

Axions/ALPs as DM and/or as DM Mediators: Phenomenology

Andreas Ringwald
FIPs 2020
Virtual Workshop
31 Aug - 04 Sep 2020



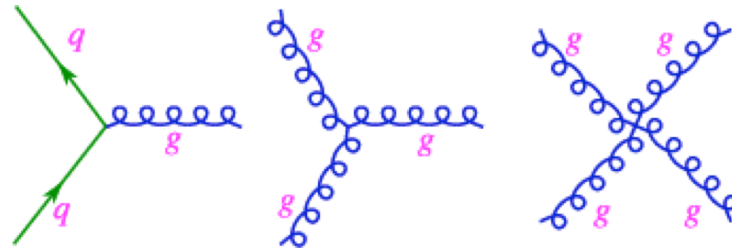
Strong CP Puzzle

Theta term in Quantum Chromodynamics

- Quantum Chromodynamics (QCD):

[Gross,Wilczek 73;Politzer 73; Fritzsche,Gell-Mann,Leutwyler 73]

$$S_{\text{QCD}} = \int d^4x \left\{ \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} \right\}$$



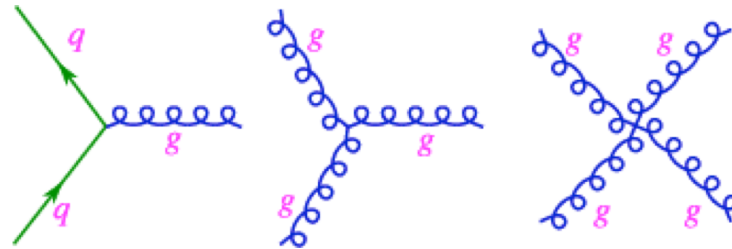
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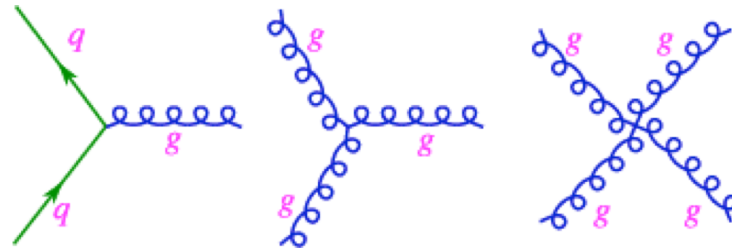
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$$\int d^4x \partial_\mu J_{\text{CS}}^\mu = 0, \pm 1, \pm 2, \dots$$

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- Topological theta term $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$
violates T and P, and thus CP

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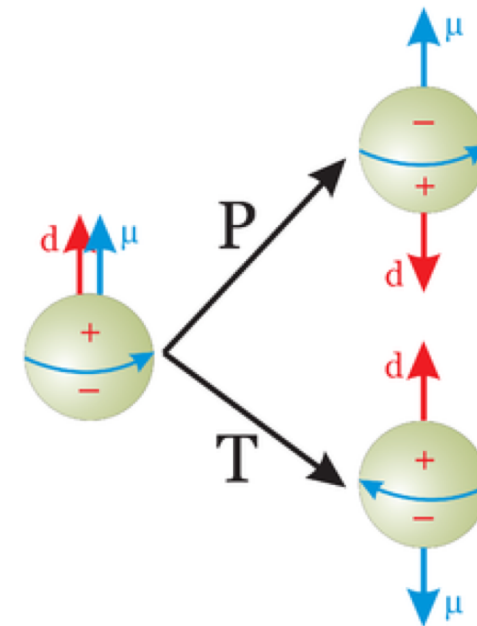
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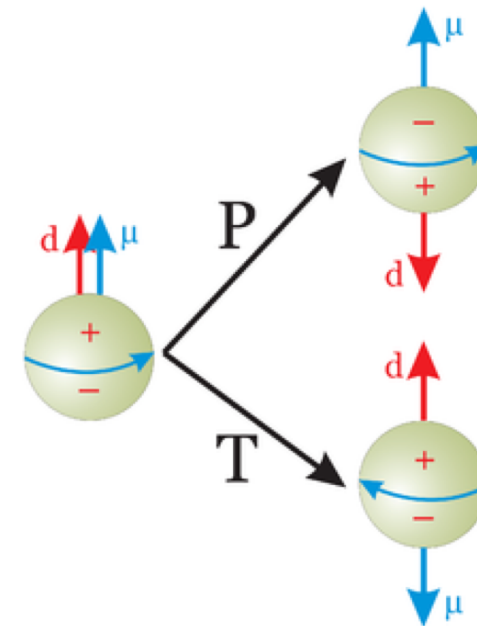
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$$d_n(\bar{\theta}) = 2.4(1.0) \times 10^{-16} \bar{\theta} e \text{ cm}$$



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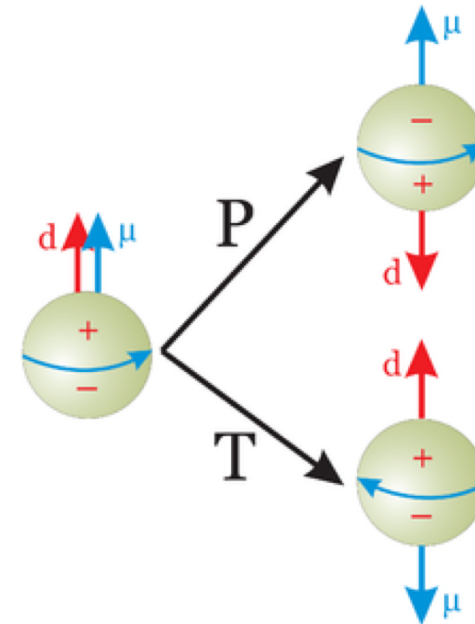
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$$d_n(\bar{\theta}) = 2.4(1.0) \times 10^{-16} \bar{\theta} e \text{ cm}$$

- Experiment: [Abel et al. 20]

$$|d_n| < 1.8 \times 10^{-26} e \text{ cm}$$

$$\Rightarrow |\bar{\theta}| < 10^{-10}$$



Axionic Solution of Strong CP Puzzle

In a nutshell: replace theta parameter by dynamical theta field

- Add to SM Nambu-Goldstone field, $\theta(x) \equiv A(x)/f_A \in [-\pi, \pi]$, respecting a non-linearly realized $U(1)_{\text{PQ}}$ symmetry ($\theta(x) \rightarrow \theta(x) + \text{const.}$), broken by coupling to gluonic topological charge density: [\[Peccei,Quinn 77\]](#)

$$\mathcal{L} \supset -\theta(x) q(x); \quad q(x) \equiv \frac{\alpha_s}{8\pi} G_{\mu\nu}^b(x) \tilde{G}^{b,\mu\nu}(x)$$

- Can eliminate QCD $\bar{\theta}$ -parameter

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} [\bar{\theta} + \theta(x)] G_{\mu\nu}^b \tilde{G}^{b,\mu\nu}$$

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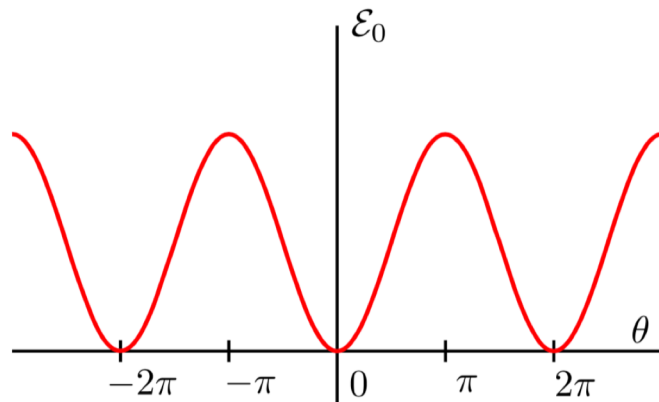
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- Effective potential at energies below Λ_{QCD} has absolute minimum at $\theta = 0$ and thus predicts vanishing vev, $\langle \theta(x) \rangle = 0$ [Vafa,Witten 84]
No strong CP violation in vacuum



$$V(\theta) = \Sigma (m_u + m_d) \left(1 - \frac{\sqrt{m_u^2 + m_d^2 + 2m_u m_d \cos \theta}}{m_u + m_d} \right)$$

$$\Sigma \equiv -\langle \bar{u}u \rangle = -\langle \bar{d}d \rangle$$

[Di Vecchia,Veneziano '80;
Leutwyler,Smilga 92]

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No strong CP violation in vacuum [Vafa,Witten 84]
- Particle excitation: pseudo Nambu-Goldstone boson “axion” [Weinberg 78; Wilczek 78]
- Topological susceptibility in QCD, $\chi \equiv \int d^4x \langle q(x)q(0) \rangle$, determines mass in units of decay constant: $m_A = \sqrt{\chi}/f_A$
- Recent precise determination (ChPT; lattice QCD):

$$m_A = 5.691(51) \left(\frac{10^9 \text{ GeV}}{f_A} \right) \text{ meV}$$

[Grilli di Cortona et al. `16;
Borsanyi et al. `16;
Gorghetto, Villadoro `19]

Peccei-Quinn Extension of Standard Model

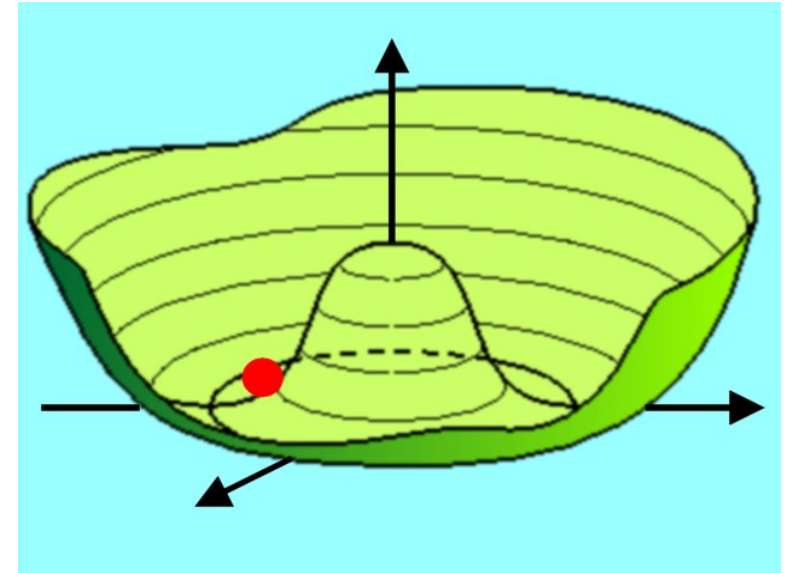
Simple way to get dynamical theta field

- Add singlet complex scalar field σ , featuring a spontaneously broken global $U(1)_{\text{PQ}}$ symmetry

