



Bundesministerium
für Bildung
und Forschung



Universität Hamburg

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LHC optics measurements and corrections

A local observable for linear imperfections in circular accelerators

Andreas Wegscheider

Introduction

- Gentner Doctoral Student since Aug. 2017
- **PhD topic:** *Development of measurement methods for circular accelerators*
- **finished projects**
 - analytical N-BPM method (more precise and faster calculation of β function)
 - local observable
- **open project**
 - forced coupling

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 - forced coupling

Overview of LHC Optics Measurement and Correction

- why is optics correction important?
- how do we perform optics measurements?
- how do we correct imperfections?

Local Observable

- why do we need a local observable?
- how is it constructed?
- which information do we get?

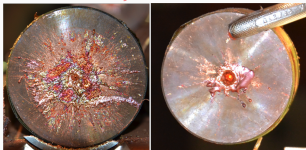
LHC Optics Measurement and Correction

LHC Optics Measurement and Correction

LHC Optics Commissioning

Importance of Optics Commissioning

- **Machine protection**



Beam hitting solid copper target ^a

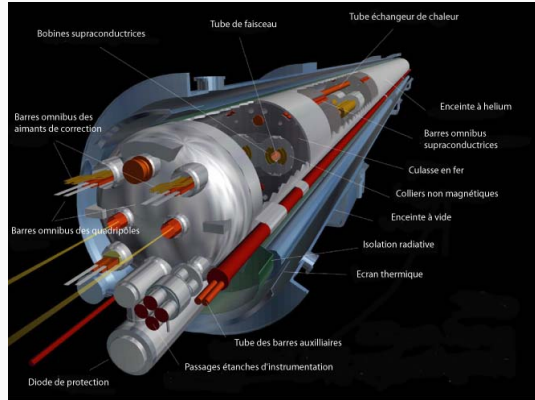
^aPhD thesis of F. Burkhart, former Gentner student

- **Machine performance**

- Optics errors can reduce delivered luminosity
- Optics errors can create luminosity imbalance between experiments critical for ATLAS and CMS
aim for 1% level control of β^*
- High quality optics improves operational control

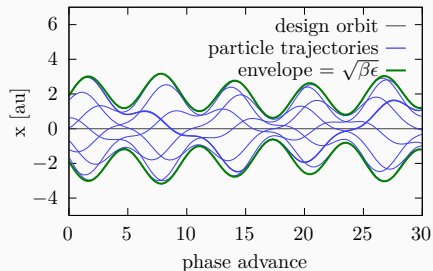
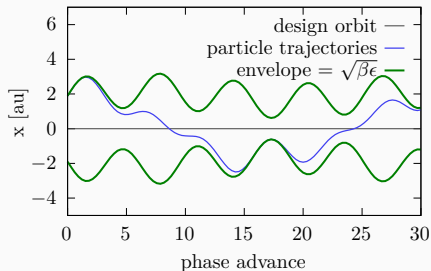
Importance of Optics Commissioning

- the LHC is a **superconducting** collider
- during one run of operation of the accelerator complex, access to the magnets for measurement is not possible
- to measure and correct lattice imperfections we need to use **beam based** measurements



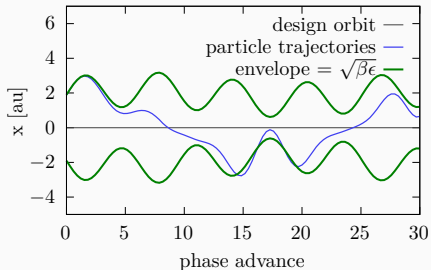
Betatron Oscillation

- particles in bunch perform betatron oscillation about the bunch center
- bunch center moves on closed orbit



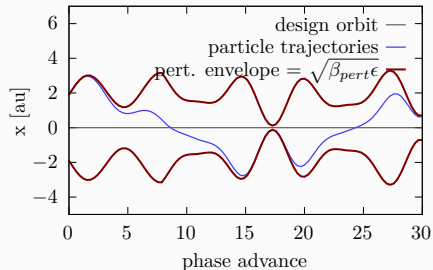
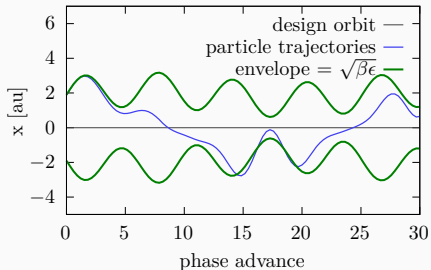
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- focusing errors change β function



