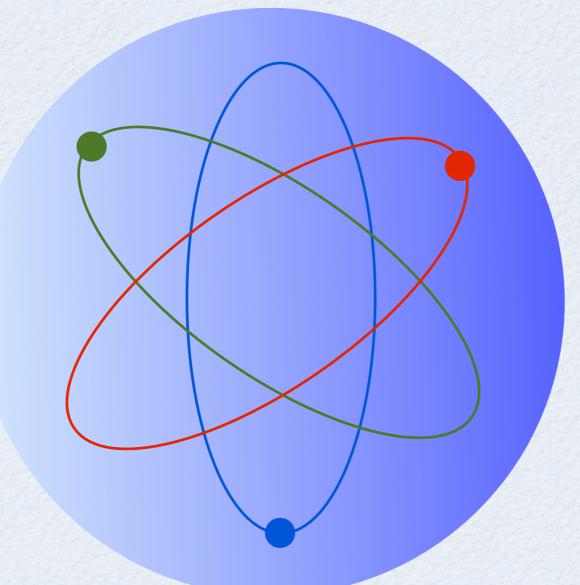
Studying the hadron structure in Drell-Yan reactions - concluding remarks



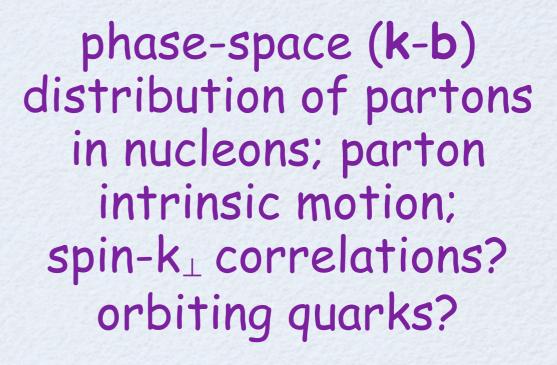
Mauro Anselmino, Torino University & INFN 26-27 April 2010 CERN

Exploring the 3-dimensional phase-space structure of the nucleon with Drell-Yan processes

S

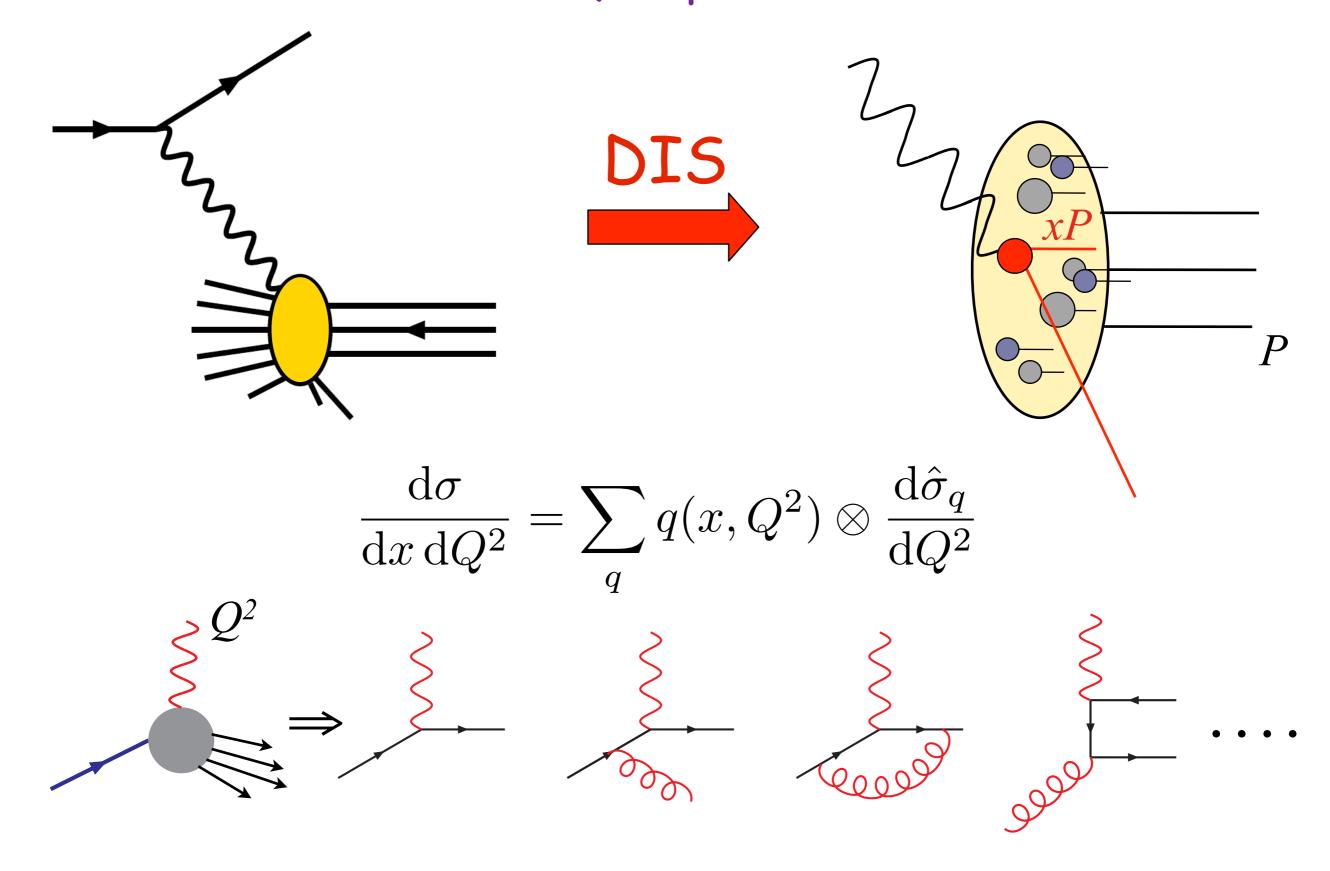
D

 $m{k}_{\perp}$

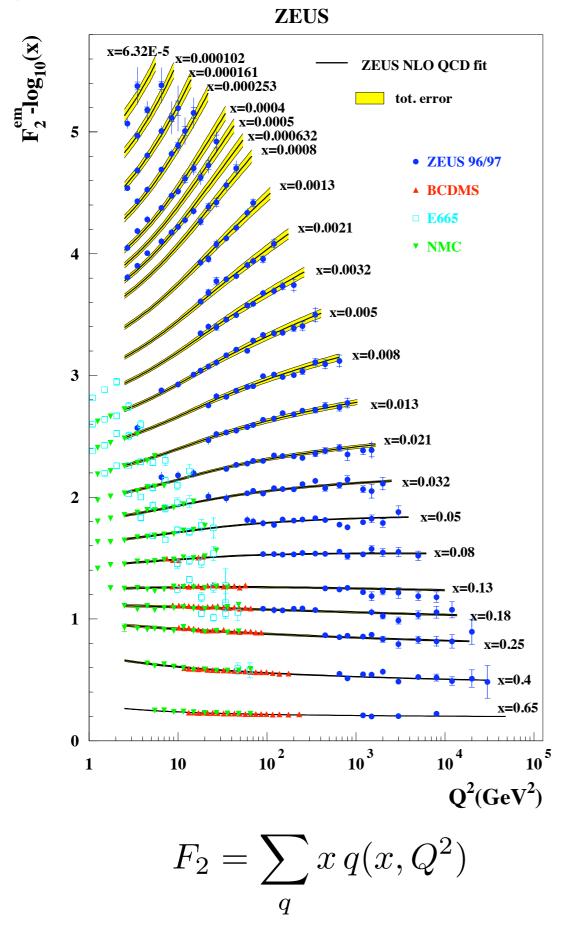


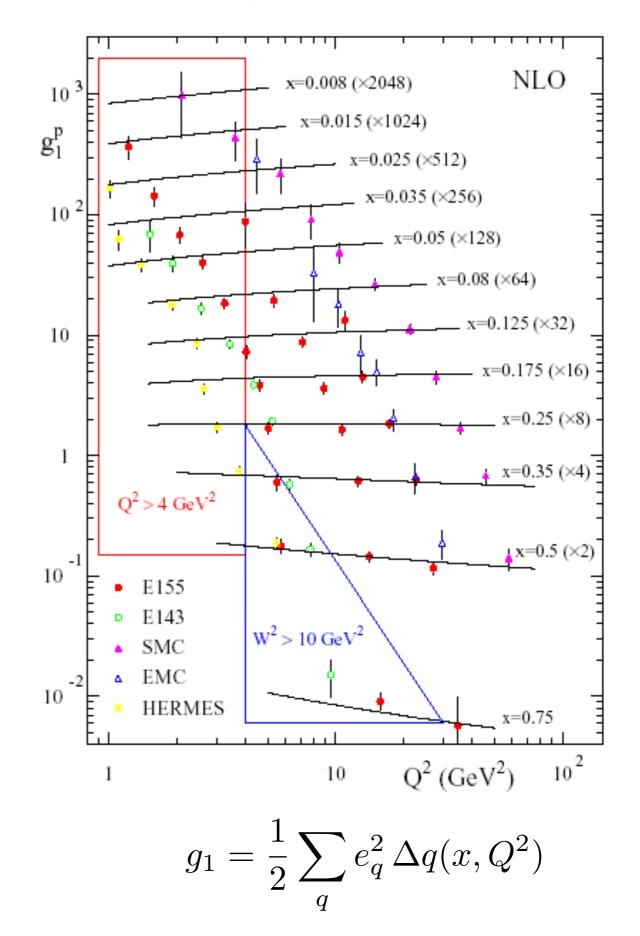
information encoded in GPDs and TMDs (exclusive and inclusive processes)

Usual way of exploring the nucleon structure: collinear QCD parton model

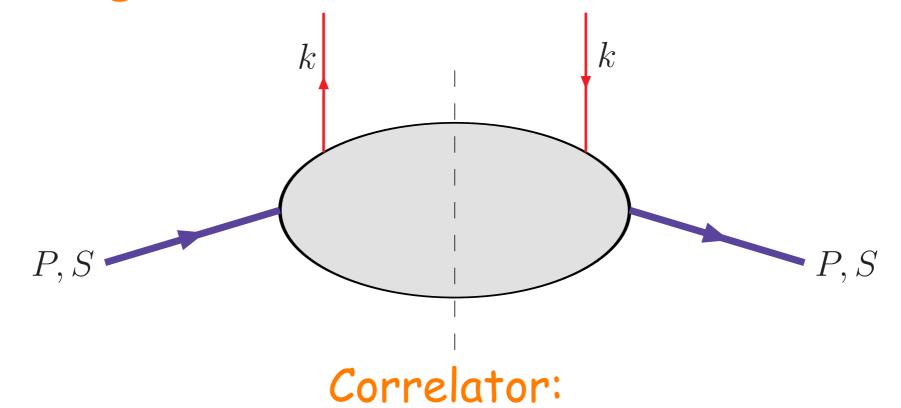


great success, but essentially x and Q^2 degrees of freedom





The nucleon, as probed in DIS, in collinear configuration: 3 distribution functions

