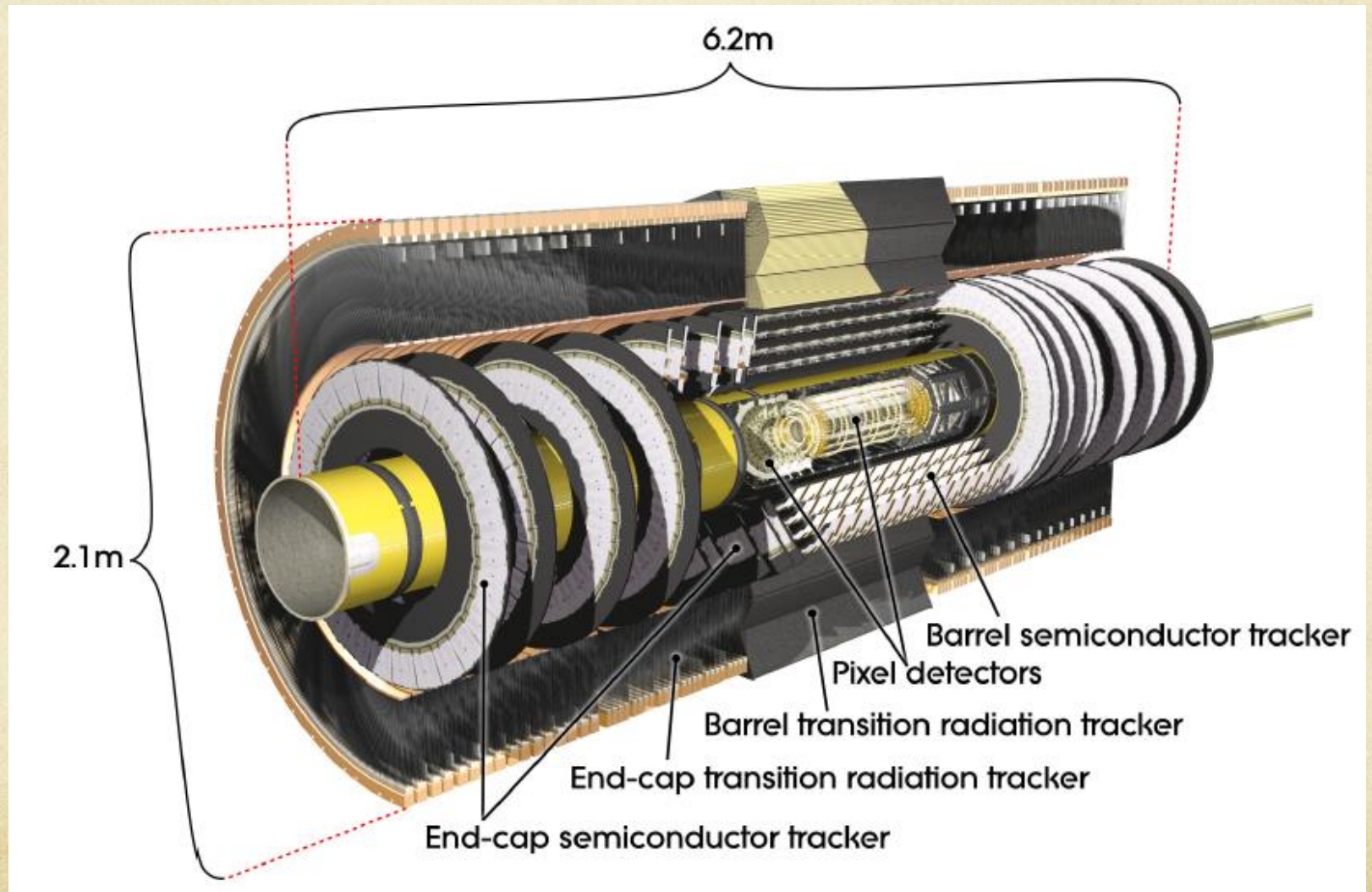
# (ALICE) TPC $dE/dx$



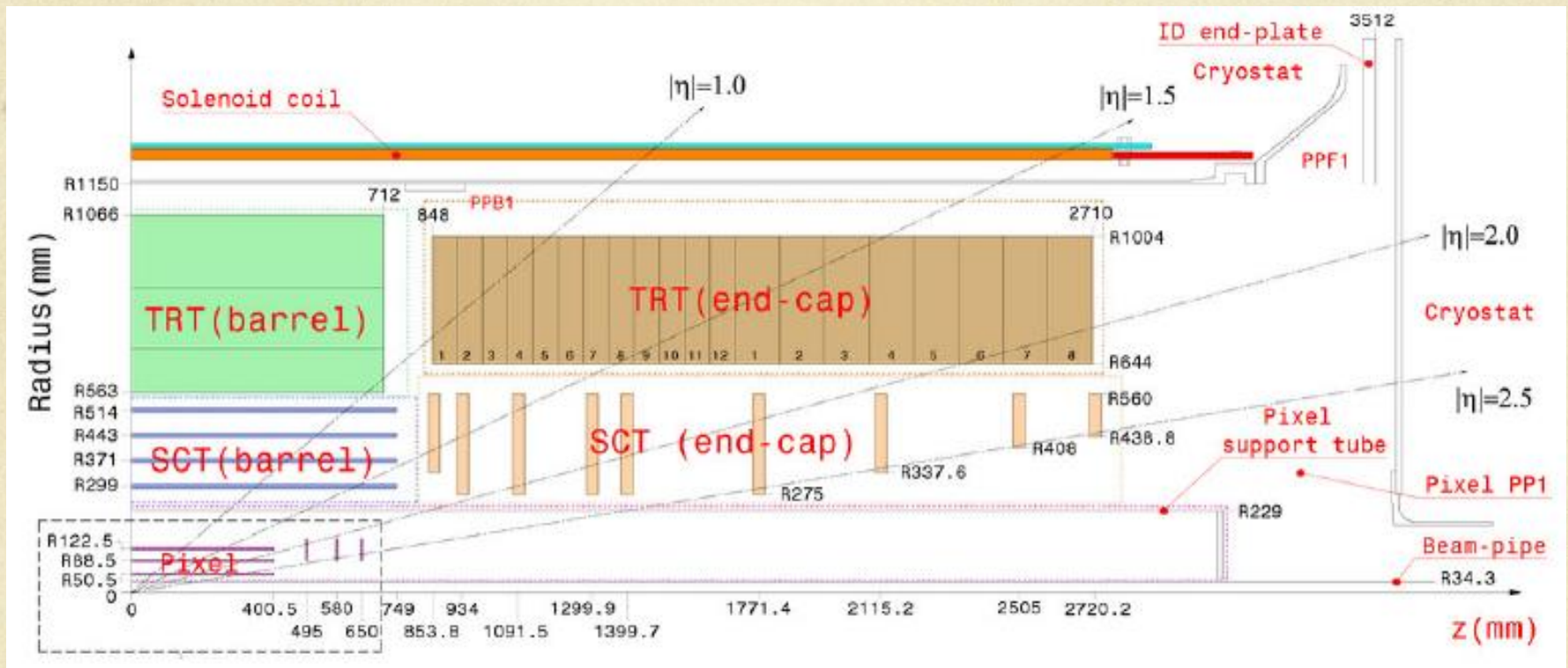


