

Amplitude for production

$$\gamma p \rightarrow \gamma^* p$$

Cross section for

$$\gamma p \rightarrow l^+ l^- p$$

Diffractive photoproduction of lepton pairs at high energy

Gabriela Ślipek

Institute of Nuclear Physics PAN, Cracow

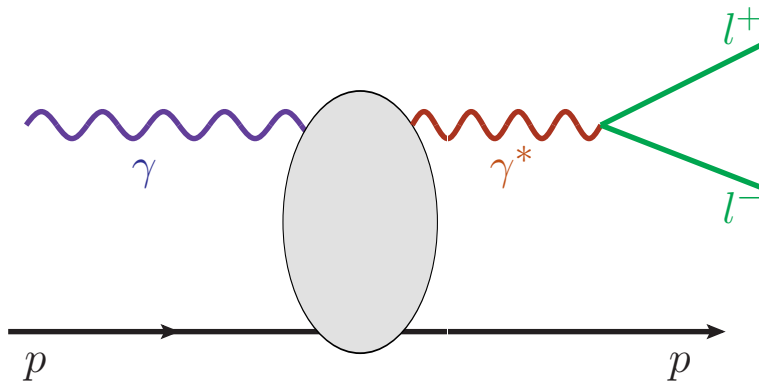
DIS 2010, 19-23 April, Florence

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Cross section for $\gamma p \rightarrow l^+ l^- p$

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in collaboration with W.Schäfer & A.Szczurek

 W. Schäfer, G. Ślipek and A. Szczurek,
arXiv:1003.0610 [hep-ph], in print in Phys. Lett. B.

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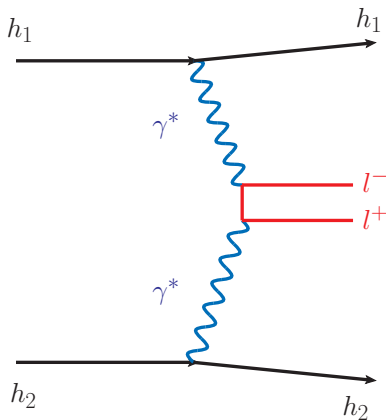
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- The QED process $pp \rightarrow pl^+l^-p$ is important for measuring the luminosity at LHC.



It is therefore important to estimate non-QED contributions to exclusive l^+l^- production.

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It is therefore important to estimate non-QED contributions to exclusive l^+l^- production.
- $VM(\text{vector meson}) \rightarrow e^+e^-$ decays is not the only source of leptons

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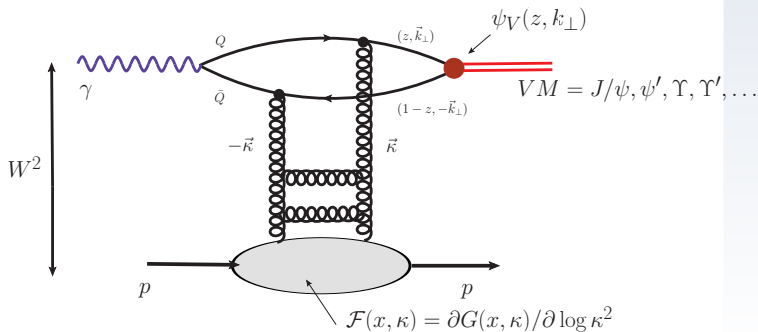
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- $VM(\text{vector meson}) \rightarrow e^+e^-$ decays is not the only source of leptons
- formalism of VM photoproduction has been worked out recently
 -  W.Schäfer and A. Szczurek Phys. Rev. D **76**, 094014 (2007).
 -  A. Rybarska, W. Schäfer and A. Szczurek, Phys. Lett. B **668** (2008) 126.

