



**Warsaw University  
of Technology**



**Faculty  
of Physics**

WARSAW UNIVERSITY OF TECHNOLOGY

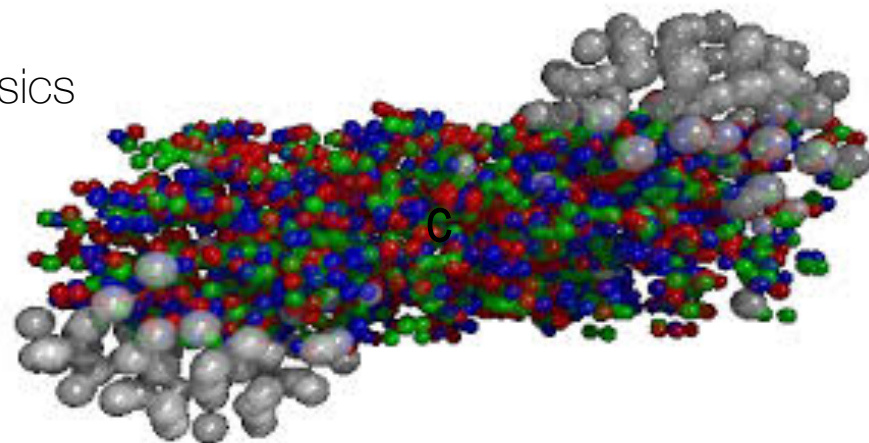
# What can we learn from femtoscopy?

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Warsaw University of Technology

Faculty of Physics



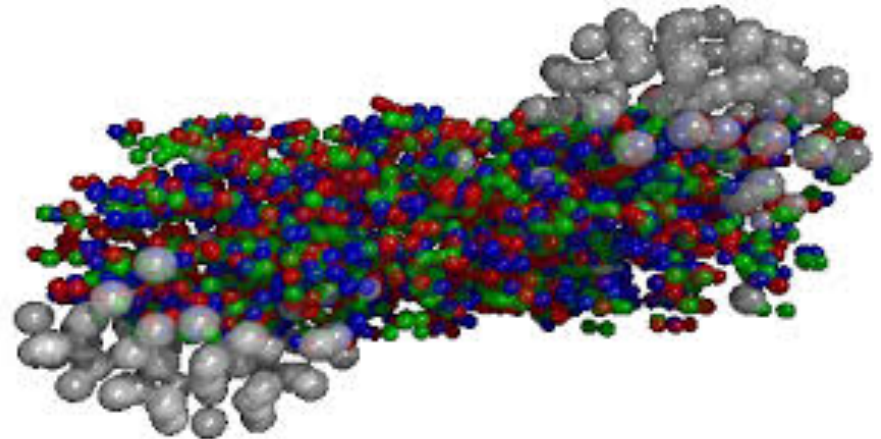
# Outline

## Introduction

- HIC and HBT method
- Correlation femtoscopy: method, frames, correlations, measures, ...
- RHIC / STAR

## Results

- a) Strong **interactions** between (anti)baryons
- b) Femtoscopy of strange baryons
- c) Beam Energy Scan Program (BES):
  - identical pion femtoscopy
  - **geometry**: centrality dependencies  
energy dependencies  
system (of pair) dependencies
  - **dynamics**: centrality dependencies  
energy dependencies  
system (of pair) dependencies

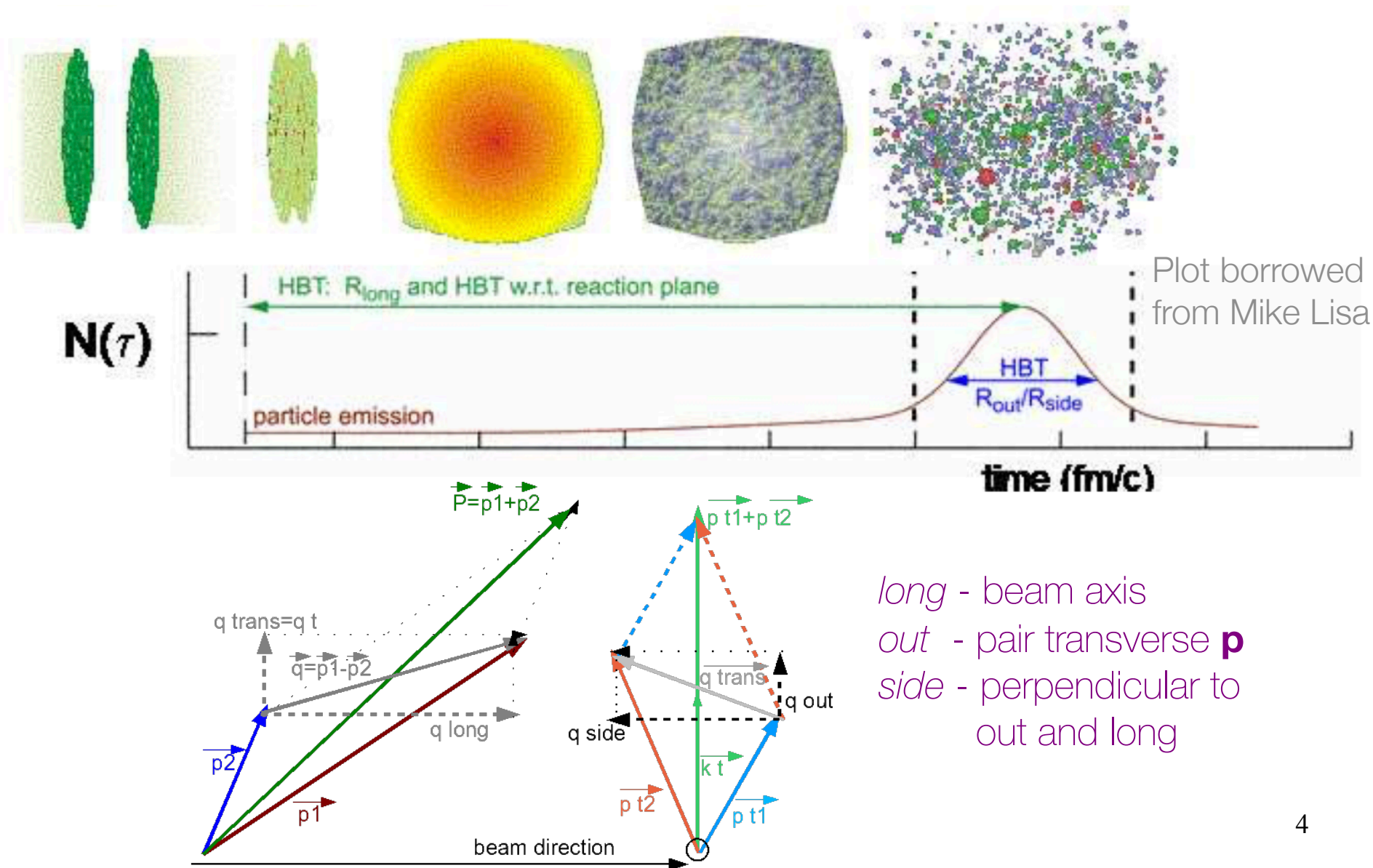


## Conclusions



# Introduction

# Heavy-ion collision and **HBT** method



# Correlation **femtoscopy**



Size:  $\sim 10^{-15}$  m (**fm**)  
Time:  $\sim 10^{-23}$  s

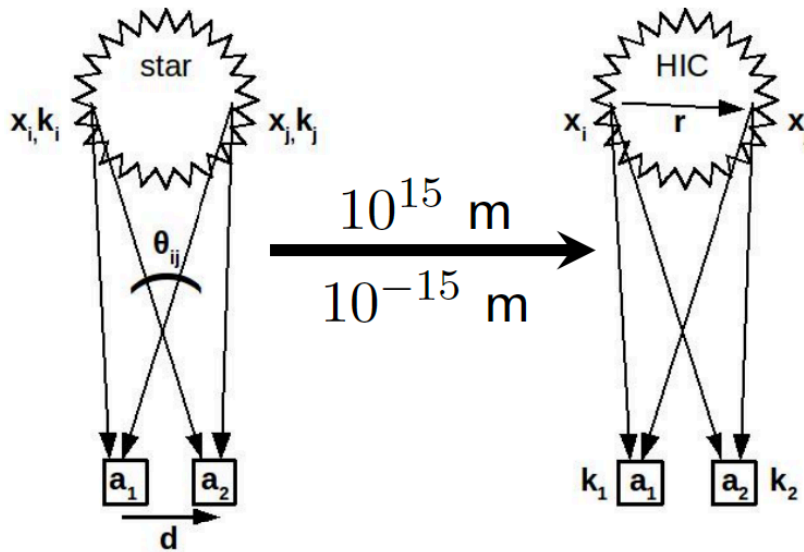
**Impossible  
to measure directly!**

# Correlation **femtosc**copy



Size:  $\sim 10^{-15}$  m (**fm**)  
Time:  $\sim 10^{-23}$  s

**Impossible  
to measure directly!**



Femtoscopia (**HIC**) inspired by  
**H**anbury **B**rown and **T**wiss  
interferometry method  
(**Astronomy**)

**but!**

- different scales,
- different measured quantities
- different determined quantities

# Femtoscopic correlations

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$x_1, x_2$  - space-time sizes and dynamics

(**can not** be measured directly)  $\rightarrow$

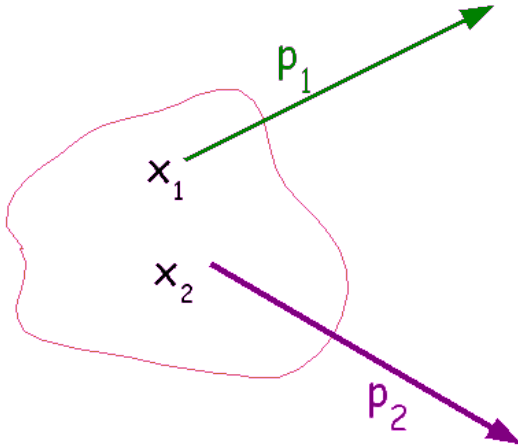
**Close velocity correlations**

**(HBT + FSI)  $\leftarrow$**

$p_1, p_2$  - momenta and momentum difference

(**can** be measured directly)

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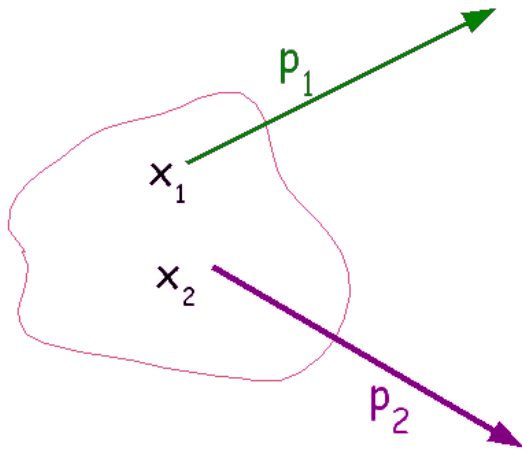




# Femtoscopic correlations and correlation function

## **S(x,p)** – emission function:

the distribution of source density  
probability of finding particle with x and p



$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3 p_1 d^3 p_2} = \int d^4 x_1 S(x_1, p_1) d^4 x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$

$x_1, x_2$  - space-time sizes and dynamics

(**can not** be measured directly) →

**Close velocity correlations**

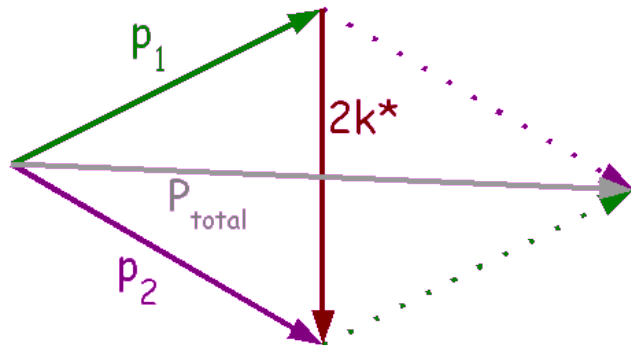
**(HBT + FSI) ←**

$p_1, p_2$  - momenta and momentum difference

(**can** be measured directly)

Single- and two-particle distributions

$$P_1(p) = E \frac{dN}{d^3 p} = \int d^4 x S(x, p)$$

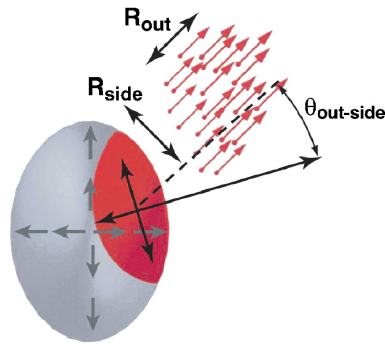
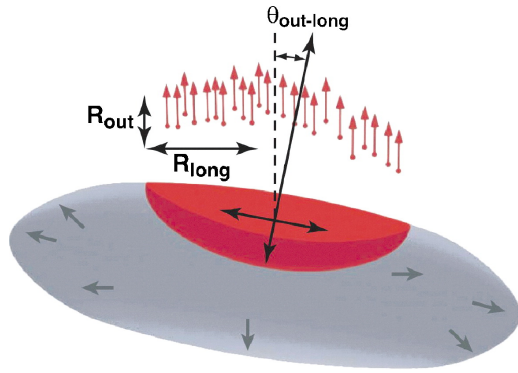


