Space-time evolution and description of the spin polarization in the Bjorken hydrodynamical scenario

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References:

Phys. Rev. C 99, 044910 (2019) [arXiv:1901.09655] Prog. Part. Nucl. Phys. 108 (2019) 103709 [arXiv:1811.04409]

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Dec 2 - Dec 6 Budapest, Hungary

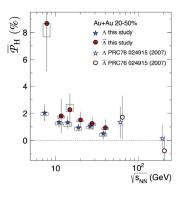


Outline:

- Motivation
- Methodology
- Results
- Summary and Future Work

Motivation:

First positive measurements of global spin polarization of Λ hyperons by STAR





 $\begin{array}{c} \text{thermal approach} \longrightarrow P_{\Lambda} \approx \frac{1}{2} \frac{\omega}{T} + \frac{\mu_{\Lambda} B}{T} \quad P_{\Lambda} \approx \frac{1}{2} \frac{\omega}{T} - \frac{\mu_{\Lambda} B}{T} \\ \text{Becattini, F., Karpenko, I., Lisa, M., Upsal, I., Voloshin, S., PRC 95, 054902 (2017)} \end{array}$

... the hottest, least viscous – and now, most vortical – fluid produced in the laboratory ...

$$\omega = \left(P_{\Lambda} + P_{\overline{\Lambda}}\right) k_B T / \hbar \sim 0.6 - 2.7 \times 10^{22} \mathrm{s}^{-1}$$

L. Adamczyk et al. (STAR) (2017), Nature 548 (2017) 62-65



Motivation:

 Non-central relativistic heavy ion collisions creates global rotation of matter. This may induce spin polarization reminding us of Einstein and de-Haas effect and Barnett effect.

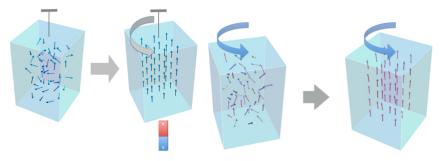


Figure: Einstein and De Haas and Barnett Effects

Motivation:

- Non-central relativistic heavy ion collisions creates global rotation of matter. This may induce spin polarization reminding us of Barnett effect and Einstein and de-Haas effect.
- Emerging particles are expected to be globally polarized with their spins on average pointing along the systems angular momentum.

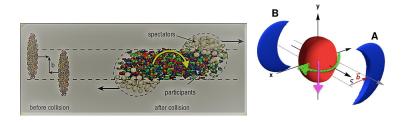
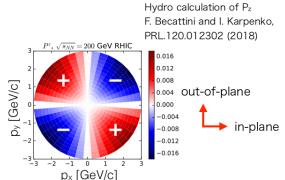


Figure: Schematic view of non-central heavy-ion collisions.

Other works:

• Other theoretical models used for the heavy-ions data interpretation dealt mainly with the spin polarization of particles at freeze-out, where the basic hydrodynamic quantity giving rise to spin polarization is the 'thermal vorticity' expressed as $\varpi_{\mu\nu} = -\frac{1}{2}(\partial_{\mu}\beta_{\nu} - \partial_{\nu}\beta_{\mu})$.

F. Becattini et.al.(Annals Phys. 338 (2013)), F. Becattini, L. Csernai, D. J. Wang (PRC 88, 034905), F. Becattini et.al.(PRC 95, 054902), Iu. Karpenko, F. Becattini (EPJC (2017) 77: 213), F. Becattini, Iu. Karpenko(PRL 120, 012302 (2018))



Our hydrodynamic framework:

- Solving the standard perfect-fluid hydrodynamic equations without spin
- Determination of the spin evolution in the hydrodynamic background
- Determination of the Pauli-Lubanski (PL) vector on the freeze-out hypersurface
- Calculation of the spin polarization of particles in their rest frame
- The spin polarization obtained is a function of the three-momenta of particles and can be directly compared with the experiment

Our hydrodynamic framework:

- In this work, we use relativistic hydrodynamic equations for polarized spin 1/2 particles to determine the space-time evolution of the spin polarization in the system using forms of the energy-momentum and spin tensors proposed by de Groot, van Leeuwen, and van Weert (GLW).
 - S. R. De Groot, Relativistic Kinetic Theory. Principles and Applications (1980).
- The calculations are done in a boost-invariant and transversely homogeneous setup. We show how the formalism of hydrodynamics with spin can be used to determine physical observables related to the spin polarization required for the modelling of the experimental data.