- Particle excitations:

$$\sigma(x) = \frac{1}{\sqrt{2}} (v_{\text{PQ}} + \rho(x)) e^{iA(x)/v_{\text{PQ}}}$$

- Mass of particle excitation of modulus: $m_\rho \sim v_{\text{PQ}}$
- Mass of particle excitation of phase: $m_A = 0$



[Raffelt]

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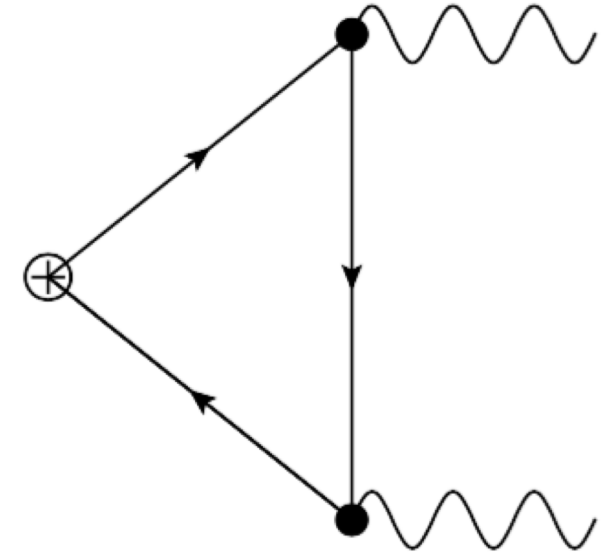
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- Coloured fermions carry PQ charges such that $U(1)_{\text{PQ}}$ is broken due to gluonic triangle anomaly:

$$\partial_\mu J_{U(1)_{\text{PQ}}}^\mu \supset -\frac{\alpha_s}{8\pi} N G_{\mu\nu}^b \tilde{G}^{b,\mu\nu}$$



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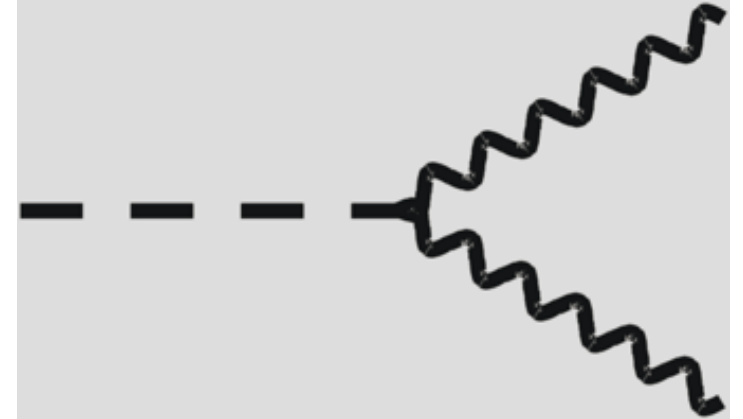
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- Low energy effective field theory at energies above Λ_{QCD} but below v ($\ll v_{\text{PQ}}$): [Peccei,Quinn 77; Weinberg 78; Wilczek 78]

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \theta(x) G_{\mu\nu}^b \tilde{G}^{b,\mu\nu}; \quad \theta(x) = A(x)/f_A; \quad f_A = v_{\text{PQ}}/N$$

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]



Peccei-Quinn Extension of Standard Model

Axion couplings to SM at energies below QCD scale

$$\mathcal{L}_A \supset -\frac{i}{2} \frac{C_{AD}}{f_A} A \bar{\Psi}_N \sigma_{\mu\nu} \gamma_5 \Psi_N F^{\mu\nu} - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\Psi}_f \gamma^\mu \gamma_5 \Psi_f$$

- Couplings to SM suppressed by inverse power of proportional to mass, since

$$f_A = v_{\text{PQ}}/N \gg v = 246 \text{ GeV}$$

$$m_A = 5.691(51) \left(\frac{10^9 \text{ GeV}}{f_A} \right) \text{ meV}$$

- EDM coupling: $C_{AD} = 2.4(1.0) \times 10^{-16} \text{ e cm}$

[Pospelov, Ritz '00]

- Photon coupling: $C_{A\gamma} = \frac{E}{N} - 1.92(4)$

[Kaplan 85; Srednicki '85; Grilli di Cortona et al. '16]

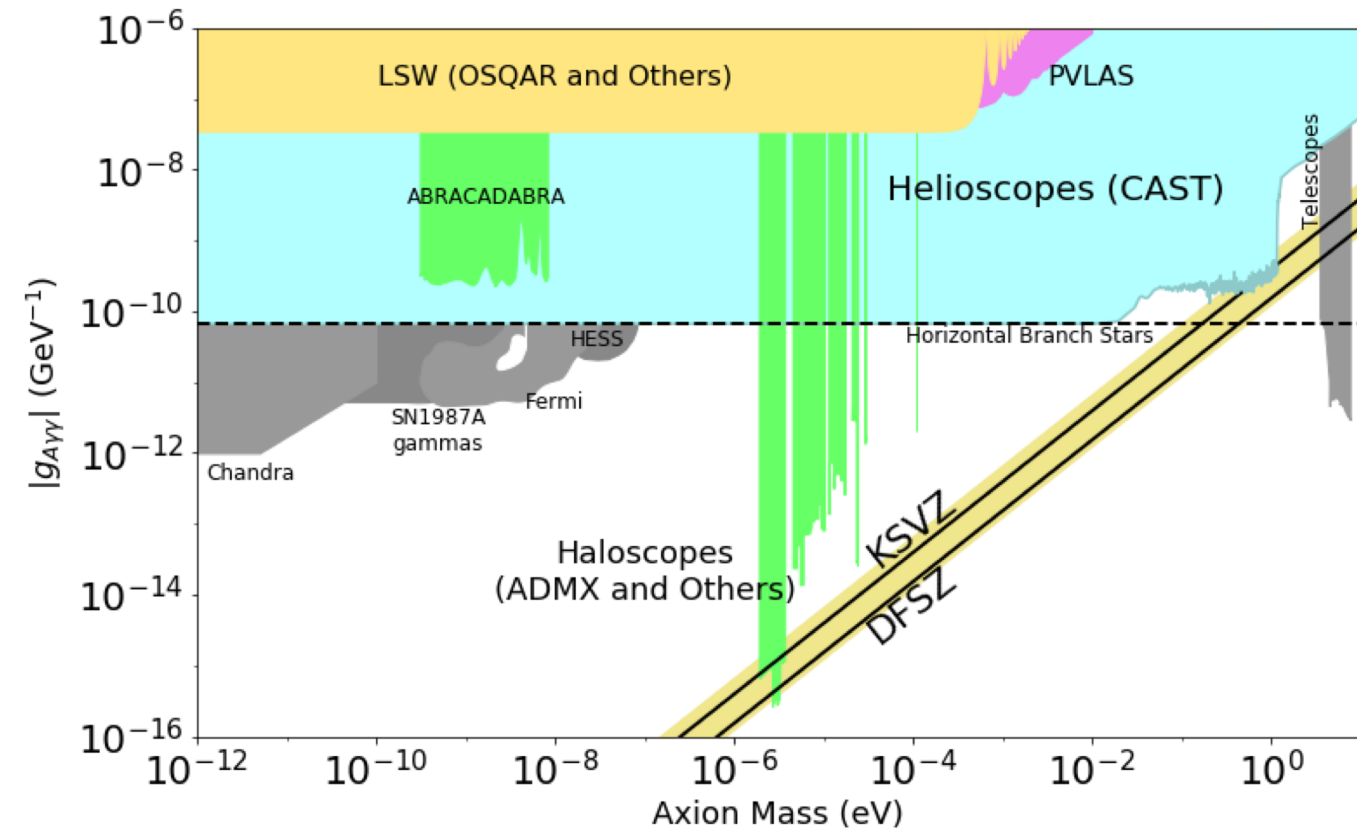
- Nucleon couplings: $C_{Ap} = -0.47(3) + 0.88(3)C_{Au} - 0.39(2)C_{Ad} - 0.038(5)C_{As}$
 $- 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At},$
 $C_{An} = -0.02(3) + 0.88(3)C_{Ad} - 0.39(2)C_{Au} - 0.038(5)C_{As}$
 $- 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At}$

- **Axion-Like Particle (ALP):** PNGB from breaking of another approximate global symmetry, e.g. Majoron, FAMILION, etc.

