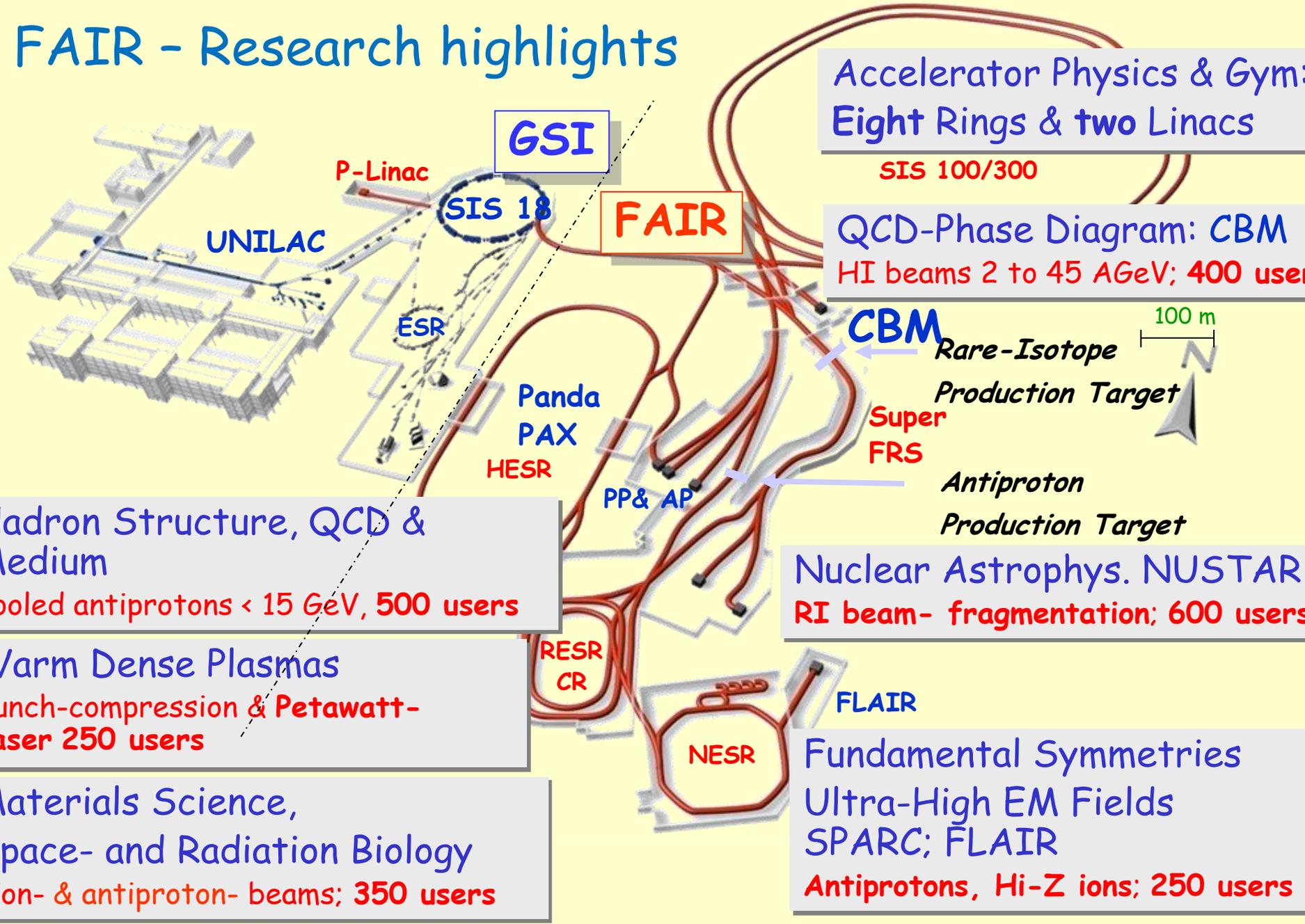


Perspectives for Drell-Yan at FAIR

Paolo Lenisa
Università di Ferrara and INFN - ITALY

Studying the hadron structure in DY-reactions
CERN - 27.04.10

FAIR - Research highlights



Accelerator Physics & Gyms
Eight Rings & two Linacs

SIS 100/300

QCD-Phase Diagram: CBM
HI beams 2 to 45 AGeV; 400 users

CBM
Rare-Isotope Production Target
Super FRS
Antiproton Production Target

Nuclear Astrophys. NUSTAR
RI beam- fragmentation; 600 users

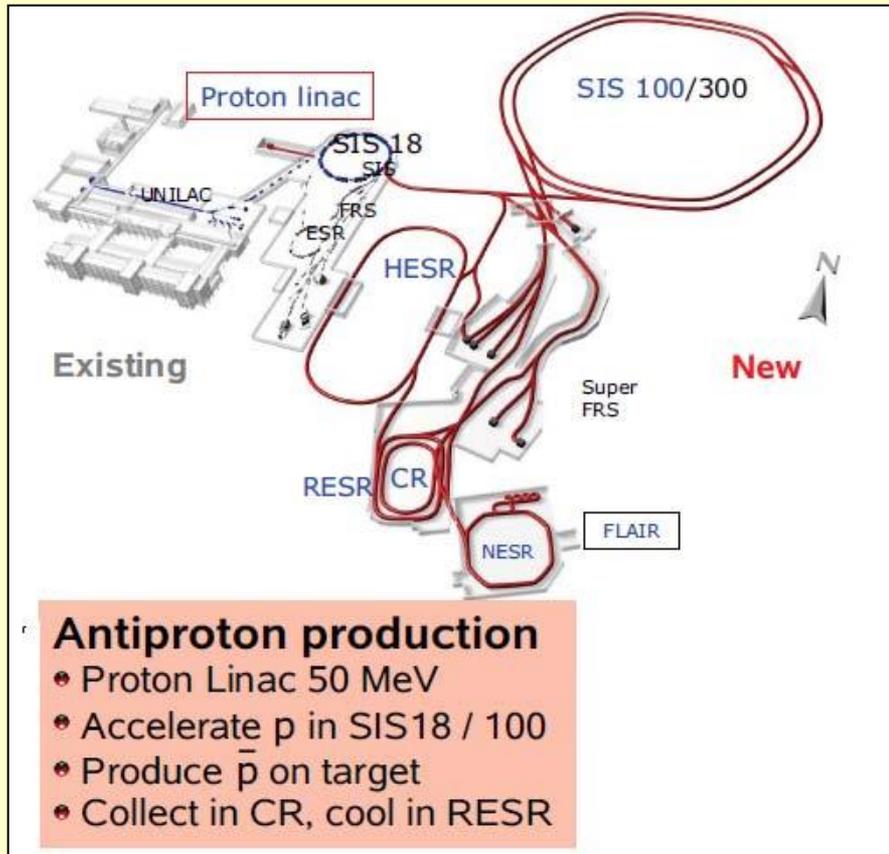
FLAIR
Fundamental Symmetries
Ultra-High EM Fields
SPARC; FLAIR
Antiprotons, Hi-Z ions; 250 users

Hadron Structure, QCD & Medium
Cooled antiprotons < 15 GeV, 500 users

Warm Dense Plasmas
Bunch-compression & Petawatt-Laser 250 users

Materials Science,
Space- and Radiation Biology
(Ion- & antiproton- beams; 350 users)

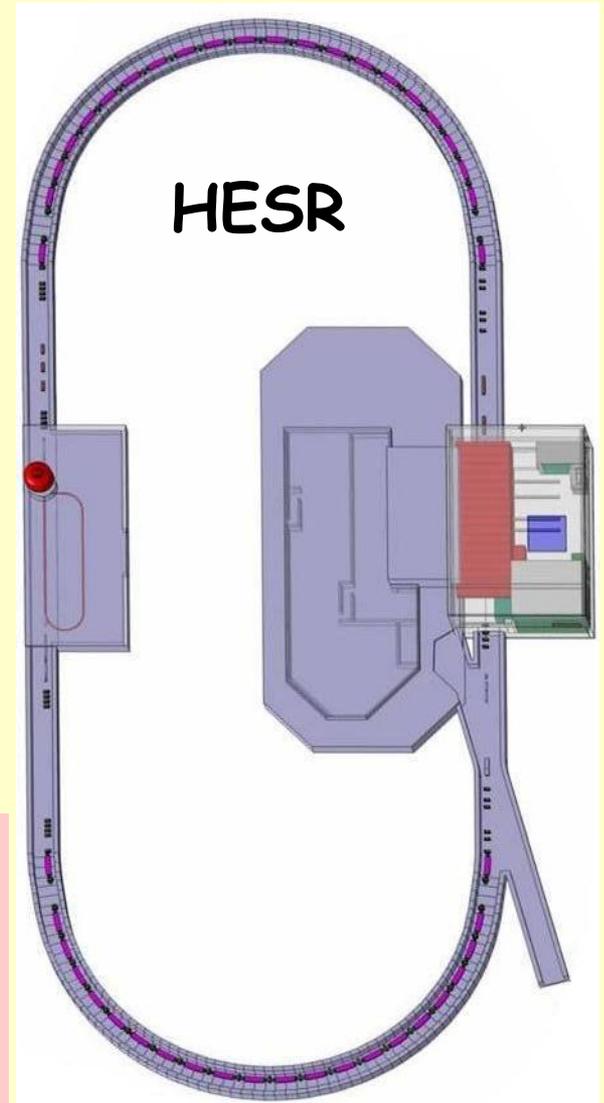
Antiprotons at FAIR



Antiproton production

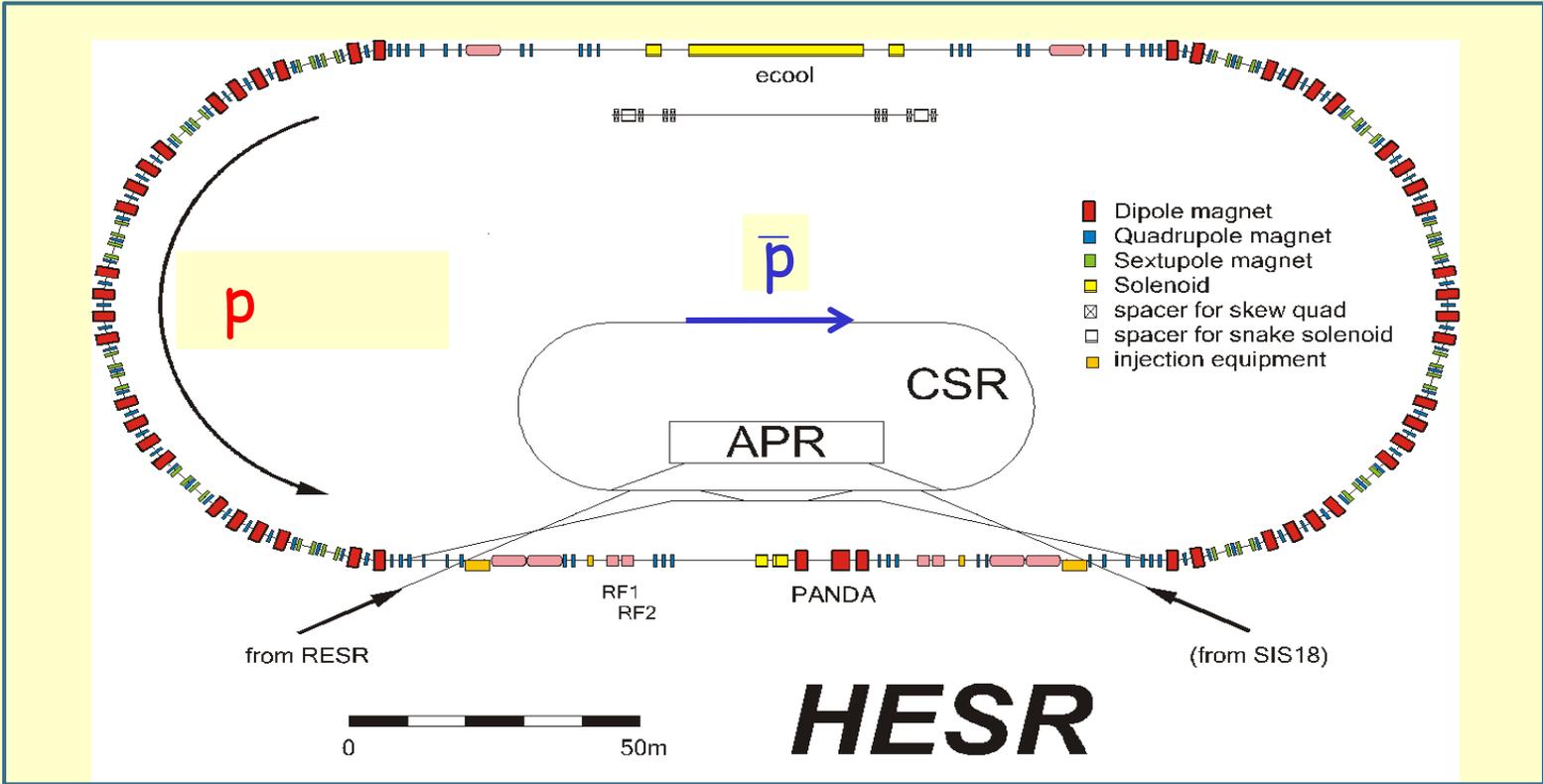
- Proton Linac 50 MeV
- Accelerate p in SIS18 / 100
- Produce \bar{p} on target
- Collect in CR, cool in RESR

- Antiprotons with $1.5 \text{ GeV}/c \leq p \leq 15 \text{ GeV}/c$
- High luminosity: $2 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
Thick targets: $4 \cdot 10^{15} \text{ cm}^{-2}$
Long beam life time: $> 30 \text{ min}$
- High momentum resolution: $\Delta p/p \leq 4 \cdot 10^{-5}$
Phase space cooling



Hadron Physics „Dream Machine“

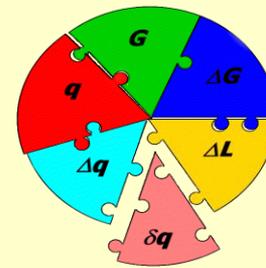
Asymmetric (double-polarized)
 proton (15 GeV/c) - antiproton (3.5 GeV/c) collider



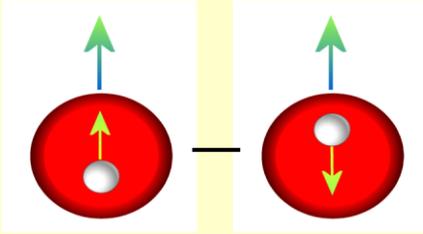
Outline

- DY with polarized antiprotons @ asymmetric collider
- Perspectives for single-single spin asymm. @ fixed target
- Status of polarized antiprotons studies

Transversity



$$h_1^q =$$

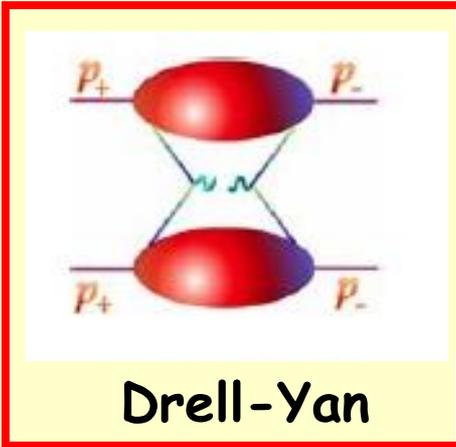


transversely polarised
quarks and nucleons

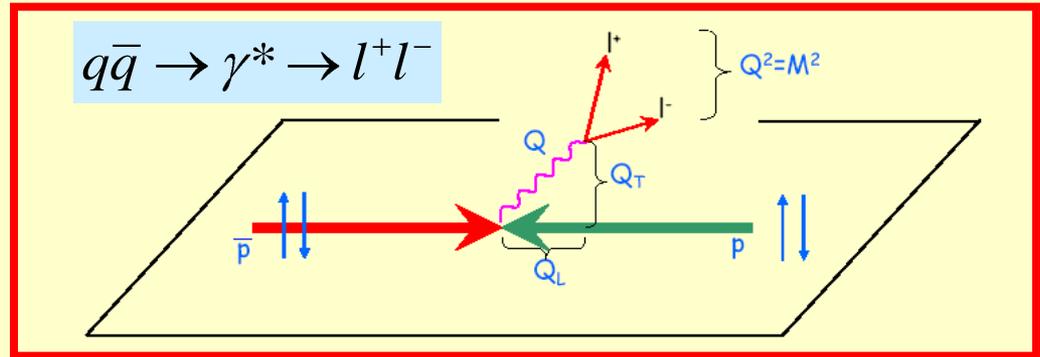
- Probes relativistic nature of quarks
- No gluon analog for spin-1/2 nucleon
- Different Q^2 evolution than Δq
- Sensitive to valence quark polarization

h_1 is chirally odd \rightarrow it needs a chirally odd partner

The "golden-gate" to transversity: h_1 from $\bar{p} \uparrow - p \uparrow$ Drell-Yan



Drell-Yan



$$\frac{d^2\sigma}{dM^2 dx_F} = \frac{4\pi\alpha^2}{9M^2 s} \frac{1}{x_1 + x_2} \sum_q e_q^2 \left[f_q(x_1) \bar{q}(x_2) + \bar{q}(x_1) q(x_2) \right]$$

