

# *Constraining the Higgs-gauge couplings through differential SMEFT analyses*

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Based on

Phys. Rev. D **98**, 095012 (2018), [arXiv:1807.01796](#) (with R. S. Gupta, C. Englert and M. Spannowsky)

Phys. Rev. D **100**, 115004, [arXiv:1905.02728](#) (with R. S. Gupta, J. Y. Reiness and M. Spannowsky)

[arXiv: 1912.07628](#) (with R. S. Gupta, J. Y. Reiness, S. Seth and M. Spannowsky)

[arXiv: 2006.abcde](#) (with J. Y. Araz, R. S. Gupta and M. Spannowsky)

# SMEFT Motivation

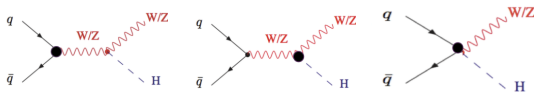
- Q: How do we reconstruct a TeV-Scale Lagrangian from this data?
- Q: How to extract the best observables to study the effects of a particular operator and for a particular process?
- New vertices ensuing from EFT can produce novel/ enhanced effects in parts of the phase space
- These questions and ideas can be addressed in the regime of high energies/ luminosities

- A bigger theory (either weakly or strongly coupled) is assumed to supersede the SM above the scale  $\Lambda$
- At the perturbative level, all heavy ( $> \Lambda$ ) DOF are decoupled from the low energy theory (Appelquist-Carazzone theorem)
- Appearance of HD operators in the effective Lagrangian valid below  $\Lambda$

$$\mathcal{L} = \mathcal{L}_{SM}^{d=4} + \sum_{d \geq 5} \sum_i \frac{f_i}{\Lambda^{d-4}} \mathcal{O}_i^d$$

- Precisely measuring the Higgs couplings  $\rightarrow$  one of the most important LHC goals
- Indirect constraints can constrain much higher scales  $S, T$  parameters being prime examples
- Q: Can LHC compete with LEP in constraining precision physics? Can LHC provide new information?  
A: From EFT correlated variables, LEP already constrained certain anomalous Higgs couplings  $\rightarrow$  Z-pole measurements, TGCs  
Going to higher energies in LHC is the only way to obtain new information

# Case study I: Higgs-Strahlung at the LHC



$$\begin{aligned}
 \Delta\mathcal{L}_6 \supset & \delta\hat{g}_{WW}^h \frac{2m_W^2}{v} h W^{+\mu} W_{\mu}^{-} + \delta\hat{g}_{ZZ}^h \frac{2m_Z^2}{v} h \frac{Z^{\mu} Z_{\mu}}{2} + \delta g_Q^W (W_{\mu}^{+} \bar{u}_L \gamma^{\mu} d_L + h.c.) \\
 & + \delta g_L^W (W_{\mu}^{+} \bar{\nu}_L \gamma^{\mu} e_L + h.c.) + g_{WL}^h \frac{h}{v} (W_{\mu}^{+} \bar{\nu}_L \gamma^{\mu} e_L + h.c.) \\
 & + g_{WQ}^h \frac{h}{v} (W_{\mu}^{+} \bar{u}_L \gamma^{\mu} d_L + h.c.) + \sum_f \delta g_f^Z Z_{\mu} \bar{f} \gamma^{\mu} f + \sum_f g_{Zf}^h \frac{h}{v} Z_{\mu} \bar{f} \gamma^{\mu} f \\
 & + \kappa_{WW} \frac{h}{v} W^{+\mu\nu} W_{\mu\nu}^{-} + \tilde{\kappa}_{WW} \frac{h}{v} W^{+\mu\nu} \tilde{W}_{\mu\nu}^{-} + \kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z_{\mu\nu} \\
 & + \tilde{\kappa}_{ZZ} \frac{h}{2v} Z^{\mu\nu} \tilde{Z}_{\mu\nu} + \kappa_{Z\gamma} \frac{h}{v} A^{\mu\nu} Z_{\mu\nu} + \tilde{\kappa}_{Z\gamma} \frac{h}{v} A^{\mu\nu} \tilde{Z}_{\mu\nu} + \delta\hat{g}_{bb}^h \frac{\sqrt{2}m_b}{v} h b \bar{b}
 \end{aligned}$$

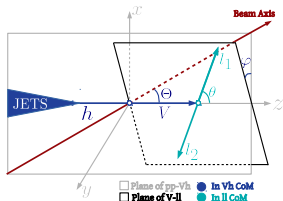
- The leading effect comes from contact interaction at high energies. The energy growth occurs because there is no propagator
- $\delta g_f^Z$ ,  $\delta\hat{g}_{ZZ}^h$  (and other terms in blue)  $\rightarrow$  deviations in SM amplitude
- These do not grow with energy and are suppressed by  $\mathcal{O}(m_Z^2/\hat{s})$ , w.r.t.  $g_{Vf}^h$

# Higgs-Strahlung: Operators at play

$\mathcal{O}_{H\Box} = (H^\dagger H)\Box(H^\dagger H)$	$\mathcal{O}_{HL}^{(3)} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{L} \sigma^a \gamma^\mu L$
$\mathcal{O}_{HD} = (H^\dagger D_\mu H)^*(H^\dagger D_\mu H)$	$\mathcal{O}_{HB} =  H ^2 B_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{Hu} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{u}_R \gamma^\mu u_R$	$\mathcal{O}_{HWB} = H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu}$
$\mathcal{O}_{Hd} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{d}_R \gamma^\mu d_R$	$\mathcal{O}_{HW} =  H ^2 W_{\mu\nu} W^{\mu\nu}$
$\mathcal{O}_{He} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{e}_R \gamma^\mu e_R$	$\mathcal{O}_{H\tilde{B}} =  H ^2 B_{\mu\nu} \tilde{B}^{\mu\nu}$
$\mathcal{O}_{HQ}^{(1)} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{Q} \gamma^\mu Q$	$\mathcal{O}_{H\tilde{W}B} = H^\dagger \sigma^a H W_{\mu\nu}^a \tilde{B}^{\mu\nu}$
$\mathcal{O}_{HQ}^{(3)} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{Q} \sigma^a \gamma^\mu Q$	$\mathcal{O}_{H\tilde{W}} =  H ^2 W_{\mu\nu}^a \tilde{W}^{a\mu\nu}$
$\mathcal{O}_{HL}^{(1)} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{L} \gamma^\mu L$	$\mathcal{O}_{yb} = y_b  H ^2 (\bar{Q} H b_R + h.c.).$

**Table:** D6 operators in Warsaw basis contributing to anomalous  $hVV^*/hV\bar{f}f$  couplings.

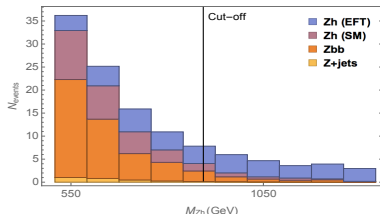
# Differential in energy and angles: $pp \rightarrow V(\ell\ell)h$ (Fat jet)



