

## Comparison of the Hadronic Structures in Structure Function Measurements of the Proton, Photon and Diffractive Exchange

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# Analysis Idea

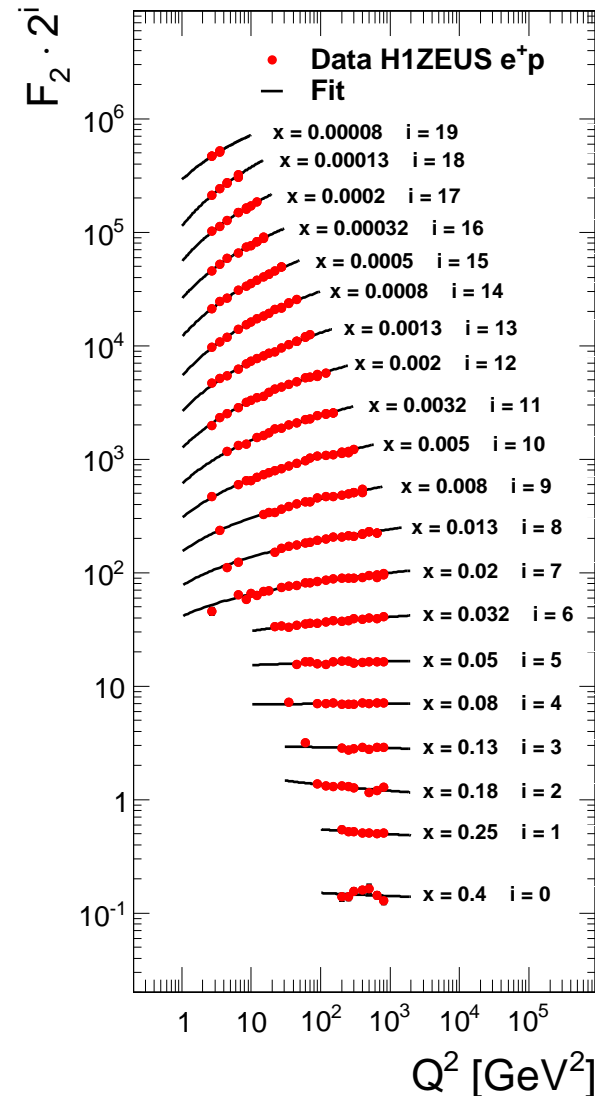
- Find an intuitive description of structure functions
- Fit structure function distribution using function:

$$F_2(x, Q^2) = a(x) \left[ \ln \left( \frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$

with  $\Lambda = 0.35 \text{ GeV}$

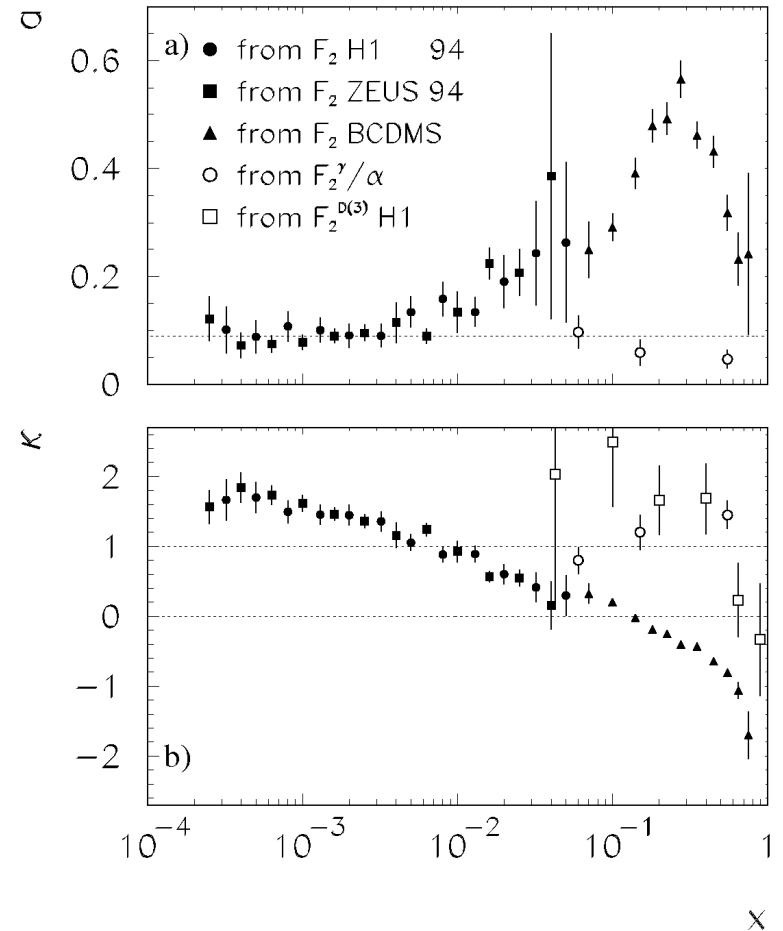
- $a(x)$  shows hadronic structure at low momentum transfer  
 $Q^2 = e \cdot \Lambda^2 = 0.3 \text{ GeV}^2$   
 $\implies F_2(x, e \cdot \Lambda^2) = a(x) \cdot 1$
- $\kappa(x)$  shows scaling violations

H1/ZEUS combined  $e^+p$  data:



# Motivation

- **Extend the Publication:**  
**“On the Structure of the Proton, the Photon, and the Colour Singlet Exchange”** by M. Erdmann, Phys.Lett.B488:131-137, 2000, hep-ex/0007058
- **Use new more precise data from HERA I (H1, ZEUS)**
  - for Proton, Diffractive Exchange
- **New data from LEP since the last publication (L3, ALEPH, OPAL, DELPHI)**
  - for Photon
- **New: add charm contribution to proton structure function (HERA I, II)**



- **Fit model allows intuitive description of hadronic structure**

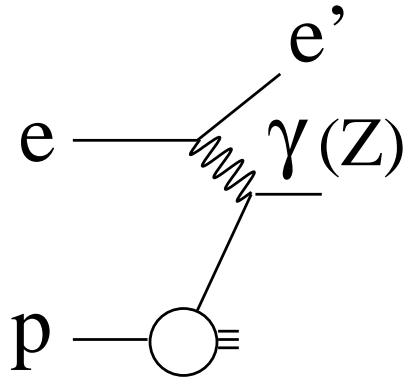
# Analysis Strategy

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- Consider all published  $F_2$  data for NC processes
- Restrict analysis for
  - $y < 0.6$
  - $2 \text{ GeV}^2 < Q^2 < 1000 \text{ GeV}^2$
- Take into account **combined statistical and systematic errors**
- If only reduced cross section provided: estimate  $F_2^{D(3)}$  using  $R = 0.25$   
(for diffractive data)
- Cut on  $x_{IP} < 0.005$  for diffractive data (Pomeron-like region)
- Make  $x$  - **binning** if needed
- Plot  $a$  and  $\kappa$  if
  - more than 2 points for a given  $x$ -bin available (2 parameters)
  - $\delta a < 0.2$  and  $\delta \kappa < 1.0$

# Proton Hadronic Structure

NC process at HERA:



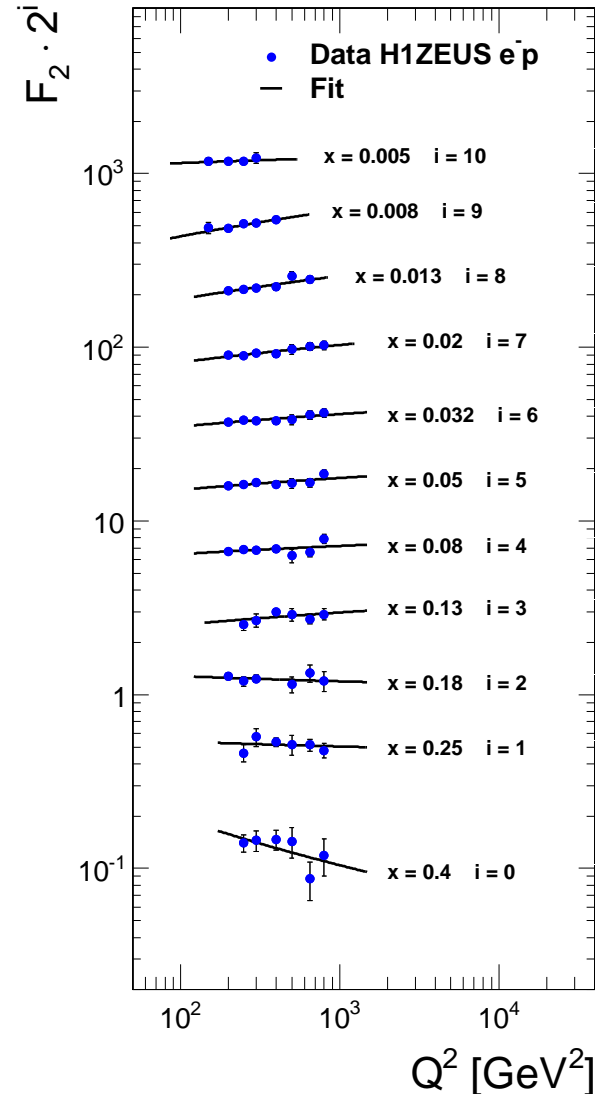
Considered data:

- Combined H1/ZEUS HERA I  $e^+p$  and  $e^-p$  data
- BCDMS data
- EMC data

Find  $a$  and  $\kappa$  from the fit:

$$F_2(x, Q^2) = a(x) \left[ \ln \left( \frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$

H1/ZEUS combined  $e^-p$  data:

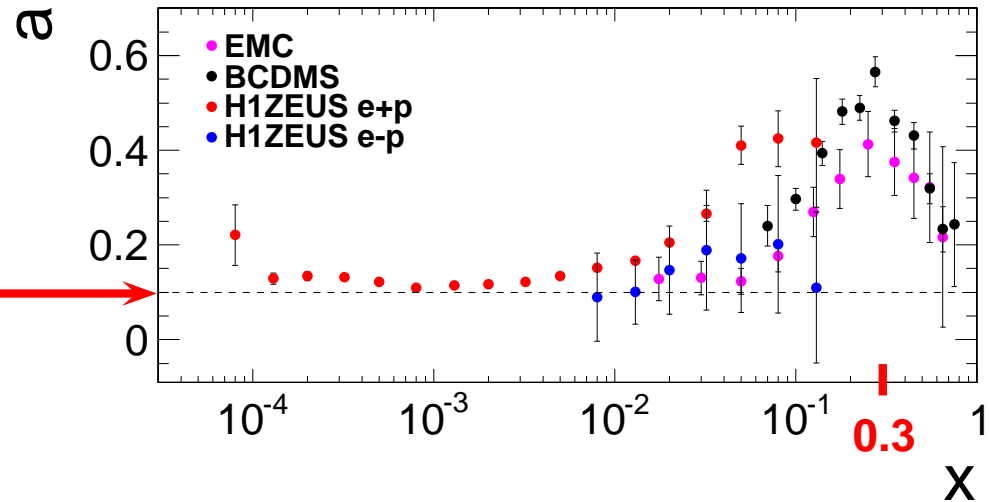


# Proton Hadronic Structure

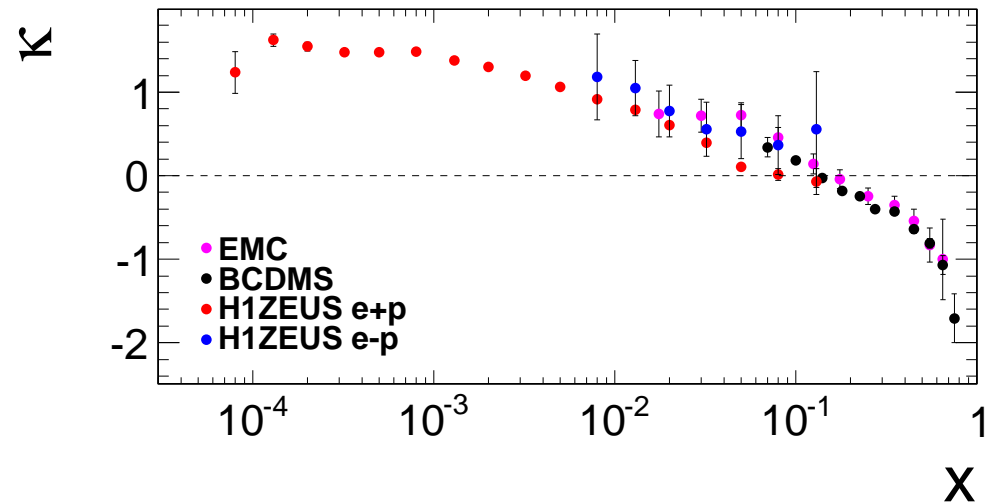
- valence quarks at  $x \sim 1/3$
- low  $x$ : sea quarks
- typical value for hadronic structure at small  $x$ :  $a = 0.1$

