

# On the frequency dependence of the admittance of radiation damaged pad diodes

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## Questions:

- What is the cause of the frequency dependence of the capacitance of irradiated sensors?
- Is there a simple model for  $Y(f; V, \Phi_{eq}, T)$  [admittance  $Y = Z^{-1}$ ] ?

## Common answer:

- $C(f)$  is the result of the response time of radiation-induced states

## Our approach :

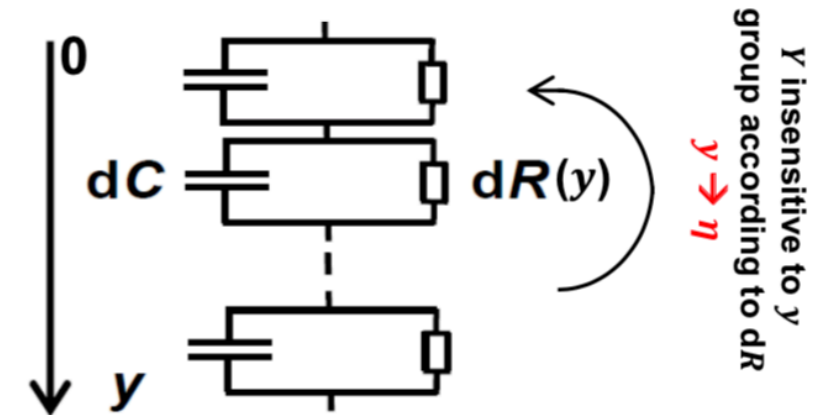
- Model fits to  $Y(f)$  data for irradiated pad diodes ( $\Phi_{eq} = 3$  to  $13 \times 10^{15} \text{ cm}^{-2}$ )

## Model:

- For interval  $dy$ :  $dC = \epsilon \cdot A/dy$  and  $dR(y) = \rho(y) \cdot dy/A$   
 $\Rightarrow dZ = (1/dR + i \cdot \omega \cdot dC)^{-1}$

- For entire sensor:

$$Z_{model} = \int_0^d dZ = \frac{1}{A} \int_0^d \frac{\rho(y) dy}{1 + i \cdot \omega \cdot \epsilon \cdot \rho(y)} = (Y_{model})^{-1}$$



## Assumption for $Y_{model}$ :

- Rad. damage affects only the resistivity  $\rho(y)$  — no effects of response time to traps!

## Expectation: for highly irradiated sensor

- In **non-depleted** (ohmic) region:  $\rho = \rho_{intr}$  (generation = recombination)
- In **depleted** (high-field) region:  $\rho \gg \rho_{intr}$  (free charge carrier density due to generation + current)

## Analysis: For every voltage and $\Phi_{eq}$ : $\chi^2$ -fit of $C_p(f) = \text{Im}(Y/\omega)$ and $\varphi(f) = \text{atan}(\text{Im}(Y/\omega)/\text{Re}(Y/\omega))$

use a 3-parameter ad-hoc parametrisation:  $\rho(\eta, V) = \rho_0(V) + \rho_1(V) \cdot e^{-\eta/\lambda(V)}$

4 different  $\rho$  parametrisations used for fits  $\rightarrow$  similar results for  $\rho(\eta)$

## Large diodes from CMS HPK campaign:

### 1. Material

- **p-type** (p-stop, p-spray)
  - Thinned **float zone FTH200** (200  $\mu\text{m}$  thick)

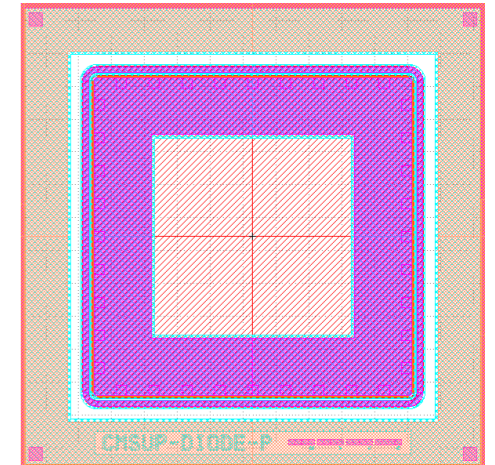
### 2. Irradiations

- **24 GeV/c**
  - $\Phi_{\text{eq}} = 3, 6, 7.75, 13 \cdot 10^{15} \text{ cm}^{-2}$
  - Annealing for **80min@60°C**