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Wojciech Florkowski et.al.(Phys. Rev. C 99, 044910), Wojciech Florkowski et.al.(Phys. Rev. C 97, 041901), Wojciech Florkowski et.al.(Phys. Rev. D 97, 116017).
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• Our hydrodynamic formulation does not allow for arbitrary large values of the spin polarization tensor, hence we have restricted ourselves to the leading order terms in the $\omega_{\mu\nu}$.

Spin polarization tensor:

The spin polarization tensor $\omega_{\mu\nu}$ is anti-symmetric and can be defined by the four-vectors κ^{μ} and ω^{μ} ,

$$\omega_{\mu\nu} = \kappa_{\mu} U_{\nu} - \kappa_{\nu} U_{\mu} + \epsilon_{\mu\nu\alpha\beta} U^{\alpha} \omega^{\beta},$$

Using these constraints,

$$\kappa \cdot U = 0, \quad \omega \cdot U = 0$$

We can express κ_{μ} and ω_{μ} in terms of $\omega_{\mu\nu}$, namely

$$\kappa_{\mu} = \omega_{\mu\alpha} U^{\alpha}, \quad \omega_{\mu} = \frac{1}{2} \epsilon_{\mu\alpha\beta\gamma} \omega^{\alpha\beta} U^{\gamma}$$

Conservation of charge:

$$\partial_{\alpha}N^{\alpha}(x)=0,$$
 where, $N^{\alpha}=nU^{\alpha}, \quad n=4\sinh(\xi) \ n_{(0)}(T).$

The quantity $n_{(0)}(T)$ defines the number density of spinless and neutral massive Boltzmann particles,

$$n_{(0)}(T) = \langle p \cdot U \rangle_0 = \frac{1}{2\pi^2} T^3 \, \hat{m}^2 K_2(\hat{m})$$

where, $\langle \cdots \rangle_0 \equiv \int dP (\cdots) e^{-\beta \cdot p}$ denotes the thermal average, $\hat{m} \equiv m/T$ denotes the ratio of the particle mass (m) and the temperature (T), and $K_2(\hat{m})$ denotes the modified Bessel function.

The factor, $4 \sinh(\xi) = 2 \left(e^{\xi} - e^{-\xi}\right)$ accounts for spin degeneracy and presence of both particles and antiparticles in the system and the variable ξ denotes the ratio of the chemical potential μ and the temperature T, $\xi = \mu/T$.

Conservation of energy and linear momentum:

$$\partial_{\alpha} T_{GLW}^{\alpha\beta}(x) = 0$$

where the energy-momentum tensor $T_{GLW}^{\alpha\beta}$ has the perfect-fluid form:

$$T_{GLW}^{\alpha\beta}(x) = (\varepsilon + P)U^{\alpha}U^{\beta} - Pg^{\alpha\beta}$$

with energy density $\varepsilon = 4 \cosh(\xi) \varepsilon_{(0)}(T)$ and pressure $P = 4 \cosh(\xi) P_{(0)}(T)$

The auxiliary quantities are:

$$\varepsilon_{(0)}(T) = \langle (p \cdot U)^2 \rangle_0$$
 and $P_{(0)}(T) = -(1/3)\langle p \cdot p - (p \cdot U)^2 \rangle_0$ are the energy density and pressure of the spin-less ideal gas respectively. In case of ideal relativistic gas of classical massive particles,

$$\varepsilon_{(0)}(T) = \frac{1}{2\pi^2} T^4 \,\hat{m}^2 \Big[3K_2(\hat{m}) + \hat{m}K_1(\hat{m}) \Big], \quad P_{(0)}(T) = Tn_{(0)}(T)$$

Above conservation laws provide closed system of five equations for five unknown functions: ξ , T, and three independent components of U^{μ} .