- positive and negative scaling violations

## Hadronic Structure of Proton:

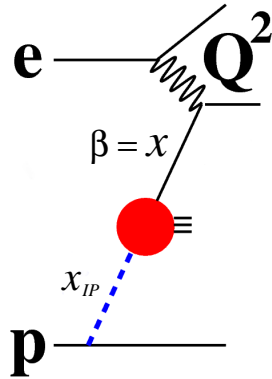


## Scaling Violations:



# Diffractive Exchange Structure

## NC diffractive process at HERA:



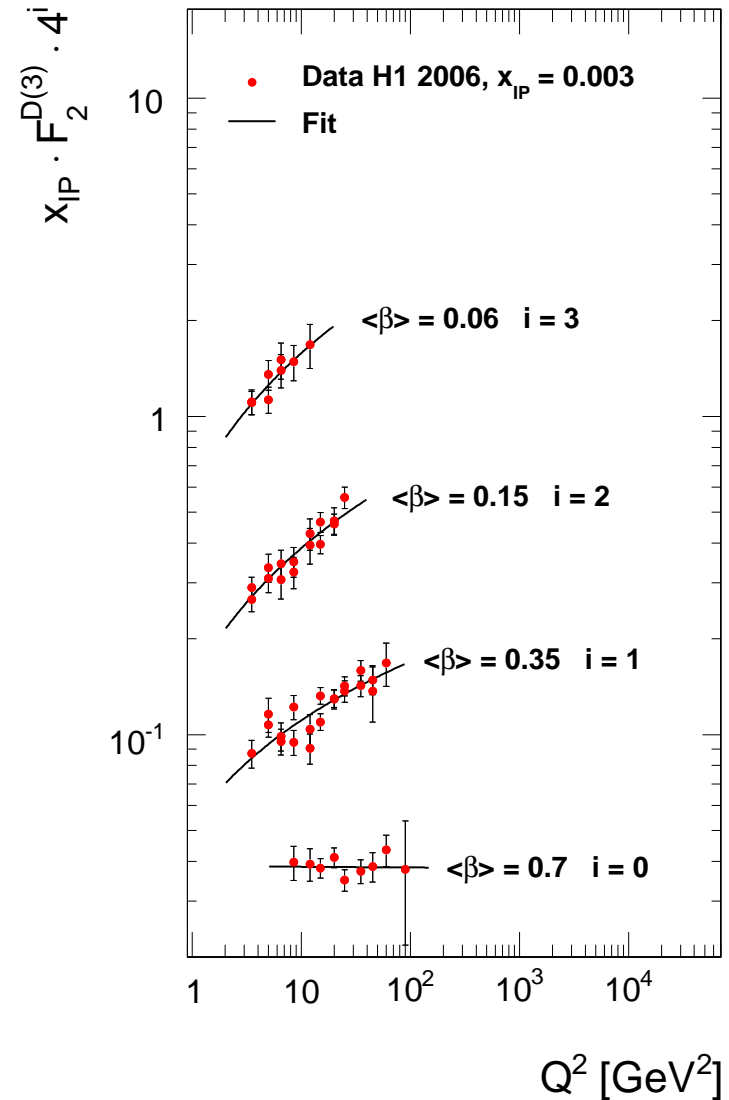
## Considered data:

- H1 and ZEUS HERA I diffractive data for Pomeron-like region:

$$x_{IP} < 0.005$$

Find  $a$  and  $\kappa$  from the fit:

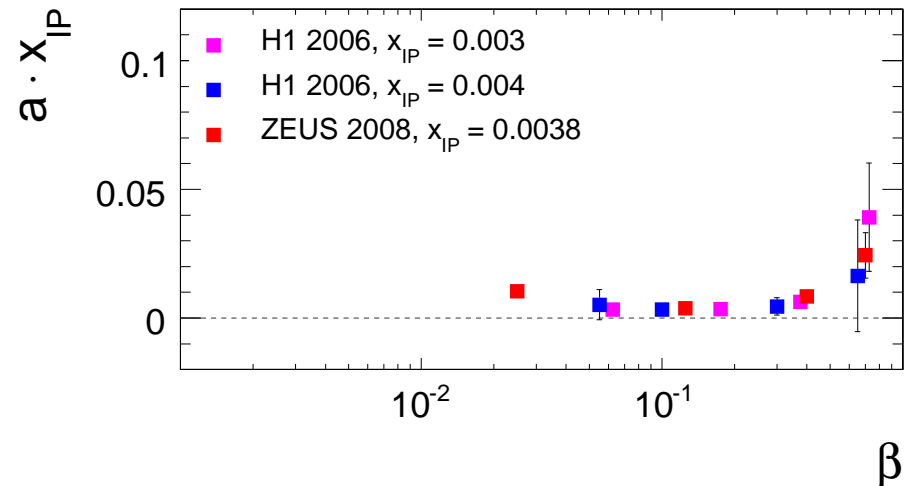
$$F_2(x, Q^2) = a(x) \left[ \ln \left( \frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$





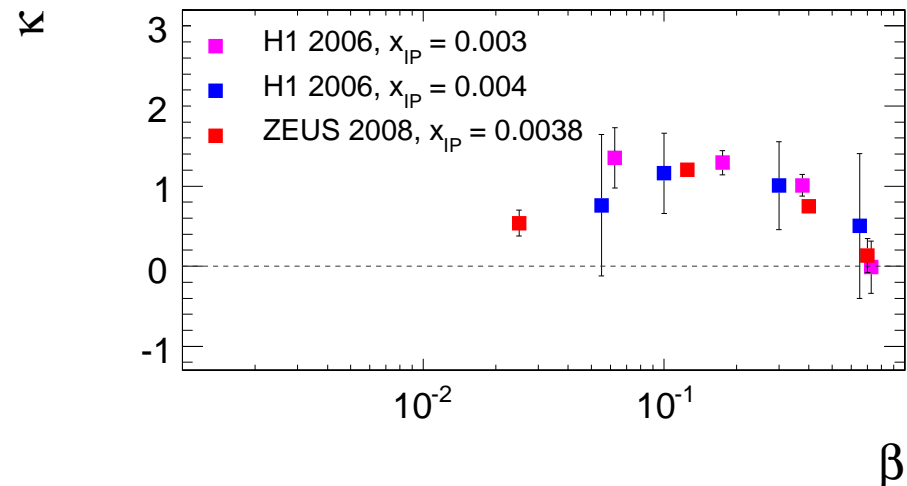
# Diffractive Exchange Structure

## Hadronic Structure:



- high density at large parton momentum, for example 2 gluons where one carries a high momentum fraction

## Scaling Violations:

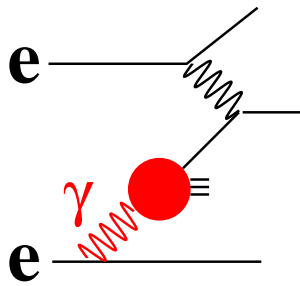


- mostly positive scaling violations

# Photon Structure

Photon structure results from fluctuations of a photon into a colour neutral and flavour neutral hadronic state

NC process for photon structure in  $e^+e^-$  collider:



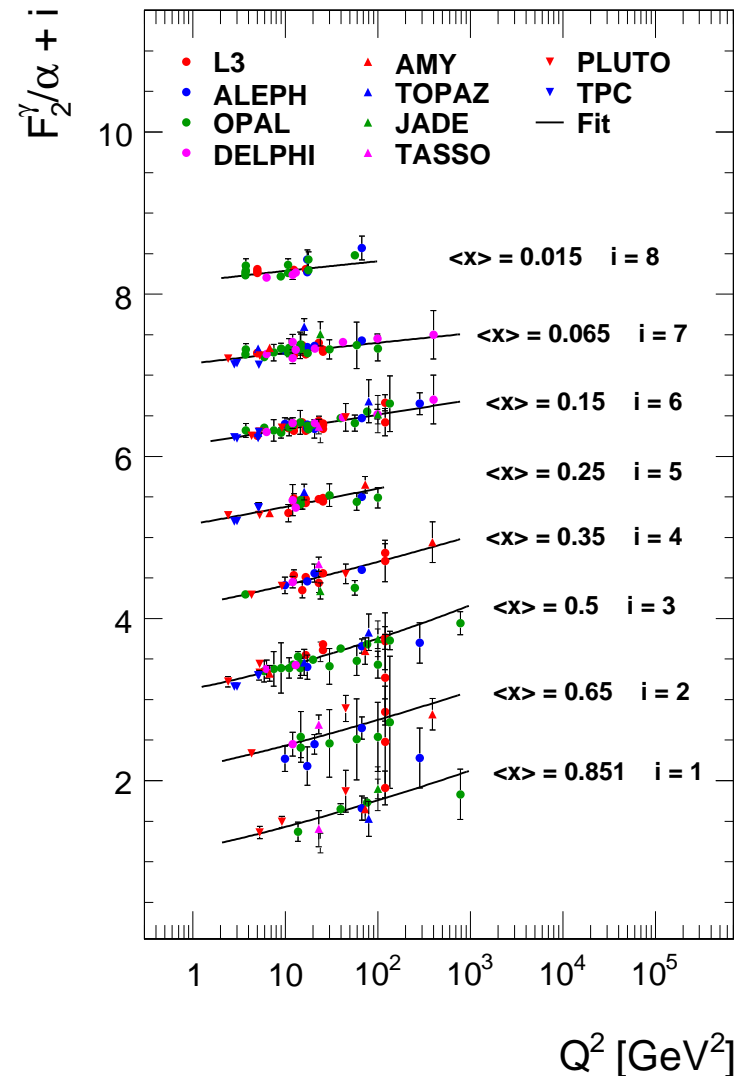
Considered data:

- LEP: L3, ALEPH, OPAL, DELPHI
- JADE, TASSO, etc.

Find  $a$  and  $\kappa$  from the fit:

$$F_2(x, Q^2) = a(x) \left[ \ln \left( \frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$

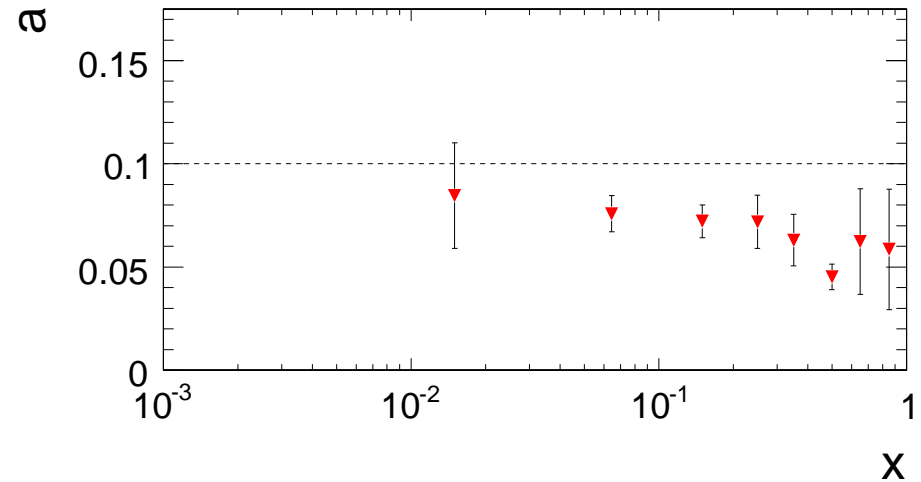
All available  $e^+e^-$  data:



