

A Light Scalar Explanation of Muon $g-2$ and the KOTO Anomaly

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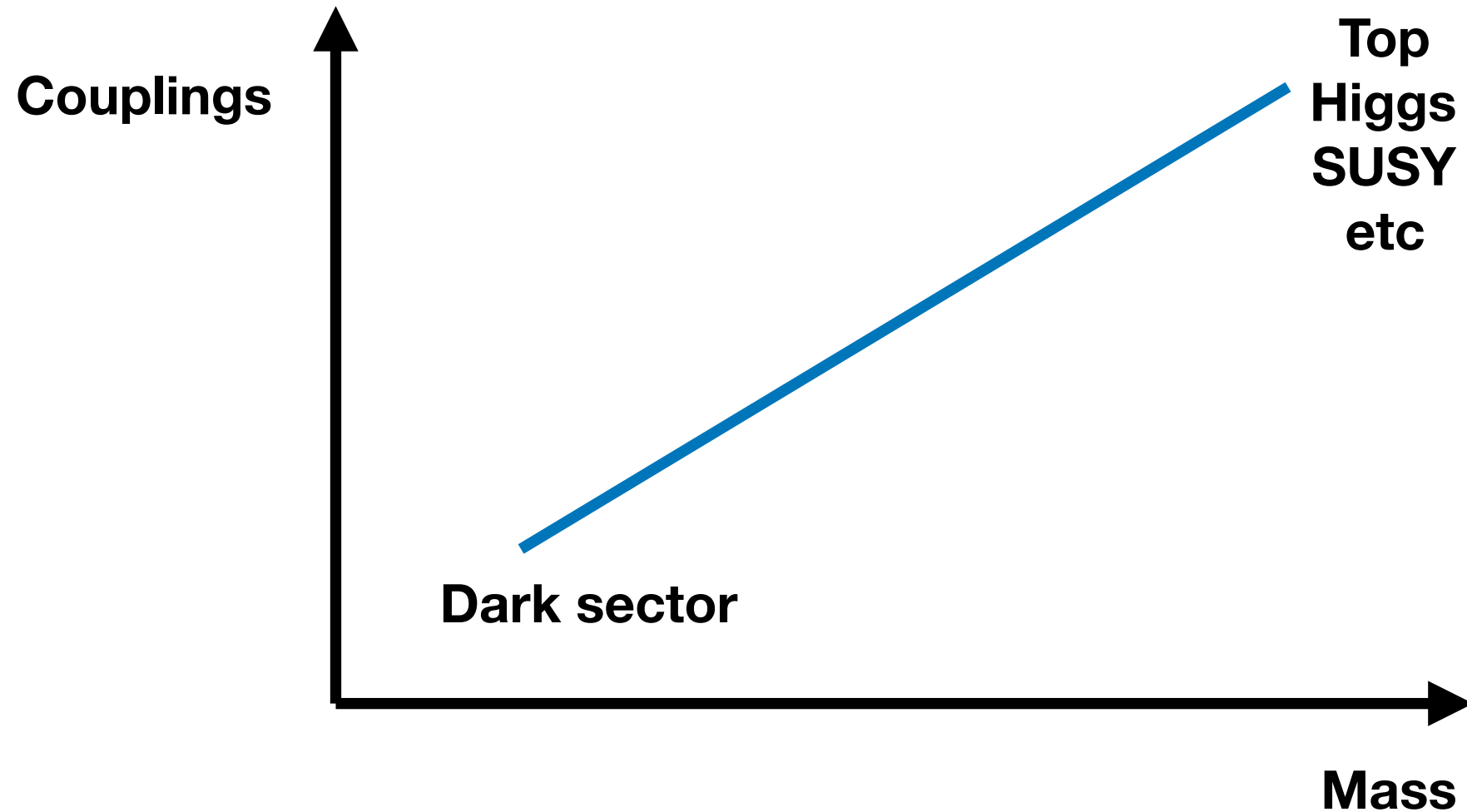
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With Navin McGinnis, Carlos E.M. Wagner and Xiao-Ping Wang
arXiv: [2001.06522](https://arxiv.org/abs/2001.06522) [JHEP04(2020)197]

05/04/2020 Phenomenology 2020 Symposium

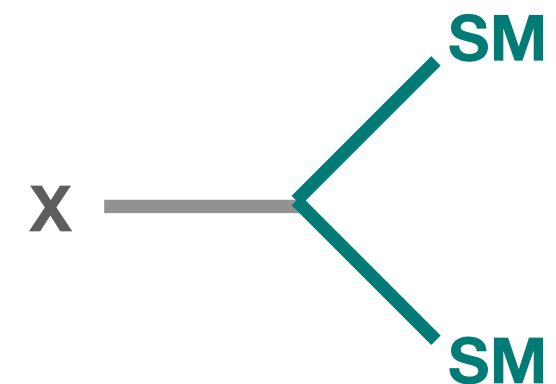
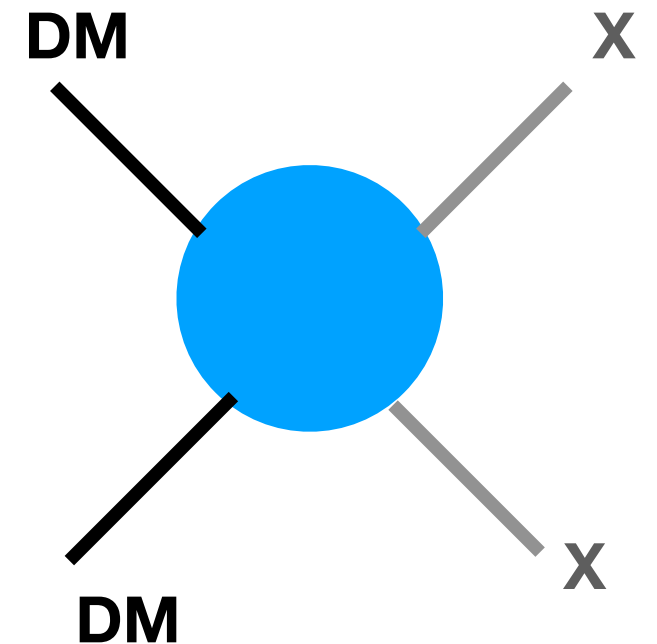
The heavy and the light



- Dark sector particles
 - New light weakly coupled particles
 - Do not interact with the known strong, weak, or electromagnetic forces

The motivation for dark sector particles

- 1. Existence of dark matter
 - do not interact with strong, weak, or electromagnetic forces
 - A zoo of similar particles in the dark sector as in the visible sector
- 2. The null detection of dark matter
 - Secluded annihilation: $DM + DM \rightarrow X + X$
 - X is light and weakly coupled to visible sector



The motivation for **light** dark sector particles

- 3. The experiment status

- Technically difficult to increase E
- Easier to accumulate higher luminosity

- 4. The low energy experiment hints

- **Lepton e/mu g-2** (light scalar at ~ 100 MeV) 1806.10252 Davoudiasl et al ...
- **KOTO**: neutral K decay into $\pi^0 + \text{MET}$ (light scalar < 200 MeV)
1909.11111 Kitahara et al ...
- **MiniBooNE**: (dark neutrino/boson at $10 \sim 100$ MeV)
1807.09877 Bertuzzo et al ...
- **Atomki**: Be^8/He^4 decay into a 17 MeV ee resonance
1604.07411 Feng et al ...