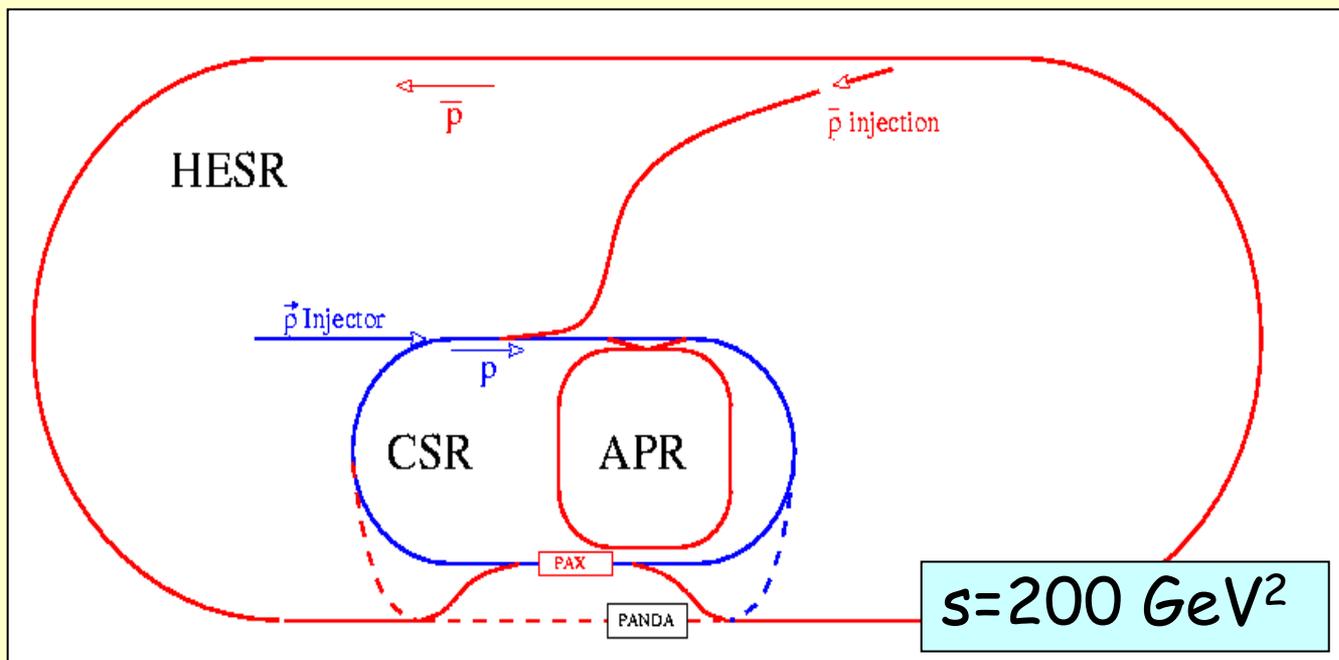
$q = u, \bar{u}, d, \bar{d}, \dots$

M invariant Mass of lepton pair

$$x_F = x_1 - x_2 \quad x_1 x_2 = M^2 / s \equiv \tau \quad x_F = 2Q_L / \sqrt{s}$$

$$A_{TT} = \frac{d\sigma^{\uparrow\uparrow} - d\sigma^{\uparrow\downarrow}}{d\sigma^{\uparrow\uparrow} + d\sigma^{\uparrow\downarrow}} = \hat{a}_{TT} \frac{\sum_q e_q^2 \left[h_{1q}(x_1) h_{1q}(x_2) + h_{1\bar{q}}(x_1) h_{1\bar{q}}(x_2) \right]}{\sum_q e_q^2 \left[f_q(x_1) q(x_2) + \bar{q}(x_1) \bar{q}(x_2) \right]}$$

PAX proposal: Phase II



EXPERIMENT:

Asymmetric collider:

polarized protons in HESR ($p=15 \text{ GeV}/c$)

polarized antiprotons in CSR ($p=3.5 \text{ GeV}/c$)

Luminosity: $1.5 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$

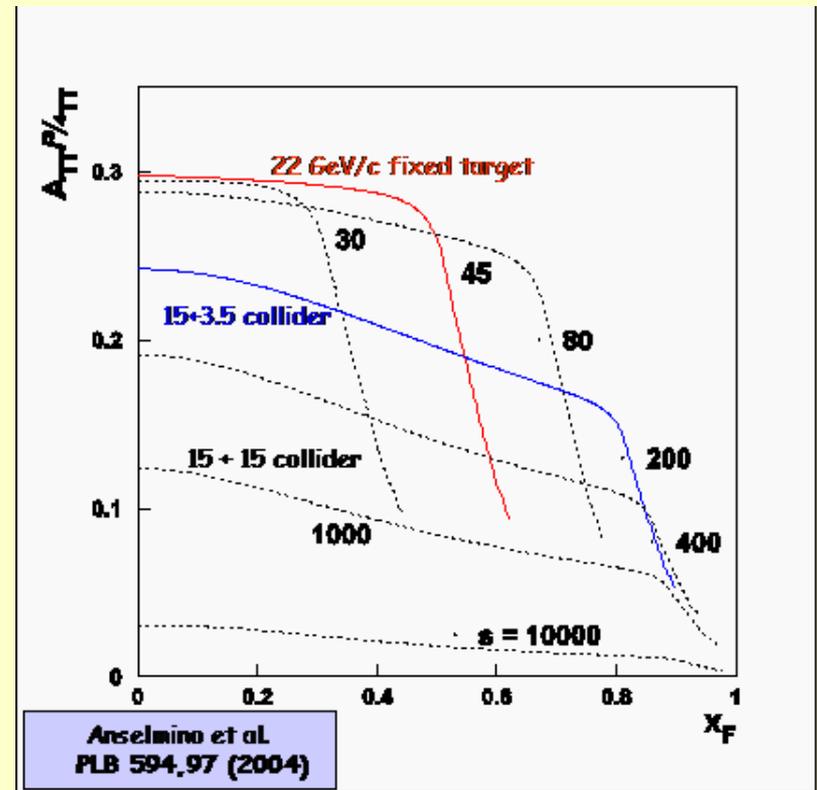
h_{1u} from $\bar{p}\uparrow - p\uparrow$ Drell-Yan at PAX

$$A_{TT} = \frac{d\sigma^{\uparrow\uparrow} - d\sigma^{\uparrow\downarrow}}{d\sigma^{\uparrow\uparrow} + d\sigma^{\uparrow\downarrow}} = \hat{a}_{TT} \frac{\sum_q e_q^2 [h_{1q}(x_1)h_{1q}(x_2) + h_{1\bar{q}}(x_1)h_{1\bar{q}}(x_2)]}{\sum_q e_q^2 [q(x_1)q(x_2) + \bar{q}(x_1)\bar{q}(x_2)]}$$

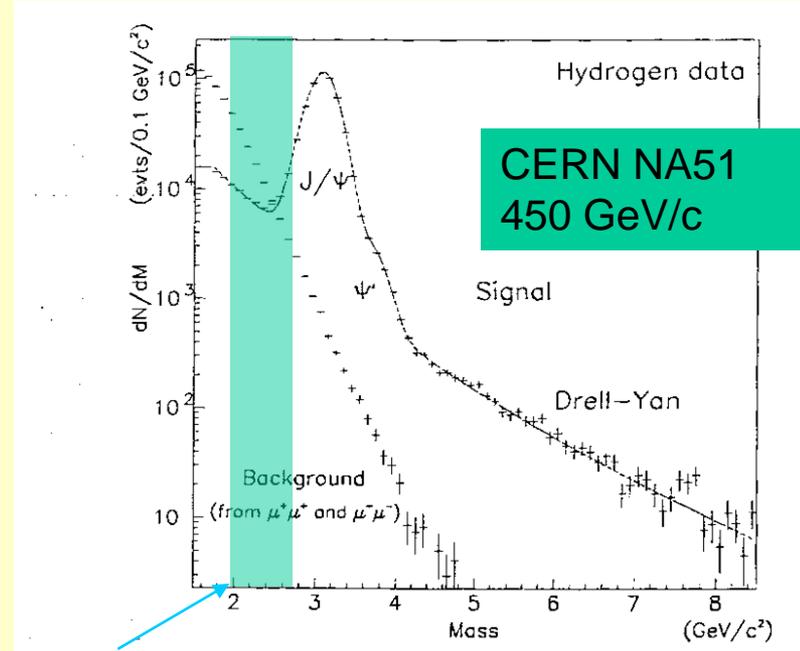
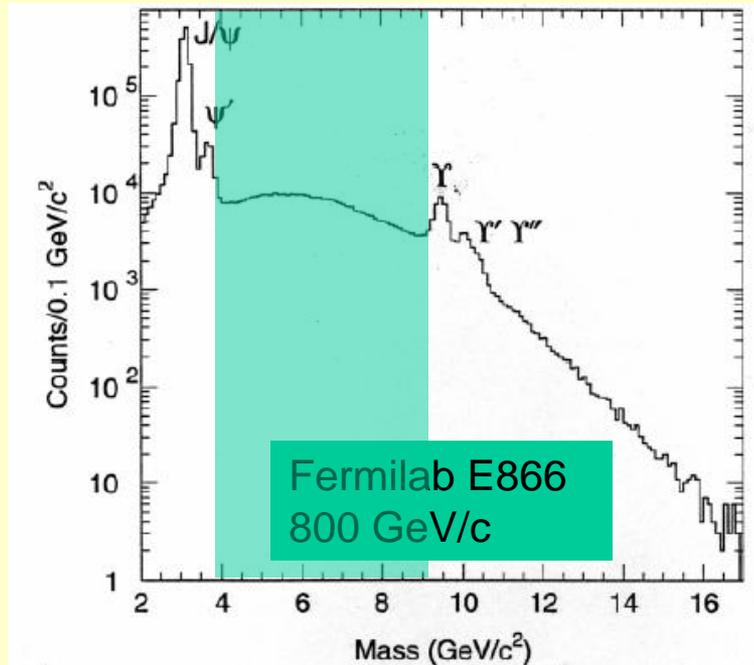
- u-dominance
- $|h_{1u}| > |h_{1d}|$

$$A_{TT} \approx \hat{a}_{TT} \frac{h_{1u}(x_1)h_{1u}(x_2)}{u(x_1)u(x_2)}$$

PAX : $M^2/s = x_1 x_2 \sim 0.02 - 0.3$
 valence quarks
 (A_{TT} large $\sim 0.2 - 0.3$)



Events for Drell-Yan processes



$$Q^2 > 4 \text{ GeV}^2$$

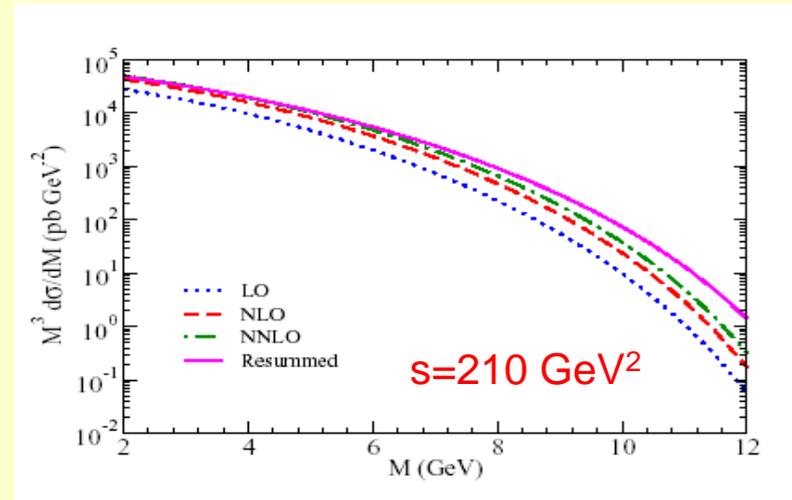
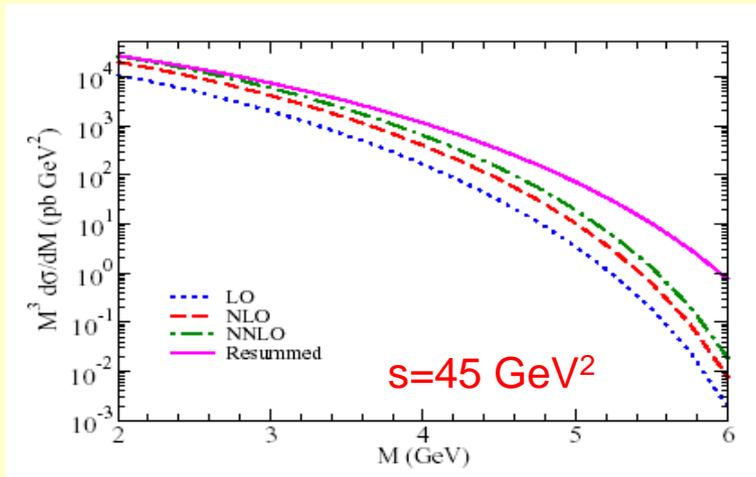
$$M \geq M_{J/\Psi}$$

Usually taken as "safe region"

$$\rightarrow \tau \geq \frac{M^2_{J/\Psi}}{S}$$

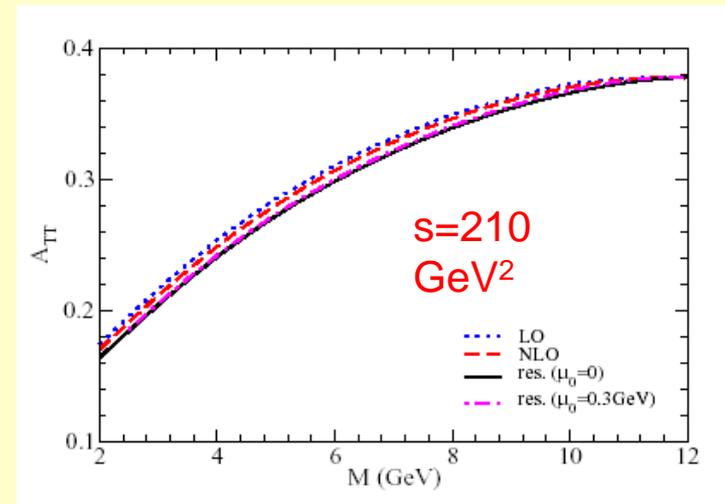
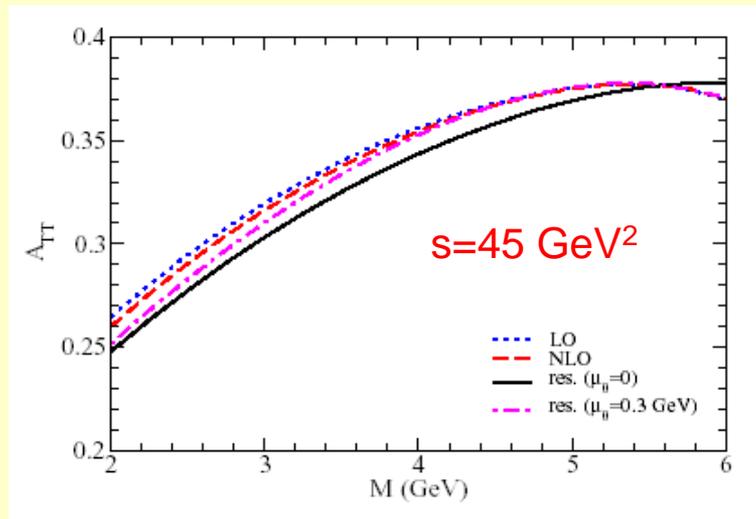
Radiative corrections

Cross-section



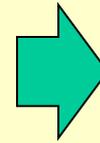
Asymmetry

Shimizu et al. PRD71 (2005) 114007



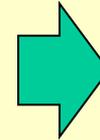
PAX Detector Concept

Physics: h_1 distribution $\sin^2\theta$
EMFF $\sin 2\theta$
pbar-p elastic high $|t|$



Azimuthally Symmetric:
BARREL GEOMETRY
LARGE ANGLES

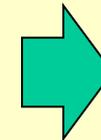
Experiment: Flexible Facility



e^+e^-

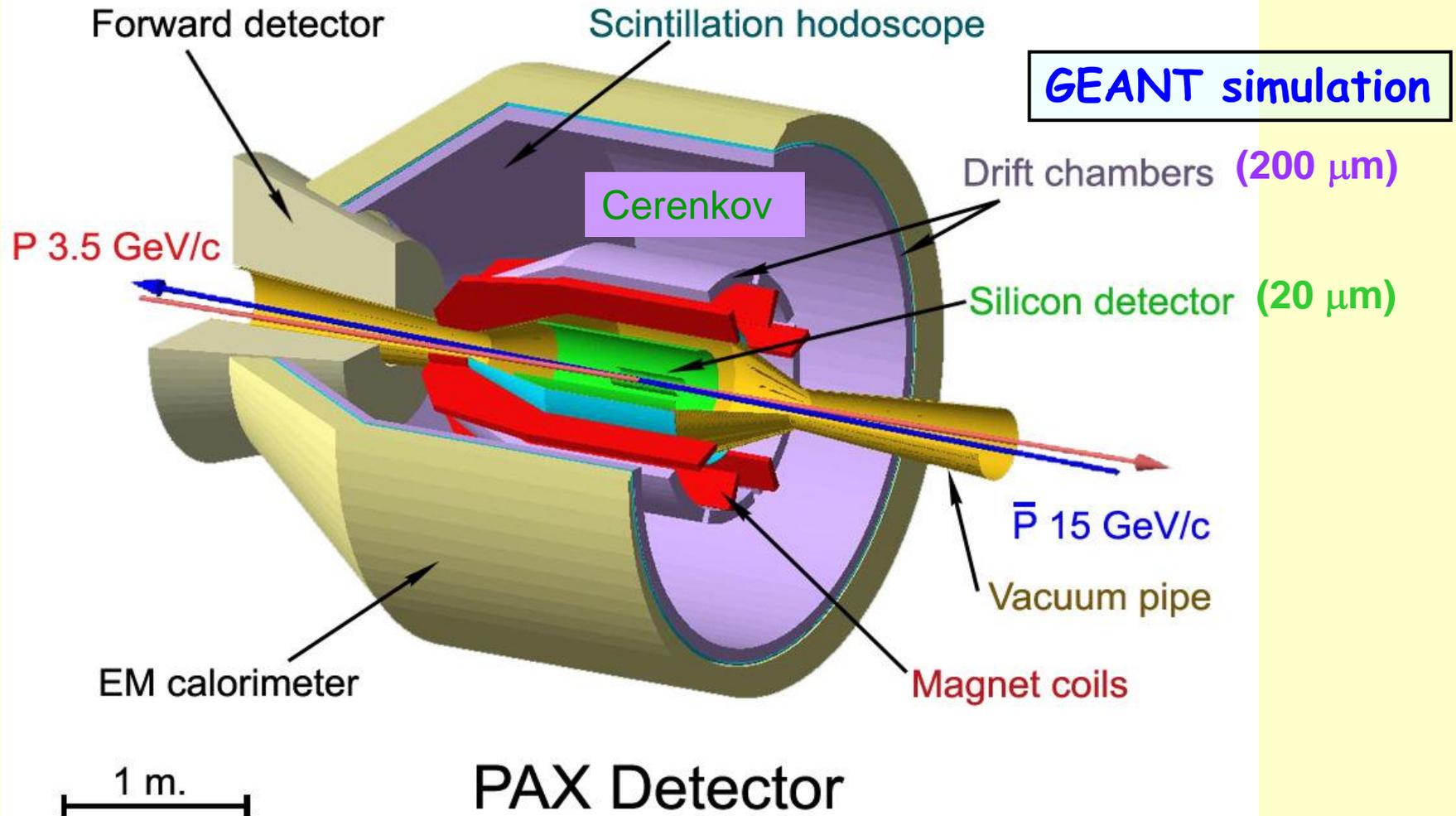
Detector: Extremely rare DY signal (10^{-7} p-pbar)
Maximum Bjorken-x coverage (M interval)
Excellent PID (hadron/e rejection $\sim 10^4$)
High mass resolution ($\leq 2\%$)
Moderate lepton energies (0.5-5 GeV)