### 3. Measurements

- Reverse voltage: 0  $\rightarrow$  1000 V, **T= -20°C** and **-30°C**, 16 frequencies 100 Hz  $\rightarrow$  2 MHz (125 x 16 measurements per T and  $\Phi_{\text{eq}}$ )
- Forward voltage: 0  $\rightarrow$  up to voltage for which current is 0.5 mA, **T= -20°C** and **-30°C** 16 frequencies 100 Hz  $\rightarrow$  2 MHz
- n<sup>+</sup>-contact and guard ring grounded
- In addition  $I_{\text{pad}}$  and  $I_{\text{guard}}$  measured separately

Diode 5mm x 5mm

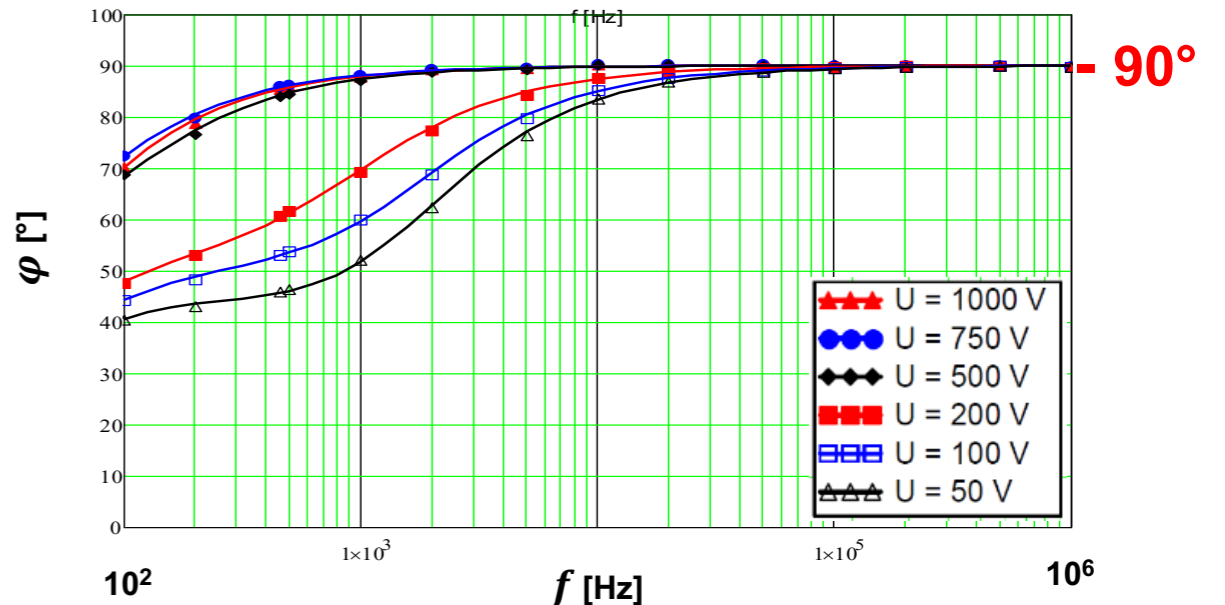
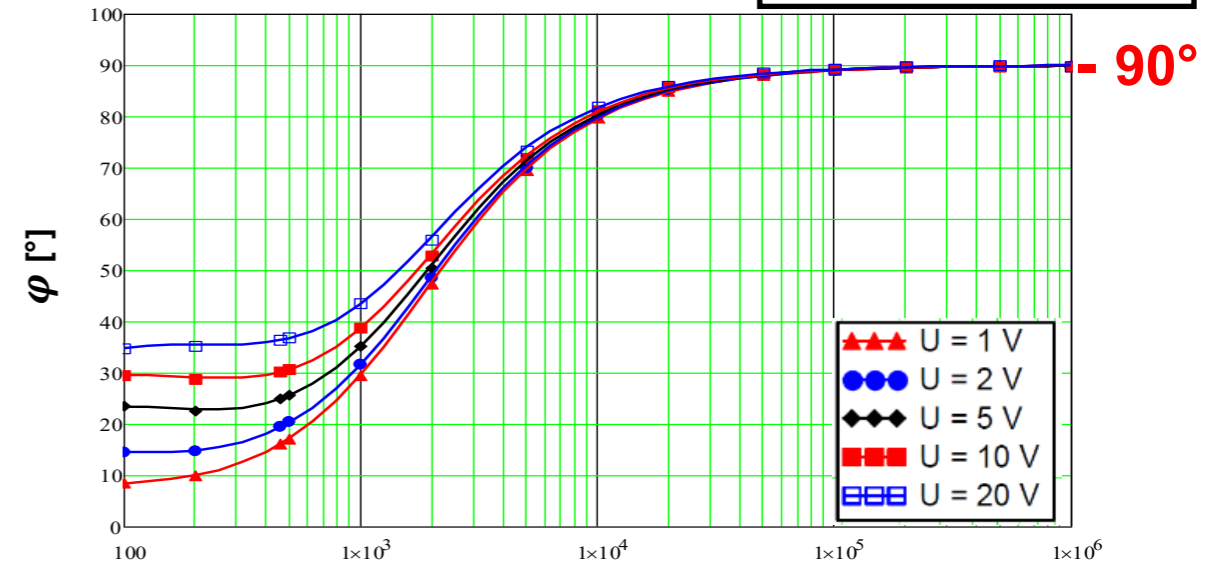
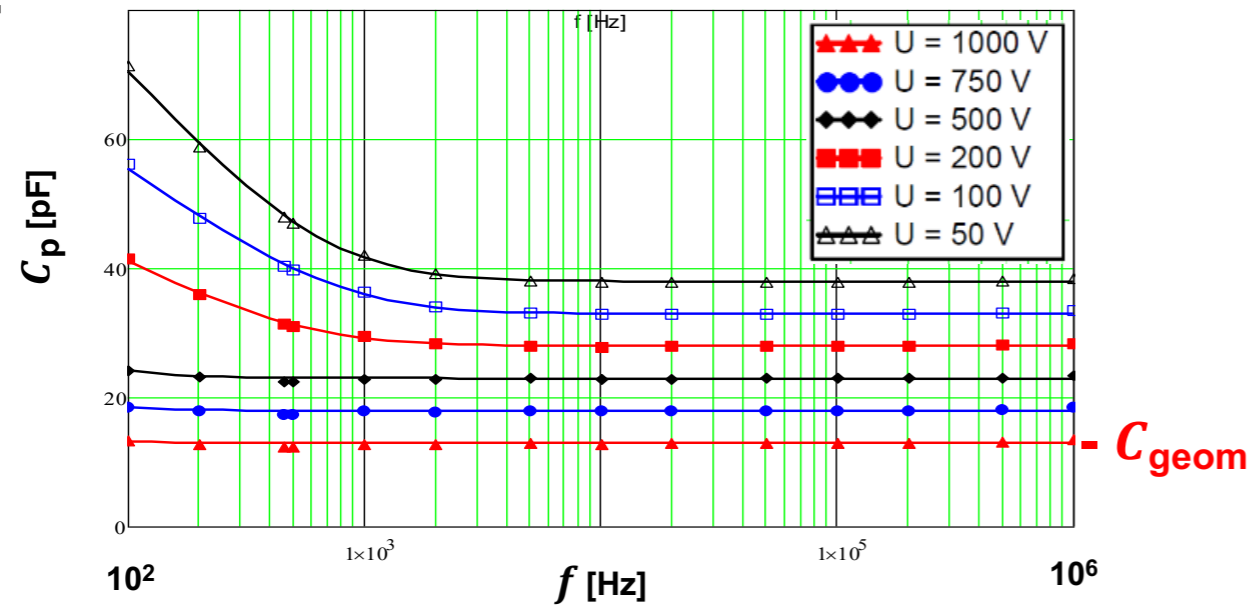
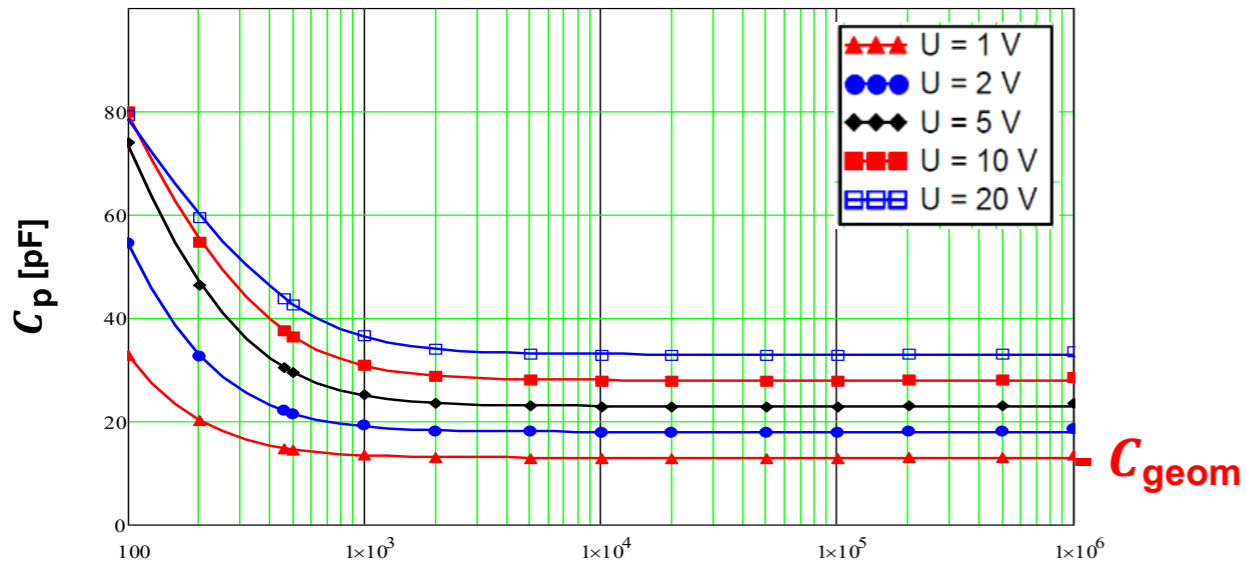


