

# 3 TeV Future Muon Collider: RCS Acceleration in SPS Tunnel

## Student Design Project

**12<sup>th</sup> March 2020**

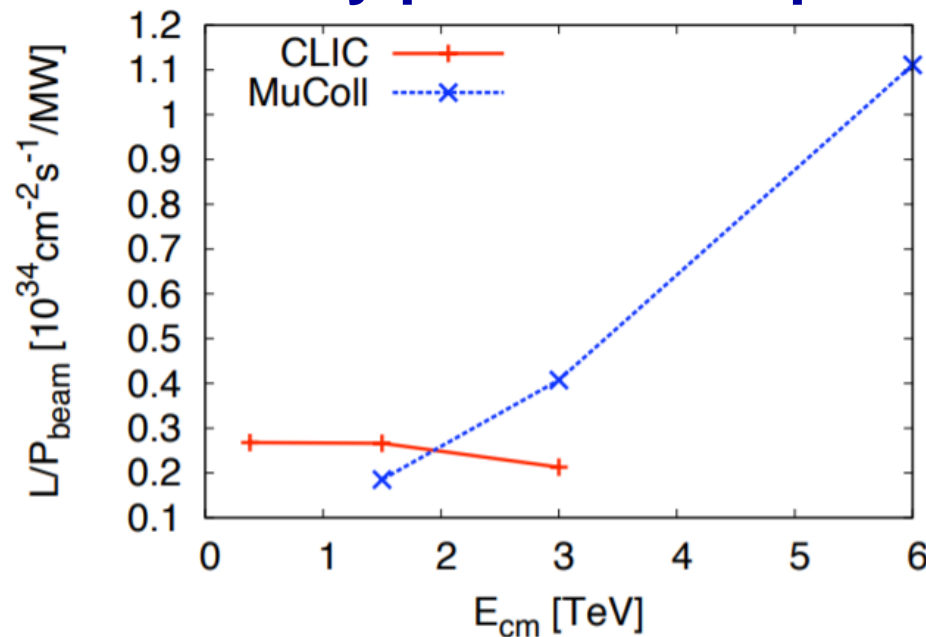
Titus-Stefan Dascalu  
Jake Flowerdew  
Peter Griffin-Hicks  
Adam Hughes  
Carlo Mussolini  
Collette Pakuza  
Max Topp-Mugglestone  
Wei-Ting Wang  
Laurence Wroe

## Why do we need a muon collider?

- **We want a lepton colliding machine to explore the energy and precision frontier**
- **A much higher discovery potential than a hadron machine of equivalent energy**
- **Does not suffer from synchrotron radiation**
- **Does not have the large footprint of a linear accelerator - it can reuse infrastructure**

## Advantages of building a muon collider?

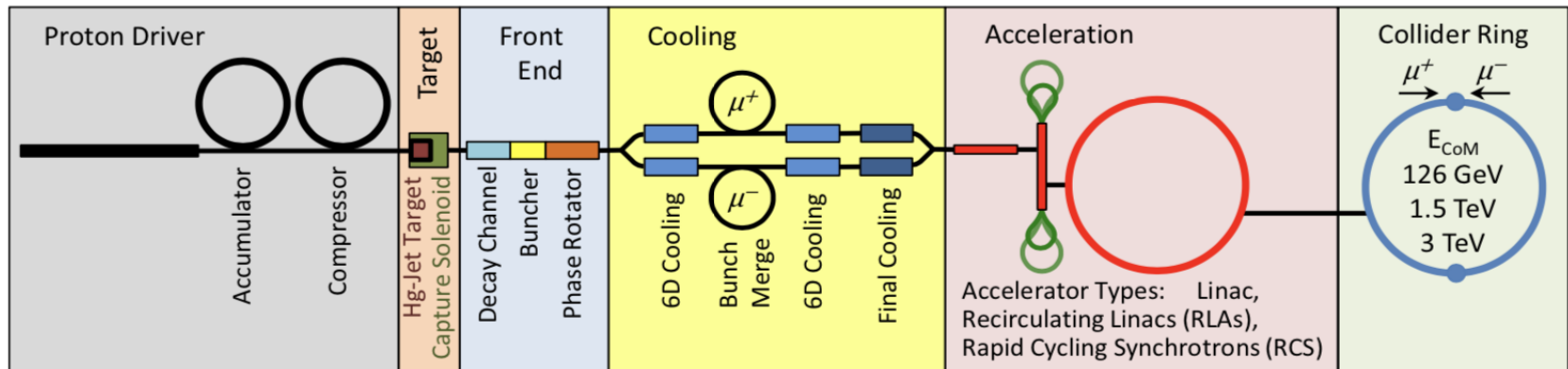
- A highly synergistic physics programme
- Can be built in stages, with interesting physics at each step
- A high luminosity per unit wall power



- Studies on overall collider scheme and basic machine parameters
- Two schemes for muon production

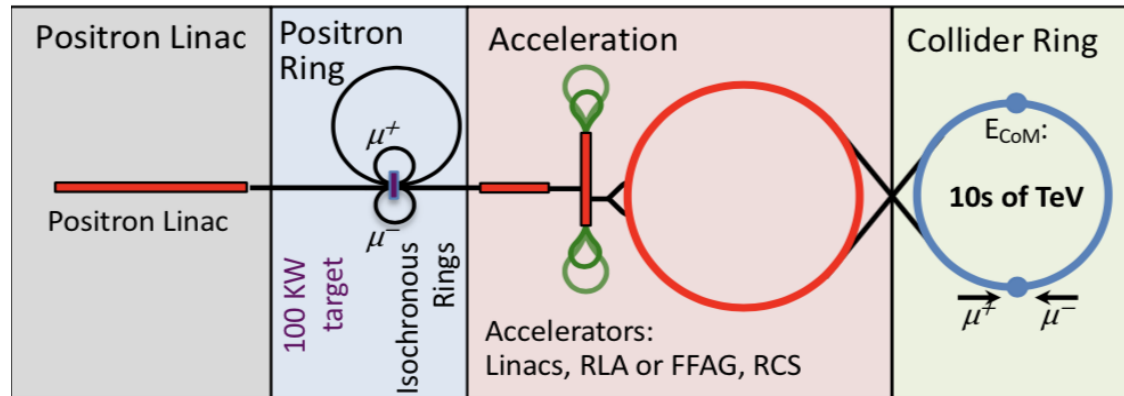
## 1. MAP scheme

- Proton on pion-producing target
- Muons created by pion decay
- Large emittance requires 6D ionization cooling
- Acceleration stage involves linac, RLAs and RCS



## 2. LEMMA scheme

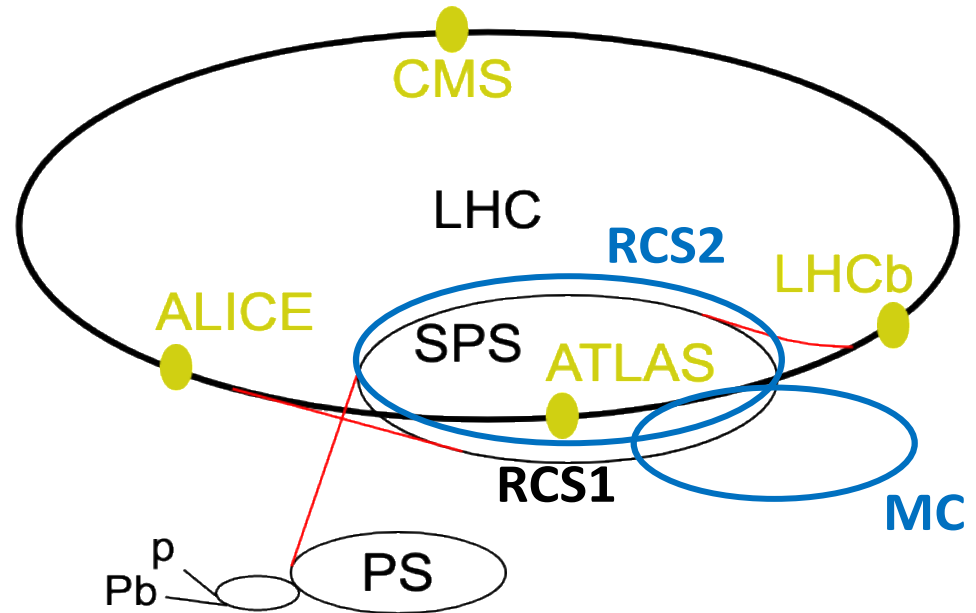
- Positron on beryllium target
- $\mu^+ \mu^-$  production at threshold
- Low emittance
- Allows lower overall charge in collider ring
- Lower backgrounds in collider detector



- We focused on acceleration stage for 3 TeV MC

- **RCS**

- Lattice
- Magnets
- RF cavities
- Radiation



- **Considerations**

- Cost and resources

- Use existing infrastructure at CERN

- Acceleration from 100 GeV to 1.5 TeV

- Divided into two stages RCS1 and RCS2

# RCS Lattice Design

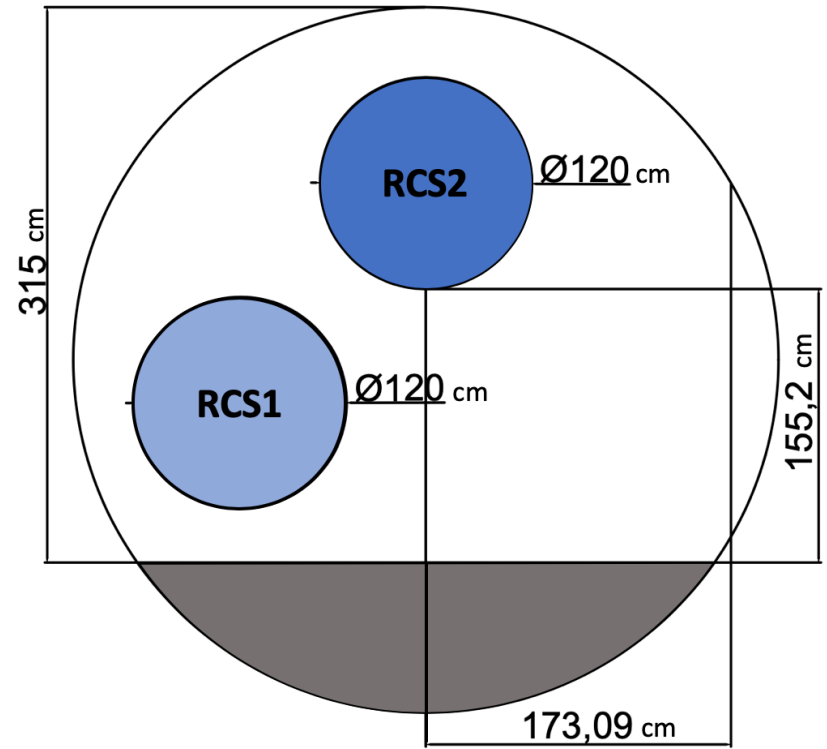
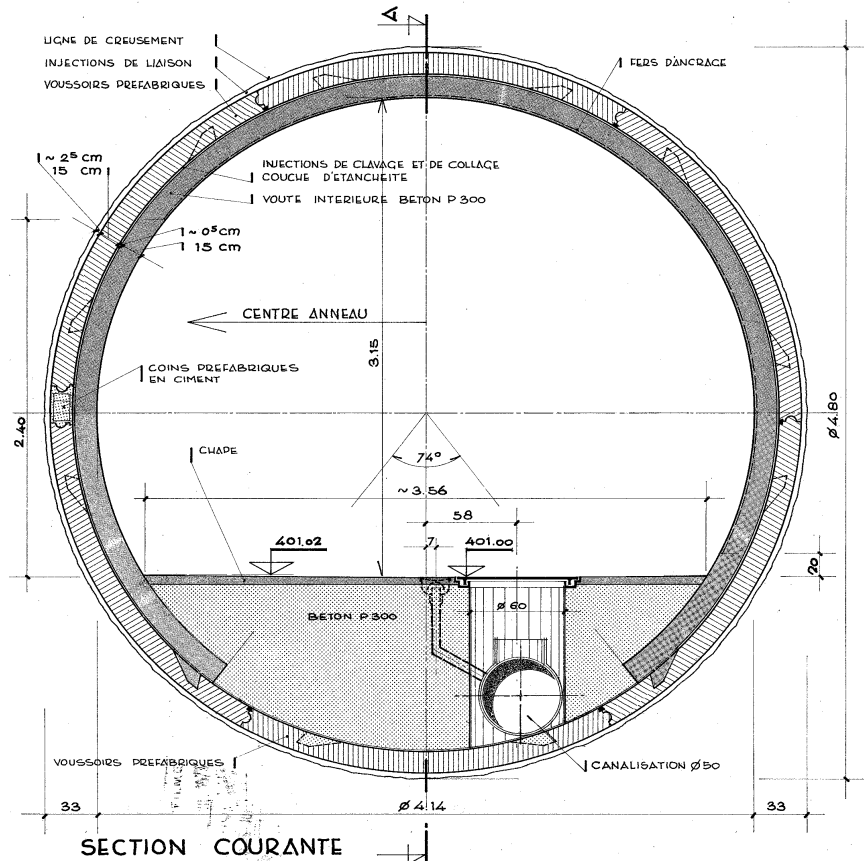
## Student Design Project

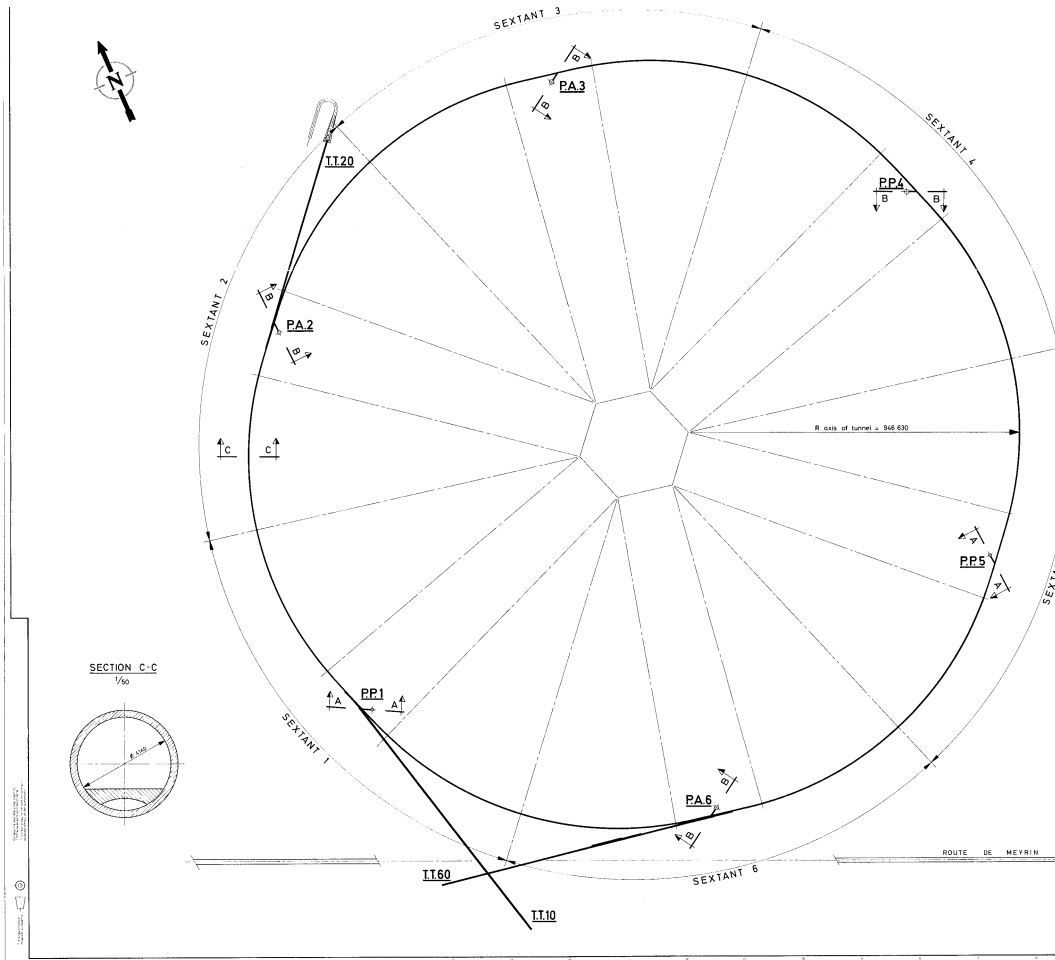
**Jake Flowerdew**  
**Collette Pakuza**  
**Peter Griffin-Hicks**