## **Correlation function**

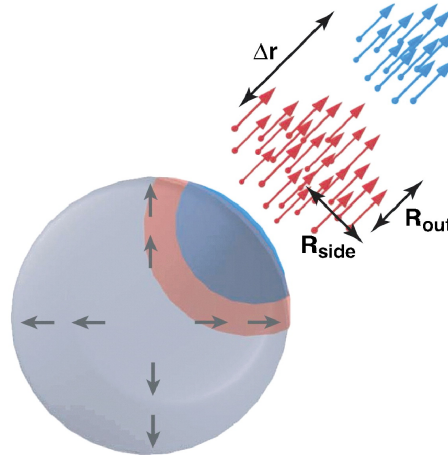
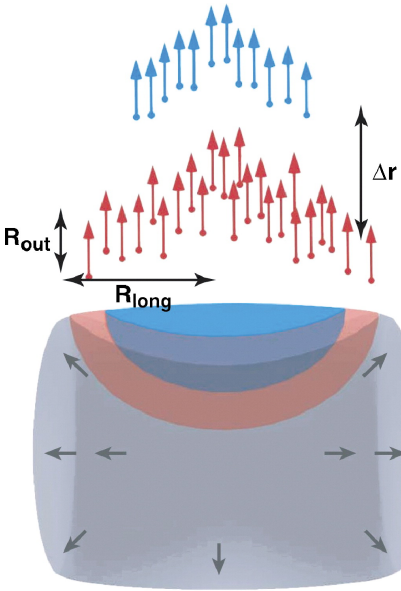
$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1) P_1(p_2)}$$



# What does femtoscopy measure?



Lisa MA, et al. 2005.  
Annu. Rev. Nucl. Part. Sci. 55:357–402

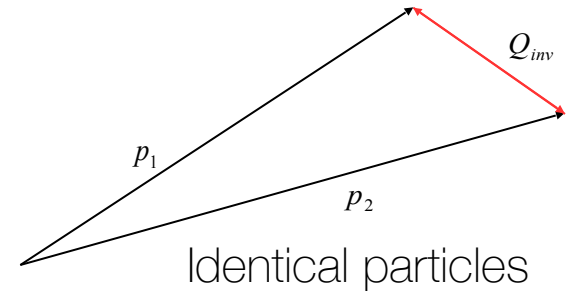


Lisa MA, et al. 2005.  
Annu. Rev. Nucl. Part. Sci. 55:357–402

## Homogeneity region

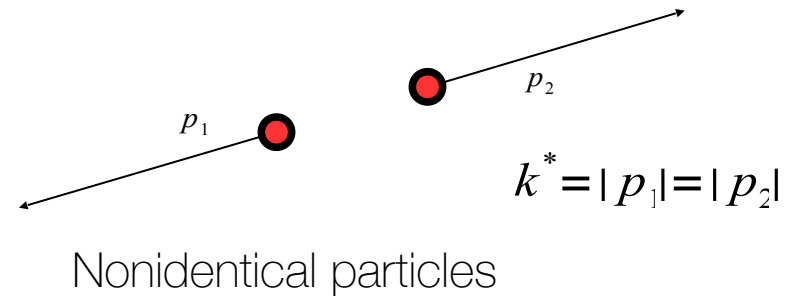
$Q_{inv}$

Longitudinal Co-Moving System - **LCMS**



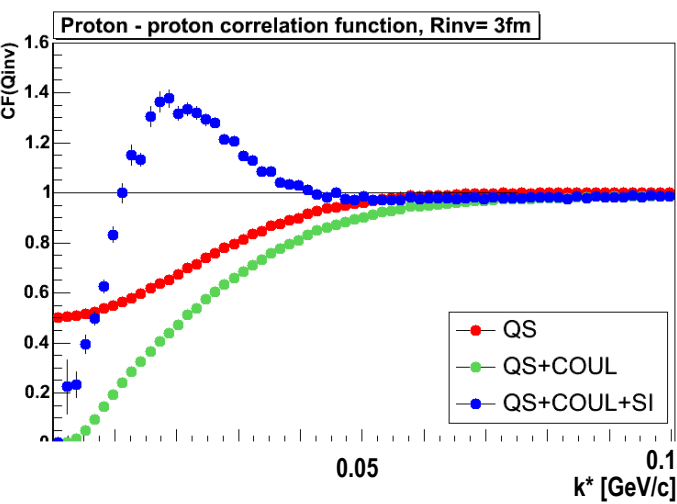
$k^*$

Pair Rest Frame - **PRF**



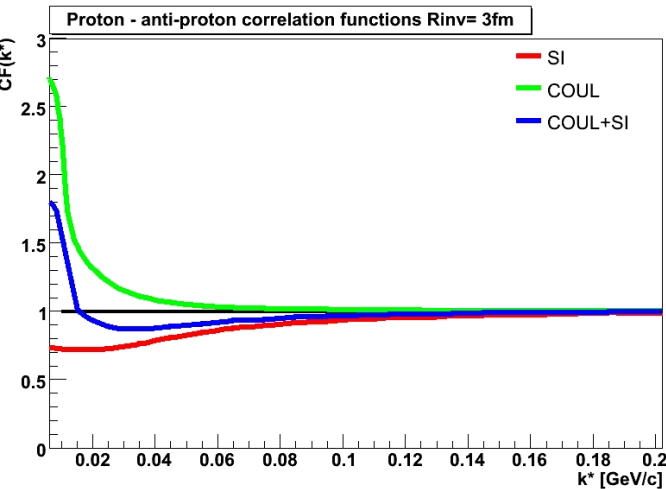
$$Q_{inv} = 2k^* \quad \text{for } m_1 = m_2$$

# Effects and interactions



## Identical baryon- baryon

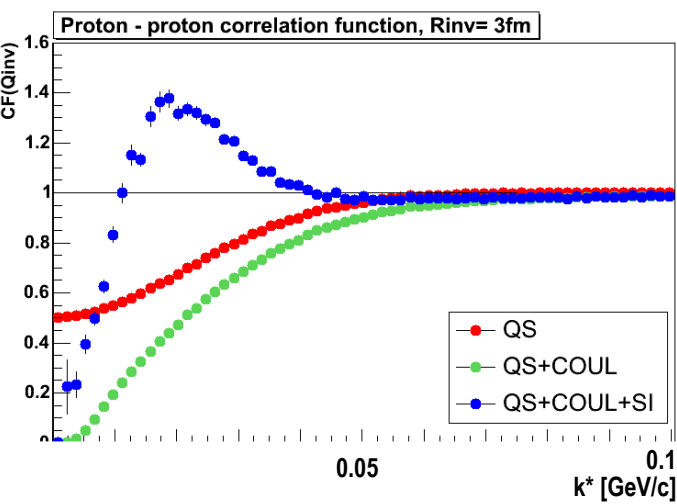
- Quantum Statistics- **QS**
- Final State Interactions- **FSI**
  - Coulomb
  - Strong



## Non-identical baryon- (anti)baryon

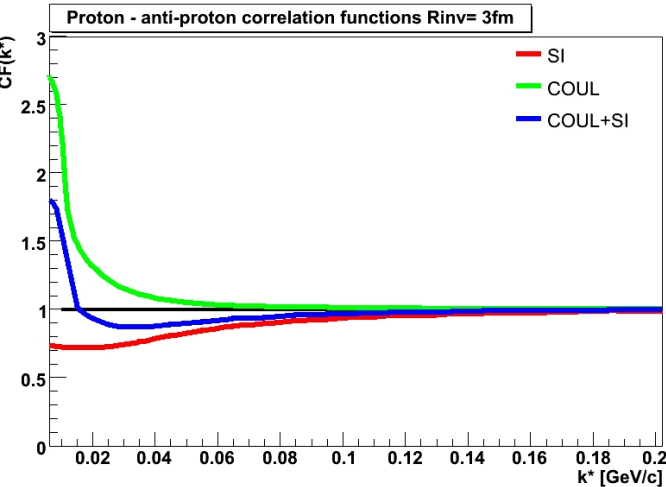
- Final State Interactions- **FSI**
  - Coulomb
  - Strong

# Effects and interactions



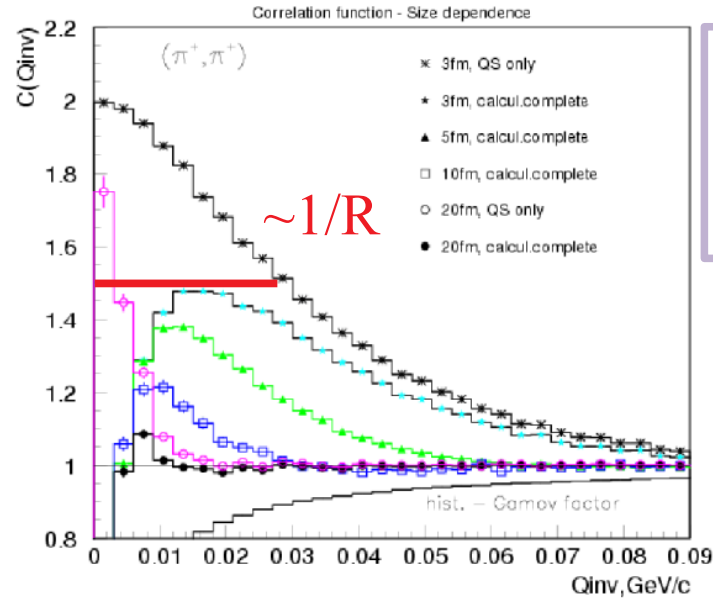
## Identical baryon- baryon

- Quantum Statistics- **QS**
- Final State Interactions- **FSI**
  - Coulomb
  - Strong