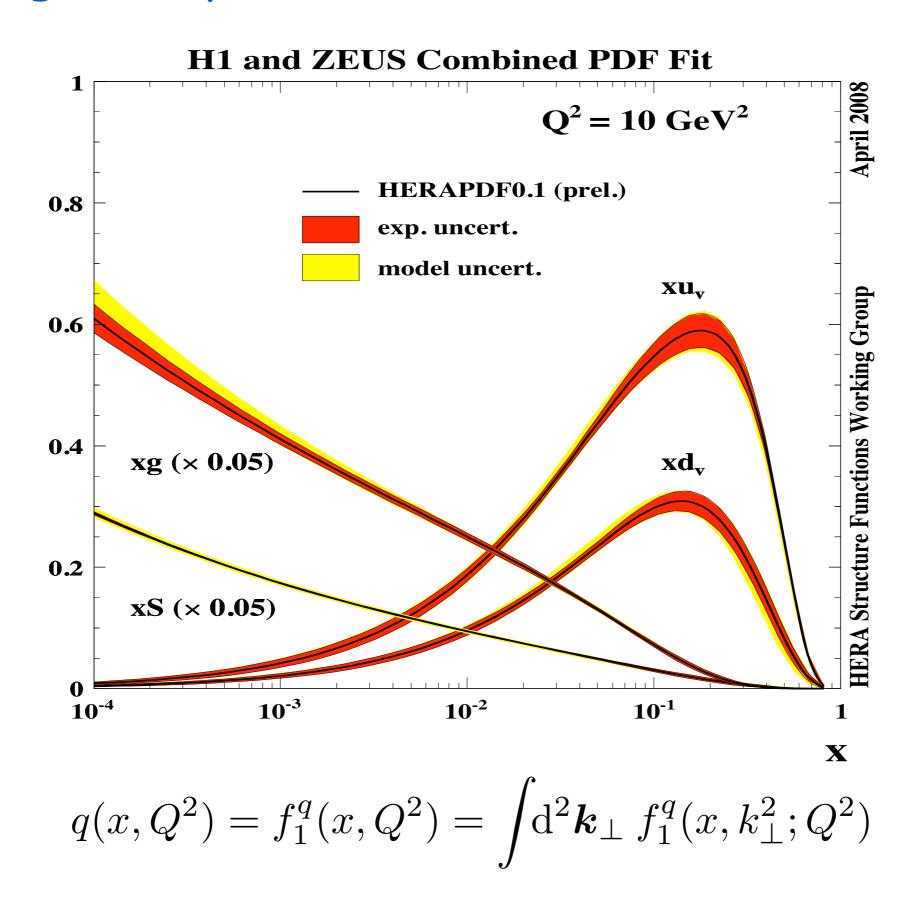


$$\Phi_{ij}(k;P,S) = \sum_{X} \int \frac{\mathrm{d}^{3} \mathbf{P}_{X}}{(2\pi)^{3} 2E_{X}} (2\pi)^{4} \delta^{4}(P-k-P_{X}) \langle PS|\overline{\Psi}_{j}(0)|X\rangle \langle X|\Psi_{i}(0)|PS\rangle$$

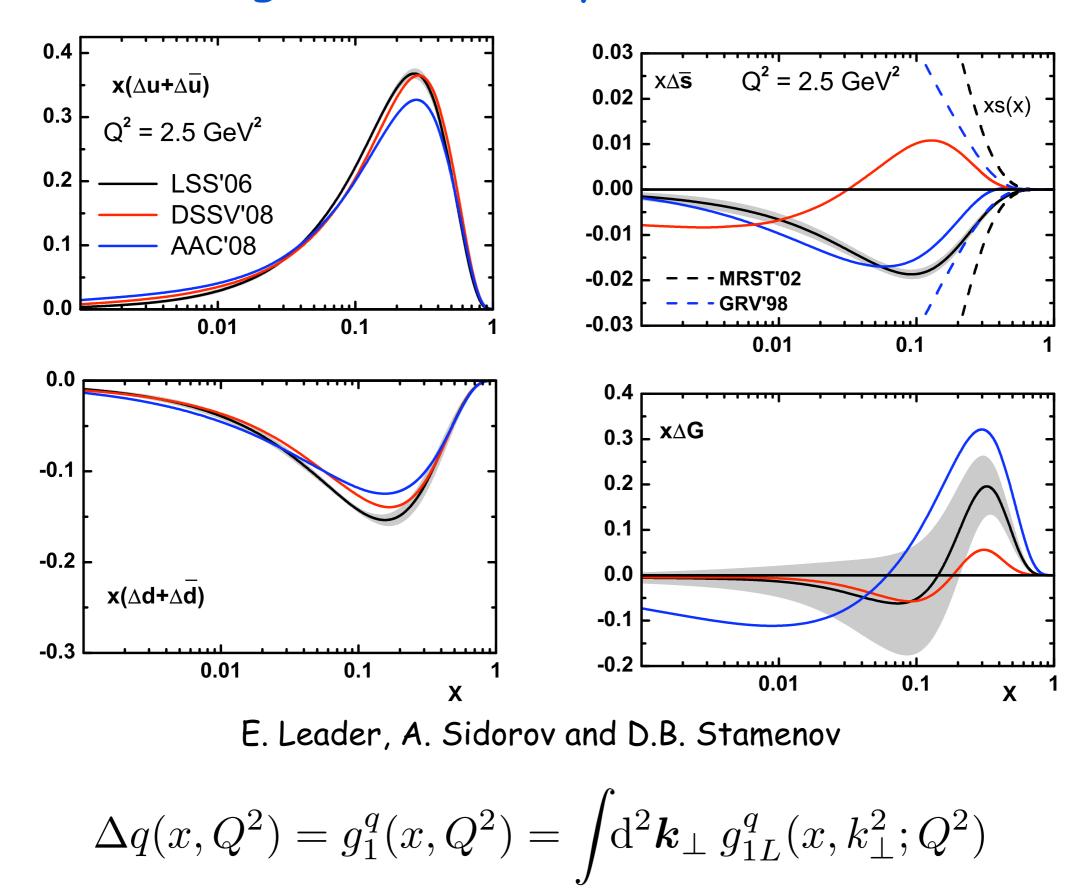
$$= \int \mathrm{d}^{4} \xi \, e^{ik \cdot \xi} \langle PS|\overline{\Psi}_{j}(0)\Psi_{i}(\xi)|PS\rangle$$

$$\Phi(x,S) = \frac{1}{2} \left[f_{1}(x) \not h_{+} + S_{L} \left(g_{1L}(x) \gamma^{5} \not h_{+} + h_{1T} \right) i \sigma_{\mu\nu} \gamma^{5} n_{+}^{\mu} S_{T}^{\nu} \right]$$

integrated parton distribution functions, PDF

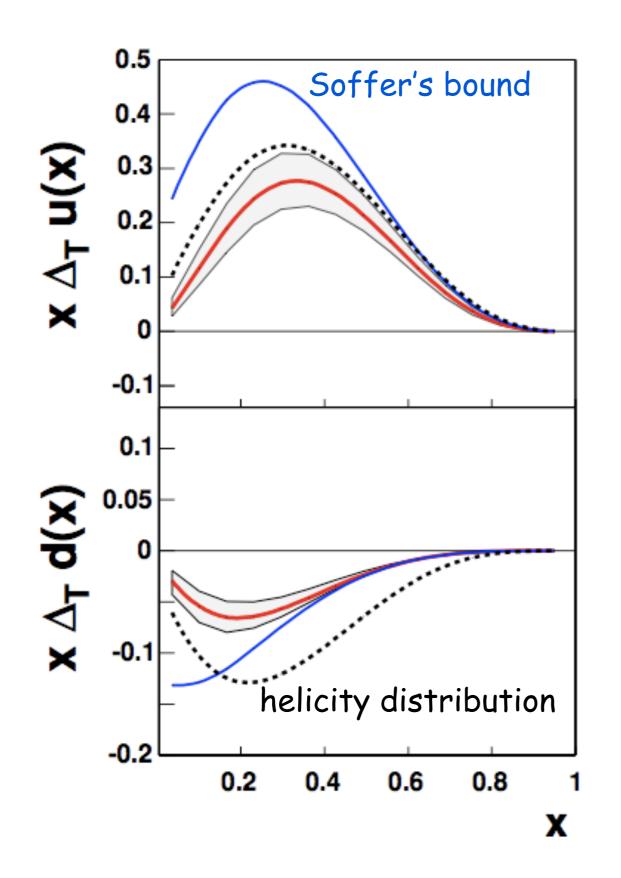


integrated helicity distributions



transversity distributions

M.A., M. Boglione, U. D'Alesio, A. Kotzinian, S. Melis, F. Murgia, A. Prokudin, C. Türk



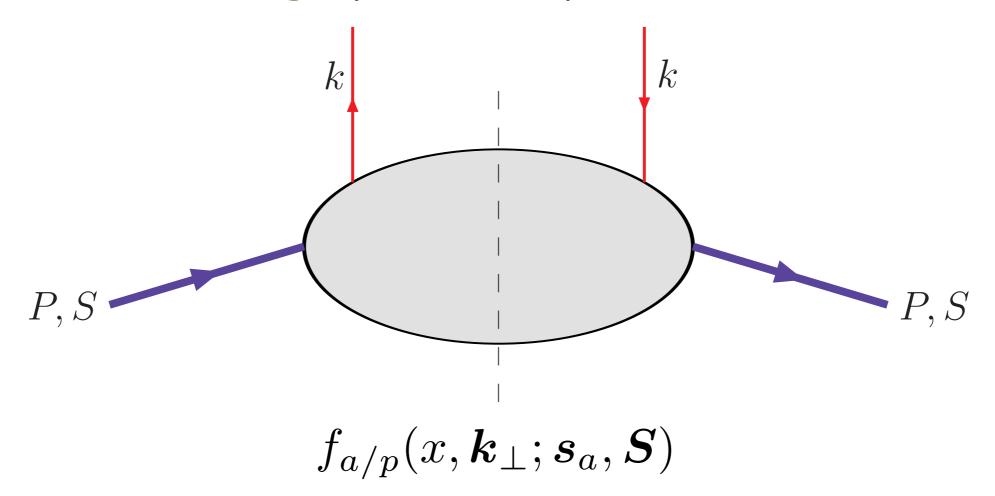
$$\Delta_T q(x, Q^2) = h_1^q(x, Q^2)$$

Extraction from SIDIS (HERMES, COMPASS-D) + e^+e^- (Belle) data, $h_1 \otimes H_1^{\perp}$

new probes and concepts to explore the nucleon structure

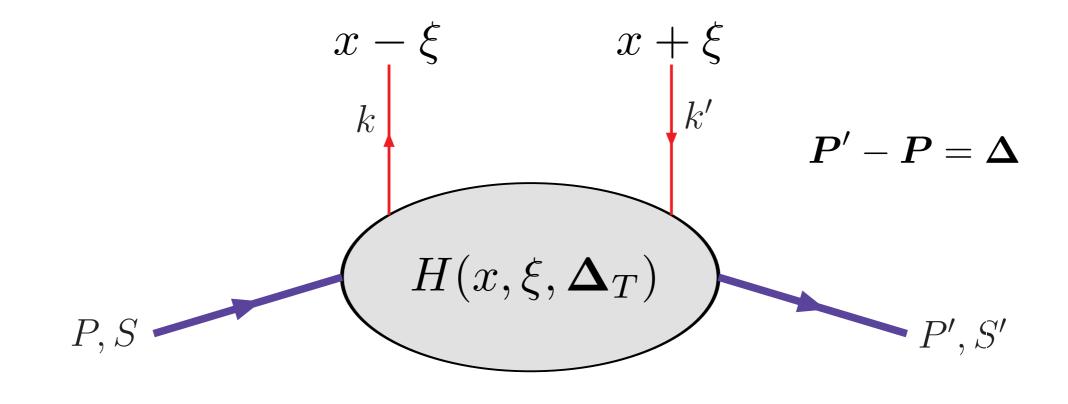
TMDs - Transverse Momentum Dependent (distribution and fragmentation functions)

> (polarized) SIDIS and Drell-Yan, spin asymmetries in inclusive (large p_T) NN processes