Constraints on Axion/ALP Couplings

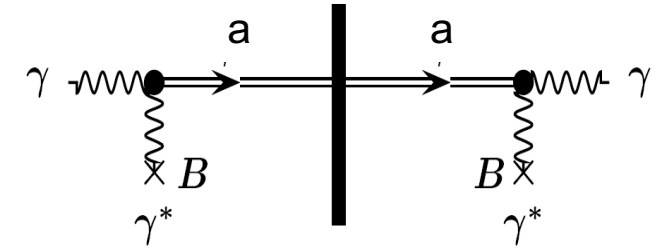
Coupling to the photon

$$g_{A\gamma\gamma} \equiv \frac{\alpha}{2\pi f_A} C_{A\gamma}$$

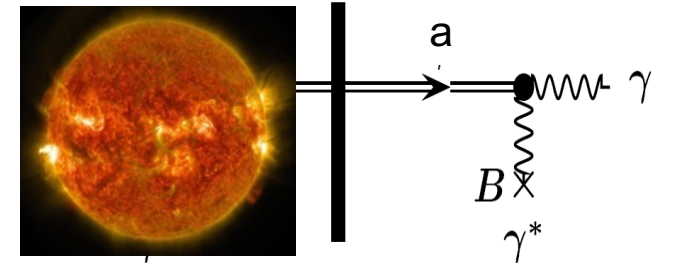


[AR,Rosenberg,Rybka in: Review of Particle Physics, PTEP 2020 (2020) 8, 083C01]

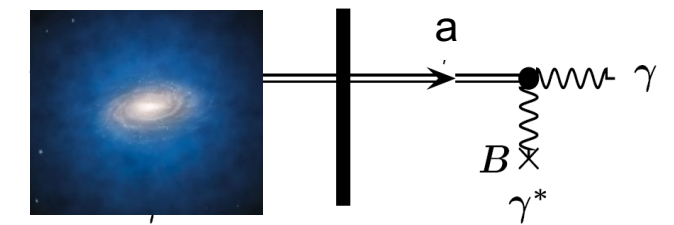
Laser shining through a wall (LSW)



Sun shining through a wall (Helioscope)



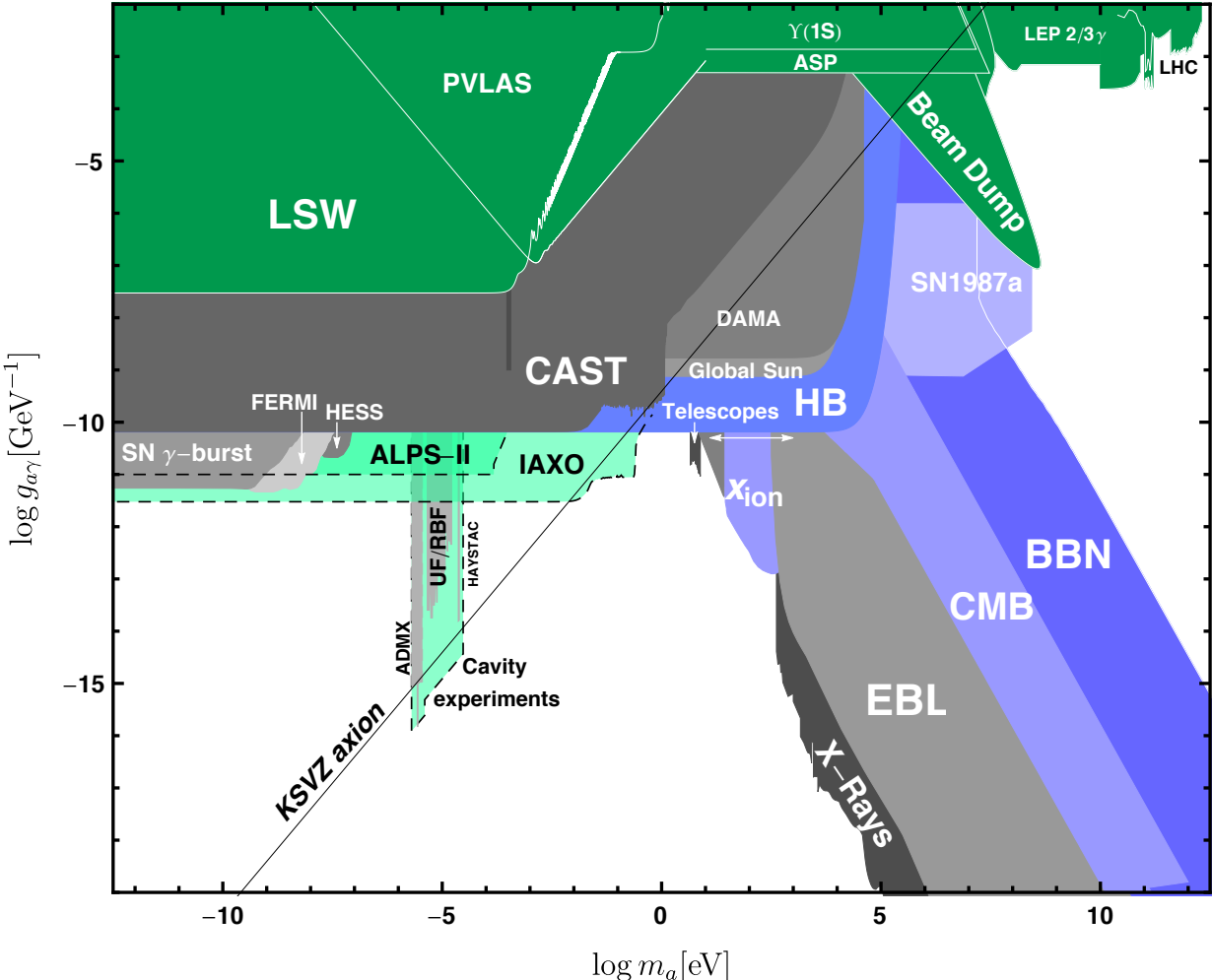
DM shining through a wall (Haloscope)



[Axel Lindner]

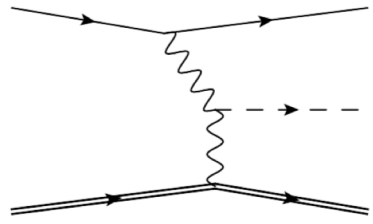
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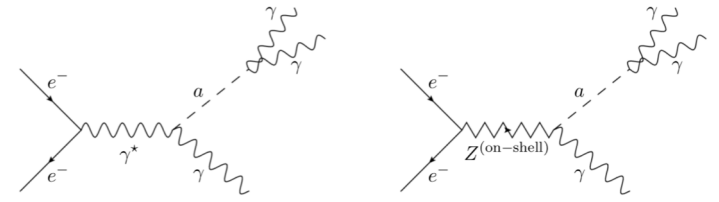


[Brun et al. [MADMAX], 1901.07401]

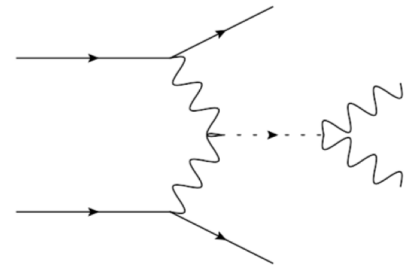
- Beam dumps



- LEP



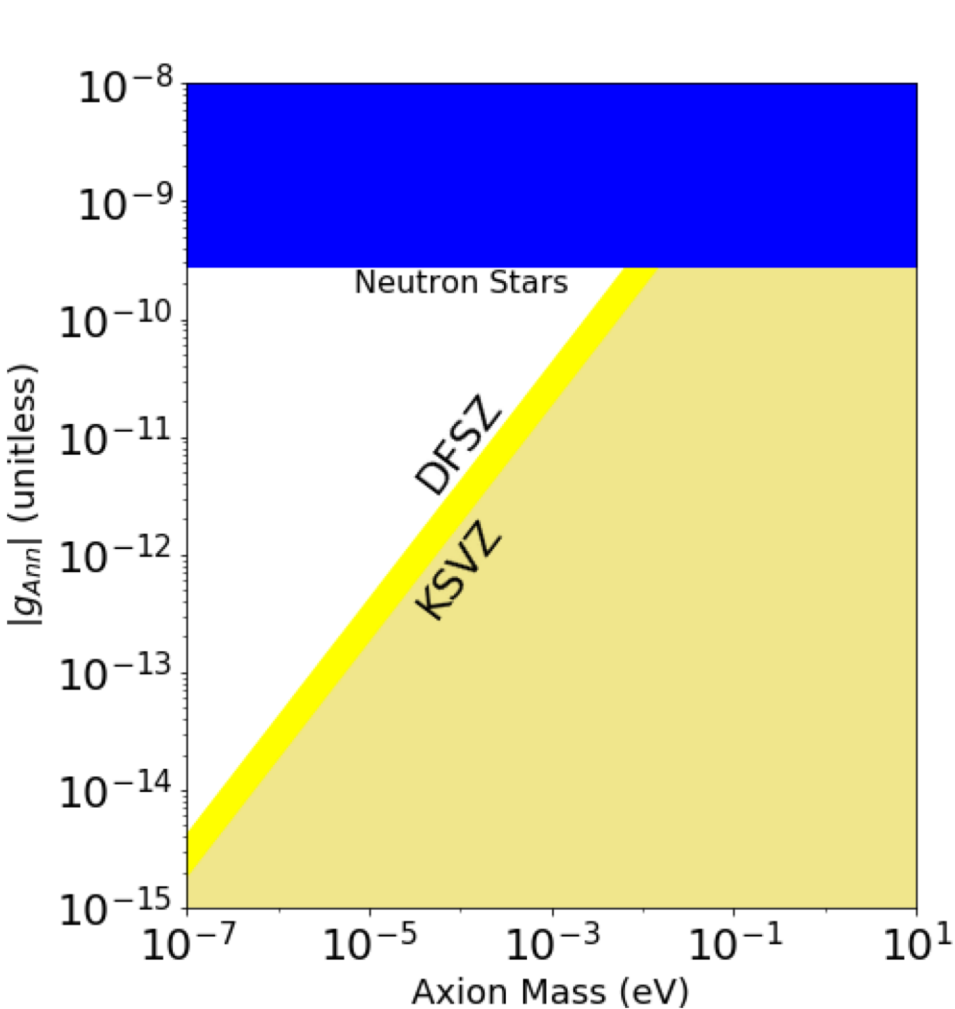
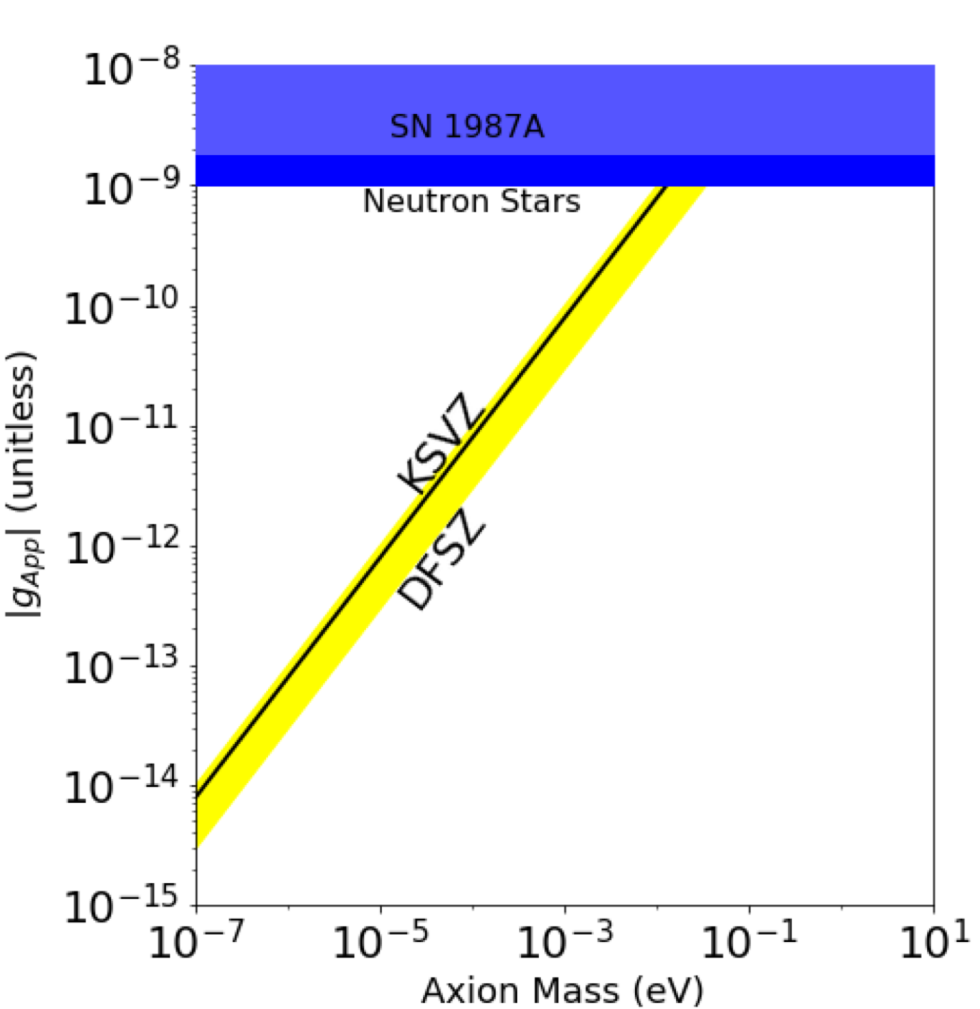
- LHC