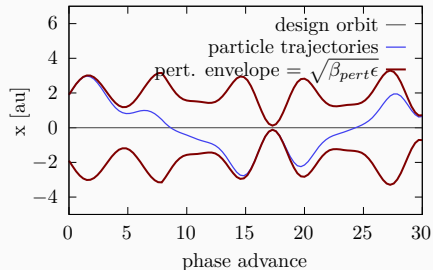
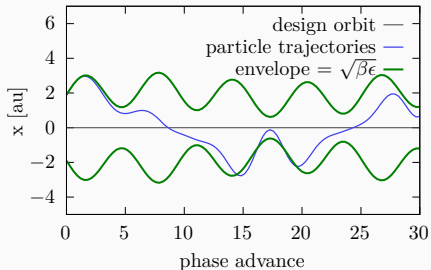
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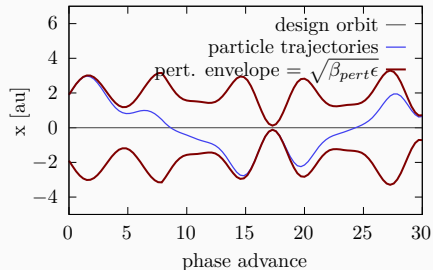
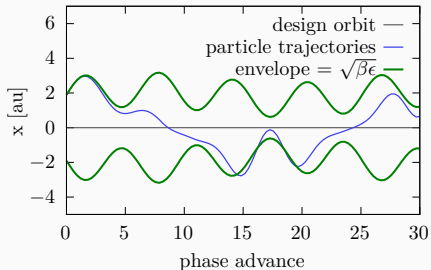
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- excitation: beam center performs betatron oscillation (if free kick)

Betatron Oscillation

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- excitation: beam center performs betatron oscillation (if free kick)
- need sufficiently strong amplitude to get good signal

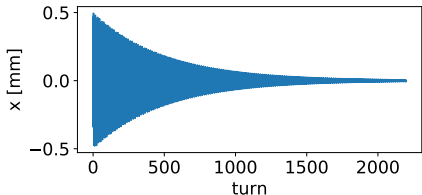
LHC Optics Measurement and Correction

Devices and Tools

Optics measurements via AC-Dipole

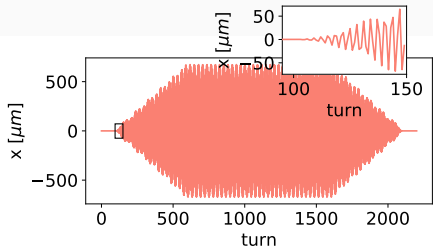
Free kick

- triggers free oscillation of beam
- amplitude of signal decreases fast
- easy to blow up emittance



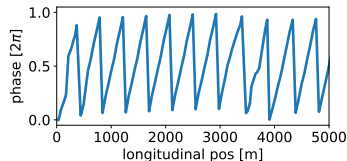
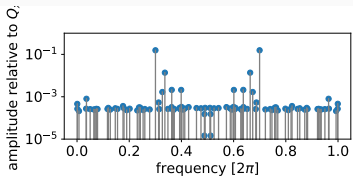
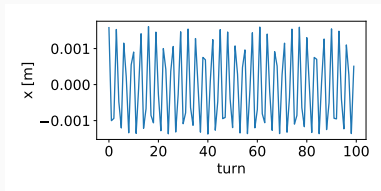
AC-Dipole

- No decoherence
- many turns for analysis
- No blow up due to adiabatic ramp-up/down
- driven oscillation \Rightarrow compensation



BPMs

- More than 500 dual plane **beam position monitors** (BPMs) record turn-by-turn betatron oscillation data during kicks
- Spectral analysis to obtain **phase advances** between BPMs
- Reconstruct β functions via N-BPM method



LHC Optics Measurement and Correction

Measurement and Correction steps

Measurement of Beta Function

Beta from phase

The β function can be calculated from the measured phase advances via:

$$\beta_i = \frac{\cot\varphi_{ij} - \cot\varphi_{ik}}{\cot\varphi_{ij}^{\text{mod}} - \cot\varphi_{ik}^{\text{mod}}} \beta_i^{\text{mod}} \quad (1)$$

Improvements in β calculation

- Traditionally neighbouring BPMs
- improvement through averaging over several combinations, using error propagation to get correlations
- further improvement using analytical formula for error propagation