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- very much the same formalism applies to $\gamma p \rightarrow l^+l^-p$ via timelike Compton scattering

Hadroproduction

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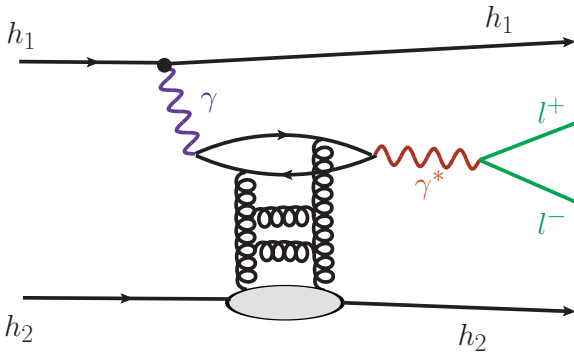
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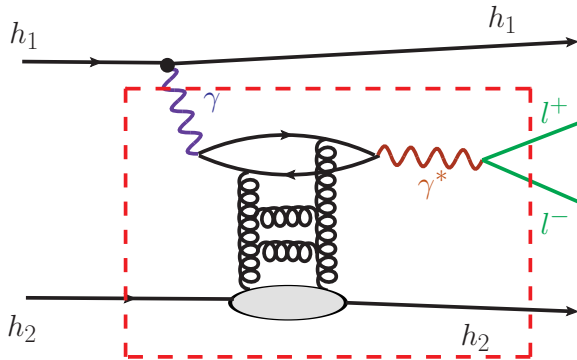
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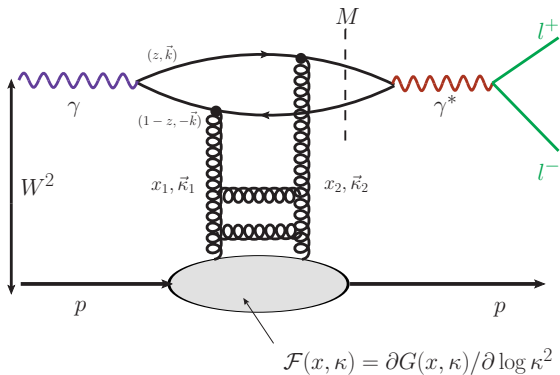
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Forward amplitude for production $\gamma p \rightarrow \gamma^* p$

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$$\mathcal{M} = \sum_f \mathcal{M}_f$$

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$$\mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2)p) = W^2 4\pi\alpha_{\text{em}} e_f^2 2 \cdot 2 \int_0^{1/2} \frac{dz}{z(1-z)} \int_0^\infty \pi dk^2 \frac{\mathcal{A}_f(z, k^2, W^2)}{\left[\frac{k^2 + m_f^2}{z(1-z)} - q^2 - i\varepsilon \right]},$$

where

- $\mathcal{A}_f(z, k^2)$ - glue convolution \rightarrow see next page

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- $\mathcal{A}_f(z, k^2)$ - glue convolution \rightarrow see next page
- z -longitudinal momentum fraction of quark in the photon

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where

- $\mathcal{A}_f(z, k^2)$ - glue convolution \rightarrow see next page
- z -longitudinal momentum fraction of quark in the photon
- k -transverse momentum of the quark
- $M^2 = \frac{k^2 + m_f^2}{z(1-z)}$ -invariant mass of $q\bar{q}$ pair

\mathcal{A}_f - function

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$$\mathcal{A}_f(z, k^2) = \pi \int_0^\infty \frac{\pi d\kappa^2}{\kappa^4} \alpha_s(q^2) \mathcal{F}(x, \kappa^2)$$
$$\left[A_{0f}(z, k^2) W_{0f}(k^2, \kappa^2) + A_{1f}(z, k^2) W_{1f}(k^2, \kappa^2) \right]$$