Magnet: Keeps beam polarization vertical
Compatible with Cerenkov
Compatible with pol. target



TOROID
NO FRINGE FIELD

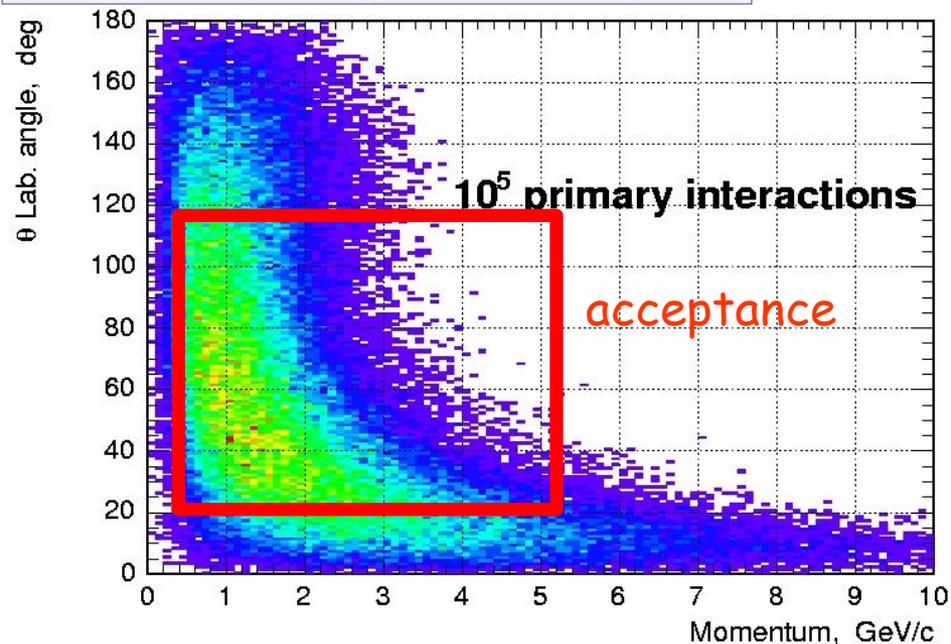
PAX Detector Concept



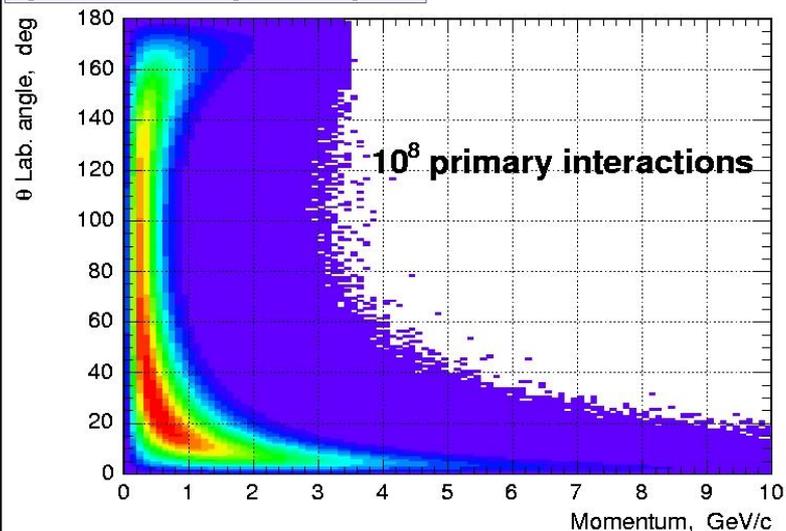
Designed for Collider but compatible with fixed target

θ -p Phase Space

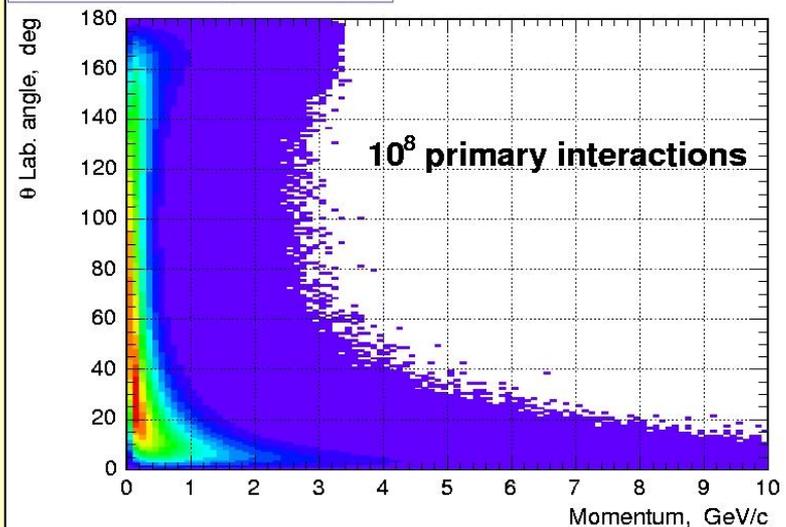
p vs θ for primary Drell-Yan leptons



p vs θ for primary π^\pm



p vs θ for primary γ

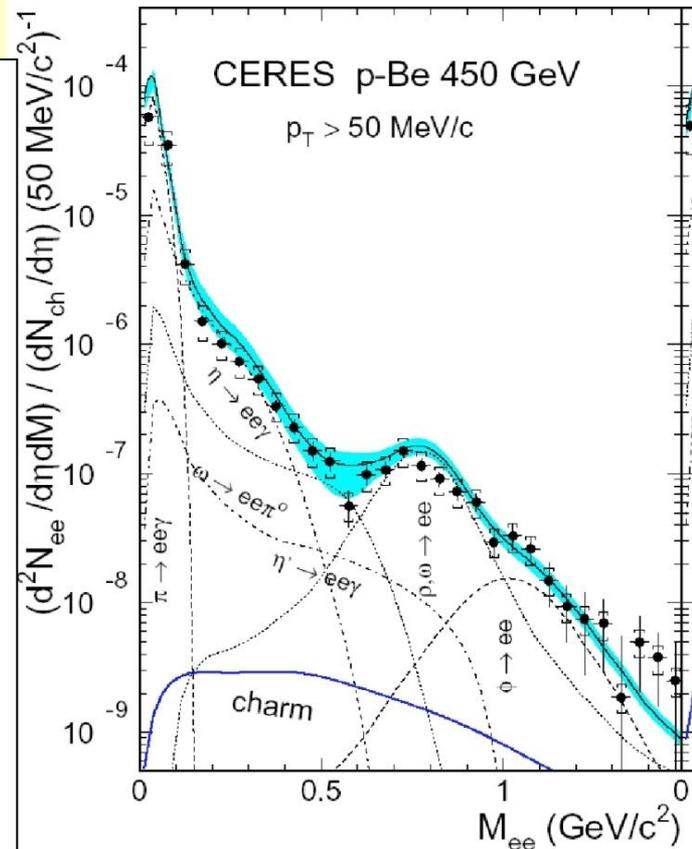
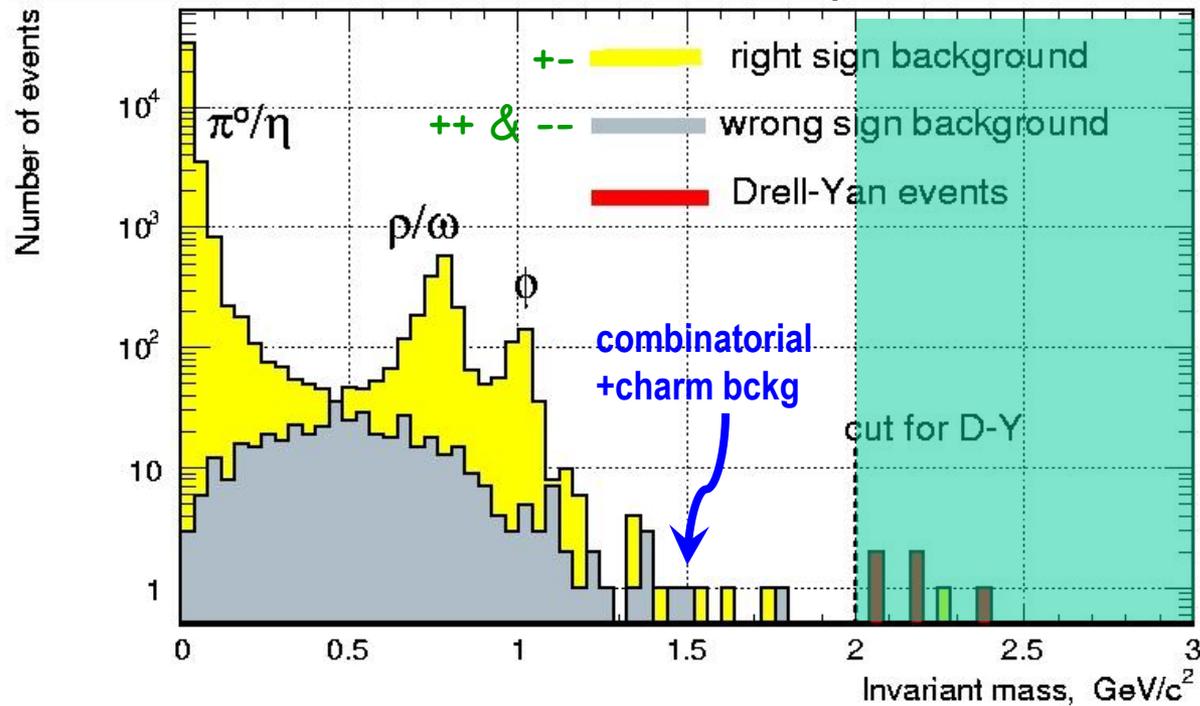


Background peaks at
* low energy
* forward direction

Background to Drell-Yan e^+e^-

10 min. experiment: $2 \cdot 10^8$ p-pbar interactions
several DY events

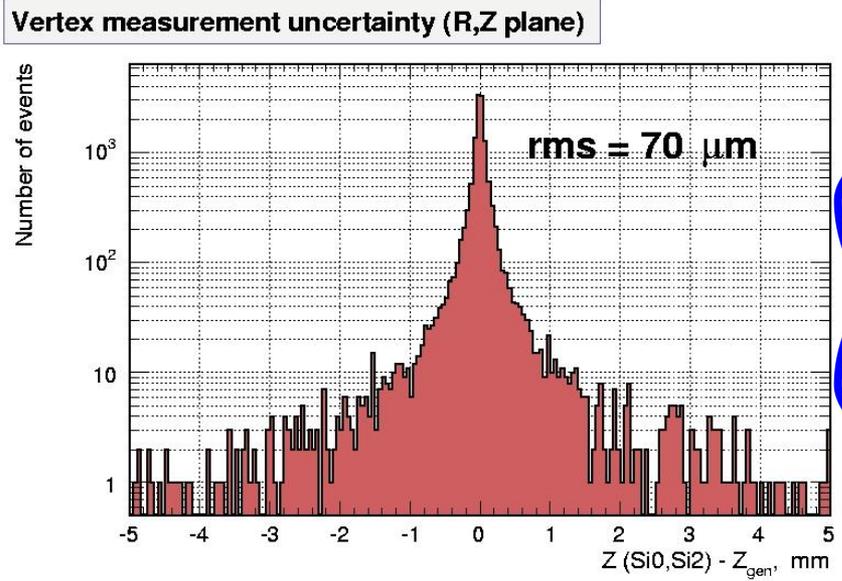
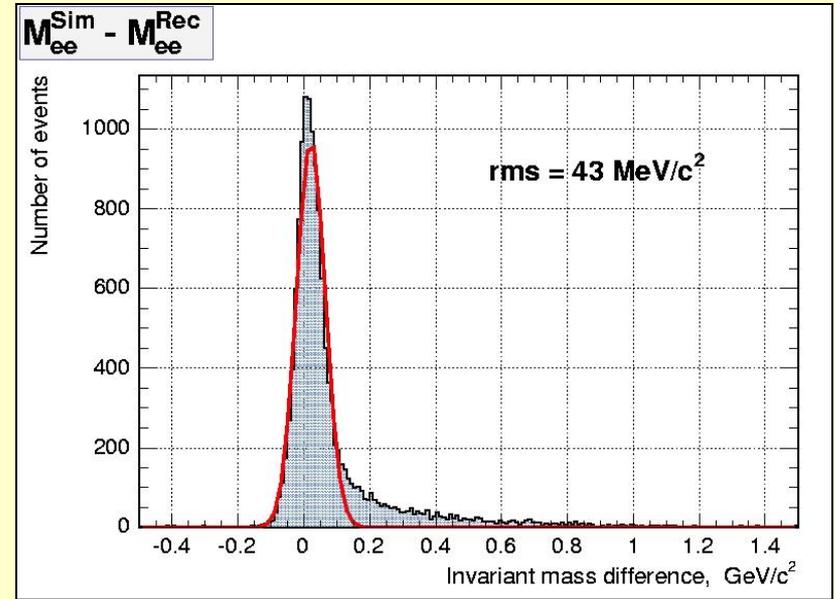
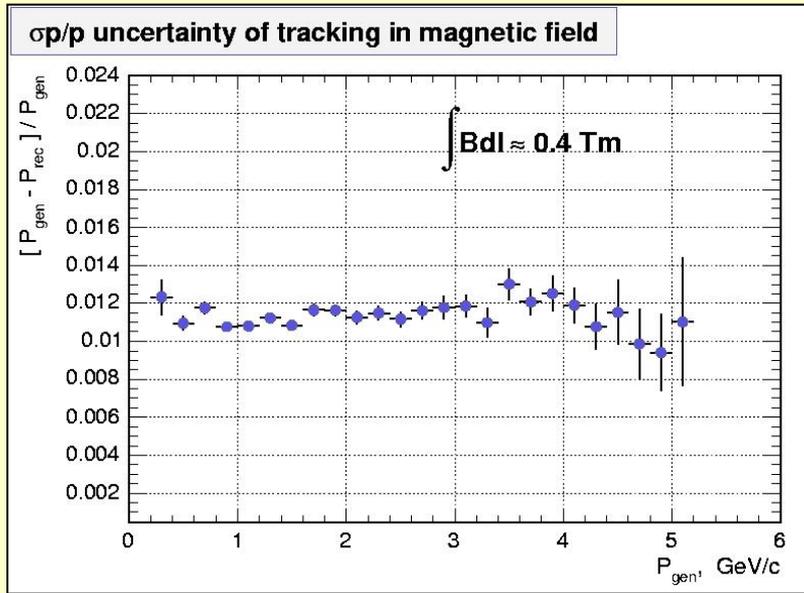
Invariant mass of ee pair



Background 1:1 to signal after PID, $E > 300 \text{ MeV}$, conversion veto, mass cut

- * the combinatorial component can be subtracted (wrong-sign control sample)
- * the charm can be reduced (vertex decay)

Resolution



Better than 2% mass resol
 * x dependence of h_1
 * resonance vs continuum

Mandatory to study M below J/ψ mass

Vertex resolution high enough to study charm background

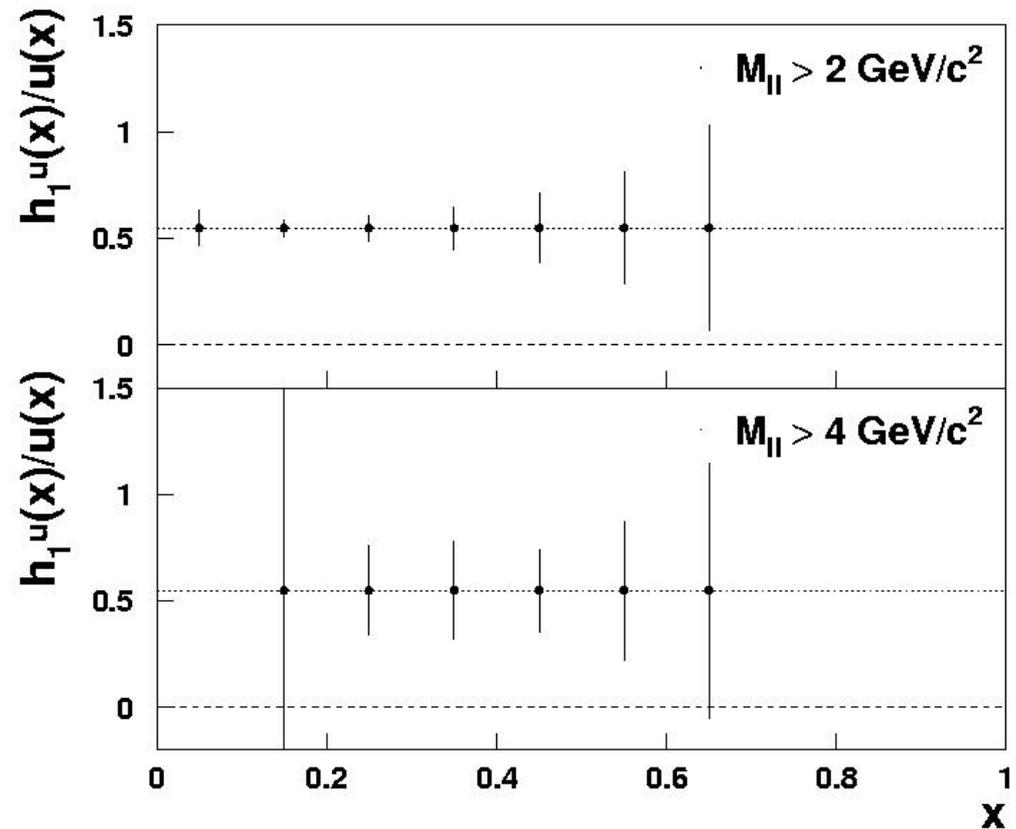
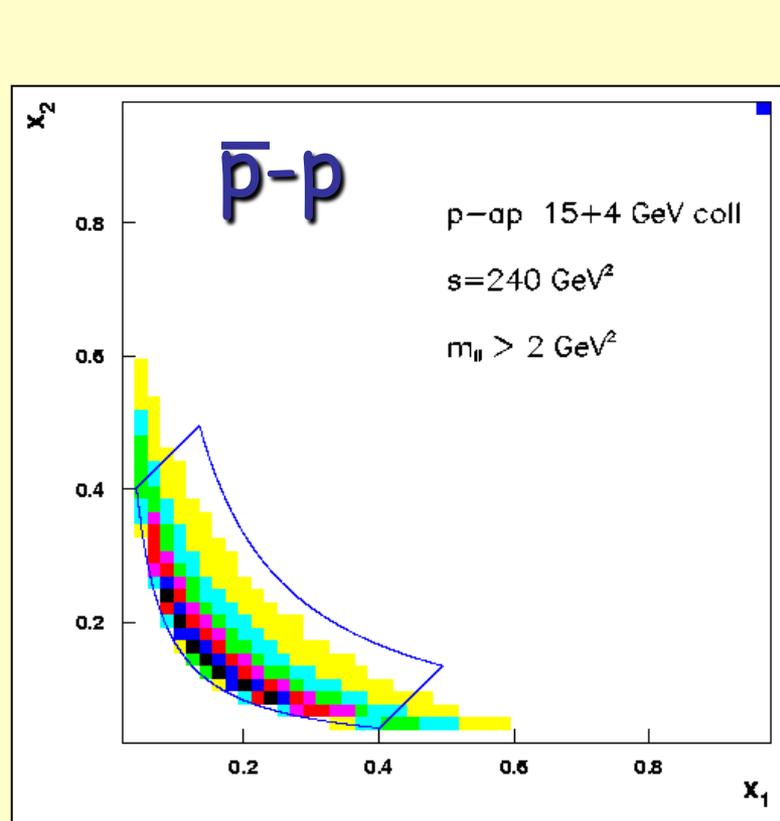
Precision in h_1 measurement

1 year of data taking at 15+3.5 GeV collider

$L = 1.5 \cdot 10^{31} \text{ cm}^{-2}\text{s}^{-1}$

$p \uparrow = 0.8$

$p\bar{b} \uparrow = 0.15$



10 % precision on the $h_1^u(x)$ in the valence region

More statistics from J/ Ψ ...