Dark sector model: the Higgs portals

- SM Higgs portal model $H^\dagger H \phi^2, H^\dagger H \phi$

$$\mathcal{L}_{\text{int}} \supset \sin \theta \times \phi \left(\sum_q \frac{m_q}{v} \bar{q}q + \sum_\ell \frac{m_\ell}{v} \bar{\ell}\ell + \dots \right)$$

- More structures with multiple Higgs doublets
 - CP-even scalar mixing

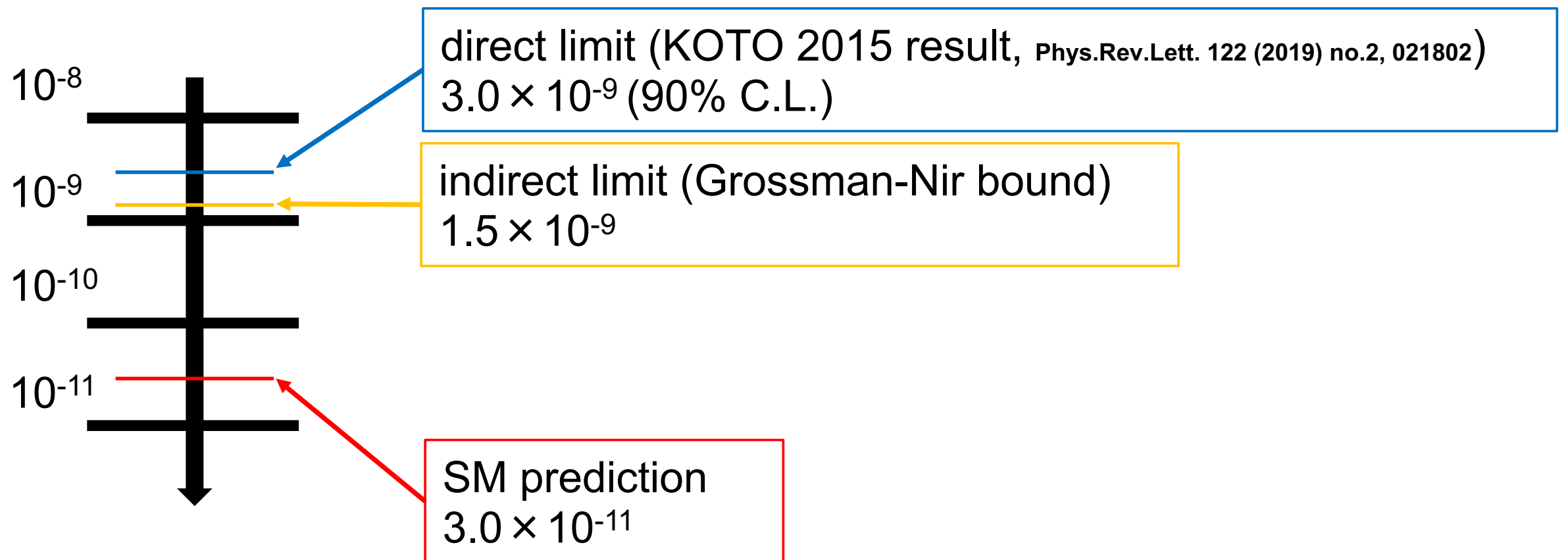
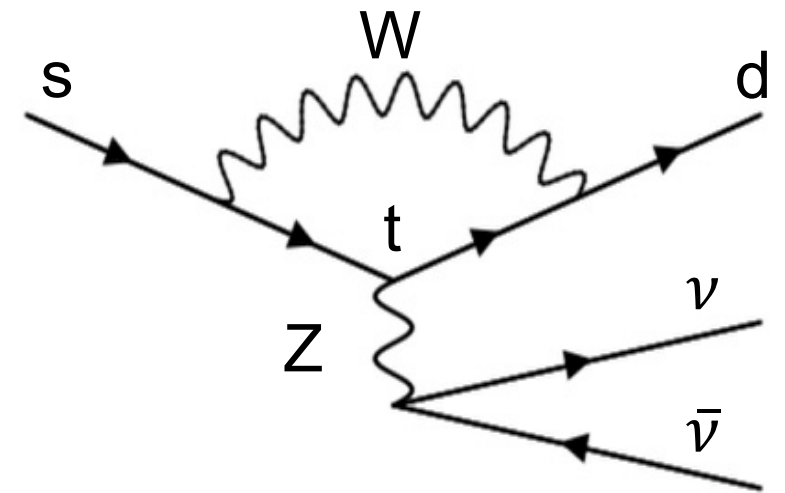
$$H_1^\dagger H_1 \phi, H_2^\dagger H_2 \phi \dots$$