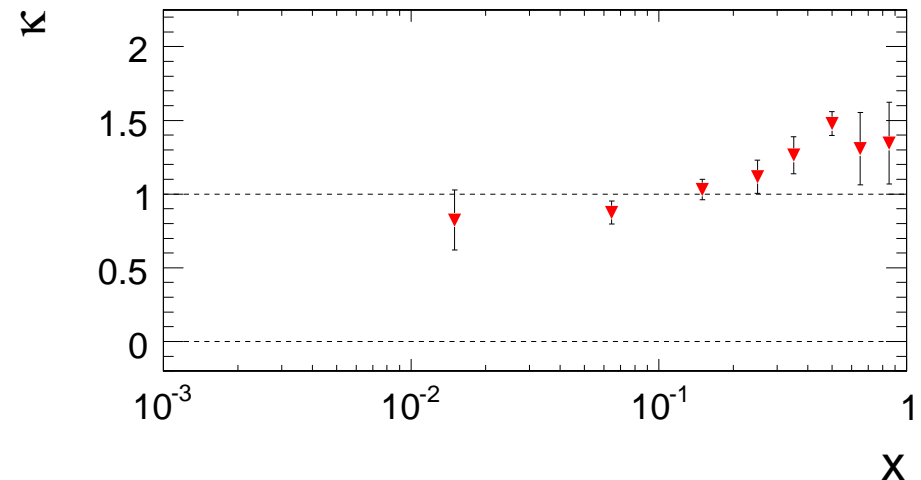
# Photon Structure

- no evidence of valence quarks
- low  $x$ : hadronic-like structure as for proton:  $a \sim 0.1$
- hadronic fall plus point-like rise?
- watch out: correlation between  $a$  and  $\kappa$
  
- positive scaling violations
- $\kappa(x) \sim 1$  as expected from QCD calculations

## Hadronic Structure of Photon:

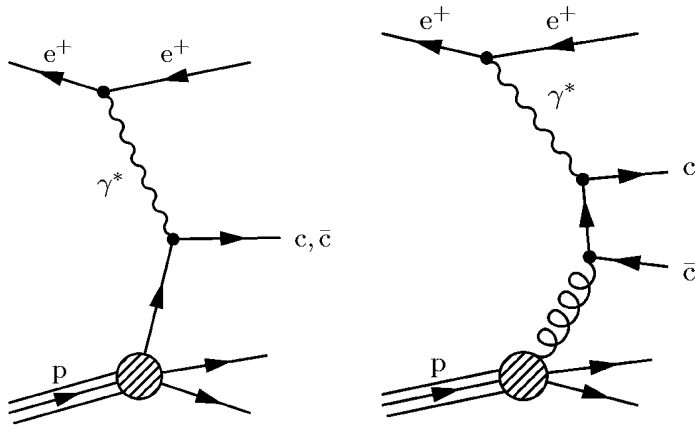


## Scaling Violations for Photon:

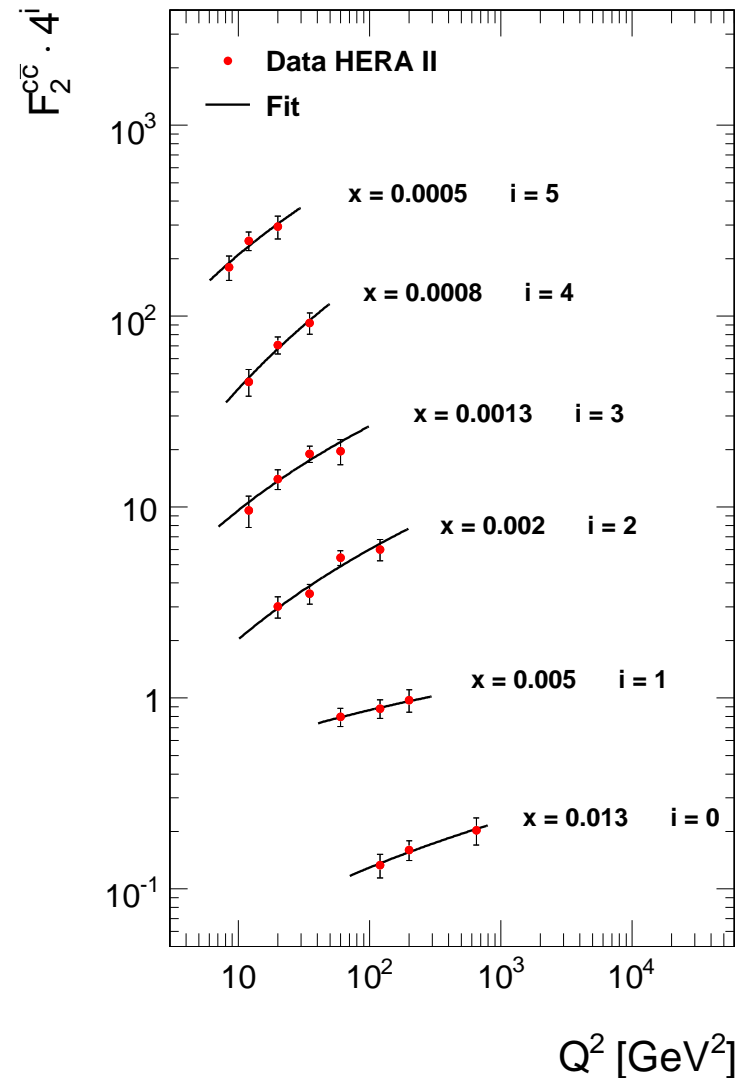


# Charm Contribution to Proton Structure

## NC processes at HERA:



## H1 HERA II charm inclusive measurements:



## Considered data:

- inclusive H1 HERA I/II data
- D-meson HERA I data from H1 and ZEUS
- EMC charm data

Find  $a$  and  $\kappa$  from the fit:

$$F_2(x, Q^2) = a(x) \left[ \ln \left( \frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$

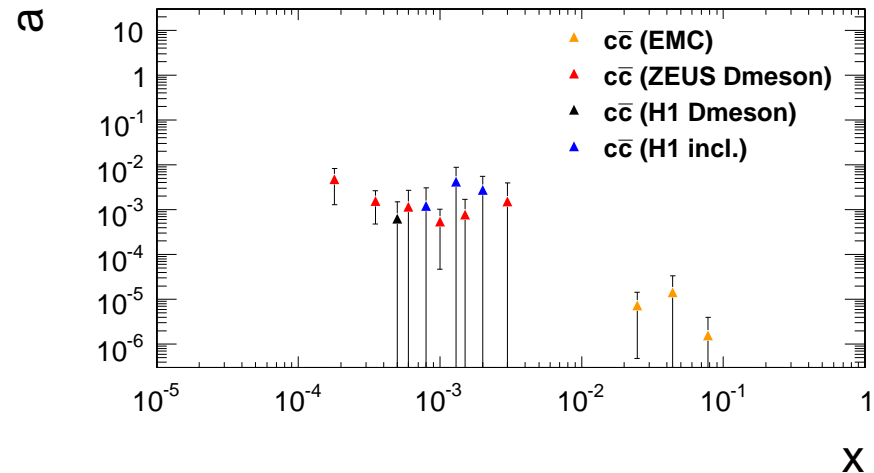
# Charm Contribution to Proton Structure

● negligible charm in the proton when probing with static resolution scale of  $Q^2 = 0.3 \text{ GeV}^2$

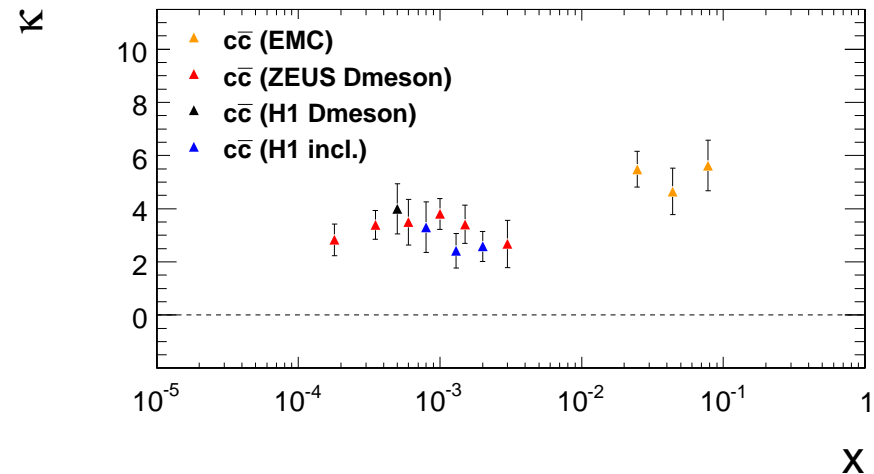
● strong positive scaling violations

● consistent with charm resulting from fluctuations

## Hadronic Structure:



## Scaling Violations:



# Comparison I: Proton and Charm Contribution

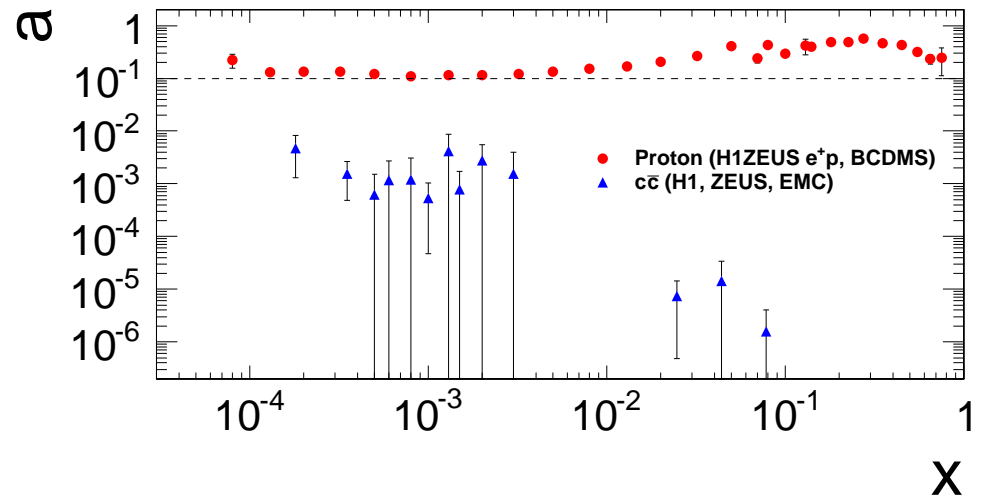
## Proton:

- valence quarks at  $x \sim 1/3$
- low  $x$ : sea quarks
- positive and negative scaling violations

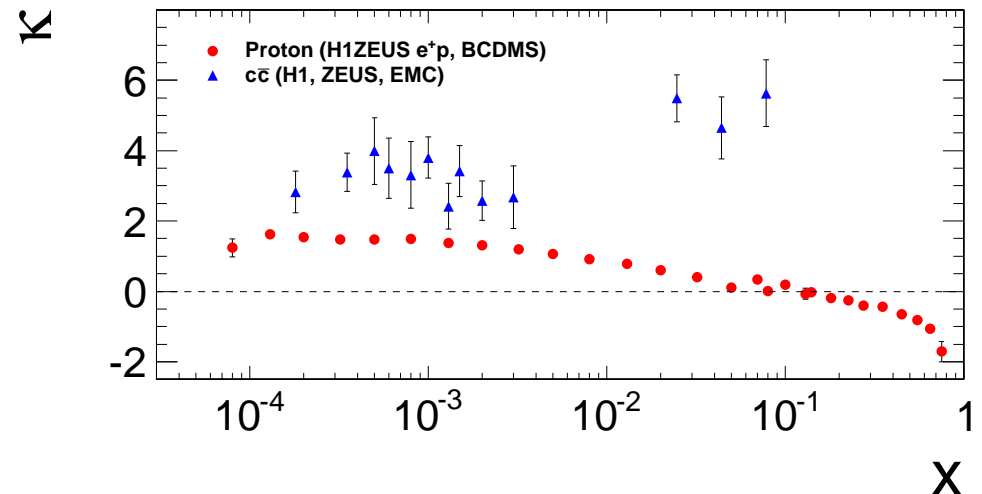
## Charm in Proton:

- strong positive scaling violations
- no charm in the proton when probing with static resolution scale of  $Q^2 = 0.3 \text{ GeV}^2$
- all charm at higher  $Q^2$  results from fluctuations

## Hadronic Structure:



## Scaling Violations:



# Comparison II: Charm, Colour Singlet, Photon

## Charm in Proton:

- strong positive scaling violations
- no charm at  $Q^2 = 0.3 \text{ GeV}^2$
- charm from fluctuations at higher  $Q^2$

