

# Fluctuations and Saturation in Diffractive Excitation



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# Content

1. Diffractive excitation often treated by two mechanisms:
  - a) Low mass: Good–Walker
  - b) High mass: Triple Regge

How are these related?

2. Fluctuations
3. Saturation – “Enhanced diagrams”
4. Bare pomeron in Good–Walker picture



## Eikonal approximation

Diffraction, saturation, and multiple interactions more easily described in impact parameter space

Convolution in transv. mom.  $\sim$  Multiplication in **b**-space

Scattering driven by absorption into inelastic states  $i$ , with weights  $2f_i$

$\Rightarrow$  Elastic amplitude  $T = 1 - e^{-F}$ , with  $F = \sum f_i$

For a structureless projectile we find:

$$\begin{cases} d\sigma_{tot}/d^2b \sim \langle 2T \rangle \\ \sigma_{el}/d^2b \sim \langle T \rangle^2 \\ \sigma_{inel}/d^2b \sim \langle 1 - e^{-\sum 2f_i} \rangle = \sigma_{tot} - \sigma_{el} \end{cases}$$



## Good - Walker

If the projectile has an **internal structure**, the mass eigenstates can differ from the eigenstates of diffraction

Diffractive eigenstates:  $\Phi_n$ ; Eigenvalue:  $T_n$

Mass eigenstates:  $\Psi_k = \sum_n c_{kn} \Phi_n$  ( $\Psi_{in} = \Psi_1$ )

Elastic amplitude:  $\langle \Psi_1 | T | \Psi_1 \rangle = \sum c_{1n}^2 T_n = \langle T \rangle$

$$d\sigma_{el}/d^2b \sim (\sum c_{1n}^2 T_n)^2 = \langle T \rangle^2$$

Amplitude for diffractive transition to mass eigenstate  $\Psi_k$ :

$$\langle \Psi_k | T | \Psi_1 \rangle = \sum_n c_{kn} T_n c_{1n}$$

$$d\sigma_{diff}/d^2b = \sum_k \langle \Psi_1 | T | \Psi_k \rangle \langle \Psi_k | T | \Psi_1 \rangle = \langle T^2 \rangle$$

Diffractive excitation determined by the fluctuations:

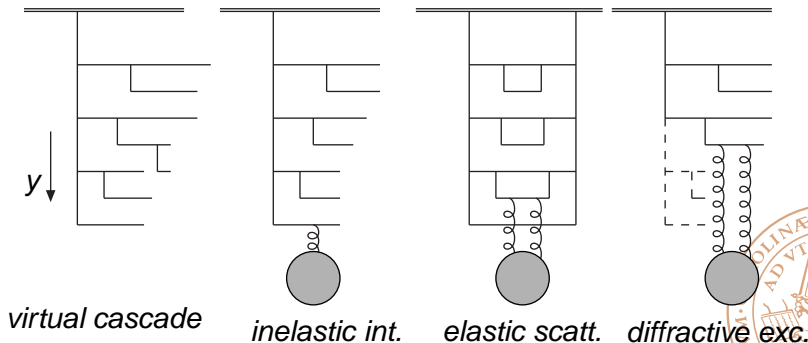
$$d\sigma_{diff\ ex}/d^2b = d\sigma_{diff} - d\sigma_{el} = \langle T^2 \rangle - \langle T \rangle^2$$



## What are the diffractive eigenstates?

Miettinen–Pumplin (1978), Hatta *et al.* (2006)

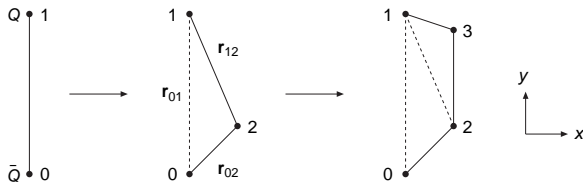
Parton cascades, which can come on shell through interaction with the target



# Dipole cascade models

## Mueller Dipole Model

Evolution in transverse coordinate space



Emission probability:  $\frac{dP}{dy} = \frac{\bar{\alpha}}{2\pi} d^2\mathbf{r}_2 \frac{r_{01}^2}{r_{02}^2 r_{12}^2}$