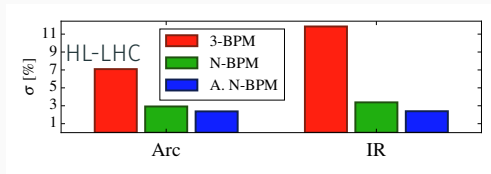
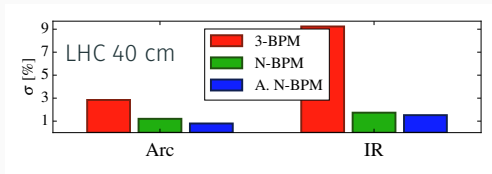
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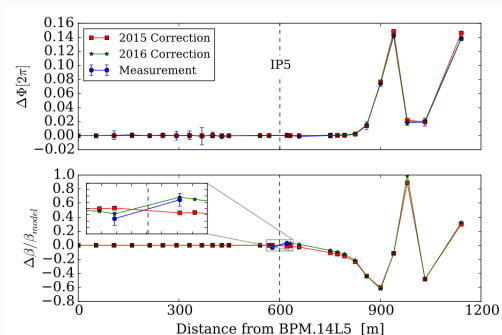
Improvements in β calculation



Local Corrections

First: apply corrections of large local errors

using phase beating = $\varphi_{\text{meas}} - \varphi_{\text{model}}$



Phase beating corrected by 2015 and 2016 optics, but only 2016 also reproduces β beating.

Segment-by-segment technique

- Treat segment of ring as transfer line, propagate measured optics from entrance, then compare modelled phase propagation to measurement
- Use models to reproduce phase deviation and apply to real LHC

Global Corrections

Response matrix approach is used to calculate global corrections

$$(\Delta\varphi_x, \Delta\varphi_y, \beta_x^*, \beta_y^*, \Delta\beta_x, \Delta\beta_y, \Delta ND_x, \Delta ND_y, \Delta Q_x, \Delta Q_y)^T = \mathbf{R} \cdot \Delta\vec{k}$$

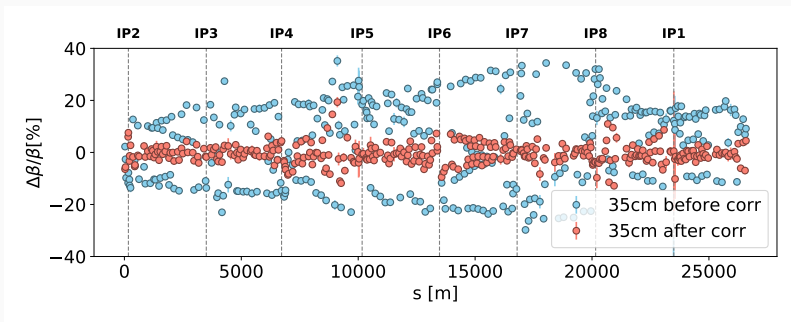


Figure 1: ATS optics MD. $\beta^* = 35$ cm

Beyond the scope of this presentation:

- transverse linear coupling
- machine learning to preselect BPMs
- **Non-linear optics**

Local Observable

Local Observable

Theory

Phase beating due to focusing errors

Quadrupolar field errors alter the phase advance between elements i and j :

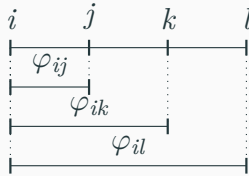


Figure 2: phase advances

Phase beating due to focusing errors

Quadrupolar field errors alter the phase advance between elements i and j :

$$\Delta\varphi_{ij} = \bar{h}_{ij} - 8 \sin^2 \varphi_{ij}^m \mathcal{R}\{f_i\} - 8 \sin \varphi_{ij}^m \cos \varphi_{ij}^m \mathcal{I}\{f_i\} + O(f^2) \quad (2)$$

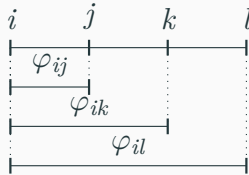


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- red: global terms
- blue: local terms

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Eliminate global terms by reshuffling:

$$\begin{aligned} \cot\varphi_{jl}^m \Delta\varphi_{jl} - \cot\varphi_{jk}^m \Delta\varphi_{jk} \\ + \cot\varphi_{ik}^m \Delta\varphi_{ik} - \cot\varphi_{il}^m \Delta\varphi_{il} \end{aligned} = \begin{aligned} \cot\varphi_{jl}^m (\bar{h}_{il} - \bar{h}_{ij}) \cot\varphi_{jk}^m (\bar{h}_{ij} - \bar{h}_{ik}) \\ + \cot\varphi_{ik}^m \bar{h}_{ik} - \cot\varphi_{il}^m \bar{h}_{il} \end{aligned}$$