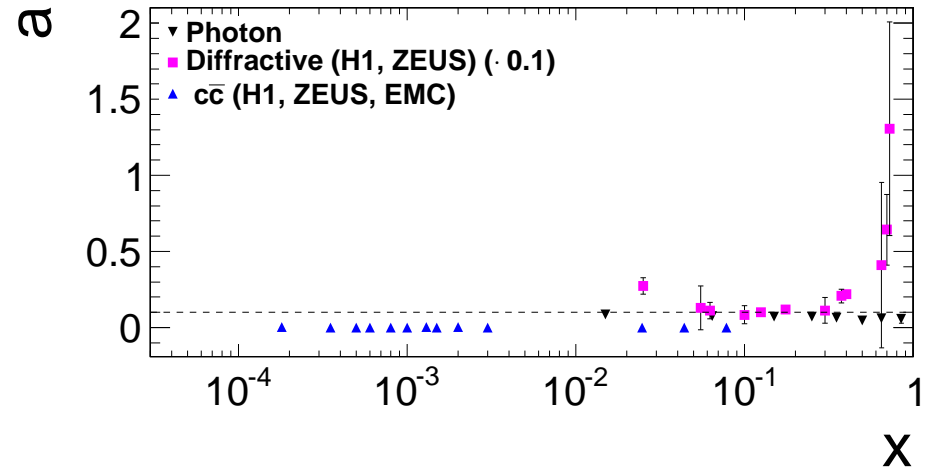
## Colour Singlet Exchange:

- $a$  divided by 10 for comparison
- high density at large  $x$ : suggestive of gluon-gluon system with 1 gluon carrying most of the momentum
- mostly positive scaling violations

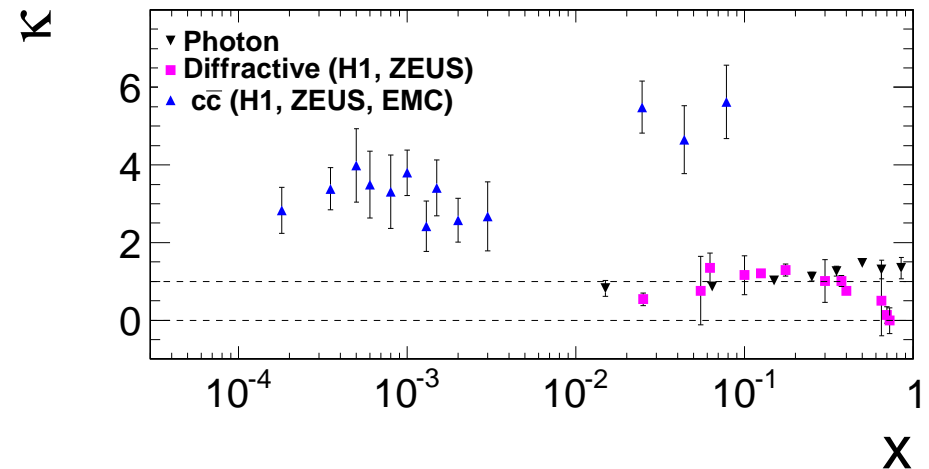
## Photon:

- only sea quarks
- $\kappa(x) \sim 1$  as expected from QCD calculations

## Hadronic Structure:



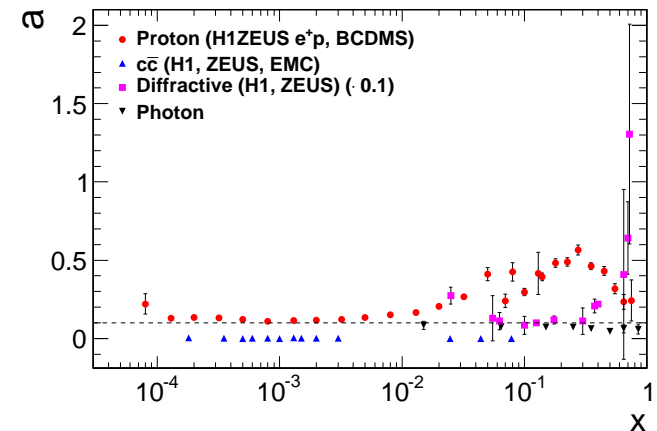
## Scaling Violations:



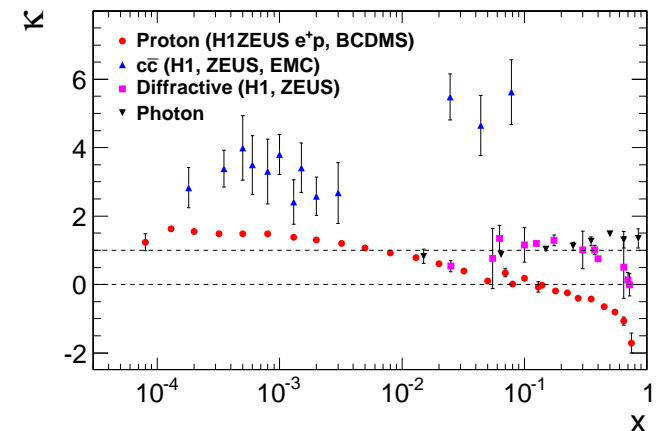
# Summary

- Wealth of new data from  $ep$  collisions at HERA and  $e^+e^-$  collisions at LEP
- Hadronic structures extrapolated to  $Q^2 = 0.3 \text{ GeV}^2$ :
  - **Proton** shows valence quarks at  $x \sim 0.3$ , at low  $x$  sea quarks with negligible heavy quark contributions
  - **Photon**: similar level of sea quarks as the proton
  - **Diffractive exchange**: similar level of sea contribution at low  $x$ , increase towards  $x = 1$  (gluons)
- Scaling violations: strongly positive for charm, photon, proton at low  $x$ , diffractive exchange (except for  $x = 1$ ), negative for proton at high  $x$

## Hadronic Structure:



## Scaling Violations:

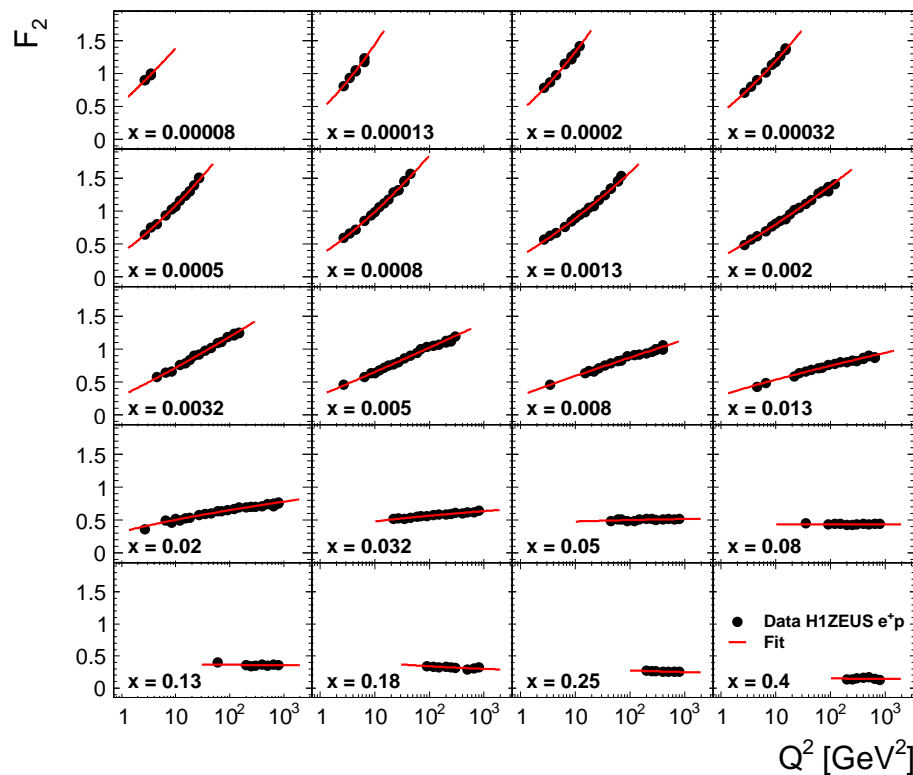




# Backup Slides

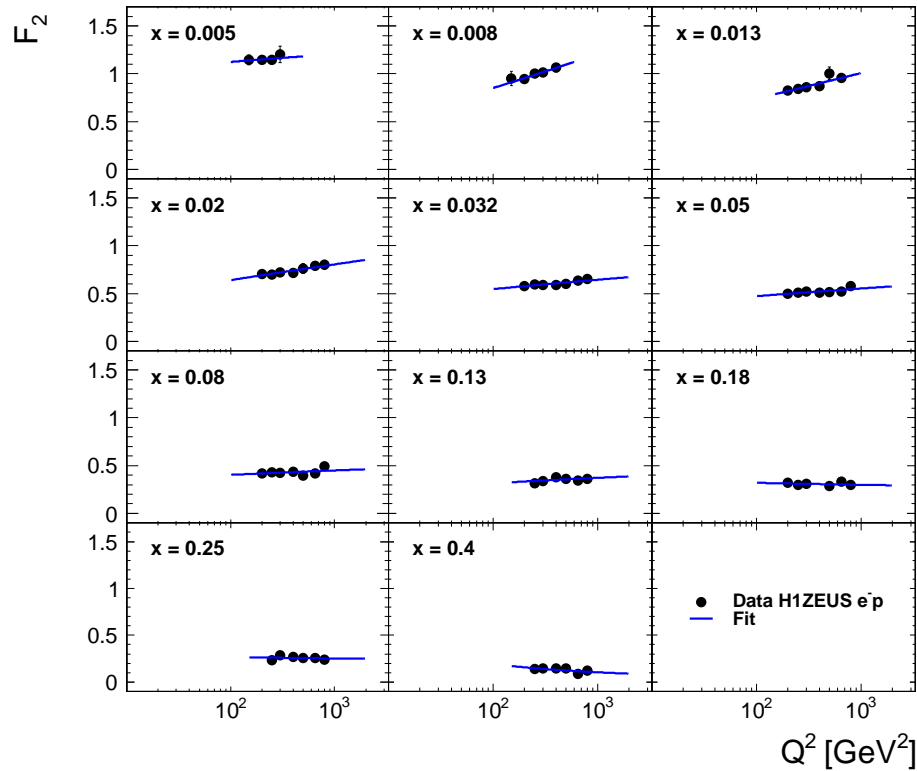
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# Fits of combined H1/ZEUS $e^+p$ data



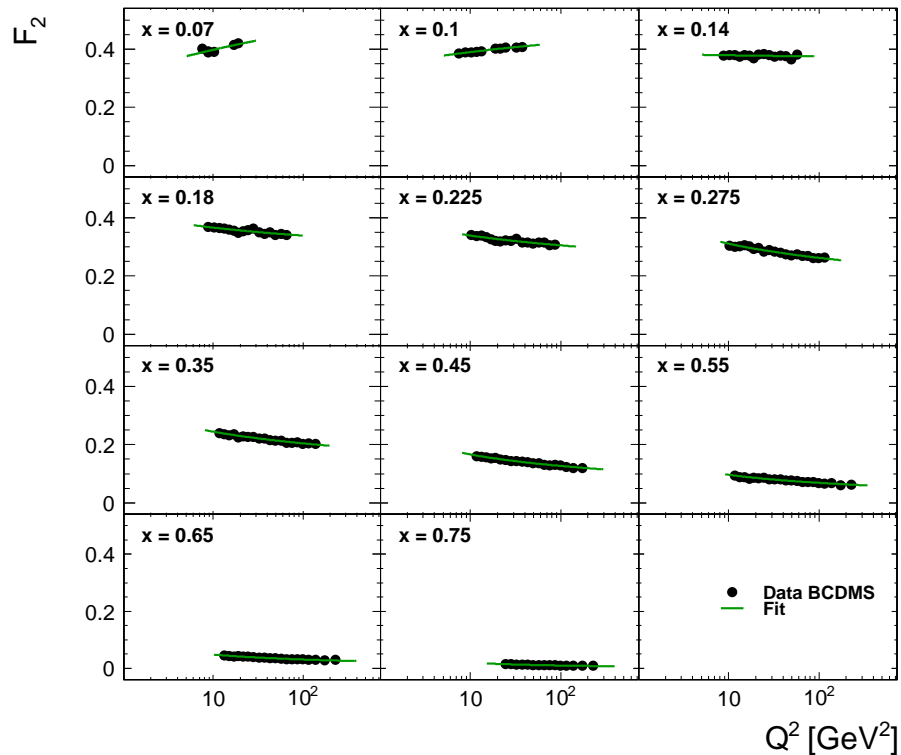
x	a	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2/ndf$
0.00008	0.221	0.064	1.237	0.249	0.80/2
0.00013	0.129	0.012	1.624	0.073	3.00/4
0.0002	0.134	0.009	1.547	0.052	4.12/7
0.00032	0.132	0.006	1.482	0.035	3.80/8
0.0005	0.122	0.005	1.477	0.026	9.99/11
0.0008	0.109	0.004	1.486	0.022	9.71/13
0.0013	0.115	0.004	1.381	0.019	20.69/15
0.002	0.116	0.003	1.303	0.017	19.42/16
0.0032	0.122	0.004	1.197	0.020	13.39/15
0.005	0.135	0.004	1.066	0.017	26.16/19
0.008	0.152	0.005	0.919	0.017	23.60/16
0.013	0.167	0.006	0.789	0.020	28.07/18
0.02	0.205	0.007	0.609	0.018	34.72/22
0.032	0.266	0.017	0.398	0.033	7.02/14
0.05	0.411	0.041	0.106	0.050	14.62/11
0.08	0.425	0.059	0.016	0.069	5.24/9
0.13	0.416	0.136	-0.071	0.156	7.20/6
0.18	0.763	0.255	-0.425	0.164	5.18/7
0.25	0.520	0.323	-0.336	0.294	0.62/5
0.4	0.225	0.238	-0.209	0.508	8.15/5