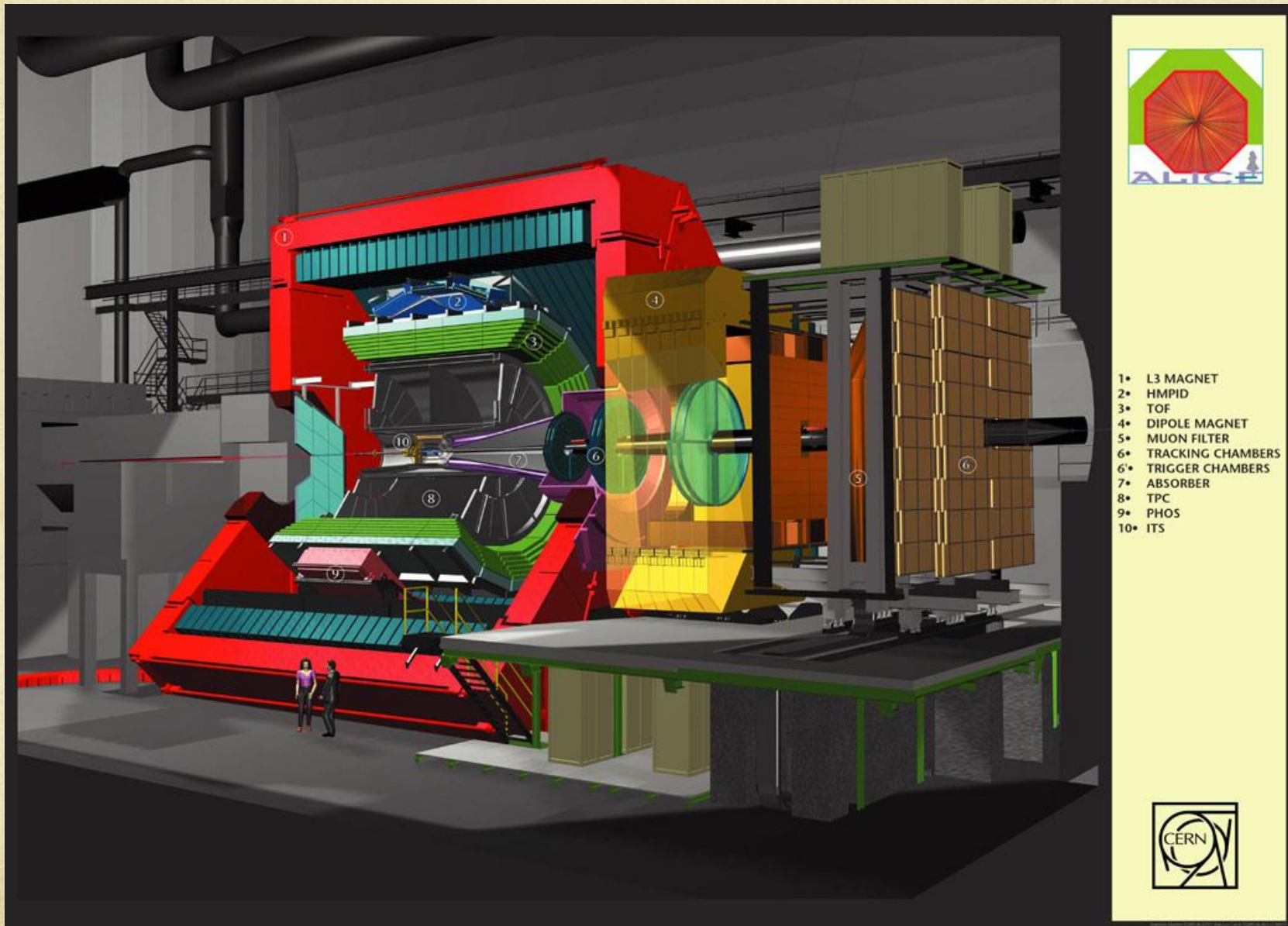




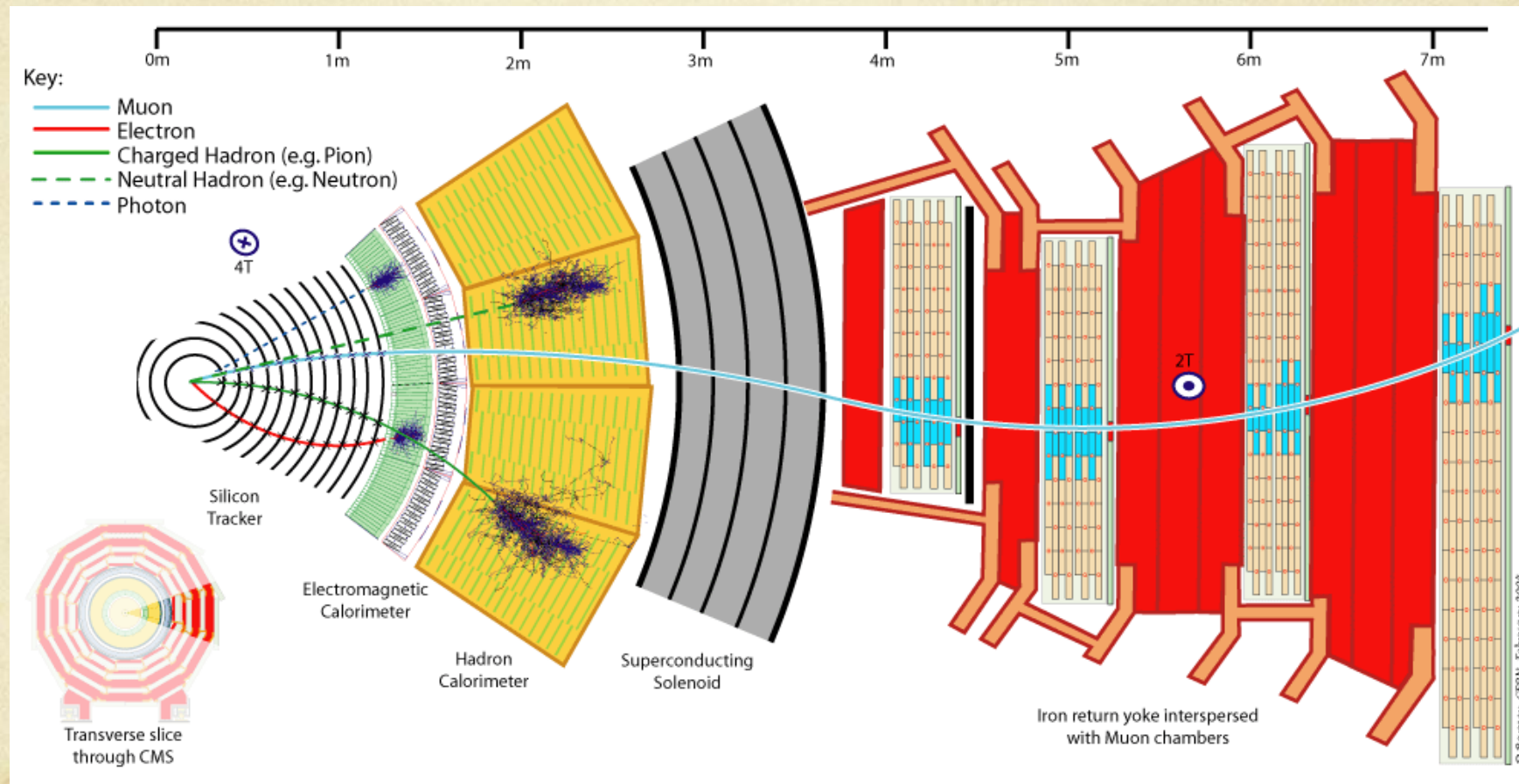