- **Feasibility of RCS1 and RCS2 in current SPS tunnel**
- **First studies of full lattice for both RCSs**
- **Developed dispersion suppressor schemes**



# Feasibility of RCSs in SPS Tunnel





- **6.9 km circumference**
- **6 arcs**
  - **Each ~1 km**
- **6 straight sections**
  - **Each 131 m**

# Previous Lattice Studies

- FODO cells with a hybrid design
- 3 pulsed magnets and 2 SC magnets per half-cell

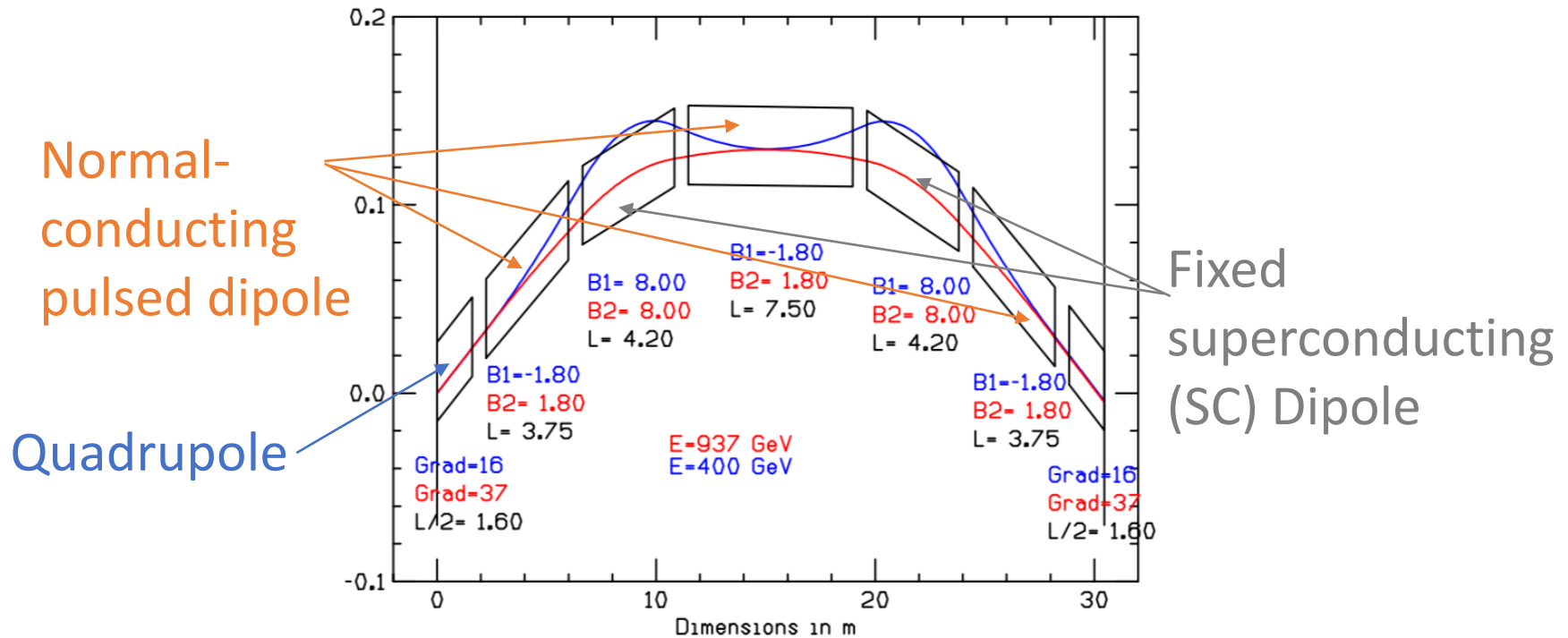
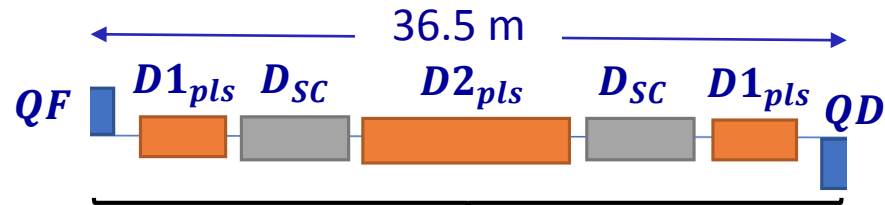


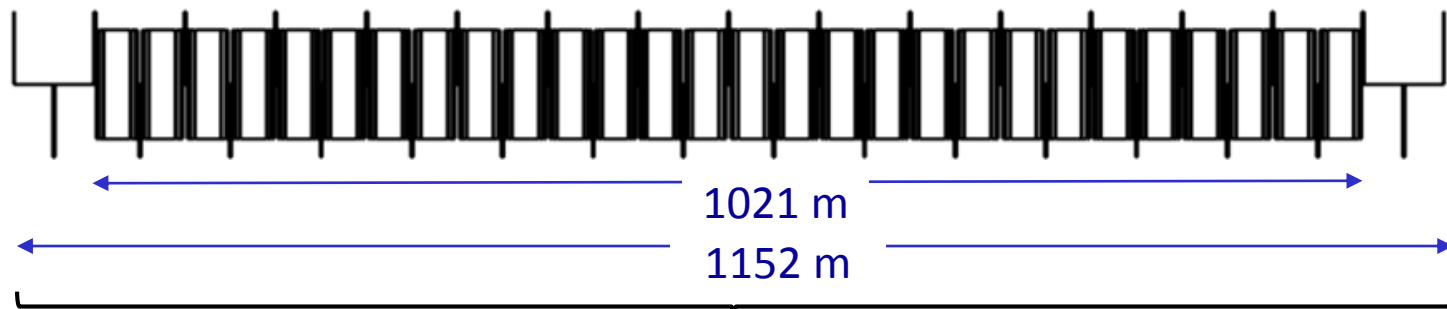
Diagram Ref: Summers, D.J., Cremaldi, L.M., Godang, R., Kipapa, B.R. & Rice, H.E., Muon acceleration to 750 GeV in the Tevatron tunnel for a 1.5 TeV  $\mu^+\mu^-$  collider, Particle Accelerator Conference (PAC 07), Albuquerque, NM, 25-29 June 2007, THPMS082.

- Based on hybrid FODO cell

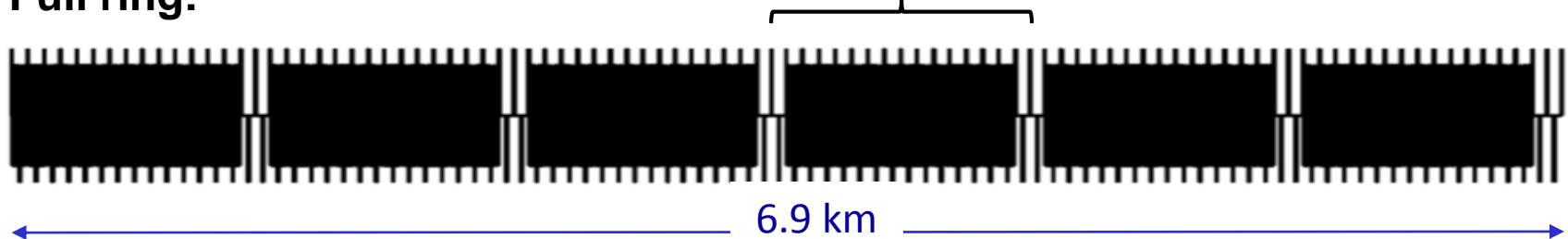
1 half-cell:



1 super-cell:



Full ring:



# Calculated Parameters

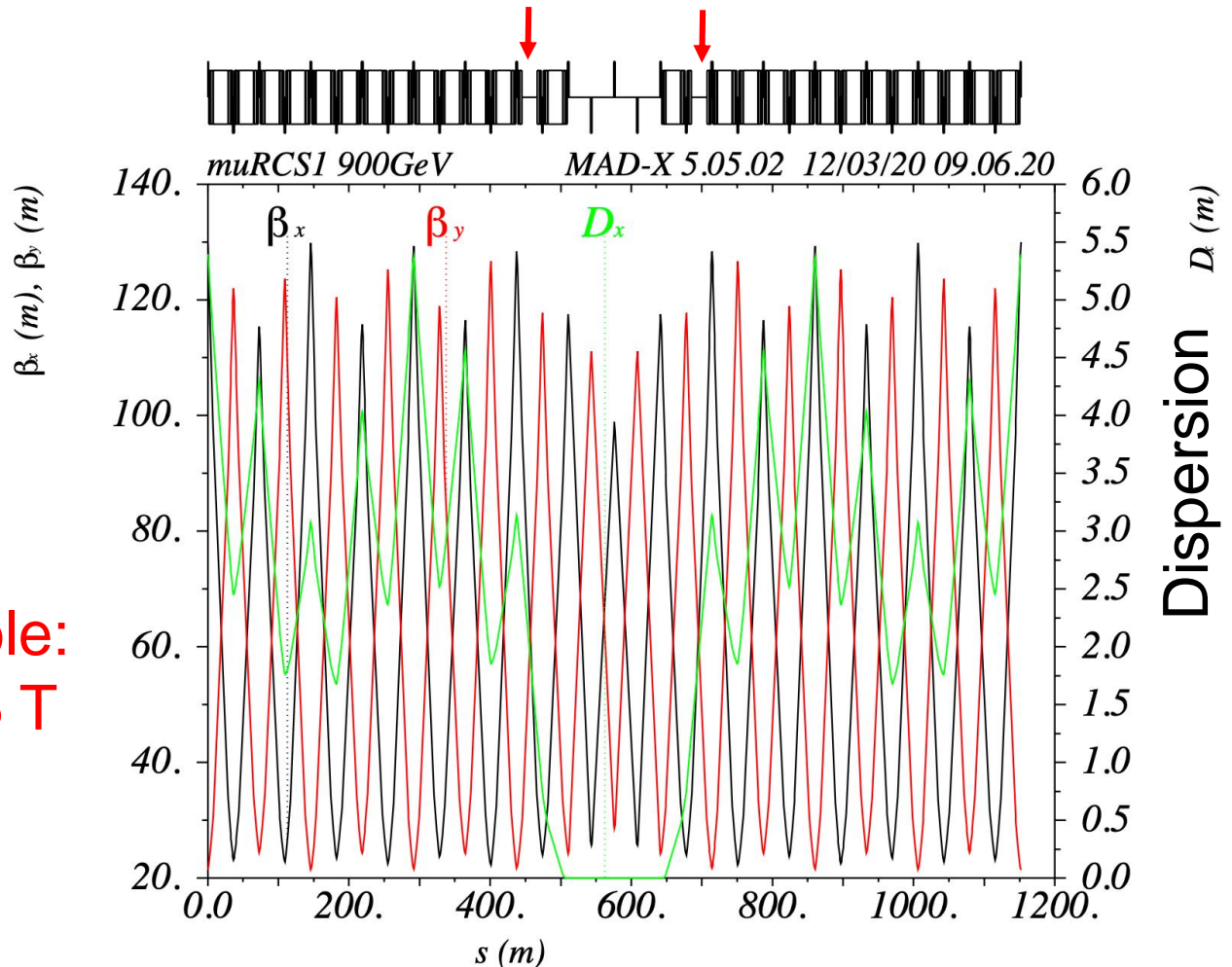
Parameter	Units	RCS1	RCS2
<b>Injection Energy</b>	GeV	100	900
<b>Extraction Energy</b>	GeV	900	1500
<i>D</i> <sub>1<math>pls</math></sub> length	m	2.0	6.0
<i>D</i> <sub>2<math>pls</math></sub> length	m	20.95 (3x7 m)	6.71
<i>D</i> <sub><math>pls</math></sub> initial magnetic field	T	-2.00	-2.00
<i>D</i> <sub><math>pls</math></sub> final magnetic field	T	2.00	2.00
<i>D</i> <sub><math>SC</math></sub> length	m	3.12	6.24
<i>D</i> <sub><math>SC</math></sub> strength	T	10.0	12.0
Quad length	m	2.0	2.0
Quad initial gradient	T/m	6.4	57.6
Quad final gradient	T/m	57.6	96.0
Number of cells		84	84
Number of cells per arc		14	14
Packing factor		0.76	0.76
Total length of straights	m	738	738
Space for RF	m	492	492
Beam aperture	mm	38	28

- Used MAD-X to plot beta and dispersion functions
- Suppress dispersion in straights

## 1. Missing Dipoles

- Advantage
  - Beta functions essentially unchanged
- Disadvantage
  - Changes the geometry of the ring or requires extra bending