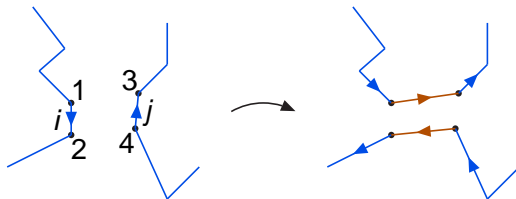
Color screening: Suppression of large dipoles

~ suppression of small  $k_{\perp}$  in BFKL



## Dipole-dipole scattering

Single gluon exchange  $\Rightarrow$  Color reconnection



Born amplitude: 
$$f_{ij} = \frac{\alpha_s^2}{2} \ln^2 \left( \frac{r_{13} r_{24}}{r_{14} r_{23}} \right)$$

Reproduces LL BFKL



# Lund Dipole Cascade model<sup>1</sup>

The Lund model is a generalization of Mueller's dipole model, with the following improvements:

- ▶ Include NLL BFKL effects
- ▶ Include Nonlinear effects in evolution
- ▶ Include Confinement effects

MC: DIPSY

Initial state wavefunctions:

$\gamma^*$ : Given by perturbative QCD.  $\Psi_{T,L}(r, z; Q^2)$

**proton**: Dipole triangle

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<sup>1</sup>E. Avsar-Flensburg-GG-Lönblad

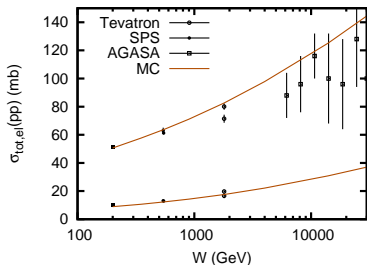




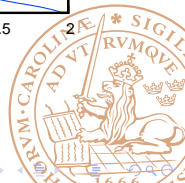
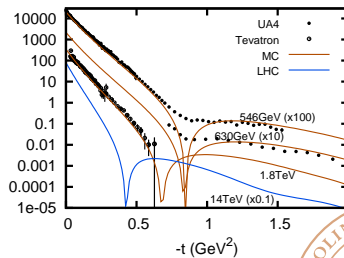
# Total and elastic cross sections

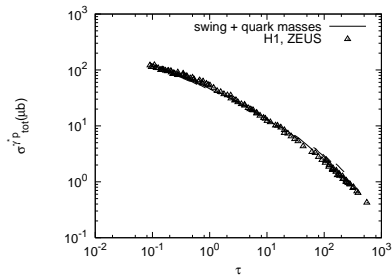
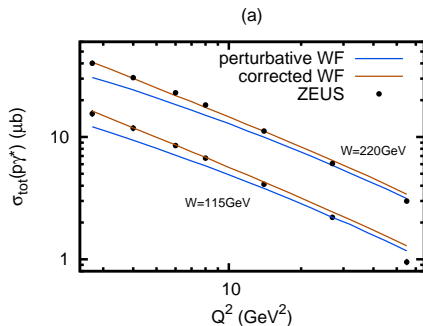
*pp*