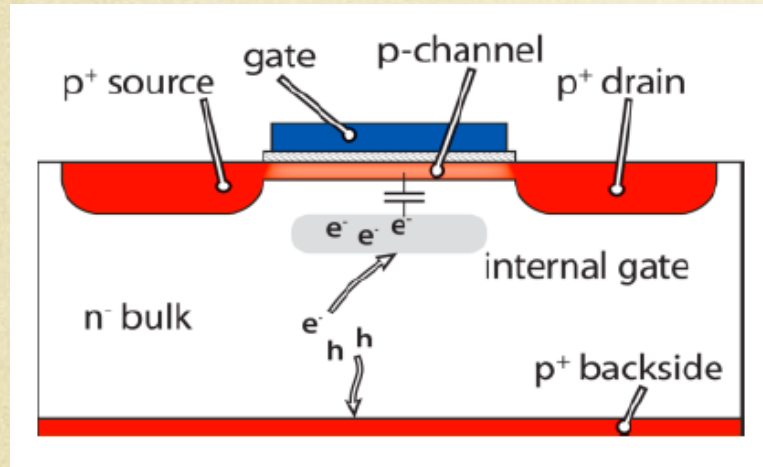




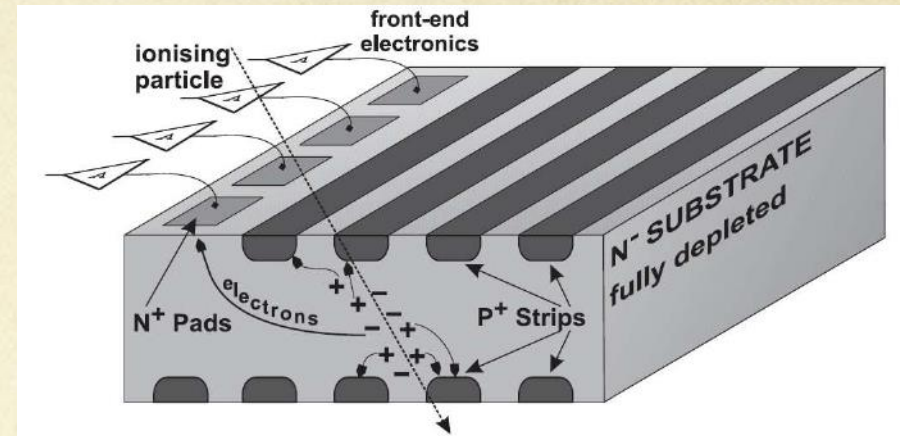