Constraints on Axion/ALP Couplings

Coupling to protons and neutrons

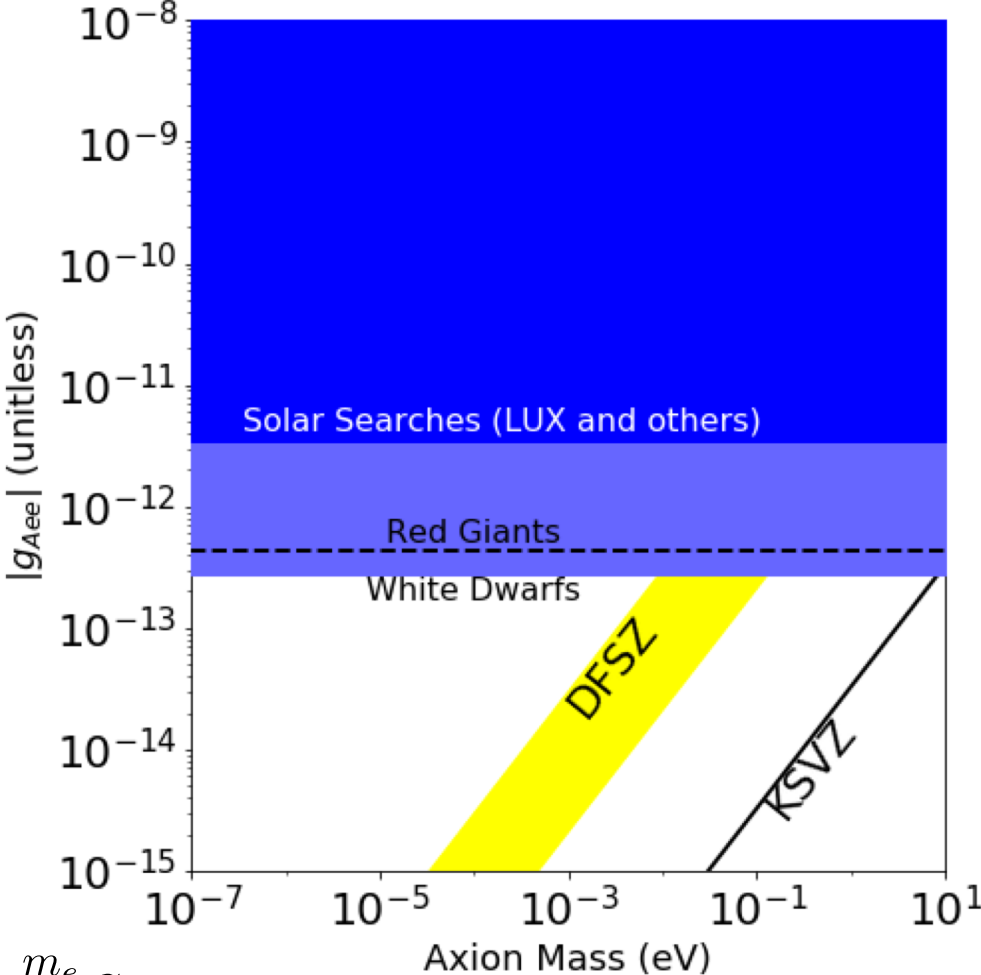
$$g_{ANN} \equiv \frac{m_N}{f_A} C_{AN}$$



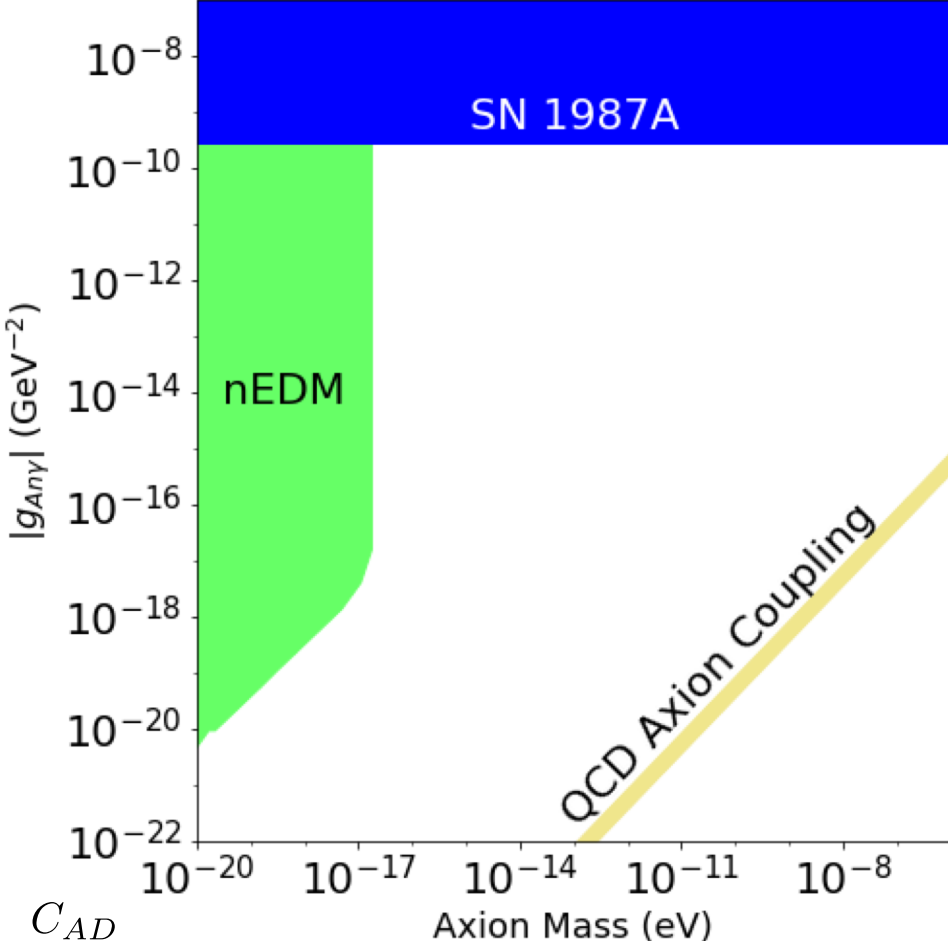
[AR,Rosenberg,Rybka in: Review of Particle Physics, PTEP 2020 (2020) 8, 083C01]

Constraints on Axion/ALP Couplings

Coupling to the electron and the neutron EDM



$$g_{Aee} \equiv \frac{m_e}{f_A} C_{Ae}$$



$$g_{An\gamma} \equiv \frac{C_{AD}}{f_A}$$

[AR,Rosenberg,Rybka in: Review of Particle Physics, PTEP 2020 (2020) 8, 083C01]