# Fits of combined H1/ZEUS $e^-p$ data



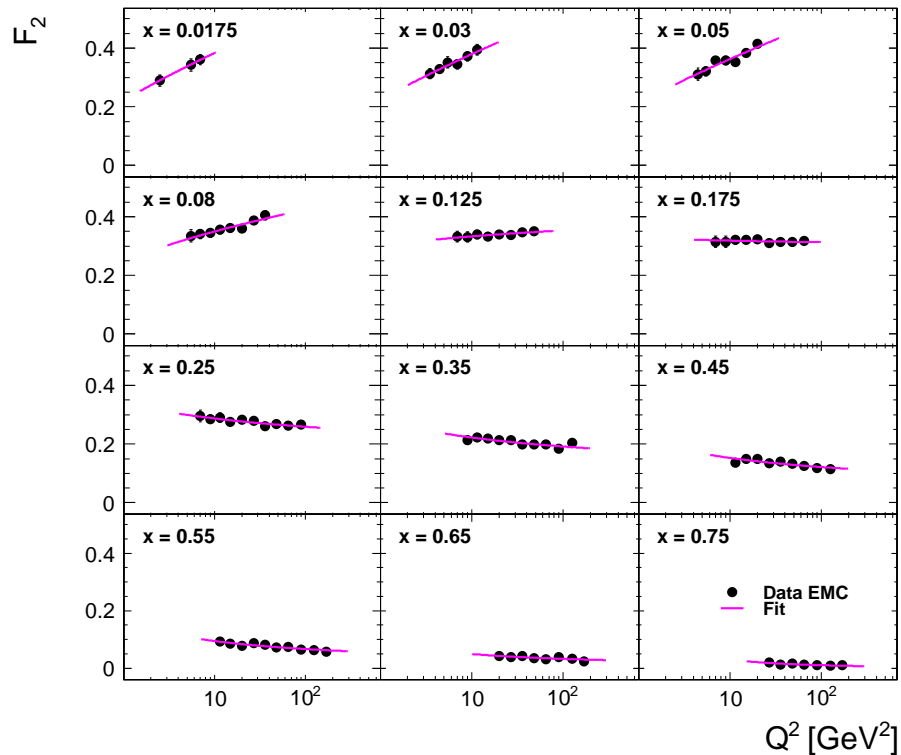
$x$	$a$	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2/ndf$
0.005	0.717	1.239	0.236	0.862	0.29/2
0.008	0.089	0.093	1.183	0.512	0.68/3
0.013	0.100	0.068	1.049	0.330	2.11/4
0.02	0.147	0.093	0.775	0.308	1.49/5
0.032	0.189	0.126	0.558	0.324	1.21/5
0.05	0.172	0.115	0.531	0.323	2.37/5
0.08	0.201	0.145	0.366	0.351	5.17/5
0.13	0.110	0.160	0.554	0.691	4.04/4
0.18	0.499	0.653	-0.234	0.640	1.55/4
0.25	0.407	0.818	-0.219	0.953	2.63/4
0.4	10.429	46.704	-2.095	2.156	3.33/4

# Fits of BCDMS data



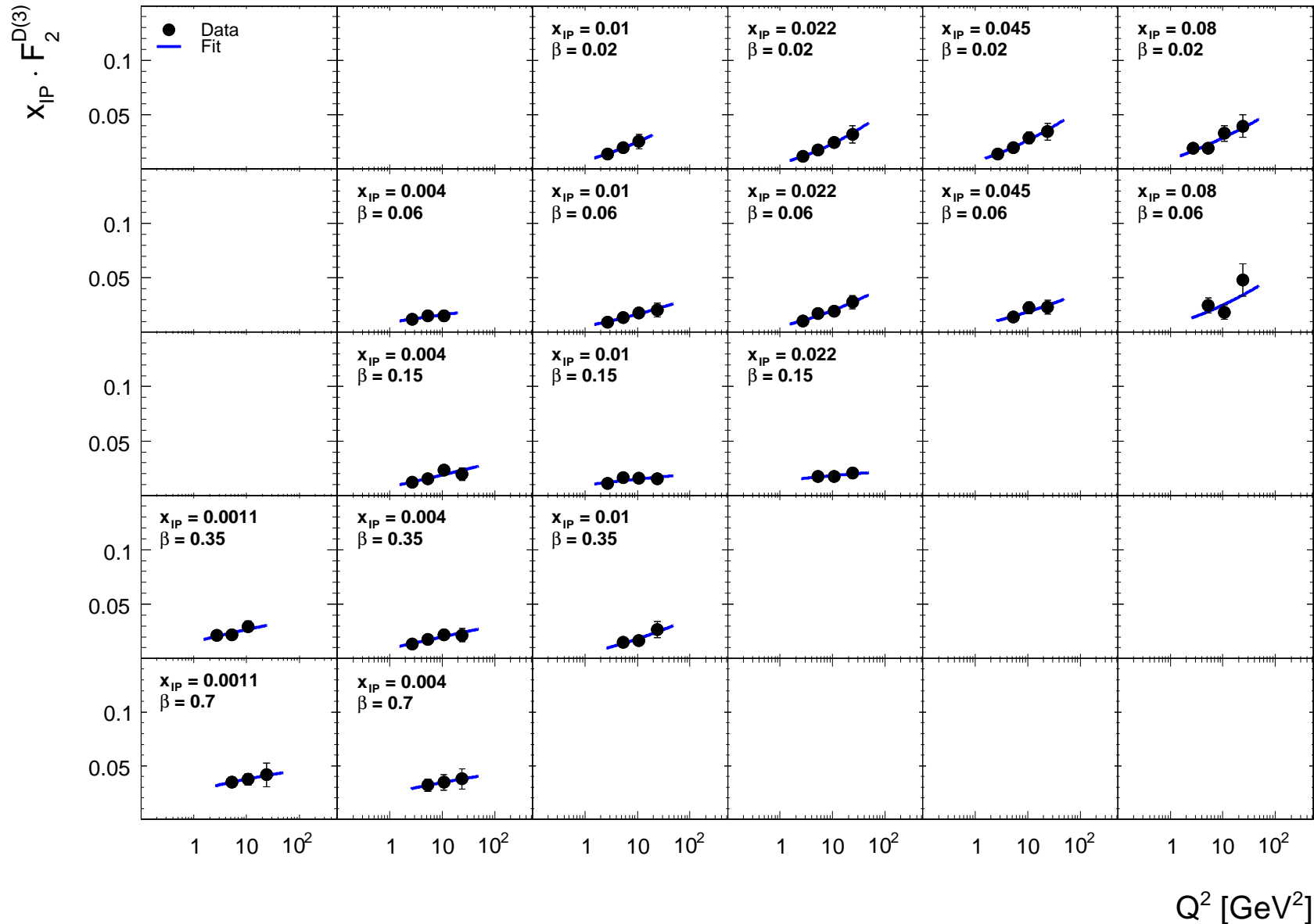
$x$	$a$	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2 / ndf$
0.07	0.240	0.043	0.341	0.118	3.17/4
0.1	0.297	0.023	0.184	0.048	0.66/8
0.14	0.394	0.025	-0.026	0.040	7.80/13
0.18	0.481	0.027	-0.185	0.033	9.11/14
0.225	0.489	0.026	-0.248	0.031	14.09/15
0.275	0.565	0.032	-0.404	0.032	12.69/17
0.35	0.462	0.023	-0.429	0.028	12.62/17
0.45	0.431	0.028	-0.643	0.036	9.79/18
0.55	0.319	0.032	-0.808	0.055	13.66/19
0.65	0.233	0.048	-1.068	0.112	4.55/18
0.75	0.243	0.131	-1.708	0.292	2.96/13

# Fits of EMC data



$x$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.0175	0.128	0.046	0.741	0.274	0.01/1
0.03	0.131	0.035	0.719	0.196	1.01/4
0.05	0.123	0.027	0.727	0.148	4.81/5
0.08	0.177	0.034	0.459	0.120	2.07/6
0.125	0.270	0.052	0.141	0.117	0.50/6
0.175	0.339	0.062	-0.042	0.110	0.77/7
0.25	0.413	0.068	-0.245	0.097	2.39/8
0.35	0.375	0.070	-0.353	0.109	3.90/8
0.45	0.342	0.086	-0.544	0.144	5.60/7
0.55	0.322	0.116	-0.829	0.204	4.24/8
0.65	0.217	0.190	-1.001	0.484	4.05/6
0.75	1.475	3.878	-2.619	1.467	1.12/5

# Fits of diffractive data (H1, DESY 06-048) I



# Fits of diffractive data (H1, DESY 06-048) II

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$x_{IP}$	$\beta$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.01	0.02	0.002	0.003	1.602	0.924	0.001/1
0.022	0.02	0.001	0.001	1.945	0.527	0.051/2
0.045	0.02	0.002	0.001	1.754	0.495	0.164/2
0.08	0.02	0.003	0.003	1.523	0.675	1.62/2
0.004	0.06	0.005	0.006	0.762	0.882	0.104/1
0.01	0.06	0.002	0.002	1.49	0.629	0.129/2
0.022	0.06	0.001	0.001	1.757	0.527	0.469/2
0.045	0.06	0.002	0.002	1.553	0.871	0.507/1
0.08	0.06	0.002	0.006	1.726	2.203	2.694/1

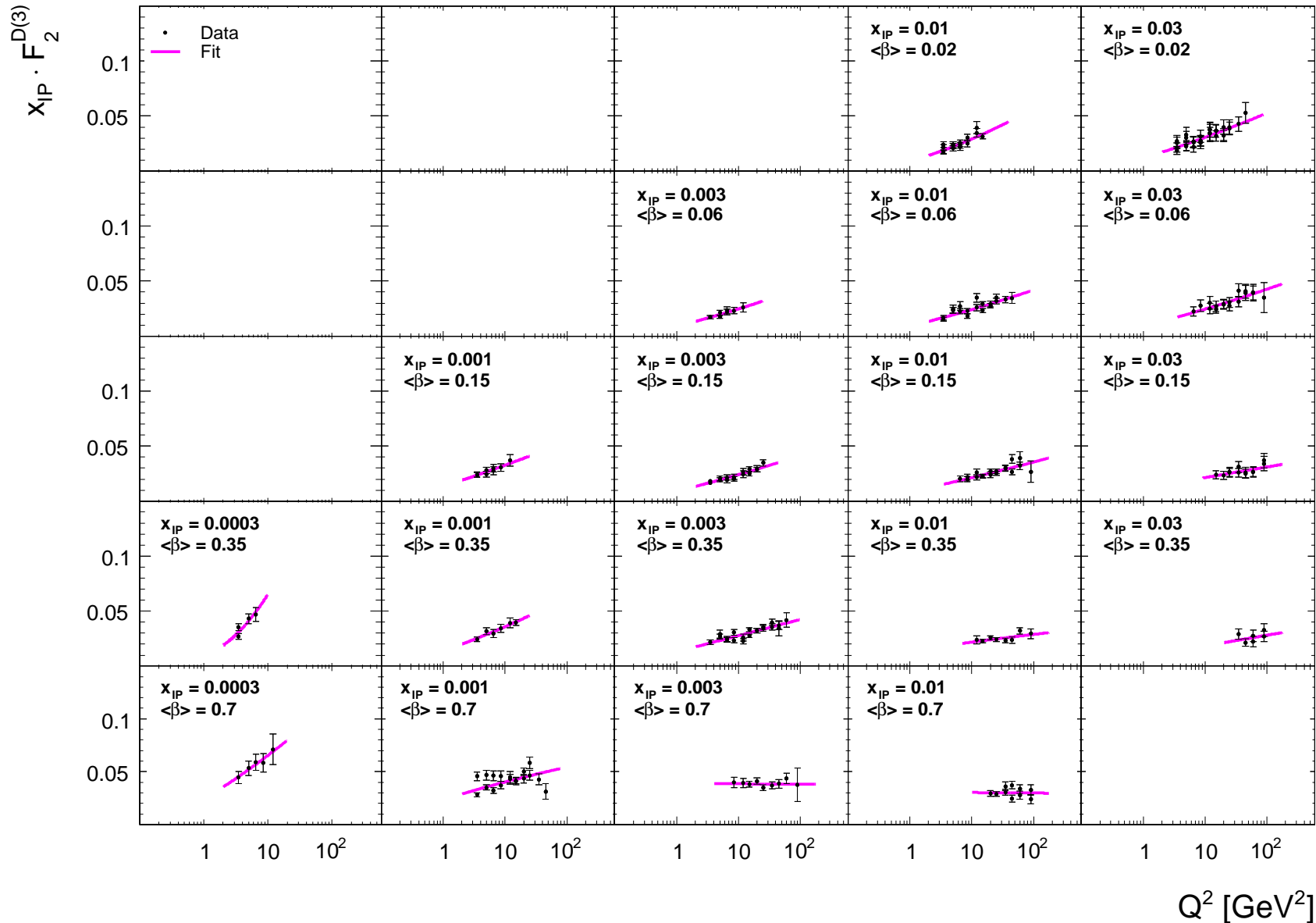
# Fits of diffractive data (H1, DESY 06-048) III