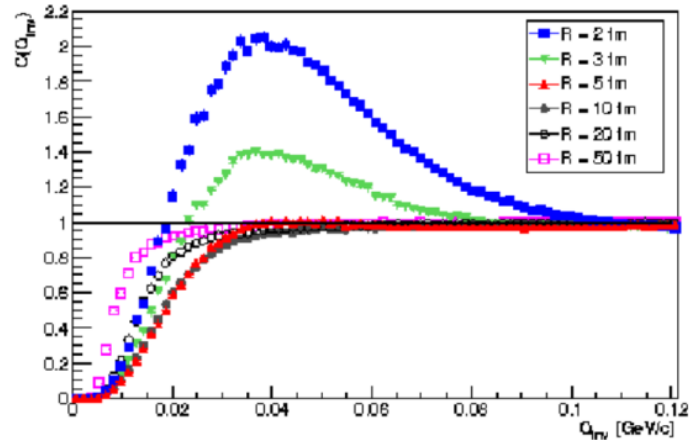


## Non-identical baryon- (anti)baryon

- Final State Interactions- **FSI**
  - Coulomb
  - Strong



Width of correlation function  
 $\sim 1/R$

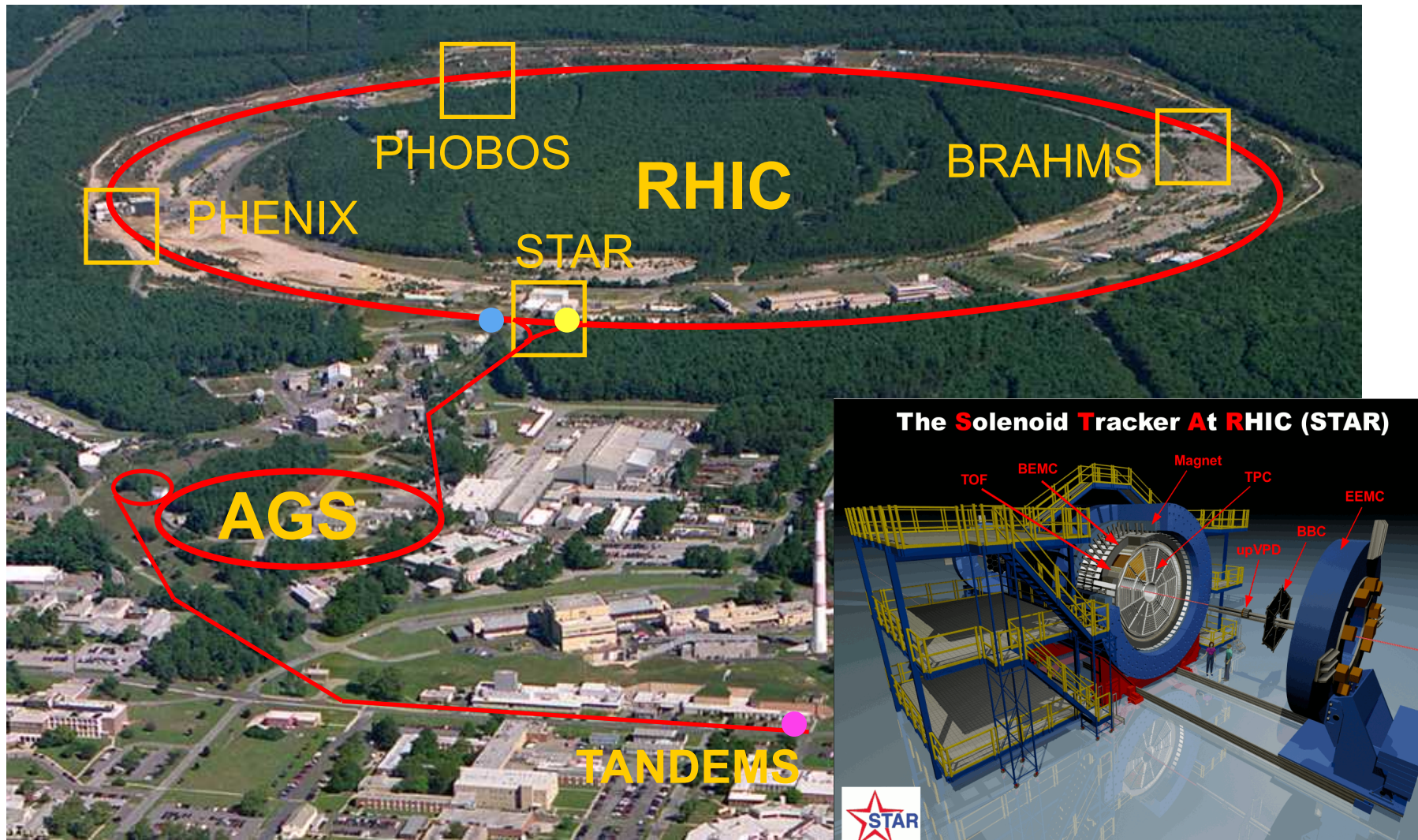


Bigger source and weaker correlation



# Relativistic Heavy Ion Collider (**RHIC**)

## Brookhaven National Laboratory (**BNL**), Upton



- 2 concentric rings of 1740 superconducting magnets
- 3.8 km circumference



# Results

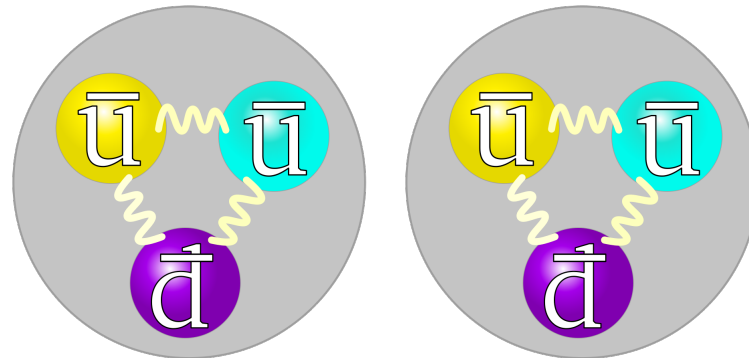
## a) Proton Femtoscopy @200 GeV

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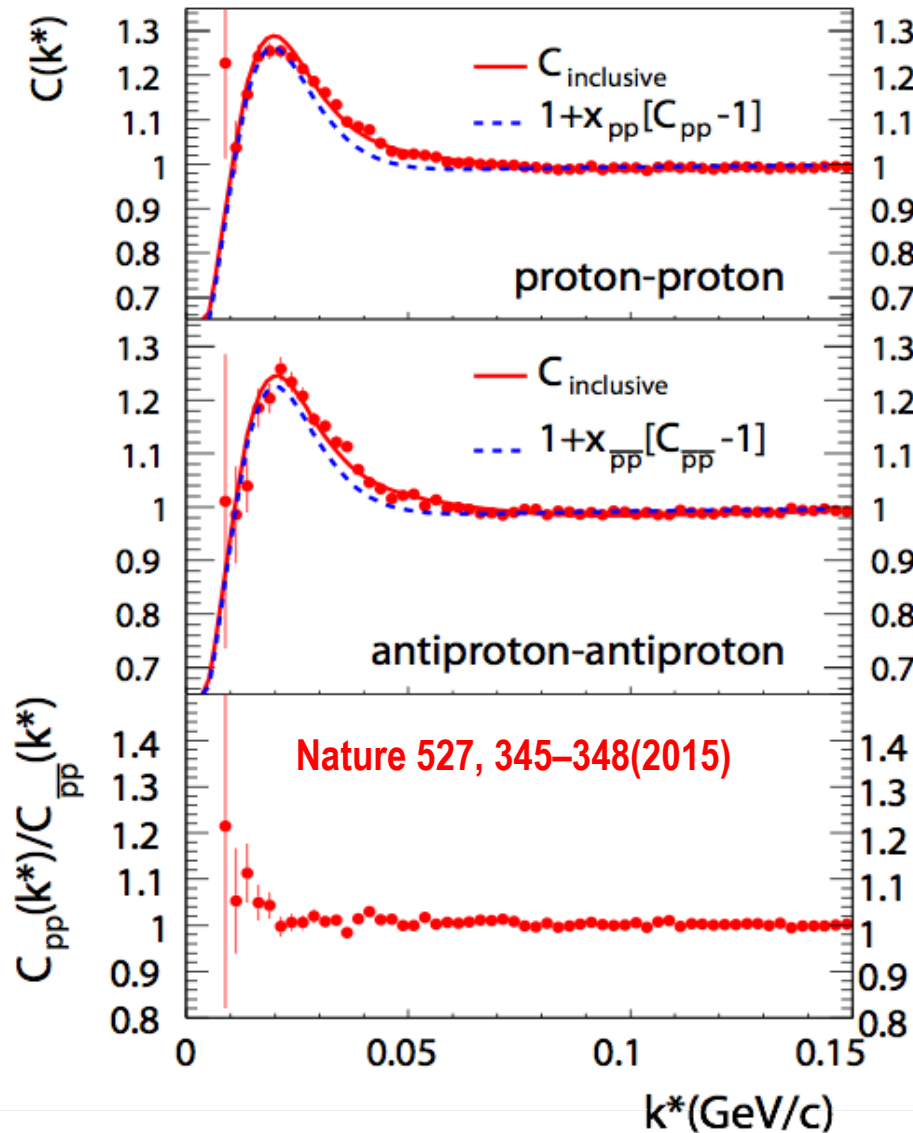
So far, the knowledge on **nuclear force** was derived from studies made on **nucleon** or / and **nuclei**.

**Nuclear force** between **anti-nucleons** is studied for the first time.

The knowledge of **interaction** between two **anti-protons** is fundamental to understand the properties of more sophisticated anti-nuclei.



# a) Strong interactions between anti-nucleons



Fit results:

**p-p** CF,

$R=2.75\pm0.01\text{fm}$ ;

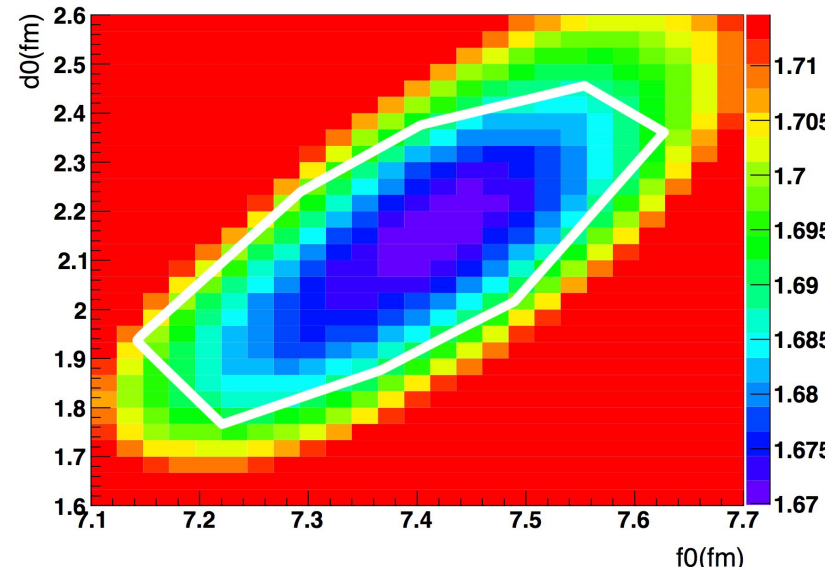
$\chi^2/\text{NDF} = 1.66$ ;

**antiproton-antiproton** CF,

$R=2.80\pm0.02\text{fm}$  ,  $f_0=7.41\pm0.19\text{fm}$ ,

$d_0=2.14\pm0.27\text{fm}$ ;

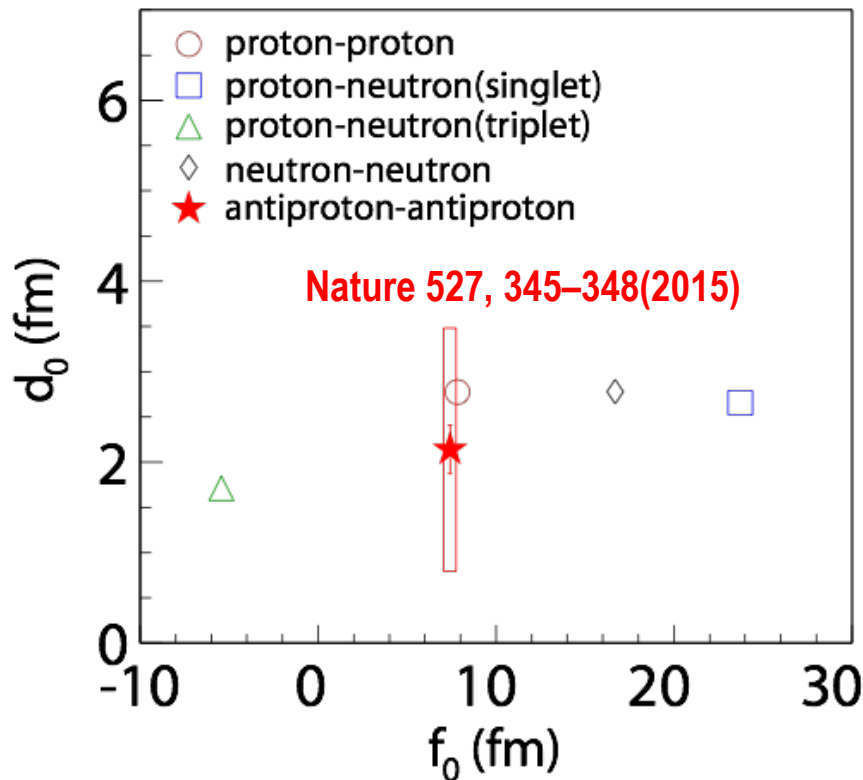
$\chi^2/\text{NDF}=1.61$



$\chi^2/\text{NDF}(f_0, d_0)$  map of the results between measured function and fitted one to find the best values of  $f_0$ ,  $d_0$  parameters



# a) Strong interactions between anti-nucleons



- $f_0$  and  $d_0$  for the antiproton-antiproton interaction consistent with parameters for the proton-proton interaction.
- Descriptions of the interaction among antimatter (based on the simplest systems of anti-nucleons) determined.
- A quantitative verification of matter-antimatter symmetry in context of the forces responsible for the binding of (anti)nuclei.

The scattering length  $f_0$ : determines low-energy scattering.

The elastic cross section,  $\sigma_e$ , (at low energies) determined solely by  $\lim_{k \rightarrow 0} \sigma_e = 4\pi f_0^2$   
the scattering length,

$d_0$  - the effective range of strong interaction between two particles.

It corresponds to the range of the potential in an extremely simplified scenario - the square well potential.

$f_0$  and  $d_0$  - two important parameters of strong interaction between two particles.

Theoretical correlation function depends on: source size,  $k^*$ ,  $f_0$  and  $d_0$ .

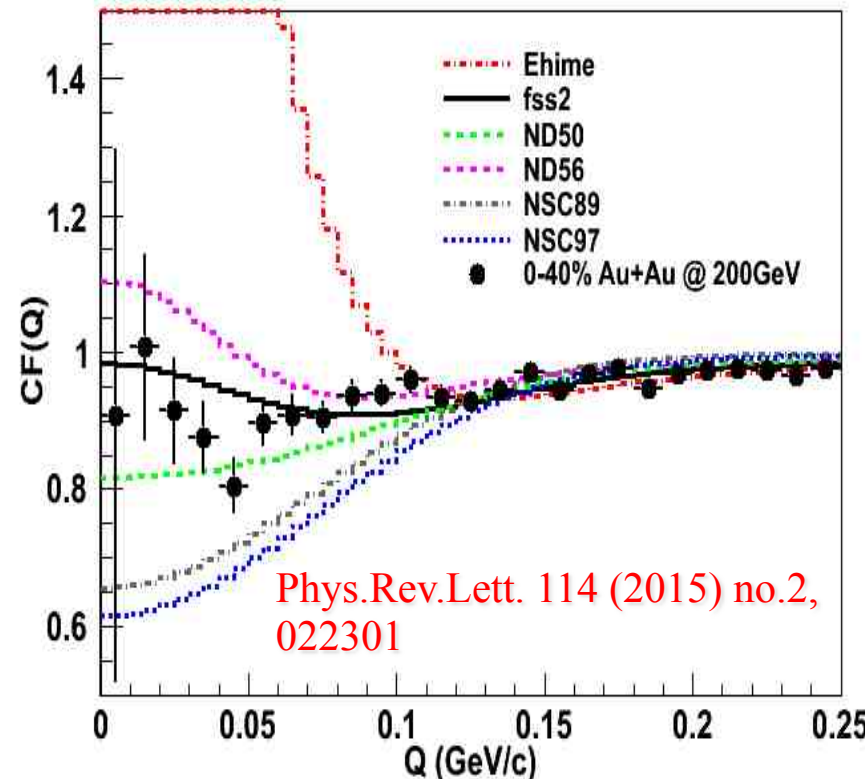
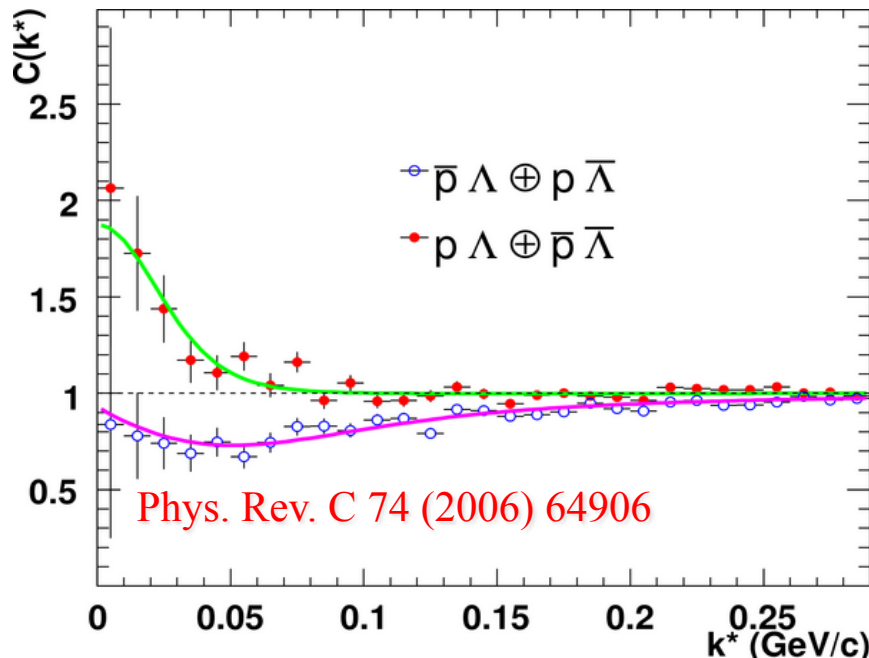
## b) Strange Baryon Correlations (Including $\Lambda$ Hyperons)