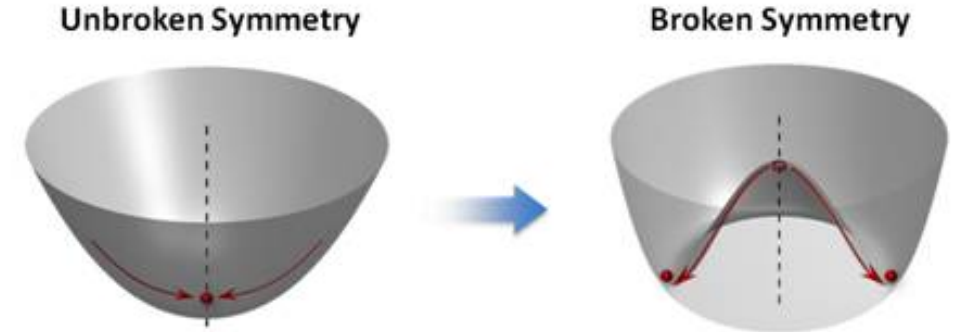
Axion Dark Matter

Vacuum re-alignment mechanism

- PQ phase transition takes place at

$$T \lesssim T_c^{\text{PQ}} \sim v_{\text{PQ}} = N f_A$$

- Axion takes random initial values in causally connected domains



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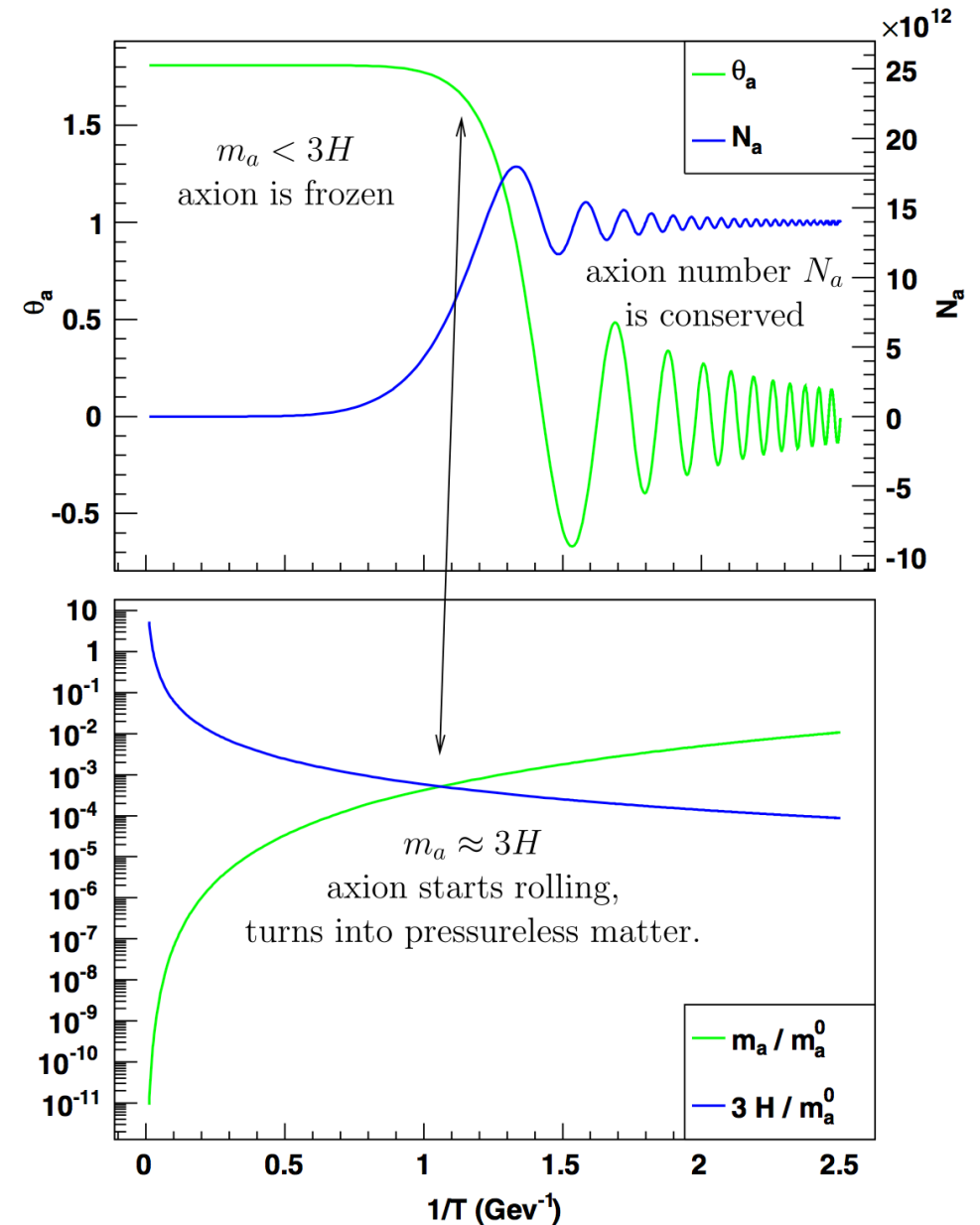
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- When $H(T) \sim m_A(T)$, axion field starts to oscillate around minimum of potential; behaves like cold dark matter: $w_A = p_A/\rho_A \simeq 0$

[Preskill,Wise,Wilczek 83; Abbott,Sikivie 83; Dine,Fischler 83,...]



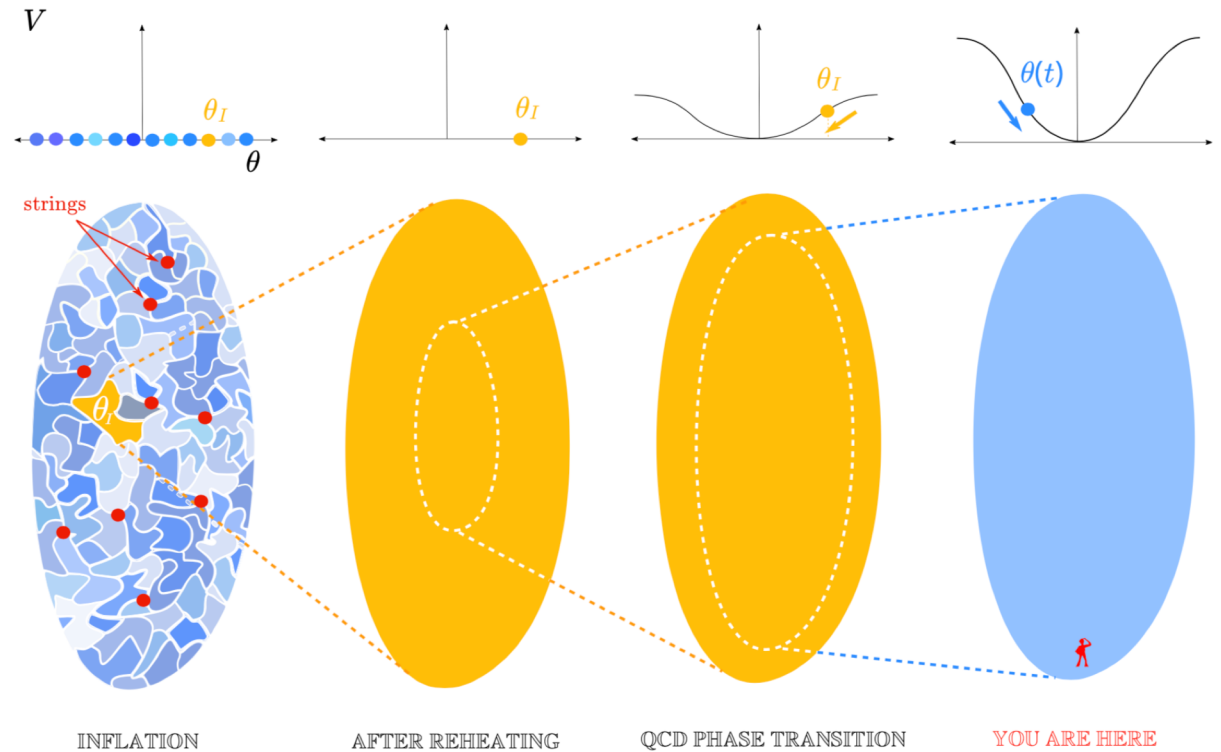
[Wantz,Shellard `09]

Axion Dark Matter

Pre-inflationary PQ SSB scenario

- If PQ symmetry broken before or during inflation ($f_A > H_I/(2\pi)$) and not restored afterwards
- Axion CDM density depends on single initial value in patch which becomes observable universe and f_A

Pre-inflationary scenarios



For illustration purposes only. Resemblance to the actual product might be limited

[Tamarit]

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$$\Omega_A^{\text{vr}} h^2 \approx 0.12 \left(\frac{f_A}{9 \times 10^{11} \text{ GeV}} \right)^{1.165} \theta_i^2$$

$$\approx 0.12 \left(\frac{6 \mu\text{eV}}{m_A} \right)^{1.165} \theta_i^2,$$

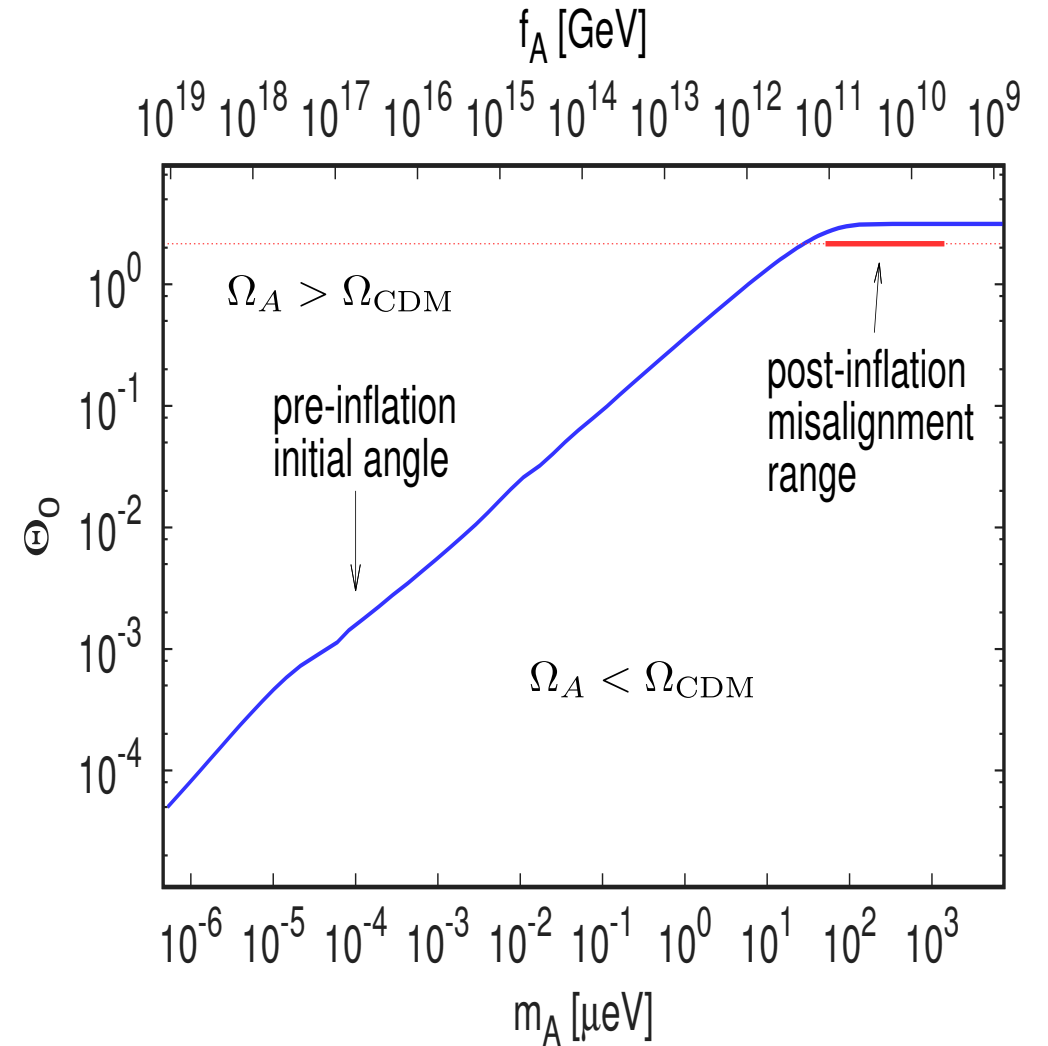
- VR works also for ALP: [Arias et al., '12]

$$\Omega_A^{\text{vr}} h^2 \approx 0.12 \left(\frac{m_A}{\text{neV}} \right)^{1/2} \left(\frac{f_A}{4.7 \times 10^{13} \text{ GeV}} \right)^2 \theta_i^2$$