- CP-odd/even scalar mixing

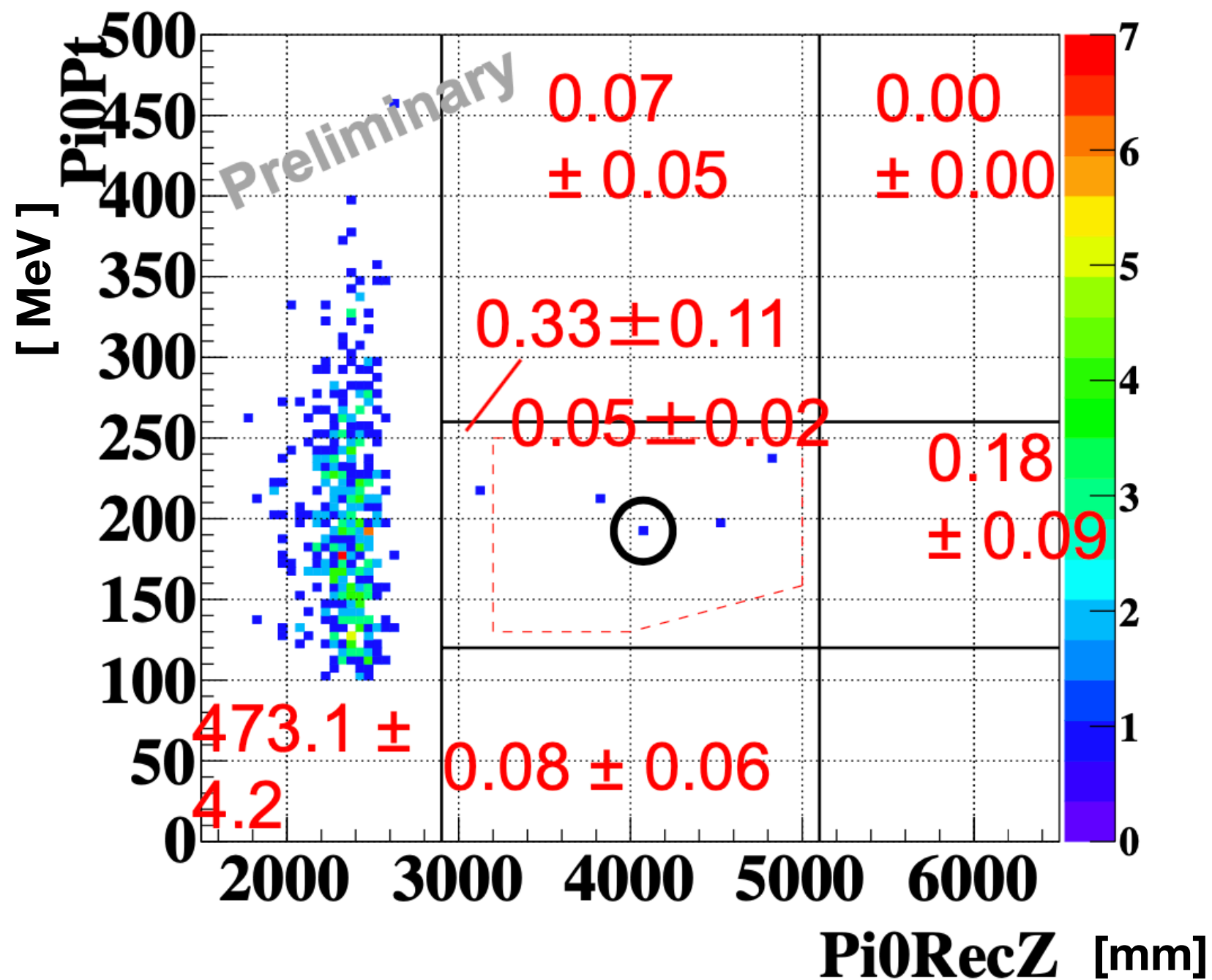
$$H_1^\dagger H_2 \phi + h.c. \dots$$

$K_L \rightarrow \pi^0 \nu \bar{\nu}$ decay

- Direct CPV
- FCNC : highly suppressed decay
 - BR (SM) : 3×10^{-11}
- Small theoretical uncertainty ($\sim 2\%$)
 - Good probe for new physics search



Results from 2016 to 2018 runs



Satoshi Shinohara at KAON2019, 10-13 September, 2019, Perugia, Italy.

Problem to generate a model: Nir-Grossman bound

- KOTO signal
 - Bkg = 0.05(0.02), obs= 3 \rightarrow $BR(K_L \rightarrow \pi^0 \nu\nu) \sim 2 \times 10^{-9}$
- NA62/E949 constraints
 - $BR(K^+ \rightarrow \pi^+ \nu\nu) < 1.85 \times 10^{-10}$
- Nir-Grossman bound
 - isospin symmetry $\Gamma(K_L(\bar{s}d) \rightarrow \pi^0(\bar{d}d)\nu\nu) \approx \Gamma(K^+(\bar{s}u) \rightarrow \pi^0(\bar{d}u)\nu\nu)$
 - Using lifetime of charged and neutral Kaons,
 $BR(K^0 \rightarrow \pi^0 \nu\nu) < 4.3 BR(K^+ \rightarrow \pi^+ \nu\nu)$

The constraint has tension with observed BRs!

Solution 1: long-lived particle

- A light particle ($m < 200$ MeV) from Kaon decay

$$K_L \rightarrow \pi^0 X, \quad K^+ \rightarrow \pi^+ X$$

- If it is long-lived enough to escape KOTO detector (few meters), it can mimic the missing energy
- But an isospin symmetric model is constrained by charged Kaon experiment (Nir-Grossman bound)
- The way out: charged Kaon experiments veto the region when X mass close to pion mass, due to large bkg from
$$K^+ \rightarrow \pi^+ \pi^0$$
- Therefore, long lived particle with mass ~ 140 MeV is viable

Model building: long-lived scalar with simple mixing to SM Higgs

- SM Higgs portal

$$\mathcal{L}_{\text{int}} \supset \sin \theta \times \phi \left(\sum_q \frac{m_q}{v} \bar{q}q + \sum_\ell \frac{m_\ell}{v} \bar{\ell}\ell + \frac{2m_W^2}{v} \phi W_\mu^+ W^{\mu-} + \dots \right)$$