Conservation of total angular momentum:

$$\partial_{\mu}J^{\mu,\alpha\beta}(x) = 0$$
, $J^{\mu,\alpha\beta}(x) = -J^{\mu,\beta\alpha}(x)$

Total angular momentum consists of orbital and spin parts:

$$J^{\mu,\alpha\beta}(x) = L^{\mu,\alpha\beta}(x) + S^{\mu,\alpha\beta}(x),$$

$$L^{\mu,\alpha\beta}(x) = x^{\alpha} T^{\mu\beta}(x) - x^{\beta} T^{\mu\alpha}(x)$$

Since the energy-momentum tensor is symmetric, the conservation of the angular momentum implies the conservation of its spin part.

$$\partial_{\lambda}J^{\lambda,\mu\nu}(x) = 0, \quad \partial_{\mu}T^{\mu\nu}(x) = 0 \implies \partial_{\lambda}S^{\lambda,\mu\nu}(x) = T^{\nu\mu}(x) - T^{\mu\nu}(x)$$

Hence, the spin tensor $S^{\mu,\alpha\beta}(x)$ is separately conserved in GLW formulation.

Conservation of spin angular momentum:

$$\partial_{\alpha} S_{GLW}^{\alpha,\beta\gamma}(x) = 0$$

GLW spin tensor in the leading order of $\omega_{\mu\nu}$ is:

$$S_{GLW}^{\alpha,\beta\gamma} = \cosh(\xi) \left(n_{(0)}(T) U^{\alpha} \omega^{\beta\gamma} + S_{\Delta GLW}^{\alpha,\beta\gamma} \right)$$

Here, $\omega^{\beta\gamma}$ is known as spin polarization tensor, whereas the auxiliary tensor $S_{ACIW}^{\alpha,\beta\gamma}$ is:

$$S_{\Delta GLW}^{\alpha,\beta\gamma} = \mathcal{A}_{(0)} U^{\alpha} U^{\delta} U^{[\beta} \omega_{\delta}^{\gamma]} + \mathcal{B}_{(0)} \left(U^{[\beta} \Delta^{\alpha\delta} \omega_{\delta}^{\gamma]} + U^{\alpha} \Delta^{\delta[\beta} \omega_{\delta}^{\gamma]} + U^{\delta} \Delta^{\alpha[\beta} \omega_{\delta}^{\gamma]} \right),$$

with,

$$\mathcal{B}_{(0)} = -\frac{2}{\hat{m}^2} s_{(0)}(T)$$
$$\mathcal{A}_{(0)} = -3\mathcal{B}_{(0)} + 2n_{(0)}(T)$$

Basis for boost invariant and transversely homogeneous systems:

For our calculations, it is useful to introduce a local basis consisting of following 4-vectors,

$$U^{\alpha} = \frac{1}{\tau} (t, 0, 0, z) = (\cosh(\eta), 0, 0, \sinh(\eta)),$$
 $X^{\alpha} = (0, 1, 0, 0),$
 $Y^{\alpha} = (0, 0, 1, 0),$
 $Z^{\alpha} = \frac{1}{\tau} (z, 0, 0, t) = (\sinh(\eta), 0, 0, \cosh(\eta)).$

where, $\tau = \sqrt{t^2 - z^2}$ is the longitudinal proper time and $\eta = \ln((t+z)/(t-z))/2$ is the space-time rapidity.