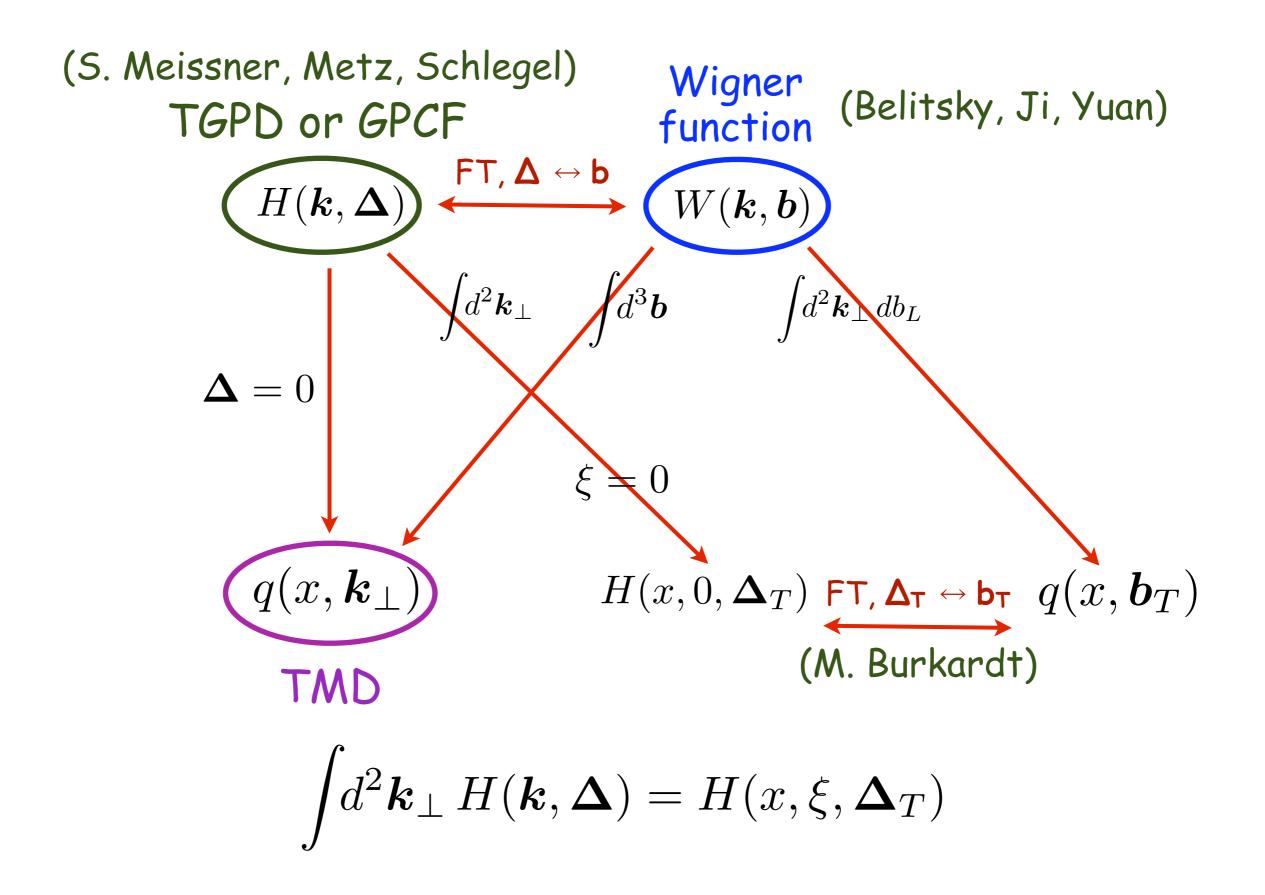
GPDs - Generalized Partonic Distributions

exclusive processes in leptonic and hadronic interactions



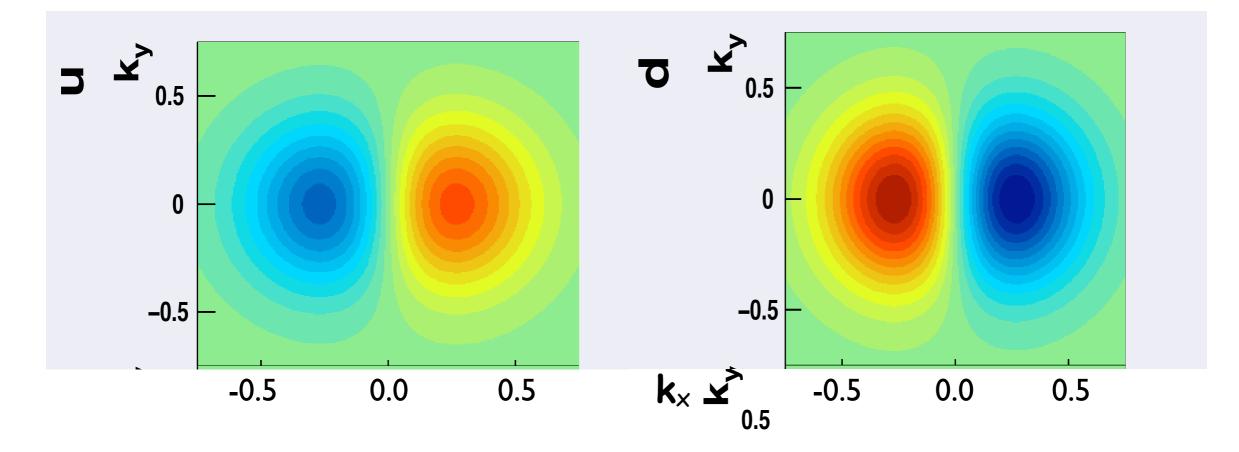
$$q(x, \boldsymbol{b}_T) = \int \frac{d^2 \boldsymbol{\Delta}_T}{(2\pi)^2} H_q(x, 0, -\boldsymbol{\Delta}_T^2) e^{-i \boldsymbol{b}_T \cdot \boldsymbol{\Delta}_T}$$

phase-space parton distribution, W(k, b)



 $q(x, \mathbf{k}_{\perp})$

Sivers u and d quark densities in transverse momentum space

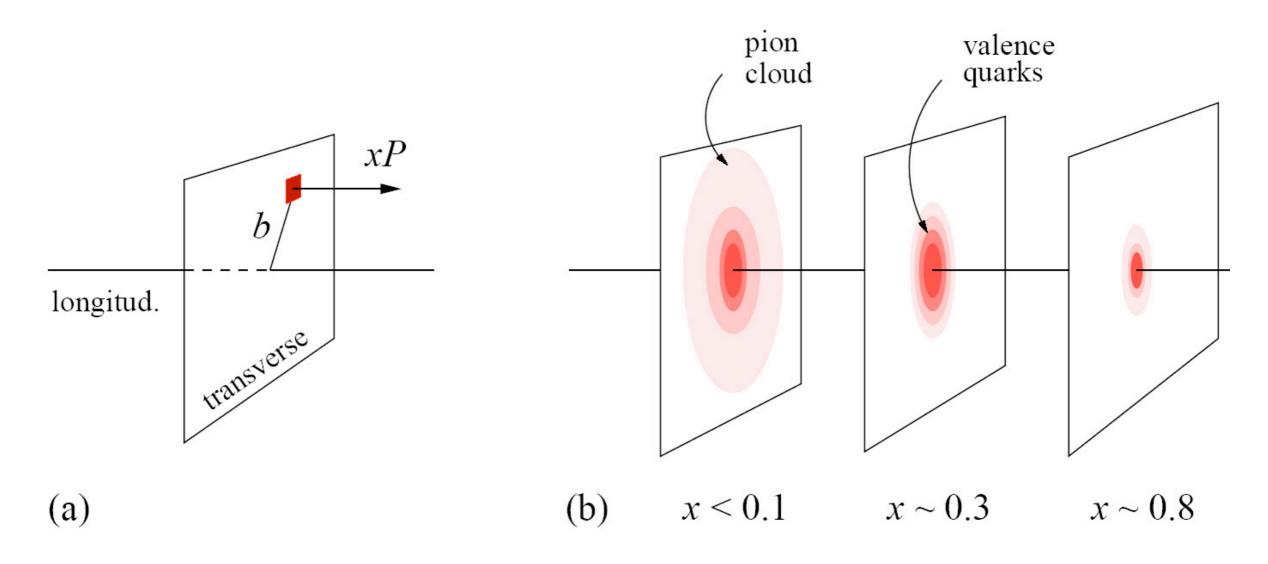


proton moving into the screen, polarization along y-axis blue: less quarks red: more quarks x = 0.2 k in GeV/c -0.5





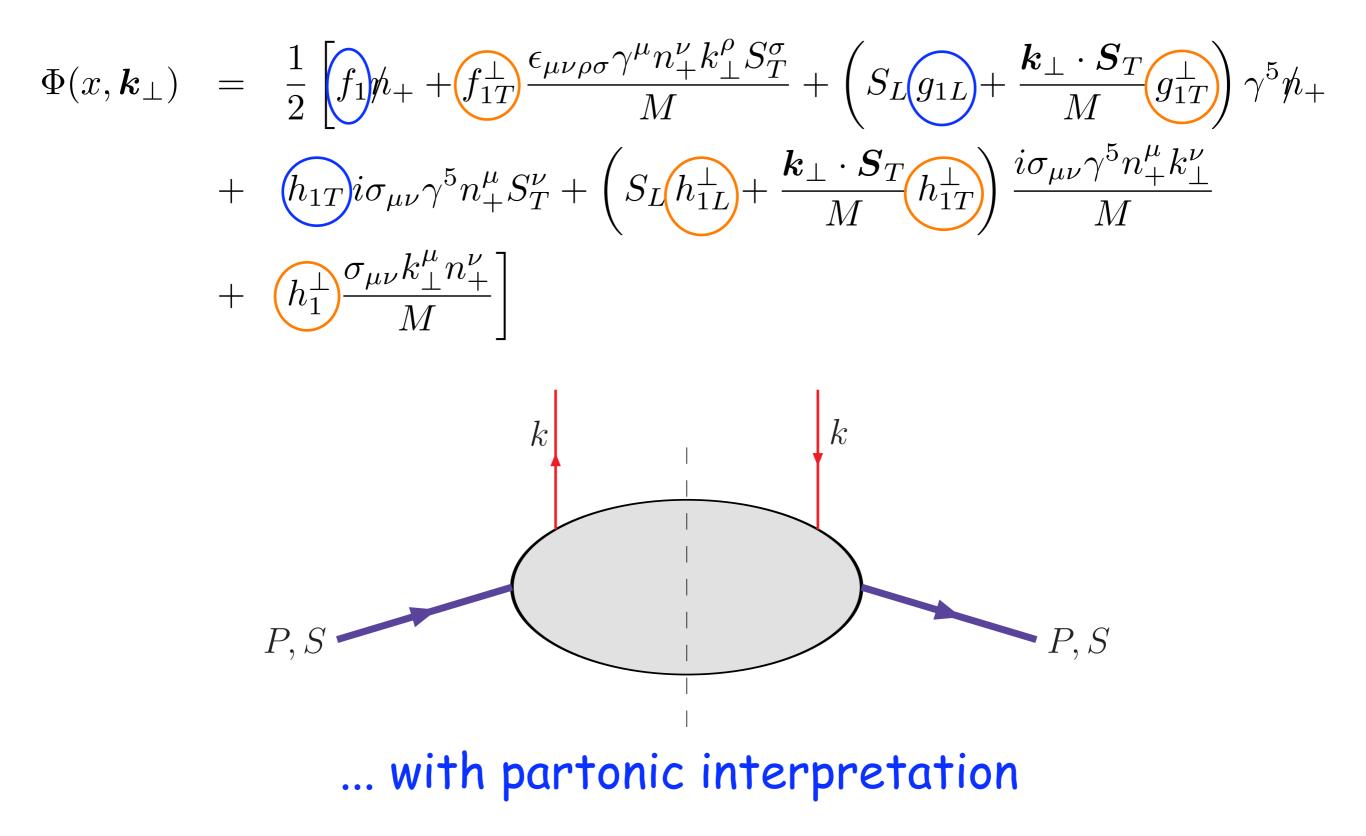
 $q(x, \boldsymbol{b}_T)$

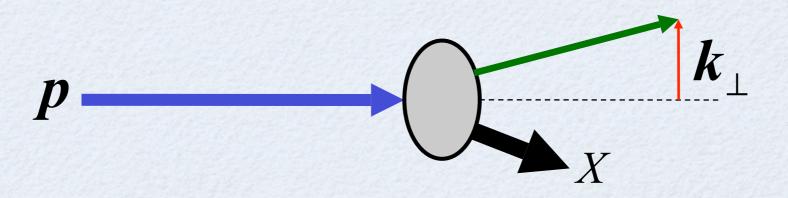


femtophotography or tomography of the nucleon

courtesy of C. Weiss

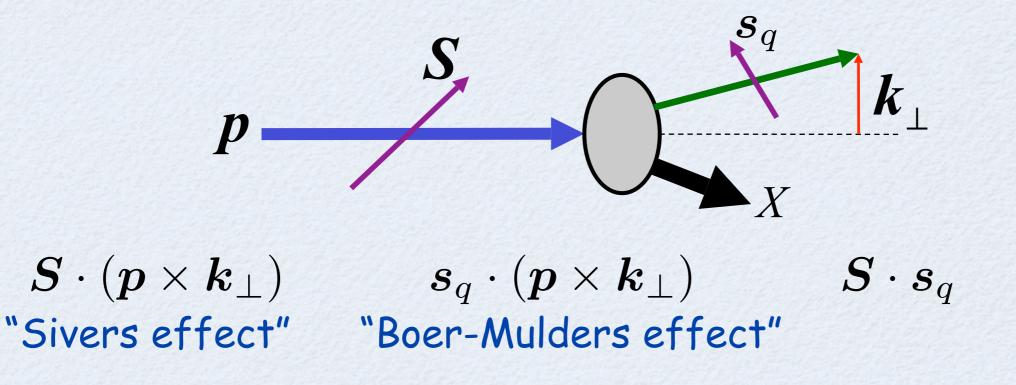
TMDs: the leading-twist correlator, with intrinsic k_{\perp} , contains 8 independent functions