# QUALITY OF Y-F FITS

Fit of  $Y(f)$  for every  $V$  and  $\Phi_{eq}$ :  $\Phi_{eq} = 3 \cdot 10^{15} \text{ cm}^{-2}$  and  $T = -30^\circ\text{C}$

data: symbols  
fits: lines

5 pF shifts →

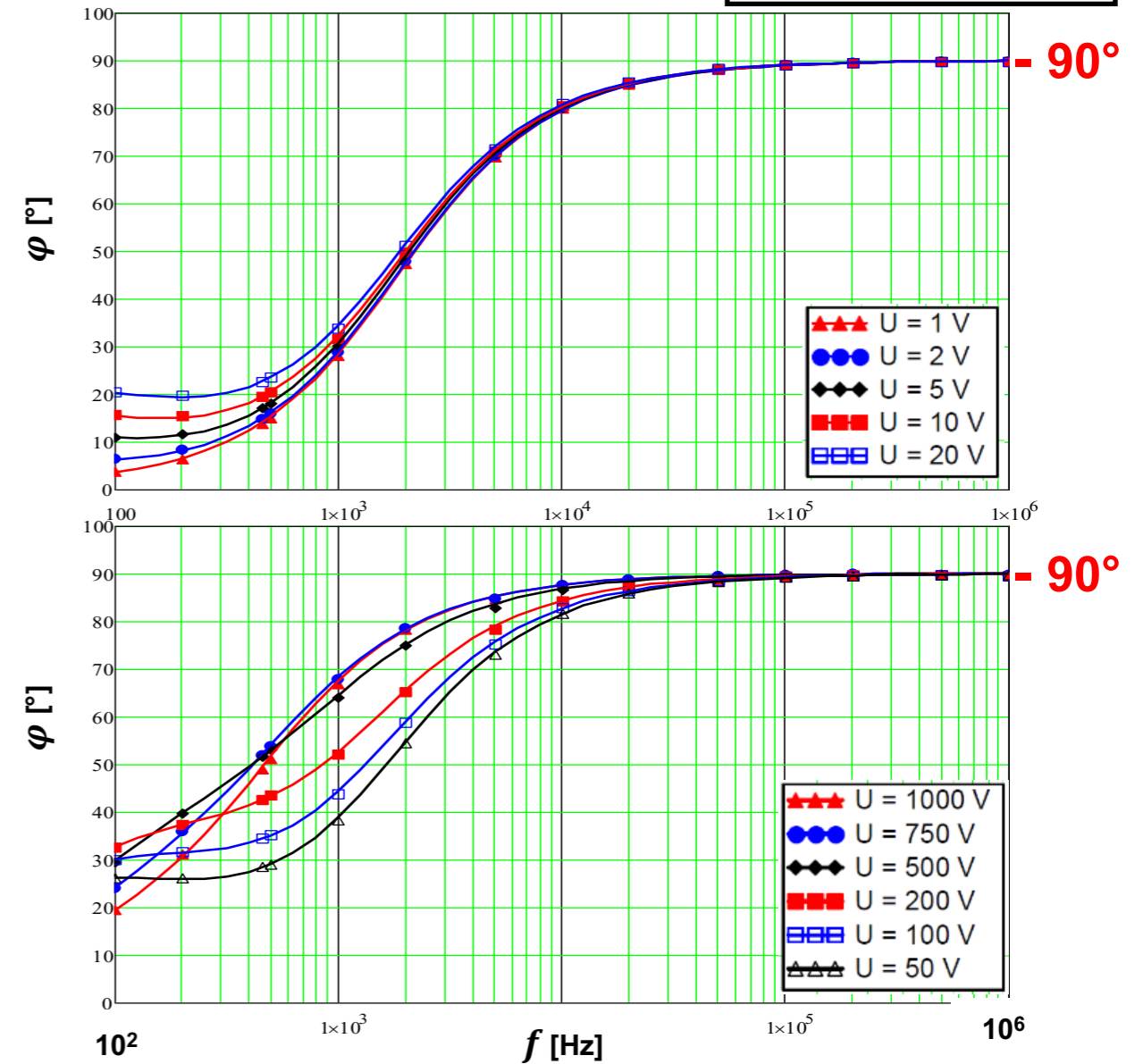
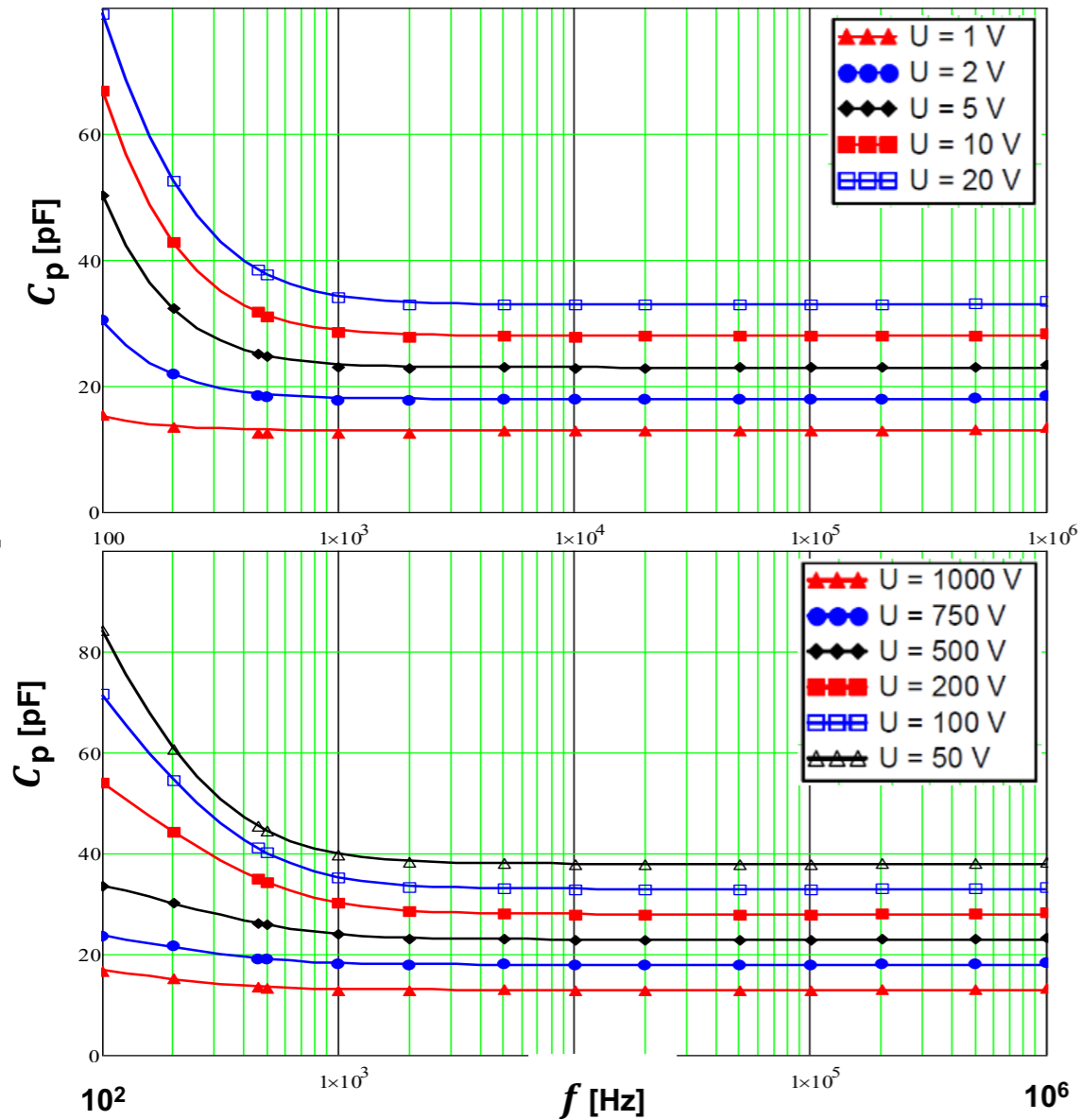