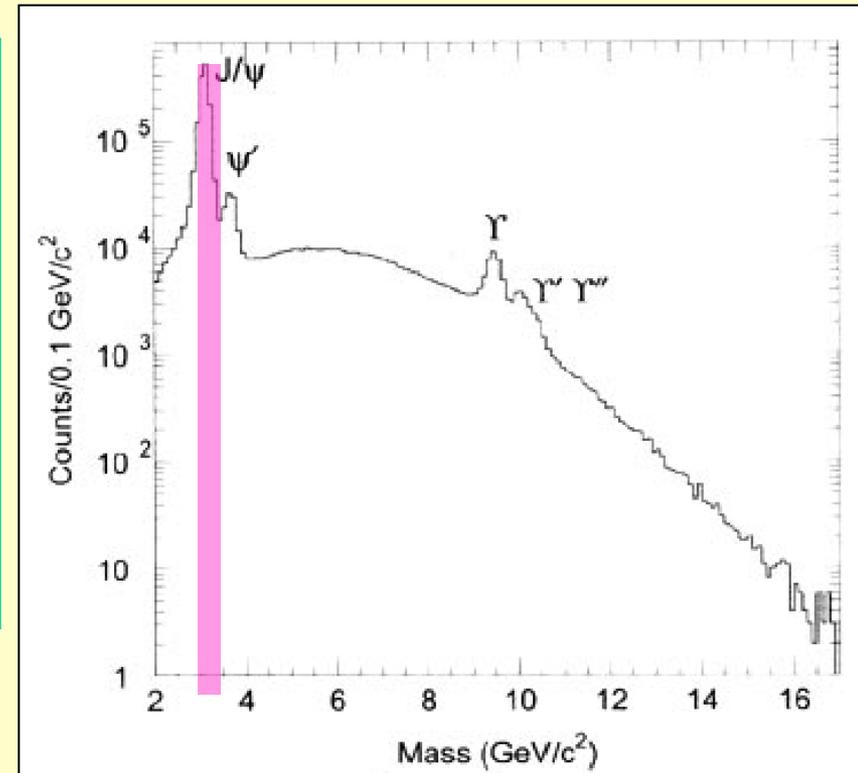
$$q\bar{q} - J/\Psi$$

→ unknown vector coupling,
but same Lorentz
and spinor structure
as other two processes

$$q\bar{q} - \gamma^*$$

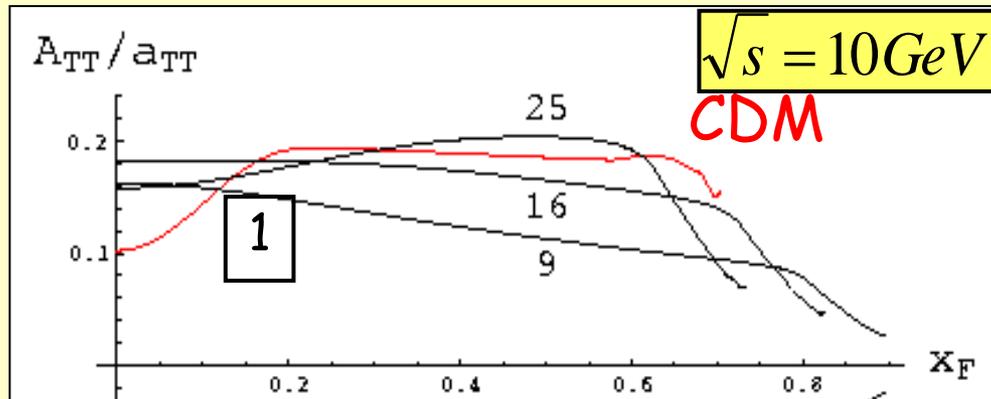
$$q\bar{q} - e^+e^-$$

Unknown quantities cancel
in the ratios for A_{TT} , but
helicity structure remains!



Expected to double the statistics → Good mass resolution fundamental

What about p-p?



A. Drago (2006)

(Asymmetry evolved under the assumption: $h_{1q}^-(x, Q_0^2) = \Delta \bar{q}(x, Q_0^2)$)

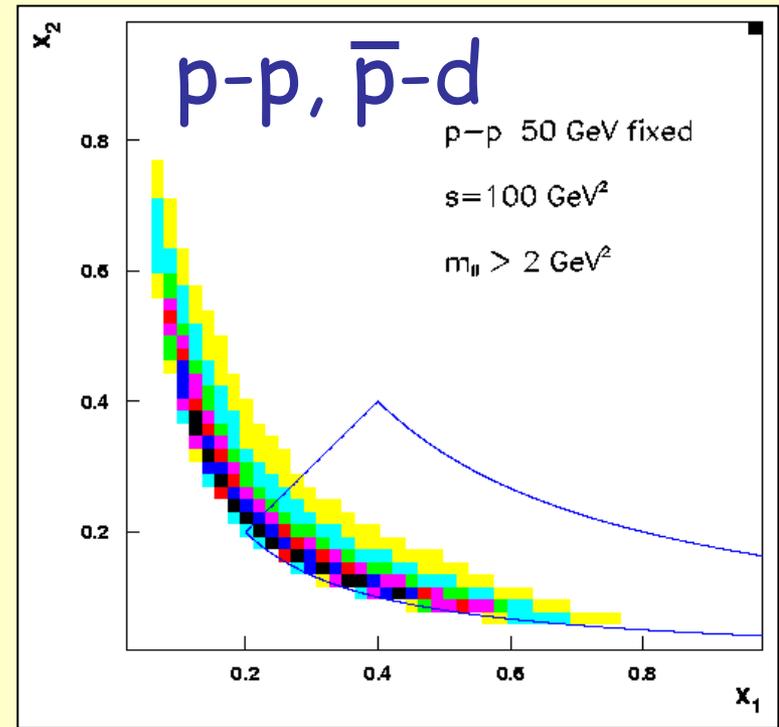
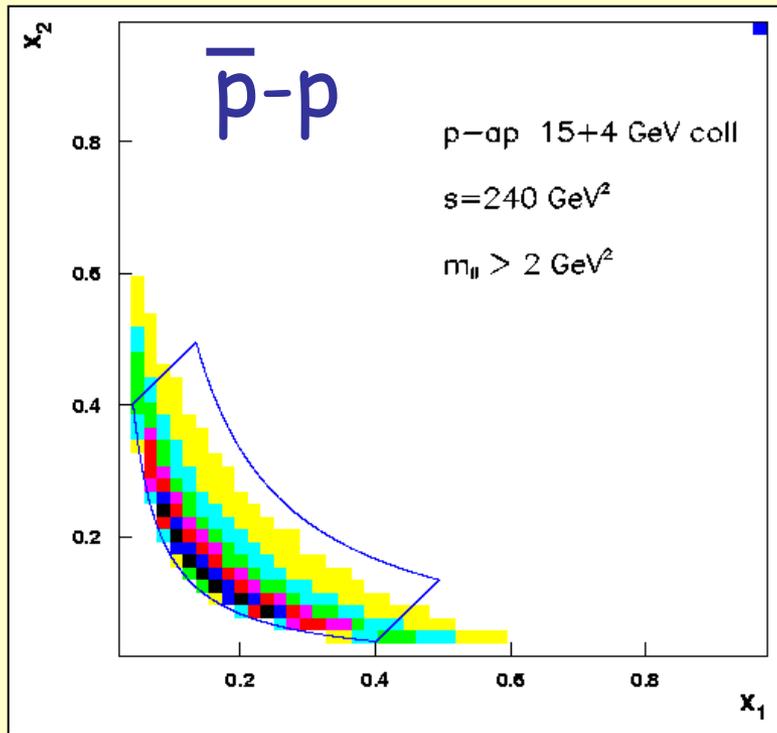
Asymmetries are estimated to be large at PAX energies \rightarrow access to $h_{1u}^-(x)$

RHIC: $\tau = x_1 x_2 \sim 10^{-3} \rightarrow$ sea quarks $(A_{TT} \sim 0.01)$

JPARC/U70: $\tau = x_1 x_2 \sim 10^{-1} \rightarrow$ valence and sea $(A_{TT} \sim 0.1)$

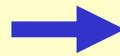
PAX: $\tau = x_1 x_2 \sim 10^{-1} \rightarrow$ valence and sea $(A_{TT} \sim 0.1)$

DY events distribution ($p \uparrow \bar{p} \uparrow$, $p \uparrow p \uparrow$ and $\bar{p} \uparrow d \uparrow$)



$$M^2/s = x_1 x_2 \sim 0.02-0.3$$

At $x_1=x_2$ $A_{TT} \sim h_{1u}^2$
 Direct measurement of h_{1u}
 for $0.05 < x < 0.5$



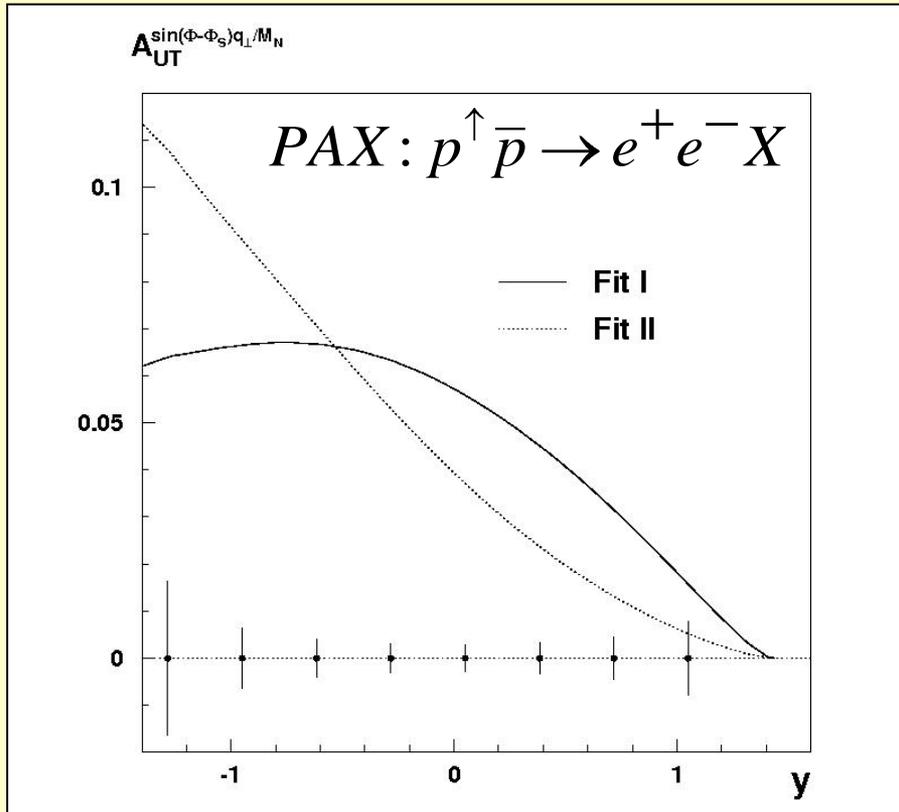
Extraction of $h_{1d}, h_{1\bar{q}}$
 for $x < 0.2$

$\bar{p} \uparrow p \uparrow, p \uparrow p \uparrow, \bar{p} \uparrow d \uparrow$: complete mapping of transversity

Single spin asymmetries: Sivers function from $p\bar{p} \rightarrow p\bar{p} \gamma$ or $p\bar{p} \rightarrow p\bar{p} \gamma$ Drell-Yan @ PAX

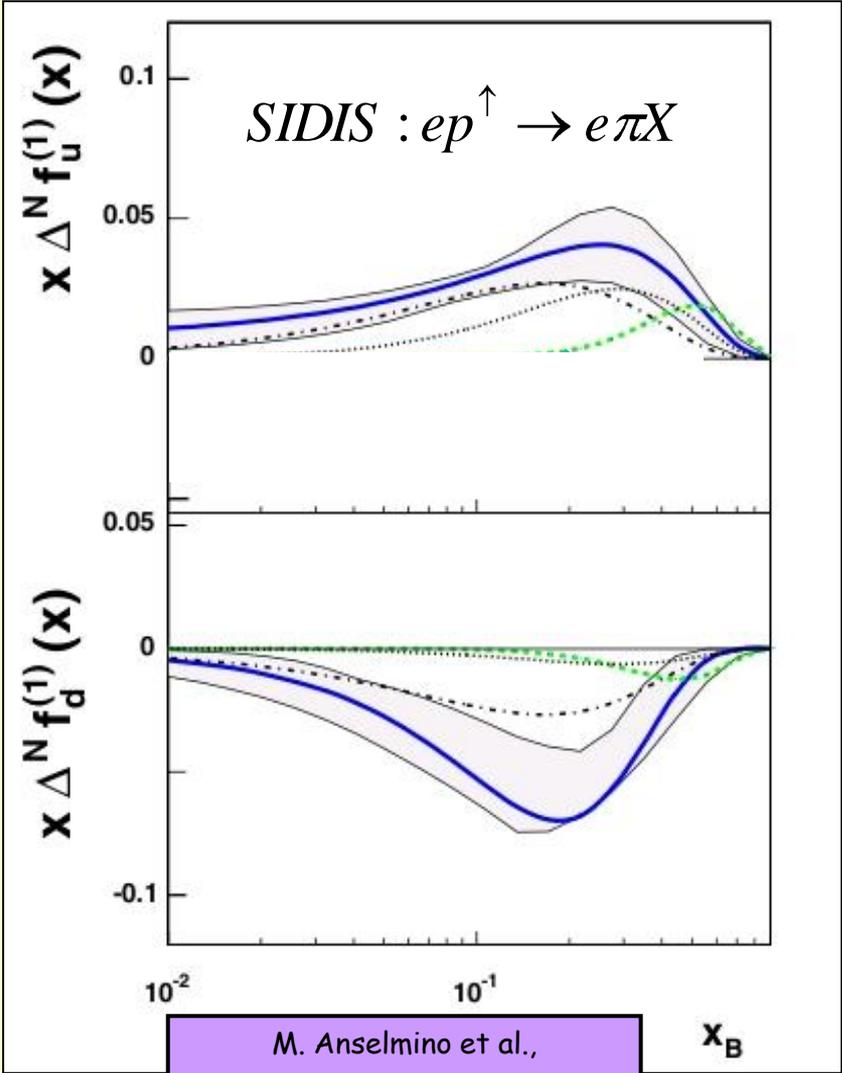
Test of Universality

$$f_{1T}^\perp(x, p_T^2)_{SIDIS} = -f_{1T}^\perp(x, p_T^2)_{DY}$$



A.V. Efremov et al.,
Phys. Lett. B 612, 233 (2005)

$$x_{1/2} = \sqrt{M^2 / s} e^{\pm y}$$

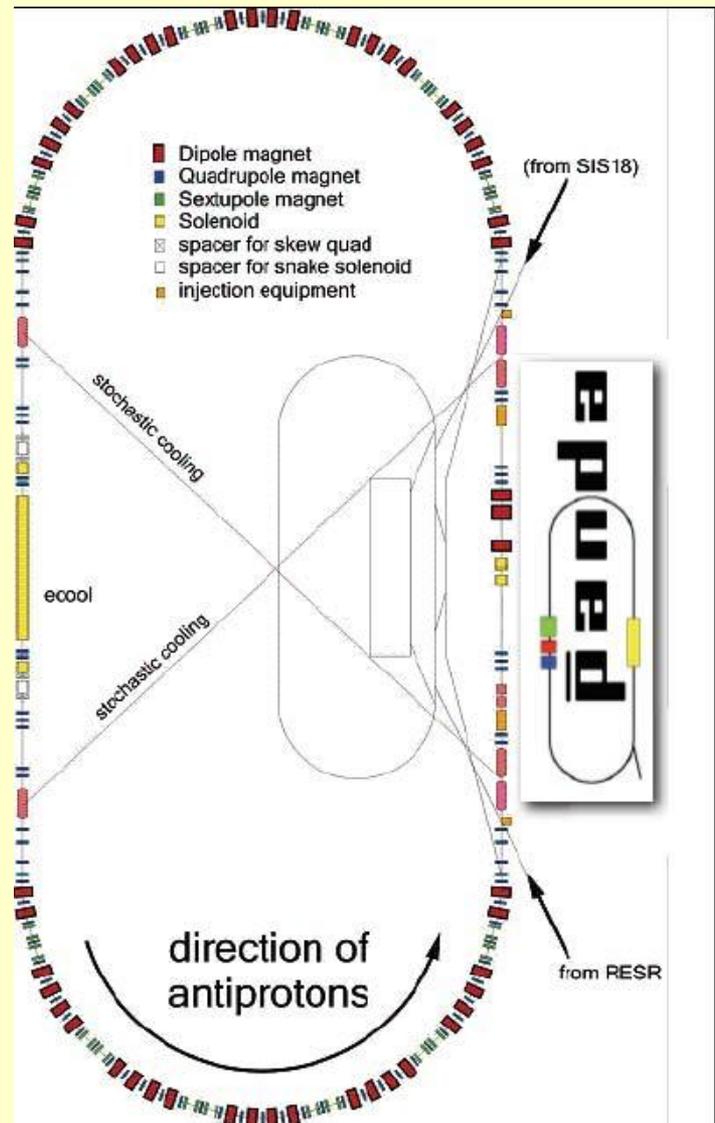


M. Anselmino et al.,
Phys. Rev. D72, 094007 (2005)

Fixed target experiments

DY measurements @ PANDA

- antiproton momentum
 $1.5 \text{ GeV}/c < p < 15 \text{ GeV}/c$
- Stochastic and electron cooling: $\Delta p/p < 10^{-5}$
- Luminosity $> 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$
- Hydrogen pellet or jet target, polarised Hydrogen under study
- Variety of nuclear targets