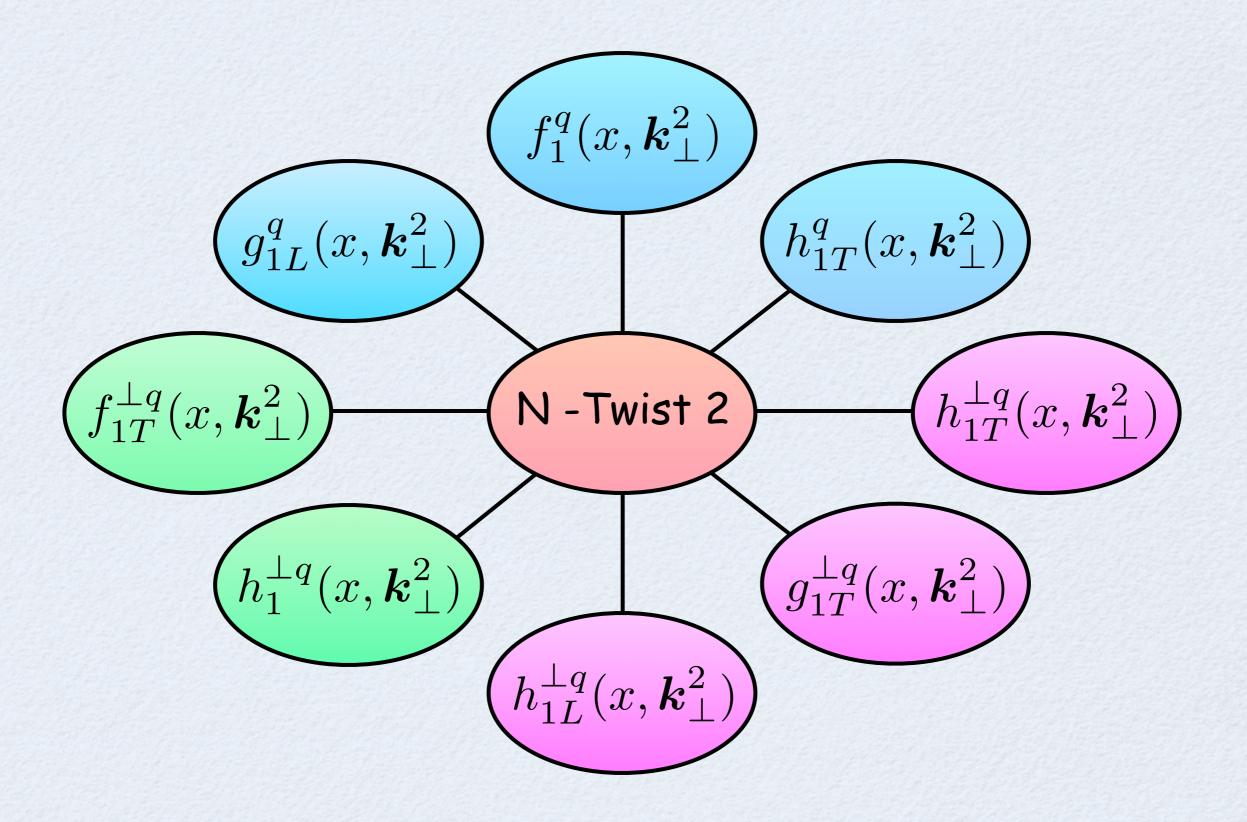


$$f_1^q(x,k_{\perp}^2) \qquad q(x) = f_1^q(x) = \int d^2 \mathbf{k}_{\perp} f_1^q(x,k_{\perp}^2)$$

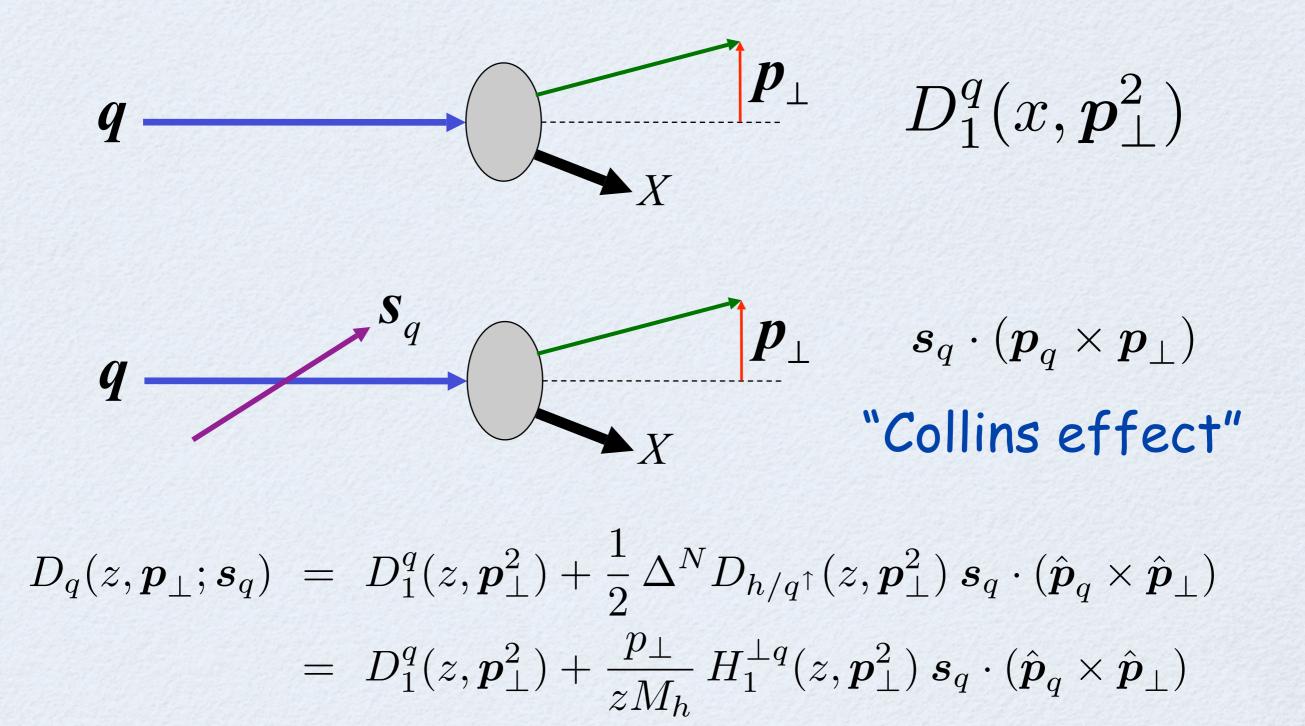
several spin-k_ correlations in TMDs: $f_q(x, k_\perp; s_q, S)$

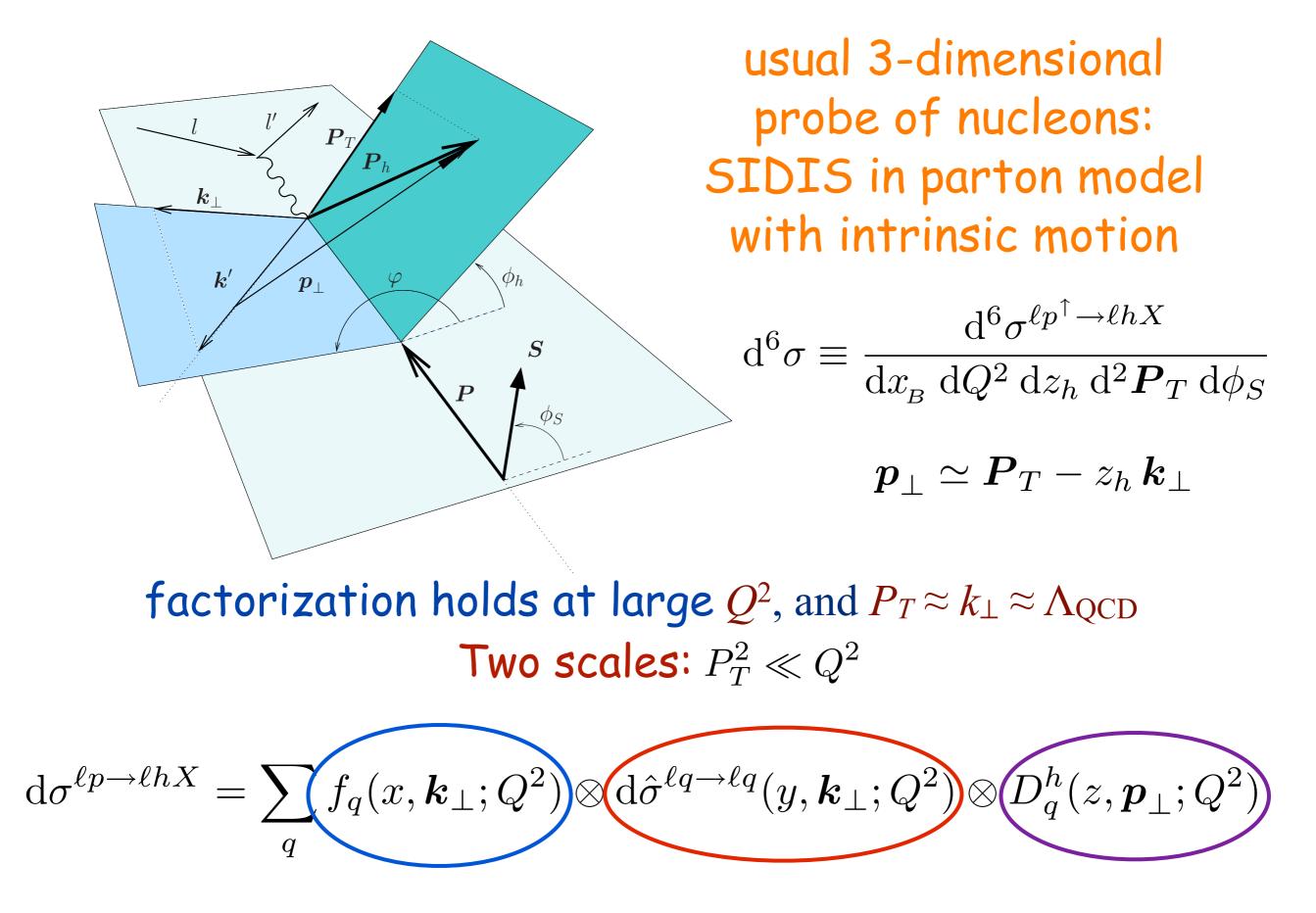


The nucleon at twist-2,



similar spin-p₁ correlations in fragmentation process (case of final spinless hadron)