$\sigma_{tot}$  and  $\sigma_{el}$



$d\sigma/dt$



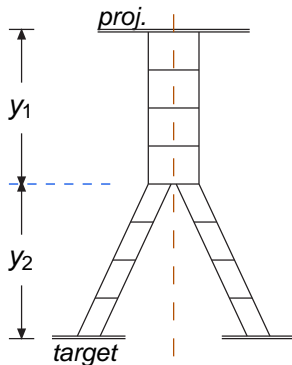
$\gamma^* p$ 

Satisfies geometric scaling



# Diffractive cross sections

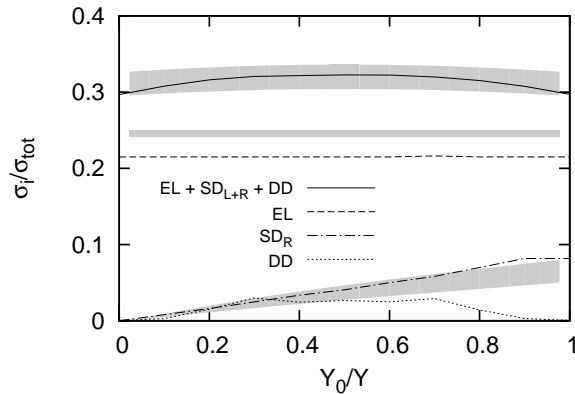
## Relation Good-Walker — Triple Regge

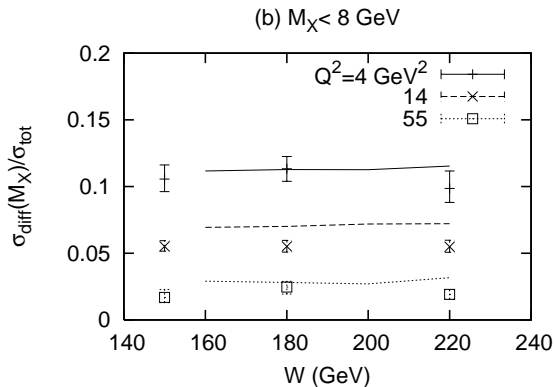


$\langle\langle T \rangle_{\text{targ}}^2 \rangle_{\text{proj}}$  gives diffractive scattering with  $M_X^2 < \exp(y_1)$

Vary  $y_1$  gives  $d\sigma/dM_X^2$



$pp$  1.8 TeV

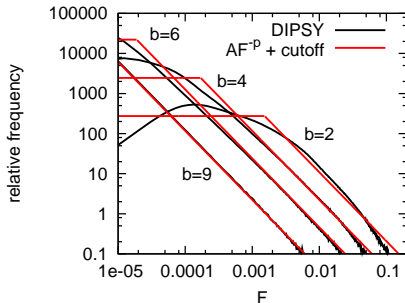
$\gamma^* p$ Example  $M_X < 8$  GeV,  $Q^2 = 4, 14, 55$  GeV<sup>2</sup>.

# What is the nature of the fluctuations?

$$\gamma^* p: \quad \frac{dP}{dF} \approx A F^{-p} \quad (\text{with cutoff for small } F\text{-values})$$

$$\Rightarrow d\sigma_{\text{diff.ex.}} \approx (1 - 1/2^{2-p}) \cdot d\sigma_{\text{tot}}$$

$$W = 220 \quad Q^2 = 14$$

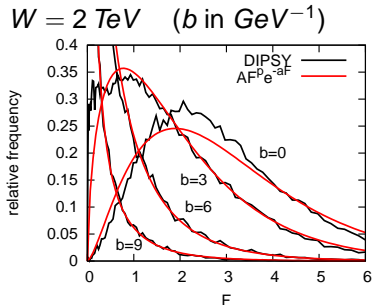
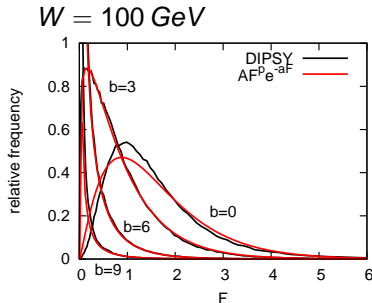


The power  $p$  is independent of  $b$  (but grows slowly with  $Q^2$ )

$\frac{\sigma_{\text{diff}}}{\sigma_{\text{tot}}} \sim 0.18$  for  $Q^2 = 14 \text{ GeV}^2$  falling to  $\sim 0.13$  at  $Q^2 = 50 \text{ GeV}^2$

*pp*: Born approximation large. Distribution

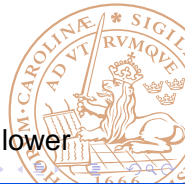
$$\frac{dP}{dF} \approx A F^p e^{-aF}$$



$a$  is independent of  $b$  (but falling with energy),

$$\frac{d\sigma_{d.ex.}}{d\sigma_{tot}} = \frac{1}{2a} \sim 0.35 \text{ for } W = 100 \text{ GeV}$$

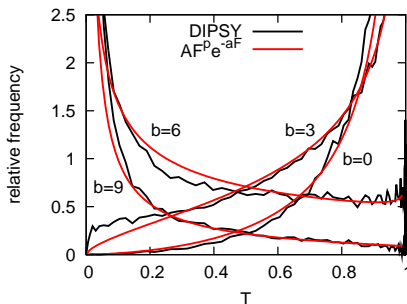
The variance in the **Born amplitude** is similar to  $\gamma^* p$  for lower  $Q^2$ -values



