



Minimal model of torsion mediated dark matter

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- We propose a minimal model of **Torsion mediated** dark matter annihilations
- Torsion: Antisymmetric part of the Affine connection in the Einstein-Cartan extension of **General Relativity**
- **Observations in DM phenomenology**
 - Particle content: A SM singlet Dirac fermion ψ , SM and Torsion : **DM DM–Torsion–SM SM**
 - The DM is naturally stable without any imposition of ad-hoc symmetry like e.g., \mathbb{Z}_2
 - Torsion in phenomenology \Rightarrow like a massive gauge boson (like Z') having only axial coupling
 - The stringent bounds on the SI DM-nucleon direct detection cross-section relaxed due to its axial nature of the torsion.
 - Mixings with SM Gauge bosons can be considered to be absent

Spacetime Torsion : useful properties

- The covariant derivative of a vector field A^ν is a tensor $\Rightarrow \nabla_\mu A^\nu = \partial_\mu A^\nu + \Gamma_{\mu\lambda}^\nu A_\lambda$ ($\Gamma_{\mu\lambda}^\nu \Rightarrow$ Affine connection)
- Affine connection \Rightarrow Christoffel Connection in Einstein **GR**
$$\Gamma_{\mu\nu}^\lambda = \frac{1}{2} g^{\lambda\alpha} (\partial_\mu g_{\nu\alpha} + \partial_\nu g_{\mu\alpha} - \partial_\alpha g_{\mu\nu})$$
- In the Einstein-Cartan extension of **GR**, the affine connection can have an **anti-symmetric part** $\tilde{\Gamma}_{\mu\nu}^\lambda = \Gamma_{\mu\nu}^\lambda + C_{\mu\nu}^\lambda$
Useful parametrization ([arXiv:hep-th/0103093](https://arxiv.org/abs/hep-th/0103093)):

$$T_{\mu\nu}^\lambda = \tilde{\Gamma}_{\mu\nu}^\lambda - \tilde{\Gamma}_{\nu\mu}^\lambda,$$
$$T_{\mu\nu\lambda} = \frac{1}{3} (T_\nu g_{\mu\lambda} - T_\lambda g_{\mu\nu}) - \frac{1}{6} \varepsilon_{\mu\nu\lambda\sigma} S^\sigma + q_{\mu\nu\lambda},$$

Definitions of the irreducible components:

- $S^\lambda = \varepsilon^{\mu\nu\alpha\lambda} T_{\mu\nu\alpha}$ is axial vector mode
- $q_{\mu\nu\alpha} \Rightarrow$ tensor satisfies $q_{\nu\mu}^\mu = 0$ and $\varepsilon^{\mu\nu\alpha\sigma} q_{\mu\nu\alpha} = 0$.
- $T_\mu = T_{\mu\alpha}^\alpha \Rightarrow$ the vector (trace) mode

Torsion interactions with DM and SM fermions

- For simplicity we consider Torsion characterized by S_μ only
- Relevant and New parts in Action:
 - S_μ -SM interactions:

$$\mathcal{S}_D = \int d^4x \left\{ i\bar{f}\gamma^\mu (\partial_\mu - i\eta_1 \gamma^5 S_\mu) f \right\},$$

- S_μ -DM interactions:

$$\mathcal{S}_{DM} = \int d^4x \left\{ i\bar{\psi}\gamma^\mu (\partial_\mu - i\eta \gamma^5 S_\mu) \psi - m_\psi \bar{\psi} \psi \right\}.$$

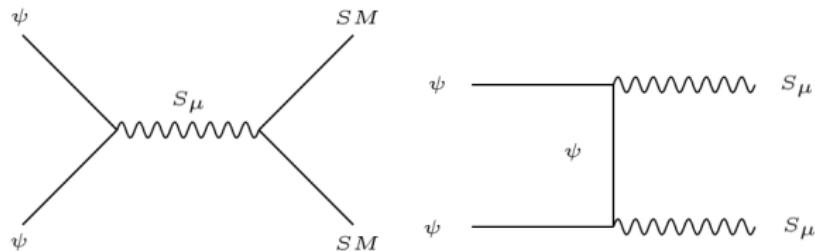
- Kinetic terms:

$$\mathcal{S}_{torsion} = \int d^4x \left\{ -\frac{1}{4} S_{\mu\nu} S^{\mu\nu} + \frac{1}{2} m_s^2 S_\mu S^\mu \right\}$$

$S_{\mu\nu} = \partial_\mu S_\nu - \partial_\nu S_\mu$ and m_s is the torsion mass

Torsion(s_μ)-DM(ψ) phenomenology

Dominant channels (**Universal coupling** : $\eta_1 = \eta$)



$$\langle\sigma v\rangle_{\bar{f}f} \sim \eta^4 \frac{m_f^2}{m_s^4} \left(\frac{\left(m_s^2 - 4m_\psi^2\right)^2}{\left(m_s^2 - 4m_\psi^2\right)^2 + \Gamma_s^2 m_s^2} \right) + v^2 \frac{\eta^4 m_\psi^2}{\left(4m_\psi^2 - m_s^2\right)^2} \times ..$$