Data described by model:  $\delta C \sim 0.5 \%$ ,  $\delta \varphi \sim 0.5^\circ$

Fit of  $Y(f)$  for every  $V$  and  $\Phi_{eq}$ :  $\Phi_{eq} = 13 \cdot 10^{15} \text{ cm}^{-2}$  and  $T = -30^\circ\text{C}$

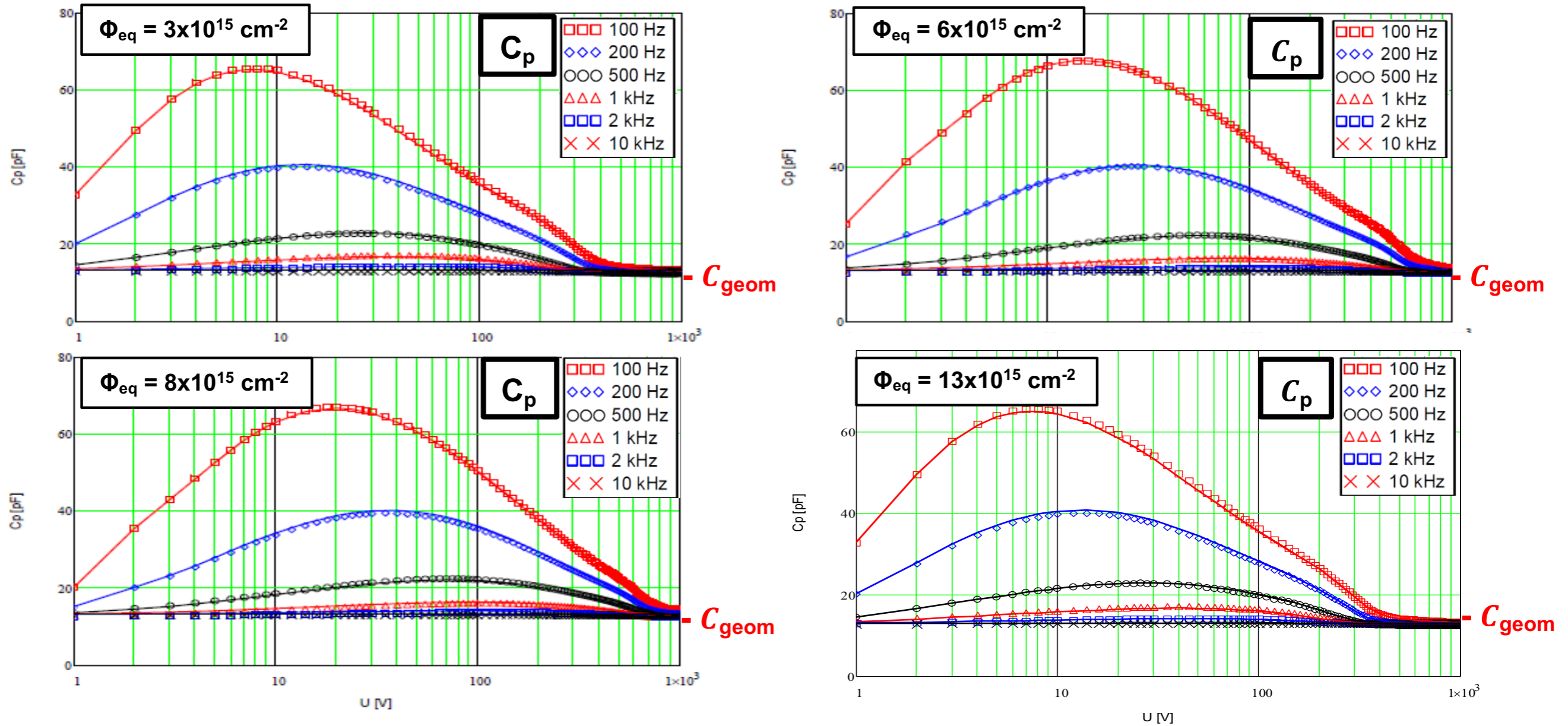
data: symbols  
fits: lines

5 pF shifts  $\longrightarrow$



Data described by model:  $\delta C \sim 0.5\%$ ,  $\delta \varphi \sim 0.5^\circ$