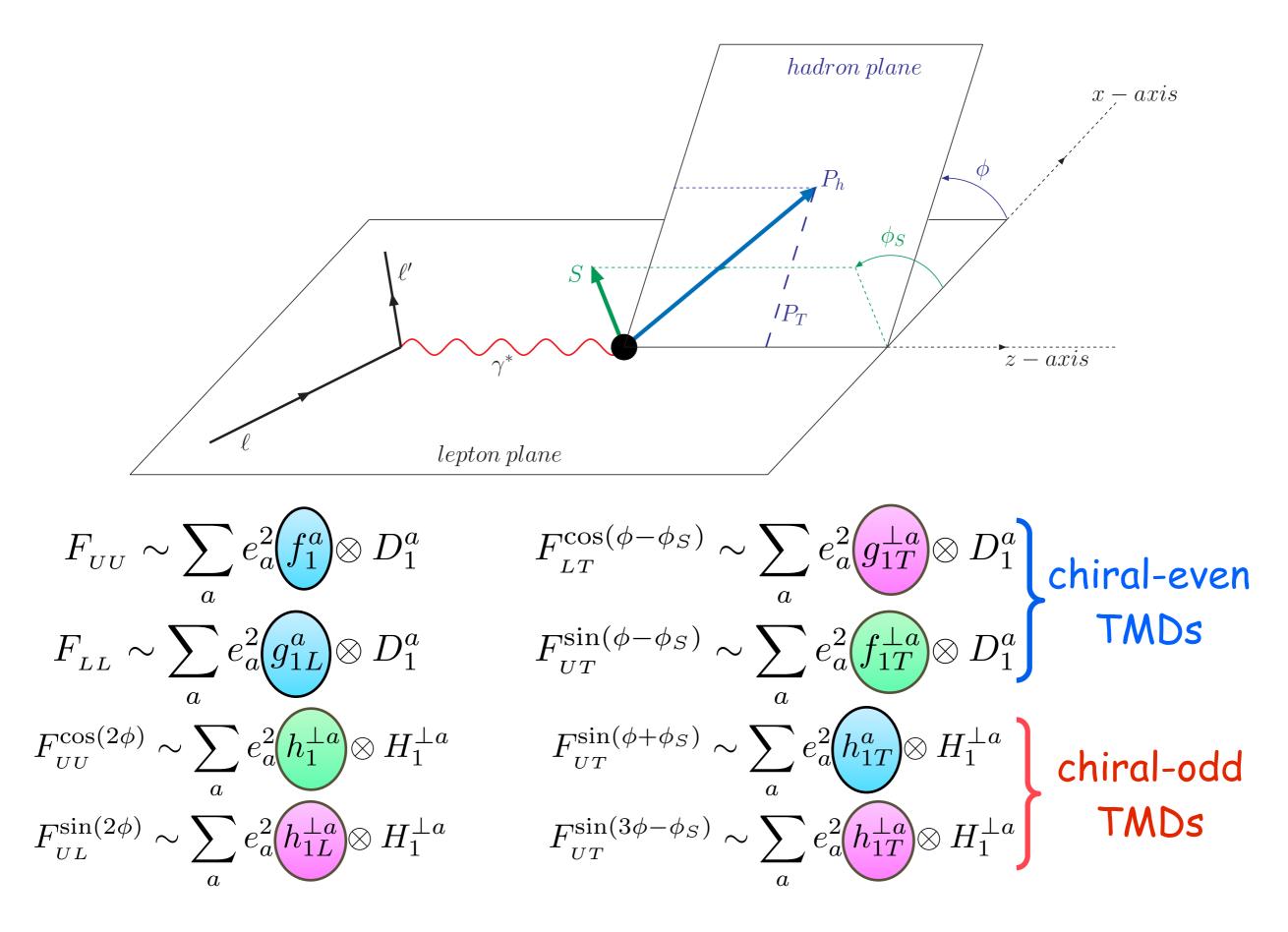
Collins, Soper, Ji, J.P. Ma, Yuan, Qiu, Vogelsang, Collins, Metz,...

general azimuthal structure of SIDIS cross-section (with leading-twist TMDs)

$$\begin{aligned} \frac{\mathrm{d}\sigma}{\mathrm{d}\phi} &= F_{UU} + \cos(2\phi) \, F_{UU}^{\cos(2\phi)} + \frac{1}{Q} \, \cos\phi \, F_{UU}^{\cos\phi} + \lambda \frac{1}{Q} \, \sin\phi \, F_{LU}^{\sin\phi} \\ &+ S_L \left\{ \sin(2\phi) \, F_{UL}^{\sin(2\phi)} + \frac{1}{Q} \, \sin\phi \, F_{UL}^{\sin\phi} + \lambda \left[F_{LL} + \frac{1}{Q} \, \cos\phi \, F_{LL}^{\cos\phi} \right] \right\} \\ &+ S_T \left\{ \sin(\phi - \phi_S) \, F_{UT}^{\sin(\phi - \phi_S)} + \sin(\phi + \phi_S) \, F_{UT}^{\sin(\phi + \phi_S)} + \sin(3\phi - \phi_S) \, F_{UT}^{\sin(3\phi - \phi_S)} \\ &+ \frac{1}{Q} \left[\sin(2\phi - \phi_S) \, F_{UT}^{\sin(2\phi - \phi_S)} + \sin\phi_S \, F_{UT}^{\sin\phi_S} \right] \\ &+ \lambda \left[\cos(\phi - \phi_S) \, F_{LT}^{\cos(\phi - \phi_S)} + \frac{1}{Q} \left(\cos\phi_S \, F_{LT}^{\cos\phi_S} + \cos(2\phi - \phi_S) \, F_{LT}^{\cos(2\phi - \phi_S)} \right) \right] \right\} \end{aligned}$$

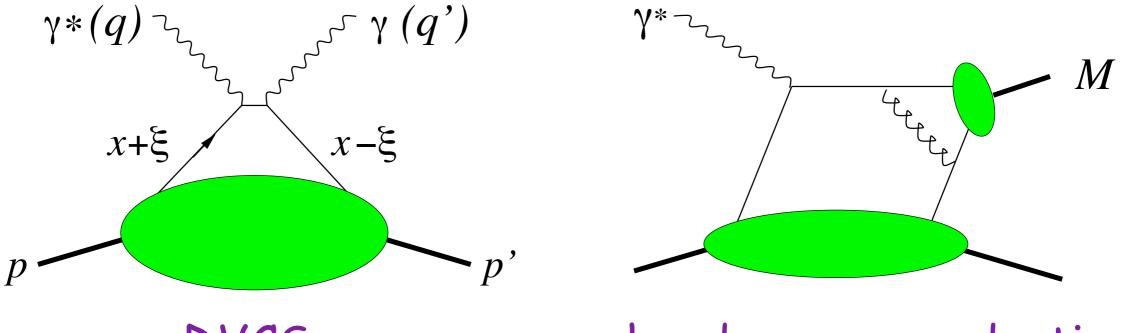
 $\begin{array}{l} \underset{\sigma(\boldsymbol{S}) \neq d\sigma(-\boldsymbol{S}) \\ F_{\boldsymbol{S}_{B}\boldsymbol{S}_{T}}^{(\ldots)} \end{array} \\ \end{array}$

Kotzinian, NP B441 (1995) 234 Mulders and Tangermann, NP B461 (1996) 197 Boer and Mulders, PR D57 (1998) 5780 Bacchetta et al., PL B595 (2004) 309 Bacchetta et al., JHEP 0702 (2007) 093 Anselmino et al., in preparation



talks by A. Kotzinian, S. Melis

GPDs (8 independent ones) (recover partonic distributions in the forward limit) $H, E, \tilde{H}, \tilde{E}; H_T, E_T, \tilde{H}_T, \tilde{E}_T(x, \xi, t)$

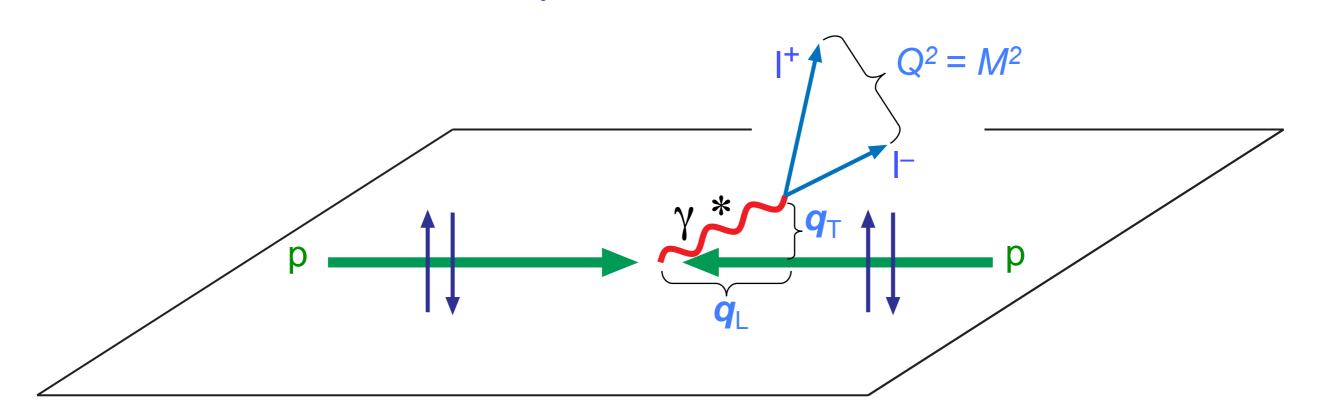


DVCS

hard meson production

exclusive leptonic processes. More possibilities with Drell-Yan production talk by B. Pire

Drell-Yan processes - TMDs



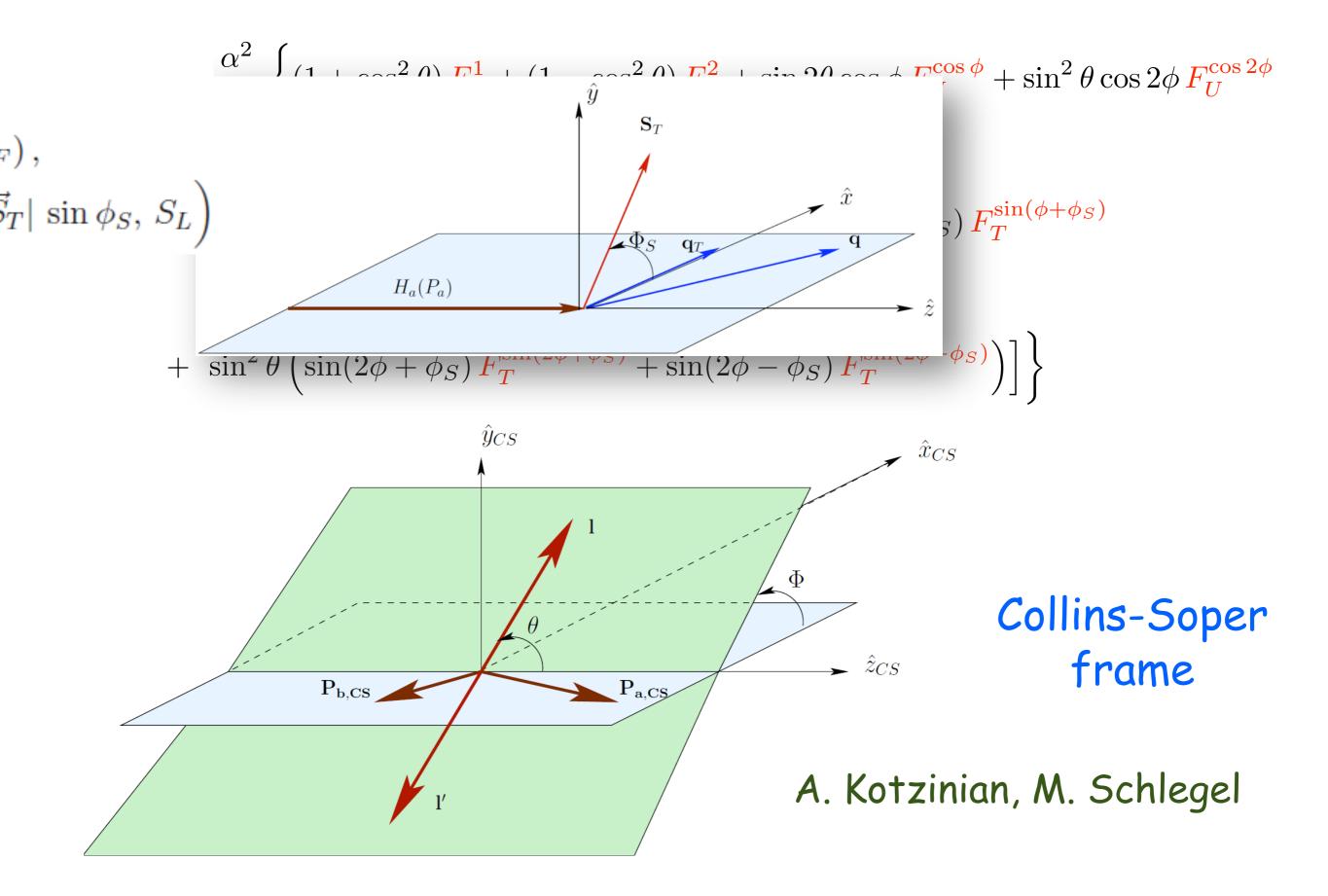
factorization holds, two scales, M^2 , and $q_T \ll M$