## RCS1 900 GeV – 1 super-cell



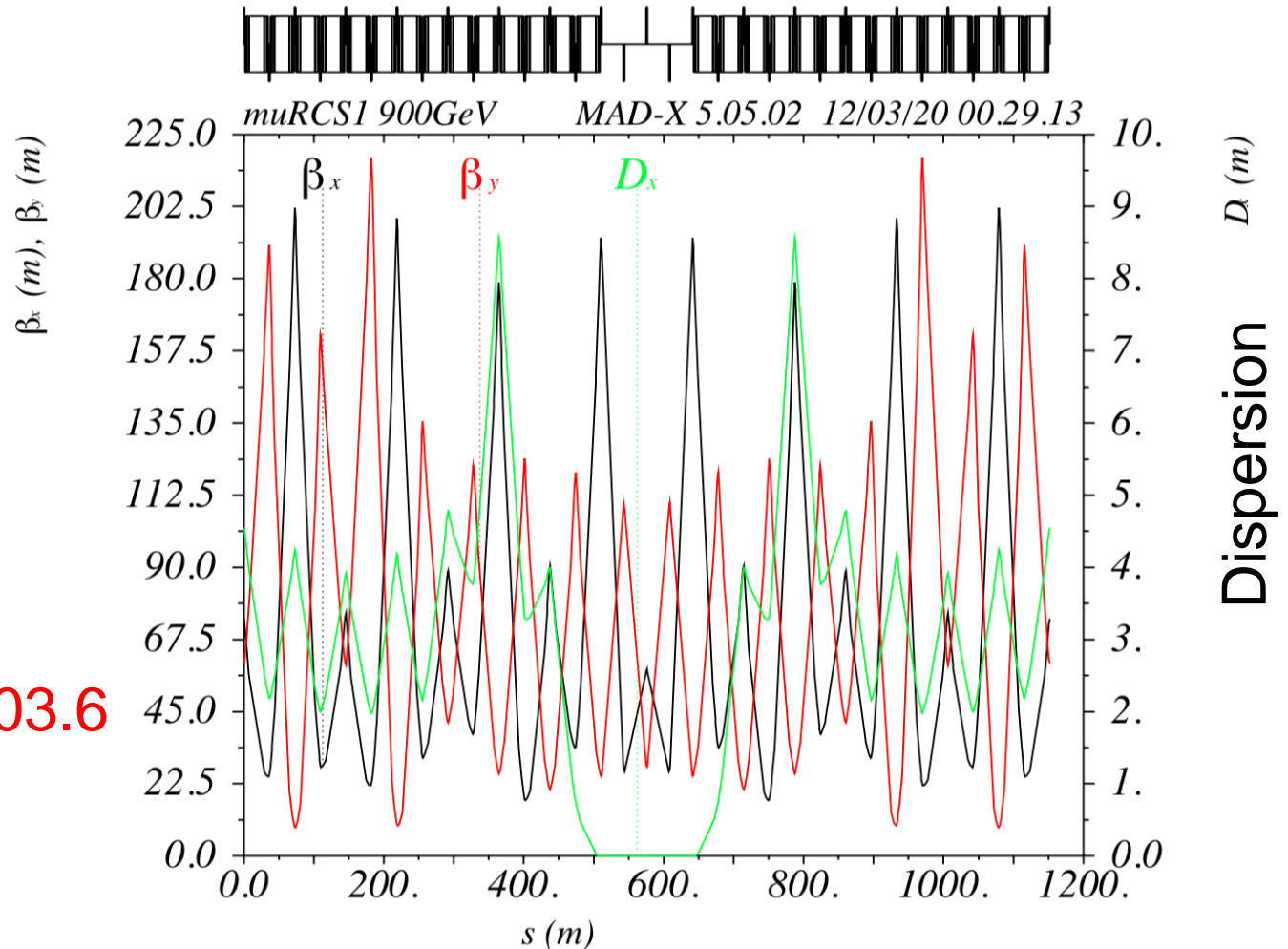
Pulsed dipole:  
-0.5 T -> -5 T

## 2. Extra Quadrupoles

- Vary the strength of 8 quadrupoles in each half super-cell
- Advantage
  - Ring geometry doesn't change
- Disadvantages
  - Increased beta functions
  - Individually powered quadrupoles



## RCS1 900 GeV – 1 super-cell



Max Quad  
strength = 103.6  
T/m

- **Utilized existing SPS tunnel which reduces costs**
- **Showed that acceleration of muons from 100 GeV to 1.5 TeV can be achieved with two RCS rings in the SPS tunnel**
- **Provided a lattice design with zero dispersion straights**

# Longitudinal Dynamics and Collective Effects

- **Longitudinal dynamics simulations**
  - **From the repetition rate of main magnets:**
    - Obtain RF voltage required per turn
    - Determine muon survival
  - **Calculate time varying parameters:**
    - Space charge tune shift
    - “Luminosity” of counter-rotating beams
    - Beam-beam parameter
  
- **Assumptions:**
  - $N = 10^{12}$  muons per bunch
  - $\epsilon_{x,y} = 25 \pi$  mm mrad
  - $\langle \beta_{x,y} \rangle \approx 60$  m

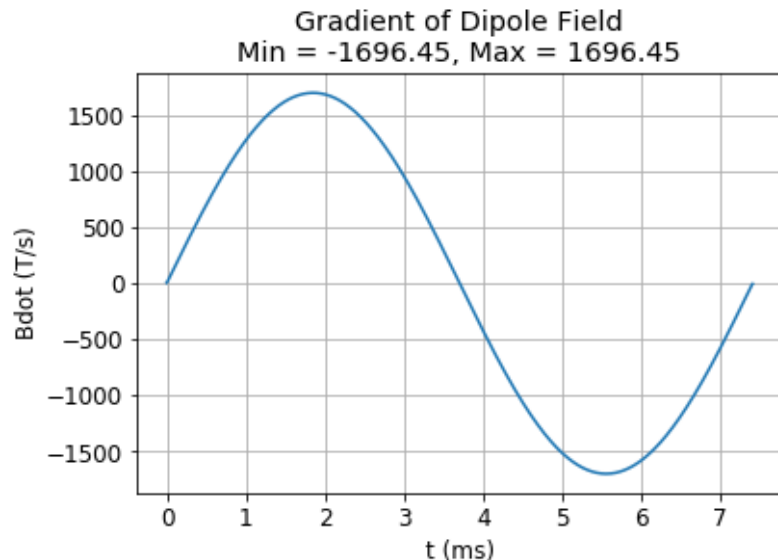
**Dynamics synchronous to the rate of change of magnetic flux – the main magnet ramp.**

$$B_{\text{fixed-field}} = \text{constant}$$

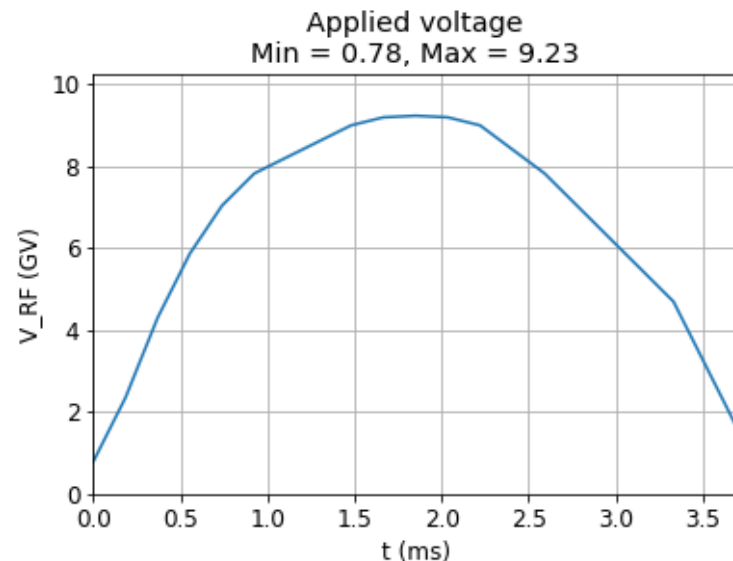
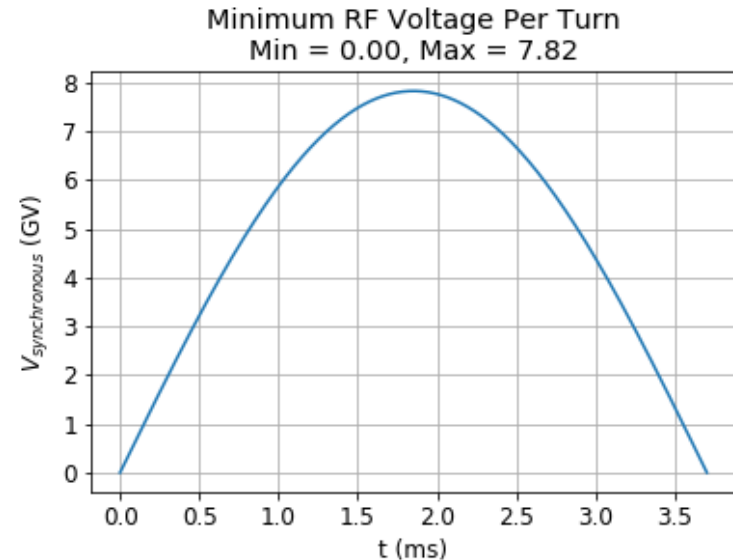
$$B_{\text{fast-ramping}} = -B_0 \cos(2\pi f_{\text{rept}} t)$$

$$\dot{B} = \frac{dB}{dt}$$

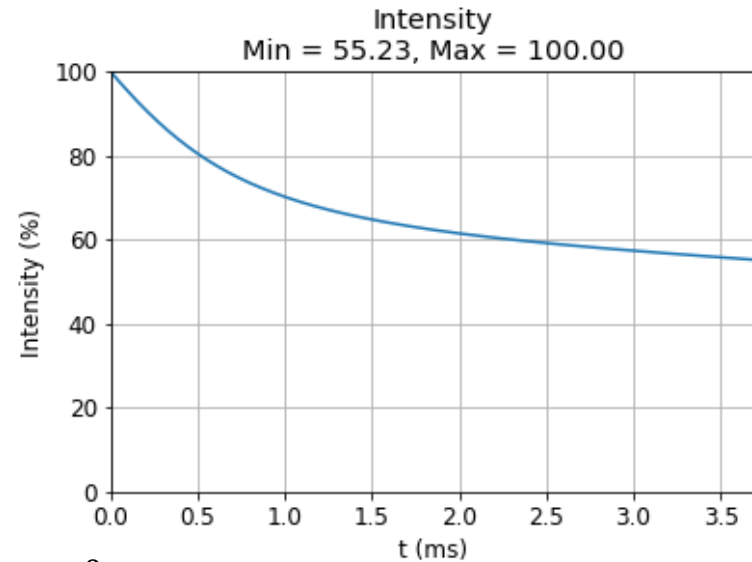
**Only linked to ramping magnets**



- As magnet current ramps:
- Beam energy must increase to keep beam on design orbit
- Minimum RF voltage per turn for ideal synchronous particle
- In reality, need more than this to create potential well in which to store accelerating particles



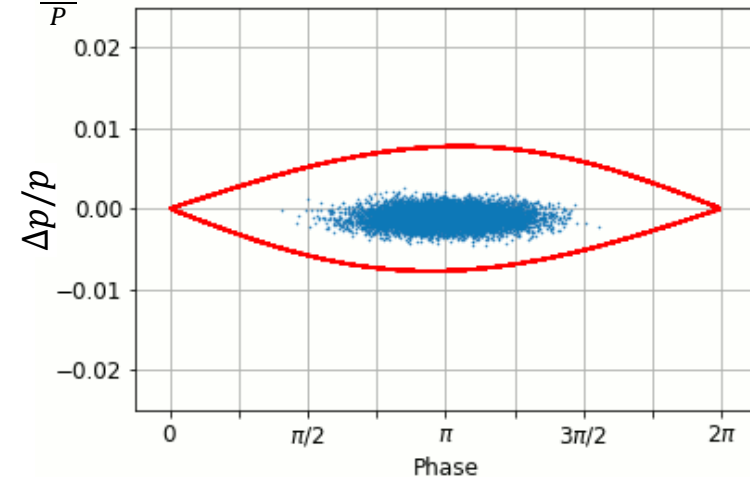
Injection energy	100	GeV
Extraction energy	900	GeV
Repetition rate	135	Hz
Time in lab frame	3.704	ms
Time in beam frame	1.304	$\mu$ s
Number of turns	161	
Muon survival	55.2	%
Bucket losses	>0.1	%
Mean rev. frequency	43.373	kHz
$\Delta f_{\text{revolution}}$	2.4e-5	kHz
RF Harmonic	29 973	
RF frequency	1300.011	MHz
Max RF voltage / turn	9.23	GV



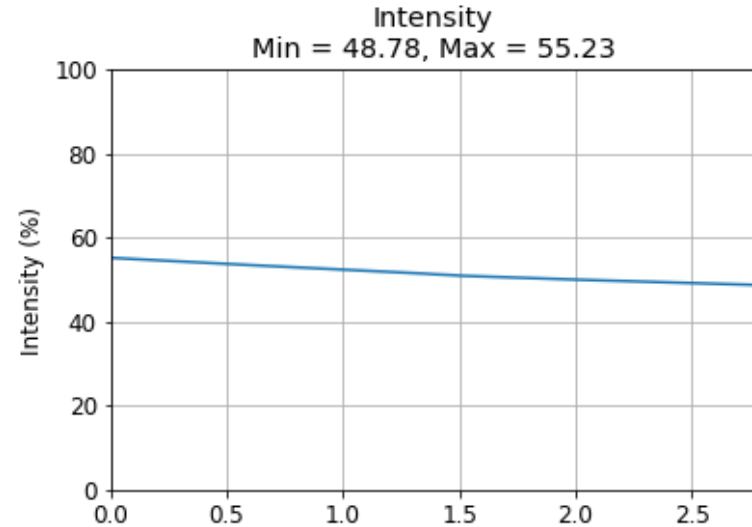
At  $t = 0$  ms

$$\sigma_{\phi} = 0.15 \pi$$

$$\sigma_{\frac{\Delta P}{P}} = 10.0 \times 10^{-4} \quad t = 0.000 \text{ ms}$$



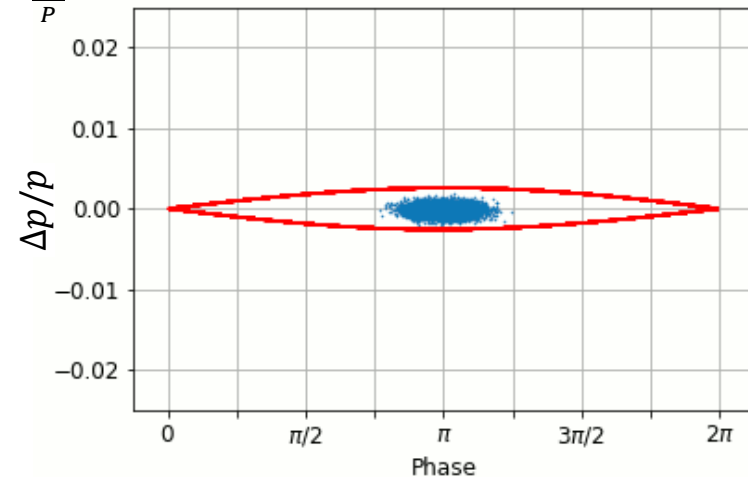
Injection energy	900	GeV
Extraction energy	1500	GeV
Repetition rate	180	Hz
Time in lab frame	2.778	ms
Time in beam frame	0.253	$\mu$ s
Number of turns	108	
Muon survival	89.1	%
Bucket losses	0.9	%
Mean rev. frequency	43.373	kHz
$\Delta f_{\text{revolution}}$	1.9e-7	kHz
RF Harmonic	29 973	
RF frequency	1300.011	MHz
Max RF voltage / turn	9.23	GV



