Discriminating among interpretations for X(2900) states

Tim Burns (Swansea University) 29 October 2020

[T.B. & E.Swanson, 2008.12838] [T.B. & E.Swanson, 2009.05352]

Two X(2900) states in $B^+
ightarrow D^+ X$, $X
ightarrow D^- K^+$

<i>X</i> ₀ (2900)	$2.866 \pm 0.007 \pm 0.002 \text{GeV}$	0^+
<i>X</i> ₁ (2900)	$2.904 \pm 0.005 \pm 0.001 \text{GeV}$	1^{-}

Two X(2900) states in $B^+
ightarrow D^+ X$, $X
ightarrow D^- K^+$

$X_0(2900)$ $X_1(2900)$	$\begin{array}{c} 2.866 \pm 0.007 \pm 0.002 \text{GeV} \\ 2.904 \pm 0.005 \pm 0.001 \text{GeV} \end{array}$	0+ 1-	
D*K*	2.902 GeV		

Two X(2900) states in $B^+
ightarrow D^+ X$, $X
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$X_0(2900)$	$2.866 \pm 0.007 \pm 0.002$ GeV	0+
$X_1(2900)$	$2.904 \pm 0.005 \pm 0.001$ GeV	1-
<i>D</i> [∗] <i>K</i> [∗]	2.902 GeV	0 ⁺ , 1 ⁺ , 2 ⁺ (in S-wave)

Two X(2900) states in $B^+
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X ₀ (2900) X ₁ (2900)	$\begin{array}{c} 2.866 \pm 0.007 \pm 0.002 \ \text{GeV} \\ 2.904 \pm 0.005 \pm 0.001 \ \text{GeV} \end{array}$	0+ 1-
$ar{D}^{*}K^{*} \ ar{D}_{1}(2420)K$	2.902 GeV 2.917 GeV	$0^+, 1^+, 2^+$ (in S-wave)

Two X(2900) states in $B^+
ightarrow D^+ X$, $X
ightarrow D^- K^+$

X ₀ (2900) X ₁ (2900)	$\begin{array}{c} 2.866 \pm 0.007 \pm 0.002 \ \text{GeV} \\ 2.904 \pm 0.005 \pm 0.001 \ \text{GeV} \end{array}$	0+ 1-
$ar{D}^*K^*$	2.902 GeV	0 ⁺ , 1 ⁺ , 2 ⁺ (in S-wave)
$ar{D}_1(2420)K$	2.917 GeV	1 ⁻ (in S-wave)

Models

Tetraquark

Tetraquark interpretations:

- ▶ [Karliner & Rosner, 2008.05993]
- [He, Wang & Zhu, 2008.07145]
- [Zhang, 2008.07295]

But

- Mass inconsistent with variational quark model [Lu, Chen, Dong, 2008.07340]
- Analogy with *bound* lattice $ud\bar{b}\bar{b}$ is questionable
- If X(2900) are orbital/radial excitations, where are ground states?
- No evidence for bound udsc in lattice [Hudspith et al 2006.14294], quark model [Zouzou et al 1986], QCD sum rules [Agaev et al 1907.04017]
- ▶ 1⁻ state awkward (P-wave)

Molecule

Many models for $0^+ X_0(2900)$:

- ▶ isoscalar D̄*K* with vector hidden gauge [Molina et al 1005.0355, 2008.11171]
- ▶ isoscalar \overline{D}^*K^* with effective Lagrangian [Liu et al 2008.07389]
- ▶ isovector D
 ^{*}K^{*} with effective Lagrangian [He and Chen 2008.07782]
- ▶ isoscalar D̄*K* with heavy quark symmetry [Hu et al 2008.06894]
- ▶ isoscalar D̄*K* with molecular and diquark d.o.f. [Chen et al 2008.07516, Xue et al 2008.09516]

The $1^- X_1(2900)$ is more difficult:

▶ virtual state from $\bar{D}_1(2420)K$ [He and Chen 2008.07782]







Channels with thresholds near 2900 MeV





colour-suppressed!



















This is an example fit.

Given parametric freedom, can't really distinguish triangle scenario (weak FSIs) from resonance scenario (strong FSIs)

Discriminating among models [T.B. & E.Swanson, 2009.05352]



$\bar{b} \rightarrow \bar{c}(c\bar{s})$ Cabibbo-favoured

colour-favoured

Other diagrams gives wrong flavours and/or are colour suppressed

















Note the absence of
$$B^+ \rightarrow D^+ D^- K^+$$









































Results for $X_1(2900)$ and its charged partners (For $X_0(2900)$ scale by 5.6 / 30.6)

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, ${\cal I}$ mixed	30.6	23.2	$4.3 \tan^2 \left(\theta + \frac{\pi}{4} \right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4} \right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