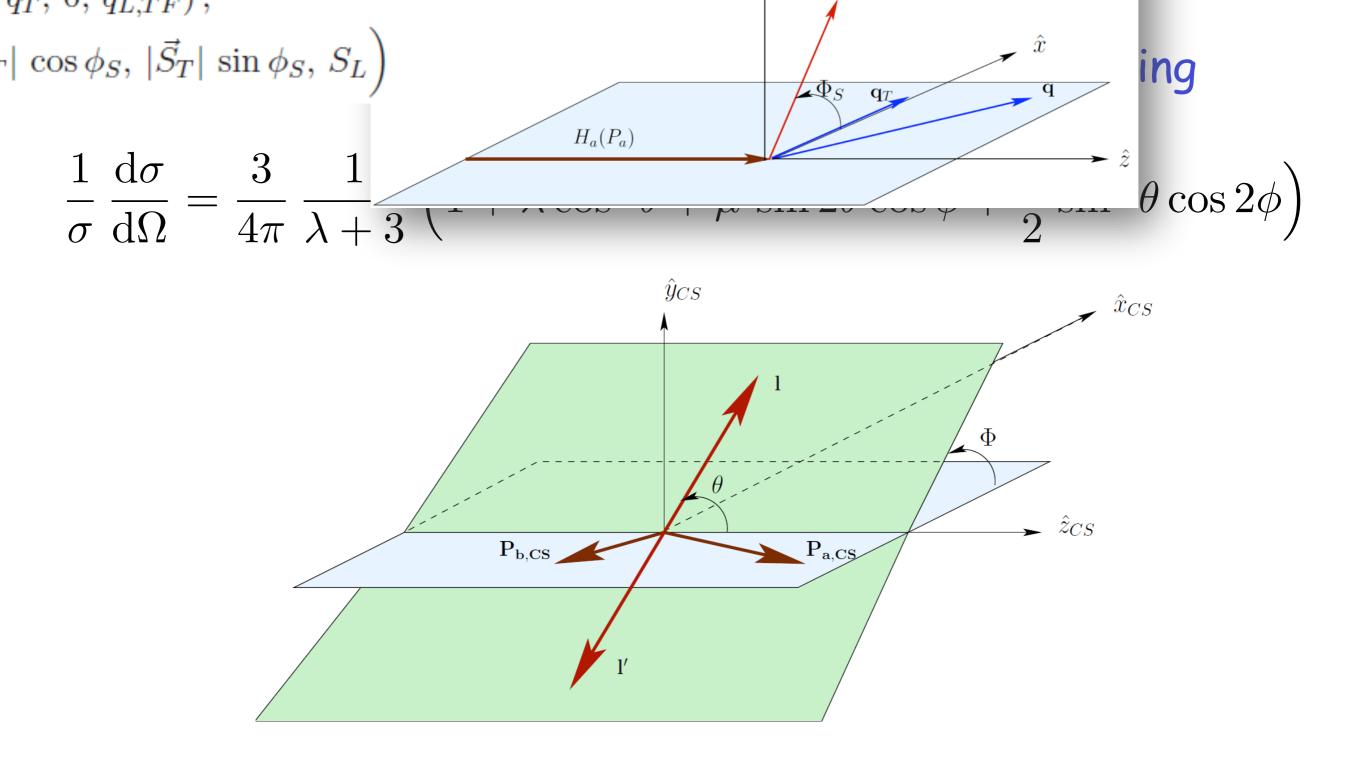
$$\mathrm{d}\sigma^{D-Y} = \sum_{a} f_q(x_1, \mathbf{k}_{\perp 1}; Q^2) \otimes f_{\bar{q}}(x_2, \mathbf{k}_{\perp 2}; Q^2) \,\mathrm{d}\hat{\sigma}^{q\bar{q} \rightarrow \ell^+ \ell^-}$$

direct product of TMDs
no fragmentation process
talks by D. Boer, W. Vogelsang

$$\begin{aligned} & \frac{d\sigma}{d^4 q d\Omega} = \frac{\alpha_{em}^2}{P_t q^2} \times \quad \text{S. Arnold, A. Metz and M. Schlegel, arXiv:0809.2262 [hep-ph]} \\ & \left\{ \left((1 + \cos^2 \theta) F_{UU}^3 + (1 - \cos^2 \theta) F_{UU}^2 + \sin 2\theta \cos \phi F_{UU}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{UU}^{\cos \phi} - \phi \right) \\ & + S_{aL} \left(\sin 2\theta \sin \phi F_{UL}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{UL}^{\sin 2\phi} \right) \\ & + S_{aL} \left(\sin 2\theta \sin \phi F_{UL}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{UL}^{\sin 2\phi} \right) \\ & + S_{bL} \left((\sin 2\theta \sin \phi F_{UL}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{UL}^{\sin 2\phi} \right) \\ & + |S_{aT}| \left[\sin \phi_a \left((1 + \cos^2 \theta) F_{U}^1 + (1 - \cos^2 \theta) F_{TU}^2 + \sin 2\theta \cos \phi F_{UU}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{UU}^{\cos 2\phi} \right) \\ & + \cos \phi_a \left(\sin 2\theta \sin \phi F_{UT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{UT}^{\sin 2\phi} \right) \right] \\ & + |S_{aT}| \left[\sin \phi_b \left((1 + \cos^2 \theta) F_{UT}^1 + (1 - \cos^2 \theta) F_{UT}^2 + \sin 2\theta \cos 2\phi F_{UT}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{UT}^{\cos 2\phi} \right) \\ & + \cos \phi_b \left(\sin 2\theta \sin \phi F_{UT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{UT}^{\sin 2\phi} \right) \right] \\ & + S_{aL} S_{bL} \left[(1 + \cos^2 \theta) F_{LL}^1 + (1 - \cos^2 \theta) F_{LT}^2 + \sin 2\theta \cos \phi F_{LL}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{LL}^{\cos 2\phi} \right) \\ & + \sin \phi_b \left(\sin 2\theta \sin \phi F_{UT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{LT}^{\sin 2\phi} \right) \right] \\ & + |S_{aT}| \left[\cos \phi_b \left((1 + \cos^2 \theta) F_{LT}^2 + (1 - \cos^2 \theta) F_{LT}^2 + \sin 2\theta \cos \phi F_{LT}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{LL}^{\cos 2\phi} \right) \\ & + \sin \phi_b \left(\sin 2\theta \sin \phi F_{LT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{LT}^{\sin 2\phi} \right) \right] \\ & + |S_{aT}| S_{bL} \left[\cos \phi_a \left((1 + \cos^2 \theta) F_{LT}^1 + (1 - \cos^2 \theta) F_{LT}^2 + \sin 2\theta \cos \phi F_{LL}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{LL}^{\cos 2\phi} \right) \\ & + \sin \phi_b \left(\sin 2\theta \sin \phi F_{LT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{LT}^{\sin 2\phi} \right) \right] \\ & + |S_{aT}| \left| S_{bL} \left[\cos \phi_a \left((1 + \cos^2 \theta) F_{LT}^1 + (1 - \cos^2 \theta) F_{LT}^2 + \sin 2\theta \cos \phi F_{TL}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{TL}^{\cos 2\phi} \right) \\ & + \sin \phi_a \left(\sin 2\theta \sin \phi F_{LT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{TL}^{\sin 2\phi} \right) \right] \\ & + |S_{aT}| \left| S_{bL} \left[\cos \phi_a \left((1 + \cos^2 \theta) F_{TL}^3 + (1 - \cos^2 \theta) F_{TT}^2 + \sin 2\theta \cos \phi F_{TT}^{\cos \phi} + \sin^2 \theta \cos 2\phi F_{TT}^{\cos 2\phi} \right) \\ & + \sin \phi_a \left(\sin 2\theta \sin \phi F_{TT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{TL}^{\sin 2\phi} \right) \\ & + \sin \phi_a \left(\sin 2\theta \sin \phi F_{TT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{TT}^{\sin 2\phi} \right) \\ & + \sin \phi_a \left(\sin 2\theta \sin \phi F_{TT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{TT}^{\sin 2\phi} \right) \\ & + \sin (\phi_a - \phi_b) \left((\sin 2\theta \sin \phi F_{TT}^{\sin \phi} + \sin^2 \theta \sin 2\phi F_{TT}^{\sin 2\phi} \right) \\ & + \sin (\phi_a - \phi_b) \left($$

Case of one polarized nucleon only

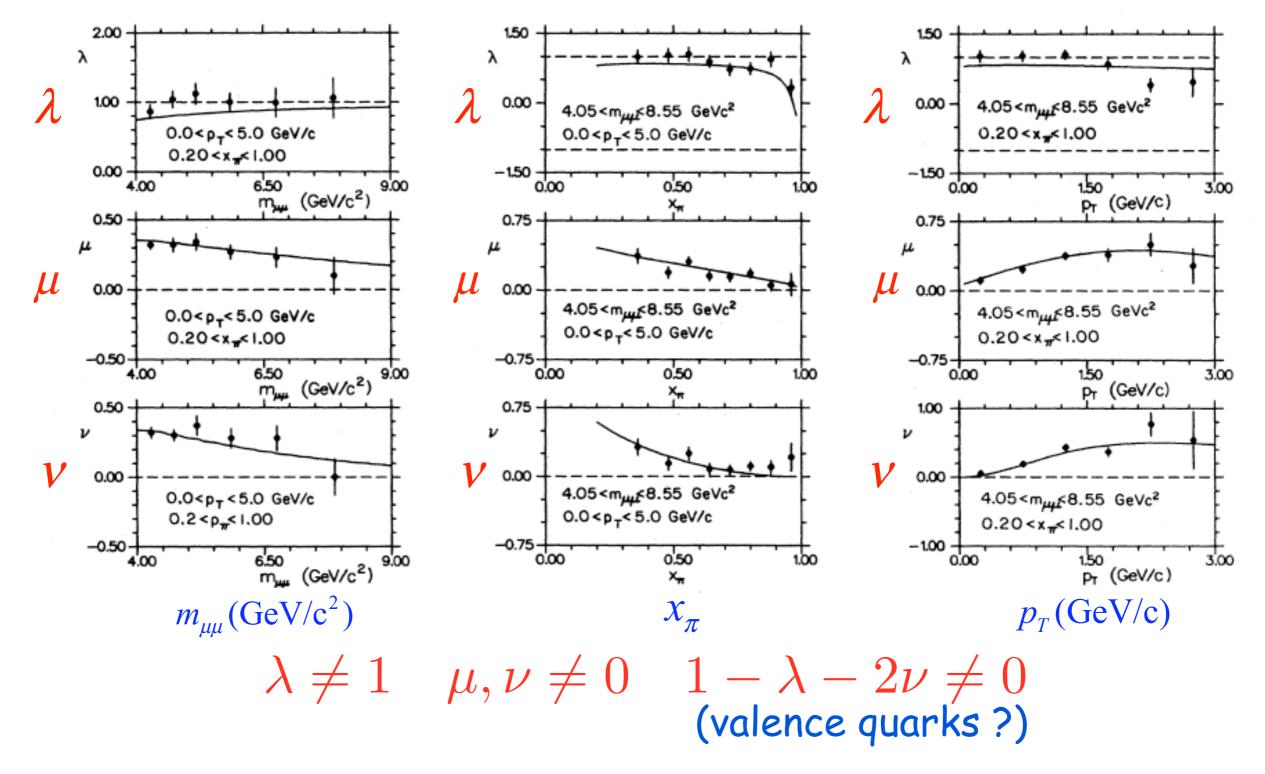




Collins-Soper frame

naive collinear parton model: $\lambda = 1$ $\mu = \nu = 0$

Decay angular distributions in pion-induced Drell-Yan E615 Data 252 GeV π^2 + W Phys. Rev. D 39 (1989) 92