At  $t = 0$  ms, based on RCS1 simulation

$$\sigma_{\phi} = 0.0615 \pi$$

$$\sigma_{\frac{\Delta P}{P}} = 5.14 \times 10^{-4} \quad t = 0.000 \text{ ms}$$



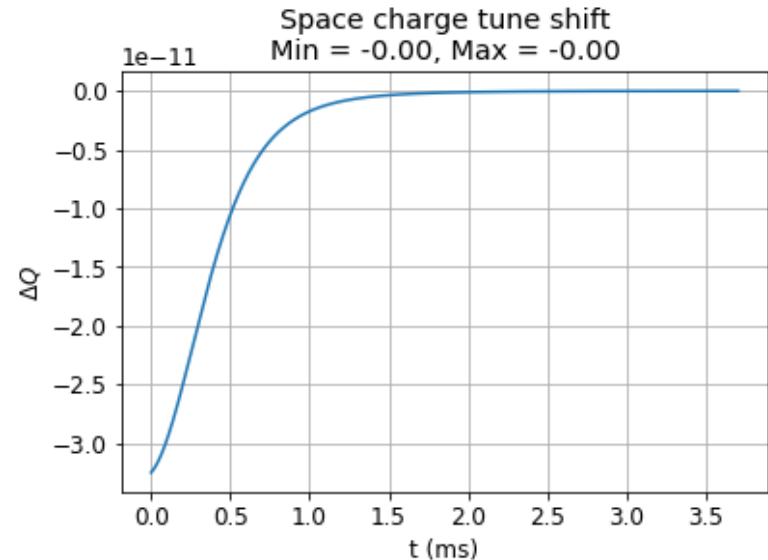


## Transverse

Linear tune shift:

$$\Delta Q = - \frac{r_0 N}{2\pi \epsilon_{x,y} \beta^2 \gamma^3}$$

Negligible

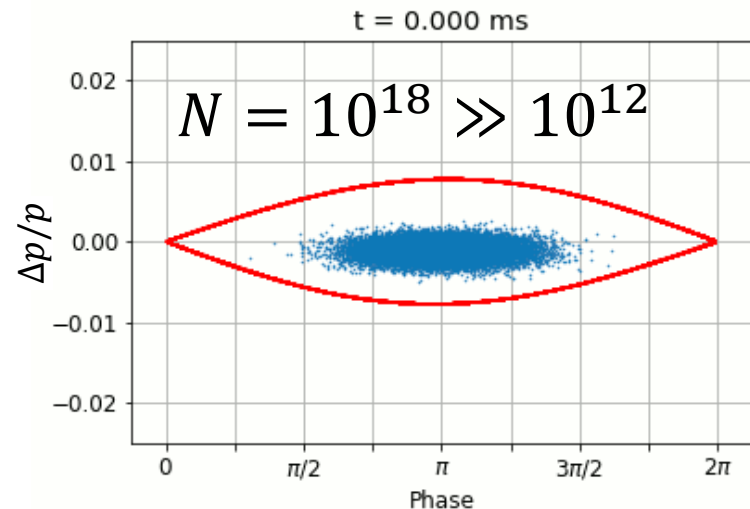


## Longitudinal

Voltage drop per turn:

$$\Delta U = -e\beta cR \frac{\partial \lambda}{\partial s} \left[ \frac{g_0 Z_0}{2\beta \gamma^2} - \omega L \right]$$

Negligible until  $N > 10^{17}$

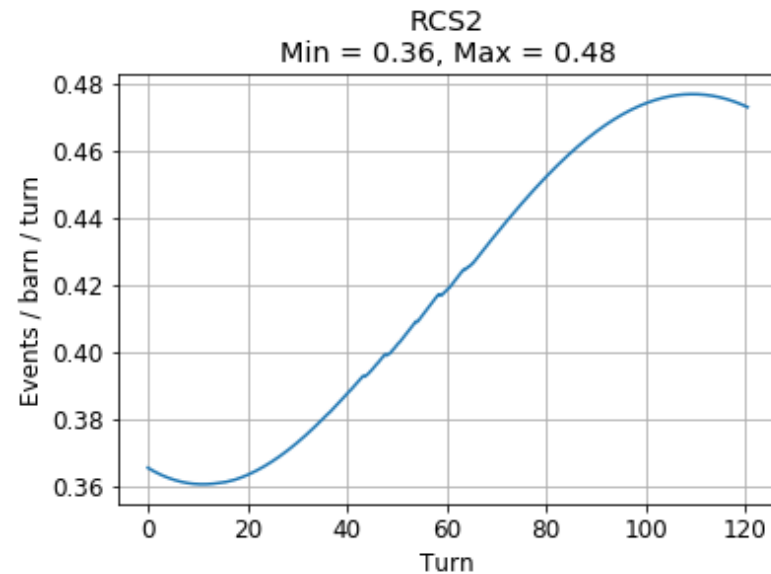
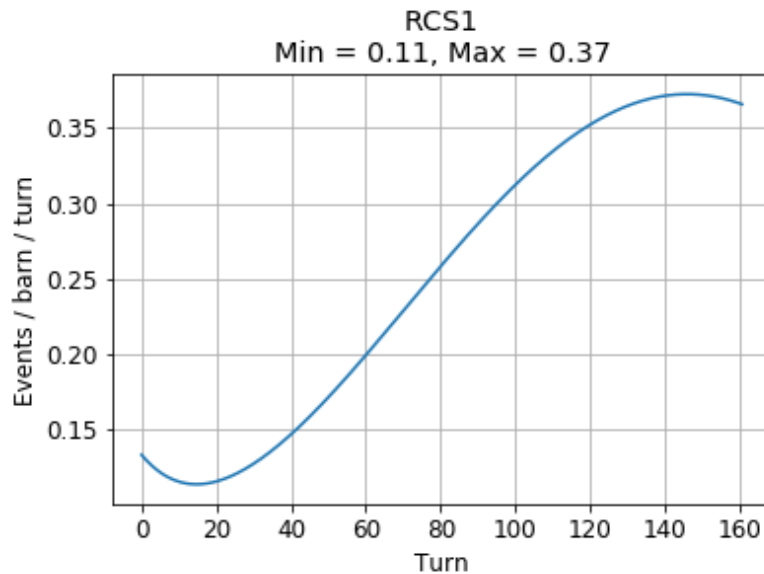


# Counter-rotating beams

Collisions between counter-rotating beams of  $\mu^+$  and  $\mu^-$  should not cause significant losses. Beams are not focussed and accelerate over a very quick time scale.

$$\text{Events per turn} = L \cdot T \cdot \sigma_X = \frac{N_1 N_2 f_{rev} N_B N_{IP}}{4\pi\sigma_{x,y}^2} \cdot \frac{1}{f_{rev}} \cdot \sigma_X(E)$$

$$\text{Events per turn} = \frac{(N_0 \exp(-t/\tau))^2 N_B^2}{4\pi\sigma_{x,y}^2(E)} \cdot \sigma_X(E)$$



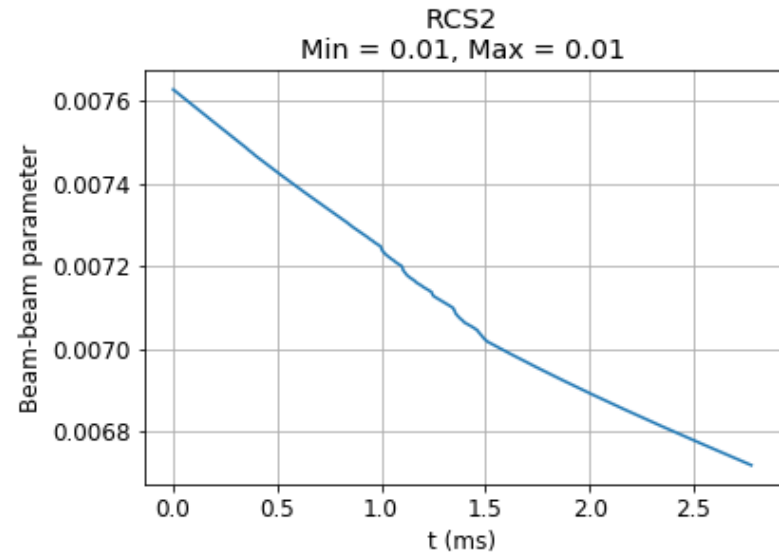
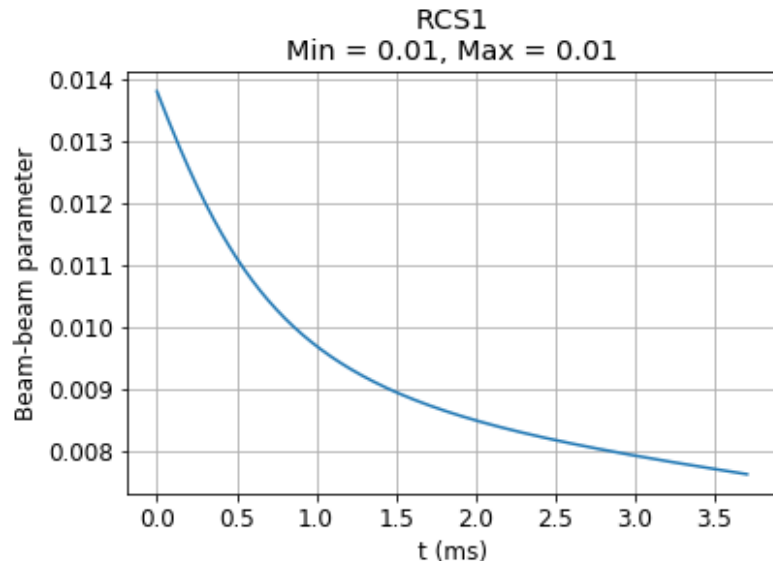
## Beam-beam effects:

$$\xi = \frac{r_0 N \beta_{x,y}}{4\pi\gamma\sigma_{x,y}^2} < 0.014$$

$$\xi_{LHC} = 0.0037^\dagger, \quad \tau_{bb} = 55 \text{ hours}^\ddagger$$

† Beam-beam effects, Werner Herr, Cockcroft Institute Lectures

‡ LHC Beam Parameters, Mike Lamont, LHC Collimation Project



- **RF voltage is minimized while keeping losses low**
  - **Can be optimized further**
- **First order collective effects are negligible**
  - **Proper simulation studies should be carried out to determined effects of counter-rotating beams**

# RCS Cavity Design

## Student Design Project

**Max Topp-Mugglestone**  
**Laurence Wroe**

## Main factors affecting RF design:

- **A large voltage gain (for  $\mu$ -decay):**
  - Maximise acceleration gradient
- **Low cost/power**
- **NC or SC**
- **Available technology/frequency**
- **Space available**
  - Radially limited by SPS tunnel

# JAI Super-Conducting vs Normal-Conducting

- **Large amount of RF operated at high-gradient, high duty factor**
  - **Need to maximise power efficiency**
    - **Effective limit on CW NC cavities  $\sim 2\text{MV/m}$**
    - **High gradient NC structures limited to  $<1\%$  duty**
- **SC enables larger aperture**
- **Disadvantages of SC:**
  - **Refrigeration requirements**

- **Choose standard frequency to enable use of off-the-shelf powerline components**
  - **352 MHz (LEP)**
  - **704 MHz (RHIC electron cooling ring)**
  - **1.3 GHz (ILC)**

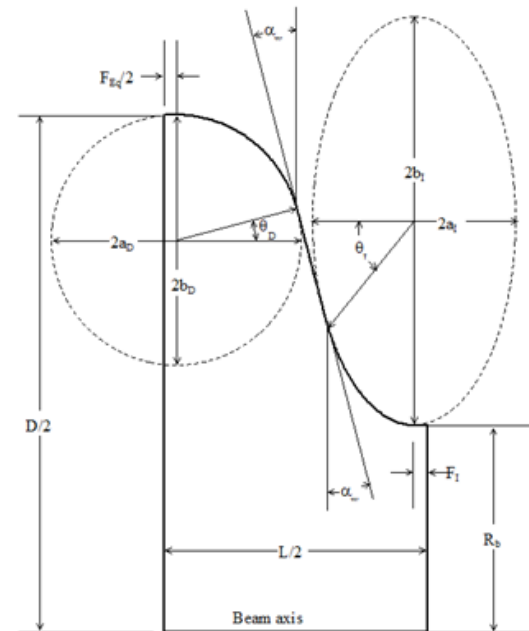


- **Cavity diameter scales as  $1/f$** 
  - Large amount of RF required (material requirements)
  - Limited space available (~90cm between RCS1 beam pipe and RCS2 beam pipe)
- **Available aperture scales as  $1/f$  too**
  - Need to ensure cavity bore is wide enough to fit the beam!
  - Wider beam pipe reduces wakefield effects

Freq [MHz]	Cavity Radius [cm]	Bore radius [cm]
352	37.55	10
704	18.98	3
1300	10.25	2

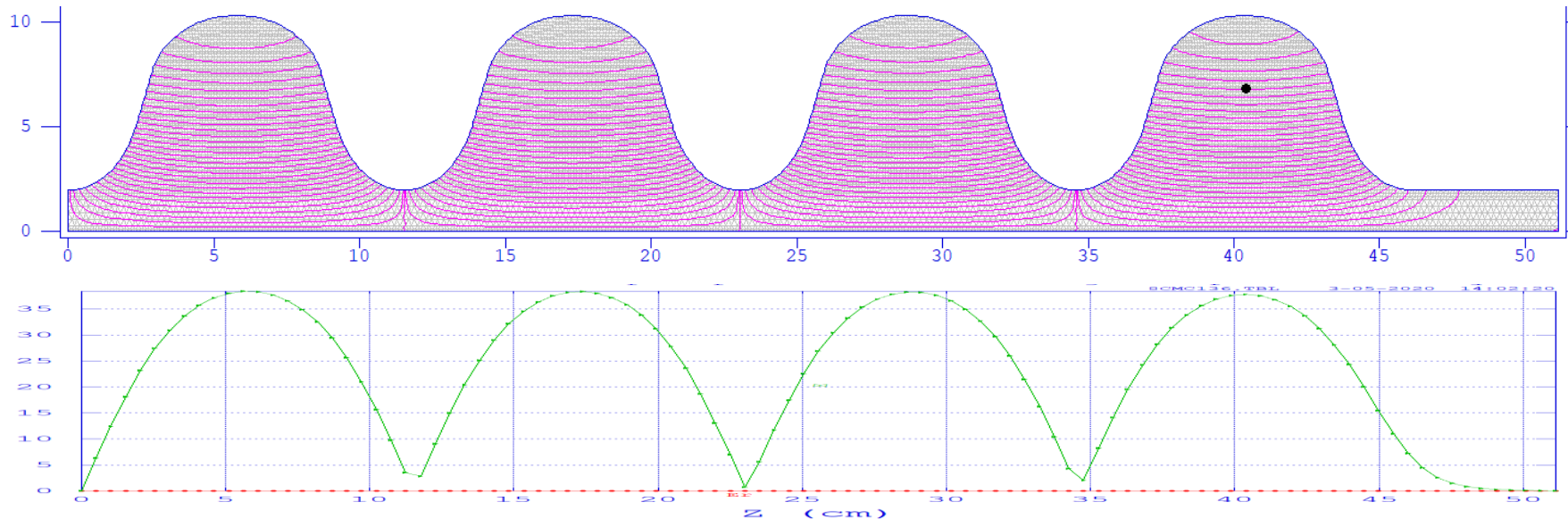
**1300 MHz is the best option!**

- **Goals:**
  - Minimise peak fields
  - Minimise  $B_{max}/E_{max}$  and  $E_{max}/E_0$
  - Minimise power losses
  - Maximise field flatness
- **Input variables**
  - Dome ellipse axes
  - Iris ellipse axes
  - Wall angle
  - Bore radius