Measurement of Transversity

	non-TMD	TMD
self-sufficient	$\bar{p}^\uparrow p^\uparrow \rightarrow \ell \bar{\ell} X$ $p^\uparrow p^\uparrow \rightarrow (\text{high-}p_T \text{ jet}) X$	$p\bar{p}^\uparrow \rightarrow \ell \bar{\ell} X$ $\bar{p}p^\uparrow \rightarrow \ell \bar{\ell} X$
needs e^+e^-	$pp^\uparrow \rightarrow \Lambda^\uparrow X$ $ep^\uparrow \rightarrow e' \Lambda^\uparrow X$ $pp^\uparrow \rightarrow (\pi^+ \pi^-) X$ $ep^\uparrow \rightarrow e' (\pi^+ \pi^-) X$	$ep^\uparrow \rightarrow e' \pi X$

D. Boer, Ferrara (2008)

- There is only a single self-sufficient process with a single polarized beam
- Single spin-asymmetry in $\bar{p}^\uparrow p$ or $p\bar{p}^\uparrow$ Drell-Yan

A "window" to transversity: $p\bar{p} \rightarrow l^+l^- X$

Only self-sufficient single spin-asymmetry (involves TMDs)

Unpolarized DY production cross-section

$$d\sigma^{DY} \propto \bar{h}_1^\perp(x_1, k_{T1}^2) \otimes h_1^\perp(x_2, k_{T2}^2) \cos 2\phi$$

↑ Boer-Mulders ↑

→ analogue of BELLE $\cos 2\phi$ asymmetry

Single-polarized DY production cross-section

$$d\sigma^{DY} \propto \bar{f}_1(x_1, k_{T1}^2) \otimes f_{1T}^\perp(x_2, k_{T2}^2) \sin(\phi - \phi_{S2}) +$$

↑ Sivers

$$+ \bar{h}_1^\perp(x_1, k_{T1}^2) \otimes h_1(x_2, k_{T2}^2) \sin(\phi + \phi_{S2}) +$$

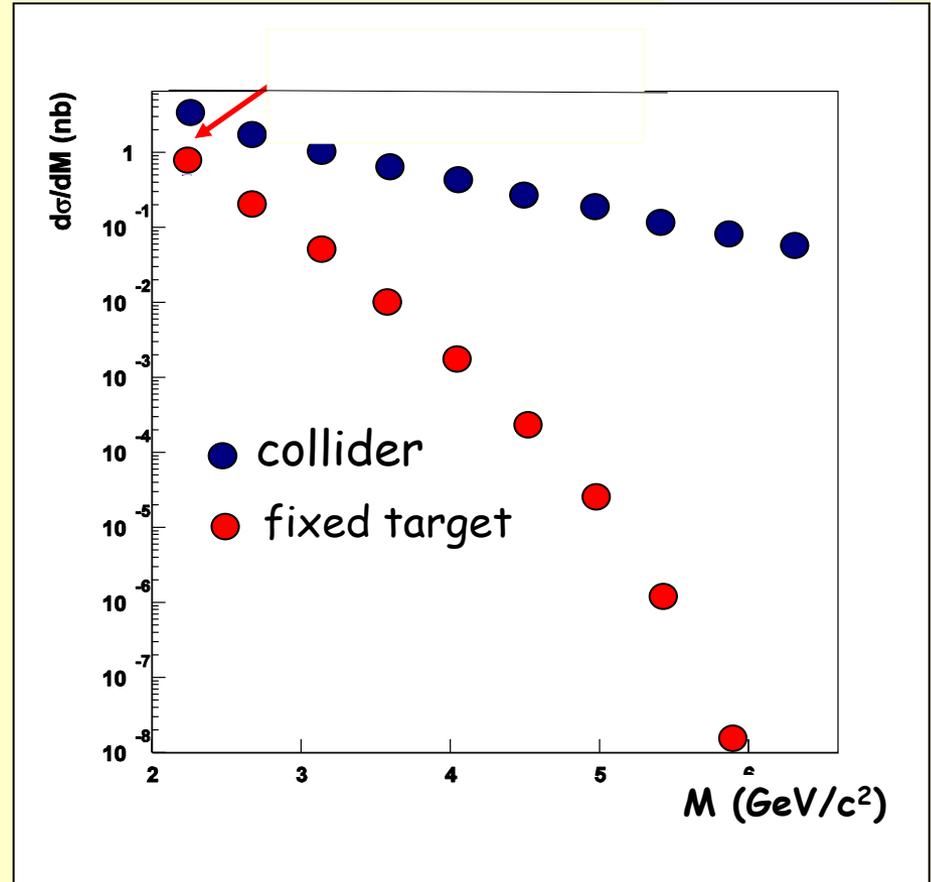
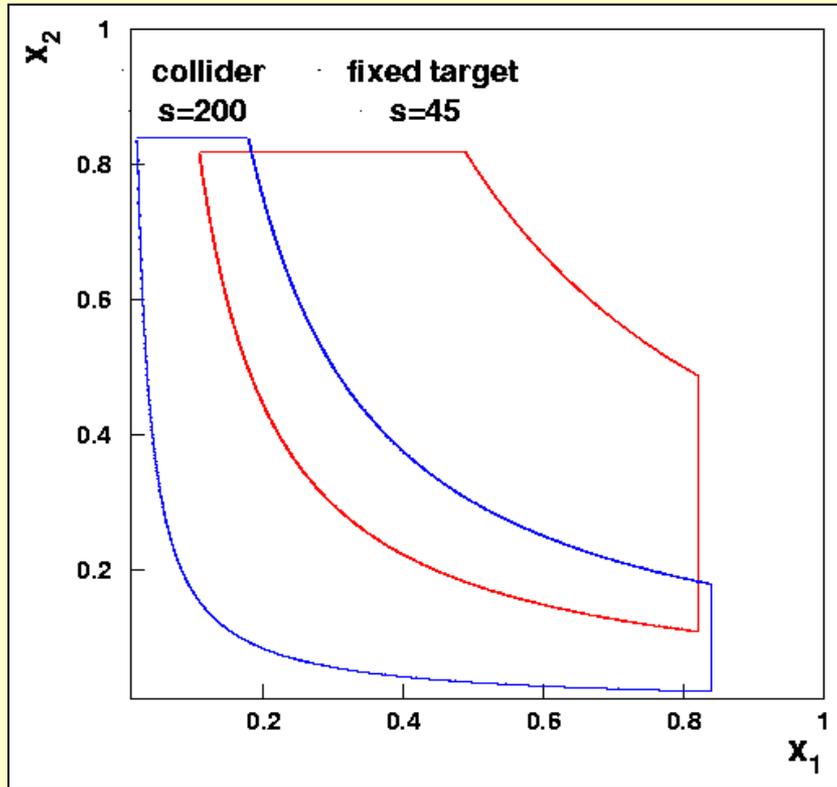
↑ Boer-Mulders ↑ Transversity

→ analogue of SIDIS Collins asymmetry

Kinematics and cross section

$$\frac{d^2\sigma}{dM^2 dx_F} = \frac{4\alpha^2\pi}{9M^2 s(x_1 + x_2)} \cdot \sum_q e_q^2 \left[\langle \bar{q}(x_1, M^2) q(x_2, M^2) \rangle + q \langle q(x_1, M^2) \bar{q}(x_2, M^2) \rangle \right]$$

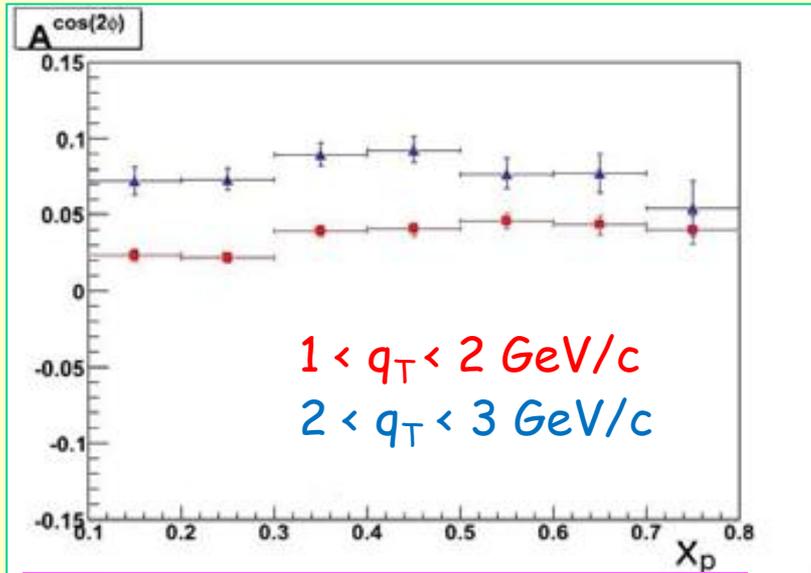
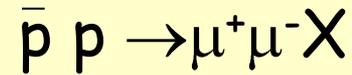
- $M^2 = s x_1 x_2$
- $x_F = 2Q_L / \sqrt{s} = x_1 - x_2$



DY@PANDA: MC - Simulations I

A. Bianconi NIM A593, 562 (2008)

Unpolarized case:



5×10^5 events

$1.5 < M_{\mu^+ \mu^-}^2 < 2.5 \text{ GeV}^2$
 $q_T > 1 \text{ GeV}/c$
 $60^\circ < \theta_{\mu^+}^{CS} < 120^\circ$

Luminosity = $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
 $\sigma = 0.8 \text{ nb}$
Rate = 0.16 s^{-1}

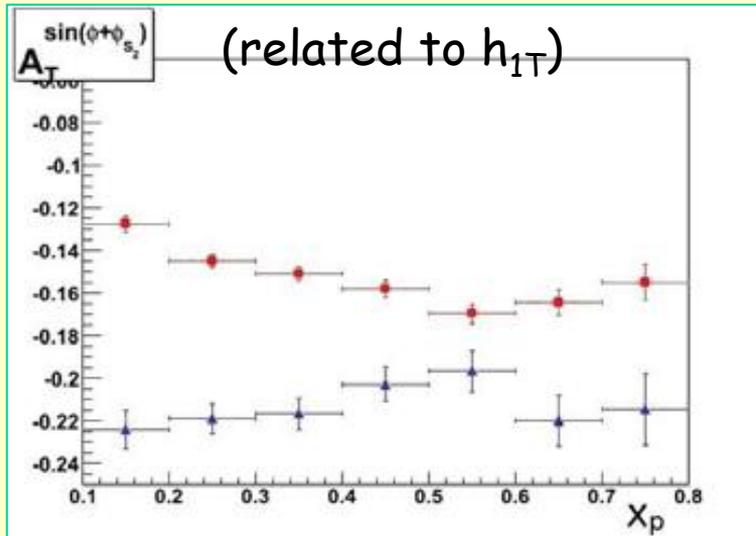
M. Maggiora Univ. Torino and INFN (I)

DY@PANDA: MC - Simulations II

A. Bianconi, M. Radici Phys. Rev. D71, 074014 (2005)

Single-spin asymmetry:

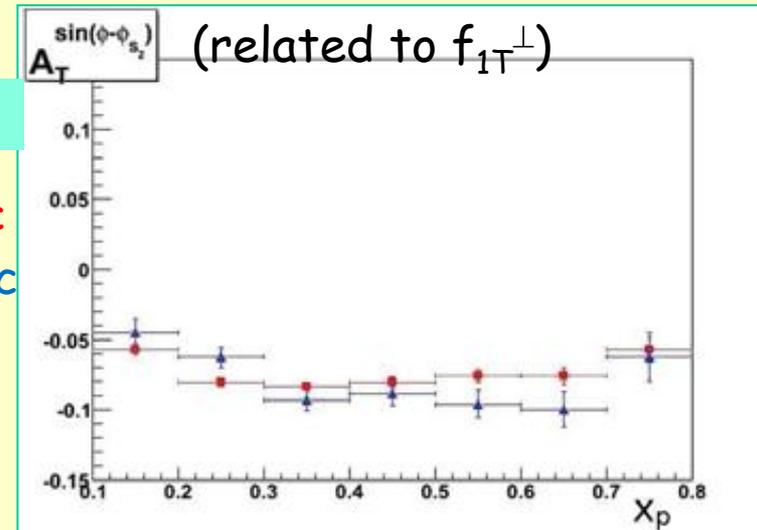
$$\bar{p} p \uparrow \rightarrow \mu^+ \mu^- X$$



5×10^5 events

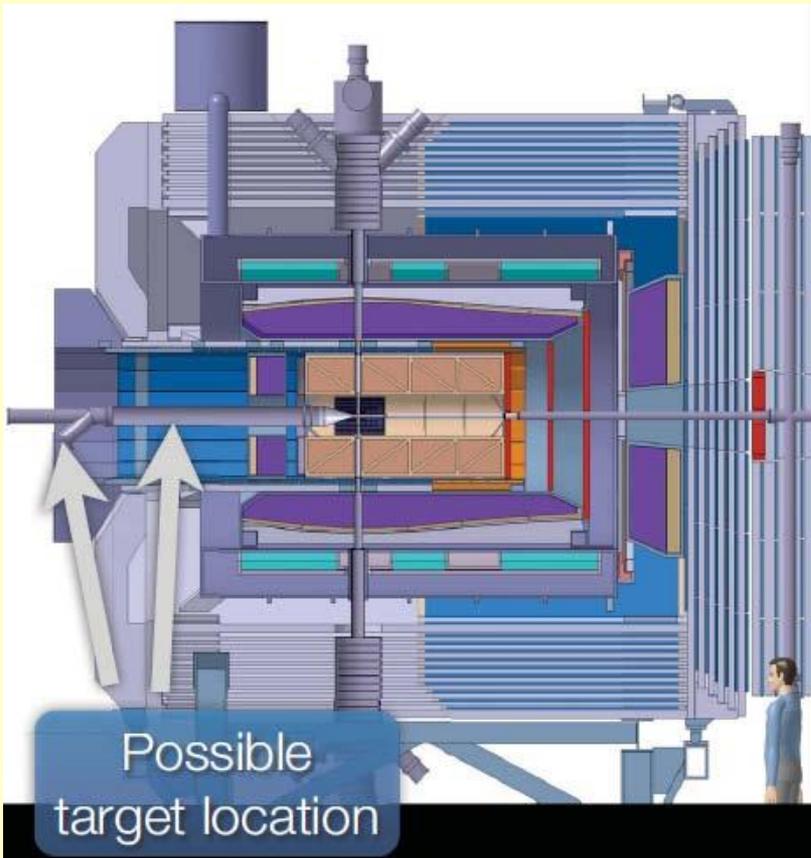
$1 < q_T < 2 \text{ GeV}/c$

$2 < q_T < 3 \text{ GeV}/c$



A polarized target in PANDA?

A very difficult task!



Positioning:

- Keep good PID for EM physics
- No parasitic run possible

Technical issues:

- Transport of polarized gas
- Compensation of solenoidal field
- Pumping of polarized gas

Possible options:

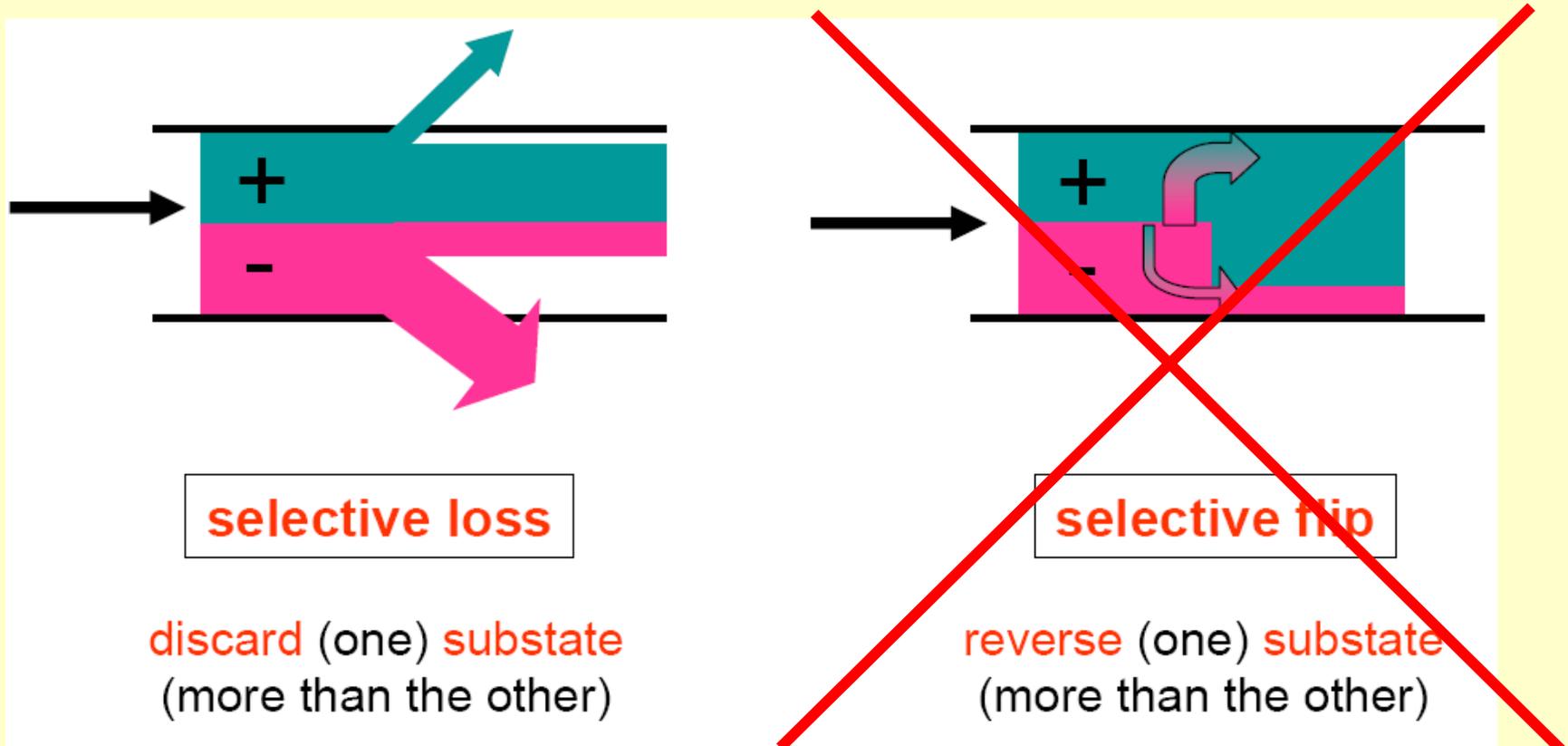
- new detector with thoroidal field?
- additional IP in HESR?