Results for $X_1(2900)$ and its charged partners								
(FOF A ₀ (2900) Scale by 5.67 50.67								
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$		
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7		
$f(B \to DX, X \to \bar{D}K)$								
Triangle, QE	30.6	23.2	0	0	4.6	8.3		
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1		
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$		
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0		
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4		
Resonance, I mixed	30.6	23.2	$4.3 \tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$				
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41		

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Results for X_1 (For $X_0(2900)$ s	charged X modes					
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$B^0 \to D^+ X^-, \\ X^- \to D^- K^0$
$\mathcal{B}(B \to D\bar{D}K)$	$2.2\ \pm 0.7$	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3 \tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

	triangle diagram with quark-exchange (QE), one-pion exchange (OPE) or effective field theory (EFT) interactions							
/		$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$	
1	$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	$14.5\ \pm 3.3$	7.5 ± 1.7	
,	$f(B \to DX, X \to \bar{D}K)$)						
	Triangle, QE	30.6	23.2	0	0	4.6	8.3	
	Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1	
	Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$	
	Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0	
	Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4	
_	Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$			
2	$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41	

		$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
B	$(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
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Δ	f/f	0.1	0.53	0.36	0.35	0.41	0.41

Resonance, either molecular or tetraquark Mixed isospin case relevant for molecule

$f(B \to DX, X \to \bar{D}K) = \mathcal{B}(B \to DX, X \to \bar{D}K)$								
[,	$\mathcal{B}(B \to L)$	$(\bar{D}K)$					
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \to D^+ X^-, \\ X^- \to D^- K^0 \end{array}$		
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$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41		

$f(B \to DX, X \to$	$(\bar{D}K) = \mathcal{B}$	$\frac{\mathcal{B}(B \to DX, X \to \bar{D}K)}{\mathcal{B}(B \to D\bar{D}K)}$		relations among matrix elements and small correction (B lifetime)		
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
${\cal B}(B\to D\bar{D}K)$	$2.2\ \pm 0.7$	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
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Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

$f(B \to DX, X \to$	$\bar{D}K) = \mathcal{B}$	$\frac{\mathcal{B}(B \to DX, Z)}{\mathcal{B}(B \to D)}$	$X \to \bar{D}K)$ $\bar{D}\bar{K})$	matrix o	elements eq	ual
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
${\cal B}(B\to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

$f(B \to DX, X \to$	$(\bar{D}K) = \mathcal{B}$	$\mathcal{B}(B \to DX, Z)$ $\mathcal{B}(B \to D)$	$X \to \bar{D}K)$	enhanceme	ent if 3-body	small
	$B^+ \to D^+ X, \\ X \to D^- K^+$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$	1					
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3 \tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

$\frac{\mathcal{B}(B \to D\bar{D}K)}{\mathcal{B}(B \to D\bar{D}K)}$									
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$B^0 \to D^+ X^-, \\ X^- \to D^- K^0$			
$\mathcal{B}(B \to D\bar{D}K)$	$2.2\ \pm 0.7$	$2.7\ \pm 1.1$	15.5 ± 2.1	$10.7 \ \pm 1.1$	14.5 ± 3.3	$7.5 \ \pm 1.7$			
$f(B \to DX, X \to \bar{D}K)$	1								
Triangle, QE	30.6	23.2	0	0	4.6	8.3			
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1			
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\tfrac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$			
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0			
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4			
Resonance, ${\cal I}$ mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$					
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41			

fractional uncertainty

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to \bar{D}K)$
		$\mathcal{B}(B \to D\bar{D}K)$

$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
30.6	23.2	0	0	4.6	8.3
30.6	23.2	1.1	1.5	1.2	2.1
30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$
30.6	23.2	4.3	5.8	0	0
30.6	23.2	4.3	5.8	18.6	33.4
30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
0.1	0.53	0.36	0.35	0.41	0.41
	$B^+ \rightarrow D^+ X, X \rightarrow D^- K^+$ 2.2 ± 0.7 30.6 30.6 30.6 30.6 30.6 30.6 0.1	$\begin{array}{cccc} B^+ \to D^+ X, \\ X \to D^- K^+ \\ \end{array} & \begin{array}{c} B^0 \to D^0 X, \\ X \to D^0 K^0 \\ \end{array} \\ \hline 2.2 \pm 0.7 \\ 2.7 \pm 1.1 \\ \hline 30.6 \\ 23.2 \\ 30.6 \\ 23.2 \\ 30.6 \\ 23.2 \\ 30.6 \\ 23.2 \\ 30.6 \\ 23.2 \\ 30.6 \\ 23.2 \\ \hline 30.6 \\ \hline$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

existing channel is largest

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to \bar{D}K)$
		$\mathcal{B}(B \to D\bar{D}K)$

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, X \to \bar{D}^0 K^0$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

neutral mode is comparable

general prediction, same for all models

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to \bar{D}K)$
		$\mathcal{B}(B \to D\bar{D}K)$