(if mass independent of decay constant)

- In general, ALP can be 100 % of DM if

$$f_a \gtrsim 10^9 \text{ GeV} \left(\frac{\text{neV}}{m_a} \right)^{1/2}$$



[Borsanyi et al., Nature '16]

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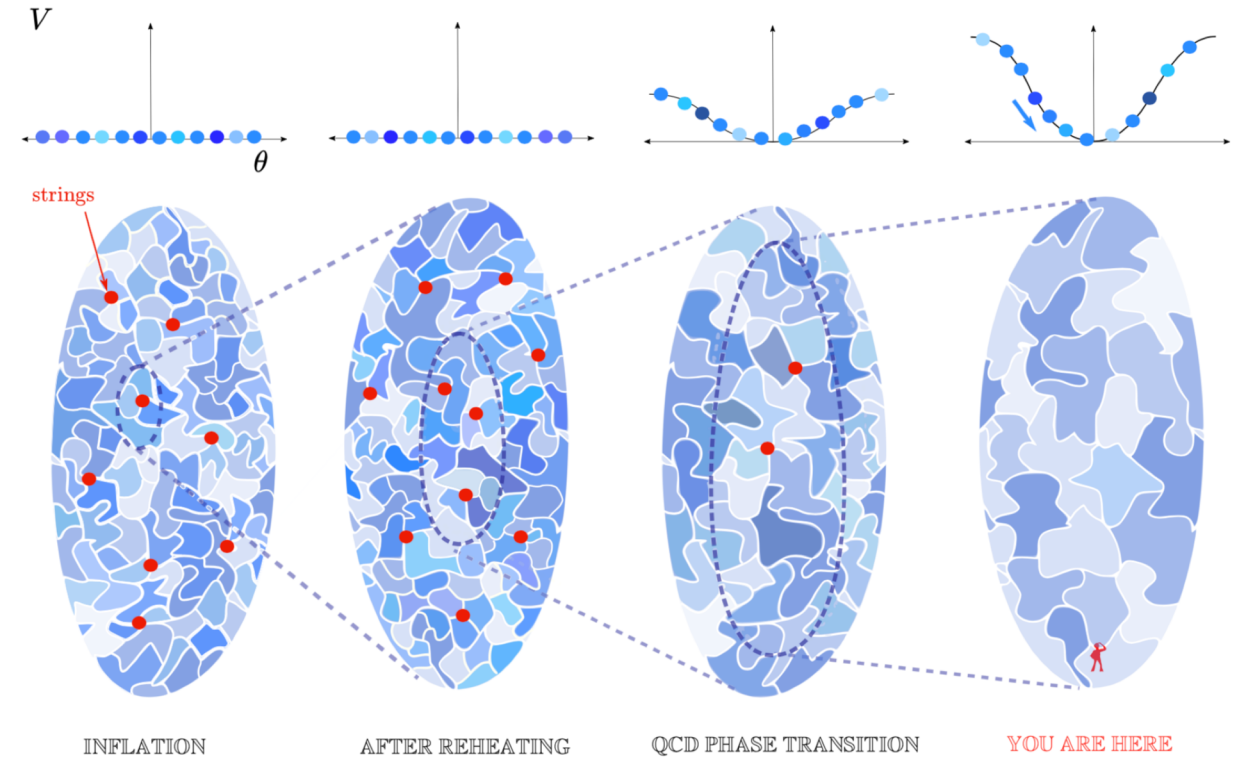
- Averaging over random initial axion field values

$$\Omega_A^{\text{vr}} h^2 \approx 0.12 \left(\frac{30 \mu\text{eV}}{m_A} \right)^{1.165}$$

- Does not exceed observed CDM abundance for

$$m_A > 28(2) \mu\text{eV} \quad [\text{Borsanyi et al., Nature '16}]$$

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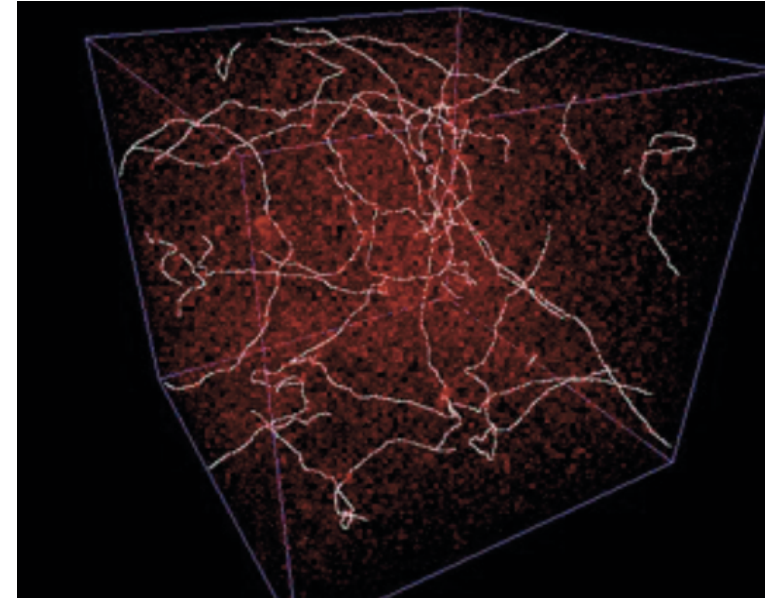
$$m_A > 28(2) \mu\text{eV} \quad [\text{Borsanyi et al., Nature `16 [1606.0794]]$$

- Axions also produced by collapse of network of topological defects – strings and domain-walls –

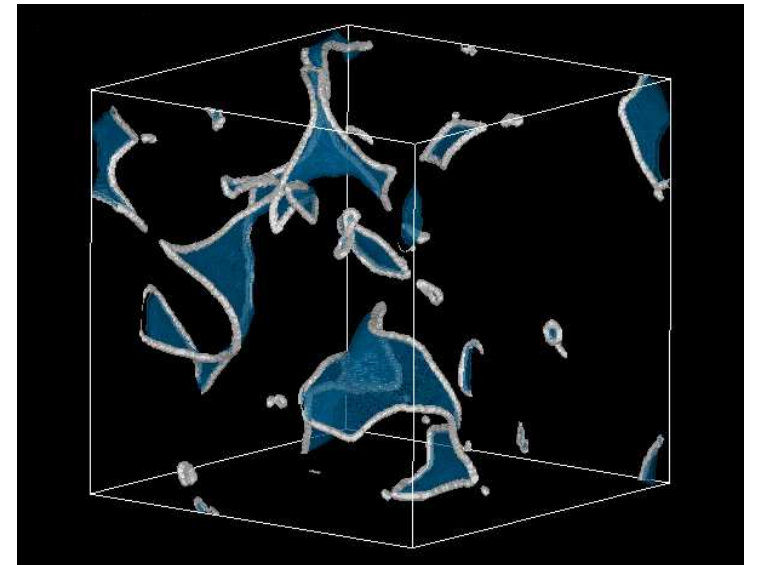
- Axion can be 100% of DM for

$$m_A \approx 25 \mu\text{eV} - 40 \text{meV}$$

[Hiramatsu et al. 11,12,13;
Kawasaki,Saikawa,Segikuchi 15;
Ballesteros et al. 16;
AR,Saikawa `16;
Klaer,Moore `17;
Gorghetto,Hardy,Villadoro `18;
Buschmann et al. 19;
Hindmarsh 19]



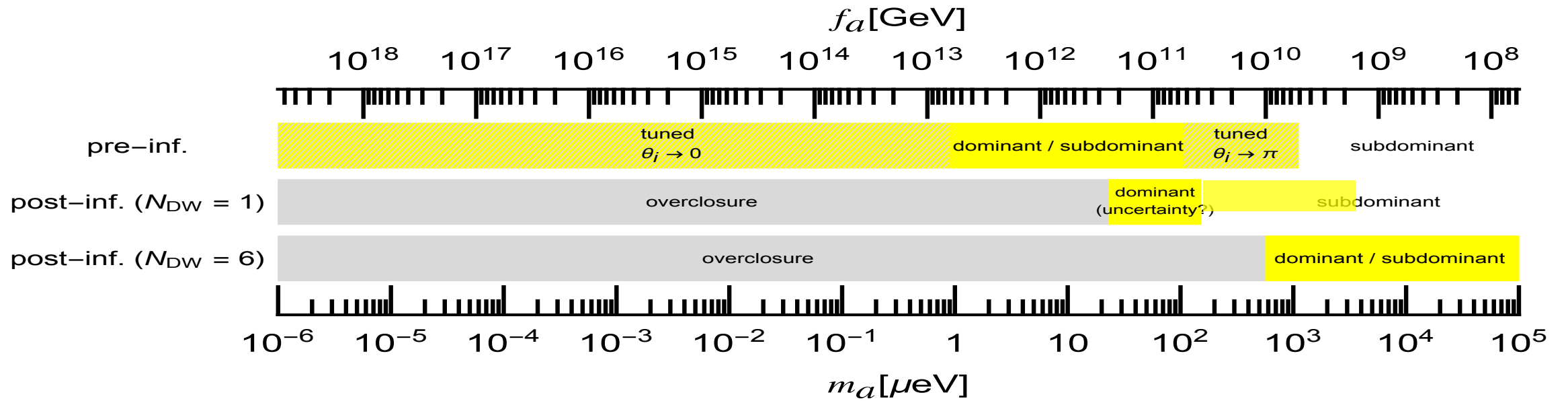
[Hiramatsu et al.]