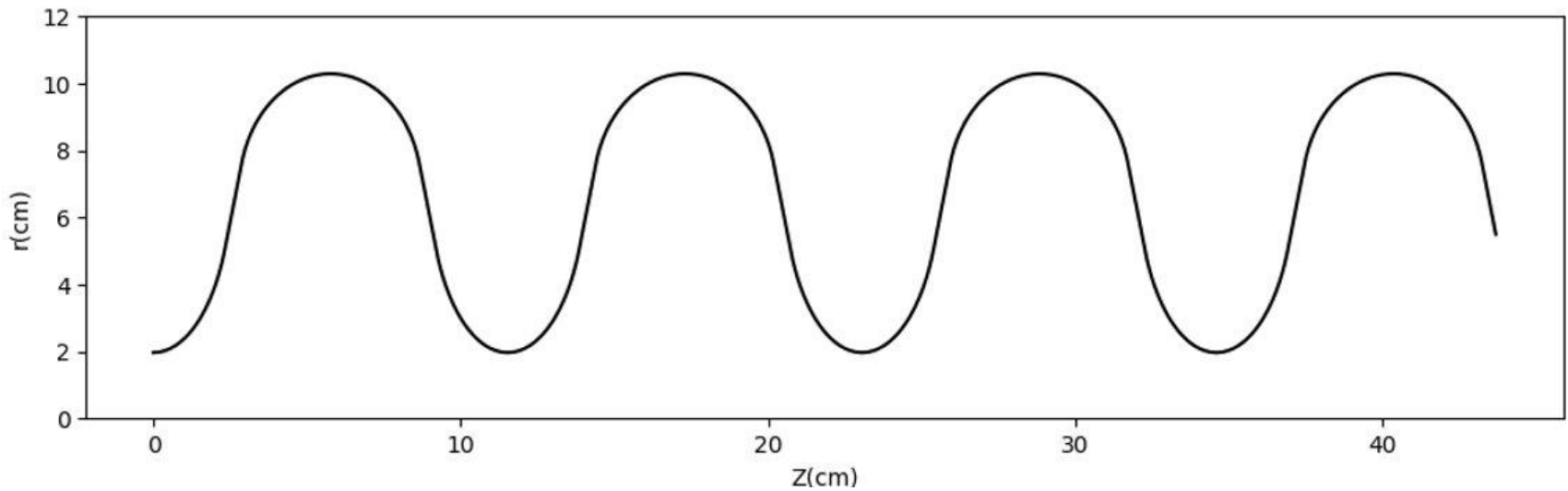
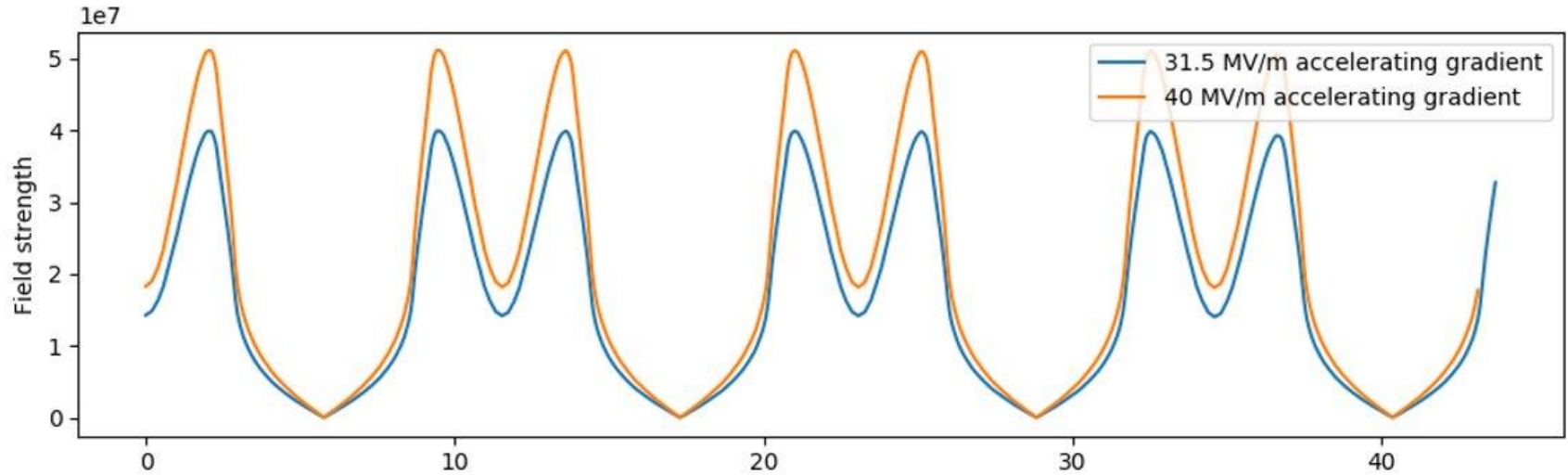


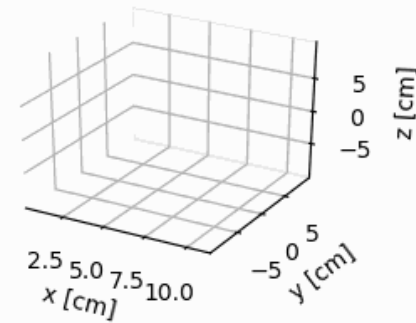
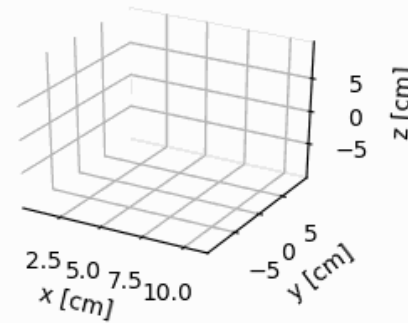
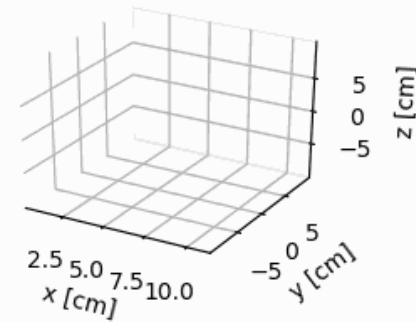
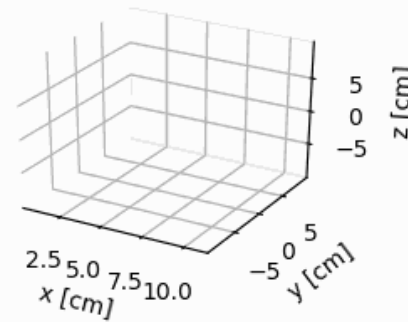
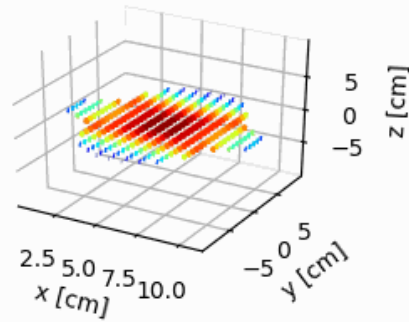
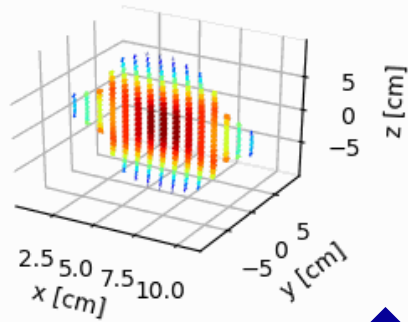
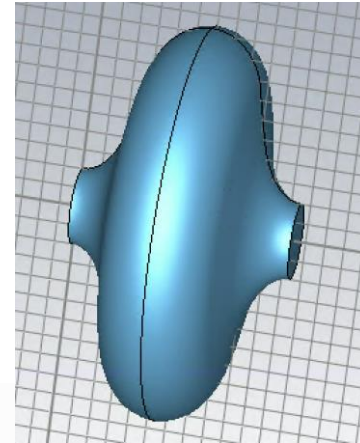
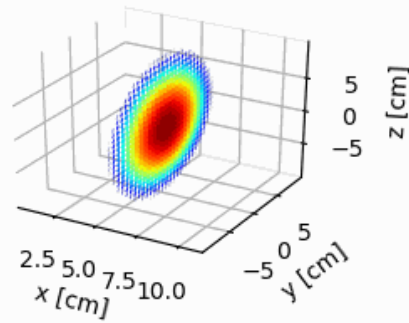
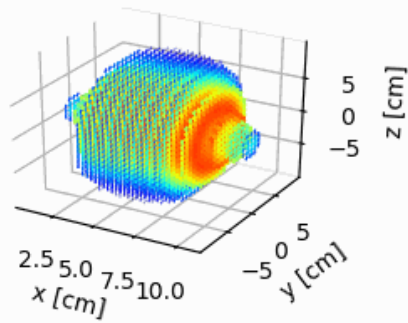
- **Our design:**

Cavity name	Length [cm]	Radius [cm]	Q [e+11]	$R_s/Q$ [ $\Omega/m$ ]	$B_{max}/E_{max}$ [mT/(MVm <sup>-1</sup> )]	$E_{max}/E_0$	Power dissipated (W)
1300 MHz 8 cell cavity	92.24	10.29	0.0826	221	2.7051	1.2690	18.3563
TESLA (from SFISH)	143.57	10.33	0.101	272	2.09	2.04	67.34
TESLA (9 cell cavity data)	127.6	10.33	>0.05	518	4.26	2.0	1400



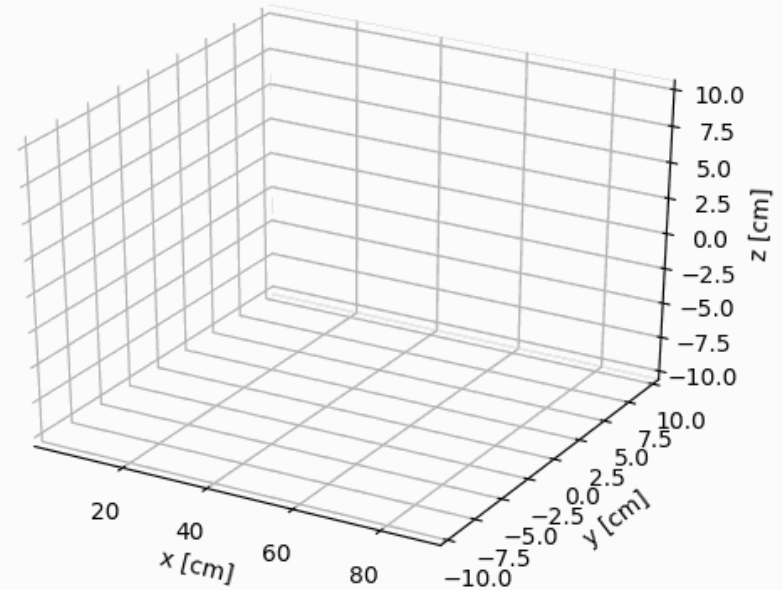
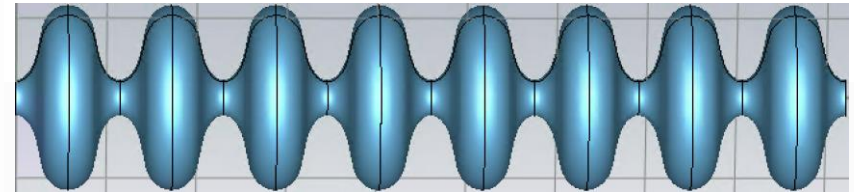
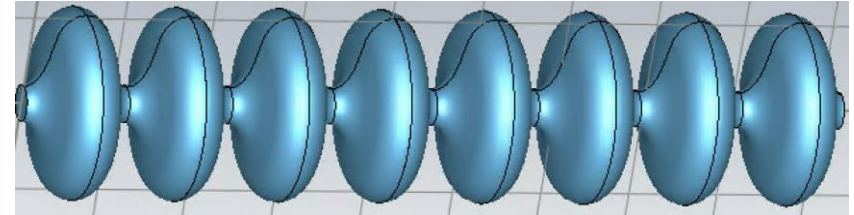
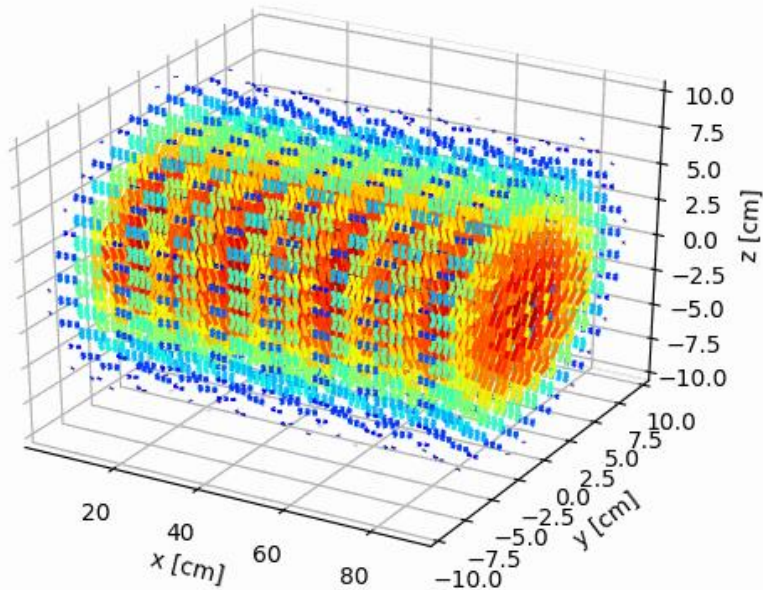
# Cavity Gradient Studies