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$x_{IP}$	$\beta$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.004	0.15	0.003	0.002	1.16	0.503	1.409/2
0.01	0.15	0.006	0.005	0.619	0.571	0.878/2
0.022	0.15	0.009	0.013	0.452	0.961	0.126/1
0.0011	0.35	0.009	0.006	0.748	0.563	0.77/1
0.004	0.35	0.004	0.003	1.006	0.548	0.416/2
0.01	0.35	0.001	0.003	1.697	1.37	0.318/1
0.0011	0.7	0.018	0.021	0.484	0.814	0.006/1
0.004	0.7	0.016	0.022	0.502	0.904	0.0/1



# Fits of diffractive data (H1, DESY 06-049) I



# Fits of diffractive data (H1, DESY 06-049) II

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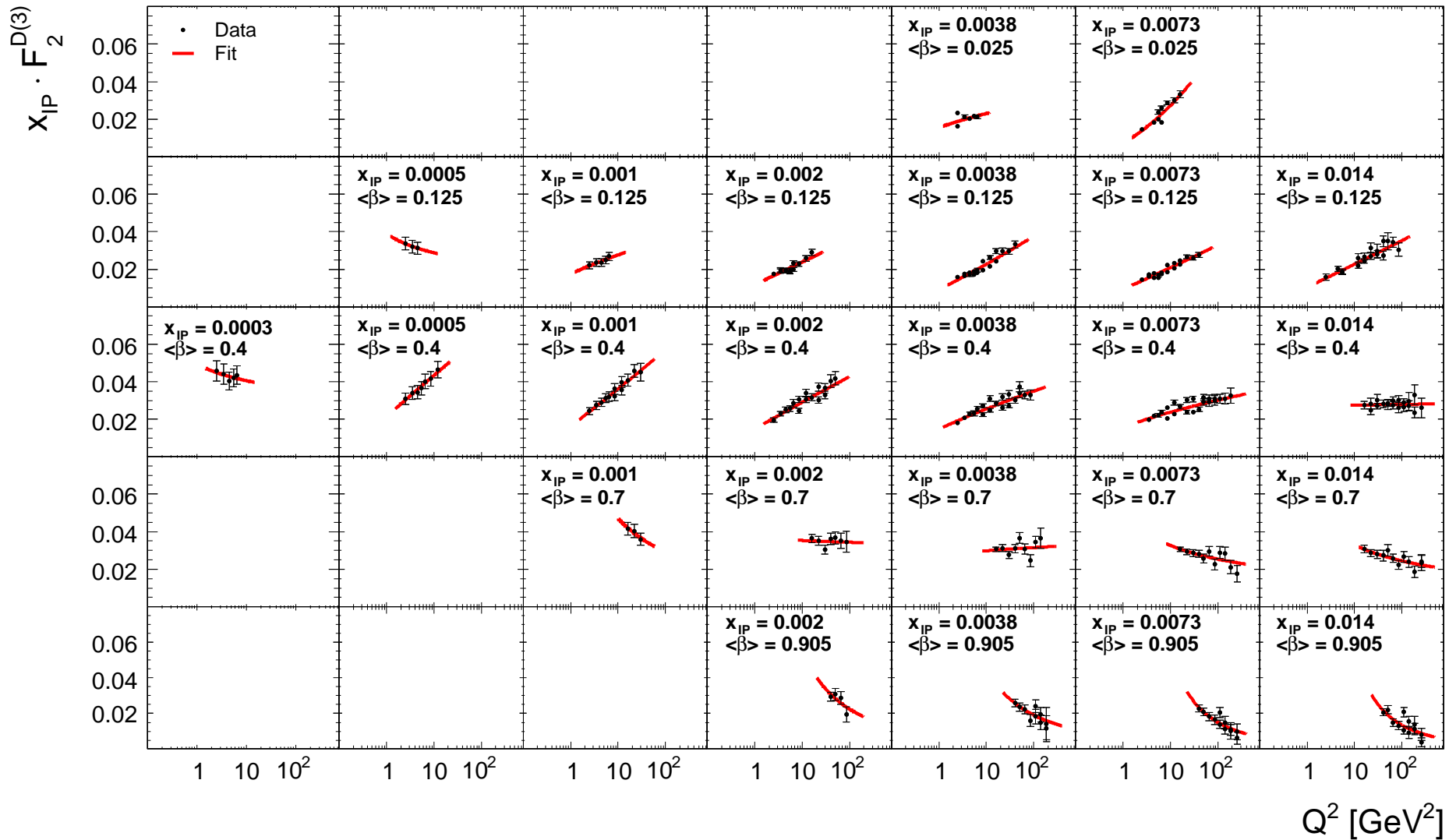
$x_{IP}$	$\beta$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.01	0.02	0.003	0.001	1.59	0.22	14.355/13
0.03	0.02	0.005	0.001	1.285	0.21	11.495/29
0.003	0.06	0.003	0.002	1.351	0.377	2.367/6
0.01	0.06	0.003	0.001	1.308	0.142	27.716/16
0.03	0.06	0.004	0.002	1.31	0.336	5.915/15
0.001	0.15	0.006	0.003	1.194	0.408	1.575/6
0.003	0.15	0.004	0.001	1.292	0.153	8.876/13
0.01	0.15	0.004	0.001	1.207	0.19	13.604/16
0.03	0.15	0.006	0.005	0.888	0.5	3.39/10

# Fits of diffractive data (H1, DESY 06-049) III

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$x_{IP}$	$\beta$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.0003	0.35	0.001	0.001	2.729	0.762	4.96/2
0.001	0.35	0.005	0.002	1.293	0.274	1.629/4
0.003	0.35	0.006	0.001	1.01	0.136	24.783/18
0.01	0.35	0.008	0.005	0.657	0.347	5.968/6
0.03	0.35	0.004	0.015	0.999	1.913	3.554/4
0.0003	0.7	0.009	0.008	1.347	0.636	0.312/3
0.001	0.7	0.014	0.003	0.72	0.127	46.23/16
0.003	0.7	0.039	0.021	-0.012	0.325	3.74/7
0.01	0.7	0.032	0.024	-0.043	0.426	13.109/8

# Fits of diffractive data (ZEUS 2008 LRG) I



# Fits of diffractive data (ZEUS 2008 LRG) II

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$x_{IP}$	$\beta$	$a$	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2 / ndf$
0.0038	0.025	0.01	0.002	0.538	0.161	40.81/4
0.0073	0.025	0.002	0.0	1.797	0.118	51.755/7
0.0005	0.125	0.053	0.052	-0.41	0.82	0.003/1
0.001	0.125	0.011	0.005	0.62	0.379	0.471/3
0.002	0.125	0.006	0.001	0.965	0.14	14.203/10
0.0038	0.125	0.004	0.0	1.206	0.069	58.196/16
0.0073	0.125	0.004	0.0	1.084	0.057	53.606/16
0.014	0.125	0.005	0.001	1.052	0.1	16.783/15
0.0003	0.4	0.06	0.043	-0.268	0.557	0.422/3
0.0005	0.4	0.011	0.004	0.957	0.285	0.501/5
0.001	0.4	0.007	0.001	1.083	0.138	3.151/10
0.002	0.4	0.007	0.001	0.918	0.076	24.762/14

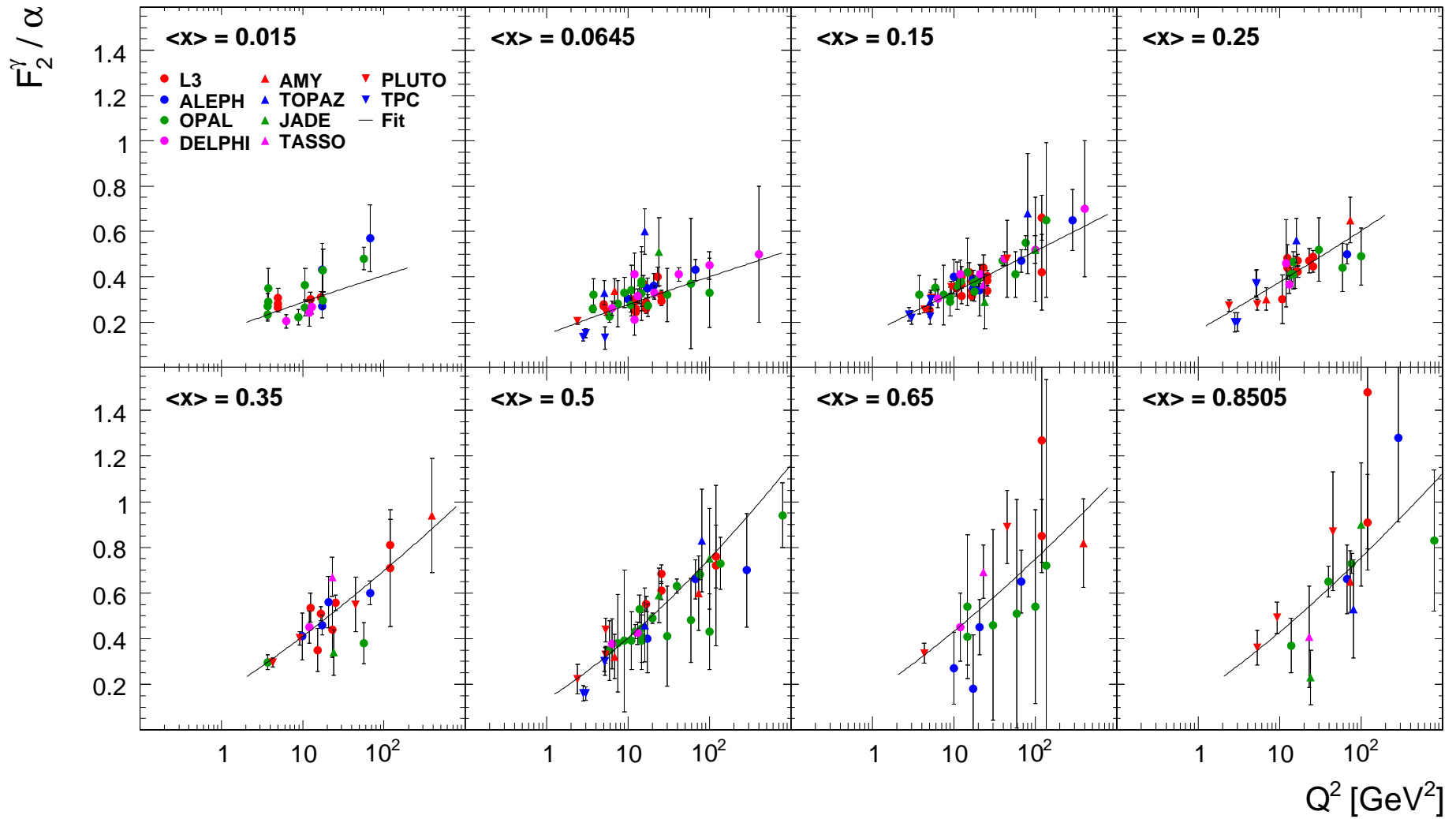
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# Fits of diffractive data (ZEUS 2008 LRG) III