Axion Dark Matter

Worldwide experimental efforts

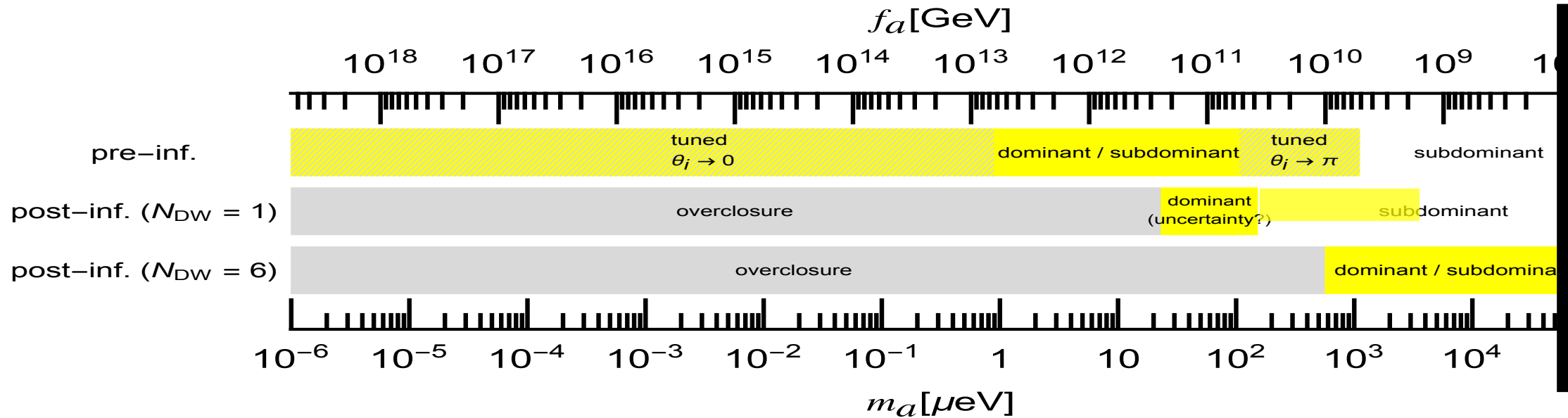
- Dark-matter axion mass spans a huge range:



Axion Dark Matter

Worldwide experimental efforts

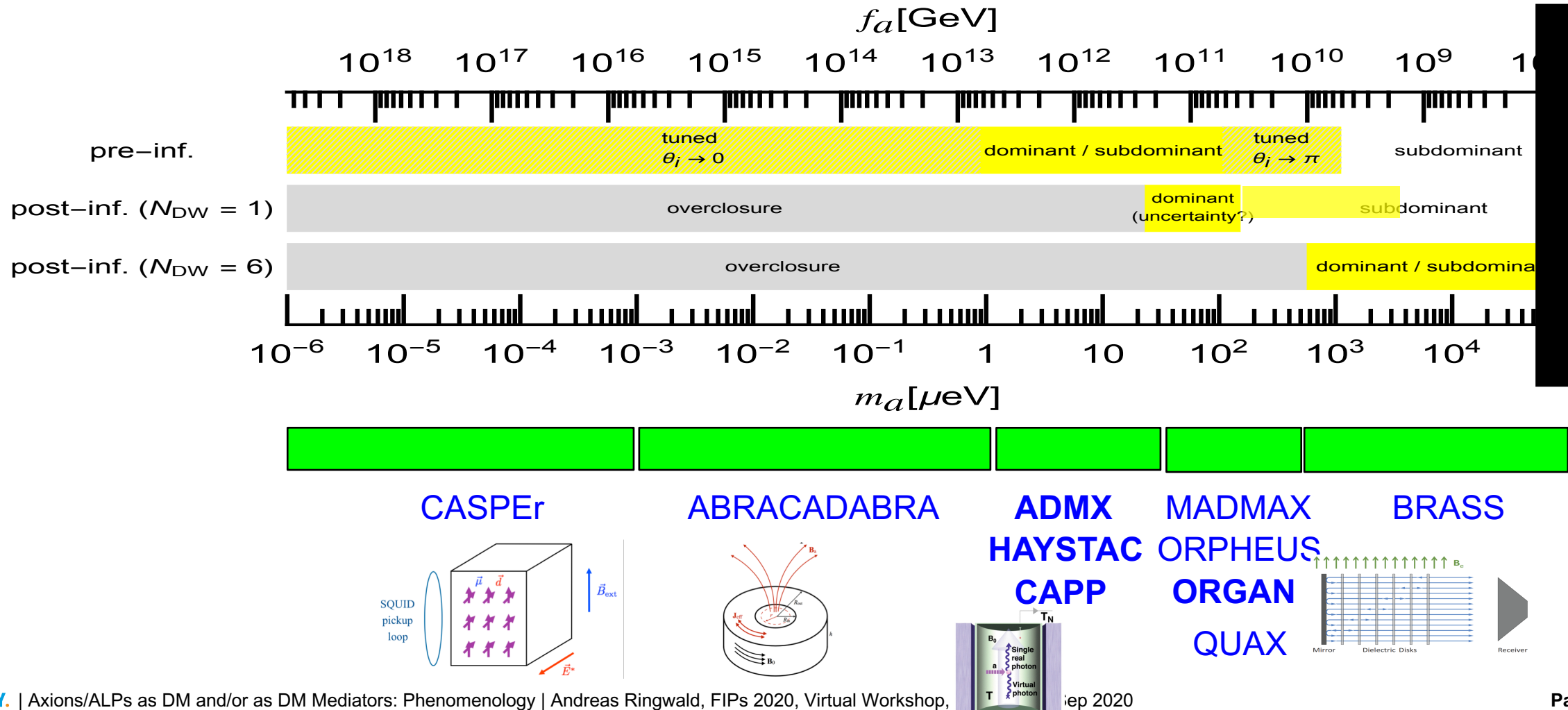
- “Axion revelation“: DM axion mass starts right at border of stellar energy loss exclusion bounds:



Axion Dark Matter

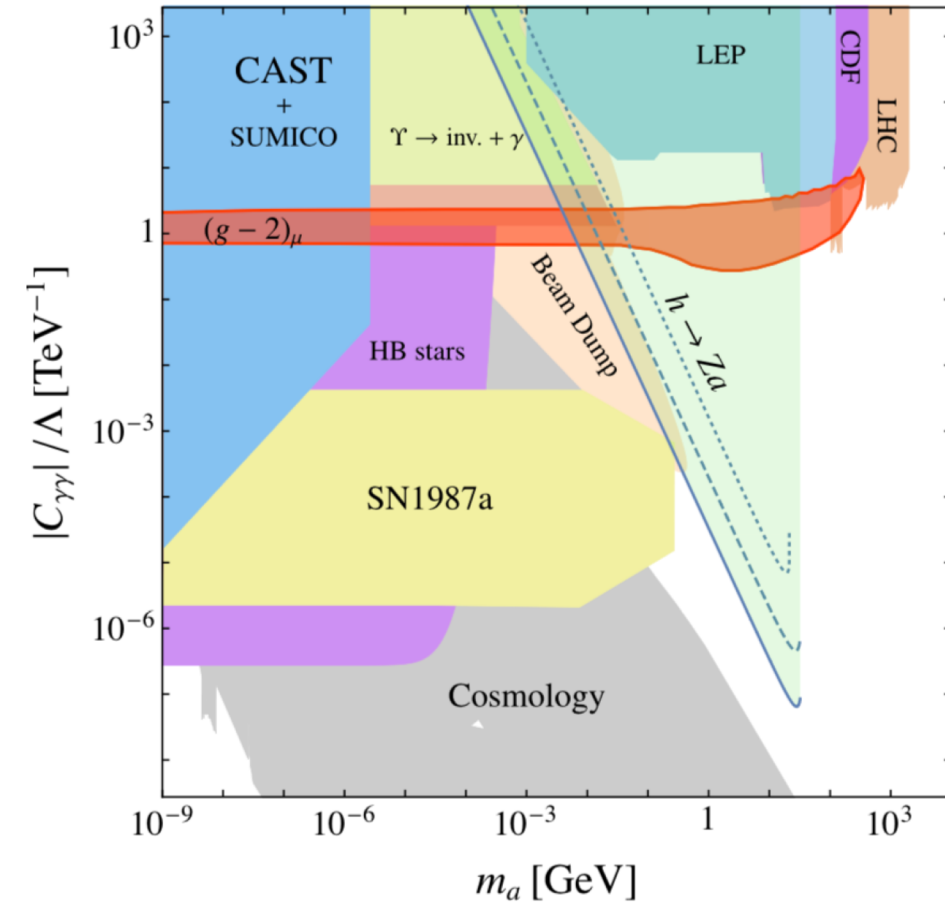
Worldwide experimental efforts

- Strong motivation for current and upcoming axion DM experiments:



Physics Case for Heavy ALPs

- Heavy ALPs coupling the visible and dark sector attractive for DM phenomenology, because they
 - easily reproduce the observed DM relic abundance from thermal freeze-out,
 - predict, at tree-level, a strong suppression of event rates in direct detection experiments,
 - may allow for observable indirect detection signals
- Heavy ALP with relatively large photon coupling may explain muon g-2 discrepancy [Chang et al. hep-ph/0009292, Marciano et al., 1607.01022]



[Bauer et al., 1704.08207]

Conclusions

- Axion extensions of SM very attractive:
 - Axion solves strong CP puzzle
 - Axion is dark matter candidate (for $f_A \gtrsim 10^8 \text{ GeV} \Leftrightarrow m_A \lesssim 60 \text{ meV}$)
- Boom in axion searches!
- Heavy ALPs also very attractive as
 - DM mediators
 - Solution of muon g-2 puzzle