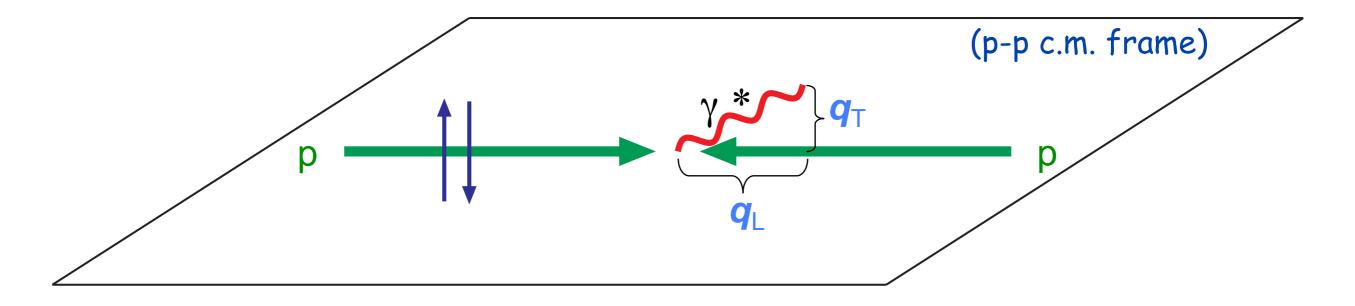
(talk by P. Reimer)

Sivers effect in D-Y processes

By looking at the $d^4 \sigma / d^4 q$ cross section one can single out the Sivers effect in D-Y processes

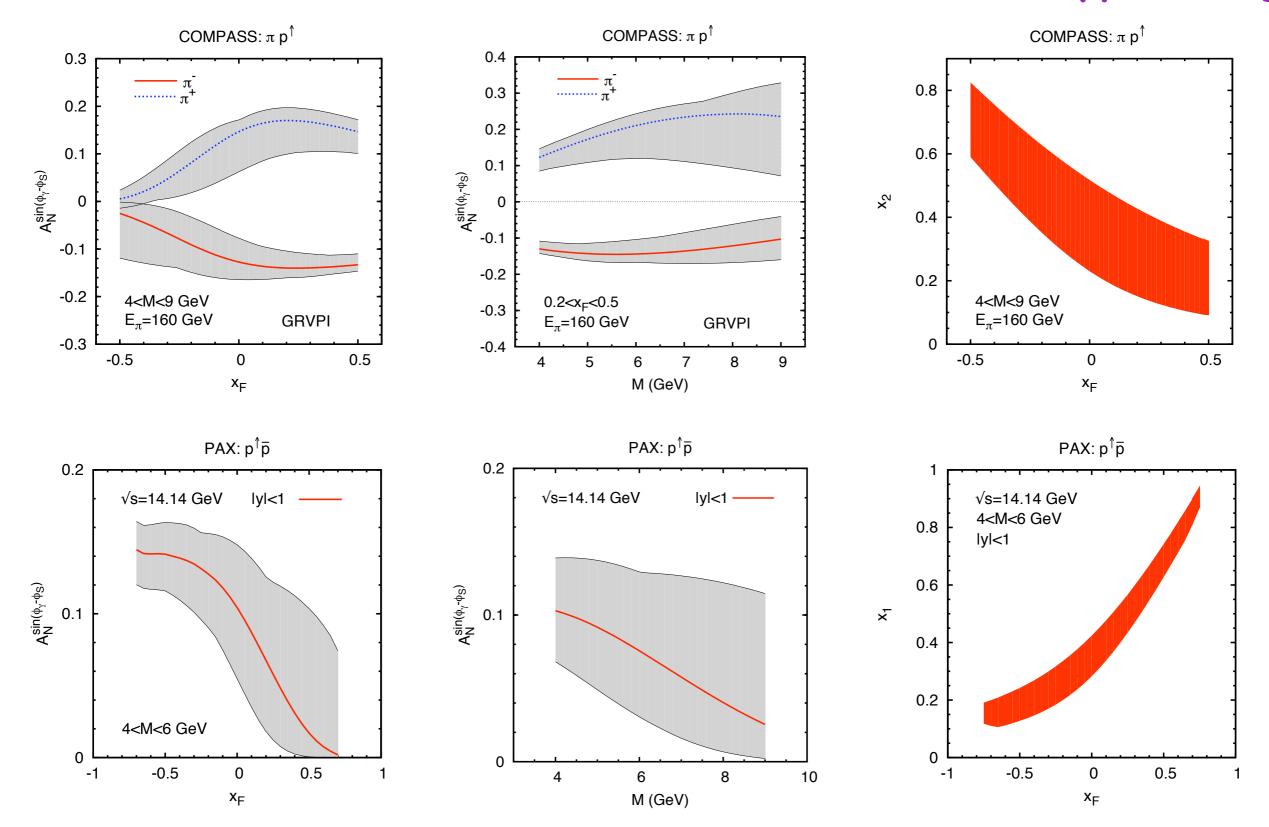
$$d\sigma^{\uparrow} - d\sigma^{\downarrow} \propto \sum_{q} \Delta^{N} f_{q/p^{\uparrow}}(x_{1}, \boldsymbol{k}_{\perp}) \otimes f_{\bar{q}/p}(x_{2}) \otimes d\hat{\sigma}$$
$$q = u, \bar{u}, d, \bar{d}, s, \bar{s}$$

$$A_N^{\sin(\phi_S - \phi_\gamma)} \equiv \frac{2\int_0^{2\pi} \mathrm{d}\phi_\gamma \left[\mathrm{d}\sigma^{\uparrow} - \mathrm{d}\sigma^{\downarrow}\right] \sin(\phi_S - \phi_\gamma)}{\int_0^{2\pi} \mathrm{d}\phi_\gamma \left[\mathrm{d}\sigma^{\uparrow} + \mathrm{d}\sigma^{\downarrow}\right]}$$

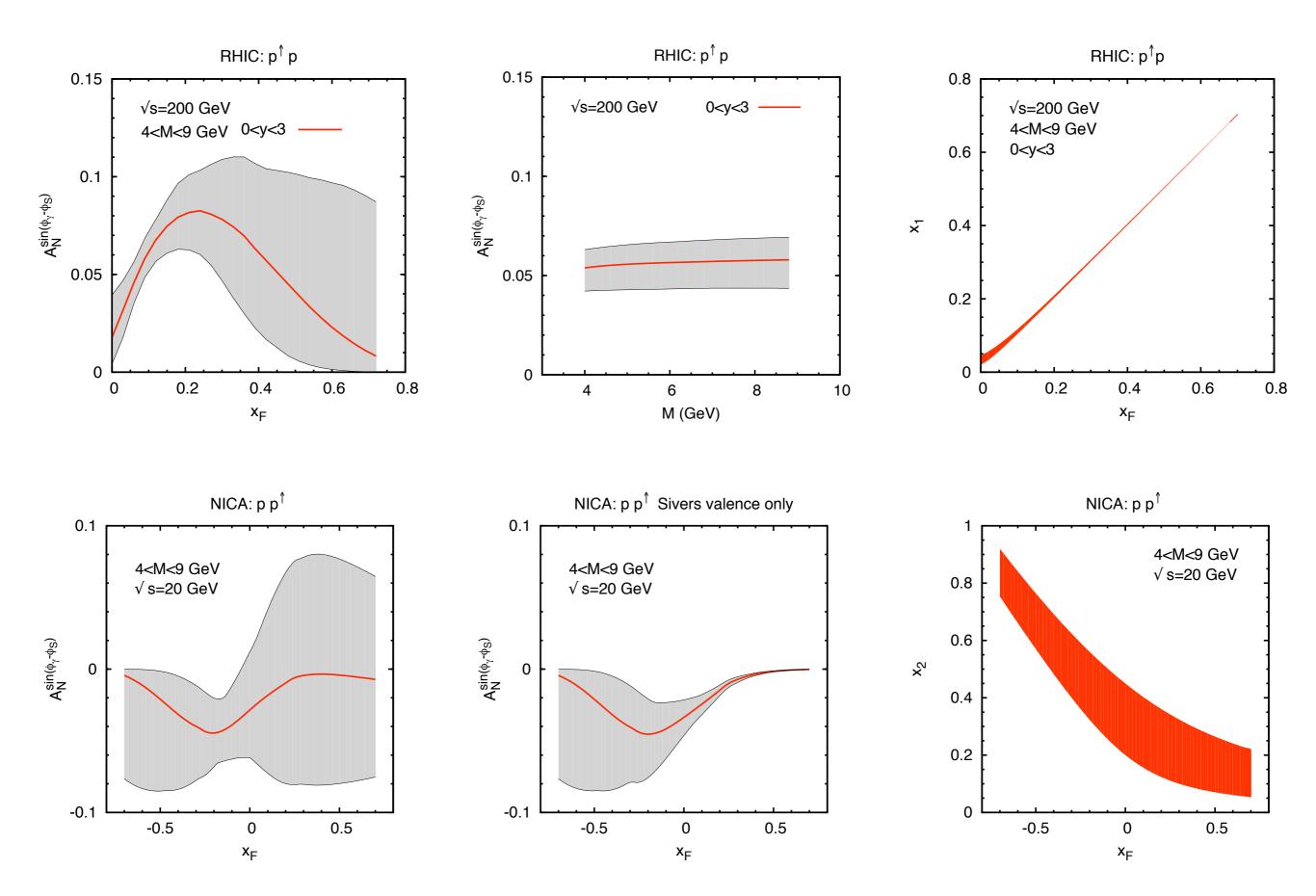


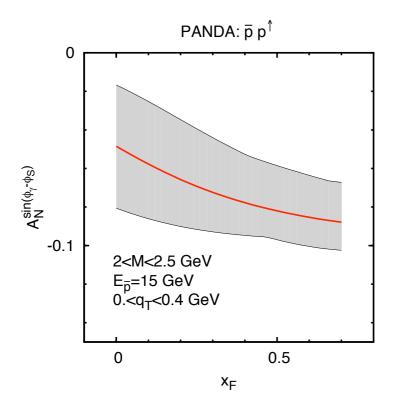
Predictions for A_N

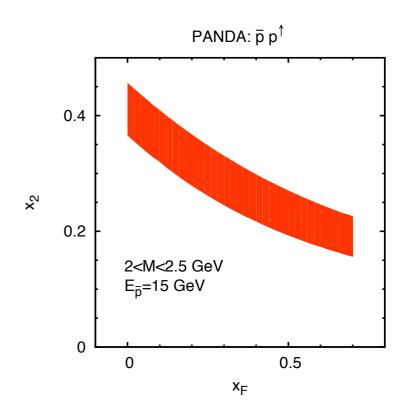
Sivers functions as extracted from SIDIS data, with opposite sign

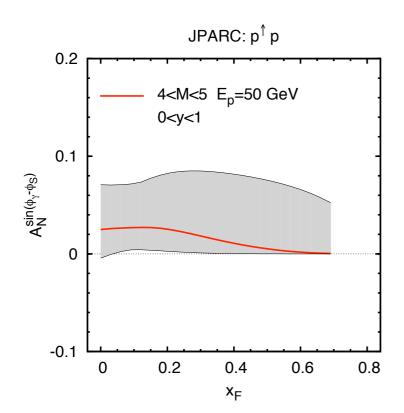


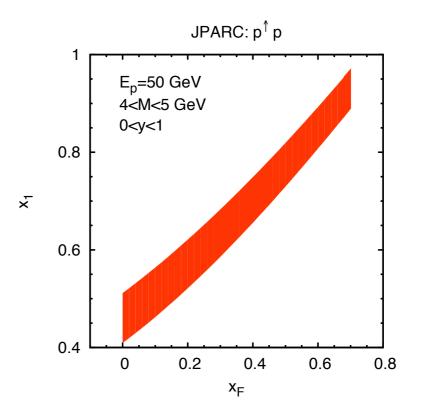
M.A., M. Boglione, U. D'Alesio, S. Melis, F. Murgia, A. Prokudin, e-Print: arXiv:0901.3078