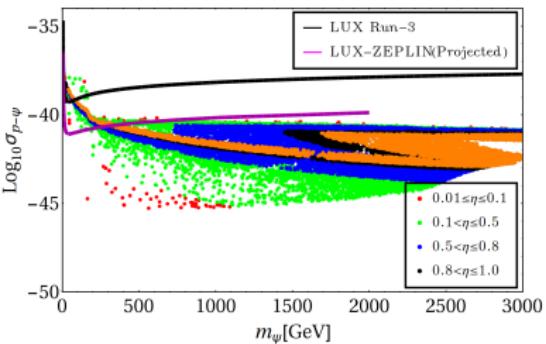
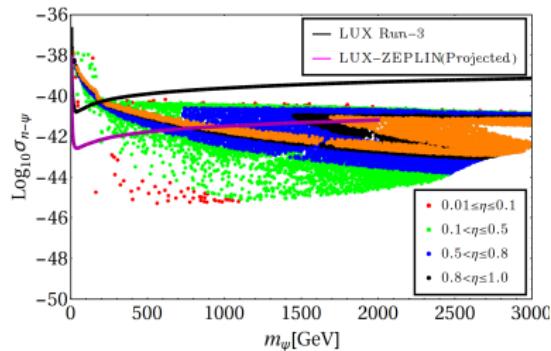
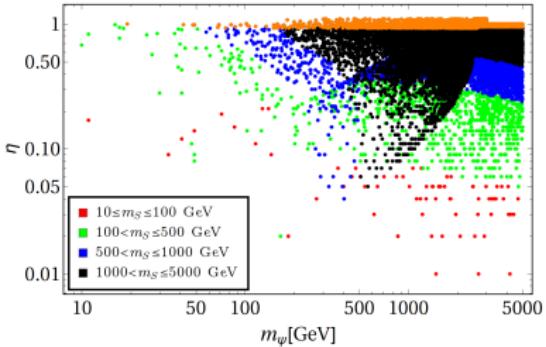
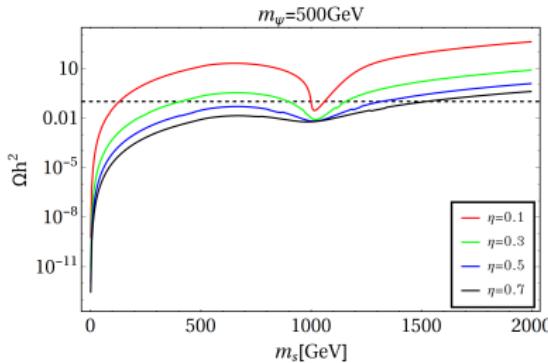
$$\langle\sigma v\rangle_{ss} \sim \frac{\eta^4}{m_\psi^2} \left(1 - \frac{m_s^2}{m_\psi^2}\right)^{3/2} \left(1 - \frac{m_s^2}{2m_\psi^2}\right)^{-2} + \mathcal{O}(v^2)$$

Contributions to relic abundance:

- A resonance at $m_\psi \simeq \frac{m_s}{2}$ can be observed
- For moderate or small m_s , (when Γ_s can be ignored), the **leading order term** in the s-channel process may not be sensitive to **Breit-Wigner type narrow width resonance**
- The **dominant** v^2 contribution carries the **resonance effect**, specially important in relic density calculation when the DM is lighter than top quark
- $DM\ DM \rightarrow t\bar{t} \sim \frac{m_f^2}{m_s^4}$ for $m_s \sim m_\psi$ can produce significant contributions
- Similarly t -channel contributions, free from v^2 suppression, are also important for $m_s \lesssim m_\psi$

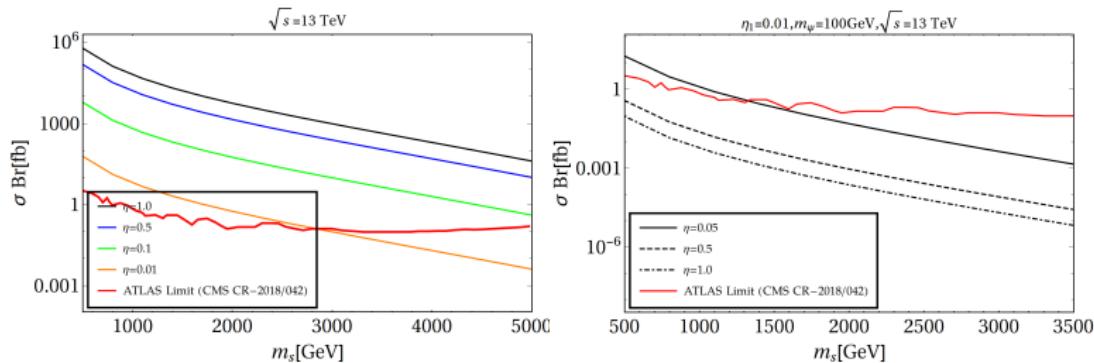
Results: relic density and SD cross-section

Universal Coupling scenario ($\eta = \eta_1$):



LHC constraints and Nonuniversal coupling scenario

- $\sigma(pp \rightarrow S_\mu) \times Br(S_\mu \rightarrow I^+I^-)$ ($I \in e, \mu$) vs. m_s in the universal and nonuniversal coupling (NU) scenario



- $\eta \simeq 1$ may lead to $\Gamma_s/m_s \geq 0.5$ narrow width approximation breaks down \Rightarrow LHC constraints relaxed
- NU scenario \Rightarrow DM phenomenology mostly unchanged

Torsion Portal- GR connection successfully explain DM phenomena

THANK YOU