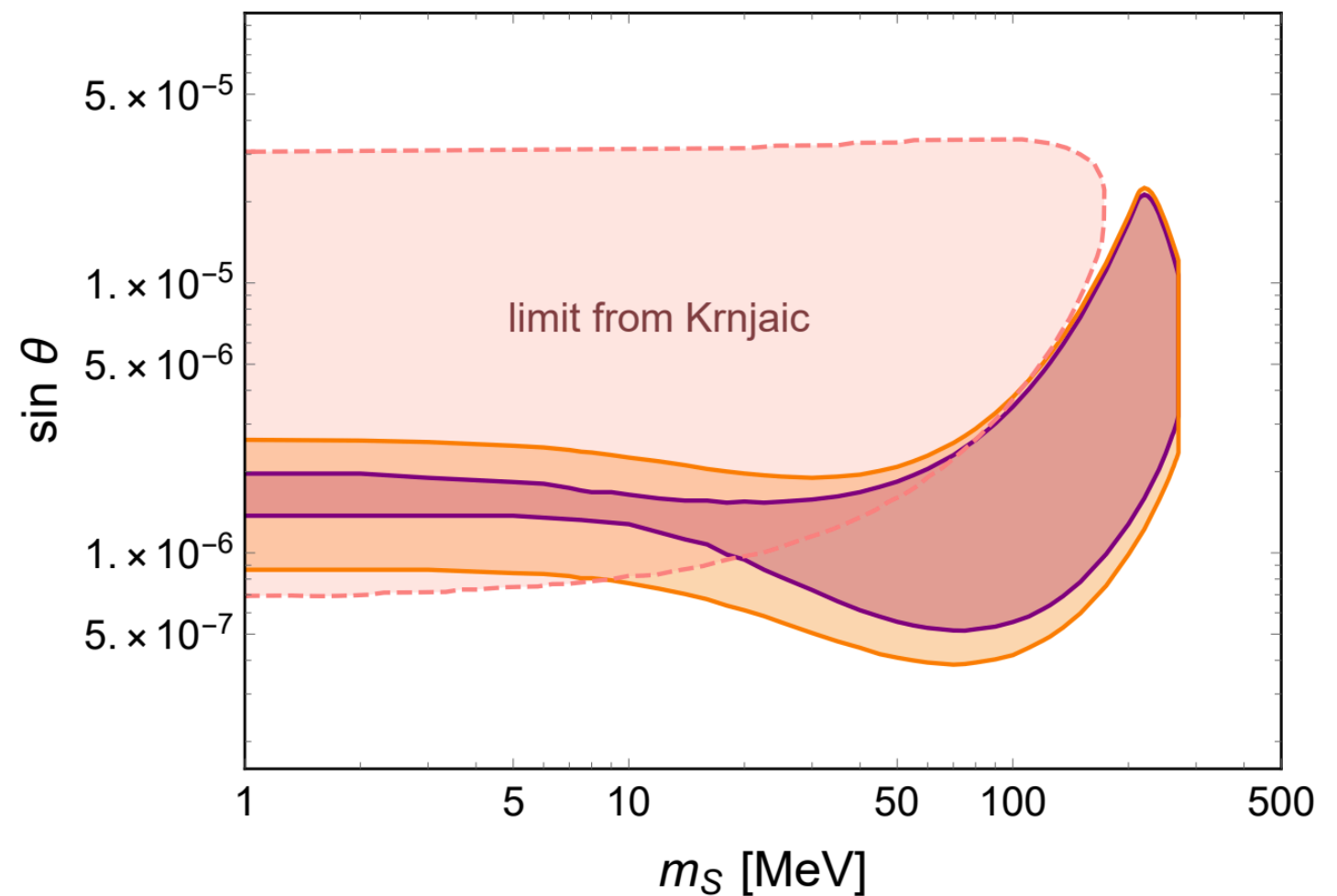
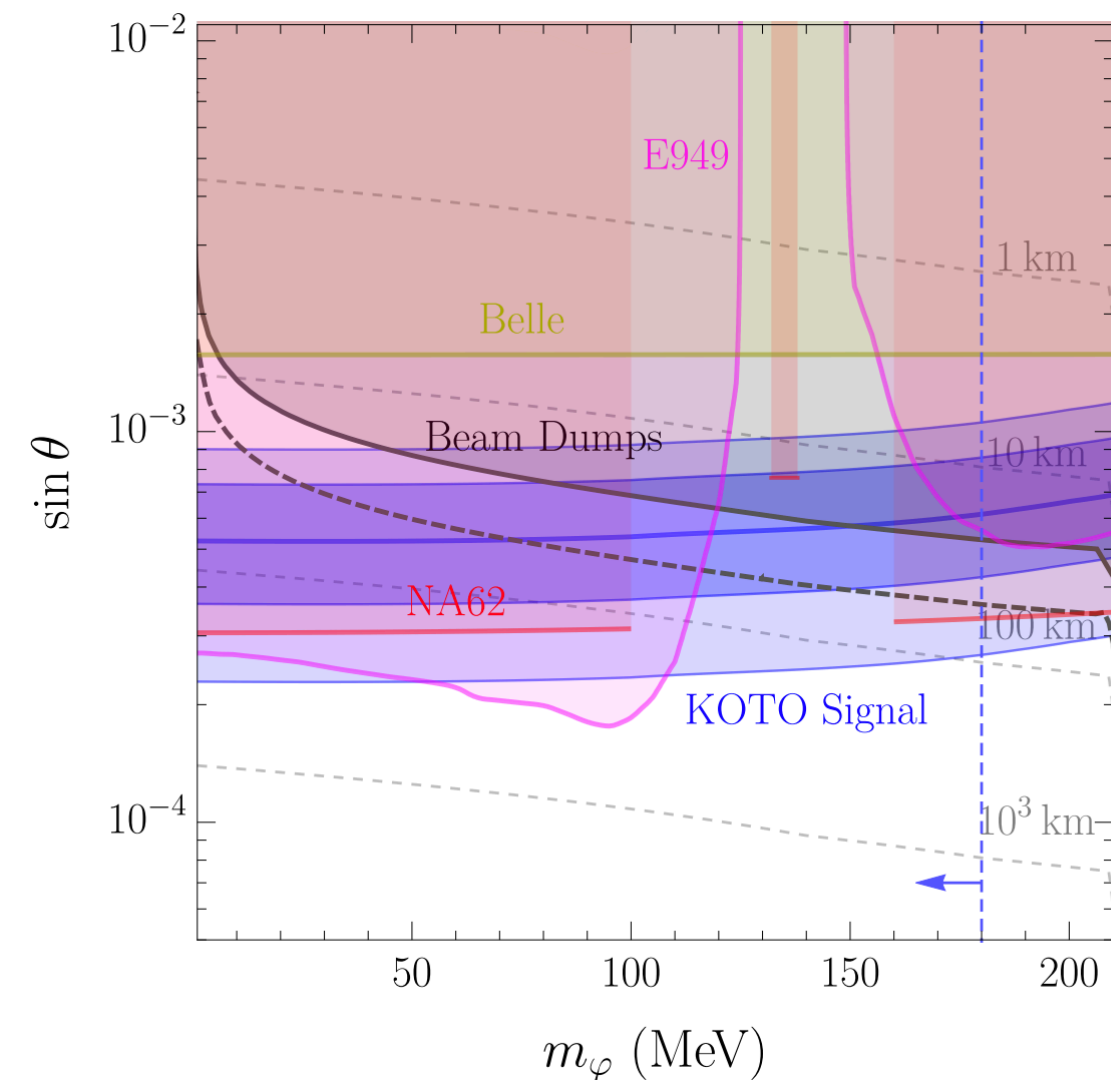
- The rates for the Kaon decay into ϕ and π from 1-loop

$$\Gamma(K_L \rightarrow \pi^0 \phi) = \frac{\left(\mathbf{Re} [g(\sin \theta)] \right)^2}{16\pi m_K^3} \lambda^{1/2}(m_K^2, m_\pi^2, m_\phi^2),$$

$$g(\sin \theta) = \frac{3m_K^2}{32\pi^2 v^3} \sin \theta \sum_{q=u,c,t} m_q^2 V_{qd}^* V_{qs},$$

Long-lived scalar mediator fits to KOTO

- Charged Kaon exp forced mass ~ 140 MeV
- highly constrained by astrophysical bounds?