Status of polarized antiproton-studies

Polarized Antiprotons.

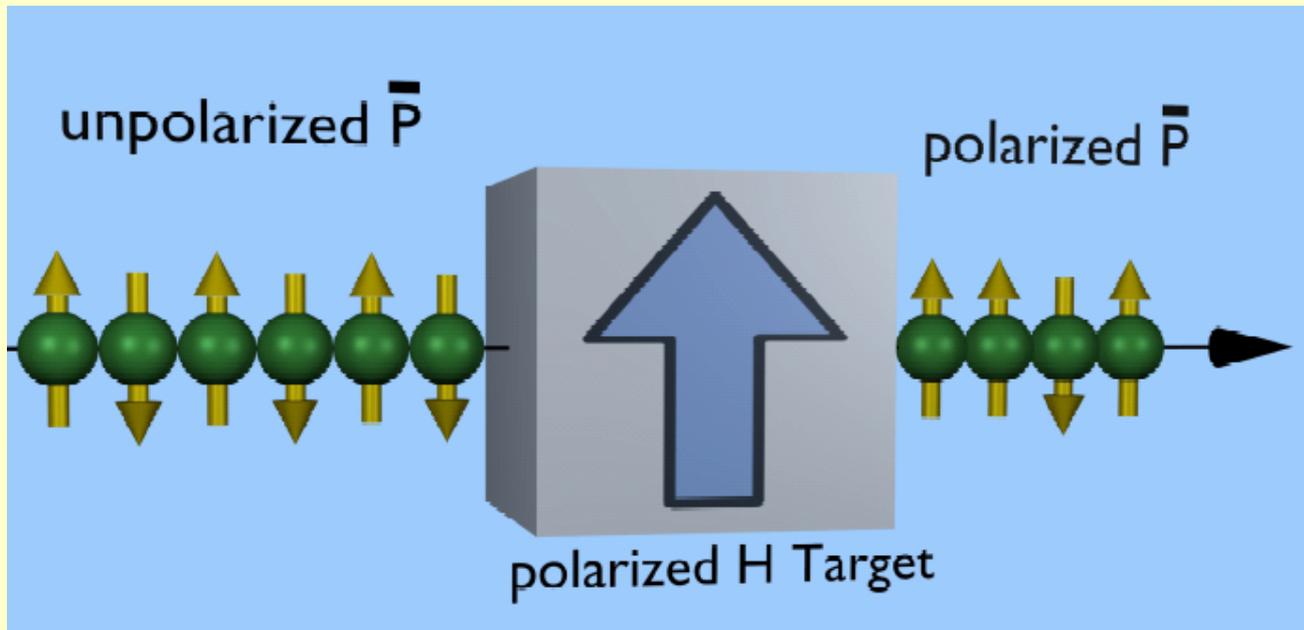
Two Methods: Loss versus spin flip

For an ensemble of spin $\frac{1}{2}$ particles with projections + (\uparrow) and - (\downarrow)

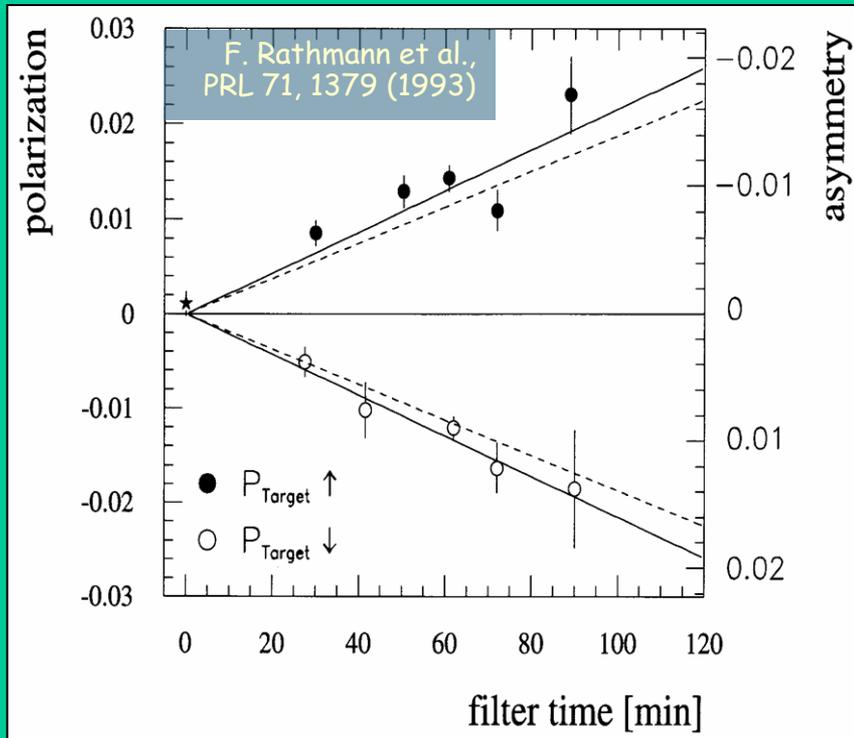


Spin-filtering

Polarization build-up of an initially unpolarized particle beam by repeated passage through a polarized hydrogen target:



Spin-filtering at TSR: „FILTEX“ - proof-of-principle



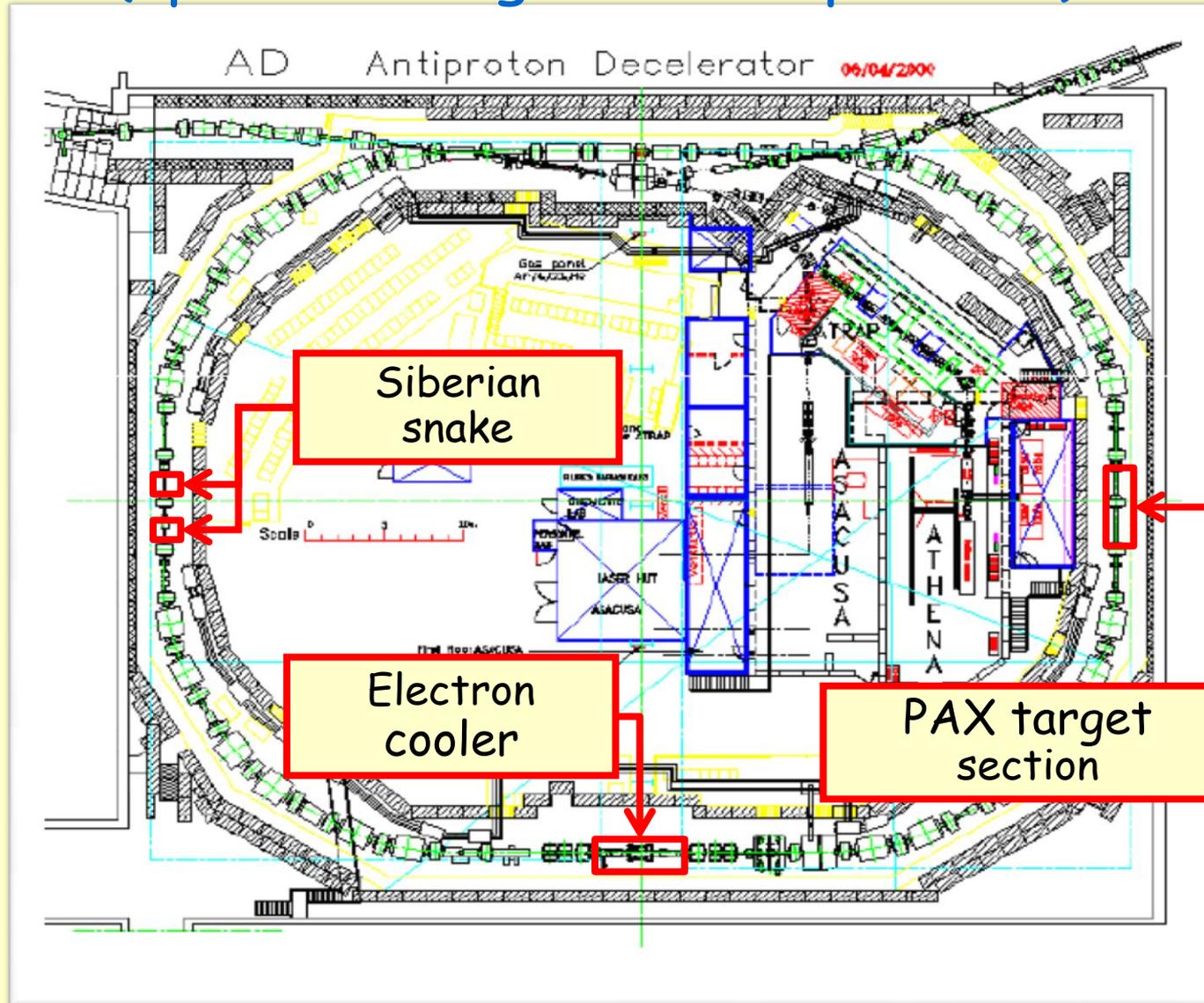
→ Spin filtering works for protons!

Polarization buildup process **quantitatively** understood!

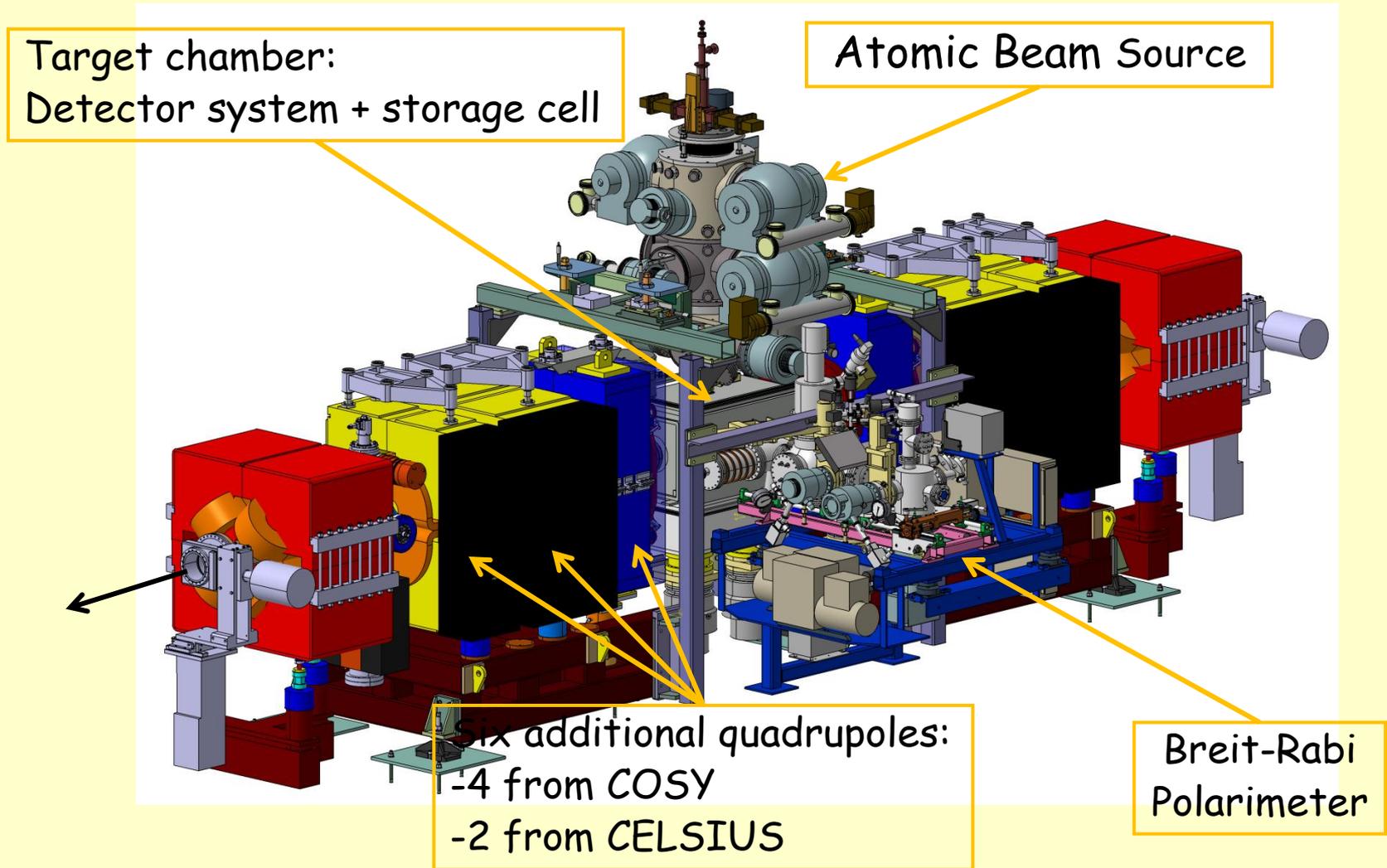
- TSR spin filtering with protons:
 $\sigma^{\text{exp}} = 73 \pm 6 \text{ mb}$
- Average theoretical value:
 $\sigma^{\text{theo}} = 86 \pm 2 \text{ mb}$
- Brief summary in: D. Oellers et al., Phys. Lett. B 674, 269 (2009).

PAX submitted new proposal to find out how well spin filtering works for antiprotons (CERN-SPSC-2009-012 / SPSC-P-337)

PAX at the CERN-AD (spin filtering with antiprotons)



Experimental Setup for AD



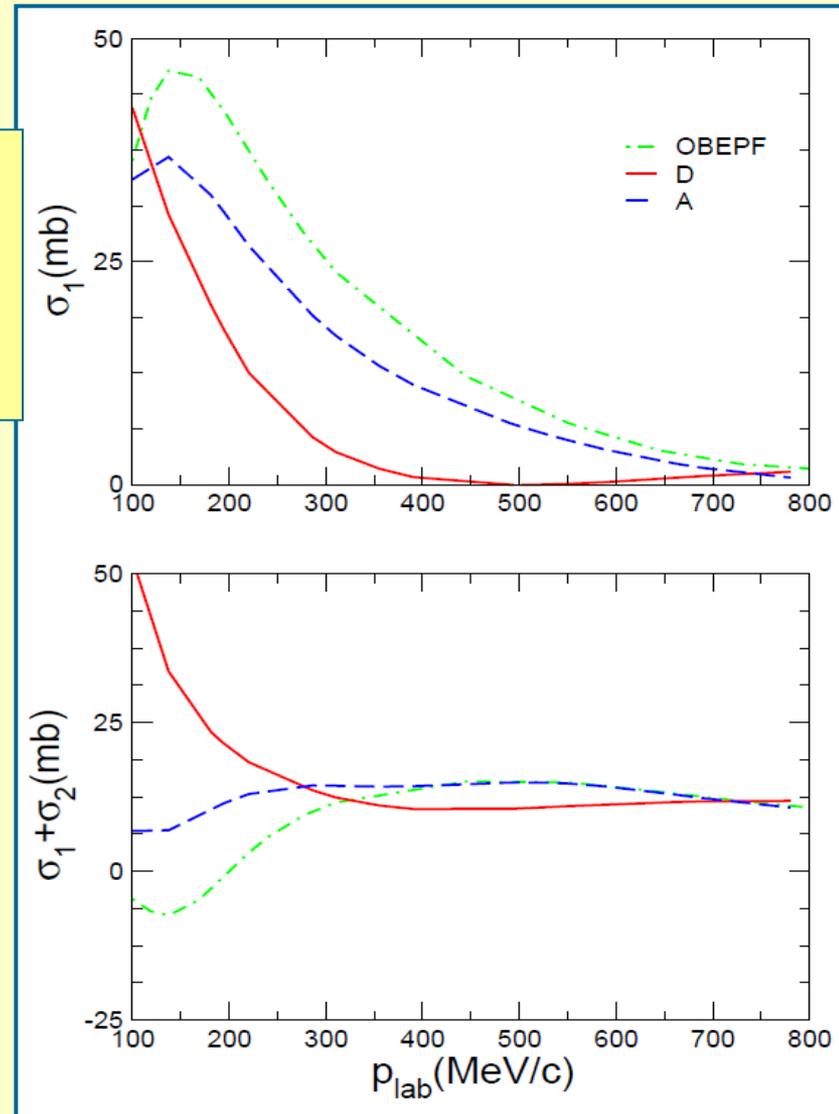
Spin-dependence of the pbar-p interaction

- Measurement of the polarization buildup equivalent to the determination of σ_1 and σ_2
- Once a polarized antiproton beam is available, spin-correlation data can be measured at AD (50-500 MeV)

Model A: T. Hippchen et al., Phys. Rev. C 44, 1323 (1991).

Model OBEPF: J. Haidenbauer, K. Holinde, A.W. Thomas, Phys. Rev. C 45, 952 (1992).

Model D: V. Mull, K. Holinde, Phys. Rev. C 51, 2360 (1995).