- $\varphi$ ,  $\Theta$  and  $\{x, y, z\}$  in **Vh CoM frame** ( $z$  identified as direction of  $V$ -boson;  $y$  identified as normal to the plane of  $V$  and beam axis;  $x$  defined to complete the right-handed set),  $\theta$  in **V CoM frame**
- Q: **How much differential information can one extract from this process?**
- For three body phase space,  $3 \times 3 - 4 = 5$  kinematic variables completely define final state
- Barring boost factor, the variables are  $\sqrt{s}$ ,  $\Theta$ ,  $\theta$ ,  $\varphi$
- Considering **10** bins per variable  $\rightarrow$  **1000** numbers per energy bin to obtain full information  
 $\rightarrow$  can be reduced to **9 per energy bin**

# Differential in Energy: $pp \rightarrow Zh$ at high energies (Contact term)

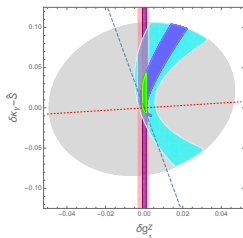
- The differential cross-section for the processes  $pp \rightarrow Z(\ell^+\ell^-)/W(\ell\nu)h(b\bar{b})$  is a differential in four variables, viz.,  $\frac{d\sigma}{dE d\Theta d\theta d\varphi}$
- Major background  $Zb\bar{b}$  ( $b$ -tagging efficiency taken to be 70%)
- Boosted substructure analysis with fat-jets of  $R = 1.2$  used
- $\sigma_{Zh}^{SM}/\sigma_{Zb\bar{b}}$  without cuts  $\sim 4.6/165$ ; With the cut-based analysis  $\rightarrow 0.26$
- With MVA optimisation  $\rightarrow 0.50$  See also [Freitas, Khosa and Sanz, 2019]
- $S/B$  changes from  $1/40$  to  $\mathcal{O}(1)$   $\rightarrow$  Close to 35 SM  $Zh(b\bar{b}\ell^+\ell^-)$  events left at  $300 \text{ fb}^{-1}$   
[SB, Englert, Gupta, Spannowsky, 2018]; NLO corrections: [Greljo, Isidori, Lindert, Marzocca, Zhang, 2017]
- See Nan Lu's slides for possible updates using future detector upgrades



Cuts	Zbb	Zh (SM)
At least 1 fat jet with 2 $B$ -mesons with $p_T > 15 \text{ GeV}$	0.23	0.41
2 OSSF isolated leptons	0.41	0.50
$80 \text{ GeV} < M_{\ell\ell} < 100 \text{ GeV}$ , $p_{T,\ell\ell} > 160 \text{ GeV}$ , $\Delta R_{\ell\ell} > 0.2$	0.83	0.89
At least 1 fat jet with 2 $B$ -meson tracks with $p_T > 110 \text{ GeV}$	0.96	0.98
2 Mass drop subjets and $\geq 2$ filtered subjets	0.88	0.92
2 $b$ -tagged subjets	0.38	0.41
$115 \text{ GeV} < m_h < 135 \text{ GeV}$	0.15	0.51
$\Delta R(b_i, \ell_j) > 0.4$ , $\cancel{E}_T < 30 \text{ GeV}$ , $ y_h  < 2.5$ , $p_{T,h/Z} > 200 \text{ GeV}$	0.47	0.69

# Differential in Energy: $pp \rightarrow Zh$ at high energies (Contact term)

- Two-parameter  $\chi^2$ -fit (at  $300 \text{ fb}^{-1}$ ) in  $\delta g_1^Z - (\delta \kappa_\gamma - \hat{S})$  plane



Blue dashed line  $\rightarrow$  direction of accidental cancellation of interference term; Gray region: LEP exclusion; pink band: exclusion from WZ [Franceschini, Panico, Pomarol, Riva and Wulzer, 2017]; Blue region: exclusion from  $Zh$ ; dark (light) shade represents bounds at  $3 \text{ ab}^{-1}$  ( $300 \text{ fb}^{-1}$ ) luminosity; Green region: Combined bound from  $Zh$  and WZ [SB, Englert, Gupta, Spannowsky, 2018]

- Bounds on pseudo observables
- Our bounds are derived by considering one parameter at a time and upon considering only interference (at 95% CL).

The four directions in LEP are at 68% CL.

$$g_{\mathbf{p}}^Z = g_{Zu_L}^h - 0.76 g_{Zd_L}^h - 0.45 g_{Zu_R}^h + 0.14 g_{Zd_R}^h$$

$$g_{Z\mathbf{p}}^h \in [-0.004, 0.004] \quad (300 \text{ fb}^{-1})$$

$$g_{Z\mathbf{p}}^h \in [-0.001, 0.001] \quad (3000 \text{ fb}^{-1})$$

	Our Projection	LEP Bound
$\delta g_{u_L}^Z$	$\pm 0.002 (\pm 0.0007)$	$-0.0026 \pm 0.0016$
$\delta g_{d_L}^Z$	$\pm 0.003 (\pm 0.001)$	$0.0023 \pm 0.001$
$\delta g_{u_R}^Z$	$\pm 0.005 (\pm 0.001)$	$-0.0036 \pm 0.0035$
$\delta g_{d_R}^Z$	$\pm 0.016 (\pm 0.005)$	$0.016 \pm 0.0052$
$\delta g_1^Z$	$\pm 0.005 (\pm 0.001)$	$0.009^{+0.043}_{-0.042}$
$\delta \kappa_\gamma$	$\pm 0.032 (\pm 0.009)$	$0.016^{+0.085}_{-0.096}$
$\hat{S}$	$\pm 0.032 (\pm 0.009)$	$0.0004 \pm 0.0007$
$W$	$\pm 0.003 (\pm 0.001)$	$0.0000 \pm 0.0006$
$Y$	$\pm 0.032 (\pm 0.009)$	$0.0003 \pm 0.0006$