See Samuel Homiller's talk
D. Egana-Ugrinovic et al, 1911.10203

See Yongchao Zhang's talk
Bhupal Dev et al, 1911.12334
Bhupal Dev et al, [2005.00490](#)

Solution 2: short-lived particle

- A light particle ($m < 200$ MeV) from Kaon decay



- If it is long-lived enough to escape KOTO detector (few meters), it can mimic the missing energy
- The way out: it is short-lived to decay inside the charged Kaon experiment, thus vetoed in measurement of



- KOTO detector scale ~ 3 m, NA62 detector ~ 150 m
- X lifetime has to be 0.1 nano-seconds ~ 3 cm

Our Model building: short-lived scalar mixing with extended Higgs sector

- **Type-X 2HDM:** one SM-like doublet coupling to quarks and one doublet coupling to leptons

$$\mathcal{L}_{\text{yuk}} = -\lambda_u \bar{Q} \tilde{\Phi}_2 u_R - \lambda_d \bar{Q} \Phi_2 d_R - \lambda_e \bar{L} \Phi_1 e_R + h.c.$$

- The light scalar mixing independently with two doublets

$$\mathcal{L}_{\text{eff}} \supset \epsilon_q \sum_q \frac{m_q}{v} \phi \bar{q} q + \epsilon_\ell \sum_\ell \frac{m_\ell}{v} \phi \bar{\ell} \ell + \epsilon_W \frac{2m_W^2}{v} \phi W_\mu^+ W^{\mu-}$$

- The coupling to gauge boson is not independent

$$\epsilon_q \simeq \frac{\sin \theta_{2\phi}}{\sin \beta}, \quad \epsilon_\ell \simeq \frac{\sin \theta_{1\phi}}{\cos \beta}$$

- In the large $\tan\beta$ limit, we obtain a simple relation

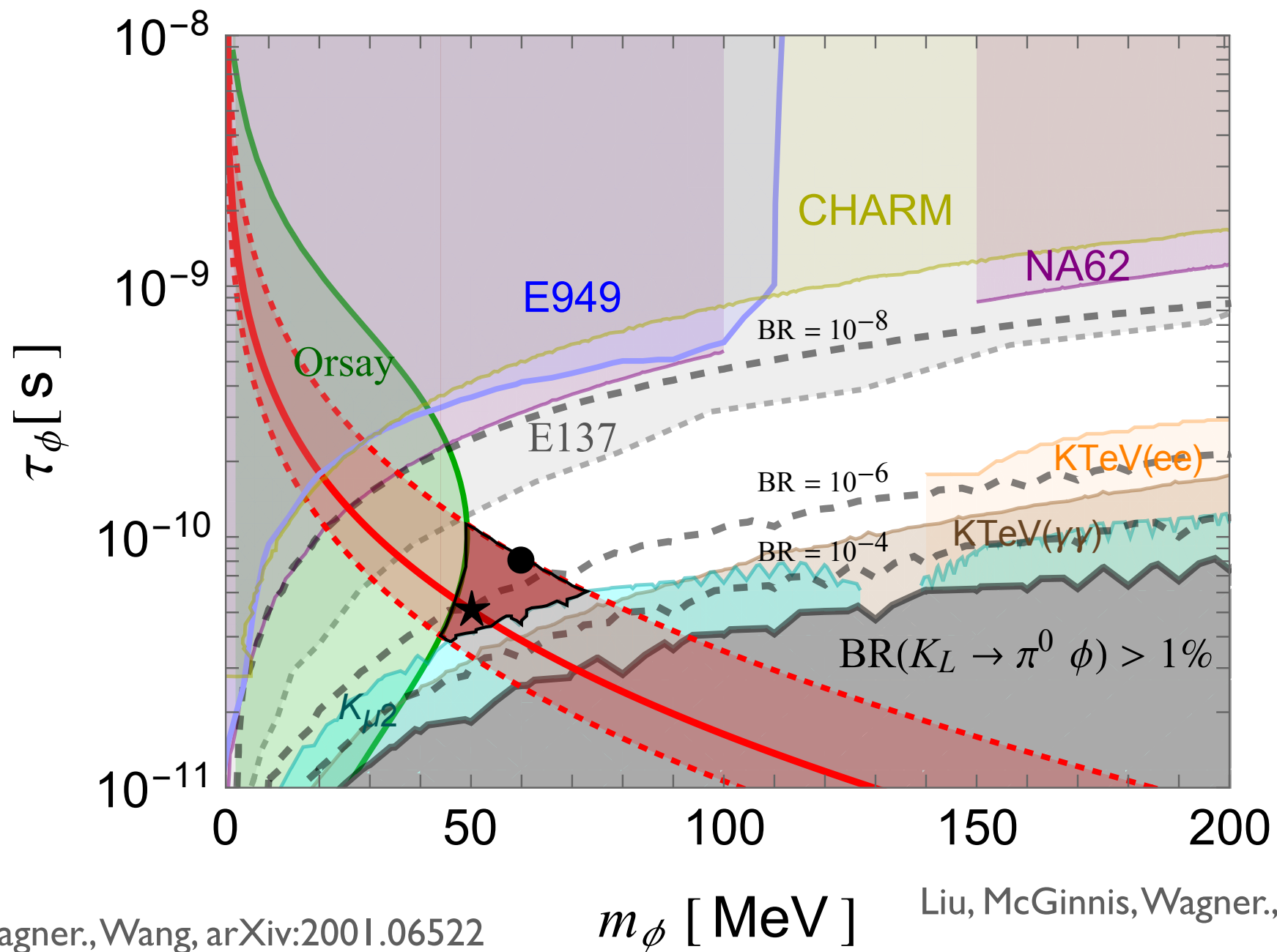
$$\begin{aligned} \epsilon_W &\simeq \left(\sin \theta_{1\phi} \cos \beta + \sin \theta_{2\phi} \sin \beta \right) \\ &\approx \epsilon_\ell \cos^2 \beta + \epsilon_q \sin^2 \beta \approx \epsilon_q, \end{aligned}$$

Fixing the model parameters

$$\mathcal{L}_{\text{eff}} \supset \epsilon_q \sum_q \frac{m_q}{v} \phi \bar{q} q + \epsilon_\ell \sum_\ell \frac{m_\ell}{v} \phi \bar{\ell} \ell + \epsilon_q \frac{2m_W^2}{v} \phi W_\mu^+ W^{\mu-}$$

- Three free parameters ϵ_q ϵ_ℓ m_ϕ
- Two requirements:
 - Muon g-2 fixes $\epsilon_\ell \sim 1$
 - Branching ratio of neutral Kaon decay to ϕ fixes $\epsilon_q \sim 0.01$
- Only mass parameter is free

The results



Liu, McGinnis, Wagner., Wang, arXiv:2001.06522

Liu, McGinnis, Wagner., Wang, arXiv:2001.06522

m_ϕ [MeV]	ϵ_q	ϵ_ℓ	$\text{BR}(K_L \rightarrow \pi^0 \phi)$	τ [s]	$\tan \beta$	$\sin \alpha$	$\sin \theta_{1\phi}$	$\sin \theta_{2\phi}$
50	1.6×10^{-2}	1.22	1.7×10^{-6}	5.1×10^{-11}	100	-0.01	0.0122	1.6×10^{-2}
60	6.8×10^{-3}	0.87	3.2×10^{-7}	8.25×10^{-11}	100	-0.01	0.0087	6.8×10^{-3}