Axion Dark Matter

Vacuum re-alignment mechanism

- PQ phase transition takes place at

$$T \lesssim T_c^{\text{PQ}} \sim v_{\text{PQ}} = N f_A$$

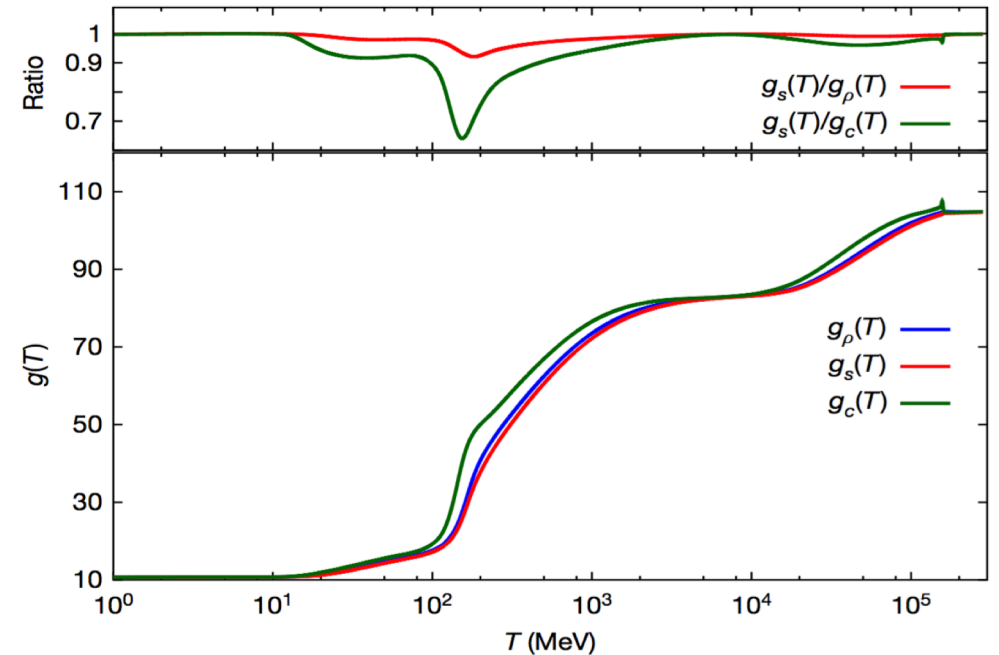
- Axion takes random initial values in causally connected domains

- When $H(T) \sim m_A(T)$, axion field starts to oscillate around minimum of potential; behaves like cold dark matter: $w_A = p_A/\rho_A \simeq 0$

[Preskill,Wise,Wilczek 83; Abbott,Sikivie 83; Dine,Fischler 83,...]

- QCD input from lattice:

- Equation of state $\Rightarrow H(T)$



[Borsanyi et al., Nature '16 [1606.0794]]

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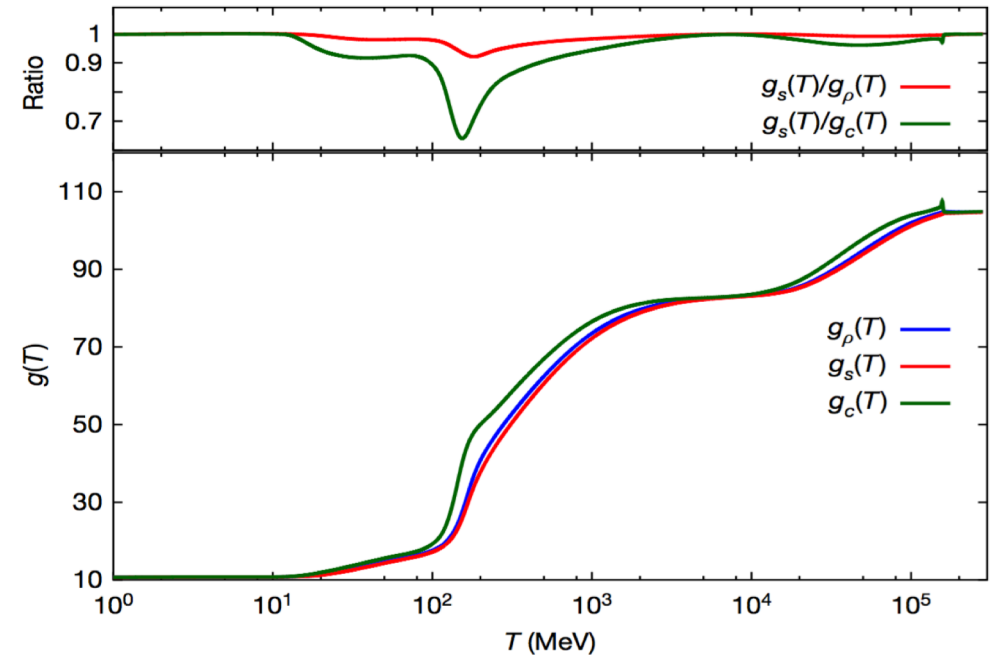
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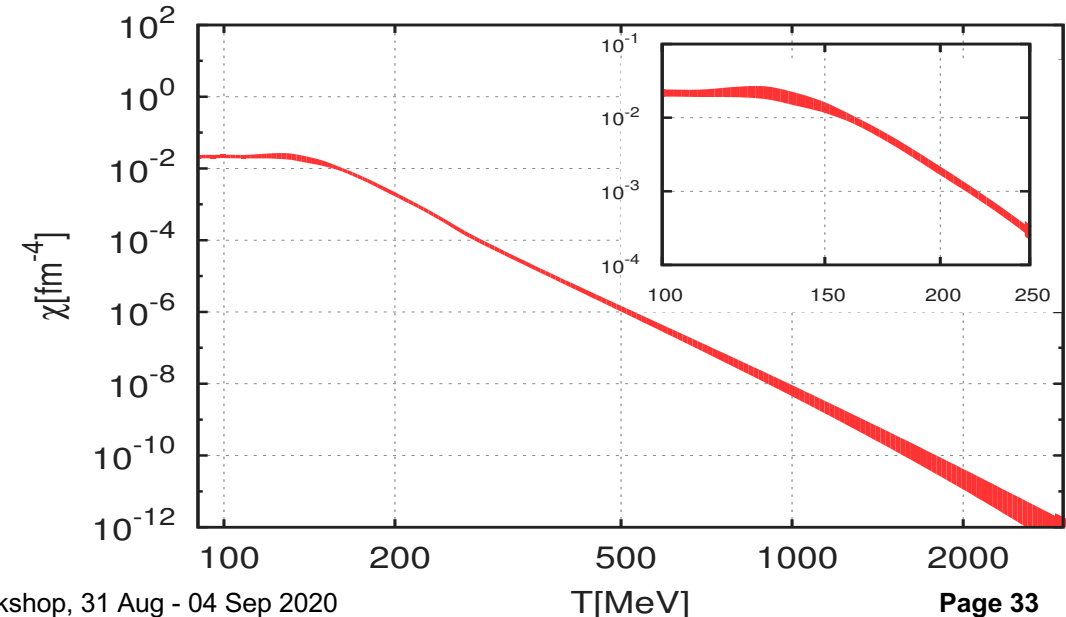
- QCD input from lattice:

- Equation of state $\Rightarrow H(T)$

- Topological susceptibility $\Rightarrow m_A(T) = \frac{\sqrt{\chi(T)}}{f_A}$



[Borsanyi et al., Nature `16 [1606.0794]]



Searches for FCNC Interactions

Minimal flavored SMASH

- Introduce right-handed singlet neutrinos N_α and complex scalar field σ with flavor-dependent spontaneously broken global chiral $U(1)_{\text{FN}}$ Froggatt-Nielsen (FN) symmetry

- Explains SM fermionic mass hierarchies and mixings by FN mechanism
- Explains neutrino masses and mixing by seesaw
- FN symmetry is at the same time a PQ symmetry
 - Nambu-Goldstone boson of FN breaking solves also strong CP problem (“axion”): “flaxion” or “axiflavor”
- Flaxion has flavor changing neutral current (FCNC) interactions

- Currently best bound from $\text{Br}(K^+ \rightarrow \pi^+ A) \lesssim 7.3 \times 10^{-11}$

$$\Rightarrow f_A \gtrsim 2 \times 10^{10} \text{ GeV} \left(\frac{26}{N_{\text{DW}}} \right) \left| \frac{(\kappa_{\text{ah}}^d)_{12}}{m_s} \right|$$

[Ema et al., 1612.05492;1802.07739; Calibbi et al., 1612.08040]

- Flaxion properties:

- Decay constant:

$$f_A = \frac{v_{\text{FN}}}{N_{\text{DW}}}, \quad N_{\text{DW}} = \text{Tr}(n^u + n^d)$$

- Typically large domain wall number

- Viable example:

$$\begin{pmatrix} q_{Q_1} & q_{Q_2} & q_{Q_3} \\ q_u & q_c & q_t \\ q_d & q_s & q_b \end{pmatrix} = \begin{pmatrix} 3 & 2 & 0 \\ -5 & -1 & 0 \\ -4 & -3 & -3 \end{pmatrix}$$

$$\begin{pmatrix} q_{L_1} & q_{L_2} & q_{L_3} \\ q_e & q_\mu & q_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ -8 & -5 & -3 \end{pmatrix}$$

$$\Rightarrow n_{ij}^u = \begin{pmatrix} 8 & 4 & 3 \\ 7 & 3 & 2 \\ 5 & 1 & 0 \end{pmatrix}, \quad n_{ij}^d = \begin{pmatrix} 7 & 6 & 6 \\ 6 & 5 & 5 \\ 4 & 3 & 3 \end{pmatrix}, \quad n_{ij}^l = \begin{pmatrix} 9 & 6 & 4 \\ 8 & 5 & 3 \\ 8 & 5 & 3 \end{pmatrix}$$

$$\Rightarrow N_{\text{DW}} = 26$$

- Coupling to photon:

$$C_{A\gamma} = \frac{2}{N_{\text{DW}}} \sum_{f=u,d,l} \left[N_f \text{Tr}(n^f) \left(q_f^{(\text{em})} \right)^2 \right] - 1.92(2)$$

- For example above: $C_{A\gamma} = 113/39 - 1.92 \simeq 0.97$

- **NA62:** reach in decay constant increased by order of magnitude!