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$x_{IP}$	$\beta$	<b>a</b>	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2 / ndf$
<b>0.0038</b>	<b>0.4</b>	<b>0.008</b>	<b>0.001</b>	<b>0.75</b>	<b>0.053</b>	<b>47.777/17</b>
<b>0.0073</b>	<b>0.4</b>	<b>0.01</b>	<b>0.001</b>	<b>0.567</b>	<b>0.051</b>	<b>83.159/21</b>
<b>0.014</b>	<b>0.4</b>	<b>0.026</b>	<b>0.008</b>	<b>0.039</b>	<b>0.166</b>	<b>8.9/17</b>
<b>0.001</b>	<b>0.7</b>	<b>0.253</b>	<b>0.365</b>	<b>-1.135</b>	<b>0.879</b>	<b>0.177/1</b>
<b>0.002</b>	<b>0.7</b>	<b>0.039</b>	<b>0.025</b>	<b>-0.067</b>	<b>0.376</b>	<b>4.028/5</b>
<b>0.0038</b>	<b>0.7</b>	<b>0.024</b>	<b>0.009</b>	<b>0.135</b>	<b>0.212</b>	<b>13.012/7</b>
<b>0.0073</b>	<b>0.7</b>	<b>0.079</b>	<b>0.024</b>	<b>-0.599</b>	<b>0.173</b>	<b>8.49/9</b>
<b>0.014</b>	<b>0.7</b>	<b>0.093</b>	<b>0.033</b>	<b>-0.703</b>	<b>0.198</b>	<b>5.798/10</b>
<b>0.002</b>	<b>0.905</b>	<b>1.358</b>	<b>3.185</b>	<b>-2.158</b>	<b>1.31</b>	<b>2.408/2</b>
<b>0.0038</b>	<b>0.905</b>	<b>0.939</b>	<b>1.196</b>	<b>-2.049</b>	<b>0.697</b>	<b>4.886/8</b>
<b>0.0073</b>	<b>0.905</b>	<b>4.618</b>	<b>4.697</b>	<b>-3.012</b>	<b>0.553</b>	<b>6.837/10</b>
<b>0.014</b>	<b>0.905</b>	<b>6.423</b>	<b>8.048</b>	<b>-3.241</b>	<b>0.68</b>	<b>20.001/10</b>

# Fits of photon data I



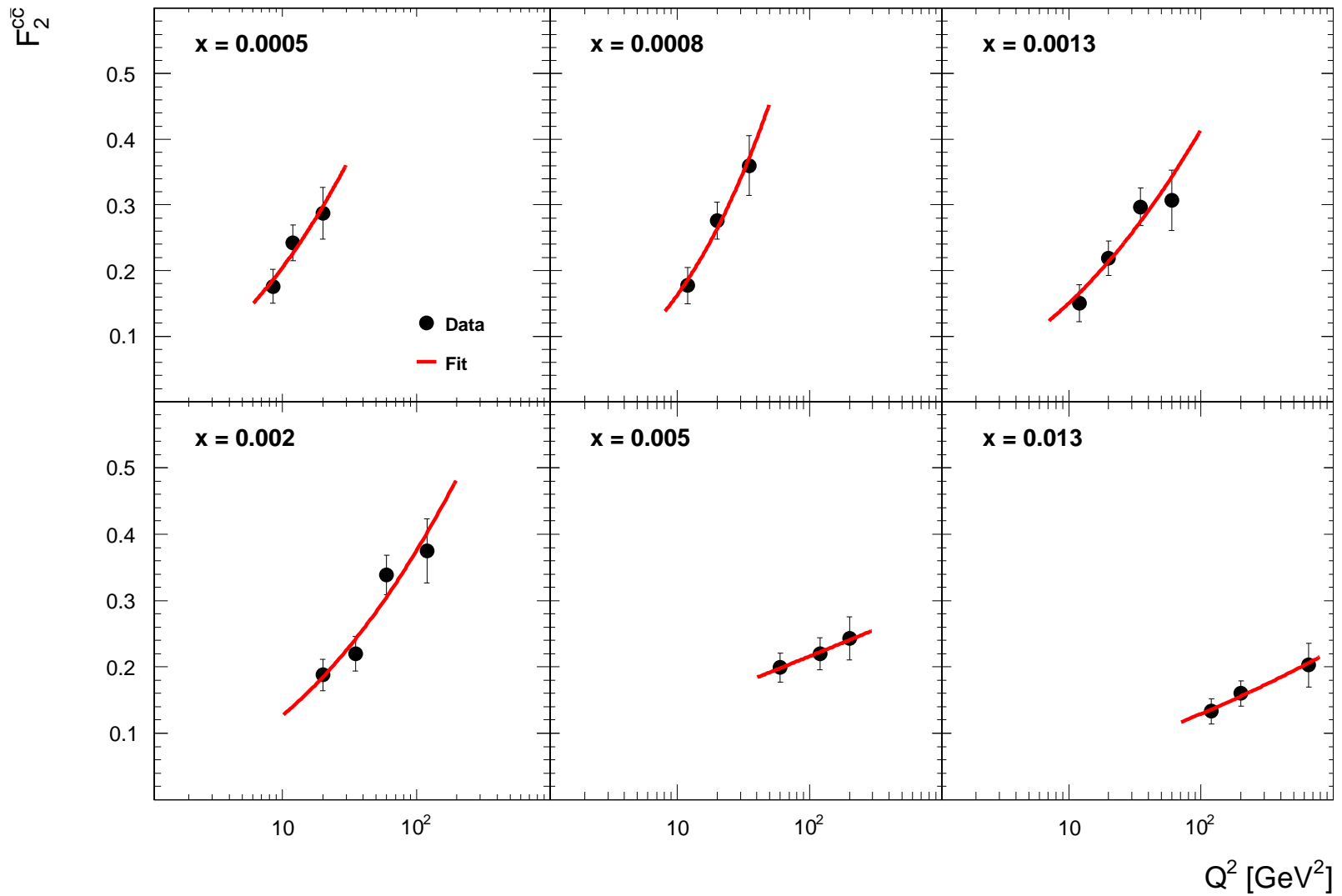
# Fits of photon data II

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$x$	$a$	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2/ndf$
0.015	0.085	0.025	0.824	0.204	26.65/19
0.065	0.076	0.009	0.874	0.077	106.539/48
0.15	0.072	0.008	1.031	0.07	57.489/53
0.25	0.072	0.013	1.118	0.114	27.169/25
0.35	0.063	0.012	1.264	0.125	23.623/18
0.5	0.045	0.006	1.477	0.081	56.96/38
0.65	0.062	0.026	1.307	0.245	10.073/15
0.851	0.059	0.029	1.345	0.277	14.723/14



# Fits of charm data (H1 inclusive) I

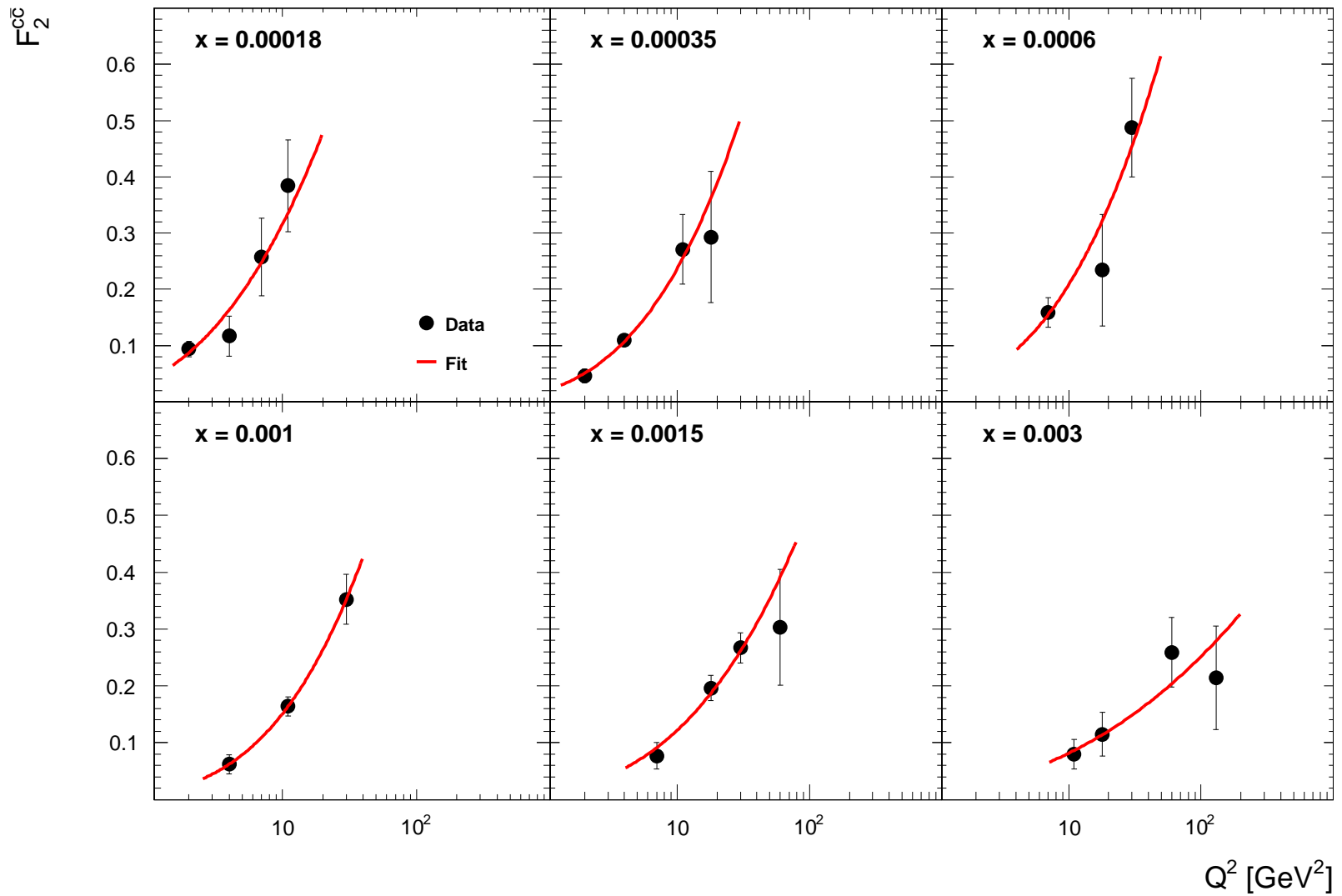


# Fits of charm data (H1 inclusive) II

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$x$	$a$	$\delta a$	$\kappa$	$\delta \kappa$	$\chi^2/ndf$
0.0005	0.005	0.008	2.561	1.077	0.519/1
0.0008	0.001	0.002	3.305	0.947	0.363/1
0.0013	0.004	0.005	2.416	0.651	1.525/2
0.002	0.003	0.003	2.581	0.563	2.279/2
0.005	0.027	0.052	1.092	1.015	0.017/1
0.013	0.004	0.007	1.89	1.005	0.084/1