- E-field
- H-field



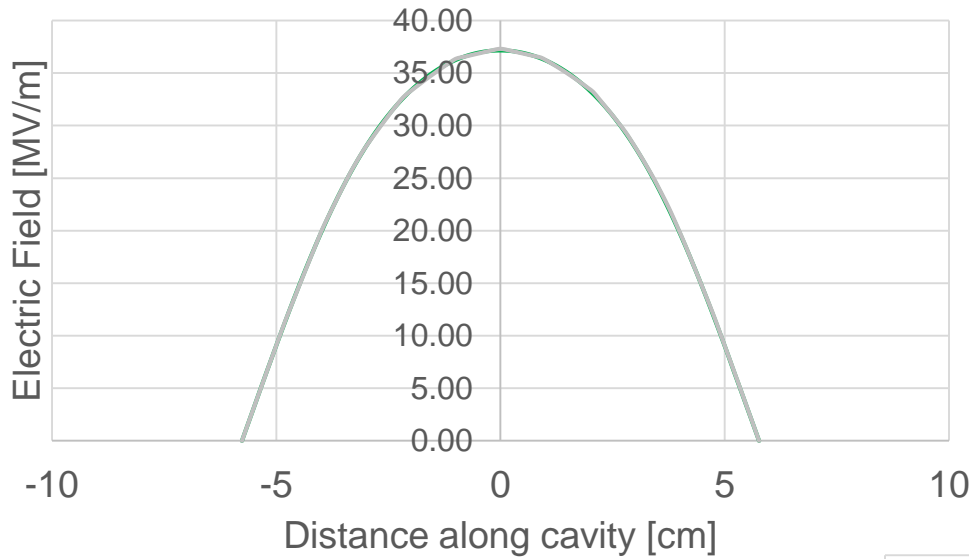


- E-field
- H-field

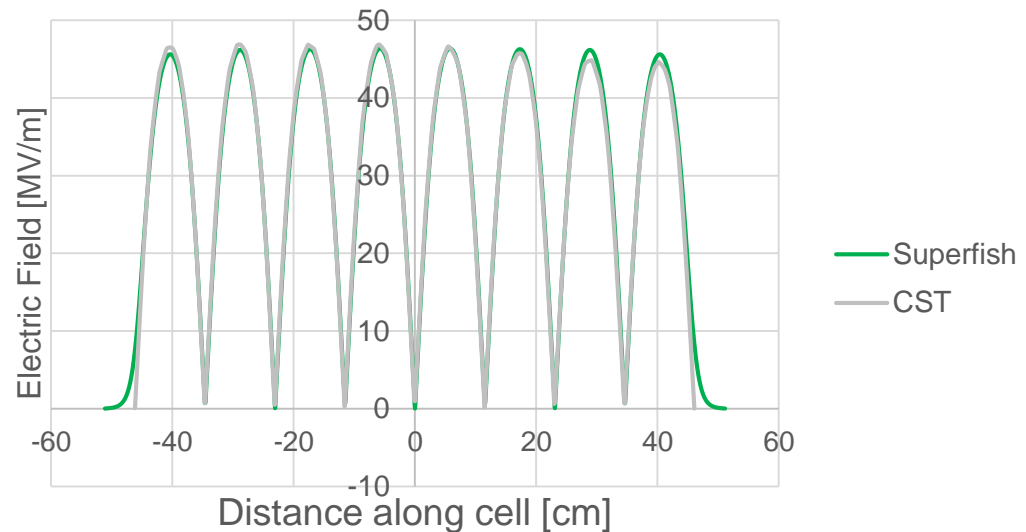




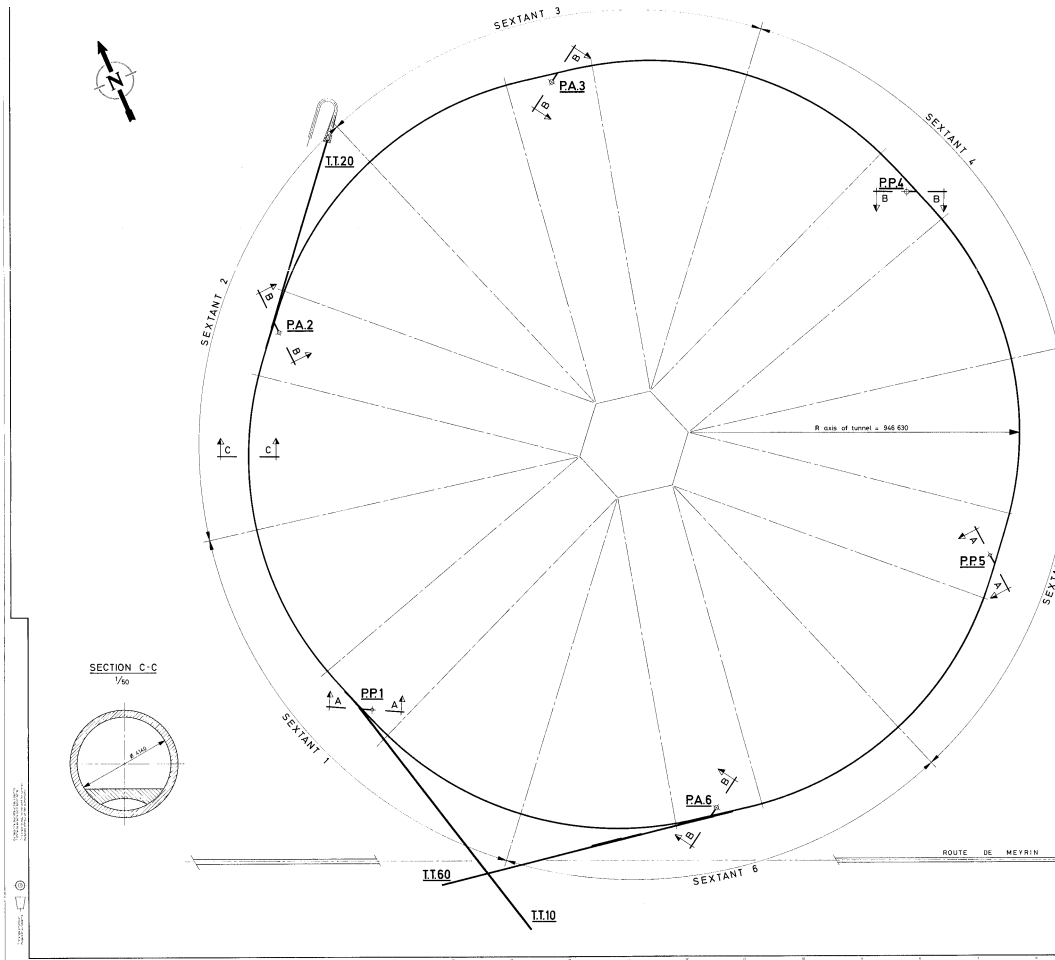
# Superfish to CST Comparison



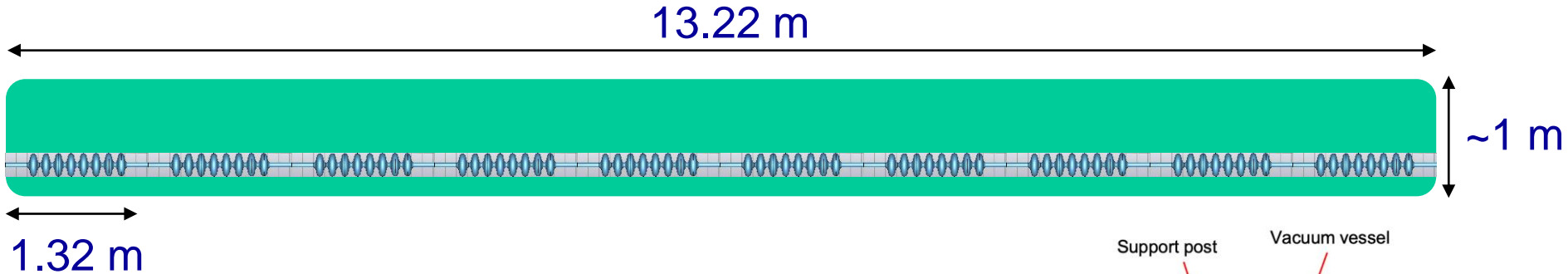
- Similar flatness
- Add in beam pipe to improve!



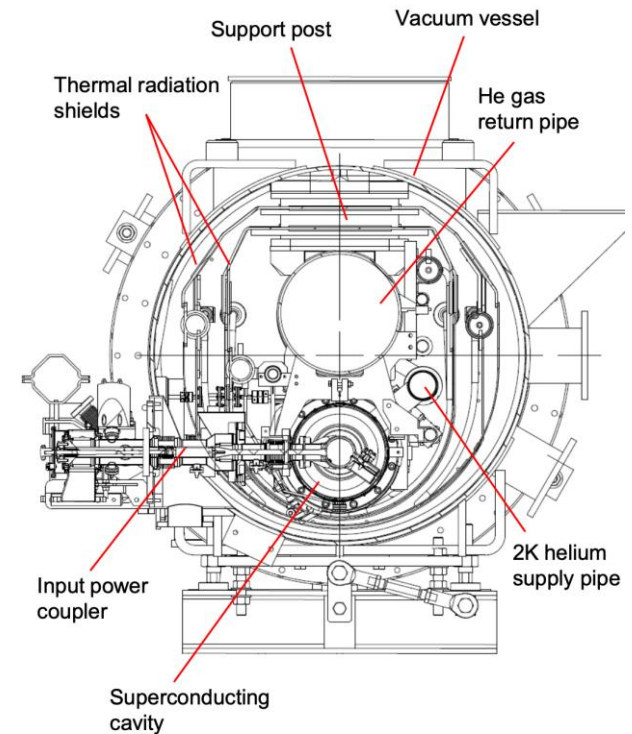




- **6.9km circumference**
- **6 straight sections**
  - **Each 131m**
- **6 arcs**
  - **Each ~1km**

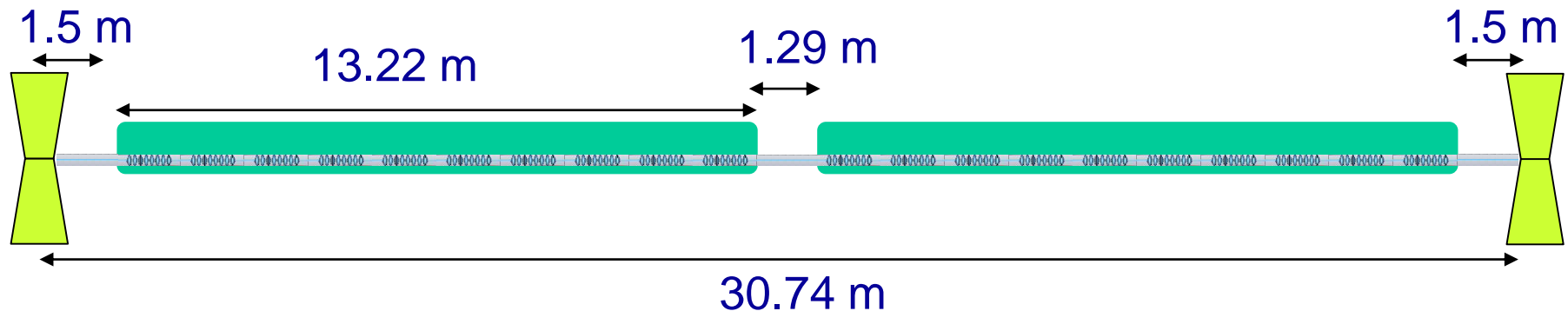


- 10 8-cell cavities in one cryomodule
  - Maximises packing factor
- Packing factor of cryomodule is 69.7%
- Thorough cryomodule design not complete...!



DESY-TESLA-TYPE-III  
Cryomodule Cross Section

- **6 straight sections of  $L = 131$  m**
- **Quads separated by 30.74 m**



- **Actual packing factor: 60%**
- **Voltage gain per 30.74 m section: 581 MV**
- **V gain per turn (4/6 straights): 9.3 GV**
- **Have 1 straight for injection, 1 for extraction – achieves required 9.23 GV**

# Luminosity Considerations

$$\mathcal{L} = \frac{c \gamma N_1 N_2}{4\pi l \varepsilon_N \beta^*} \Rightarrow \frac{c \gamma}{4\pi l \varepsilon_N \beta^*} N_{0\mu\text{-Coll}}^2 e^{-\frac{2t}{\gamma t_\mu}}$$

$$\langle \mathcal{L} \rangle = \frac{c \gamma}{4\pi l \varepsilon_N \beta^*} \frac{1}{2} \frac{\gamma t_\mu}{t_b} N_{0\mu\text{-Coll}}^2$$

$$\therefore N_{0\mu\text{-Coll}} = 2.36e12$$

$$\text{Using } N_0^{MAP} = 2e12 \Rightarrow P_{RCS1 \rightarrow \mu\text{-Coll}} = \frac{N_{0\mu\text{-Coll}}}{N_0^{MAP} P_{MAP \rightarrow RCS1}} = \frac{1.18}{P_{MAP \rightarrow RCS1}}$$

Where:

$$\langle \mathcal{L} \rangle = 2e34 \text{ cm}^{-2} \text{ s}^{-1}, \quad \gamma = \frac{1.5 \text{ TeV}}{105.66 \text{ MeV}}, \quad l = 4500 \text{ m}, \quad \varepsilon_N = 25 \pi \mu\text{m rad},$$

$$\beta^* = 0.5 \text{ cm}, \quad t_\mu = 2.2 \mu\text{s}, \quad t_b = 1/12 \text{ s}$$

Source: *Muon Colliders*, The Muon Collider Working Group – Input to the European Particle Physics Strategy

- **Proves maximization of muon survival in our acceleration is key: need closer to 100% than 1%!**
- **More work needed on the production and collider processes to maximise average luminosity**

- Literature review completed and suitable design identified
- High gradient (31.5 MV/m) cavity design has been demonstrated in Superfish and CST
- Allows fast acceleration (50% survival) from RCS1 to  $\mu$ -collider

## To Do:

- Detailed physics reach study needed
- Optimise in CST and adding in further components into design:
  - Detailed cryomodule design
  - HOM couplers
  - Power source and transfer design

# Magnet Design

**Titus-Stefan Dascalu**  
**Adam Hughes**  
**Wei-Ting Wang**

# Pulsed Dipole Design

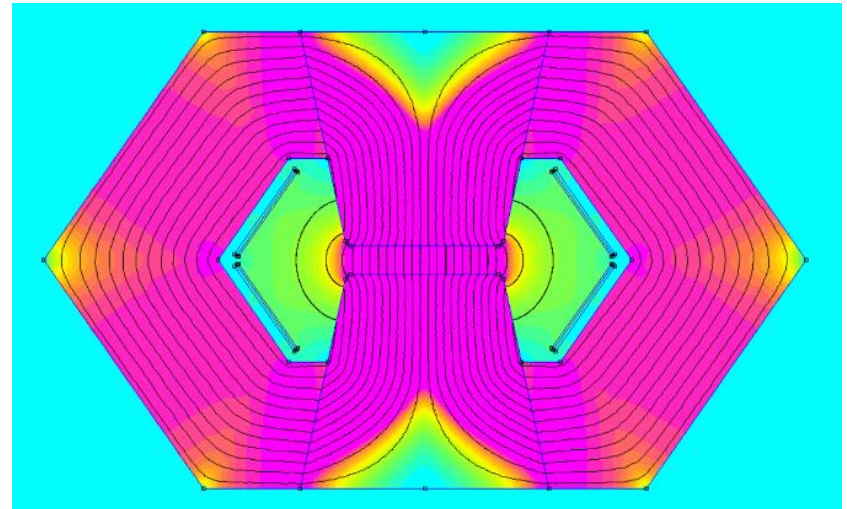
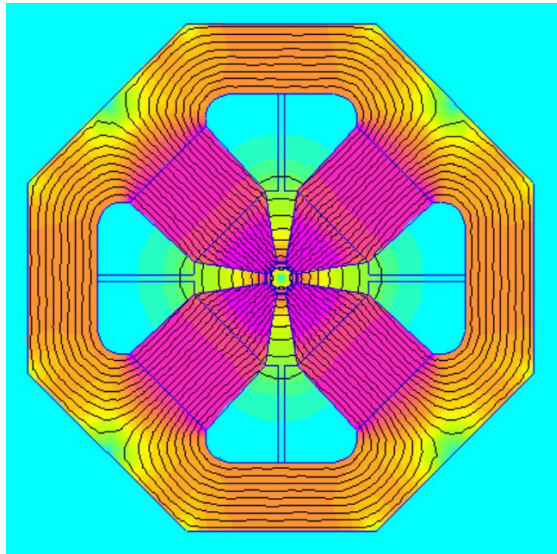
## Outline:

- **Design Requirements**
- **Material Selection**
- **Dipole Geometry**
- **Field Strength**
- **Field Quality**
- **Power Consumption**
- **Conclusions**

- **Magnetic Flux Density of 2 T**
- **Field Quality**
  - **Condition for “good field” region:  $\frac{\Delta B}{B} \leq 10^{-4}$**
- **Functionality**
  - **Work against superconducting dipoles at low energy**
  - **Work with superconducting dipoles at high energy**
  - **Max. ramp rate of 200 Hz**
- **Dimensions**
  - **Smaller than tunnel diameter of 1.2 m**
  - **Aperture width of 30 mm**
- **Power Consumption**
  - **Current density of 1.5 A/mm<sup>2</sup> for resistive power losses**
  - **Dipole power consumption in order of kW**

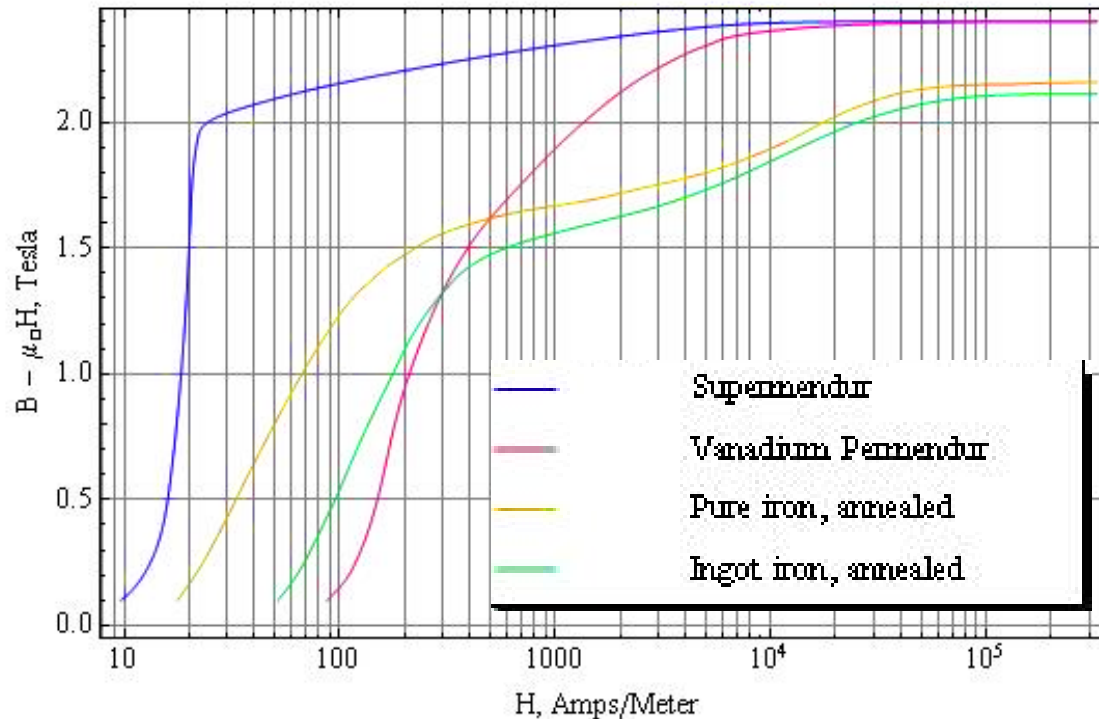


- **Finite Element Method Magnetics**
  - **2D planar domain**
  - **Low frequency**
  - **Linear/nonlinear magnetostatics**
  - **Linear/nonlinear time harmonic magnetics**



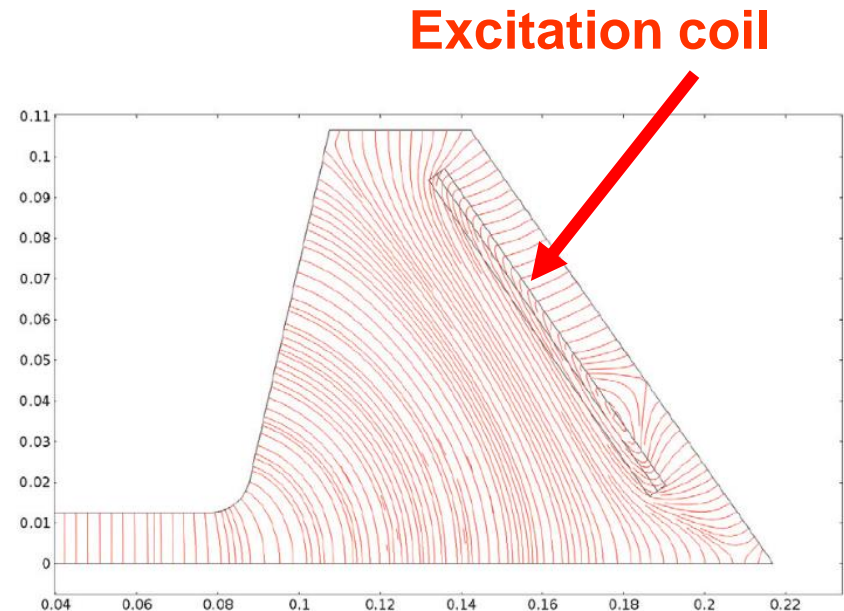
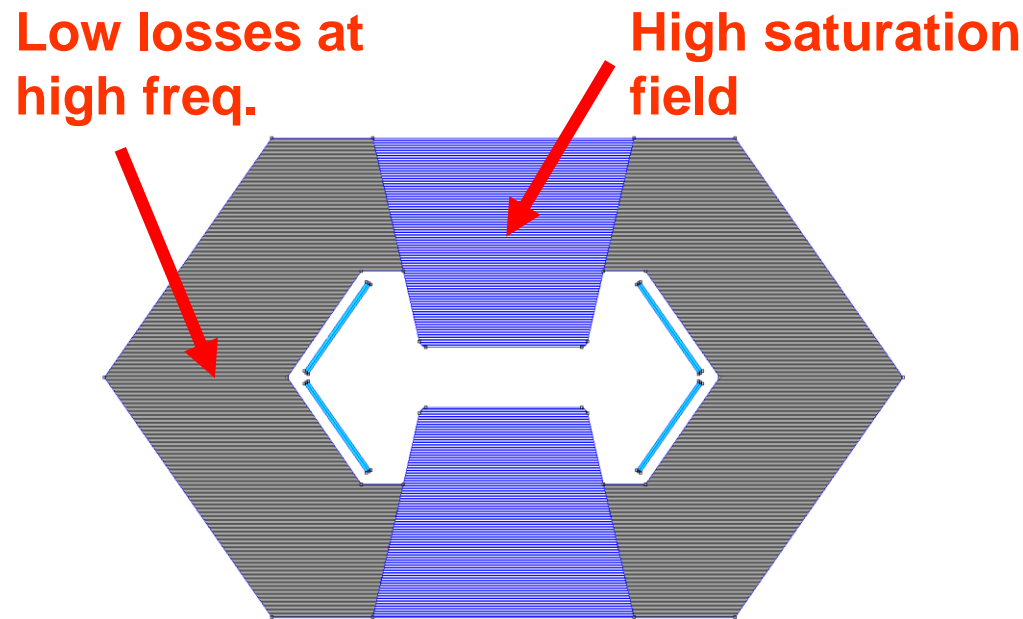
- **Material Options for Poles**

- **Permendur: 50% Steel, 48% Cobalt, 2% Vanadium**
- **Supermendur: 50% Steel, 48% Cobalt, 2% Purified Vanadium**
- **M-15 Steel (SiFe): 96% Steel, 2-4% Silicon**



FEMM Magnetics, "DC Magnetization Curves of Soft Magnetic Materials," FEMM Magnetics, 15 June 2016. [Online]. Available: <http://www.femm.info/wiki/SoftMagneticMaterials>. [Accessed 8 March 2020].

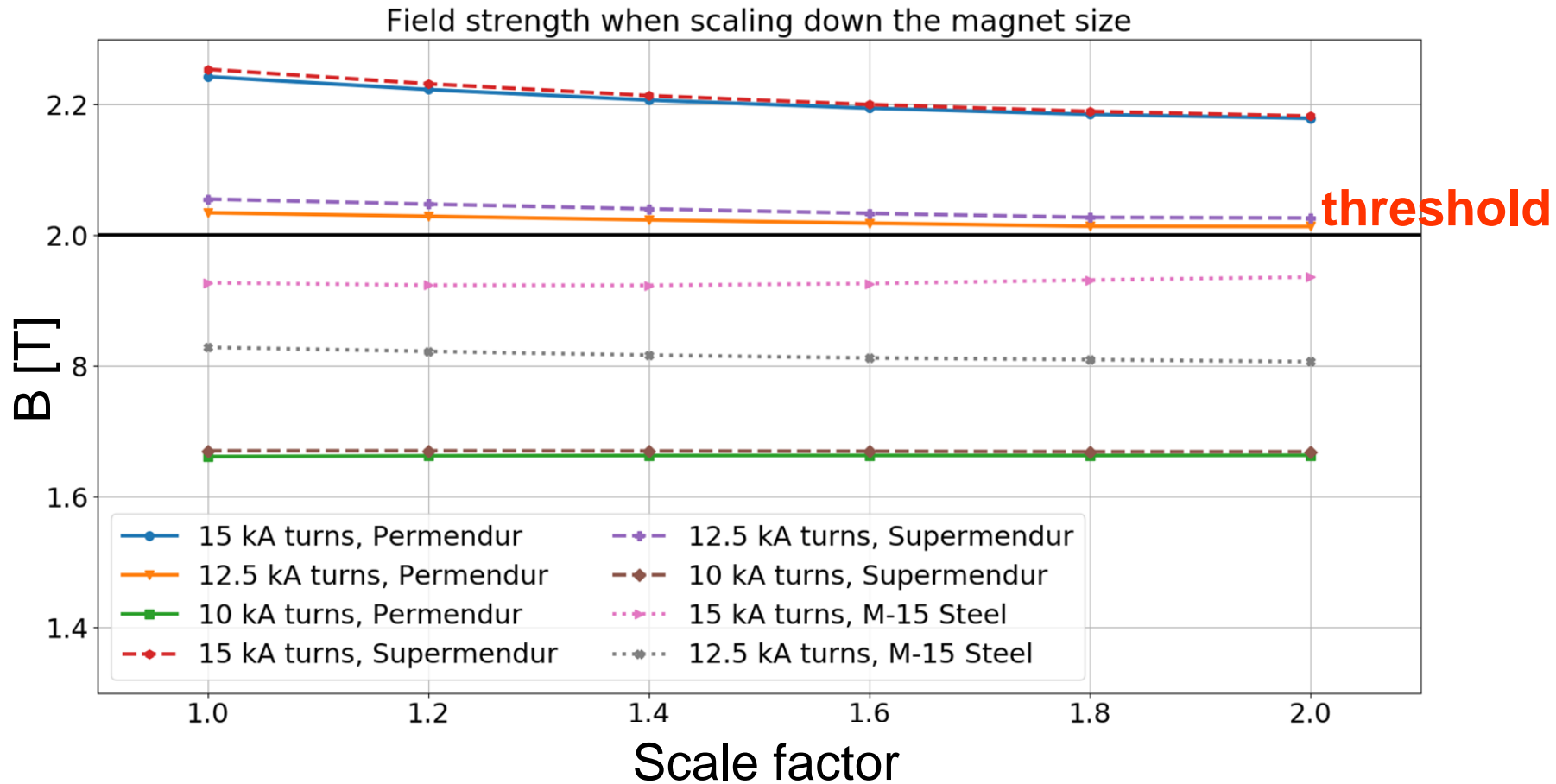
- **Model based on previous design<sup>1</sup>**
  - **Multiple materials**
  - **Coil config. minimizes eddy current losses**



<sup>1</sup>Berg, J. Scott, and Holger, Witte. "Pulsed synchrotrons for very rapid acceleration". *AIP Conference Proceedings* 1777, no.1 (2016)

<https://doi.org/10.1063/1.4965683>

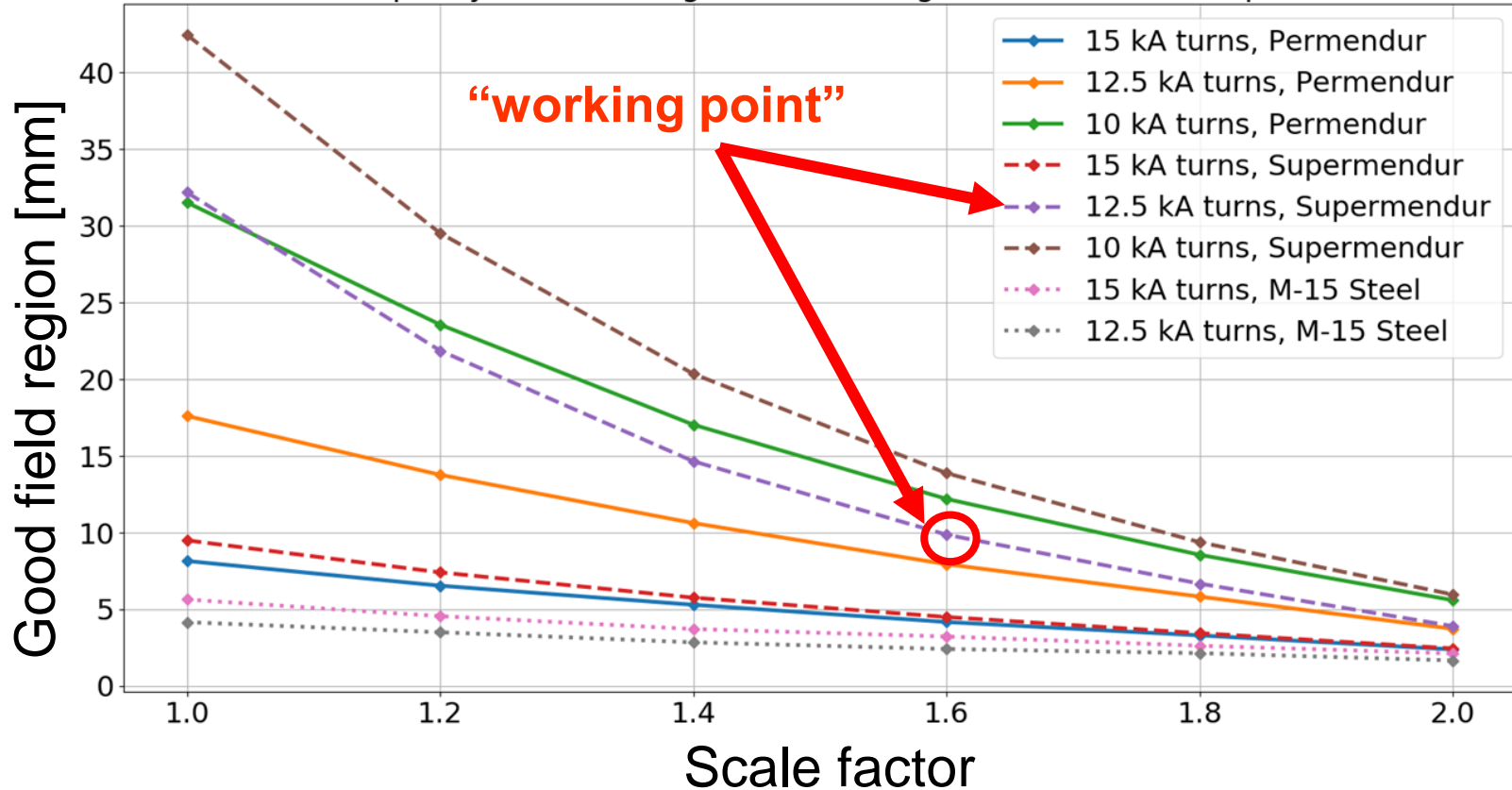
# Field Strength



- **Small variation of field strength with dipole size**
- **Small difference between the proposed materials**