\mathcal{A}_f - function

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$$A_{0f}(z, k^2) = m_f^2$$

$$A_{1f}(z, k^2) = [z^2 + (1-z)^2] \frac{k^2}{k^2 + m_f^2}$$

$$W_{01}(k^2, \kappa^2) = \frac{1}{k^2 + m_f^2} - \frac{1}{\sqrt{(k^2 - m_f^2 - \kappa^2)^2 + 4m_f^2 k^2}}$$

$$W_{1f}(k^2, \kappa^2) = 1 - \frac{k^2 + m_f^2}{2k^2} \left(1 + \frac{k^2 - m_f^2 - \kappa^2}{\sqrt{(k^2 - m_f^2 - \kappa^2)^2 + 4m_f^2 k^2}} \right)$$

$$\mathcal{A}_f(z, k^2) = \pi \int_0^\infty \frac{\pi d\kappa^2}{\kappa^4} \alpha_s(q^2) \mathcal{F}(x, \kappa^2)$$
$$\left[A_{0f}(z, k^2) W_{0f}(k^2, \kappa^2) + A_{1f}(z, k^2) W_{1f}(k^2, \kappa^2) \right]$$

- $\mathcal{F}(x, \kappa^2) = \frac{\partial G(x, \kappa^2)}{\partial \log \kappa^2}$ - unintegrated gluon distribution
- $x = \frac{M^2}{W^2}$ - longitudinal momentum fraction of the gluon
- κ^2 - transverse momentum of the gluon

\mathcal{A}_f - function

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Cross section for

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$$(z, k^2) \rightarrow (M^2, k^2)$$

$$\mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2)p) = W^2 16\pi^2 \alpha_{\text{em}} e_f^2 \cdot$$

$$\int_{4m_f^2}^{\infty} \frac{a_f(W^2, M^2)}{M^2 - q^2 - i\epsilon} dM^2.$$

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spectral density

$$a_f(W^2, M^2) = \int_0^{\frac{1}{4}M^2 - m_f^2} \frac{dk^2}{J_f} \mathcal{A}_f(M^2, k^2, W^2)$$

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Spectral density

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spectral density

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$$J_f = \sqrt{1 - 4 \left(\frac{k^2 + m_f^2}{M^2} \right)}$$

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non-forward amplitude

$$\mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2) p; t) = \mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2) p) \exp[Bt]$$

Cross section for $\gamma p \rightarrow l^+ l^- p$

non-forward amplitude

$$\mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2)p; t) = \mathcal{M}_f(\gamma p \rightarrow \gamma^*(q^2)p) \exp[Bt]$$

$$\sigma(\gamma p \rightarrow \gamma^* p) = \frac{(\Re \frac{\mathcal{M}}{W^2})^2 + (\Im \frac{\mathcal{M}}{W^2})^2}{16\pi\mathcal{B}}$$

Cross section for $\gamma p \rightarrow l^+ l^- p$

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$$\frac{d\sigma}{dq^2}(\gamma p \rightarrow l^+ l^- p) = \frac{\alpha_{em}}{3\pi q^2} \sigma(\gamma p \rightarrow \gamma^* p)$$

Cross section for $\gamma p \rightarrow l^+ l^- p$

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- $\mathcal{M} = \sum_f \mathcal{M}_f$
- \mathcal{B} - slope parameter
- q^2 - invariant mass of $l^+ l^-$

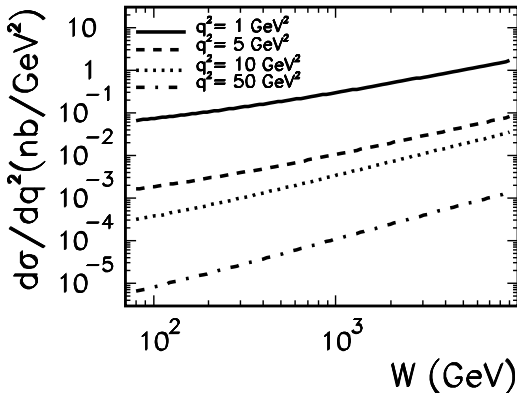
$d\sigma/dq^2$ as a function of γp cm energy

