

# Investigation of different $b^*$ prescriptions in SCETlib.

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SCETlib: Markus Ebert, Johannes Michel, FT



$$\frac{d\sigma}{dp_T} = \int_0^\infty db_T J_0(p_T b_T) p_T b_T \tilde{\sigma}[b_T, \mu_i(\dots)]$$

- One always resums ratio of high scale  $\sim Q$  / low scales  $\sim 1/b_T \sim p_T$
- Canonical logs are resummed by canonical scale choices

$$\mu_H = \nu_B = Q, \quad \mu_B = \mu_S = \nu_S = b_0/b_T$$

- $\alpha_s$  appears at  $\alpha_s(\mu_H)$ ,  $\alpha_s(\mu_B)$ ,  $\alpha_s(\mu_S)$ , PDFs appear at  $f_i(\mu_B)$ 
  - ▶ Encounter Landau pole for  $b_0/b_T < 1 \text{ GeV}$
  - ▶ This is actually *not* an artifact of  $b_T$ -space evolution or scale setting, it's a physical effect signifying sensitivity to nonperturbative effects (analogous effect also appears in exact  $p_T$ -space evolution [Ebert, FT, 1611.08610])

# $b^*$ Prescription(s).

Basic idea: Replace

$$b_T \rightarrow b^*(b_T) = \frac{b_T}{\sqrt{1 + (b_T/b_{\max})^2}} \Rightarrow \begin{cases} b^*(b_T \rightarrow 0) \rightarrow b_T \\ b^*(b_T \rightarrow \infty) \rightarrow b_{\max} \end{cases}$$

- $b_0/b^*(b_T \rightarrow \infty) \rightarrow b_0/b_{\max}$ , so take  $b_0/b_{\max} \sim 1 \text{ GeV}$  as cutoff

Different options:

- “Global  $b^*$ ”: original, most often used

$$\tilde{\sigma}(b_T) \equiv \tilde{\sigma}[b_T, \mu_i(b_T)] \rightarrow \tilde{\sigma}(b^*) \equiv \tilde{\sigma}[b^*, \mu_i(b^*)]$$

- “Local  $b^*$ ”: when keeping all RGE scales explicit

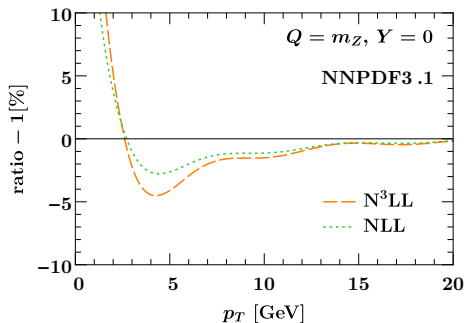
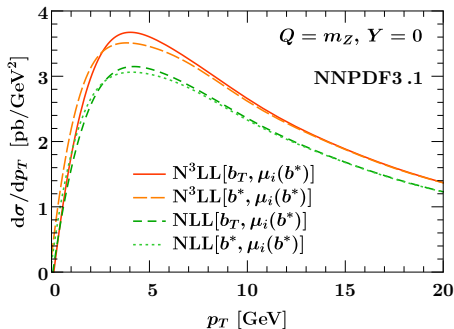
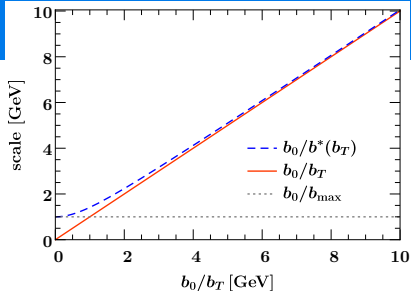
[for more details see Lusterans, Michel, FT, Waalewijn, 1901.03331]

$$\tilde{\sigma}[b_T, \mu_i(b_T)] \rightarrow \tilde{\sigma}[b_T, \mu_i(b^*)]$$

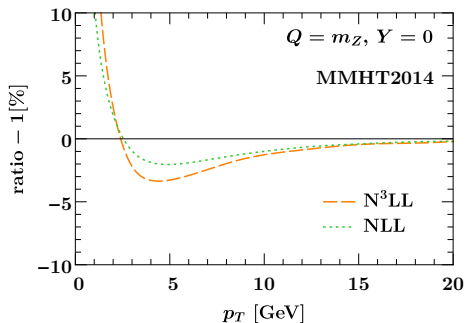
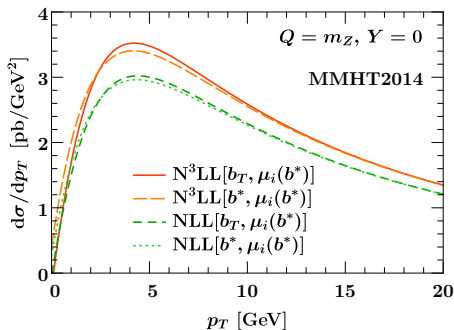
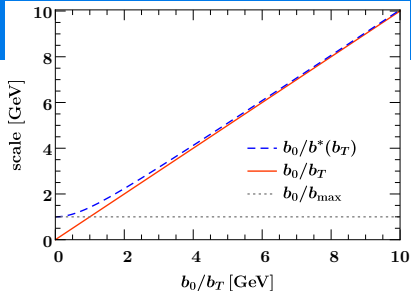
- Intermediate versions are possible as well

- ▶ All amount to factorizing pert. from nonpert. contributions, “ad-hocness” introduced in pert. prediction is cancelled by nonpert. completion

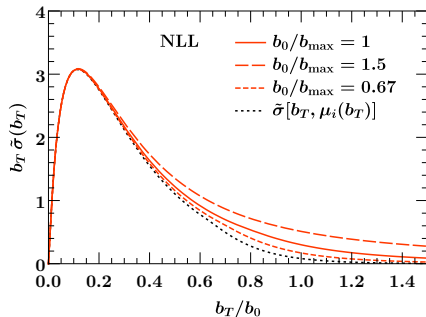
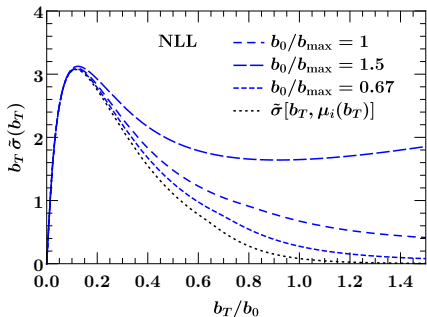
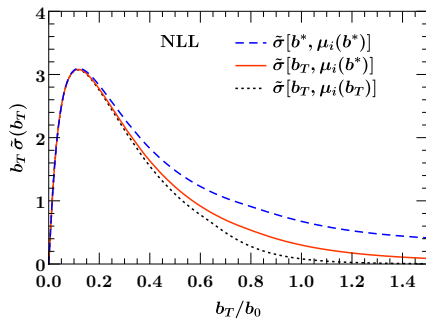
# Comparison in $p_T$ space.



# Comparison in $p_T$ space.



# Comparison in $b_T$ space.



# Comparison in $b_T$ space.