Local Observable from phase beating

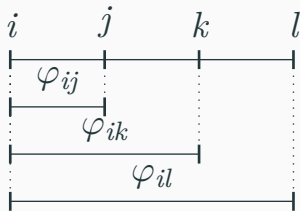


Figure 2: BPM combinations

$$\begin{aligned}
 \cot\varphi_{jl}^m \Delta\varphi_{jl} - \cot\varphi_{jk}^m \Delta\varphi_{jk} &\equiv \cot\varphi_{jl}^m (\bar{h}_{il} - \bar{h}_{ij}) \cot\varphi_{jk}^m (\bar{h}_{ij} - \bar{h}_{ik}) \\
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Local Observable from phase beating

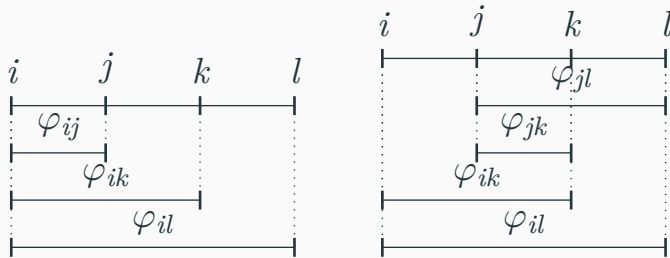


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Local Observable

Simulations

Element
MQ.22R4

$\sigma_{K_1}/K [10^{-4}]$
0.1

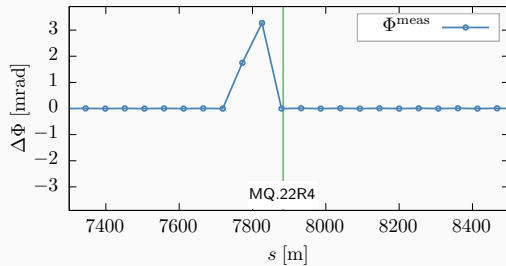


Figure 3: local observable

Locality

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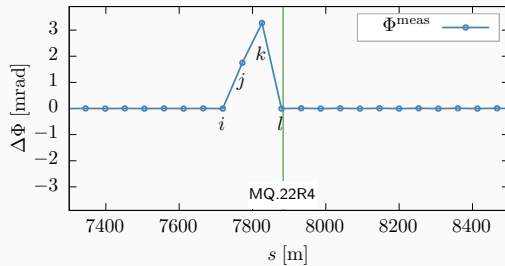
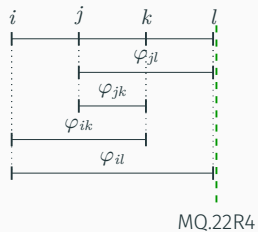


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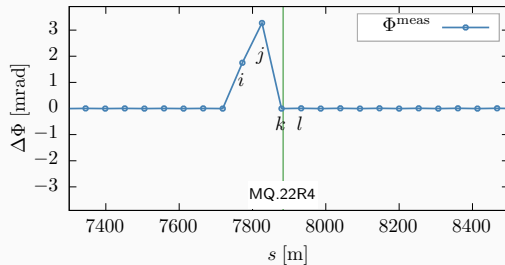
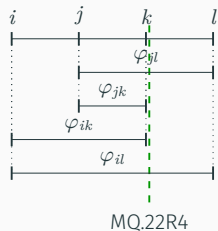


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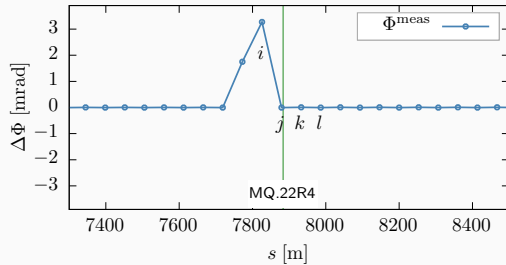
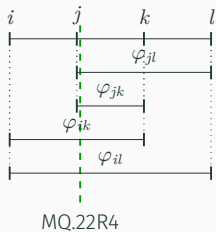