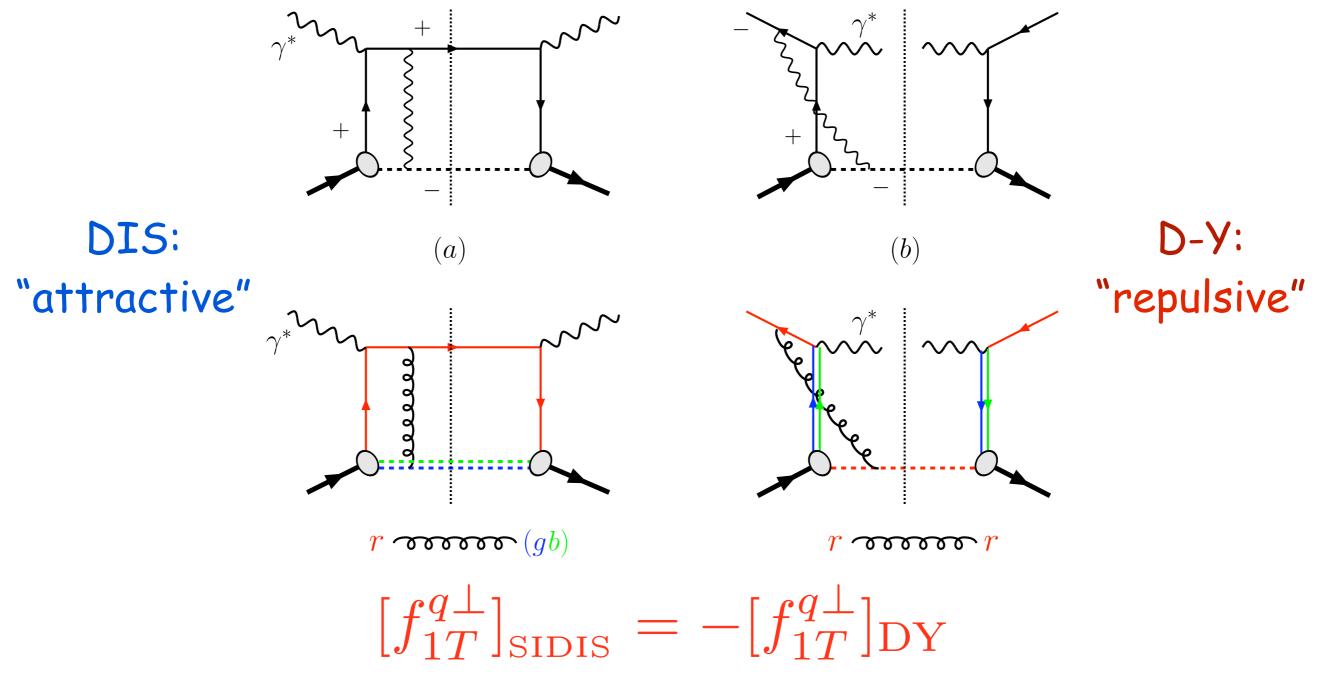




Crucial role of gauge-links in TMDs

Brodsky, Hwang, Schmidt; Collins; Belitsky, Ji, Yuan; Boer, Mulders, Pijlman

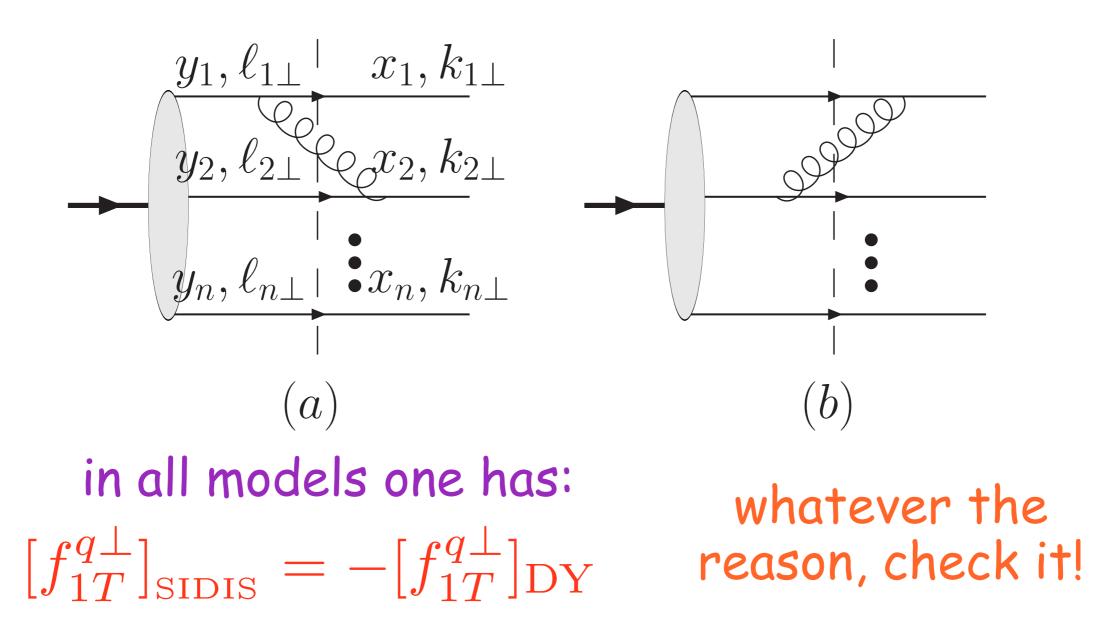
process-dependence of Sivers functions



Talks by D. Boer, A. Bacchetta, round table

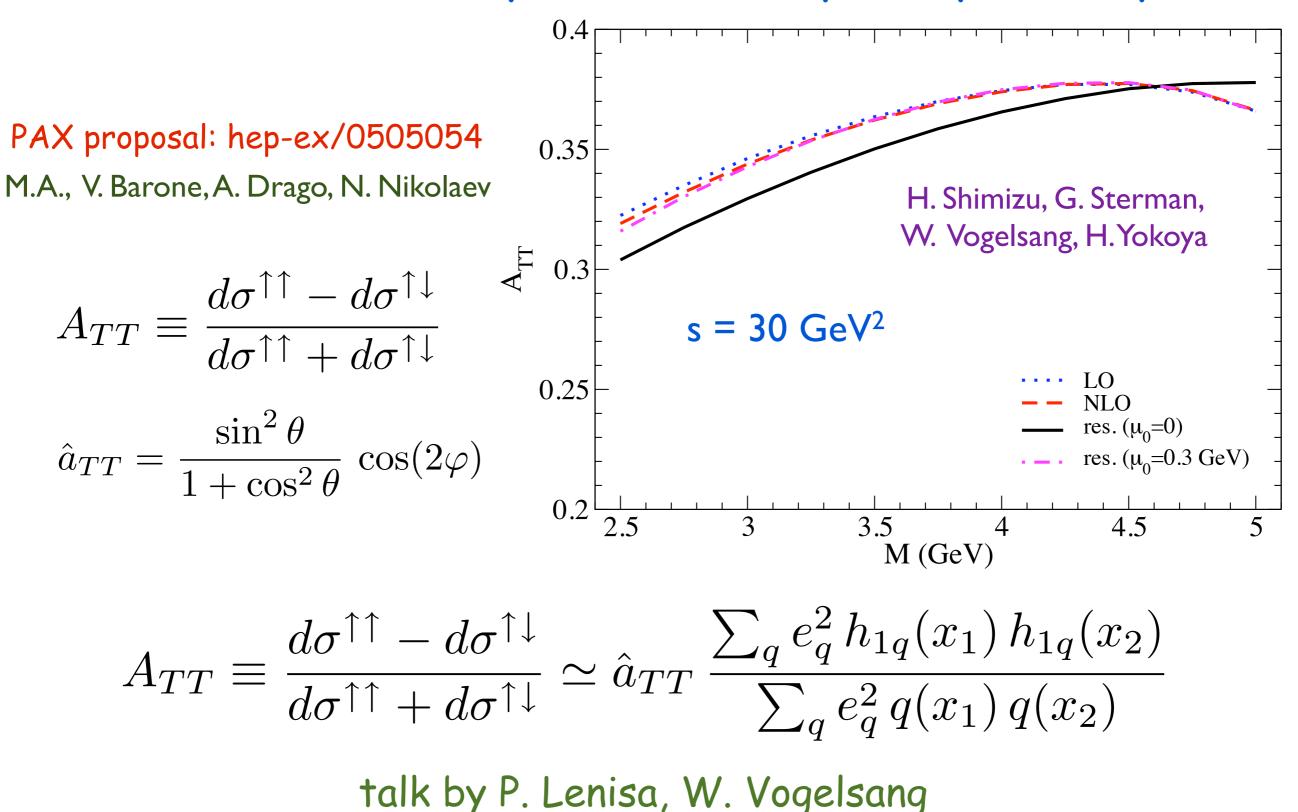
Sivers function from light-front wave function

Brodsky, Pasquini, Xiao, Yuan, arXiv:1001.1163 Pasquini, Yuan, arXiv:1001.5398

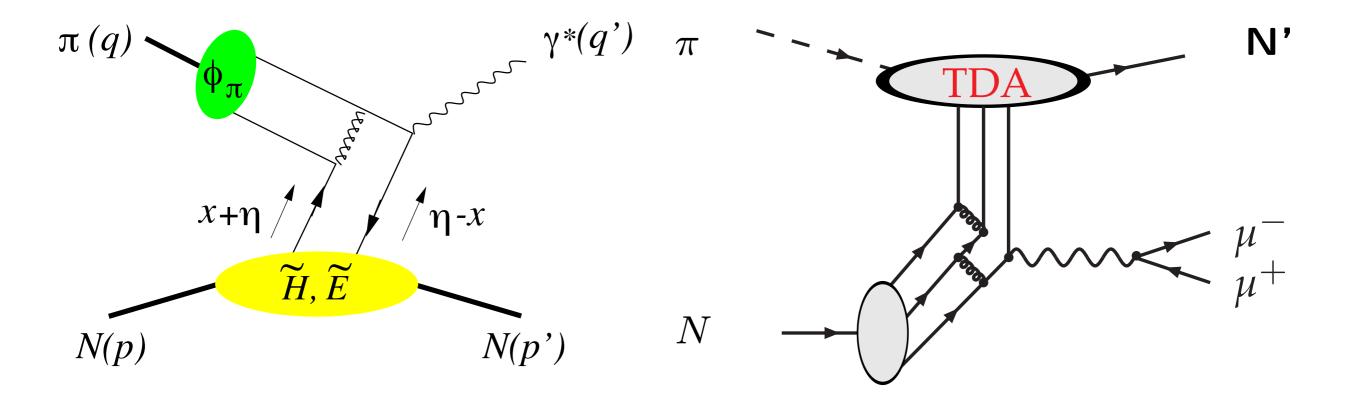


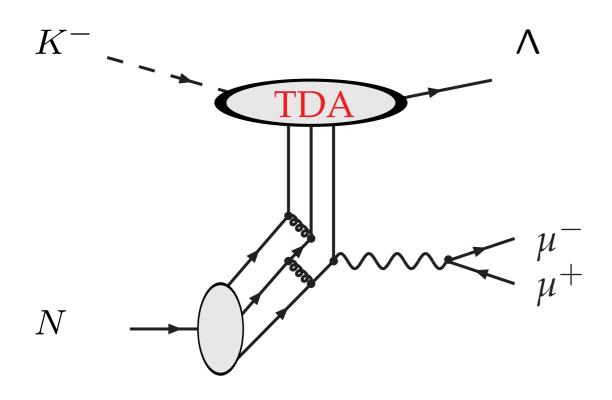
see also Hwang, arXiv:1003.0867 - incorporation of final state interactions into the light-cone wave function

The dream experiment, D-Y with polarized antiprotons measure transversity via double spin asymmetry A_{TT}



Drell-Yan processes - GPDs and TDAs





exclusive limits of Drell-Yan processes (B. Pire)

Conclusions

3-dimensional exploration of nucleon has just started: collect as much data as possible and try to reconstruct the nucleon phase-space structure Drell-Yan processes are cleanest probe ideal machines: x-range including the valence region, Q^2 , M^2 high enough to control higher-twist corrections P_T , Q_T ranges large enough to see transition from TMDs to collinear factorization plenty of challenging theoretical issues.... many thanks to the organizers!