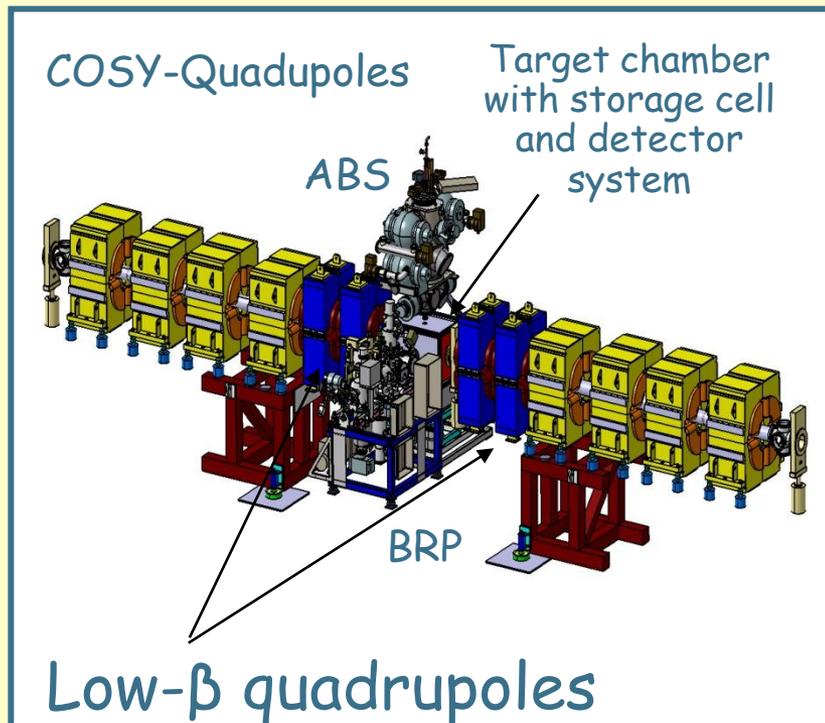
Spin-filtering studies at COSY- FZJ-Germany

Main purpose:

1. Confirm understanding of spin-filtering with protons.
2. Commissioning of the experimental setup for AD

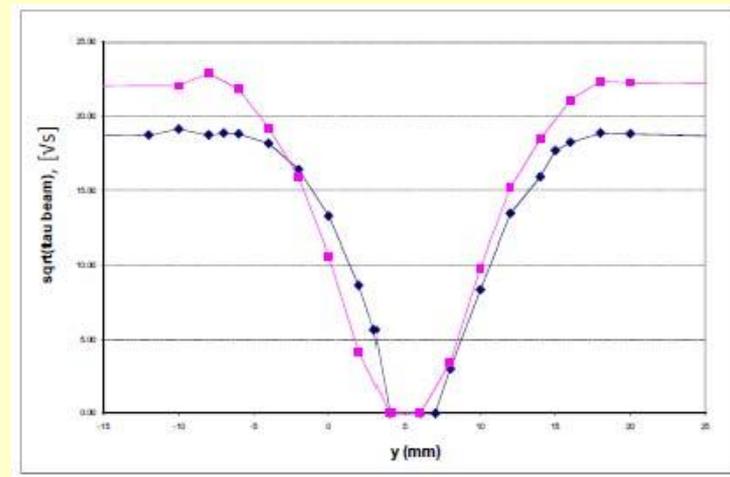
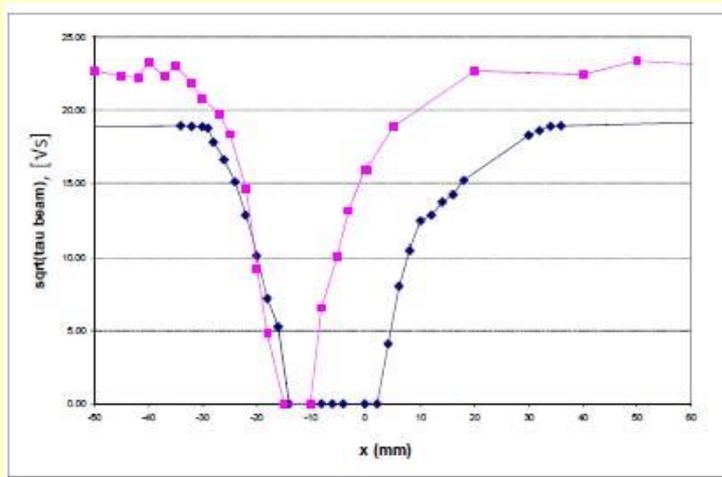
Proposal to COSY PAC
(submitted in July 2009)

Low- β magnet installation at COSY
(summer 2009)



Low- β section commissioning (Feb. 2010)

Acceptance measurements with scrapers



- New low- β section
- Old lattice

Low- β section does not limit the machine acceptance

Conclusions

- Outstanding case for DY with polarized antiprotons
- Interesting perspectives for DY on fixed target
 - Polarized target in PANDA technical challenge
- Studies on polarized antiprotons undertaken by PAX Collab.



Ferrara International School Niccolò Cabeo



The Ferrara PhD School in Physics, in collaboration with the Pavia, Torino and Trieste Universities, has organized a permanent International School on hadron structure and interactions.

The School is mainly addressed to young PhD students, both theoreticians and experimentalists, although advanced PhD students as well as post-docs and young researchers are also welcome.



Every year the School will offer two levels of plenary lectures: one "pedagogical", on relevant subjects in hadron physics usually not covered in great detail in the normal undergraduate and graduate courses, and the other, more technical, on specific related items.

The school lasts one week, and includes several sections devoted to informal conversations with teachers. Every year proceedings of the lectures will be published and delivered to the students.

A permanent Advisory Scientific Committee serves the School by proposing, each year, the lecturers and reviewing the program. It also provides the necessary connections among the Universities and the laboratories involved, and eventually seeks for funding.



The main topic of this year is:

Transverse Momentum Dependent Parton Distribution Functions



The first session of the school is announced:

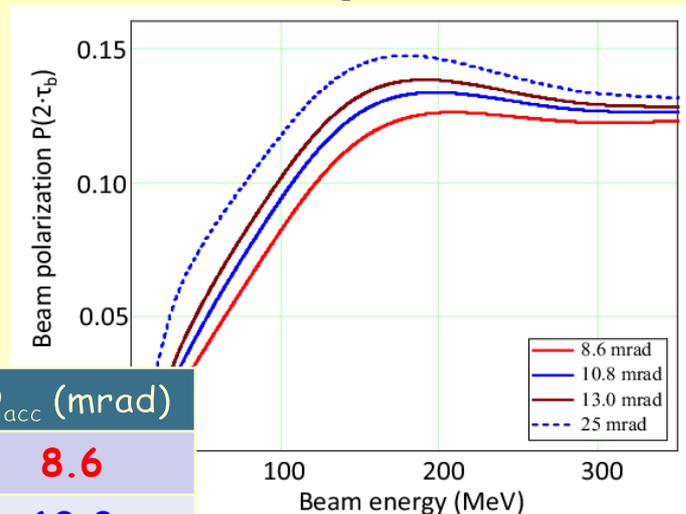
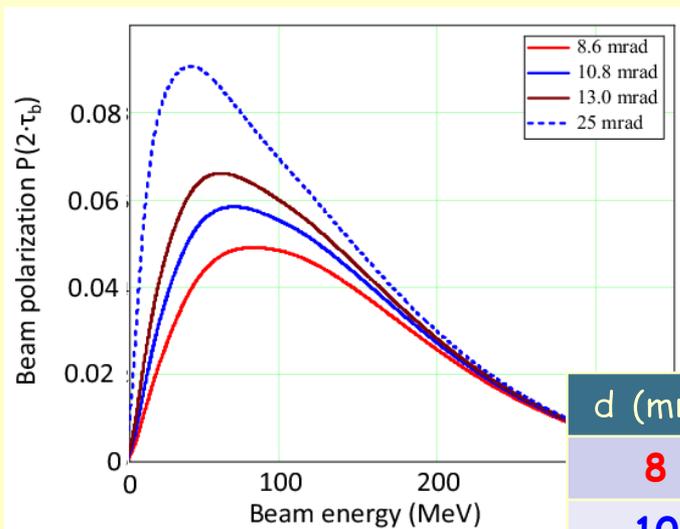
May, 24-28 2010
IUSS, Via delle Scienze 41b, 44100 Ferrara (Italy)



Expected polarizations after filtering for two lifetimes at AD

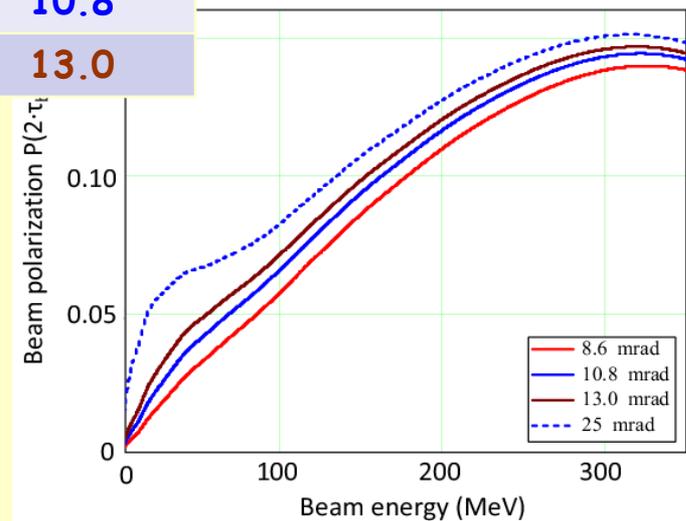
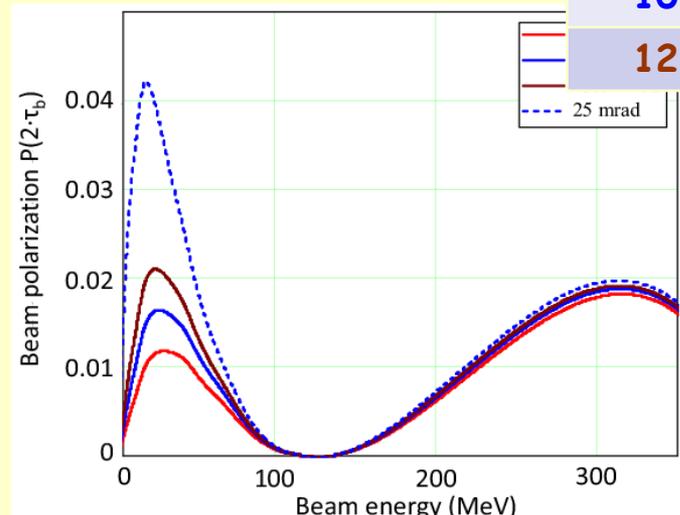
transverse

longitudinal



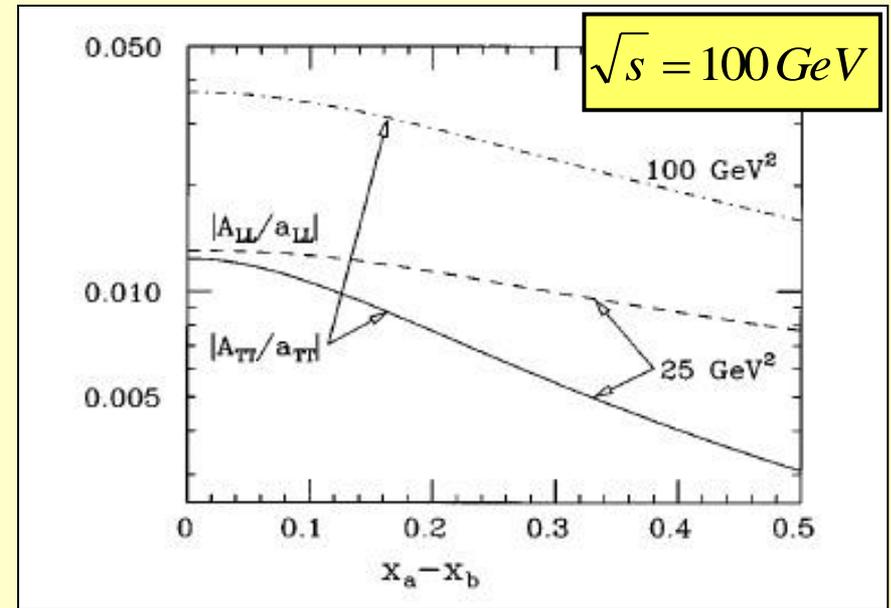
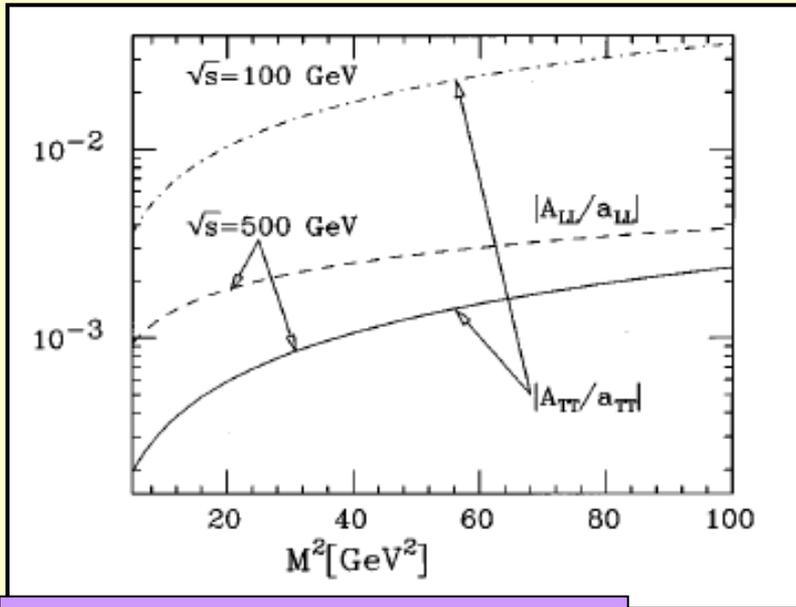
A

d (mm)	Θ_{acc} (mrad)
8	8.6
10	10.8
12	13.0



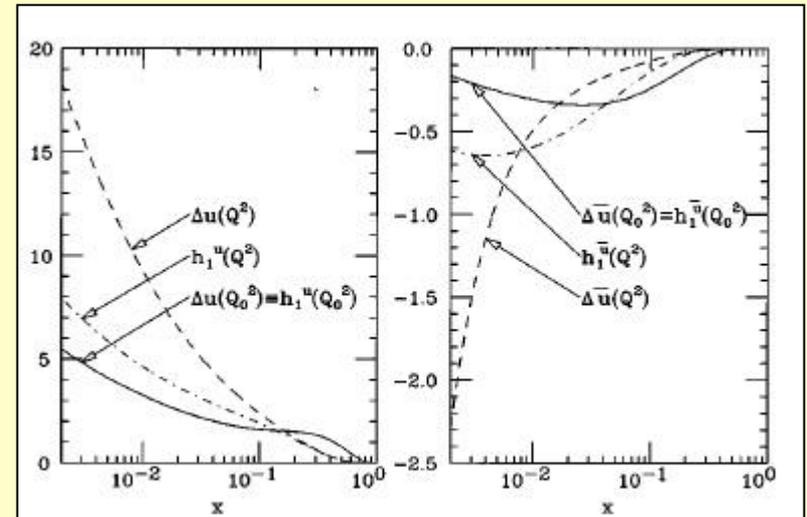
D

Higher energy p-p machine



V. Barone, T. Calarco and A. Drago
Phys. Rev. D 56 (1997) 527

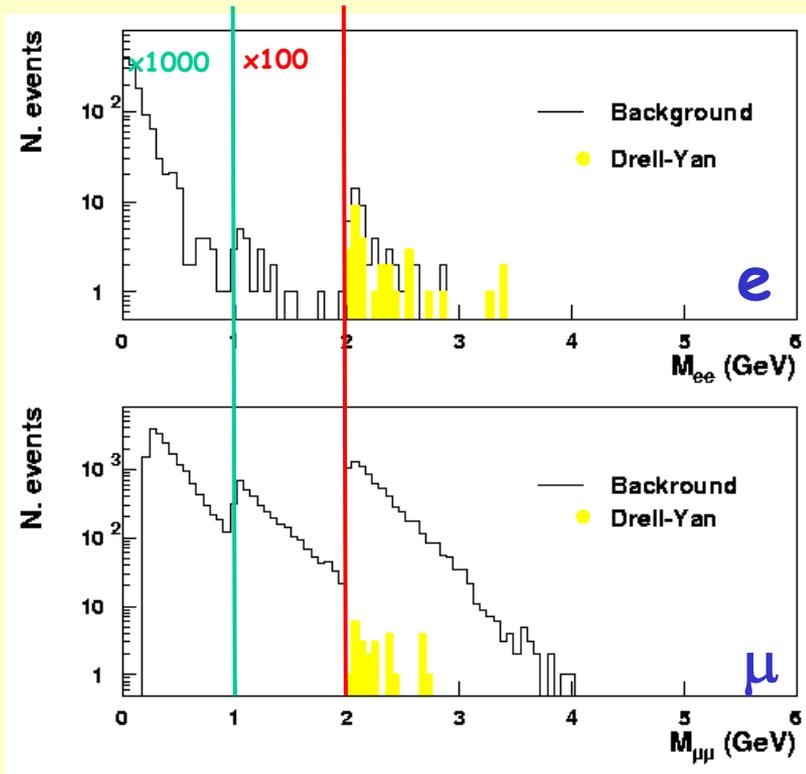
- $s \uparrow$
- Asymmetry \downarrow
- $A_{LL} > A_{TT}$
- S_{JPARC} ideal



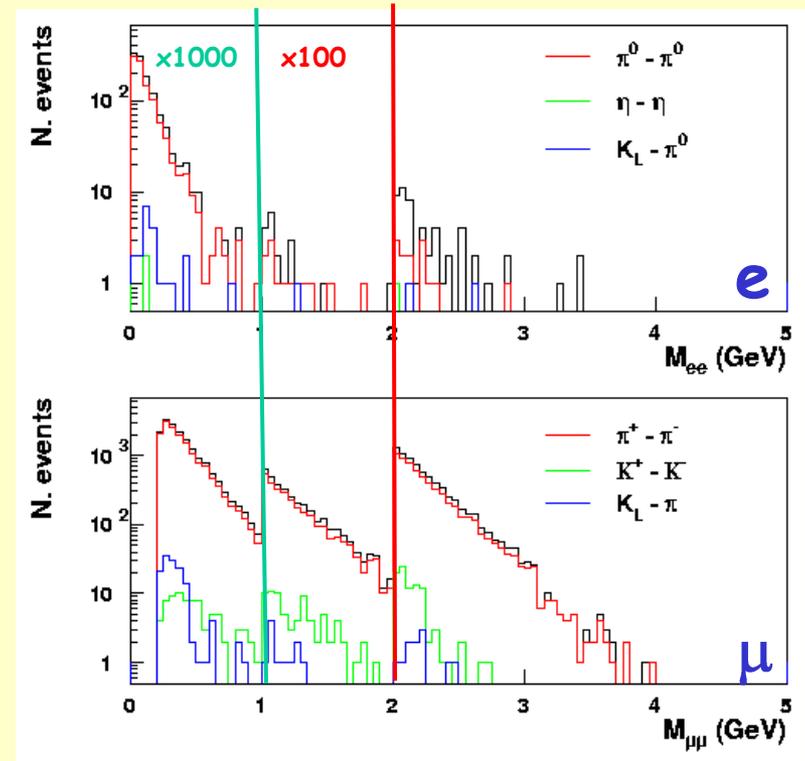
Background for $\bar{p}p \rightarrow e^+e^-X$

Preliminary PYTHIA result ($2 \cdot 10^9$ events)

Total background

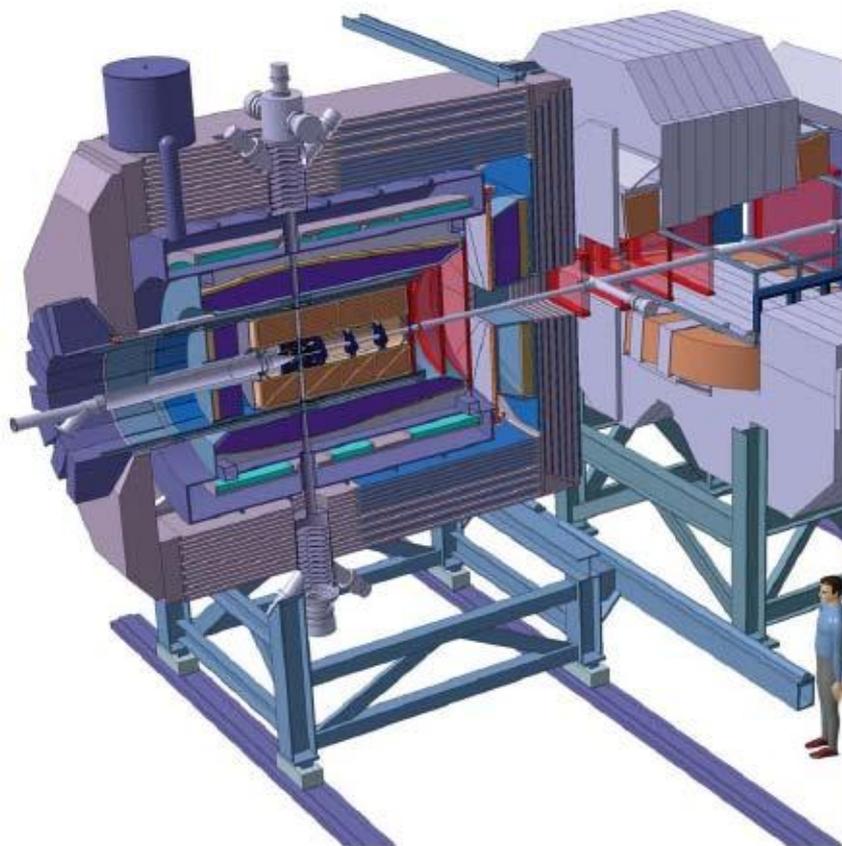


Background origin



- Background higher for μ than for e
- Background from charge conjugated mesons negligible for e .