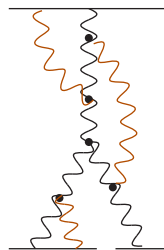
## Saturation reduces the fluctuations

$\langle F \rangle$  is large  $\Rightarrow$  Unitarity effects important

$T$ -distribution,  $W = 2$  TeV



“Enhanced diagrams”



Saturation  $\Rightarrow$  Factorization breaking in diffractive excitation



# Impact parameter profile

Central collisions:

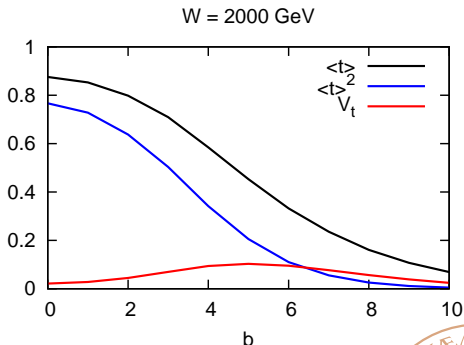
$\langle T \rangle$  large  $\Rightarrow$

Fluctuations small

Peripheral collisions:

$\langle T \rangle$  small  $\Rightarrow$

Fluctuations small



Largest fluctuations when  $\langle F \rangle \sim 1$  and  $\langle T \rangle \sim 0.5$

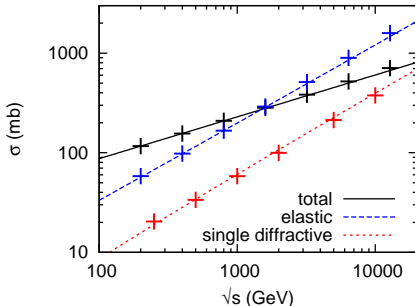
Circular ring expanding to larger radius at higher energy



# Relation Good-Walker — Triple-Regge

*BARE* pomeron without saturation effects

Total, elastic and singlet diffractive cross sections



Lines are triple-Regge fit with a single pomeron pole

$$\alpha(0) = 1.21, \quad \alpha' = 0.2 \text{ GeV}^{-2}$$

$$g_{pP}(t) = (5.6 \text{ GeV}^{-1}) e^{1.9t}, \quad g_{3P}(t) = 0.31 \text{ GeV}^{-1}$$



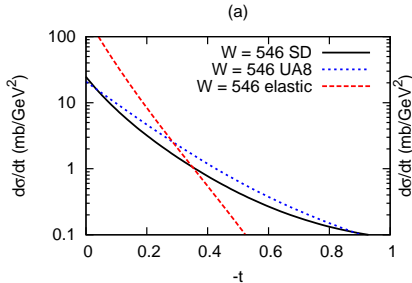
# Summary

- ▶ In the eikonal approximation diffractive excitation is directly determined by the **fluctuations** in the scattering process
- ▶ The Lund Dipole Cascade Model can describe  $pp$  and  $\gamma^*p$  total, elastic, and **diffr. exc. to small and large masses**
- ▶ The fluctuations in the cascade evolutions are **large**
- ▶  $\Rightarrow$  Diffractive excitation is **large in  $\gamma^*p$  collisions**
- ▶ In  $pp$  the fluctuations are large for the Born amplitudes, but strongly **suppressed by unitarity** above  $\sim 20$  GeV
- ▶ Diffr. exc. in  $pp$  is an expanding ring in  $b$ -space
- ▶ Neglecting saturation, the dipole model reproduces the triple-Regge result for a **bare pomeron**, which is a simple pole with  $\alpha(0) = 1.21$  and  $\alpha' = 0.2$   
(With saturation the cross section grows  $\sim s^{0.1}$  up to  $\sim 50$  TeV)