**proton-lambda** correlations:  
sensitive to the Strong FSI only

**lambda-lambda** correlations:  
sensitive to the Quantum Statistical  
effects and Strong FSI

lambda-lambda and proton-lambda correlations:  
contain contributions from **Residual** feed-down  
**Correlations (RC)**

System	$r_0$ (fm)
$p - \Lambda$	$2.97 \pm 0.34^{+0.19}_{-0.25} \pm 0.2$
$\bar{p} - \bar{\Lambda}$	$3.24 \pm 0.59^{+0.24}_{-0.14} \pm 0.2$
$p - \Lambda \oplus \bar{p} - \bar{\Lambda}$	$3.09 \pm 0.30^{+0.17}_{-0.25} \pm 0.2$
$\bar{p} - \Lambda$	$1.56 \pm 0.08^{+0.10}_{-0.14} \pm 0.3$
$p - \bar{\Lambda}$	$1.41 \pm 0.10 \pm 0.11 \pm 0.3$
$\bar{p} - \Lambda \oplus p - \bar{\Lambda}$	$1.50 \pm 0.05^{+0.10}_{-0.12} \pm 0.3$



## b) Strange Baryon Correlations (Including $\Lambda$ Hyperons)

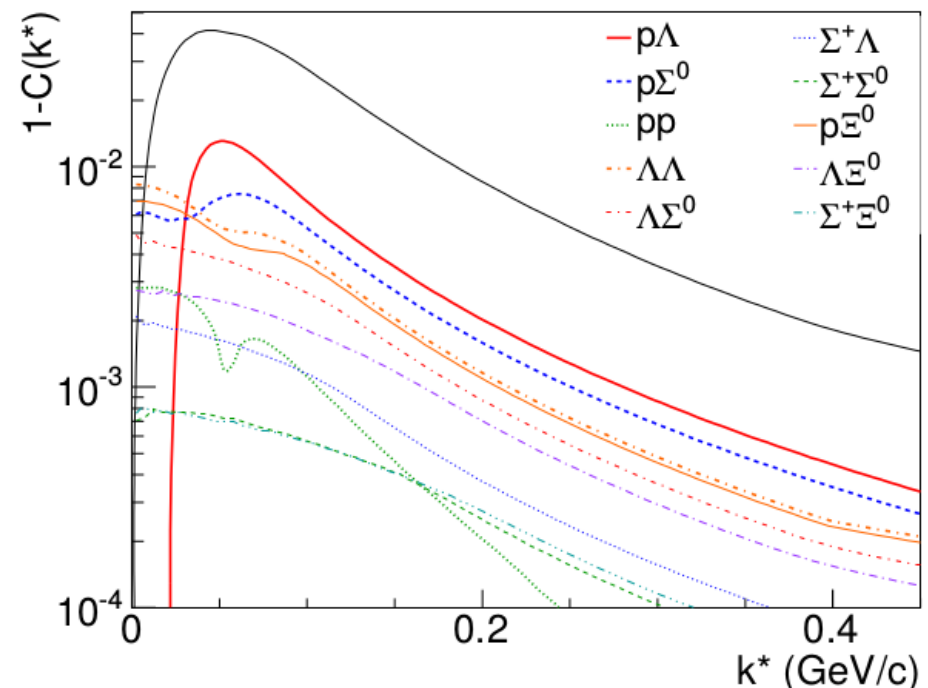
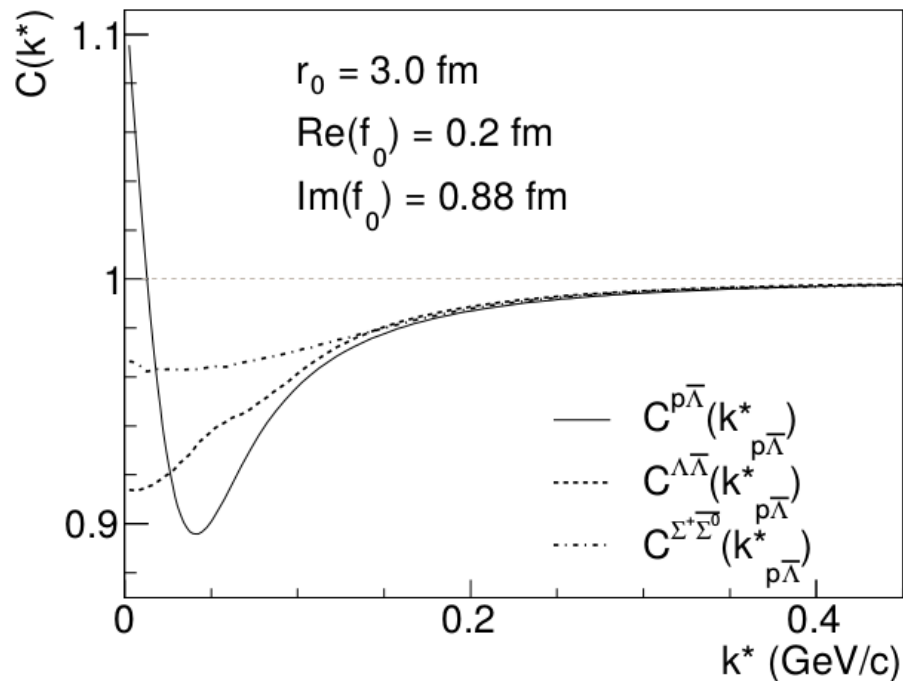
For residual correlations correction  
see talk by S. Siejka

$$C^{X\bar{Y} \rightarrow p\bar{\Lambda}}(k_{p\bar{\Lambda}}^*) = \frac{\int C^{X\bar{Y}}(k_{X\bar{Y}}^*) W(k_{X\bar{Y}}^*, k_{p\bar{\Lambda}}^*) dk_{X\bar{Y}}^*}{\int W(k_{X\bar{Y}}^*, k_{p\bar{\Lambda}}^*) dk_{X\bar{Y}}^*},$$

$$C(k_{p\bar{\Lambda}}^*) = 1 + \lambda_{p\Lambda} \left( C^{p\bar{\Lambda}}(k_{p\bar{\Lambda}}^*) - 1 \right) + \sum_{X\bar{Y}} \lambda_{X\bar{Y}} \left( C^{X\bar{Y}}(k_{p\bar{\Lambda}}^*) - 1 \right)$$

**HZ, A. Kisiel, M. Szymański**

**Phys.Rev. C89 (2014) no.5, 054916**



# b) Strange Baryon Correlations (including $p\text{-}\Omega$ )

Binding energy  $E_{\text{bin}}$  [MeV]

Scattering length  $a_0$  [fm]

Effective range  $r_{\text{eff}}$  [fm]

for 3 scenarios:

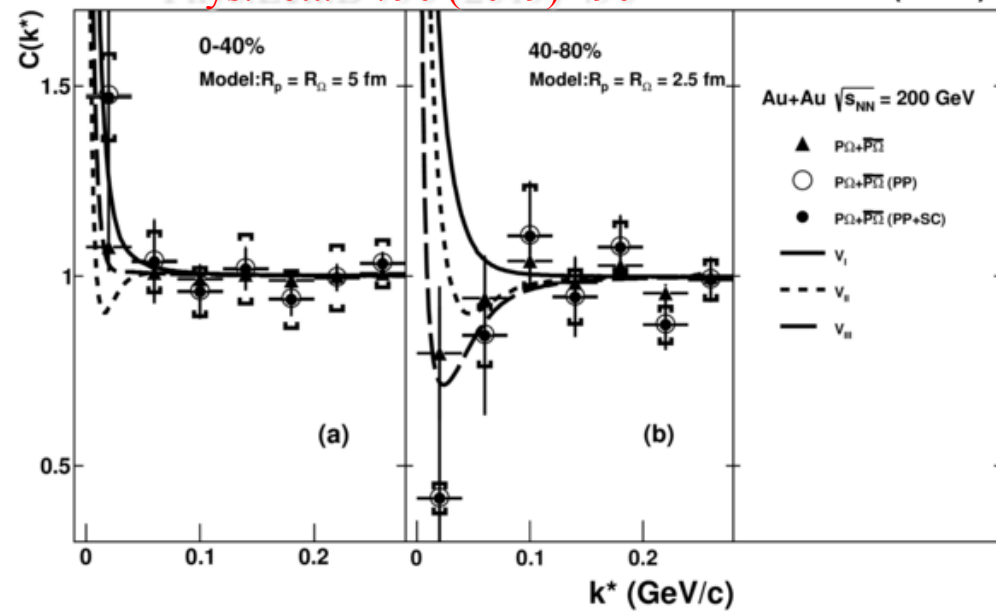
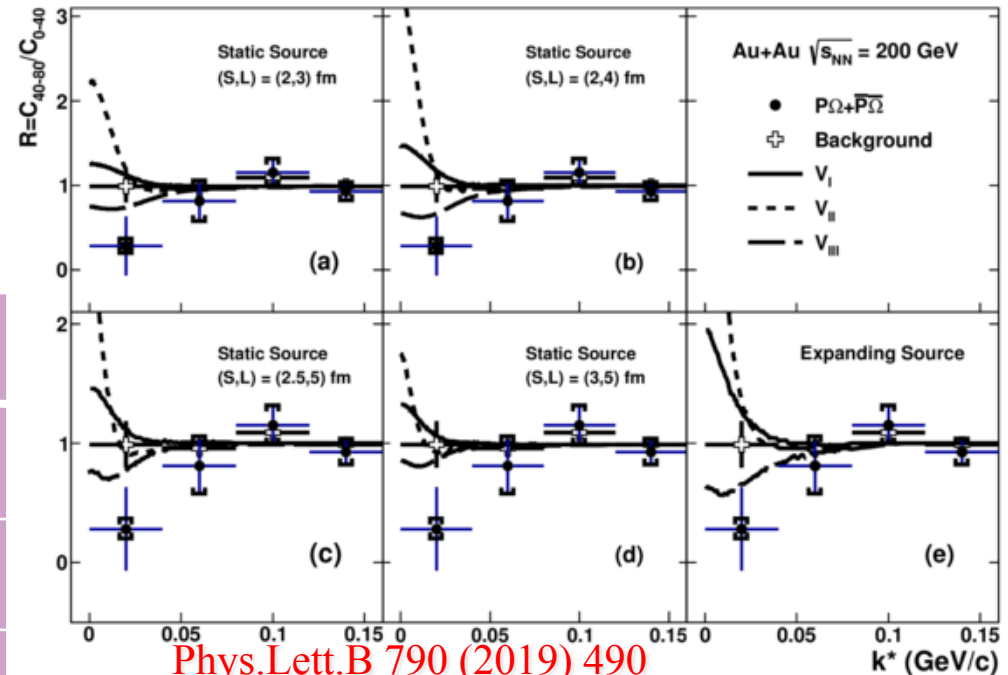
K. Morita et al. Phys. Rev. C 94, 031901 (2016)

	$V_1$	$V_2$	$V_3$
$E_{\text{bin}}$ [MeV]	-	6.3	26.9
$a_0$ [MeV]	-1.12	5.79	1.29
$r_{\text{eff}}$ [MeV]	-1.16	0.96	0.65

