



# **Braneworld Cosmological Effect on Freeze-In Dark Matter Density and Lifetime Frontier**

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# Freeze-in DM

- DM possibly never in thermal equilibrium with SM particle plasma.
- Instead, DM relic density determined by “Freeze-in” mechanism [1].
- Thermal DM case:  $Y = Y_{eq}$  for  $x \ll 1$ ,  $x = m/T$

$$\frac{dY}{dx} = -\frac{s(T=m)}{H(T=m)} \frac{\langle \sigma v_{rel} \rangle}{x^2} (Y^2 - Y_{EQ}^2)$$

- Freeze-in case:  $Y(x_{RH}) = 0$  leads to

$$\frac{dY}{dx} \simeq \frac{s(m)}{H(m)} \frac{\langle \sigma v_{rel} \rangle}{x^2} Y_{EQ}^2 \simeq 0.698 \frac{g_{DM}^2}{g_*^{3/2}} m M_P \frac{\langle \sigma v_{rel} \rangle}{x^2}$$

- In both cases, DM density determined as

$$\Omega_{DM} h^2 = \frac{m Y(\infty) s_0}{\rho_c / h^2}$$



# Freeze-in DM

- Given  $\langle \sigma v_{rel} \rangle$  as a function of  $x$ , Boltzmann equation can be integrated up to  $x = 1$  (kinematic boundary)
- Example: light vector-boson mediator

$$\langle \sigma v_{rel} \rangle = \frac{g_V^4}{128\pi} \frac{x^2}{m^2}$$

leads to DM density of

$$\Omega_{DM} h^2 = \frac{mY(x=\infty)s_0}{\rho_c/h^2} \simeq \frac{mY(x=1)s_0}{\rho_c/h^2} \simeq 1.16 \times 10^{24} \frac{g_{DM}^2}{g_*^{3/2}} g_V^4$$

- Observed DM density of  $\Omega_{DM} h^2 \simeq 0.12$  [2] reproduced by  $g_V = 2.31 \times 10^{-6}$



# Braneworld Cosmologies

- **Modified Friedmann Equation**

- For  $T/T_t < 1$ , standard Big Bang cosmology is reproduced.
- For  $T/T_t > 1$ , the universe evolves differently. Parametrize modified Friedmann equation as

$$H = H_{st}(T) \times F(T)$$

- We assume the following form for  $F(T)$  for  $T/T_t > 1$

$$F(T/T_t) = \left(\frac{T}{T_t}\right)^\gamma = \left(\frac{x_t}{x}\right)^\gamma$$



# Brane-world Cosmologies

- Apply adjusted Hubble parameters to Boltzmann equation. The effective change is

$$\langle \sigma v_{rel} \rangle \rightarrow \left( \frac{\langle \sigma v_{rel} \rangle}{F(x_t/x)} \right) = \langle \sigma v_{rel} \rangle \left( \frac{x_t}{x} \right)^{-\gamma}$$

- DM relic abundance enhanced (reduced) for  $\gamma < 0$  ( $\gamma > 0$ )
- For vector boson mediated process:

$$\Omega_{DM} h^2 = \frac{mY(x=\infty)s_0}{\rho_c/h^2} \simeq \frac{mY(x=1)s_0}{\rho_c/h^2} \simeq 1.16 \times 10^{24} \frac{g_{DM}^2}{g_*^{3/2}} g_V^4 \times \frac{x_t^{-\gamma}}{\gamma+1}$$

$$\Omega_{DM} h^2 = 0.12 \Rightarrow g_V \rightarrow g_V \times \left( \frac{x_t^{-\gamma}}{\gamma+1} \right)^{-\frac{1}{4}}$$



# Braneworld Cosmologies

- **Randall-Sundrum (RS) II Model**

- Friedmann equation for a spatially flat universe [2] yields:

$$H^2 = \frac{\rho}{3M_P^2} \left( 1 + \frac{\rho}{\rho_{RS}} \right) \Rightarrow H \simeq H_{st} \sqrt{\frac{\rho}{\rho_{RS}}} = H_{st} \times \left( \frac{x_t}{x} \right)^2$$

- **Gauss Bonnet (GB) Model**

- Found by adding higher curvature terms to RS action [3].
- Phenomenological requirements fix free parameters.
- Friedmann equation in highest temperature epoch becomes:

$$H \simeq \left( \frac{1 + \beta}{4\beta} \frac{\mu}{M_P^2} \rho \right)^{\frac{1}{3}} \simeq H_{st} \times \left( \frac{\rho}{\rho_{GB}} \right)^{-\frac{1}{6}} = H_{st} \times \left( \frac{x_t}{x} \right)^{-\frac{2}{3}}$$

[3] Binetruy, Deffayet, & Langlois, 2000

[4] Kim et al., 2000



# Application to $Z'$ portal DM with RHN

- Minimal B-L SM Extension with RHN as a DM candidate [4]
  - RHN DM communicates with SM via Higgs-mediated (Higgs-portal) or  $Z'$  mediated ( $Z'$ -portal) processes.
  - DM experiments and LHC have narrowed parameter space for  $Z'$  mediated RHN freeze-in DM [5].