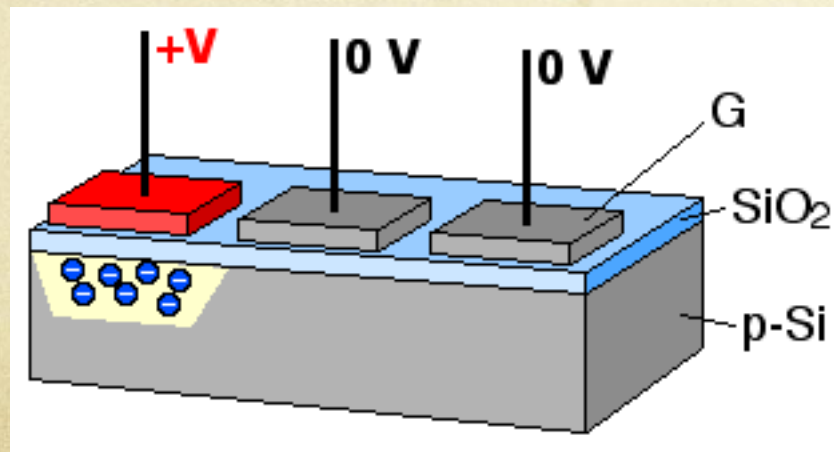
## DEPFET



## Silicon drift



## CCD



## MICROMEAS