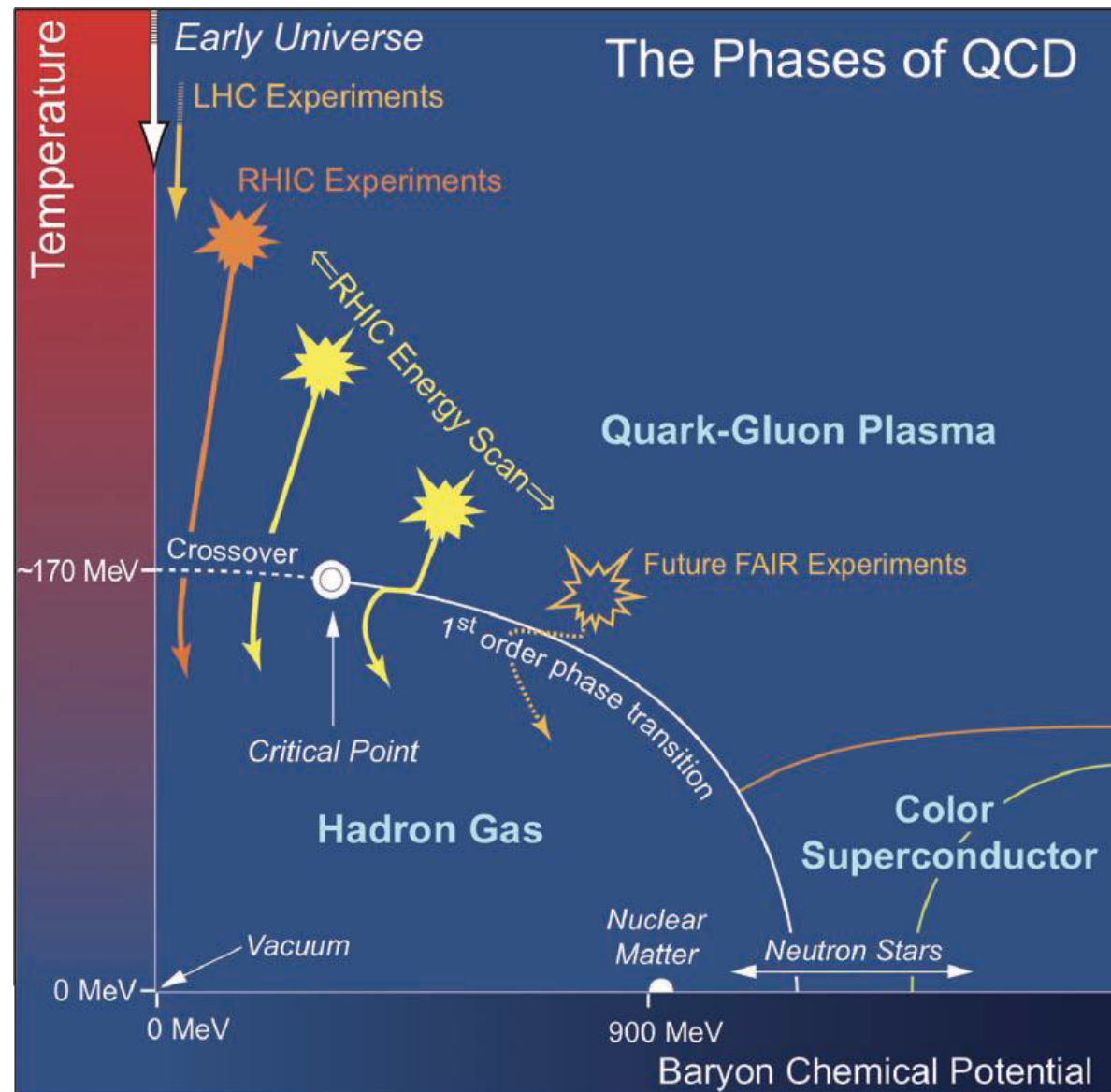
A comparison of the measured correlation functions from Au+Au collisions with theoretical predictions

**Scattering length is positive and favor  $p\Omega$  bound state hypothesis**

For strange meson correlations see talk by D. Pawłowska



## c) Program **B**eam **E**nergy **S**can

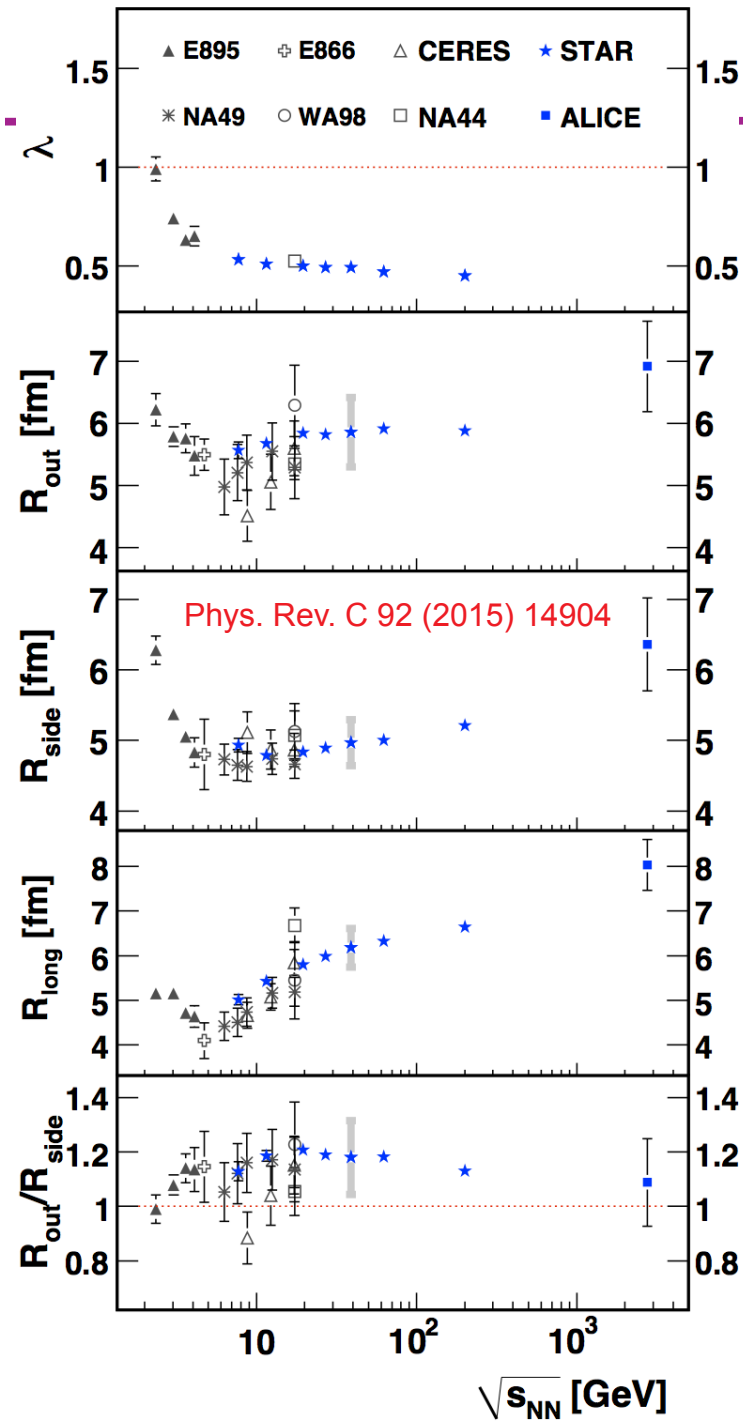


RHIC Top Energy  
 p+p, p+Al, p+Au, d+Au,  
 $^3\text{He}+\text{Au}$ , Cu+Cu, Cu+Au,  
 Ru+Ru, Zr+Zr, Au+Au, U+U  
 QCD at high energy  
 density/temperature  
 Properties of QGP, EoS

**B**eam **E**nergy **S**can  
 Au+Au 7.7-62 GeV  
 QCD phase transition  
 Search for critical point  
 Turn-off of QGP signatures

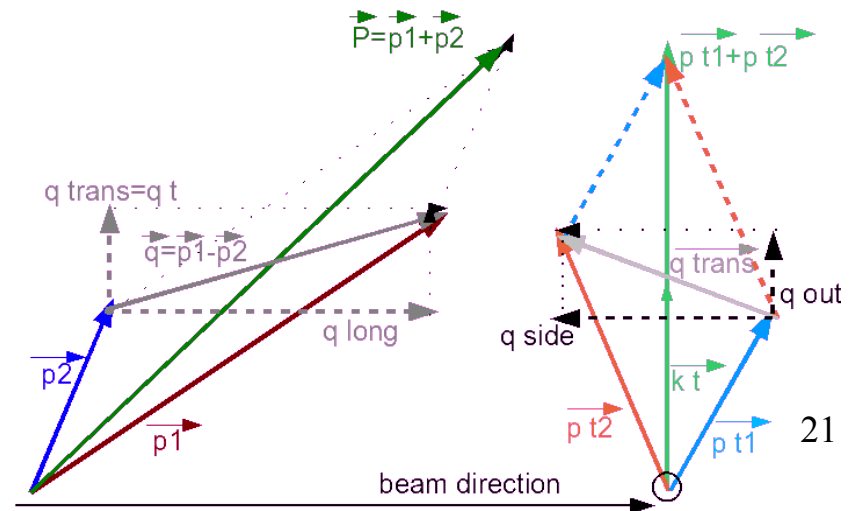
Fixed-Target Program  
 Au+Au = 3.0-7.7 GeV  
 High baryon density regime  
 with 420-720 MeV

# Program BES



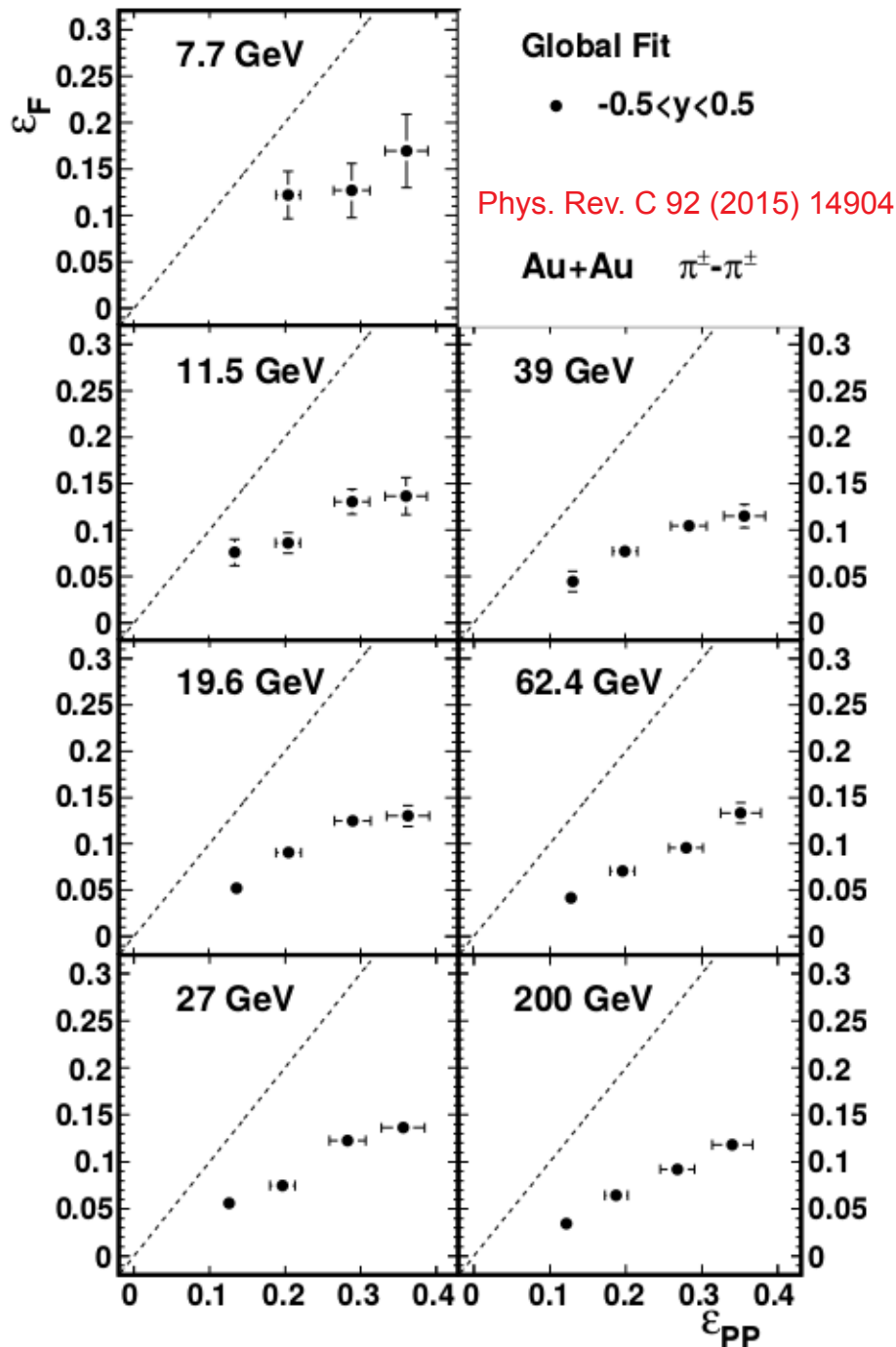
- $R_{\text{side}}$  spatial source evolution in the transverse direction
- $R_{\text{out}}$  related to spatial and time components
- $R_{\text{out}}/R_{\text{side}}$  (before!) signature of phase transition
- $R_{\text{out}}^2 - R_{\text{side}}^2 = \Delta\tau^2 \beta_t^2$ ;  $\Delta\tau$  – emission time
- $R_{\text{long}}$  temperature of kinetic freeze-out and source lifetime

$$C(\vec{q}) = (1 - \lambda) + K_{\text{Coul}}(q_{\text{inv}})\lambda \\ \times \exp(-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 - 2q_o q_s R_{os}^2 - 2q_o q_l R_{ol}^2)$$