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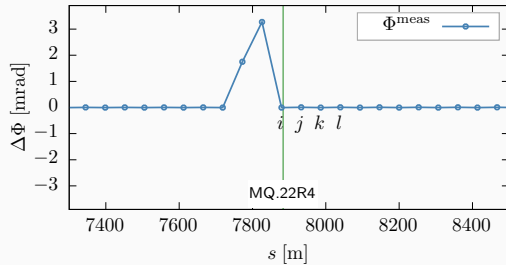
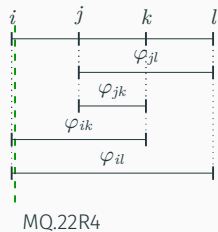
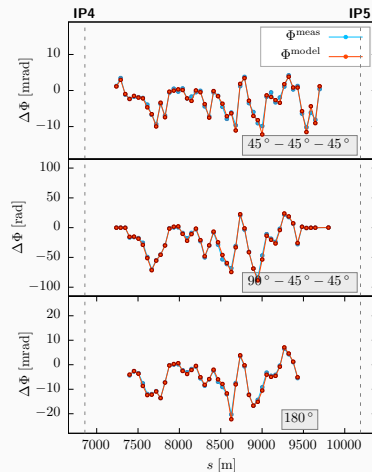


Figure 3: local observable

Design error distribution

Element	$\sigma_{K_1}/K [10^{-4}]$
MQ	12
MQT	75
MQM	12
MQY	11
MQW	15
MQX	1
MB	40

Table 1: Error distribution at 6.5 TeV

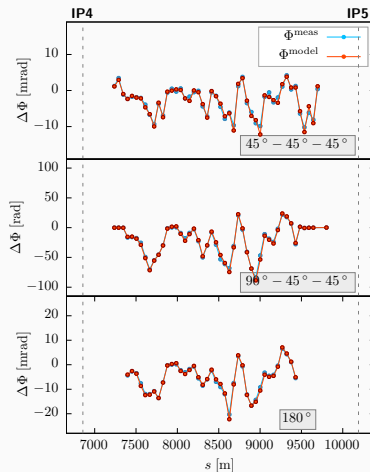


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good agreement between model and simulation

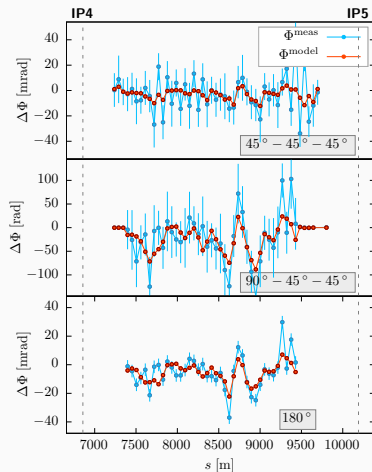


Design error distribution with noise

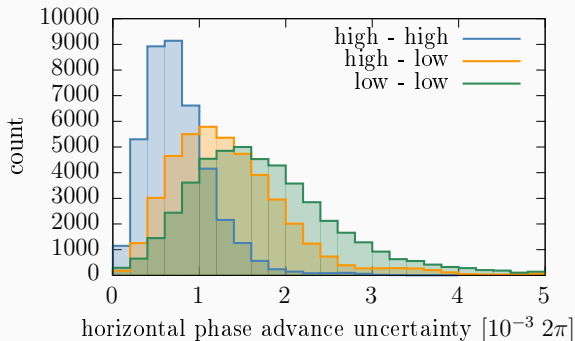
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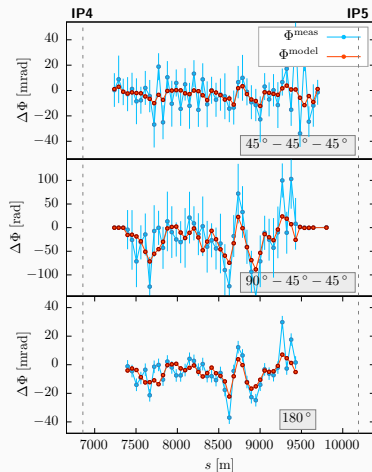
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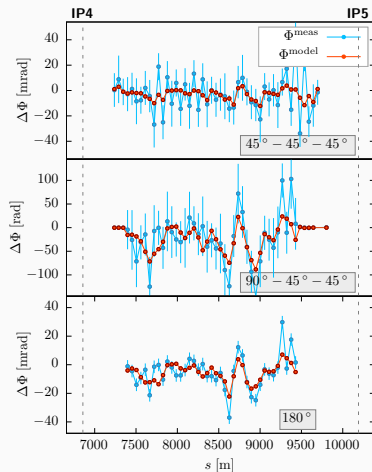
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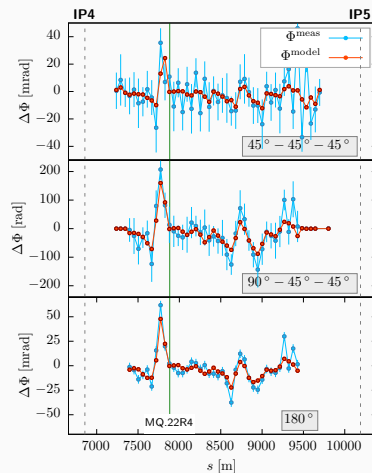