# Helicity Amplitudes

- For a  $2 \rightarrow 2$  process  $f(\sigma)\bar{f}(-\sigma) \rightarrow Vh$ , the helicity amplitudes are given by

$$\mathcal{M}_{\sigma}^{\lambda=\pm} = \sigma \frac{1 + \sigma\lambda \cos \Theta}{\sqrt{2}} G_V \frac{m_V}{\sqrt{\hat{s}}} \left[ 1 + \left( \frac{g_{Vf}^h}{g_f^V} + \hat{\kappa}_{VV} - i\lambda \hat{\kappa}_{VV} \right) \frac{\hat{s}}{2m_V^2} \right]$$

$$\mathcal{M}_{\sigma}^{\lambda=0} = -\frac{\sin \Theta}{2} G_V \left[ 1 + \delta \hat{g}_{VV}^h + 2\hat{\kappa}_{VV} + \delta g_f^Z + \frac{g_{Vf}^h}{g_f^V} \left( -\frac{1}{2} + \frac{\hat{s}}{2m_V^2} \right) \right]$$

$$[\hat{\kappa}_{WW} = \kappa_{WW}, \hat{\kappa}_{ZZ} = \kappa_{ZZ} + \frac{Q_f e}{g_f^Z} \kappa_{Z\gamma}, \tilde{\kappa}_{ZZ} = \tilde{\kappa}_{ZZ} + \frac{Q_f e}{g_f^Z} \tilde{\kappa}_{Z\gamma}]$$

- $\lambda = \pm 1$  and  $\sigma = \pm 1$  are, respectively, the helicities of the  $Z/W$ -boson and initial-state fermions,  $g_f^Z = g(T_3^f - Q_f s_{\theta_W}^2)/c_{\theta_W}$
- Leading SM is longitudinal ( $\lambda = 0$ ), Leading effect of  $\kappa_{WW}$ ,  $\kappa_{ZZ}$ ,  $\tilde{\kappa}_{ZZ}$  is in the transverse-longitudinal (LT) interference, LT term vanishes if we aren't careful
- The amplitude at decay level:  $\mathcal{A}(\hat{s}, \Theta, \theta, \varphi) = \frac{-ig_{\ell}^V + \delta g_{\ell}^V}{\Gamma_V} \sum_{\lambda} \mathcal{M}_{\sigma}^{\lambda}(\hat{s}, \Theta) d_{\lambda,1}^{J=1}(\theta) e^{i\lambda\varphi}$
- $d_{\pm 1,1}^{J=1} = \tau \frac{1 \pm \tau \cos \theta}{\sqrt{2}}$ ,  $d_{0,1}^{J=1} = \sin \theta$  are the Wigner functions,  $\tau$  is lepton helicity,  $\Gamma_V$  is the  $V$ -width and  $g_f^Z = g(T_3^f - Q_f s_{\theta_W}^2)/c_{\theta_W}$  and  $g_f^W = g/\sqrt{2}$
- $\hat{\varphi} \rightarrow$  azimuthal angle of positive helicity lepton,  $\hat{\theta} \rightarrow$  its polar angle in  $V$ -rest frame
- Polarisation of lepton is experimentally not accessible



# Helicity Amplitudes: Angular Moments

- We sum over lepton polarisations and express the analogous angles  $(\theta, \varphi)$  for the positively-charged lepton

$$\sum_{L,R} |\mathcal{A}(\hat{s}, \Theta, \theta, \varphi)|^2 = \alpha_L |\mathcal{A}_h(\hat{s}, \Theta, \theta, \varphi)|^2 + \alpha_R |\mathcal{A}_h(\hat{s}, \Theta, \pi - \theta, \pi + \varphi)|^2$$

- $\alpha_{L,R} = (g_{L,R}^Z)^2 / [(g_L^Z)^2 + (g_R^Z)^2] \rightarrow$  fraction of  $Z \rightarrow \ell^+ \ell^-$  decays to leptons with left-handed (right-handed) chiralities  $\epsilon_{LR} = \alpha_L - \alpha_R \approx 0.16$
- For left-handed chiralities, positive-helicity lepton  $\rightarrow$  positive-charged lepton
- For right-handed chiralities, positive-helicity lepton  $\rightarrow$  negative-charged lepton  $\rightarrow (\hat{\theta}, \hat{\varphi}) \rightarrow (\pi - \theta, \pi + \varphi) \rightarrow$  Following 9 coefficients are 9 angular moments for  $pp \rightarrow Z(\ell\ell)h$

$$\begin{aligned} \sum_{L,R} |\mathcal{A}(\hat{s}, \Theta, \theta, \varphi)|^2 &= a_{LL} \sin^2 \Theta \sin^2 \theta + a_{TT}^1 \cos \Theta \cos \theta \\ &+ a_{TT}^2 (1 + \cos^2 \Theta)(1 + \cos^2 \theta) + \cos \varphi \sin \Theta \sin \theta \\ &\times (a_{LT}^1 + a_{LT}^2 \cos \theta \cos \Theta) + \sin \varphi \sin \Theta \sin \theta \\ &\times (\tilde{a}_{LT}^1 + \tilde{a}_{LT}^2 \cos \theta \cos \Theta) + a_{TT'} \cos 2\varphi \sin^2 \Theta \sin^2 \theta \\ &+ \tilde{a}_{TT'} \sin 2\varphi \sin^2 \Theta \sin^2 \theta \end{aligned}$$

See also [Azatov, Elias-Miro, Reyimuaji, Venturini; 2017]

# Differential in angles: Constraining the LT terms

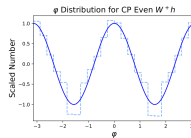
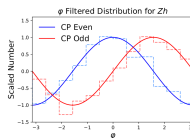
$a_{LL}$	$\frac{\mathcal{G}^2}{4} \left[ 1 + 2\delta\hat{g}_{VV}^h + 4\hat{\kappa}_{VV} + 2\delta g_f^Z + \frac{g_{Vf}^h}{g_f} (-1 + 4\gamma^2) \right]$
$a_{TT}^1$	$\frac{\mathcal{G}^2 \sigma_{\epsilon RL}}{2\gamma^2} \left[ 1 + 4 \left( \frac{g_{Vf}^h}{g_f} + \hat{\kappa}_{VV} \right) \gamma^2 \right]$
$a_{TT}^2$	$\frac{\mathcal{G}^2}{8\gamma^2} \left[ 1 + 4 \left( \frac{g_{Vf}^h}{g_f} + \hat{\kappa}_{VV} \right) \gamma^2 \right]$
$a_{LT}^1$	$-\frac{\mathcal{G}^2 \sigma_{\epsilon RL}}{2\gamma} \left[ 1 + 2 \left( \frac{2g_{Vf}^h}{g_f} + \hat{\kappa}_{VV} \right) \gamma^2 \right]$
$a_{LT}^2$	$-\frac{\mathcal{G}^2}{2\gamma} \left[ 1 + 2 \left( \frac{2g_{Vf}^h}{g_f} + \hat{\kappa}_{VV} \right) \gamma^2 \right]$
$\tilde{a}_{LT}^1$	$-\mathcal{G}^2 \sigma_{\epsilon RL} \hat{\kappa}_{VV} \gamma$
$\tilde{a}_{LT}^2$	$-\mathcal{G}^2 \hat{\kappa}_{VV} \gamma$
$a_{TT'}$	$\frac{\mathcal{G}^2}{8\gamma^2} \left[ 1 + 4 \left( \frac{g_{Vf}^h}{g_f} + \hat{\kappa}_{VV} \right) \gamma^2 \right]$
$\tilde{a}_{TT'}$	$\frac{\mathcal{G}^2}{2} \hat{\kappa}_{VV}$

Contribution of the different anomalous couplings to the angular coefficients up to linear order. Contributions subdominant in  $\gamma = \sqrt{s}/(2m_V)$  are neglected, with the exception of the next-to-leading EFT contribution to  $a_{LL}$ , which we retain in order to keep the leading effect of the  $\delta\hat{g}_{VV}^h$  term.  $\mathcal{G} = g g_f^Z \sqrt{(g_L^Z)^2 + (g_R^Z)^2} / (c_{\theta_W} \Gamma_Z)$ .