# Program BES

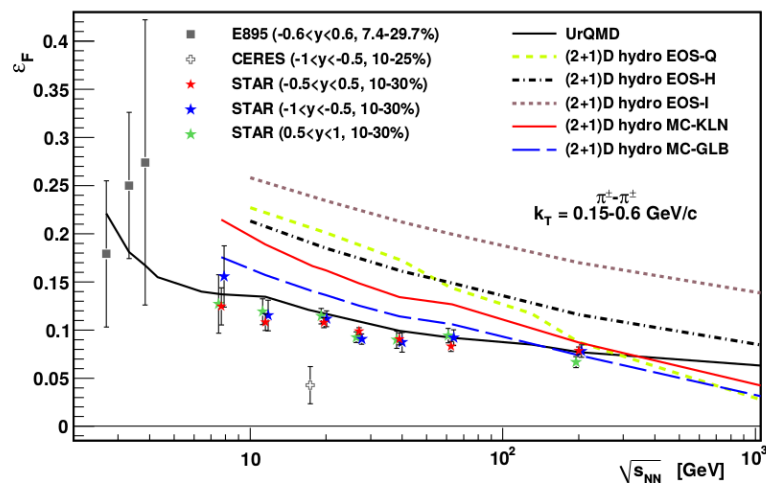


$$\varepsilon_{PP} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_x^2 + \sigma_y^2}, \quad \varepsilon_F = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

$$\sigma_x^2 = \{x^2\} - \{x\}^2 \text{ and } \sigma_y^2 = \{y^2\} - \{y\}^2$$

$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6,\dots} R_{\mu,n}^2 \cos(n\Phi) \quad (\mu = o, s, l, ol)$$

$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6,\dots} R_{\mu,n}^2 \sin(n\Phi) \quad (\mu = os)$$

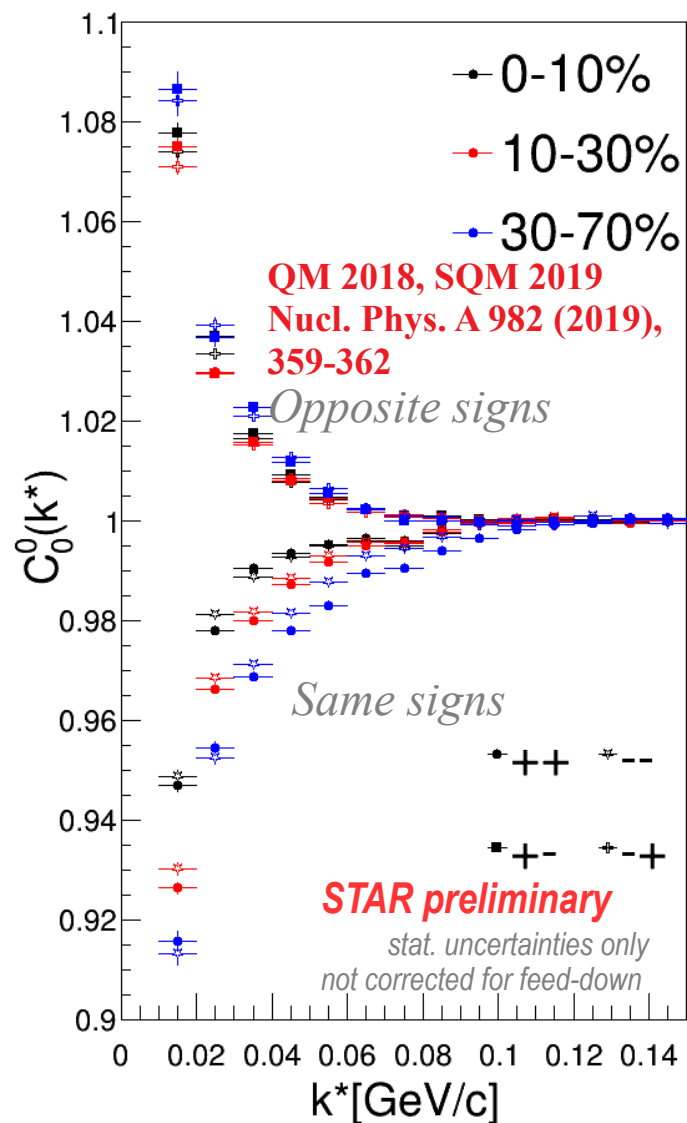


**System evolves faster in the reaction plane than in the direction perpendicular to it**

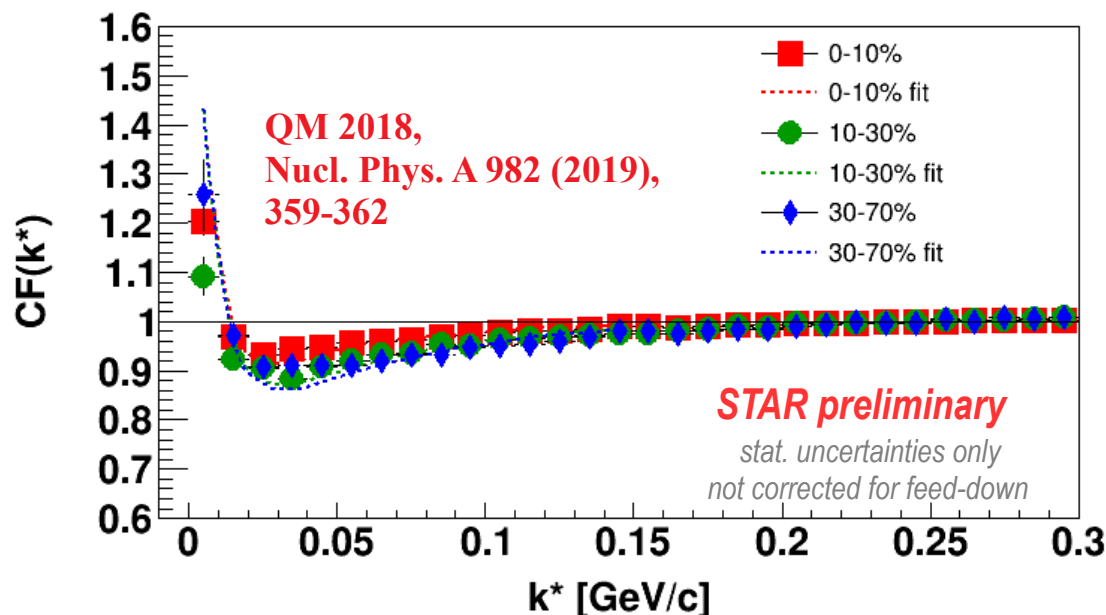


# Geometry: dependence on collision centrality

$\pi - K$  @ Au+Au 39 GeV



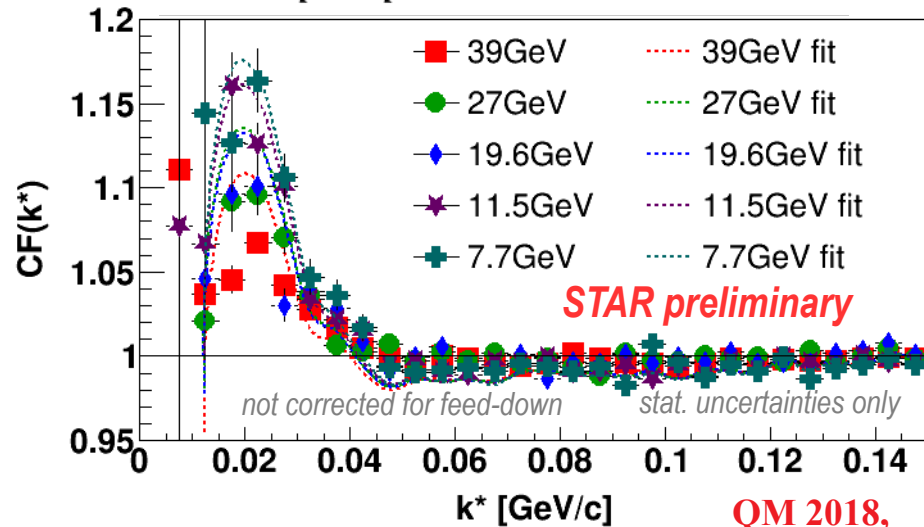
$p - \bar{p}$  @ Au+Au 39 GeV



Clear **centrality** dependence  
 $R(0-10\%) > R(10-30\%) > R(30-70\%)$

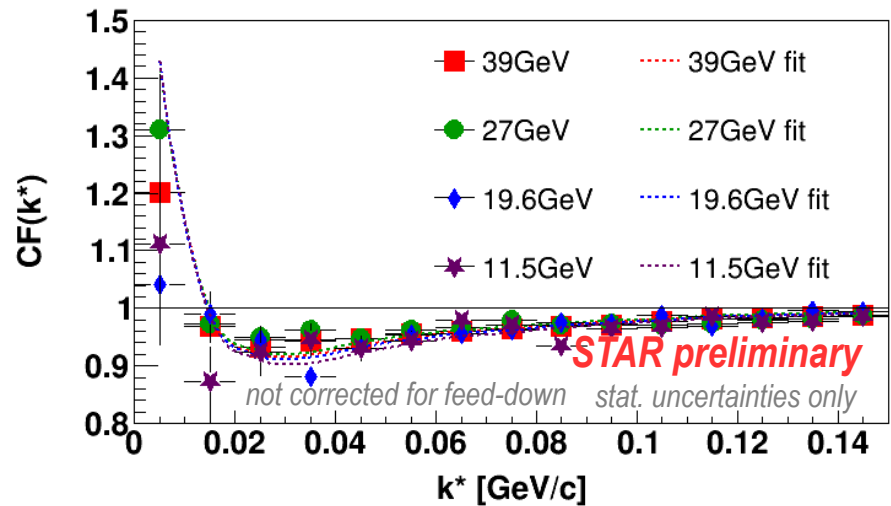
# Dependence on collision **energy**

$p - p$  : Au+Au 0-10%

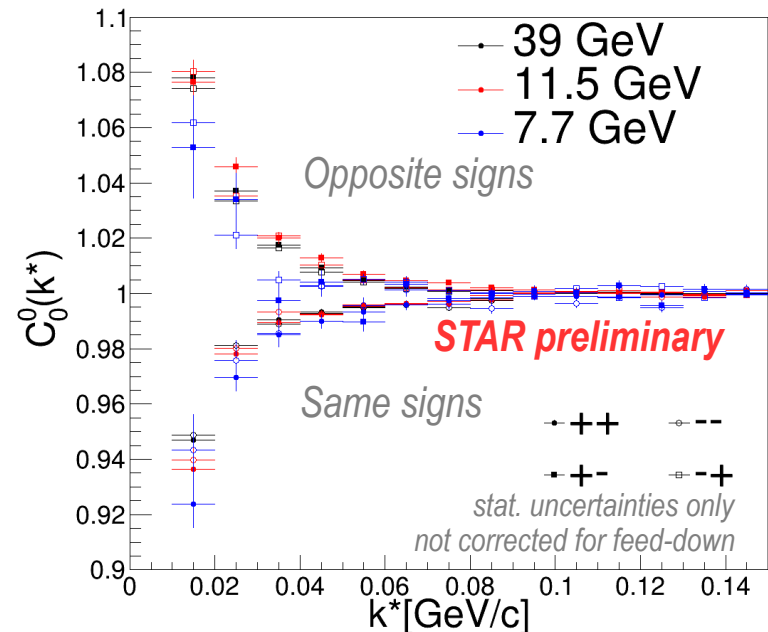


QM 2018,  
Nucl. Phys. A 982 (2019), 359-362

$p - \bar{p}$  : Au+Au 0-10%



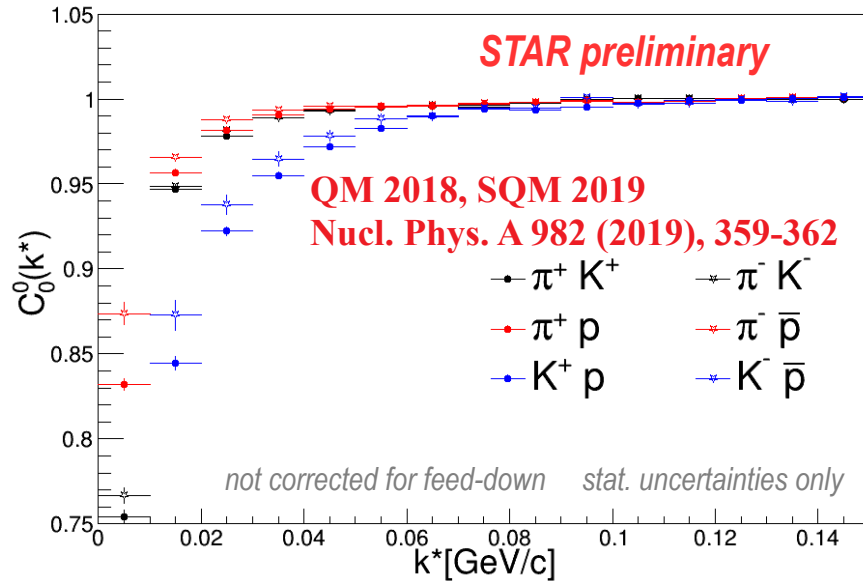
$\pi - K$  : Au+Au 0-10 %



Clear **energy** dependence  
 $R(39 \text{ GeV}) > R(11.5 \text{ GeV}) > R(7.7 \text{ GeV})$