strong error source

Element	$\sigma_{K_1}/K [10^{-4}]$
MQ	12
MQ.22R4	100
MQT	75
MQM	12
MQY	11
MQW	15
MQX	1
MB	40

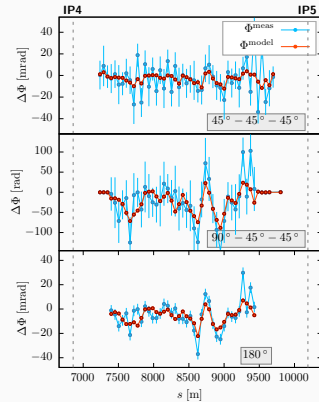
Table 2: introduced strong error in MQ.22R4

error peak clearly visible



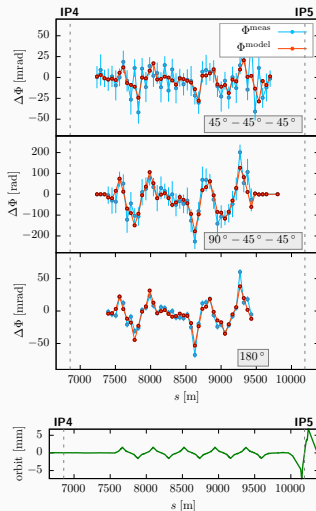
orbit offsets

- orbit offset feeds down to quadrupolar errors in sextupoles



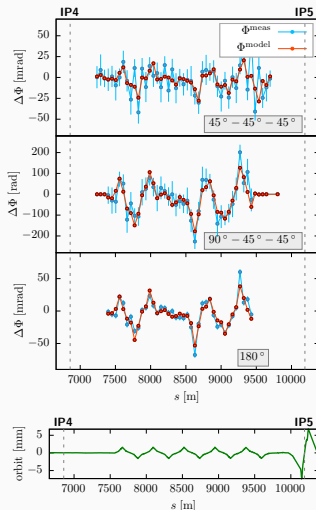
orbit offsets

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- add orbit offsets



orbit offsets

- orbit offset feeds down to quadrupolar errors in sextupoles
- add orbit offsets
- red line: model values with dispersion bumps and no errors
- blue line: measured (simulated) values with disp. bumps and errors



Local Observable

Measurements

measurements

- simulations with dispersion bumps on
- red line: model values with dispersion bumps and no errors
- blue line: measured (simulated) values with disp. bumps and errors

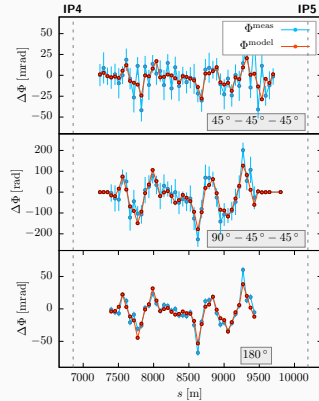


Figure 4: simulation

measurements

- measurement data from 02.04.2018
- LHC beam commissioning, $\beta^* = 30$ cm
- dispersion bumps were on
- **red line: model values with dispersion bumps and no errors**
- **blue line: actual measurement**

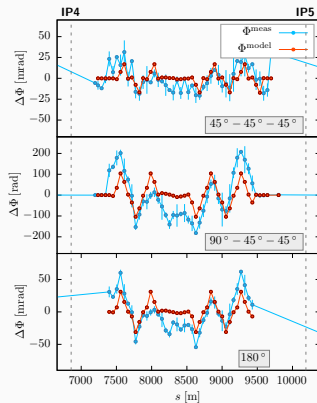


Figure 4: measurement

Local Observable

Conclusion

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- strong error sources ($\gtrsim 1\%$) are clearly visible

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- strong error sources ($\gtrsim 1\%$) are clearly visible
- presence of dispersion bumps can be seen and reproduced in simulations