Summary

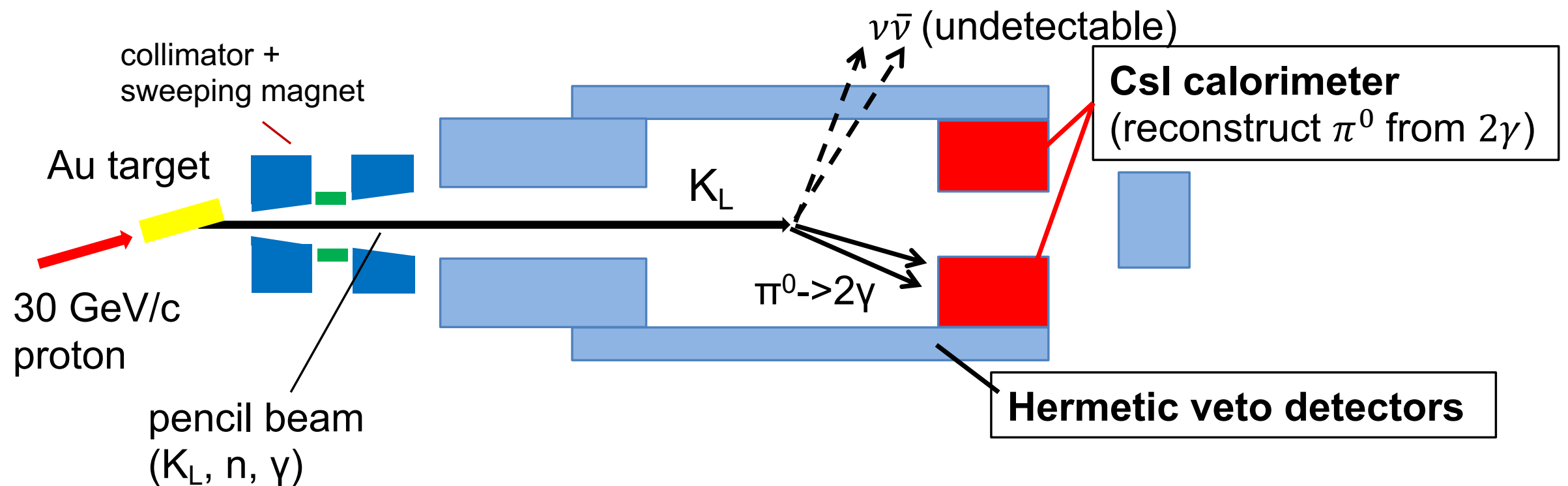
- Recent low energy anomalies might hint new light dark sector particles, but require further cross-checks from independent experiments
- We show the light scalars can be related to lepton $g-2$ and KOTO exp
- The muon $g-2$ could be explained by a scalar of mass of about 50 MeV and couplings to muons of the order of the SM Higgs ones.
- Such a scalar can also lead to an explanation of the KOTO excess, for appropriate values of the quark couplings
- The model can be validated by the vetoed di-electron events in KOTO experiment

Thank you!

Backup slides

KOTO experiment setup

$$K_L \rightarrow \pi^0 \nu \bar{\nu} : (\pi^0 \rightarrow) 2\gamma + \text{nothing}$$

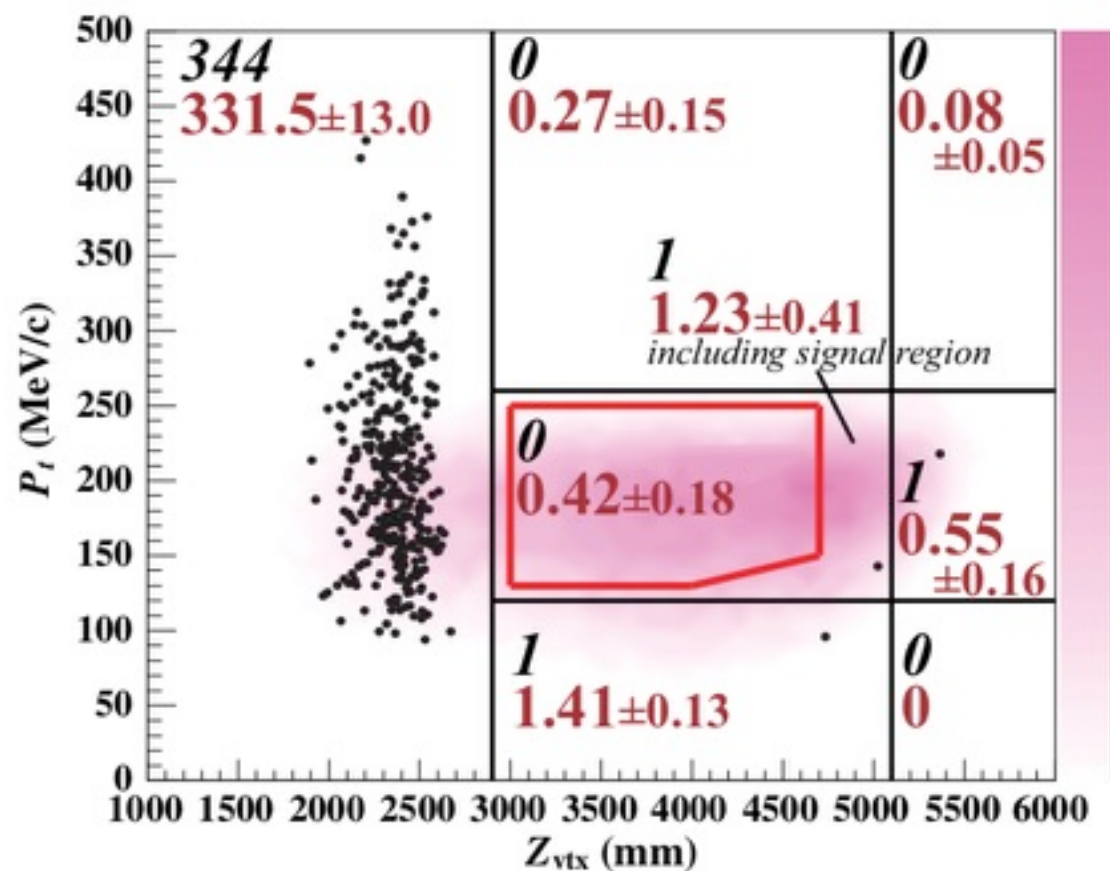


- Neutrinos are not detected
- A new weakly-coupled particle X either stable or decay outside of detector can mimic missing energy

$$K_L \rightarrow \pi^0 X$$

Result of 2015 physics run

Phys. Rev. Lett. 122, 021802



observed

expectation

contour : $K_L \rightarrow \pi^0 \nu \bar{\nu}$ (MC)

PHYSICAL REVIEW LETTERS 122, 021802 (2019)

Search for $K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 X^0$ Decays at the J-PARC KOTO Experiment