- As anticipated, the parametrically-largest contribution is to the LT interference terms

$$\frac{a_{LT}^2}{4} \cos \varphi \sin 2\theta \sin 2\Theta + \frac{\tilde{a}_{LT}^2}{4} \sin \varphi \sin 2\theta \sin 2\Theta$$

- These terms vanish on integration of any angle
- Q: How to probe  $\kappa_{ZZ}$  and  $\tilde{\kappa}_{ZZ}$ ?  
A: Simplified approach  $\rightarrow$  Flip sign in regions to maintain positive  $\sin 2\theta \sin 2\Theta$   
A: Sophisticated approach  $\rightarrow$  Use method of moments
- Expect  $\cos \varphi$  distribution for CP-even and  $\sin \varphi$  distribution for CP-odd



Q: Are the LO theoretical shapes preserved upon the inclusion of NLO effects, radiations, showering, experimental cuts, etc.?

A: For the azimuthal angles, they are. [SB, Gupta, Reiness, Spannowsky; 2019], [SB, Gupta, Reiness, Seth, Spannowsky; 2019]

# Differential in angles: Method of moments

- An analog of **Fourier analysis** utilised to extract the aforementioned angular moments

- Our squared amplitude can be parametrised as,  
 $|\mathcal{A}|^2 = \sum_i a_i(E) f_i(\Theta, \theta, \varphi)$

- We look for weight functions,  $w_i(\Theta, \theta, \varphi)$ , such that  
 $\langle w_i | f_j \rangle = \int d(\Theta, \theta, \varphi) w_i f_j = \delta_{ij}$

- One can then pick out the angular moments,  $a_i$  as  
 $a_i = \int d(\Theta, \theta, \varphi) |\mathcal{A}|^2 w_i$

- For the set of basis functions, we get the following matrix

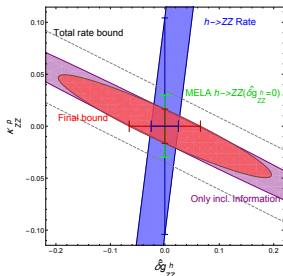
$$M = \begin{pmatrix} \frac{512\pi}{225} & 0 & \frac{128\pi}{25} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{8\pi}{9} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{128\pi}{25} & 0 & \frac{6272\pi}{225} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{16\pi}{9} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{16\pi}{225} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{16\pi}{9} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{16\pi}{225} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{256\pi}{225} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{256\pi}{225} \end{pmatrix}$$

- $w_i \propto f_i$  except for  $i = 1, 3$
- We rotate the (1,3) system to an orthogonal basis
- Using discrete method, we find:  
 $a_i(M) = \frac{\hat{N}}{N} \sum_{n=1}^N w_i(\Theta_n, \theta_n, \varphi_n)$
- Events divided in bins of final state invariant mass ( $M \rightarrow$  central value of bin),  $N(M)(N(M)) \rightarrow$  number of MC (actual) events in that bin for a fixed integrated luminosity

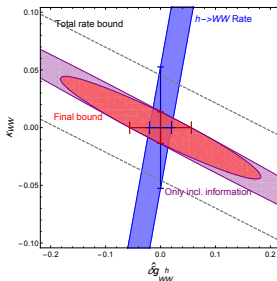
# Results: Contact terms, $Zh$ , $Wh$ , $Zh + Wh$ combination

- We have limited our calculations to include only the interference terms
- The four-point contact vertex is **constrained upon using the  $E^2$  dependent terms**
- The  $a_{LL}$  term dominates at high energies  $\rightarrow |g_{WQ}^h| < 6 \times 10^{-4}$  and  $\rightarrow |g_{Zf}^h| < 4 \times 10^{-4}$  at  $\mathcal{L} = 3 \text{ ab}^{-1}$

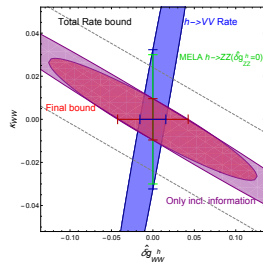
- Method of moments used to constrain the other couplings
- We obtain **percent level bounds on  $\kappa_{ZZ}$  and in the  $(\kappa_{ZZ}, \delta g_{ZZ}^h)$  plane**
- Competitive and complementary bounds to previous analyses
- Independent bound on the CP-odd coupling,  $|\tilde{\kappa}_{ZZ}^P| < 0.03$



- We obtain **percent level bounds on  $\kappa_{WW}$  and in the  $(\kappa_{WW}, \delta g_{WW}^h)$  plane**
- Competitive and complementary bounds to previous analyses
- Independent bound on the CP-odd coupling,  $|\tilde{\kappa}_{WW}^P| < 0.04$



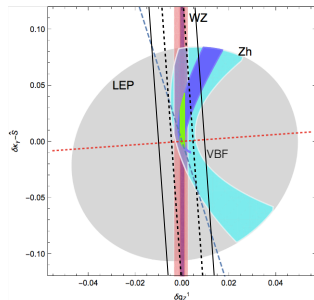
- Upon assuming a linearly realised electroweak symmetry and correlations, we can combine the above bounds



# Case study II: Weak boson fusion (preliminary)

- Process:  $pp \rightarrow h(\gamma\gamma)jj$
- Fake backgrounds are still to be taken properly
- $h \rightarrow \tau\tau$  analyses are underway