The PANDA detector



- 4π acceptance
- High rate capability:
 $2 \times 10^7 \text{ s}^{-1}$ interactions
- Efficient event selection
 - Sampling acquisition
- Momentum resolution $\sim 1\%$
- Vertex info for D, K_S^0 , Y
($\tau = 317 \text{ }\mu\text{m}$ for D^\pm)
 - Good tracking
- Good PID (γ , e, μ , π , K, p)
 - **DIRC** *ToF, dE/dx*
- γ -detection 1 MeV – 10 GeV
 - *Crystal Calorimeter*

*From DY to elastic e^+e^- production:
Proton Electromagnetic Form Factors
@fixed target*

Background in $p\bar{p} \rightarrow e^+e^-$

- ✓ Reactions with at least 3 particles produced:
(e^+e^-X , $\pi^+\pi^-X$,...)

Particle identification and kinematics constraints

→ no problem (still to be quantified)

- ✓ Reactions with 2 charged particles ($\pi^+\pi^-$)

- $\sigma(\pi^+\pi^-)/\sigma(e^+e^-) \approx 10^6$ ($2\mu\text{b}/8\text{pb}$ at $q^2=9.(\text{GeV}/c)^2$)

need rejection of $p\bar{p} \rightarrow \pi^+\pi^-$ by 10^{-8}

binary event, mean reject. of 10^{-4} per π^+ and per π^-

- very close kinematics
- PID is crucial, EMC, DIRC, dE/dx

DY with e^+/e^- @ PANDA?

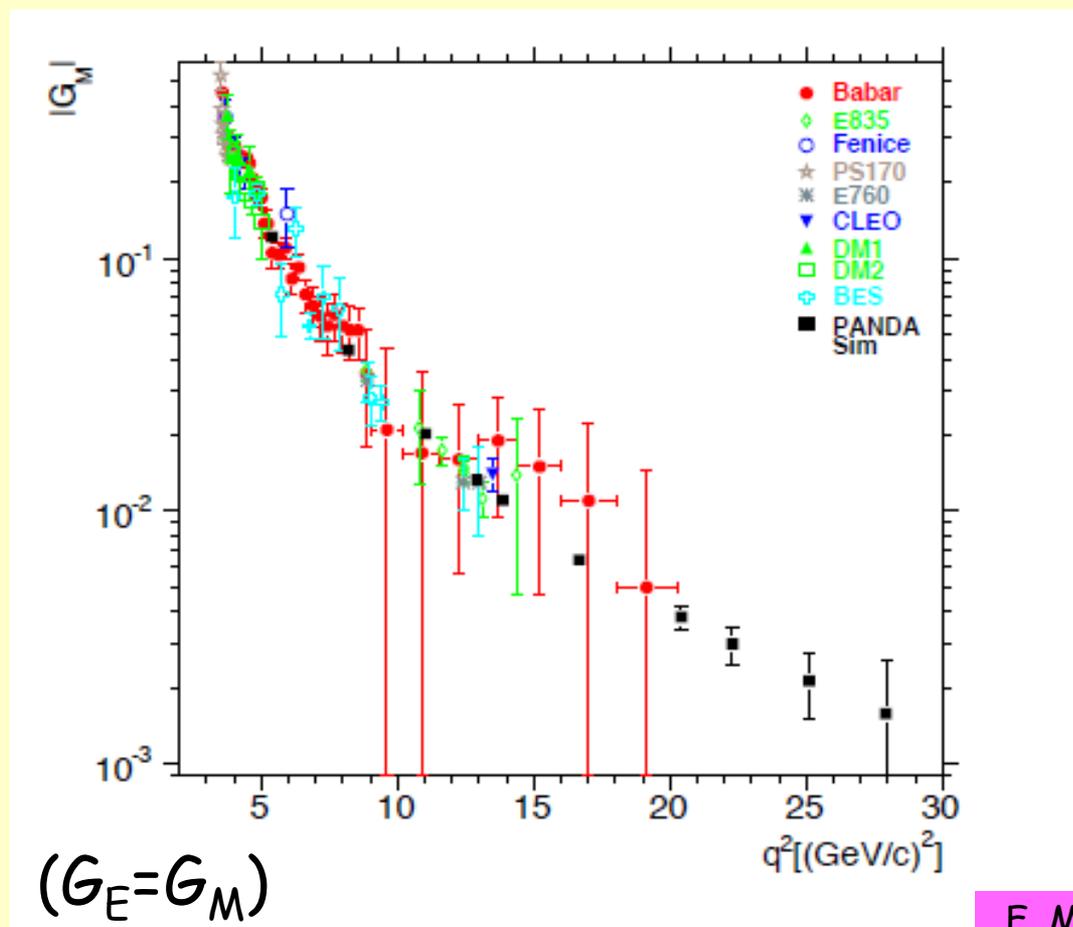
Pion-rejection promising...

T_{p_bar} (GeV)	Q^2 (GeV/c) ²	θ_{CM}	θ_{lab}	p_{lab} (GeV/c)	one π Misident. Probability ECAL×DIRC×dE/dx	$\pi^+\pi^-$ Misident. Probability
1.	5.4	20°	13°	2.2	$0.001 \times 0.5 \times 0.05 = 2.5 \cdot 10^{-5}$	0.1 10^{-9}
		160°	132°	0.57	$0.033 \times 0.003 \times 0.03 = 3.0 \cdot 10^{-6}$	
		90°	54°	1.43	$0.001 \times 0.3 \times 0.03 = 9 \cdot 10^{-6}$	0.1 10^{-9}
		90°	54°	1.43	$0.001 \times 0.3 \times 0.03 = 9 \cdot 10^{-6}$	
2.5	8.2	20°	10°	3.7	$0.001 \times 1 \cdot 0.05 = 5 \cdot 10^{-5}$	0.3 10^{-9}
		160°	117°	0.7	$0.014 \times 0.014 \times 0.03 = 6 \cdot 10^{-6}$	
		90°	41°	2.2	$0.001 \times 1 \cdot 0.03 = 3 \cdot 10^{-5}$	0.9 10^{-9}
		90°	41°	2.2	$0.001 \times 1 \cdot 0.03 = 3 \cdot 10^{-5}$	
5.	12.9	20°	7.4°	6.1	$0.001 \times 1 \cdot 0.1 = 10^{-4}$	0.6 10^{-9}
		160°	102°	0.8	$0.014 \times 0.014 \times 0.03 = 6 \cdot 10^{-6}$	
		90°	32°	3.4	$0.001 \times 1 \cdot 0.05 = 5 \cdot 10^{-5}$	2.5 10^{-9}
		90°	32°	3.4	$0.001 \times 1 \cdot 0.05 = 5 \cdot 10^{-5}$	
10.	22.3	20°	5.4°	10.9	$0.001 \times 1 \cdot 0.3 = 3 \cdot 10^{-4}$	5.4 10^{-9}
		160°	85°	1.0	$0.005 \times 0.12 \times 0.03 = 1.8 \cdot 10^{-5}$	
		90°	24°	5.95	$0.001 \times 1 \cdot 0.1 = 1 \cdot 10^{-4}$	10. 10^{-9}
		90°	24°	5.95	$0.001 \times 1 \cdot 0.1 = 1 \cdot 10^{-4}$	

F. Maas Univ. of Mainz - GSI (D)

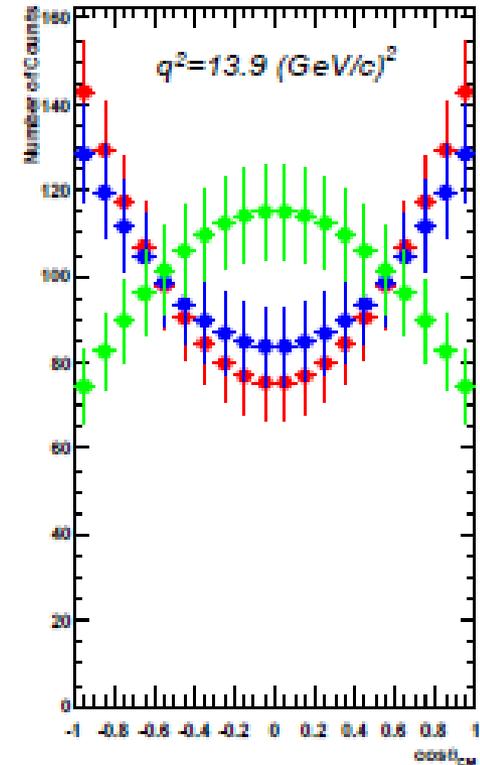
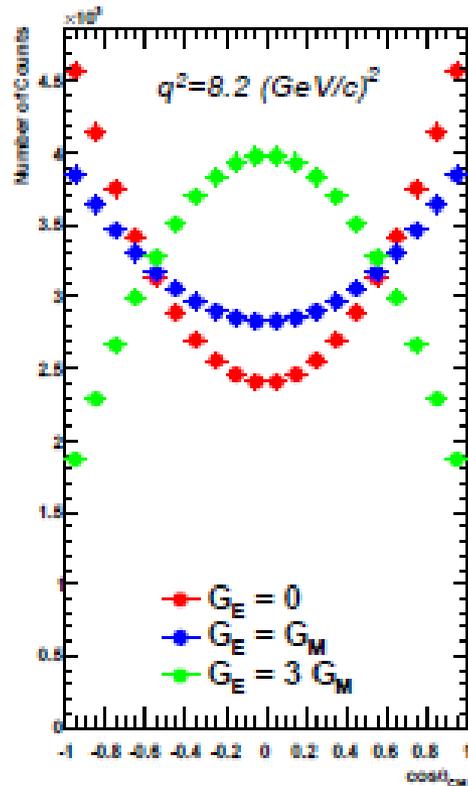
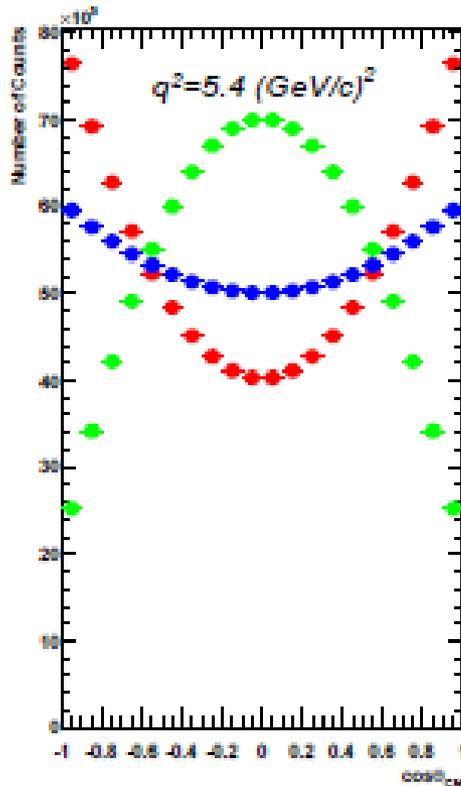
$\text{Pbar-p} \rightarrow e^+e^-$

Statistical projection for timelike FF @ PANDA



Measurement of G_E and G_M moduli @ PANDA

- Use of different angular dependence for G_E and G_M



F. Maas

-Generated events:

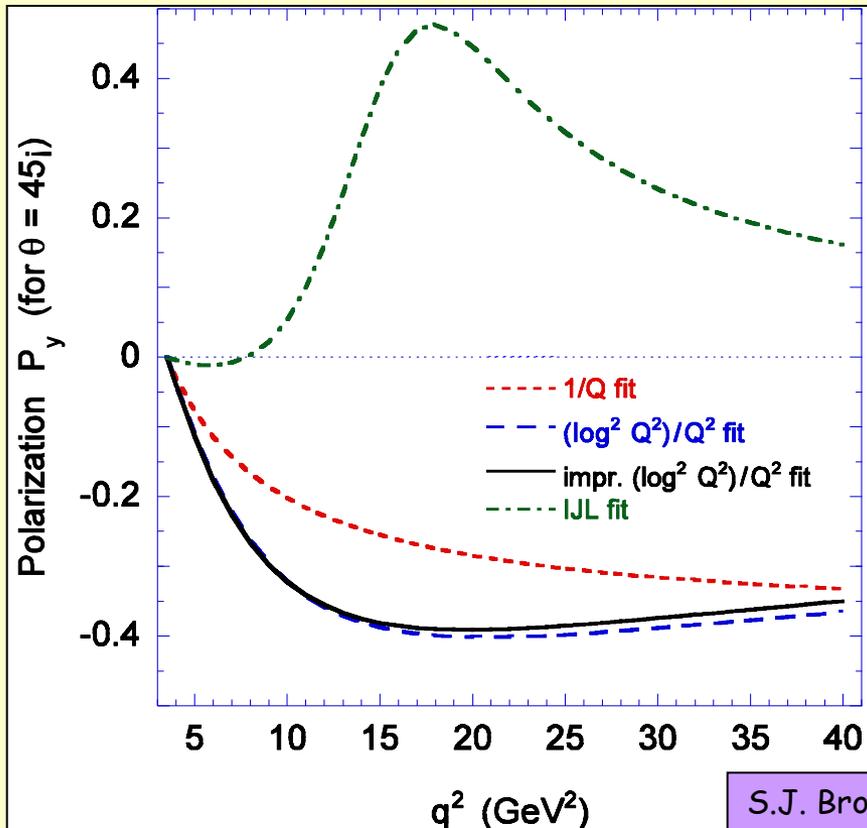
2fb^{-1} (4 months @ $2 \times 10^{32} \text{cm}^{-2}\text{s}^{-1}$)

Single Spin Observables

$$\frac{d\sigma}{d\Omega}(P_y) = \left(\frac{d\sigma}{d\Omega}\right)_0 [1 + \mathcal{A}P_y],$$

$$\mathcal{A} = \frac{\sin 2\theta \operatorname{Im} G_E^* G_M}{D\sqrt{\tau}}, \quad D = |G_M|^2(1 + \cos^2 \theta) + \frac{1}{\tau}|G_E|^2 \sin^2 \theta$$

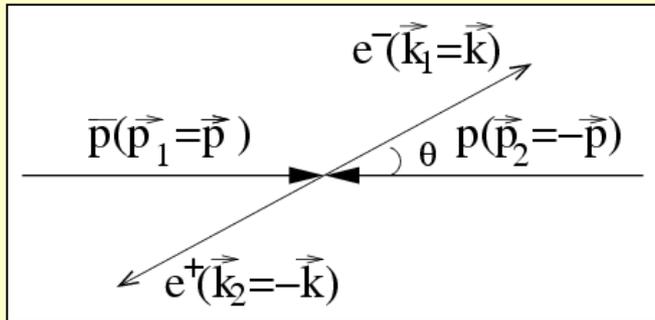
A. Z. Dubnickova, S. Dubnicka, M.P. Rekalo Nuovo Cimento A109, 241 (1996)



- Contains imaginary part
 - Access relative phase
- Very sensitive to different models

S.J. Brodsky, C.E. Carlson, J.R. Hiller, D.S. Hwang PRD 69, 054022 (2004)

Double polarized pbar-p annihilation:



$$\left(\frac{d\sigma}{d\Omega}\right)_0 A_{xx} = \sin^2 \theta \left(|G_M|^2 + \frac{1}{\tau} |G_E|^2 \right) \mathcal{N},$$

$$\left(\frac{d\sigma}{d\Omega}\right)_0 A_{yy} = -\sin^2 \theta \left(|G_M|^2 - \frac{1}{\tau} |G_E|^2 \right) \mathcal{N},$$

$$\left(\frac{d\sigma}{d\Omega}\right)_0 A_{zz} = \left[(1 + \cos^2 \theta) |G_M|^2 - \frac{1}{\tau} \sin^2 \theta |G_E|^2 \right] \mathcal{N},$$

$$\left(\frac{d\sigma}{d\Omega}\right)_0 A_{xz} = \left(\frac{d\sigma}{d\Omega}\right)_0 A_{zx} = \frac{1}{\sqrt{\tau}} \sin 2\theta \operatorname{Re} G_E G_M^* \mathcal{N}.$$

E. Tomasi, F. Lacroix, C. Duterte, G.I. Gakh, EPJA 24, 419(2005)

- Most contain moduli G_E, G_M
 - Independent G_E - G_M separation
 - Test of Rosenbluth separation in the time-like region
- Access to G_E - G_M phase
- Very sensitive to different models (next transparencies)