The basis vectors satisfy the following normalization and orthogonal conditions: $U \cdot U = 1$

Boost-invariant form for the spin polarization tensor:

We use the following decomposition of the vectors κ^{μ} and ω^{μ} ,

$$\begin{array}{rcl} \kappa^{\alpha} & = & C_{\kappa U}U^{\alpha} + C_{\kappa X}X^{\alpha} + C_{\kappa Y}Y^{\alpha} + C_{\kappa Z}Z^{\alpha}, \\ \omega^{\alpha} & = & C_{\omega U}U^{\alpha} + C_{\omega X}X^{\alpha} + C_{\omega Y}Y^{\alpha} + C_{\omega Z}Z^{\alpha}. \end{array}$$

Here, the scalar coefficients are functions of the proper time τ only due to boost invariance. Since $\kappa \cdot U = 0$, $\omega \cdot U = 0$, therefore

$$\kappa^{\alpha} = C_{\kappa X} X^{\alpha} + C_{\kappa Y} Y^{\alpha} + C_{\kappa Z} Z^{\alpha},$$

$$\omega^{\alpha} = C_{\omega X} X^{\alpha} + C_{\omega Y} Y^{\alpha} + C_{\omega Z} Z^{\alpha}.$$

$$\omega_{\mu\nu}=\kappa_{\mu}U_{\nu}-\kappa_{\nu}U_{\mu}+\epsilon_{\mu\nu\alpha\beta}U^{\alpha}\omega^{\beta}$$
 can be written as,

$$\omega_{\mu\nu} = C_{\kappa Z}(Z_{\mu}U_{\nu} - Z_{\nu}U_{\mu}) + C_{\kappa X}(X_{\mu}U_{\nu} - X_{\nu}U_{\mu}) + C_{\kappa Y}(Y_{\mu}U_{\nu} - Y_{\nu}U_{\mu}) + \epsilon_{\mu\nu\alpha\beta}U^{\alpha}(C_{\omega Z}Z^{\beta} + C_{\omega X}X^{\beta} + C_{\omega Y}Y^{\beta})$$

In the plane z = 0 we find:

$$\omega_{\mu\nu} = \begin{bmatrix} 0 & C_{\kappa X} & C_{\kappa Y} & C_{\kappa Z} \\ -C_{\kappa X} & 0 & -C_{\omega Z} & C_{\omega Y} \\ -C_{\kappa Y} & C_{\omega Z} & 0 & -C_{\omega X} \\ -C_{\kappa Z} & -C_{\omega Y} & C_{\omega X} & 0 \end{bmatrix}$$

Boost-Invariant form of fluid dynamics with spin:

Conservation law of charge can be written as:

$$U^{\alpha}\partial_{\alpha}n + n\partial_{\alpha}U^{\alpha} = 0$$

Therefore, for Bjorken type of flow we can write,

$$\dot{n} + \frac{n}{\tau} = 0$$

Conservation law of energy-momentum can be written as:

$$U^{\alpha}\partial_{\alpha}\varepsilon + (\varepsilon + P)\partial_{\alpha}U^{\alpha} = 0$$

Hence for the Bjorken flow,

$$\dot{\varepsilon} + \frac{(\varepsilon + P)}{\tau} = 0$$

Boost-Invariant form of fluid dynamics with spin:

Using the equations,

$$\begin{split} S_{\Delta GLW}^{\alpha,\beta\gamma} &= \mathcal{A}_{(0)} U^{\alpha} U^{\delta} U^{[\beta} \omega^{\gamma]}_{\delta} \\ + \mathcal{B}_{(0)} \left(U^{[\beta} \Delta^{\alpha\delta} \omega^{\gamma]}_{\delta} + U^{\alpha} \Delta^{\delta[\beta} \omega^{\gamma]}_{\delta} + U^{\delta} \Delta^{\alpha[\beta} \omega^{\gamma]}_{\delta} \right), \\ & \qquad \qquad \text{and} \\ S_{GLW}^{\alpha,\beta\gamma} &= \cosh(\xi) \left(n_{(0)} (T) U^{\alpha} \omega^{\beta\gamma} + S_{\Delta GLW}^{\alpha,\beta\gamma} \right) \\ & \qquad \qquad \qquad \text{in} \\ \partial_{\alpha} S_{GLW}^{\alpha,\beta\gamma} (x) &= 0 \end{split}$$