	Background		SM Signal	
	Events	Efficiency	Events	Efficiency
Presel.	369176.1 (3691761.0)	-	1365.2 (13651.6)	-
$N_{\text{j}et} \geq 2$	286704.2 (2867042.3)	77.66%	1144.9 (11449.3)	83.87%
Bjet veto	274869.6 (2748696.5)	95.87%	1108.2 (11081.7)	96.79%
$ \Delta\eta_{jj}  > 3$	164813.0 (1648129.7)	59.96%	838.0 (8380.1)	75.62%
$\eta_{j1} \cdot \eta_{j2} < 0$	161844.1 (1618441.5)	98.20%	827.2 (8272.2)	98.71%
$M_{jj} > 600$ [GeV]	93105.4 (931054.2)	57.53%	658.6 (6586.0)	79.62%
$N_\gamma = 2$	20244.1 (202441.2)	21.74%	432.8 (4328.5)	65.72%
$I_\gamma^{rel} < 15\%$	19876.9 (198768.7)	98.19%	431.9 (4318.6)	99.77%
$\Delta R_{\gamma j}^{min} > 1.5$	8379.1 (83790.7)	42.15%	382.6 (3825.6)	88.58%
$ \Delta\Phi_{\gamma\gamma,jj}  > 1.5$	7896.7 (78967.4)	94.24%	373.4 (3734.4)	97.62%
$\Delta\Phi_{j1,j2} < 2$	2393.7 (23936.9)	30.31%	227.7 (2277.0)	60.97%
$122 < M_{\gamma\gamma} < 128$ [GeV]	88.1 (880.6)	3.68%	226.9 (2268.9)	99.64%
$y_{j1,2}^{min} < y_h < y_{j1,2}^{max}$	78.0 (780.4)	88.63%	223.2 (2232.5)	98.40%
S/B	286.06%			
S/(B+S)	74.10%			
$S/\sqrt{B}$	25.27 (79.91)			

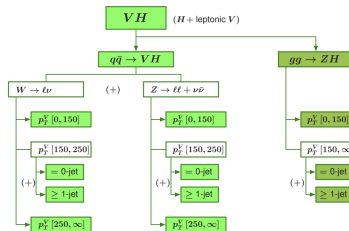
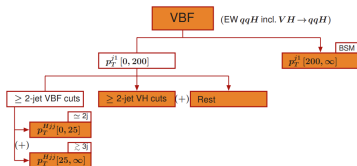
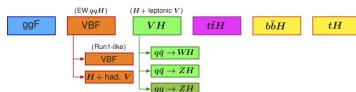
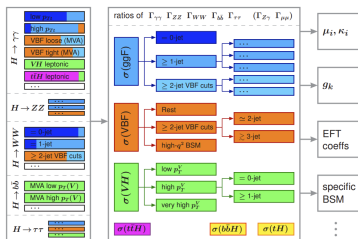


Direction:  $g_p^{VBF} = g_{Zu_L}^h - 0.93g_{Zd_L}^h - 0.13g_{Zu_R}^h + 0.04g_{Zd_R}^h$

[J. Y. Araz, SB, R. S. Gupta, M. Spannowsky, *Coming soon!!!*]

# STXS (plots from LHC Higgs cross-section WG's note)

- Evolving from signal strength measurements performed during Run I, by reducing uncertainties and by providing finely-grained measurements
- Allows combination of measurements in several decay channels. Several stages proposed. **Measuring cross-sections instead of signal strengths**
- **Stage 0 corresponds to production mode categorisation; Stage 1 defines complete setup with potential bin merging etc.**
- From the various bins, one can translate to signal strength measurements, measurements on EFT coefficients, BSM coefficients etc.



# STXS (slide from S. Jiggins)

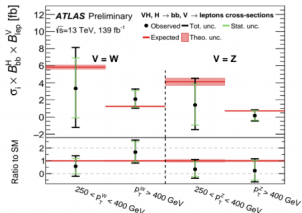
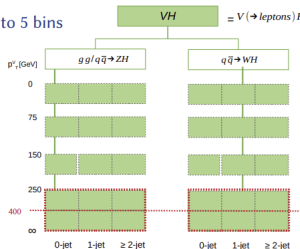
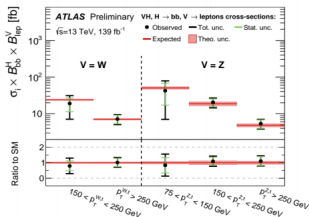


## VH → bb STXS

ATLAS-CONF-2020-006

ATLAS-CONF-2020-007

→ **VHbb resolved**: Stage 1.2 STXS scheme merged down to 5 bins



→ **VHbb Resolved**: Increased precision of 5 POI  $\sigma^{W/ZH}$  results:  
 $80 \text{ fb}^{-1}$ : 50%-125% uncertainty on  $\sigma^{W/ZH}$   
 $139 \text{ fb}^{-1}$ : 30%-85% uncertainty on  $\sigma^{W/ZH}$

→ **VHbb boosted**: Stage 1.2 STXS scheme merged down to **4 bins**  
 - Measurement of  $p_T^V(\text{truth}) > 400 \text{ GeV}$

→ **VHbb resolved + boosted not orthogonal!**

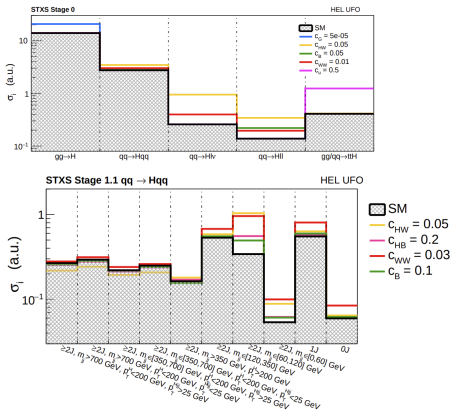
→ See talk by [Nikita Belyaev](#) for more STXS/EFT results  
 → Or backup for questions!

Stephen Jiggins

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See slides from Stephen Jiggins, Jonathan M. Langford and Nikita Belyaev

## STXS (plots from J. M. Langford)

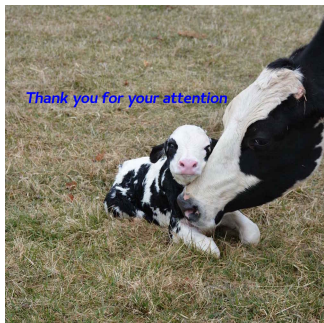


- The STXS method evolves with increasing statistics and requires intuition and systematic understanding of the data
- The various stages of binning help us with an excellent understanding of the present data
- STXS gradually moves forward to a fully differential analysis with shape information
- STXS can be connected to EFTs,  $\kappa$  framework, various BSM scenarios, etc. It is a powerful tool.
- The Matrix Element Method (MEM) is one of the most powerful tools to discern the full structure of any process
- The Method of Moments (MoM), as described in this talk, has comparable sensitivity to the Matrix Element method
- MoM exploits the full angular structure for the squared amplitude in a transparent and experiment-friendly manner
- MoM combines the advantages of both STXS and the MEM, to a certain extent

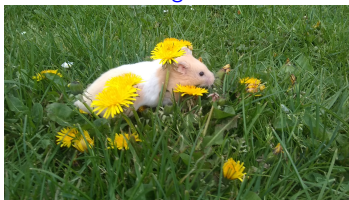


# Summary and conclusions

- HL-LHC can thus strongly compete with LEP and can be considered a good precision machine at the moment
- EFT's essence shows that many anomalous Higgs couplings were already constrained by LEP through  $Z$ -pole and di-boson measurements
- The full  $hZZ$  and  $hWW$  tensor structures can be disentangled by using fully differential information and sophisticated techniques like the Method of moments
- Studying complementary directions like the  $WBF$  is also important
- STXS is a powerful tool that gains in sophistication with more data accumulated
- One should explore the STXS, MoM and Matrix Element methods for comparison and transparency
- Upcoming work using the MoM method for the  $gg \rightarrow h \rightarrow ZZ^* \rightarrow 4\ell$  channel [SB, R. S. Gupta, M. Spannowsky, O. Ochoa-Valeriano and E. Venturini] → Stay tuned!!!