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{B-L}$	$Z_2$
$q_L^i$	<b>3</b>	<b>2</b>	1/6	1/3	+
$u_R^i$	<b>3</b>	<b>1</b>	2/3	1/3	+
$d_R^i$	<b>3</b>	<b>1</b>	-1/3	1/3	+
$l_L^i$	<b>1</b>	<b>2</b>	-1/2	-1	+
$N_R^j$	<b>1</b>	<b>1</b>	0	-1	+
$N_R$	<b>1</b>	<b>1</b>	0	-1	-
$e_R^i$	<b>1</b>	<b>1</b>	-1	-1	+
$H$	<b>1</b>	<b>2</b>	-1/2	0	+
$\Phi$	<b>1</b>	<b>1</b>	0	2	+

[5] Okada et al., 2010

[6] Bauer et. al., 2018



# Application to $Z'$ portal DM with RHN

- Process:  $f\bar{f} \rightarrow Z' \rightarrow NN$

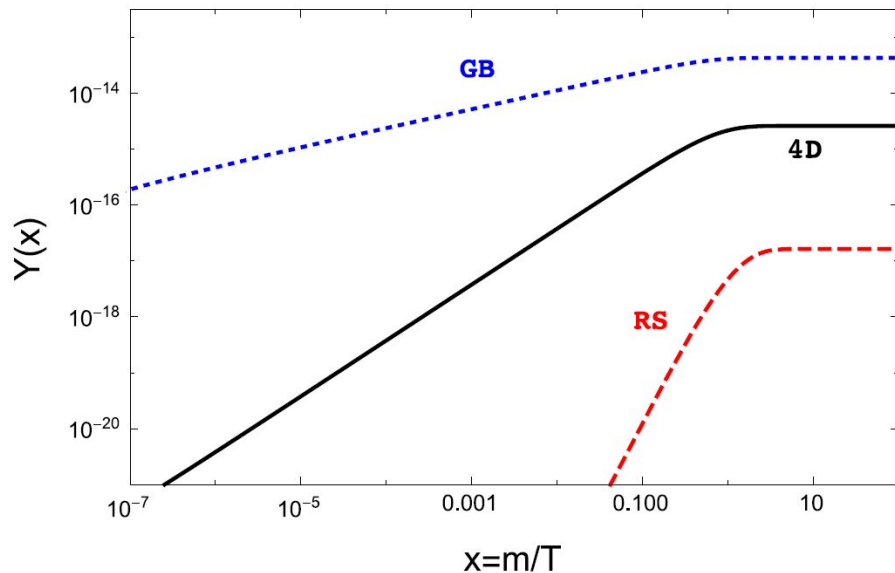
- Numerically solved

Boltzmann equations

- GB Yield enhanced
- RS Yield reduced

- Densities become:

- GB:  $\Omega_{DM} h^2 = 0.12$
- 4D:  $\Omega_{DM} h^2 = 7.2 \times 10^{-3}$
- RS:  $\Omega_{DM} h^2 = 4.5 \times 10^{-5}$



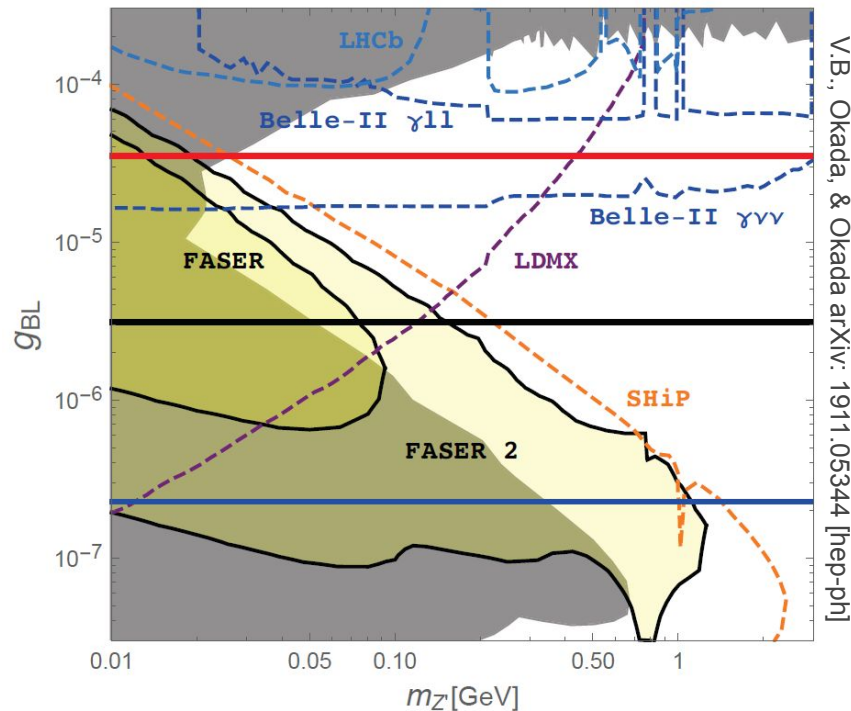
$$m = 10 \text{ TeV}, T_t = 1 \text{ TeV}, m_{Z'} = 1 \text{ GeV}, g_{BL} = 1.54 \times 10^{-6}$$





# Lifetime Frontier Experiments

- Reproducing  $\Omega_{DM} h^2 \simeq 0.12$  requires different values of  $g_{BL}$  for the RS, GB, and standard cosmologies.
- Small  $g_{BL} \Rightarrow$  long-lived  $Z'$
- ForwArD Search ExpeRiment (FASER) for LHC Run-3 and FASER 2 at HL-LHC could search for such a  $Z'$ .





# Summary

- Considered “Freeze-In” DM in the context of 5D Braneworld cosmology.
- Friedmann equation modified in early universe, in turn modifying DM relic density for nonstandard cosmologies.
- For  $Z'$ -portal RHN DM in minimal B-L SM extension, braneworld effect affects value of coupling. Results from Lifetime Frontier Experiments directly inform possibilities for BSM physics and accurate cosmological description of the universe.



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