Contracting the final equation with $U_{\beta}X_{\gamma}$, $U_{\beta}Y_{\gamma}$, $U_{\beta}Z_{\gamma}$, $Y_{\beta}Z_{\gamma}$, $X_{\beta}Z_{\gamma}$ and $X_{\beta}Y_{\gamma}$.

$$\begin{bmatrix} \mathcal{L}(\tau) & 0 & 0 & 0 & 0 & 0 \\ 0 & \mathcal{L}(\tau) & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \mathcal{L}(\tau) & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \mathcal{P}(\tau) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \mathcal{P}(\tau) & 0 \\ 0 & 0 & 0 & 0 & 0 & \mathcal{P}(\tau) \end{bmatrix} \begin{bmatrix} \dot{\mathcal{L}}_{\kappa X} \\ \dot{\mathcal{L}}_{\kappa Y} \\ \dot{\mathcal{L}}_{\omega Y} \\ \dot{\mathcal{L}}_{\omega Y} \\ \dot{\mathcal{L}}_{\omega Z} \\ \dot{\mathcal{L}}_{\omega Z} \\ \dot{\mathcal{L}}_{\omega Z} \end{bmatrix} = \begin{bmatrix} \mathcal{Q}_{1}(\tau) & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \mathcal{Q}_{1}(\tau) & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \mathcal{Q}_{2}(\tau) & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \mathcal{R}_{1}(\tau) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \mathcal{R}_{1}(\tau) & 0 & 0 \\ 0 & 0 & 0 & 0 & \mathcal{R}_{1}(\tau) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \mathcal{R}_{2}(\tau) \end{bmatrix} \begin{bmatrix} \mathcal{L}_{\kappa X} \\ \mathcal{L}_{\kappa Y} \\ \mathcal{L}_{\kappa Z} \\ \mathcal{L}_{\omega Z} \\$$

where,
$$\mathcal{L}(\tau) = \mathcal{A}_1 - \frac{1}{2}\mathcal{A}_2 - \mathcal{A}_3,$$

$$\mathcal{P}(\tau) = \mathcal{A}_1,$$

$$\mathcal{Q}_1(\tau) = -\left[\dot{\mathcal{L}} + \frac{1}{\tau}\left(\mathcal{L} + \frac{1}{2}\mathcal{A}_3\right)\right],$$

$$\mathcal{A}_2 = \cosh(\xi)\left(\eta_{(0)} - \mathcal{B}_{(0)}\right),$$

$$\mathcal{A}_2 = \cosh(\xi)\left(\mathcal{A}_{(0)} - \mathcal{B}_{(0)}\right),$$

$$\mathcal{A}_3 = \cosh(\xi)\mathcal{B}_{(0)}$$

$$\mathcal{R}_1(\tau) = -\left[\dot{\mathcal{P}} + \frac{1}{\tau}\left(\mathcal{P} - \frac{1}{2}\mathcal{A}_3\right)\right],$$

$$\mathcal{R}_2(\tau) = -\left(\dot{\mathcal{P}} + \frac{\mathcal{P}}{\tau}\right).$$

Background evolution:

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Initial baryon chemical potential \mu_0=800~{\rm MeV}
Initial temperature T_0=155~{\rm MeV}
Particle mass m=1116~{\rm MeV}
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Initial and final proper time is $\tau_0 = 1$ fm and $\tau_f = 10$ fm, respectively.