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$ \begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array} $
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

remaining predictions discriminate among models , uncertainties are large but predictions still discriminate

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to \bar{D}K)$
		$\mathcal{B}(B \to D\bar{D}K)$

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$	
${\cal B}(B\to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7	
$f(B \to DX, X \to \bar{D}K)$							
Triangle, QE	30.6	23.2	0	0	4.6	8.3	
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1	
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$	
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0	
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4	
Resonance, I mixed	30.6	23.2	$4.3 \tan^2 \left(\theta + \frac{\pi}{4} \right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$			
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41	
same production mode							

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to DK)$
		$\mathcal{B}(B \to D\bar{D}K)$

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1\left(1-\frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\tfrac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3 \tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4} \right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41
same production mode						

$f(B \to DX, X \to X)$	(DK) = ($\frac{\mathcal{B}(B \to DX, Z)}{\mathcal{B}(B \to D)}$	$\overline{D}\overline{D}\overline{K}$	selectior /	n rule	
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, X \to \bar{D}^0 K^0$	$ \begin{array}{c} B^+ \to D^+ X, \\ X \to \overline{D}^0 K^0 \end{array} $	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \to D^+ X^-, \\ X^- \to D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41
	sam	e production m	iode	-		

$f(B \to DX, X \to X)$	$B \to DX, X \to \bar{D}K) = \frac{\mathcal{B}(B \to DX, X \to DK)}{\mathcal{B}(B \to D\bar{D}K)}$				discriminates, despite large uncertainties		
	$B^+ \to D^+ X, \\ X \to D^- K^+$	$B^0 \to D^0 X, X \to \bar{D}^0 K^0$	$ \begin{array}{c} B^+ \to D^+ X, \\ X \to \overline{D}^0 K^0 \end{array} $	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$B^0 \to D^+ X^-, \\ X^- \to D^- K^0$	
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7	
$f(B \to DX, X \to \bar{D}K)$							
Triangle, QE	30.6	23.2	0	0	4.6	8.3	
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1	
Triangle, EFT	30.6	23.2	$1.1\left(1-\frac{C_0}{C_y}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$	
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0	
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4	
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$)		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41	
	sam	e production m	node				

	,	$\mathcal{B}(B \to D)$	$(\bar{D}K)$	со	nstraint on co	ntact terms
	$B^+ \to D^+ X, \\ X \to D^- K^+$	$B^0 \to D^0 X, X \to \bar{D}^0 K^0$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \to D^+ X^-, \\ X^- \to D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1\left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3 \tan^2\left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4} \right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41
	sam	e production m	ode	-		

$f(B \to DX, X \to X)$	$X \to \bar{D}K) = \frac{\mathcal{B}(B \to DX, X \to DK)}{\mathcal{B}(B \to D\bar{D}K)}$			constraint on isospin mixing angle		
	$B^+ \to D^+ X, \\ X \to D^- K^+$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$ \begin{array}{c} B^+ \to D^+ X, \\ X \to \overline{D}^0 K^0 \end{array} $	$ \begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array} $	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \to D^+ X^-, \\ X^- \to D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	9	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1 - \frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8\tan^2\left(\theta-\frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41
	sam	e production m	iode			

$f(B \to DX, X \to \bar{D}K)$	=	$\mathcal{B}(B \to DX, X \to \bar{D}K)$
		$\mathcal{B}(B \to D\bar{D}K)$

	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, \\ X \to \overline{D}^0 K^0$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$B^0 \to D^0 X, \\ X \to D^- K^+$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$	1					
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1\left(1-\frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\tfrac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8\tan^2\left(\theta-\frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

similar patterns for neutral X in neutral B decays

$f(B \to DX, X \to$	$(\bar{D}K) = l$	$\bar{D}K$) = $\mathcal{B}(B \to DX, X \to DK)$			triangle selection rule opposite		
	,	$\mathcal{B}(B \to A)$	$D\bar{D}K)$	/			
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$B^0 \to D^0 X, \\ X \to \overline{D}^0 K^0$	$B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0$	$ \begin{array}{c} B^0 \to D^0 X, \\ X \to D^- K^+ \end{array} $	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$B^0 \to D^+ X^-, \\ X^- \to D^- K^0$	
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7	
$f(B \to DX, X \to \bar{D}K)$							
Triangle, QE	30.6	23.2	0	0	4.6	8.3	
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1	
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$	
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0	
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4	
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8\tan^2\left(\theta-\frac{\pi}{4}\right)$			
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41	

similar patterns for neutral X in neutral B decays

$(B \to DX, X \to \overline{D}K) = \frac{\mathcal{B}(B \to DX, X \to \overline{D}K)}{\mathcal{B}(B \to D\overline{D}K)}$					charged partners discriminate among models	
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array}$	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	$2.2\ \pm 0.7$	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$	1					
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