*For further questions, please join: [Zoom link]*  
Meeting ID: 925 6370 6395, Password: 596513



# Backup Slides

# STU oblique parameters



$$\Pi_{\gamma\gamma}(q^2) = q^2 \Pi'_{\gamma\gamma}(0) + \dots$$

$$\Pi_{Z\gamma}(q^2) = q^2 \Pi'_{Z\gamma}(0) + \dots$$

$$\Pi_{ZZ}(q^2) = \Pi_{ZZ}(0) + q^2 \Pi'_{ZZ}(0) + \dots$$

$$\Pi_{WW}(q^2) = \Pi_{WW}(0) + q^2 \Pi'_{WW}(0) + \dots$$

$$\alpha S = 4s_w^2 c_w^2 \left[ \Pi'_{ZZ}(0) - \frac{c_w^2 - s_w^2}{s_w c_w} \Pi'_{Z\gamma}(0) - \Pi'_{\gamma\gamma}(0) \right]$$

$$\alpha T = \frac{\Pi_{WW}(0)}{M_W^2} - \frac{\Pi_{ZZ}(0)}{M_Z^2}$$

$$\alpha U = 4s_w^2 \left[ \Pi'_{WW}(0) - c_w^2 \Pi'_{ZZ}(0) - 2s_w c_w \Pi'_{Z\gamma}(0) - s_w^2 \Pi'_{\gamma\gamma}(0) \right]$$

1. Any BSM correction which is indistinguishable from a redefinition of  $e$ ,  $G_F$  and  $M_Z$  (or equivalently,  $g_1$ ,  $g_2$  and  $v$ ) in the Standard Model proper at the **tree level** does not contribute to  $S$ ,  $T$  or  $U$ .
2. Assuming that the **Higgs sector** consists of electroweak doublet(s)  $H$ , the effective action term  $|H^\dagger D_\mu H|^2 / \Lambda^2$  only contributes to  $T$  and not to  $S$  or  $U$ . This term violates **custodial symmetry**.
3. Assuming that the **Higgs sector** consists of electroweak doublet(s)  $H$ , the effective action term  $H^\dagger W^{\mu\nu} B_{\mu\nu} H / \Lambda^2$  only contributes to  $S$  and not to  $T$  or  $U$ . (The contribution of  $H^\dagger B^{\mu\nu} B_{\mu\nu} H / \Lambda^2$  can be absorbed into  $g_1$  and the contribution of  $H^\dagger W^{\mu\nu} W_{\mu\nu} H / \Lambda^2$  can be absorbed into  $g_2$ ).
4. Assuming that the **Higgs sector** consists of electroweak doublet(s)  $H$ , the effective action term  $(H^\dagger W^{\mu\nu} H) (H^\dagger W_{\mu\nu} H) / \Lambda^4$  contributes to  $U$ .

# VH: Relations to the Warsaw Basis

$$\begin{aligned}
 g_{Wf}^h &= \sqrt{2}g \frac{v^2}{\Lambda^2} c_{HF}^{(3)}, \quad \delta \hat{g}_{WW}^h = \frac{v^2}{\Lambda^2} \left( c_{H\Box} - \frac{c_{HD}}{4} \right) \\
 \kappa_{WW} &= \frac{2v^2}{\Lambda^2} c_{HW}, \quad \tilde{\kappa}_{WW} = \frac{2v^2}{\Lambda^2} c_{H\tilde{W}} \\
 \delta g_f^Z &= -\frac{g' Y_f}{c_{\theta_W}} c_{WB} \frac{v^2}{\Lambda^2} - \frac{g}{c_{\theta_W}} \frac{v^2}{\Lambda^2} (|T_3^f| c_{HF}^{(1)} - T_3^f c_{HF}^{(3)} + (1/2 - |T_3^f|) c_{Hf}) c_{\theta_W} \\
 &+ \frac{\delta m_Z^2}{m_Z^2} \frac{g}{2c_{\theta_W} s_{\theta_W}^2} (T_3 c_{\theta_W}^2 + Y_f s_{\theta_W}^2) \\
 \delta \hat{g}_{ZZ}^h &= \frac{v^2}{\Lambda^2} \left( c_{H\Box} + \frac{c_{HD}}{4} \right), \quad g_{Zf}^h = -\frac{2g}{c_{\theta_W}} \frac{v^2}{\Lambda^2} (|T_3^f| c_{HF}^{(1)} - T_3^f c_{HF}^{(3)} + (1/2 - |T_3^f|) c_{Hf}) \\
 \kappa_{ZZ} &= \frac{2v^2}{\Lambda^2} (c_{\theta_W}^2 c_{HW} + s_{\theta_W}^2 c_{HB} + s_{\theta_W} c_{\theta_W} c_{HWB}) \\
 \tilde{\kappa}_{ZZ} &= \frac{2v^2}{\Lambda^2} (c_{\theta_W}^2 c_{H\tilde{W}} + s_{\theta_W}^2 c_{H\tilde{B}} + s_{\theta_W} c_{\theta_W} c_{H\tilde{W}B}), \quad \delta \hat{g}_{bb}^h = y y y c_{y_b}
 \end{aligned}$$

# EFT validity

- Till now, we have dropped the  $gg \rightarrow Zh$  contribution which is  $\sim 15\%$  of the  $qq$  rate
- It doesn't grow with energy in presence of the anomalous couplings
- We estimate the scale of new physics for a given  $\delta g_{Zf}^h$
- Example: Heavy  $SU(2)_L$  triplet (singlet) vector  $W'^a$  ( $Z'$ ) couples to SM fermion current  $\bar{f}\sigma^a\gamma_\mu f$  ( $\bar{f}\gamma_\mu f$ ) with  $g_f$  and to the Higgs current

$iH^\dagger\sigma^a\overleftrightarrow{D}_\mu H$  ( $iH^\dagger\overleftrightarrow{D}_\mu H$ ) with  $g_H$

$$g_{Zu_L, d_L}^h \sim \frac{g_H g^2 v^2}{2\Lambda^2},$$

$$g_{Zf}^h \sim \frac{g_H g g_f v^2}{\Lambda^2} \quad g_{Zu_R, d_R}^h \sim \frac{g_H g g' Y_{u_R, d_R} v^2}{\Lambda^2}$$