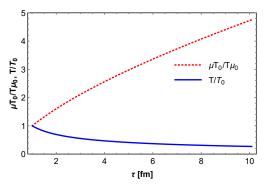


Figure: Proper-time dependence of T divided by its initial value T_0 (solid line) and the ratio of baryon chemical potential μ and temperature T re-scaled by the initial ratio μ_0/T_0 (dotted line) for a boost-invariant one-dimensional expansion,

Spin polarization evolution:

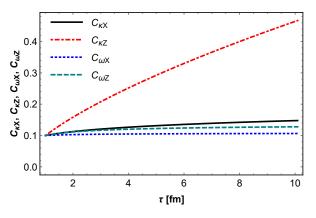


Figure: Proper-time dependence of the coefficients $C_{\kappa X}$, $C_{\kappa Z}$, $C_{\omega X}$ and $C_{\omega Z}$. The coefficients $C_{\kappa Y}$ and $C_{\omega Y}$ satisfy the same differential equations as the coefficients $C_{\kappa X}$ and $C_{\omega X}$.

Spin polarization of particles at the freeze-out:

Average spin polarization per particle $\langle \pi_{\mu}(p) \rangle$ is given as:

$$\langle \pi_{\mu} \rangle = \frac{E_{p} \frac{d\Pi_{\mu}(p)}{d^{3}p}}{E_{p} \frac{d\mathcal{N}(p)}{d^{3}p}}$$

where, the total value of the Pauli-Lubański vector for particles with momentum p is:

$$E_{\rho} \frac{d\Pi_{\mu}(\rho)}{d^{3}p} = -\frac{\cosh(\xi)}{(2\pi)^{3}m} \int \Delta\Sigma_{\lambda} p^{\lambda} e^{-\beta \cdot p} \, \tilde{\omega}_{\mu\beta} p^{\beta}$$

momentum density of all particles is given by:

$$E_p \frac{d\mathcal{N}(p)}{d^3p} = \frac{4\cosh(\xi)}{(2\pi)^3} \int \Delta\Sigma_{\lambda} p^{\lambda} e^{-\beta \cdot p}$$

and freeze-out hypersurface is defined as:

$$\Delta\Sigma_{\lambda} = U_{\lambda} dx dy \, \tau d\eta$$

Assuming that freeze-out takes place at a constant value of τ and parameterizing the particle four-momentum p^{λ} in terms of the transverse mass m_{T} and rapidity y_{p} , we get:

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Boost to the local rest frame (LRF) of the particle:

Polarization vector $\langle \pi_{\mu}^{\star} \rangle$ in the local rest frame of the particle can be obtained by using the canonical boost. Using the parametrizations $E_p = m_T \cosh(y_p)$ and $p_z = m_T \sinh(y_p)$ and applying the appropriate Lorentz transformation we get,

$$\langle \boldsymbol{\pi}_{\mu}^{\star} \rangle = -\frac{1}{8m} \begin{bmatrix} 0 \\ \left(\frac{\sinh(y_{r})_{P_{r}}}{m_{r}\cosh(y_{r})+m}\right) \left[\chi\left(C_{\kappa x}\rho_{y} - C_{\kappa Y}\rho_{x}\right) + 2C_{\omega z}m_{T}\right] + \frac{\chi_{P_{r}}\cosh(y_{r})\left(C_{\omega x}\rho_{x} + C_{\omega Y}\rho_{x}\right)}{m_{r}\cosh(y_{r})+m} + 2C_{\kappa z}\rho_{y} - \chi C_{\omega x}m_{T} \\ \left(\frac{\sinh(y_{r})_{P_{r}}}{m_{r}\cosh(y_{r})+m}\right) \left[\chi\left(C_{\kappa x}\rho_{y} - C_{\kappa Y}\rho_{x}\right) + 2C_{\omega z}m_{T}\right] + \frac{\chi_{P_{r}}\cosh(y_{r})\left(C_{\omega x}\rho_{x} + C_{\omega Y}\rho_{x}\right)}{m_{r}\cosh(y_{r})+m} - 2C_{\kappa z}\rho_{x} - \chi C_{\omega Y}m_{T} \\ - \left(\frac{m\cosh(y_{r}) + m_{r}}{m_{r}\cosh(y_{r}) + m}\right) \left[\chi\left(C_{\kappa x}\rho_{y} - C_{\kappa Y}\rho_{x}\right) + 2C_{\omega z}m_{T}\right] - \frac{\chi_{m}\sinh(y_{r})\left(C_{\omega x}\rho_{x} + C_{\omega Y}\rho_{x}\right)}{m_{r}\cosh(y_{r}) + m} \end{bmatrix}$$

where,

$$\chi(\hat{m}_T) = (K_0(\hat{m}_T) + K_2(\hat{m}_T))/K_1(\hat{m}_T),$$

 $\hat{m}_T = m_T/T$

Momentum dependence of polarization:

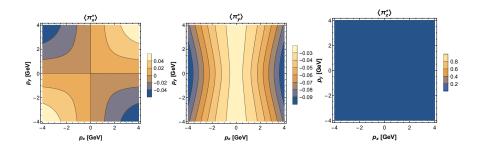
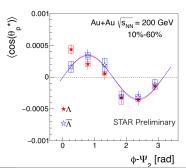


Figure: Components of the PRF mean polarization three-vector of Λ 's. The results obtained with the initial conditions $\mu_0=800$ MeV, $T_0=155$ MeV, $\boldsymbol{C}_{\kappa,0}=(0,0,0)$, and $\boldsymbol{C}_{\omega,0}=(0,0.1,0)$ for $y_p=0$.

Summary:

- We have discussed relativistic hydrodynamics with spin based on the GLW formulation of energy-momentum and spin tensors.
- For boost invariant and transversely homogeneous set-up we show how our hydrodynamic framework with spin can be used to determine the spin polarization observables measured in heavy ion collisions.
- ullet Since we worked with 0+1 dimensional expansion, our results cannot be compared with the experimental data.
- Our future work is to extend our hydrodynamic approach for 1+3 dimensions and interpret the experimental data correctly.



Thank you for your attention!

Back-Up Slides

Measuring polarization in experiment:

Parity-violating decay of hyperons

Daughter baryon is preferentially emitted in the direction of hyperon's spin (opposite for anti-particle)

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_{\rm H} \mathbf{P}_{\rm H} \cdot \mathbf{p}_{\rm p}^*)$$

PH: A polarization

 p_p *: proton momentum in the Λ rest frame α_H : Λ decay parameter

 $(\alpha \wedge = -\alpha \hat{\Lambda} = 0.642 \pm 0.013)$



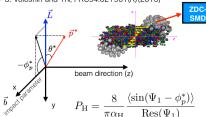


C. Patrignani et al. (PDG), Chin. Phys. C 40, 100001 (2016)

Projection onto the transverse plane

Angular momentum direction can be determined by spectator deflection (spectators deflect outwards)

- S. Voloshin and TN, PRC94.021901(R)(2016)



 Ψ_1 : azimuthal angle of b

 $\phi_{\,\mathrm{p}}$: ϕ of daughter proton in Λ rest frame STAR, PRC76, 024915 (2007)

Source: T. Niida, WWND 2019



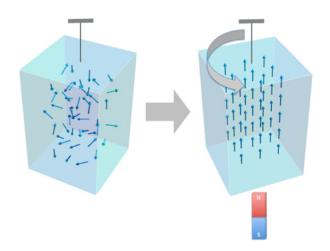


Figure: Einstein-De Haas Effect

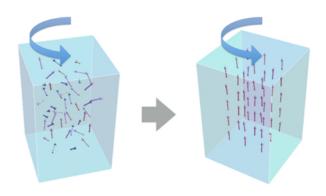


Figure: Barnett Effect

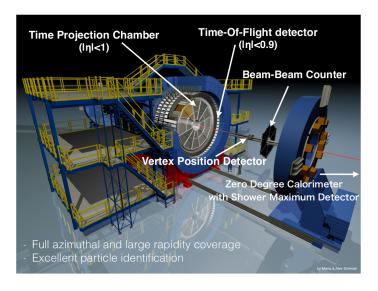


Figure: Schematic view of STAR Detector