# Dependence on interacting **system**

Same charges 0-10% @ Au+Au 39 GeV

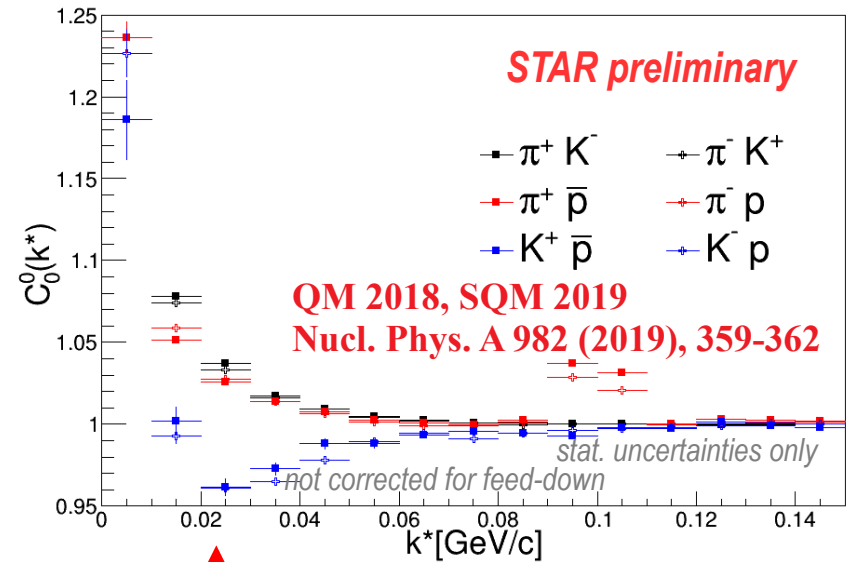


Determined by **Coulomb** Interactions

Clear **system** dependence

For non-identical particle correlations  
see talk by P. Szymański

Opposite charges 0-10% @ Au+Au 39 GeV



$C_0^0(K-p)$  different shape due to strong interaction

Determined by full **FSI**: **Coulomb** and **Strong** interactions (kaon-proton)

# Dynamics: Space-time asymmetry in emission process

$$C(q) = \sum_{l,m} C_l^m(q) Y_l^m(\theta, \phi)$$

$$C_l^m(q) = \int_{\Omega} C(q, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

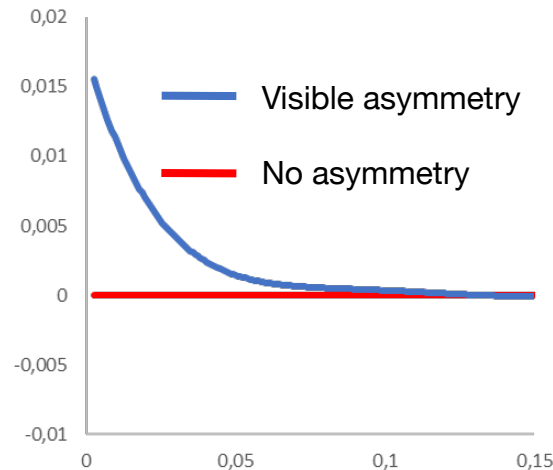
$\Omega$  – full solid angle

$Y_l^m(\theta, \phi)$  – spherical harmonic function

$q = |\mathbf{q}|$ ,  $\theta, \phi$  – spherical coordinates

**C00** → source **size**

**C11** → space-time **asymmetry**

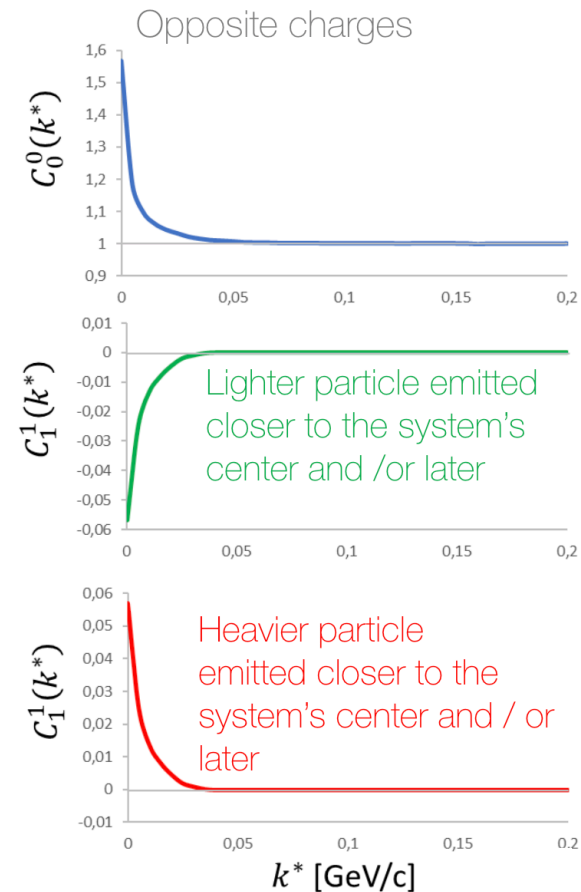
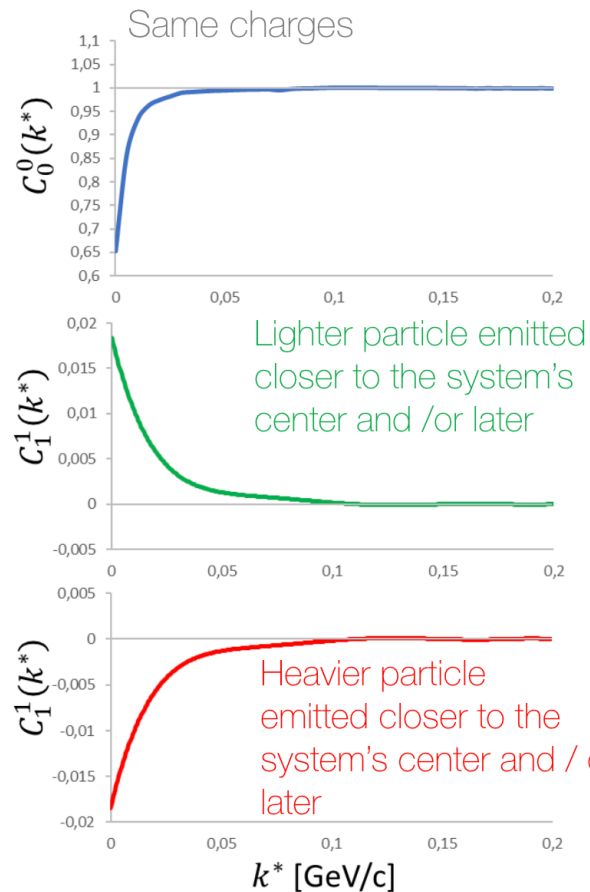


A. Kisiel  
Phys. Rev. C81:064906 2010

A. Kisiel and D. A. Brown  
Phys. Rev. C80:064911 2009

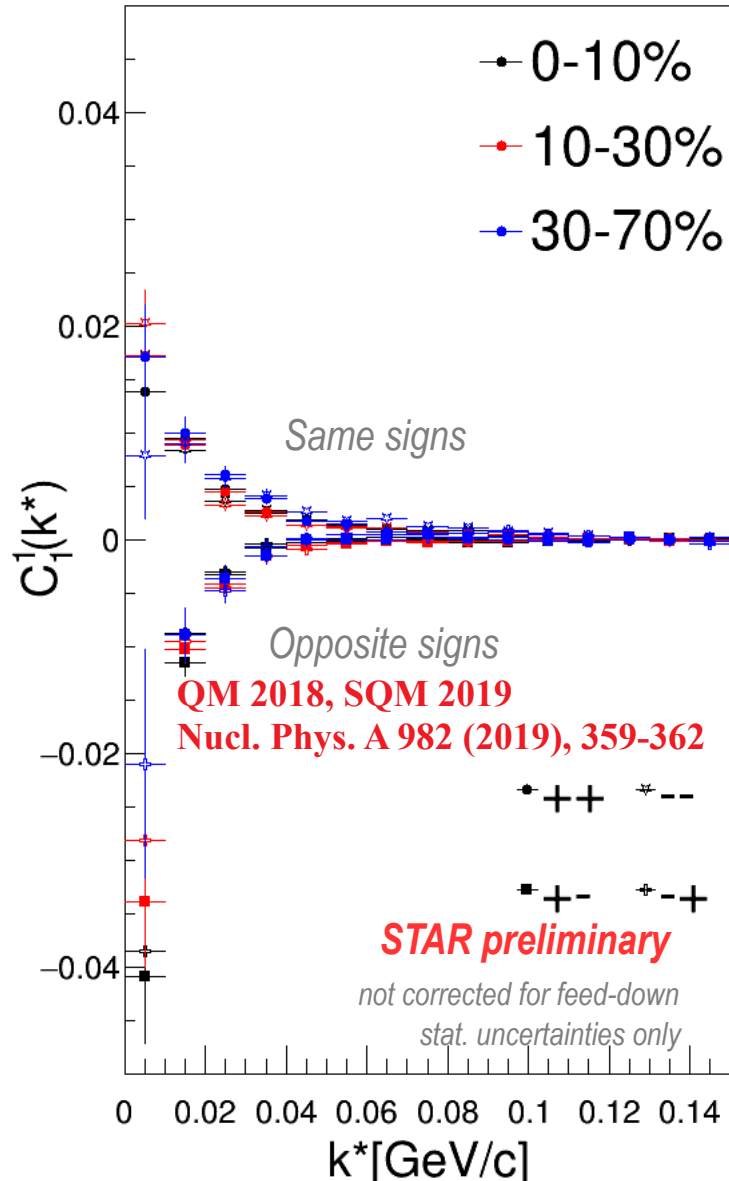
P. Danielewicz and S. Pratt.  
Phys. Lett. B618: 60 2005

P. Danielewicz and S. Pratt.  
Phys. Rev. C75:034907 2007



# Dynamics: centrality and energy dependencies

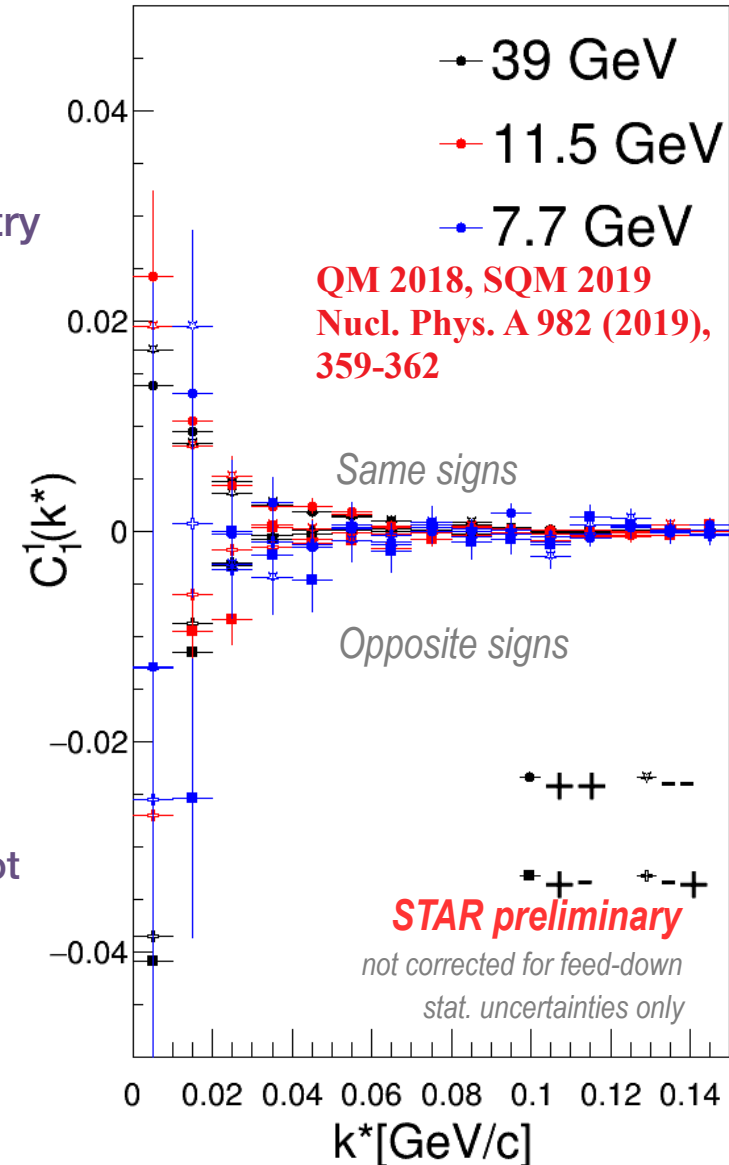
$\pi - K$  @ Au+Au 39 GeV



Clear signal of  
emission asymmetry

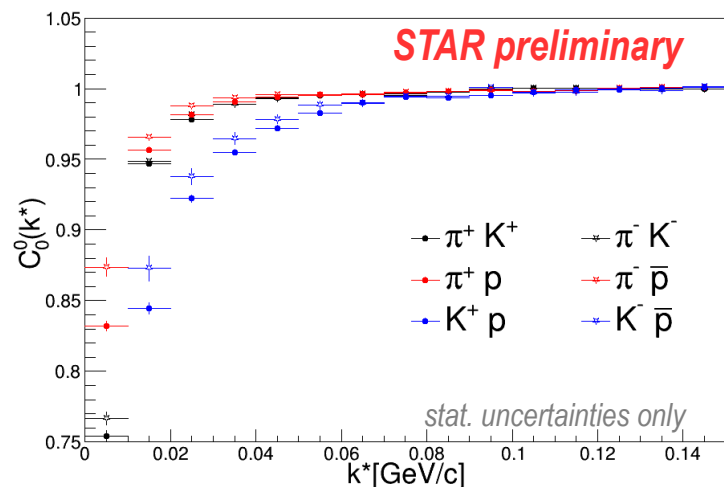
Asymmetry does not  
disappear in lower  
energies