- $\Lambda \rightarrow$  mass scale of vector and thus cut-off for low energy EFT
- Assumed  $g_f$  to be a combination of  $g_B = g' Y_f$  and  $g_W = g/2$  for universal case

# The EFT space directions at high energies

- Five directions:  $g_{Zf}^h$  with  $f = u_L, u_R, d_L, d_R$  and  $g_{WQ}^h \rightarrow$  only four operators in Warsaw basis  $\rightarrow g_{WQ}^h = c_\theta \frac{g_{Zu_L}^h - g_{Zd_L}^h}{\sqrt{2}}$
- Knowing proton polarisation is not possible and hence in reality there are two directions Also, upon only considering interference terms, we have

$$g_{\mathbf{u}}^Z = g_{Zu_L}^h + \frac{g_{u_R}^Z}{g_{u_L}^Z} g_{Zu_R}^h$$

$$g_{\mathbf{d}}^Z = g_{Zd_L}^h + \frac{g_{d_R}^Z}{g_{d_L}^Z} g_{Zd_R}^h \quad g_{\mathbf{p}}^Z = g_{\mathbf{u}}^Z + \frac{\mathcal{L}_d(\hat{s})}{\mathcal{L}_u(\hat{s})} g_{\mathbf{d}}^Z$$

$$g_{\mathbf{p}}^Z = g_{Zu_L}^h - 0.76 g_{Zd_L}^h - 0.45 g_{Zu_R}^h + 0.14 g_{Zd_R}^h$$

$$g_{Z\mathbf{p}}^h = -0.14 (\delta\kappa_\gamma - \hat{S} + Y) - 0.89 \delta g_1^Z - 1.3 W$$

$$g_f^Z = g(T_3^f - Q_f s_{\theta_W}^2)/c_{\theta_W}$$

$$g_{\mathbf{p}}^h = 2\delta g_{Zu_L}^h - 1.52 g_{Zd_L}^h - 0.90 g_{Zu_R}^h + 0.28 g_{Zd_R}^h - 0.14 \delta\kappa_\gamma - 0.89 \delta g_1^Z$$

# The four di-bosonic channels

- The four directions, viz.,  $Zh$ ,  $Wh$ ,  $W^+W^-$  and  $W^\pm Z$  can be expressed (at high energies) respectively as  $G^0h$ ,  $G^+h$ ,  $G^+G^-$  and  $G^\pm G^0$  and the Higgs field can be written as

$$\begin{pmatrix} G^+ \\ \frac{h+iG^0}{2} \end{pmatrix}$$

- These four final states are **intrinsically connected**
- At high energies  $W/Z$  production dominates
- With the **Goldstone boson equivalence** it is possible to compute amplitudes for various components of the Higgs in the unbroken phase
- Full SU(2) theory is manifest** [Franceschini, Panico, Pomarol, Riva, Wulzer, 2017]



# BDRS: An aside

2

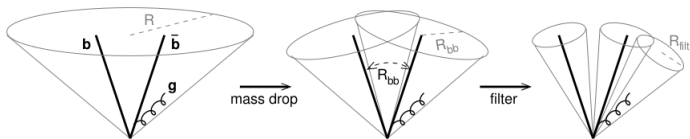


FIG. 1: The three stages of our jet analysis: starting from a hard massive jet on angular scale  $R$ , one identifies the Higgs neighbourhood within it by undoing the clustering (effectively shrinking the jet radius) until the jet splits into two subjects each with a significantly lower mass; within this region one then further reduces the radius to  $R_{\text{filt}}$  and takes the three hardest subjects, so as to filter away UE contamination while retaining hard perturbative radiation from the Higgs decay products.

Given a hard jet  $j$ , obtained with some radius  $R$ , we then use the following new iterative decomposition procedure to search for a generic boosted heavy-particle decay. It involves two dimensionless parameters,  $\mu$  and  $y_{\text{cut}}$ :

1. Break the jet  $j$  into two subjects by undoing its last stage of clustering. Label the two subjects  $j_1, j_2$  such that  $m_{j_1} > m_{j_2}$ .
2. If there was a significant mass drop (MD),  $m_{j_1} < \mu m_j$ , and the splitting is not too asymmetric,  $y = \frac{\min(p_{tj_1}^2, p_{tj_2}^2) \Delta R_{j_1, j_2}^2}{m_j^2} > y_{\text{cut}}$ , then deem  $j$  to be the heavy-particle neighbourhood and exit the loop. Note that  $y \simeq \min(p_{tj_1}, p_{tj_2}) / \max(p_{tj_1}, p_{tj_2})$ .<sup>1</sup>
3. Otherwise redefine  $j$  to be equal to  $j_1$  and go back to step 1.

The final jet  $j$  is to be considered as the candidate Higgs boson if both  $j_1$  and  $j_2$  have  $b$  tags. One can then identify  $R_{bb}$  with  $\Delta R_{j_1, j_2}$ . The effective size of jet  $j$  will thus be just sufficient to contain the QCD radiation from the

In practice the above procedure is not yet optimal for LHC at the transverse momenta of interest,  $p_T \sim 200 - 300 \text{ GeV}$  because, from eq. (1),  $R_{bb} \gtrsim 2m_b/p_T$  is still quite large and the resulting Higgs mass peak is subject to significant degradation from the underlying event (UE), which scales as  $R_{bb}^4$  [19]. A second novel element of our analysis is to filter the Higgs neighbourhood. This involves resolving it on a finer angular scale,  $R_{\text{fis}} < R_{bb}$ , and taking the three hardest objects (subjects) that appear — thus one captures the dominant  $\mathcal{O}(\alpha_s)$  radiation from the Higgs decay, while eliminating much of the UE contamination. We find  $R_{\text{fis}} = \min(0.3, R_{bb}/2)$  to be rather effective. We also require the two hardest of the subjects to have the  $b$  tags.