J. K. Ahn,¹ B. Beckford,² J. Beecher,² K. Bryant,² M. Campbell,² S. H. Chen,³ J. Comfort,⁴ K. Dona,² N. Hara,⁵ H. Haraguchi,⁵ Y. B. Hsiung,³ M. Hutcheson,² T. Inagaki,⁶ I. Kamiji,⁷ N. Kawasaki,⁷ E. J. Kim,⁸ J. L. Kim,^{1†} Y. J. Kim,⁹ J. W. Ko,⁹ T. K. Komatsubara,^{6,10} K. Kotera,⁵ A. S. Kurilin,^{11*} J. W. Lee,^{5,‡} G. Y. Lim,^{6,10} C. Lin,³ Q. Lin,¹² Y. Luo,¹² J. Ma,¹² Y. Maeda,^{7,‡} T. Mari,⁵ T. Masuda,^{7,‡} T. Matsumura,¹³ D. McFarland,⁴ N. McNeal,² J. Micallef,² K. Miyazaki,⁵ R. Murayama,^{5,‡} D. Naito,^{7,‡} K. Nakagiri,⁷ H. Nanjo,^{7,‡} H. Nishimiya,⁵ T. Nomura,^{6,10} M. Ohsugi,⁵ H. Okuno,⁶ M. Sasaki,¹⁴ N. Sasao,¹⁵ K. Sato,^{5,††} T. Sato,⁶ Y. Sato,⁵ H. Schamis,² S. Seki,⁷ N. Shimizu,⁵ T. Shimogawa,^{16,‡} T. Shinkawa,¹³ S. Shinohara,⁷ K. Shiomi,^{6,10} S. Su,² Y. Sugiyama,^{5,‡} S. Suzuki,¹⁶ Y. Tajima,¹⁴ M. Taylor,² M. Tecchio,² M. Togawa,^{5,‡} Y. C. Tung,¹² Y. W. Wah,¹² H. Watanabe,^{6,10} J. K. Woo,⁹ T. Yamanaka,⁵ and H. Y. Yoshida¹⁴

(KOTO Collaboration)

- Single event sensitivity : $(1.30 \pm 0.01_{stat} \pm 0.14_{syst}) \times 10^{-9}$
- No event in the signal region

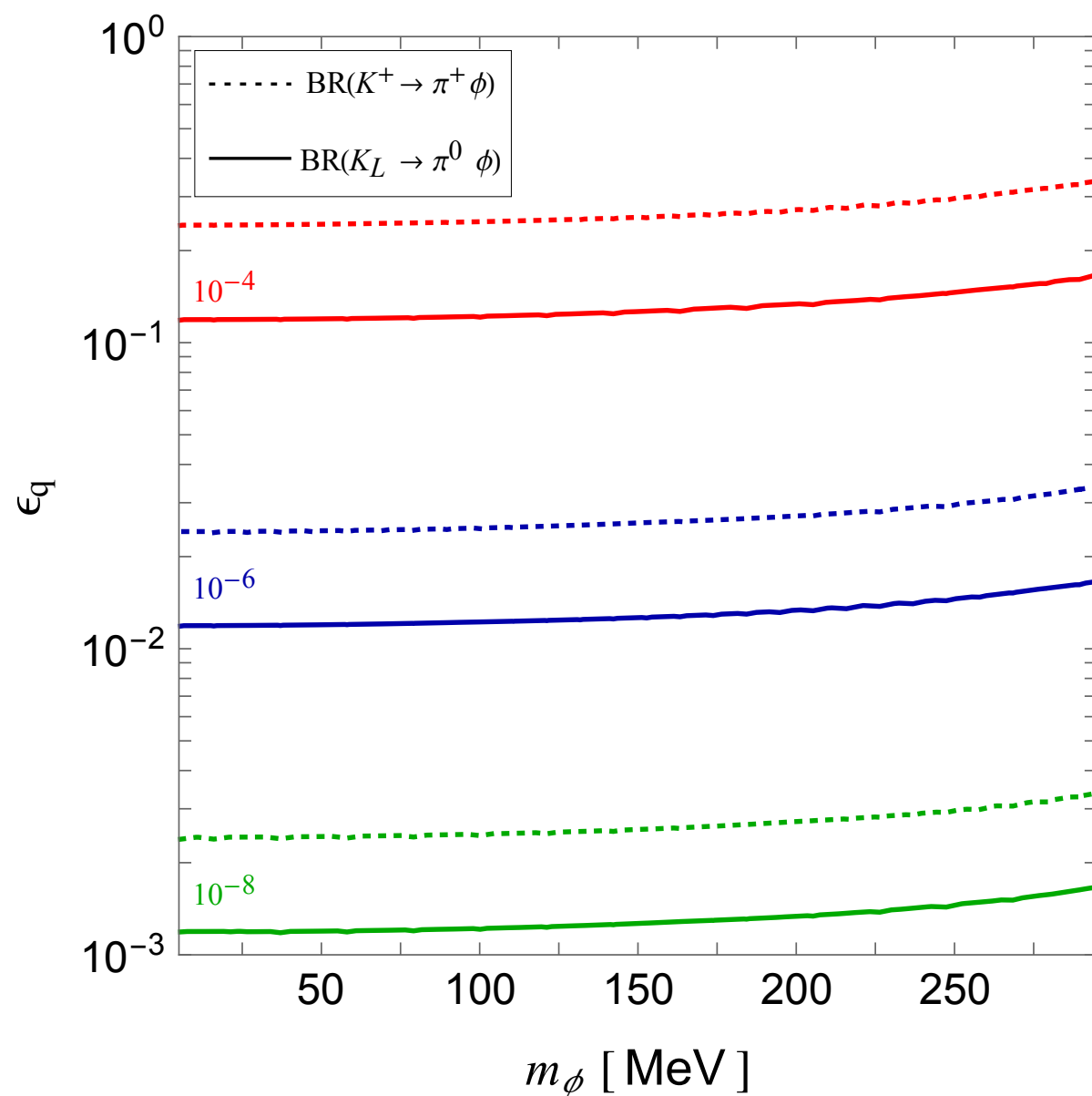
➔ Upper limit (90% C.L.) : $\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$

× 10 improvement from previous limit (KEK E391a)

The Kaon decay branching ratio

- The effective BR fitted to KOTO experiment

$$\text{BR}(K_L \rightarrow \pi^0 \phi; \text{KOTO}) = \epsilon_{\text{eff}} \text{BR}(K_L \rightarrow \pi^0 \phi) e^{-\frac{L}{p\phi} \frac{m\phi}{\tau\phi}}$$