## $C_p(V, \Phi_{eq})$ for selected $f$



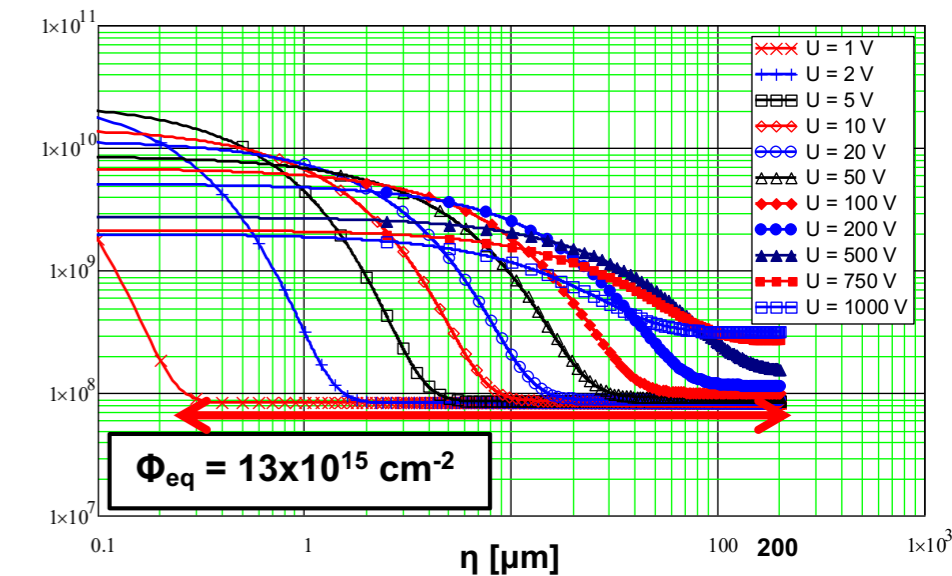
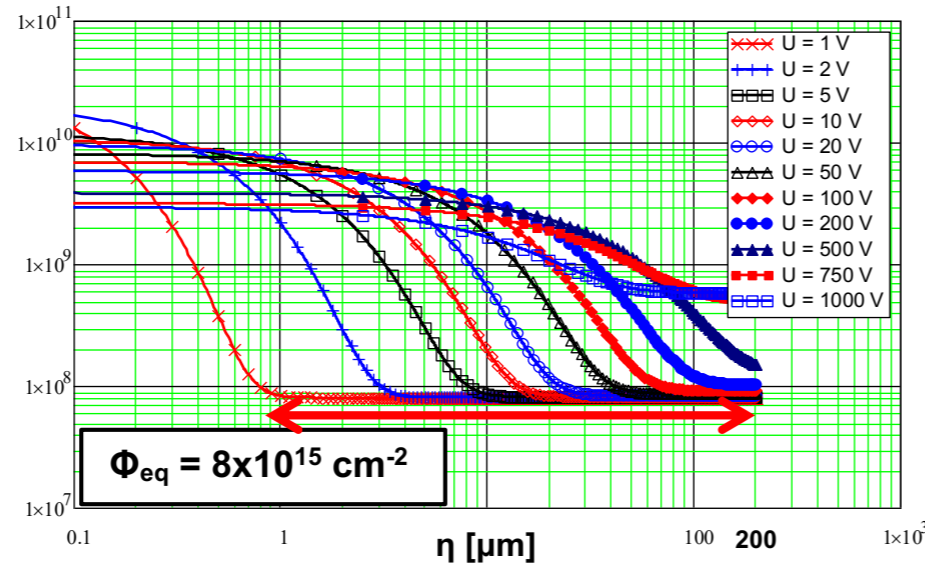
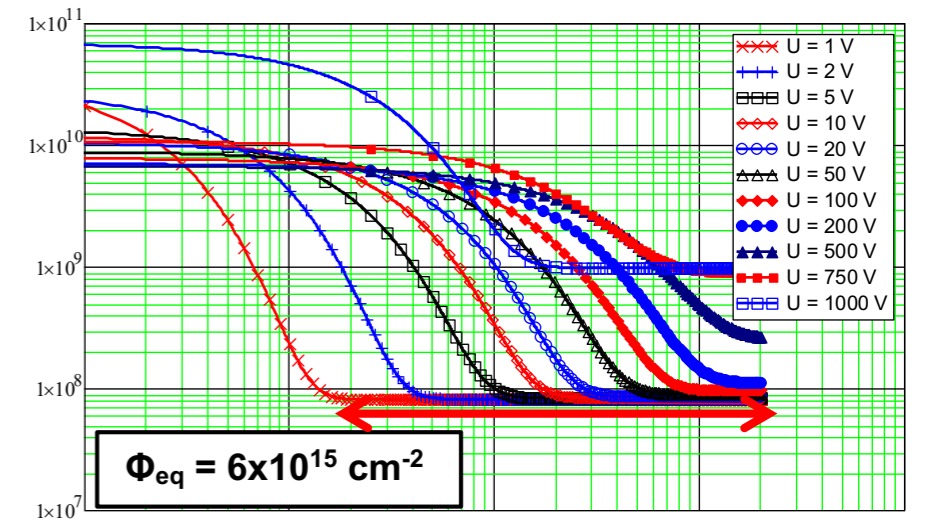
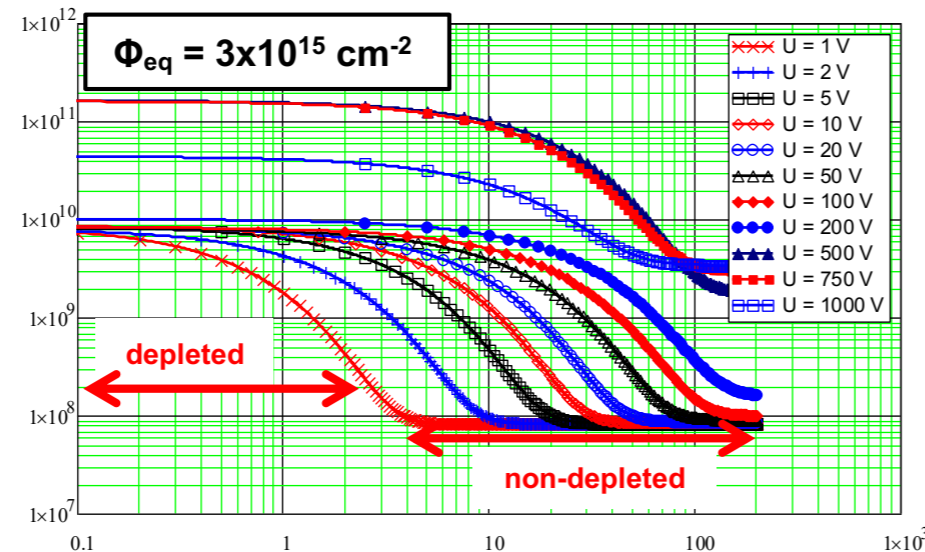
Data described by model: No need for response time of rad.-induced traps