## ZH: Four directions in the EFT space (SILH Basis)

$$\begin{aligned}g_{Zu_Lu_L}^h &= \frac{g}{c_{\theta_W}} \frac{m_W^2}{\Lambda^2} (c_W + c_{HW} - c_{2W} - \frac{t_{\theta_W}^2}{3} (c_B + c_{HB} - c_{2B})) \\g_{Zd_Ld_L}^h &= -\frac{g}{c_{\theta_W}} \frac{m_W^2}{\Lambda^2} (c_W + c_{HW} - c_{2W} + \frac{t_{\theta_W}^2}{3} (c_B + c_{HB} - c_{2B})) \\g_{Zu_Ru_R}^h &= -\frac{4gs_{\theta_W}^2}{3c_{\theta_W}^3} \frac{m_W^2}{\Lambda^2} (c_B + c_{HB} - c_{2B}) \\g_{Zd_Rd_R}^h &= \frac{2gs_{\theta_W}^2}{3c_{\theta_W}^3} \frac{m_W^2}{\Lambda^2} (c_B + c_{HB} - c_{2B})\end{aligned}$$

## ZH: Four directions in the EFT space (Higgs Primaries Basis)

$$\begin{aligned}g_{Zu_Lu_L}^h &= 2\delta g_{Zu_Lu_L}^Z - 2\delta g_1^Z(g_f^Z c_{2\theta_W} + eQ s_{2\theta_W}) + 2\delta\kappa_\gamma g' Y_h \frac{s_{\theta_W}}{c_{\theta_W}^2} \\g_{Zd_Ld_L}^h &= 2\delta g_{Zd_Ld_L}^Z - 2\delta g_1^Z(g_f^Z c_{2\theta_W} + eQ s_{2\theta_W}) + 2\delta\kappa_\gamma g' Y_h \frac{s_{\theta_W}}{c_{\theta_W}^2} \\g_{Zu_Ru_R}^h &= 2\delta g_{Zu_Ru_R}^Z - 2\delta g_1^Z(g_f^Z c_{2\theta_W} + eQ s_{2\theta_W}) + 2\delta\kappa_\gamma g' Y_h \frac{s_{\theta_W}}{c_{\theta_W}^2} \\g_{Zd_Rd_R}^h &= 2\delta g_{Zd_Rd_R}^Z - 2\delta g_1^Z(g_f^Z c_{2\theta_W} + eQ s_{2\theta_W}) + 2\delta\kappa_\gamma g' Y_h \frac{s_{\theta_W}}{c_{\theta_W}^2}\end{aligned}$$

[Gupta, Pomarol, Riva, 2014]

## ZH: Four directions in the EFT space (Universal model Basis)

$$\begin{aligned}g_{Zu_Lu_L}^h &= -\frac{g}{c_{\theta_W}} \left( (c_{\theta_W}^2 + \frac{s_{\theta_W}^2}{3}) \delta g_1^Z + W + \frac{t_{\theta_W}^2}{3} (\hat{S} - \delta\kappa_\gamma - Y) \right) \\g_{Zd_Ld_L}^h &= \frac{g}{c_{\theta_W}} \left( (c_{\theta_W}^2 - \frac{s_{\theta_W}^2}{3}) \delta g_1^Z + W - \frac{t_{\theta_W}^2}{3} (\hat{S} - \delta\kappa_\gamma - Y) \right) \\g_{Zu_Ru_R}^h &= -\frac{4gs_{\theta_W}^2}{3c_{\theta_W}^3} (\hat{S} - \delta\kappa_\gamma + c_{\theta_W}^2 \delta g_1^Z - Y) \\g_{Zd_Rd_R}^h &= \frac{2gs_{\theta_W}^2}{3c_{\theta_W}^3} (\hat{S} - \delta\kappa_\gamma + c_{\theta_W}^2 \delta g_1^Z - Y)\end{aligned}$$

[Franceschini, Panico, Pomarol, Riva, Wulzer, 2017]

# The four dibosonic channels

Amplitude	High-energy primaries	Amplitude	High-energy primaries
$\bar{u}_L d_L \rightarrow W_L Z_L, W_L h$	$\sqrt{2} a_q^{(3)}$	$\bar{u}_L d_L \rightarrow W_L Z_L, W_L h$	$\frac{g_{Z d_L d_L}^h - g_{Z u_L u_L}^h}{\sqrt{2}}$
$\bar{u}_L u_L \rightarrow W_L W_L$ $\bar{d}_L d_L \rightarrow Z_L h$	$a_q^{(1)} + a_q^{(3)}$	$\bar{u}_L u_L \rightarrow W_L W_L$ $\bar{d}_L d_L \rightarrow Z_L h$	$g_{Z d_L d_L}^h$
$\bar{d}_L d_L \rightarrow W_L W_L$ $\bar{u}_L u_L \rightarrow Z_L h$	$a_q^{(1)} - a_q^{(3)}$	$\bar{d}_L d_L \rightarrow W_L W_L$ $\bar{u}_L u_L \rightarrow Z_L h$	$g_{Z u_L u_L}^h$
$\bar{f}_R f_R \rightarrow W_L W_L, Z_L h$	$a_f$	$\bar{f}_R f_R \rightarrow W_L W_L, Z_L h$	$g_{Z f_R f_R}^h$

$VH$  and  $VV$  channels are entwined by symmetry and they constrain the same set of observables at High energies but may have different directions [Franceschini, Panico, Pomarol, Riva, Wulzer, 2017 & SB, Gupta, Reiness, Seth (in progress)]

# Higgs-Strahlung at FCC-hh

- With a similar analysis, we obtain much stronger bounds with the 100 TeV collider

	Our 100 TeV Projection	Our 14 TeV projection	LEP Bound
$\delta g_{u_L}^Z$	$\pm 0.0003$ ( $\pm 0.0001$ )	$\pm 0.002$ ( $\pm 0.0007$ )	$-0.0026 \pm 0.0016$
$\delta g_{d_L}^Z$	$\pm 0.0003$ ( $\pm 0.0001$ )	$\pm 0.003$ ( $\pm 0.001$ )	$0.0023 \pm 0.001$
$\delta g_{u_R}^Z$	$\pm 0.0005$ ( $\pm 0.0002$ )	$\pm 0.005$ ( $\pm 0.001$ )	$-0.0036 \pm 0.0035$
$\delta g_{d_R}^Z$	$\pm 0.0015$ ( $\pm 0.0006$ )	$\pm 0.016$ ( $\pm 0.005$ )	$0.0016 \pm 0.0052$
$\delta g_1^Z$	$\pm 0.0005$ ( $\pm 0.0002$ )	$\pm 0.005$ ( $\pm 0.001$ )	$0.009^{+0.043}_{-0.042}$
$\delta \kappa_\gamma$	$\pm 0.0035$ ( $\pm 0.0015$ )	$\pm 0.032$ ( $\pm 0.009$ )	$0.016^{+0.085}_{-0.096}$
$\hat{S}$	$\pm 0.0035$ ( $\pm 0.0015$ )	$\pm 0.032$ ( $\pm 0.009$ )	$0.0004 \pm 0.0007$
$W$	$\pm 0.0004$ ( $\pm 0.0002$ )	$\pm 0.003$ ( $\pm 0.001$ )	$0.0000 \pm 0.0006$
$Y$	$\pm 0.0035$ ( $\pm 0.0015$ )	$\pm 0.032$ ( $\pm 0.009$ )	$0.0003 \pm 0.0006$

[SB, Englert, Gupta, Spannowsky (in progress)]