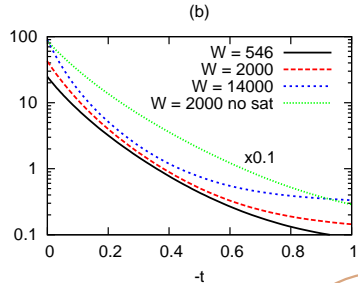


## Extra slides

### $t$ -dependence for single diffraction



546 GeV compared with  
 a fit to UA8 data, and with  
 elastic scattering

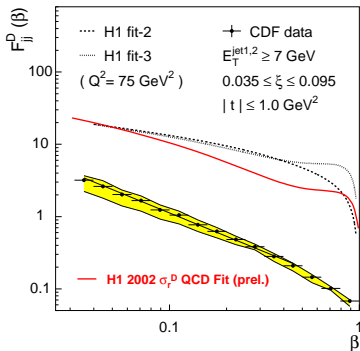


Energy dependence, and  
 result without saturation  
 at 2 TeV



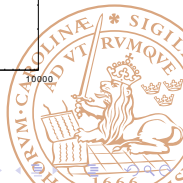
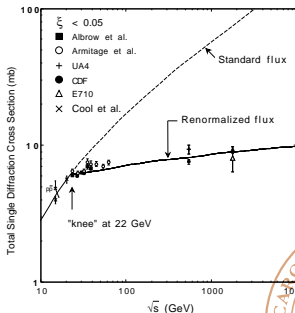
## Factorization breaking

Difference between  
 $pp$  and  $\gamma^*p$



Cf. Goulianos' saturation of  
 pomeron flux

$pp$  scattering



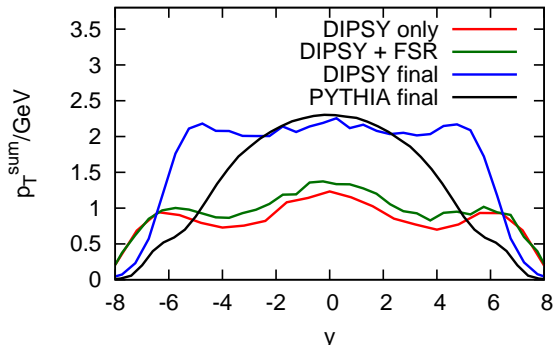
## Final states

Remove branches which have not interacted. What is left corresponds to “ $k_{\perp}$ -changing emissions”

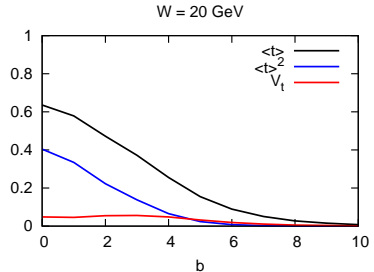
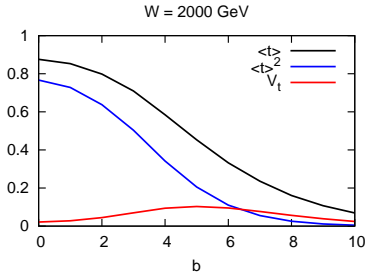
Add final state radiation and hadronization

Very preliminary result:

$W = 2000 \text{ GeV}$



## Impact parameter profile



As observed earlier, **diffractive excitation is a peripheral process**

Circular ring expanding to larger radius at higher energy.

**Extrapolate to smaller energy  $\Rightarrow$**

**The hole closed for  $W \sim 20$  GeV. Agrees with Goulios estimate!**



## Diffractive final states

Coherence effects important for subtracting el. scatt.

$$d\sigma_n = c_n^2 \left( \sum_m d_m^2 t_{nm} - \langle t \rangle \right)^2$$

$$\langle t \rangle = \sum_n \sum_m c_n^2 d_m^2 t_{nm}$$





## Toy model

(Abelian emissions; no saturation)

$$\Psi_{in} = \prod_i (\alpha_i + \beta_i) |0\rangle$$

parton  $i$  produced with prob.  $|\beta_i|^2$ , interacts with weight  $f_i$

Diff. exc. states:

$$\Psi_j = (-\beta_j + \alpha_j) \prod_{i \neq j} (\alpha_i + \beta_i) |0\rangle$$

$$d\sigma_{el} \sim (\sum_i \beta_i^2 f_i)^2$$

$$d\sigma_j \sim \alpha_j^2 \beta_j^2 f_j^2$$



## $pp$ scattering

$$\langle t \rangle = 1 - \left(\frac{a}{a+1}\right)^{p+1} = 1 - \left(\frac{a}{a+1}\right)^{a\langle f \rangle} \rightarrow 1 \text{ when } \langle f \rangle \rightarrow \infty$$

$$V_t = \left(\frac{a}{a+2}\right)^{p+1} - \left(\frac{a}{a+1}\right)^{2p+2} \rightarrow 0 \text{ when } \langle f \rangle \rightarrow \infty$$