## Resistivity $\rho(\eta)$ vs. $\Phi_{eq}$

**$T = -30^\circ\text{C}$ :**  
 $\rho_{intr} = 70 \text{ M}\Omega\cdot\text{cm}$  (calc.)  
 $\rho_{min} = 81 \text{ M}\Omega\cdot\text{cm}$  (fit)

**$T = -20^\circ\text{C}$ :**  
 $\rho_{intr} = 23 \text{ M}\Omega\cdot\text{cm}$  (calc.)  
 $\rho_{min} = 27 \text{ M}\Omega\cdot\text{cm}$  (fit)

Approx. agreement



**Non-depleted region:**  
 $\rho \sim \rho_{intr} = \text{constant}$   
 (generation-recombination equilibrium)  
 width decreases with  $V$   
 and increases with  $\Phi_{eq}$

**Width depleted region:**  
 $\rightarrow$  increases with  $V$  and decreases with  $\Phi_{eq}$   
 for  $V > 500 \text{ V} \rightarrow$  fully depleted  
 $\rightarrow$  For high  $\rho$ ,  $\rho$  is only poorly determined

$\eta$ -region with  $\rho \gg \rho_{intr} \rightarrow$  "effective" depletion depth



## Frequency dependence of $Y$

- Simple model with a position-dependent resistivity  $\rho(\eta)$  describes the  $Y(f;V,\Phi_{eq})$  data of highly-irradiated sensors
- Low field region with  $\rho \sim \rho_{intr}$ , which decreases with  $V$  and increases with  $\Phi_{eq}$
- High  $\rho \rightarrow$  depleted region, high field region increases with  $V$  until the entire sensor is depleted
- No need to include the response-time of radiation-induced traps in the model!!!

**Progress towards understanding of the f-dependence of  $C$  but the understanding of the results is not so clear**

## Thank you for your attention!