$\mathcal{B}(B \to DX, X \to \bar{D}K) = \frac{\mathcal{B}(B \to DX, X \to DK)}{\mathcal{B}(B \to D\bar{D}K)}$					charged partners discriminate among models	
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$ \begin{array}{c} B^+ \rightarrow D^0 X^+, \\ X^+ \rightarrow \bar{D}^0 K^+ \end{array} $	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	$2.2\ \pm 0.7$	$2.7\ \pm 1.1$	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1 \left(1 + \frac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8 <	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2\left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

E TO

10/ 0

absent only in I=0 resonance scenario

$(B \to DX, X \to \bar{D}K) = \frac{\mathcal{B}(B \to DX, X \to DK)}{\mathcal{B}(B \to D\bar{D}K)}$					charged partners discriminate among models	
	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to \bar{D}^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$ \begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to \bar{D}^0 K^+ \end{array} $	$\begin{array}{c} B^0 \rightarrow D^+ X^-, \\ X^- \rightarrow D^- K^0 \end{array}$
$\mathcal{B}(B \to D\bar{D}K)$	2.2 ± 0.7	2.7 ± 1.1	15.5 ± 2.1	10.7 ± 1.1	14.5 ± 3.3	7.5 ± 1.7
$f(B \to DX, X \to \bar{D}K)$	1					
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$1.1 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.5\left(1-\frac{C_0}{C_1}\right)^2$	$1.2\left(1+\frac{C_0}{C_1}\right)^2$	$2.1\left(1+\tfrac{C_0}{C_1}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$4.3\tan^2\left(\theta+\frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0.36	0.35	0.41	0.41

E TO

10 (D)

enormous fit fractions in I=1 resonance scenario

Resonance scenarios only:

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$$\mathcal{B}(B \to DX, X \to \bar{D}K) = \mathcal{B}(B \to DX)\mathcal{B}(X \to \bar{D}K)$$

Resonance scenarios only:

 $\mathcal{B}(B \to DX, X \to \bar{D}K) = \mathcal{B}(B \to DX)\mathcal{B}(X \to \bar{D}K)$



Resonance scenarios only:

 $\mathcal{B}(B \to DX, X \to \bar{D}K) = \mathcal{B}(B \to DX)\mathcal{B}(X \to \bar{D}K)$





Triangle and resonance scenarios fit experimental data in amplitude model



 K^0

 D^+

Triangle and resonance scenarios fit experimental data in amplitude model

Assuming

- dominance of colour-favoured transitions, and
- isospin

we get relations among fit fractions



	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^- K^+ \end{array}$	$\begin{array}{c} B^0 \to D^0 X, \\ X \to D^0 K^0 \end{array}$	$\begin{array}{c} B^+ \to D^+ X, \\ X \to D^0 K^0 \end{array}$	$\begin{array}{c} B^0 \rightarrow D^0 X, \\ X \rightarrow D^- K^+ \end{array}$	$\begin{array}{c} B^+ \to D^0 X^+, \\ X^+ \to D^0 K^+ \end{array}$	$B^0 \rightarrow D^+ X^-$, $X^- \rightarrow D^- K^0$
$B(B \rightarrow D\bar{D}K)$	$2.2\ \pm 0.7$	$2.7\ \pm 1.1$	15.5 ± 2.1	$10.7\ \pm 1.1$	14.5 ± 3.3	$7.5~\pm 1.7$
$f(B \rightarrow DX, X \rightarrow DK)$						
Triangle, QE	30.6	23.2	0	0	4.6	8.3
Triangle, OPE	30.6	23.2	1.1	1.5	1.2	2.1
Triangle, EFT	30.6	23.2	$-1.1\left(1-\frac{C_0}{C_1}\right)^2$	$1.5 \left(1 - \frac{C_0}{C_1}\right)^2$	$1.2 \left(1 + \frac{C_0}{C_1}\right)^2$	$2.1 \left(1 \pm \frac{C_4}{C_3}\right)^2$
Resonance, $I = 0$	30.6	23.2	4.3	5.8 <	0	0
Resonance, $I = 1$	30.6	23.2	4.3	5.8	18.6	33.4
Resonance, I mixed	30.6	23.2	$-4.3 \tan^2 \left(\theta + \frac{\pi}{4}\right)$	$5.8 \tan^2 \left(\theta - \frac{\pi}{4}\right)$		
$\Delta f/f$	0.1	0.53	0,35	0.35	0.11	0.41
		absent o	only in Ia0 reso	nance scenari	in É	

 D^+

Triangle and resonance scenarios fit experimental data in amplitude model

Assuming

- dominance of colour-favoured transitions, and
- isospin

we get relations among fit fractions

Six possible modes

- some new modes have very large fit fraction
- pattern can discriminate among models