$\pi - K$  : Au+Au 0-10%

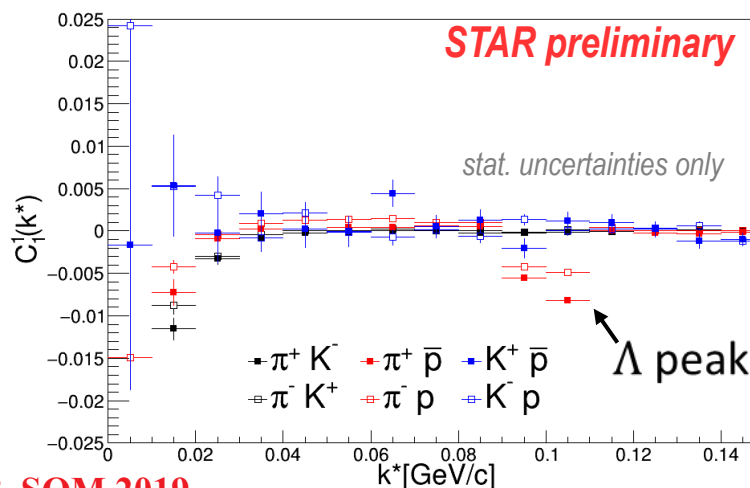
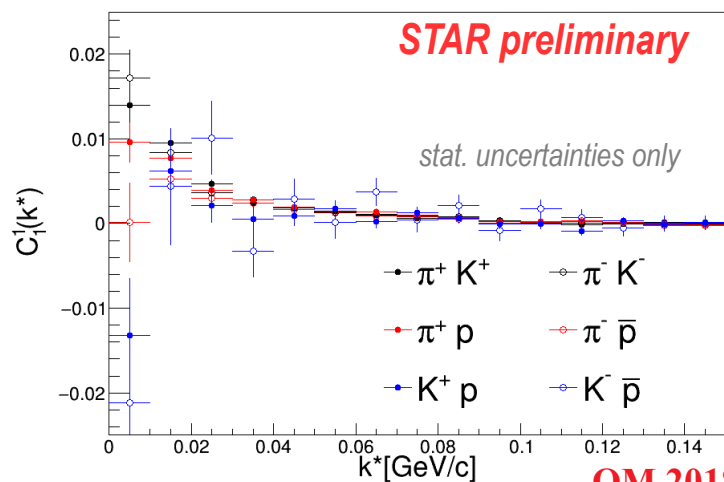
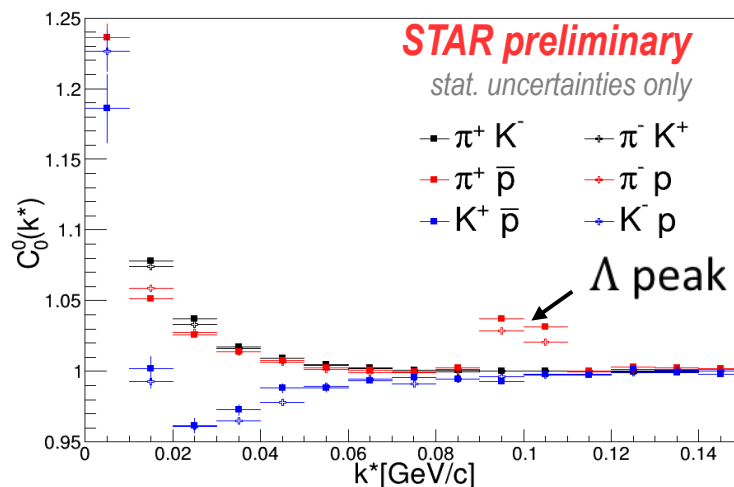


# Source dynamics: **system** dependence

Like-sign 0-10% @ Au+Au 39 GeV



Unlike-sign 0-10% @ Au+Au 39 GeV



Heavier particles  
directed towards  
edge of the  
source.

Heavier particles  
freeze-out earlier

Phys. Rev. C81:064906  
2010

QM 2018, SQM 2019  
Nucl. Phys. A 982 (2019),  
359-362



# Conclusions & Summary

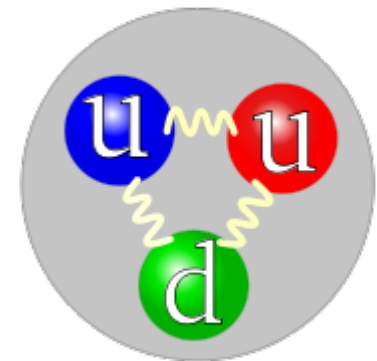


# Summary

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Correlation **femtoscscopy** probes the source:

- **geometry** (sizes)
- **dynamics** (evolution process, emission sequence, ..)
- **interactions** (strong, Coulomb)



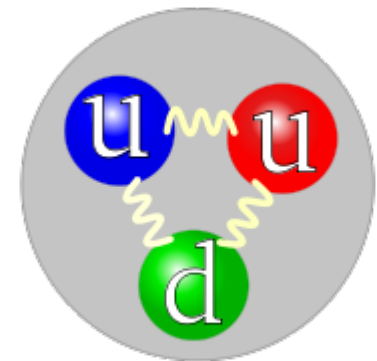
# Summary

---

Correlation **femtoscscopy** probes the source:

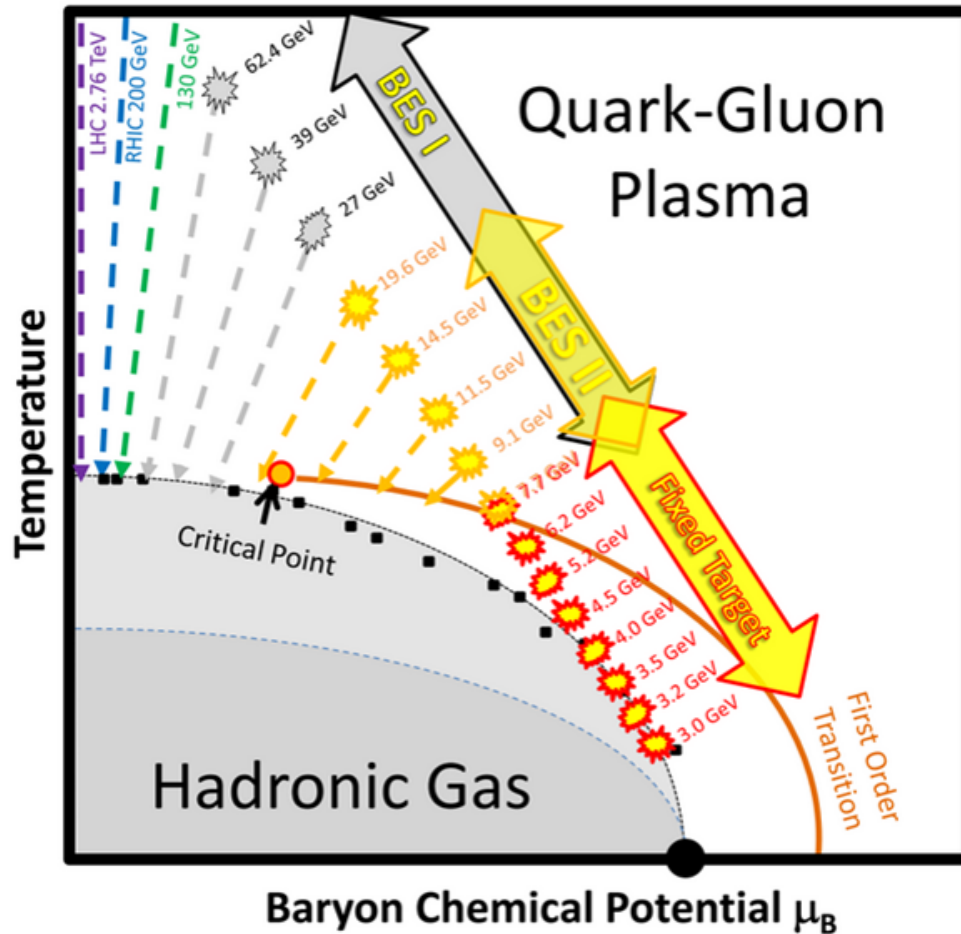
- **geometry** (sizes)
- **dynamics** (evolution process, emission sequence, ..)
- **interactions** (strong, Coulomb)

Thank you for Your attention



Back-up slides

# Program **B**eam **E**nergy **S**can



BES Program goals:

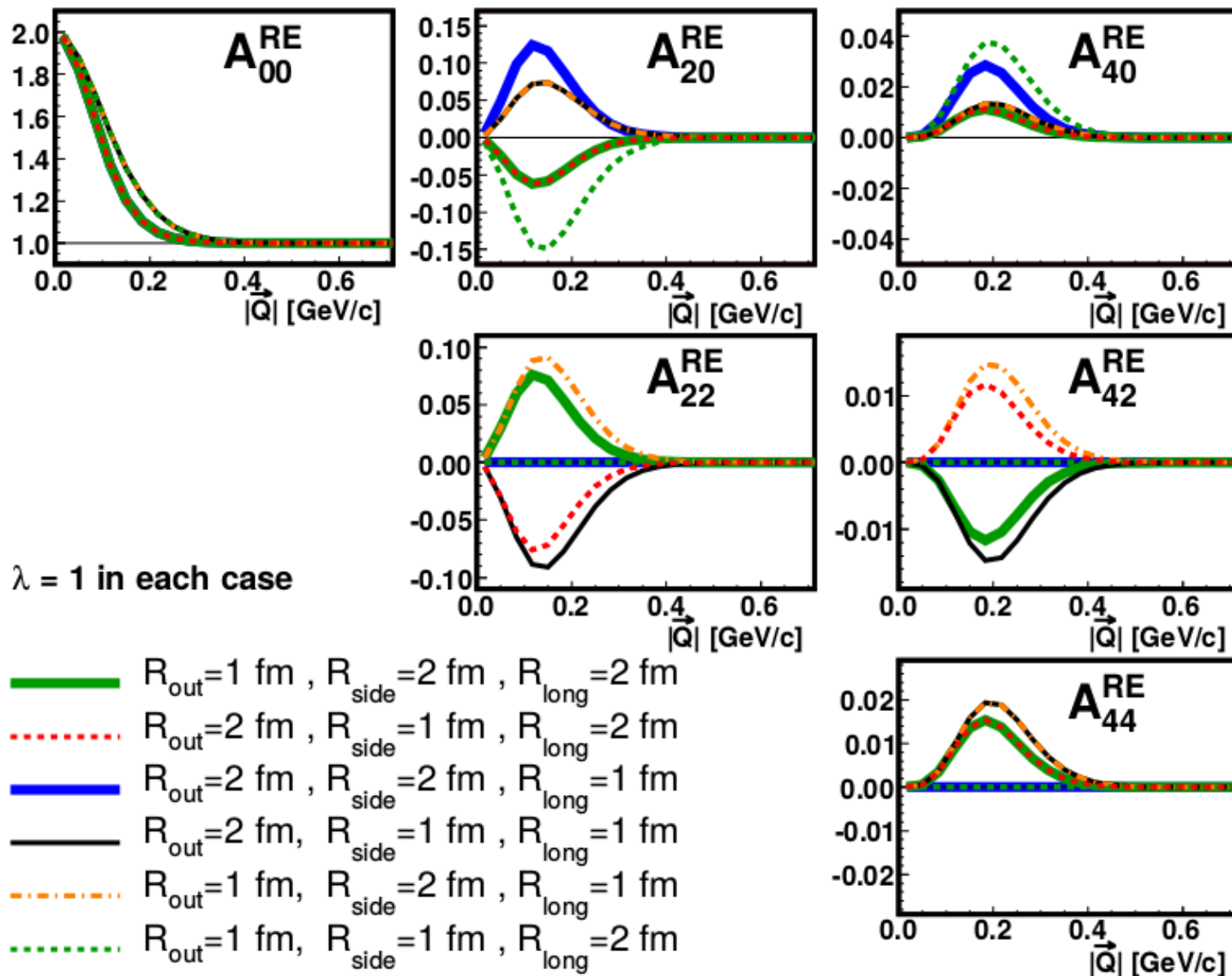
Study QCD Phase Diagram

1) localize where the QGP is not registered

2) signatures of the 1st order Phase transition

3) localize the Critical Point

# Spherical Harmonics



# Source dynamics