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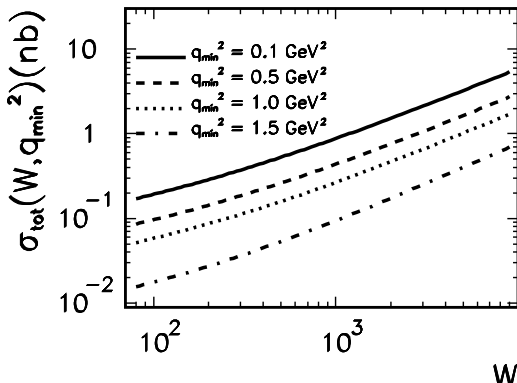
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$$\gamma p \rightarrow l^+ l^- p$$

Energy dependence



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$$\sigma_{tot}(\gamma p \rightarrow l^+ l^- p; q_{min}^2) = \int_{q_{min}^2}^{\infty} \frac{d\sigma}{dq^2} dq^2$$

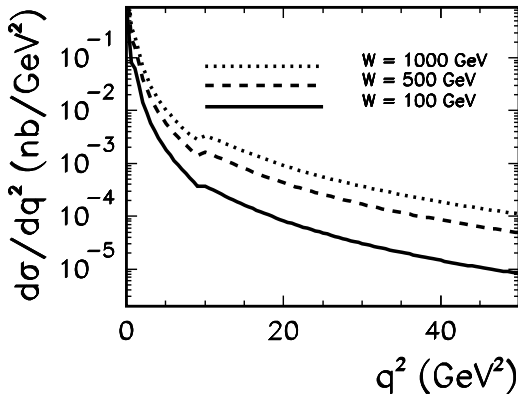
Dependence on dilepton invariant mass

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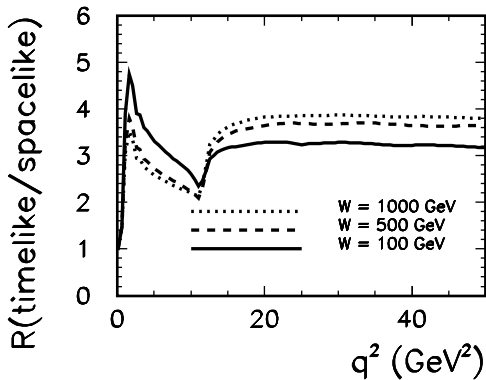


- q^2 - invariant mass of l^+l^-

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timelike

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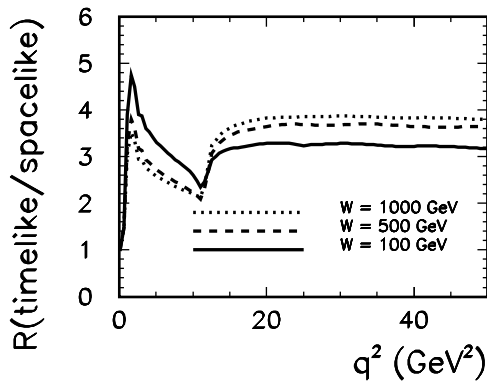
spacelike

$$\mathcal{M}_f = W^2 16\pi^2 \alpha_{\text{em}} e_f^2 \cdot \int_{4m_f^2}^{\infty} \frac{a_f(W^2, M^2)}{M^2 + q^2} dM^2.$$

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- Amplitude for the $\gamma p \rightarrow \gamma^* p$ has been derived in the k_t - factorization approach.
- I have presented results for exclusive photoproduction of lepton pairs (energy and q dependences).
- I have done calculations assuming time-like photons instead of space-like photons as wrongly done in the literature. This leads to an enhancement of the cross section compared to earlier estimates.
- Future: go to hadroproduction and see what is background to the QED process (luminosity monitor).

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