# Fits of charm data (ZEUS D meson) I

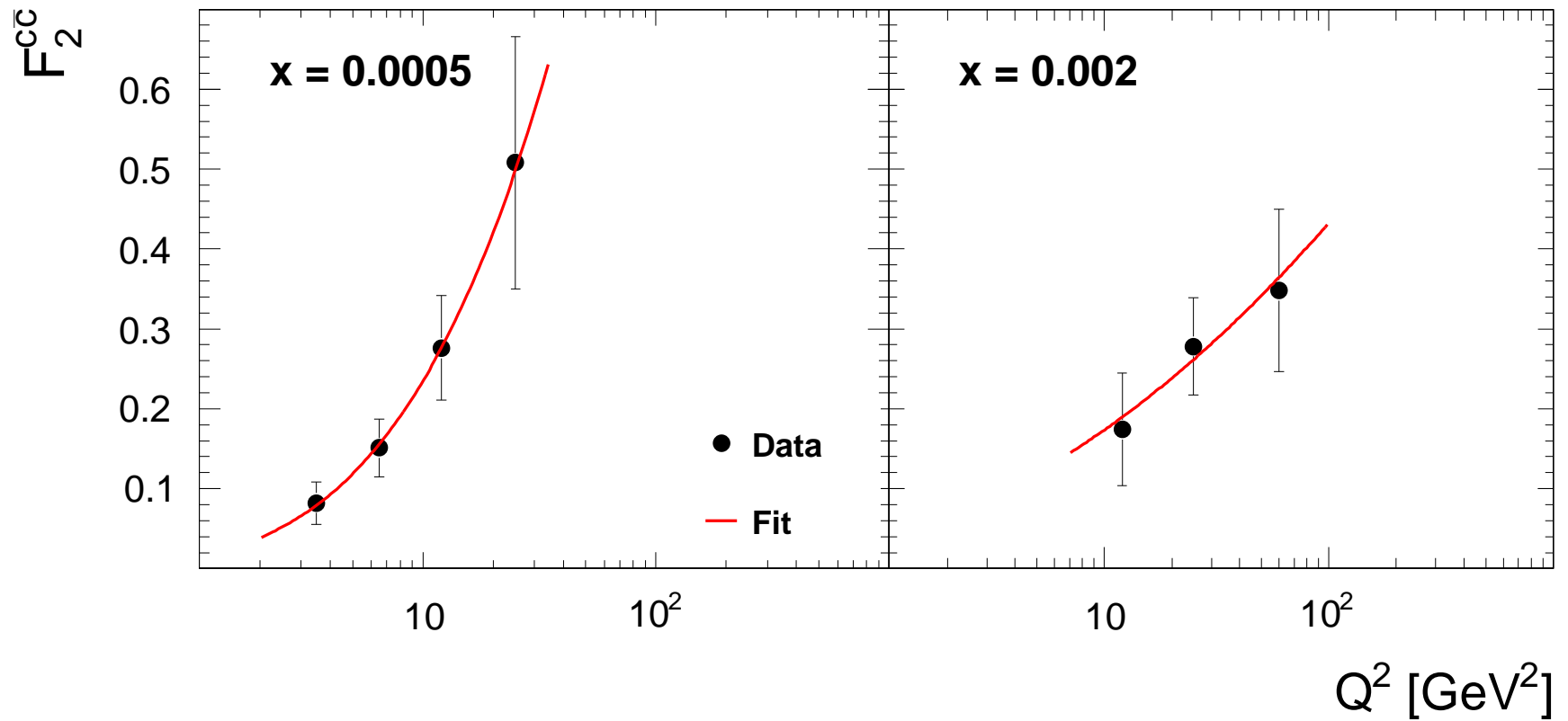


# Fits of charm data (ZEUS D meson) II

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$x$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.0002	0.005	0.003	2.829	0.591	2.294/2
0.0004	0.002	0.001	3.385	0.542	0.639/2
0.0006	0.001	0.002	3.495	0.859	0.963/1
0.001	0.001	0.0	3.802	0.585	0.0/1
0.0015	0.001	0.001	3.413	0.722	1.345/2
0.003	0.002	0.002	2.677	0.89	1.384/2

# Fits of charm data (H1 D meson) I

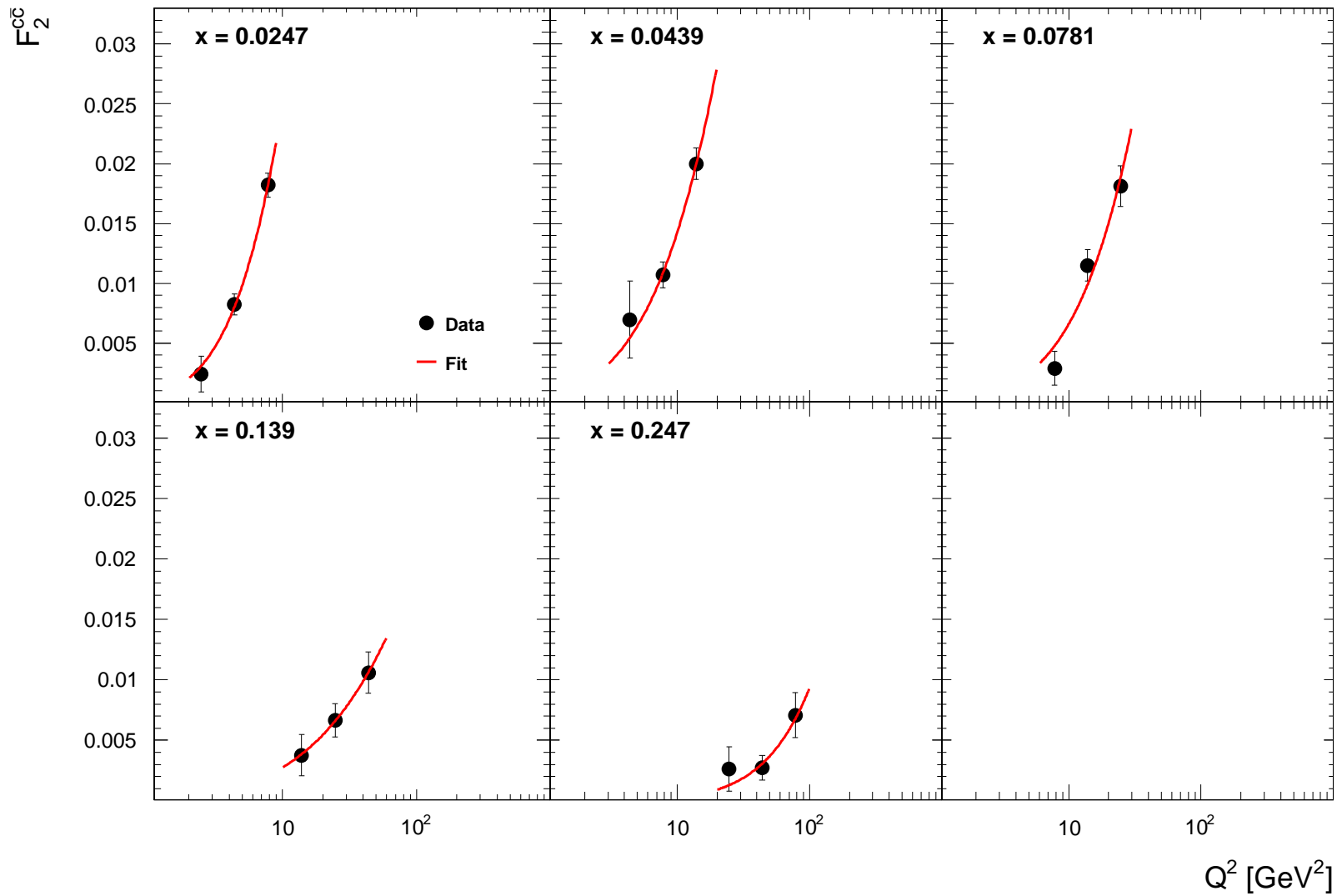


# Fits of charm data (H1 D meson) II

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$x$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
<b>0.0005</b>	<b>0.001</b>	<b>0.001</b>	<b>3.992</b>	<b>0.945</b>	<b>0.031/2</b>
<b>0.002</b>	<b>0.007</b>	<b>0.017</b>	<b>2.173</b>	<b>1.465</b>	<b>0.147/1</b>

# Fits of charm data (EMC) I



# Fits of charm data (EMC) II

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$x$	$a$	$\delta a$	$\kappa$	$\delta\kappa$	$\chi^2/ndf$
0.0247	0.0	0.0	5.486	0.671	0.239/1
0.0439	0.0	0.0	4.65	0.878	0.253/1
0.0781	0.0	0.0	5.626	0.947	3.448/1
0.139	0.0	0.0	4.668	1.815	0.005/1
0.247	0.0	0.0	8.497	4.54	0.678/1



# Used Publications I

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## Proton:

- J. J. Aubert *et al.* [European Muon Collaboration], Nucl. Phys. B 259 (1985) 189.
- A. C. Benvenuti *et al.* [BCDMS Collaboration], Phys. Lett. B 223 (1989) 485.
- F. D. Aaron *et al.* [H1 Collaboration and ZEUS Collaboration], JHEP 1001 (2010) 109 [arXiv:0911.0884 [hep-ex]].

## Diffractive Exchange:

- S. Chekanov *et al.* [ZEUS Collaboration], Nucl. Phys. B 816 (2009) 1 [arXiv:0812.2003 [hep-ex]].
- S. Chekanov [ZEUS Collaboration], Nucl. Phys. B 800 (2008) 1 [arXiv:0802.3017 [hep-ex]].
- A. Aktas *et al.* [H1 Collaboration], Eur. Phys. J. C 48 (2006) 749 [arXiv:hep-ex/0606003].
- A. Aktas *et al.* [H1 Collaboration], Eur. Phys. J. C 48 (2006) 715 [arXiv:hep-ex/0606004].

# Used Publications II

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## Photon:

- M. Acciarri *et al.* [L3 Collaboration], Phys. Lett. B 436 (1998) 403.
- M. Acciarri *et al.* [L3 Collaboration], Phys. Lett. B 447 (1999) 147.
- M. Acciarri *et al.* [L3 Collaboration], Phys. Lett. B 483 (2000) 373 [arXiv:hep-ex/0004005].
- P. Achard *et al.* [L3 Collaboration], Phys. Lett. B 622 (2005) 249 [arXiv:hep-ex/0507042].
- R. Akers *et al.* [OPAL Collaboration], Z. Phys. C 61 (1994) 199.
- K. Ackerstaff *et al.* [OPAL Collaboration], Z. Phys. C 74 (1997) 33.
- K. Ackerstaff *et al.* [OPAL Collaboration], Phys. Lett. B 411 (1997) 387 [arXiv:hep-ex/9708019].
- K. Ackerstaff *et al.* [OPAL Collaboration], Phys. Lett. B 412 (1997) 225 [arXiv:hep-ex/9708028].
- G. Abbiendi *et al.* [OPAL Collaboration], Eur. Phys. J. C 18 (2000) 15 [arXiv:hep-ex/0007018].
- R. Barate *et al.* [ALEPH Collaboration], Phys. Lett. B 458 (1999) 152.
- A. Heister *et al.* [ALEPH Collaboration], Eur. Phys. J. C 30 (2003) 145.
- P. Abreu *et al.* [DELPHI Collaboration], Z. Phys. C 69 (1996) 223.
- T. Sasaki *et al.* [AMY Collaboration], Phys. Lett. B 252 (1990) 491.
- S. K. Sahu *et al.* [AMY Collaboration], Phys. Lett. B 346 (1995) 208.

# Used Publications III

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## Photon (continued):

- T. Kojima *et al.* [AMY Collaboration], Phys. Lett. B 400 (1997) 395.
- K. Muramatsu *et al.* [TOPAZ Collaboration], Phys. Lett. B 332 (1994) 477.
- M. Althoff *et al.* [TASSO Collaboration], Z. Phys. C 31 (1986) 527.
- W. Bartel *et al.* [JADE Collaboration], Z. Phys. C 24 (1984) 231.
- W. Bartel *et al.* [JADE Collaboration], Phys. Lett. B 121 (1983) 203.
- C. Berger *et al.* [PLUTO Collaboration], Phys. Lett. B 142 (1984) 111.
- C. Berger *et al.* [PLUTO Collaboration], Nucl. Phys. B 281 (1987) 365.
- H. Aihara *et al.* [TPC/Two Gamma Collaboration], Z. Phys. C 34 (1987) 1.
- H. Aihara *et al.* [TPC/Two Gamma Collaboration], Phys. Rev. Lett. 58 (1987) 97.

# Used Publications IV

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## Charm Structure Function:

- C. Adloff *et al.* [H1 Collaboration], Phys. Lett. B 528 (2002) 199 [arXiv:hep-ex/0108039].
- F. D. Aaron *et al.* [H1 Collaboration], Eur. Phys. J. C 65 (2010) 89 [arXiv:0907.2643 [hep-ex]].
- S. Chekanov *et al.* [ZEUS Collaboration], Phys. Rev. D 69 (2004) 012004 [arXiv:hep-ex/0308068].
- A. Aktas *et al.* [H1 Collaboration], Eur. Phys. J. C 40 (2005) 349 [arXiv:hep-ex/0411046].
- A. Aktas *et al.* [H1 Collaboration], Eur. Phys. J. C 45 (2006) 23 [arXiv:hep-ex/0507081].
- J. J. Aubert *et al.* [European Muon Collaboration], Nucl. Phys. B 213 (1983) 31.