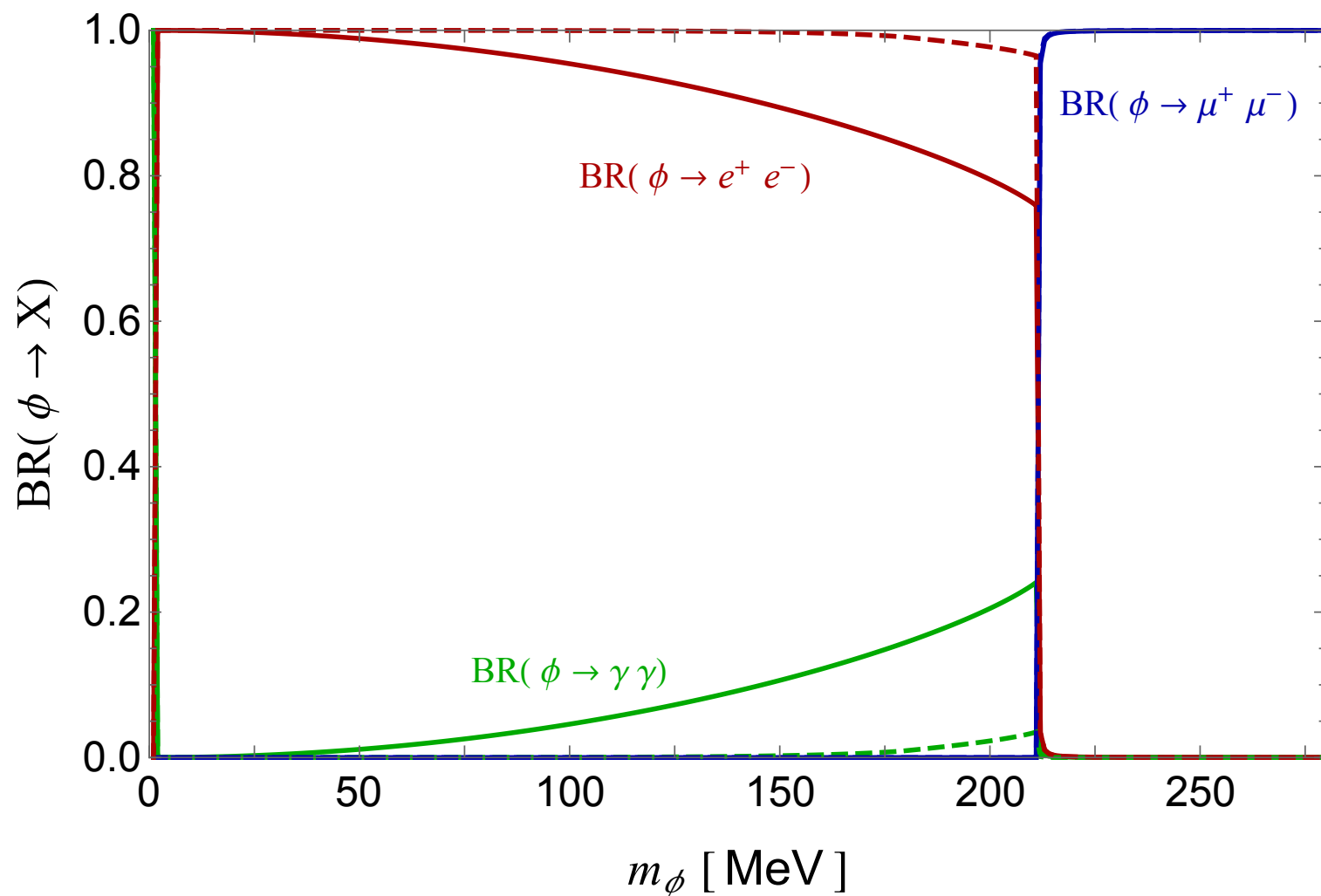
- The true BR for neutral Kaon and charged Kaon decay
- $\text{BR}(\text{KOTO}) \sim 2 \times 10^{-9}$ according to 3 obs events, relying on both quark coupling and lifetime
- Check charged Kaon BR to avoid constraints

The lifetime of ϕ

- The decay width for a light ϕ

$$\Gamma(\phi \rightarrow \ell\ell) = \frac{\epsilon_\ell^2 m_\ell^2}{8\pi v^2} m_\phi (1 - \tau_\ell)^{3/2} \theta(m_\phi^2 - 4m_\ell^2)$$

$$\Gamma(\phi \rightarrow \gamma\gamma) = \frac{\alpha^2 m_\phi^3}{1024\pi^3} \left| \sum_q \frac{6\epsilon_q}{v} Q_q^2 A_{1/2}(\tau_q) + \sum_\ell \frac{2\epsilon_\ell}{v} A_{1/2}(\tau_\ell) + \frac{2\epsilon_W}{v} A_1(\tau_W) \right|^2$$



- Our model: $\epsilon_l \sim 1 \gg \epsilon_q \sim 0.01$
- Dashed line for simple mixing model (with accidental cancellation in $\gamma\gamma$)
- solid line for our model.
- In region of interest, the lifetime depends dominantly on ϵ_l and the decay into ee .

$$\text{BR}(\phi \rightarrow e^+e^-) \approx 100\%$$

Experimental constraints

- Proton beam dump
 - E949 and NA62: looking for $K^+ \rightarrow \pi^+ \bar{\nu} \nu$
 - CHARM: looking for displaced decay (480 m) from $K \rightarrow \pi + (ee/\gamma\gamma/\mu\mu)$
 - K μ 2: using stopped charged Kaon looking for $K^+ \rightarrow \pi^+ \phi$
 - KTeV/E799: looking for ee but requires $m_{ee} > 140$ MeV $K^0 \rightarrow \pi^0 e^+ e^-$
- Electron beam dump
 - Orsay: looking for the radiation of light particles decaying into electron pairs $eN \rightarrow eN\phi, \phi \rightarrow e^+ e^-$
 - Similar experiment E137, although analysis was done for a dark photon, mixing with the photon and have to be reinterpreted in the scalar framework.
- B physics and collider constraints: like $B \rightarrow K\phi, \phi \rightarrow e^+ e^-$ avoided due to relative long lifetime

Comments

- Main difference between short-lived scalar (cm) and long-lived scalar (100 km)

- B physics measurement at LHCb

$$\text{BR}(B^0 \rightarrow K^{*0}e^+e^-) = 3.1_{-0.88}^{+0.94} \times 10^{-7}, \quad \text{BR}(B^0 \rightarrow K^{*0}e^+e^-)^{\text{th}} = (2.3 \pm 0.6) \times 10^{-7}$$

- Our benchmark model

$$\text{BR}(B \rightarrow K^*\phi) \simeq 10^{-4}, \quad \text{BR}(\phi \rightarrow e^+e^-) \approx 100\%$$

- However, LHCb requires a good quality vertex: ee pair vertex coincide with K^* vertex, within vertex resolution $L \sim 5$ mm

- $\phi \rightarrow ee$ lifetime ~ 1.5 cm, safe from LHCb constraints.

- KOTO can reexamine the vetoed events

$$K_L \rightarrow \pi^0\phi, \phi \rightarrow e^+e^-$$