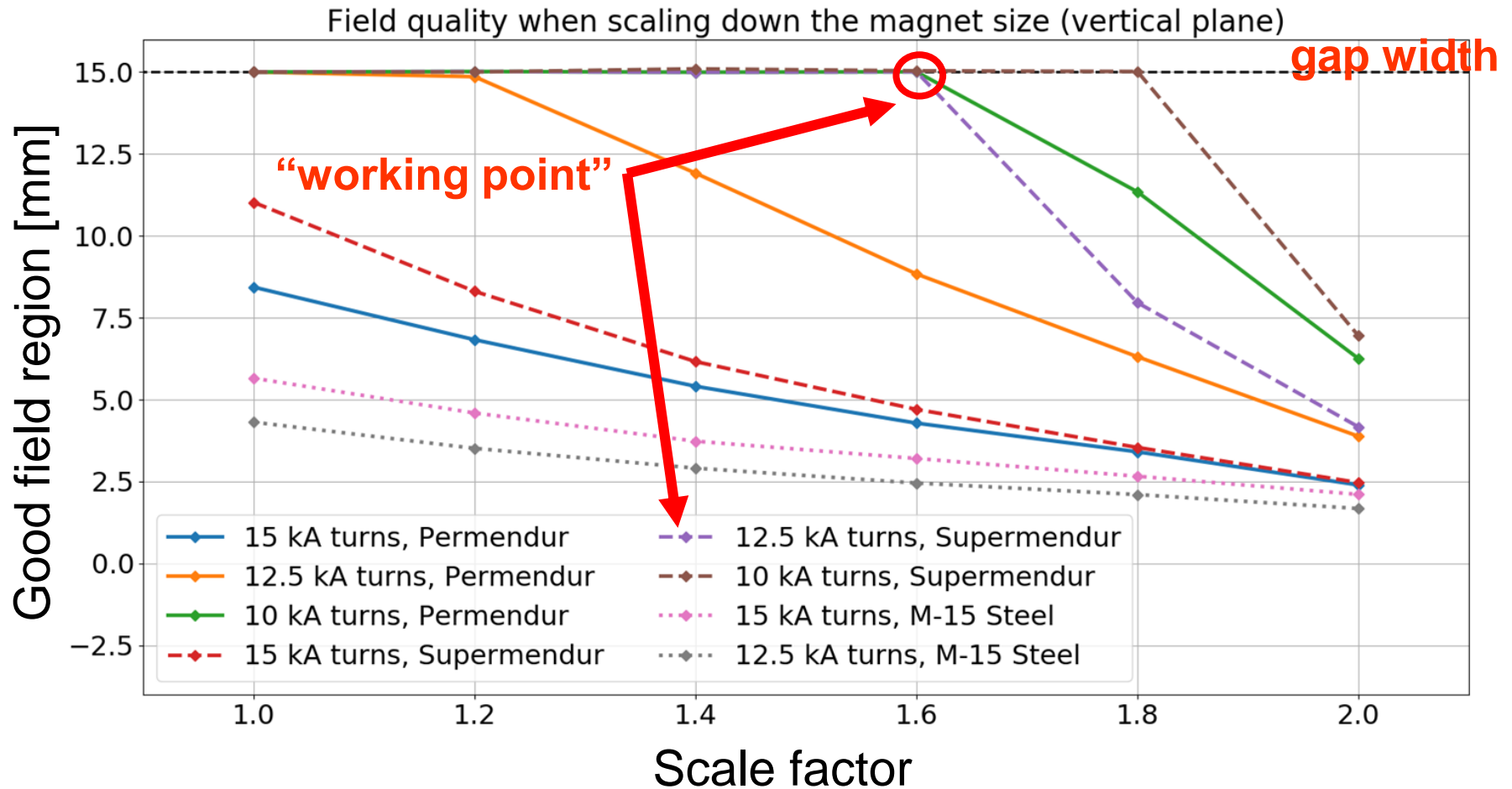
# Field Quality – Horizontal Plane

Field quality when scaling down the magnet size (horizontal plane)



- Significant reduction in horizontal field quality with size
- Supermendur maintains the field quality better

# Field Quality – Vertical Plane



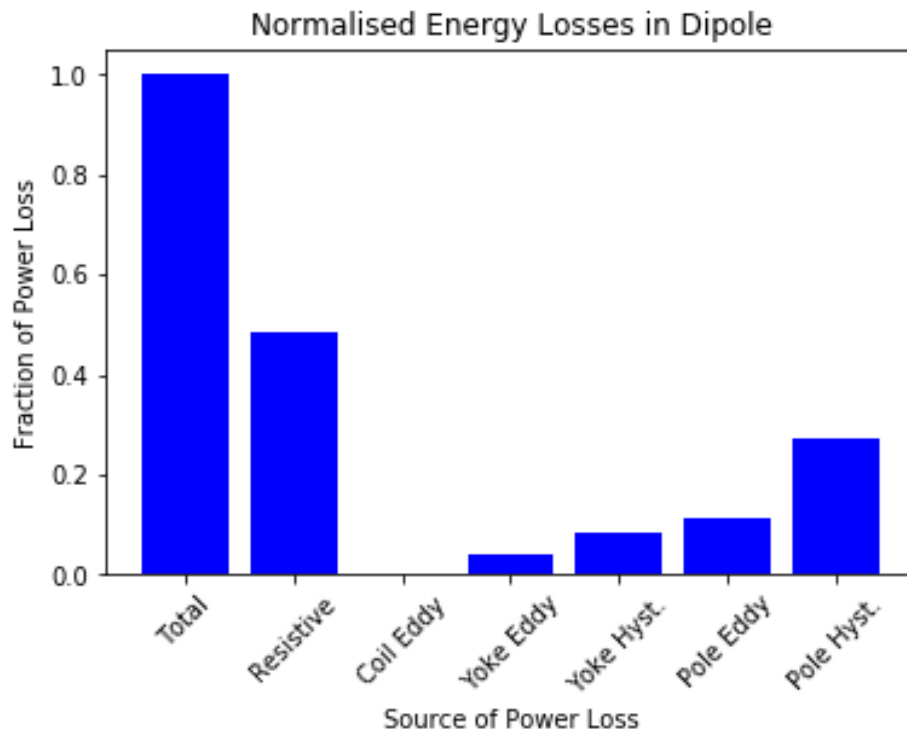
- Vertical field quality less sensitive to size
- Supermendur maintains the field quality better

Dipole specification	
Dimensions	500 x 300 mm <sup>2</sup>
Gap size	30 mm
Maximum field $B_{\max}$	2.0 T
Field quality at $B_{\max}$	$1 \times 10^{-4}$
Good field region (h x v)	20 x 30 mm <sup>2</sup>
Number of bus bars	4
Current per bus bar	12500 A turns
Average peak current density cable	5.3 A/mm <sup>2</sup>
Ramp rate	200 Hz



- **Overall Power Consumption**

- **113 kW per dipole**
- **23 MW consumption by entire system of dipoles**



- **High resistive losses**

- **Current Density of 5.3 A/mm<sup>2</sup>**
- **Limited space for wire with large cross-sectional area**

- **Low eddy current losses**

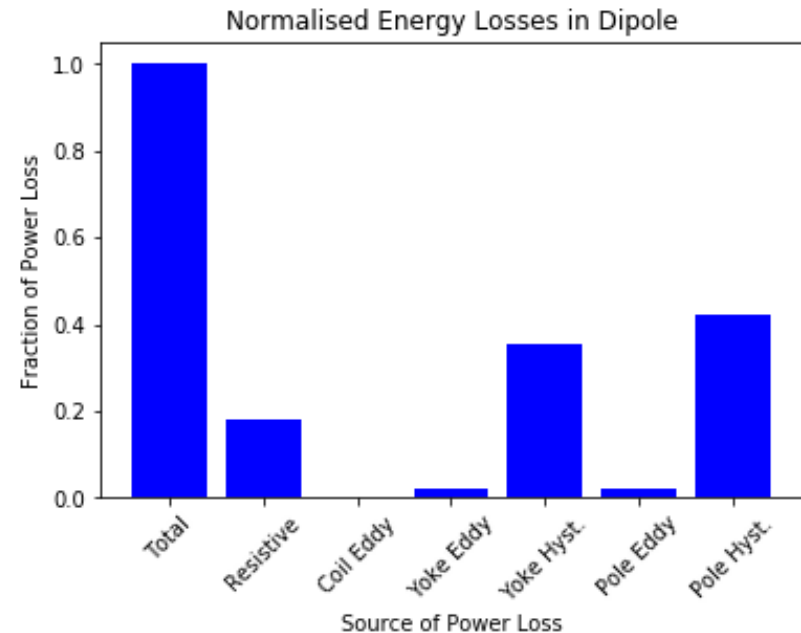
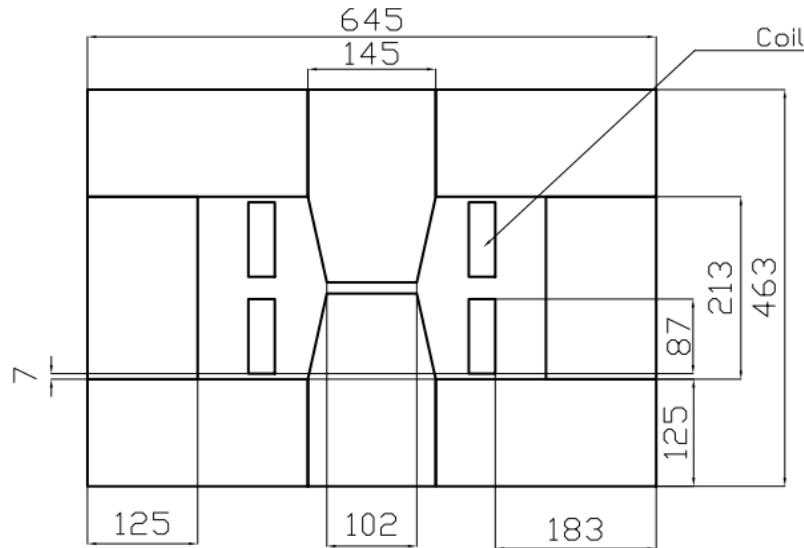
- **Magnets arranged in stacked 0.27 mm laminate sheets<sup>2</sup>**

- **Low hysteresis losses**

- **High proportion of permendur in regions of high magnetic field**



- Alternative Design<sup>2</sup>



- 63 kW power consumption per dipole
- Higher eddy current and hysteresis losses
- Resistive losses of 6 kW per dipole
  - Copper mesh cross-sectional area can be as large as 8 cm<sup>2</sup>
  - Current density of 1.5 A/mm<sup>2</sup>

<sup>2</sup> H. Witte, J. Berg, P. Kovach, M. Anerella and M. Lopes, "Rapid Cycling Dipole Magnet," in Proceedings of PAC2013, Pasadena, CA USA RAPID, Pasadena, 2013.

- Main Design**

Material	Mass Required (One Dipole)/Tonnes	Mass Required (System)/Tonnes
Coils (Copper Wire)	0.11	22.71
Yoke (3% Si-Fe)	4.28	857.22
Poles (Supermendur)	4.11	823.43

- Alternative Design**

Material	Mass Required (One Dipole)/Tonnes	Mass Required (System)/Tonnes
Coils (Copper Wire)	0.62	124.74
Yoke (3% Si-Fe)	10.91	2181.78
Poles (Supermendur)	3.87	775.46

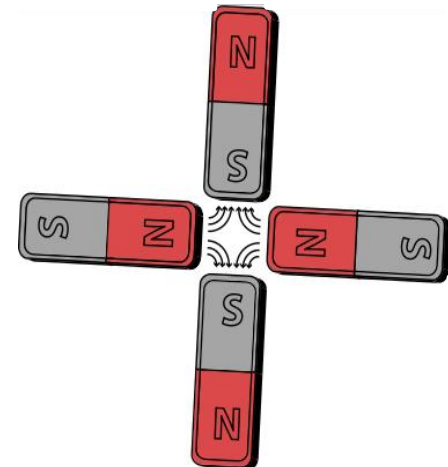
**Larger amounts of M-15 Steel and Copper wire required**

- **Magnetic Flux Density**
  - **Magnetic flux density of 2 T achieved in FEMM**
- **Field Quality**
  - **Field quality of  $\frac{\Delta B}{B} \leq 10^{-4}$  obtained with supermendur poles at 12500 A turns**
- **Power Consumption**
  - **113 kW per dipole (23 MW total)**
  - **Limited by cross-sectional area of copper wire**
  - **Magnet size has been minimised to reduce power consumption and mass requirements**

# Quadrupole Magnets

## Outline:

- Design Requirements
- Material Selection
- Design Layouts
- Performance
- Power Loss
- Conclusions



## Extra Quadrupole scheme

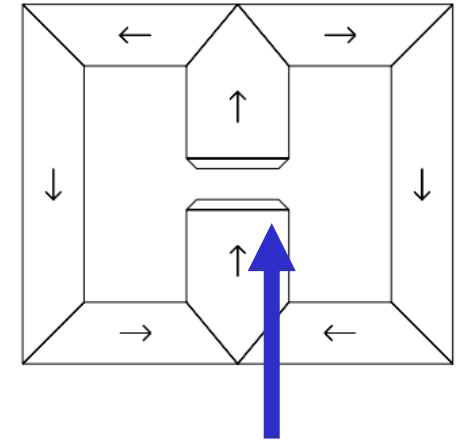
	Quads In RCS1	Quads in RCS2	DS quads in RCS 1	DS quads in RCS 2
<b>Number</b>	96	96	96	96
<b>Ramping rate (Hz)</b>	135	180	135	180
<b>Aperture size (mm)</b>	<b>38</b>	<b>28</b>	<b>38</b>	<b>28</b>
<b>Gradient (T/m)</b>	<b>57.6</b>	<b>96</b>	<b>57.6</b>	<b>103.6</b>

**DS: dispersion suppression**

## Accelerating Muons to 2400 GeV/c with Dogbones Followed by Interleaved Fast Ramping Iron and Fixed Superconducting Magnets

D. J. Summers\*  
University of Mississippi-Oxford, University

Published in 2002

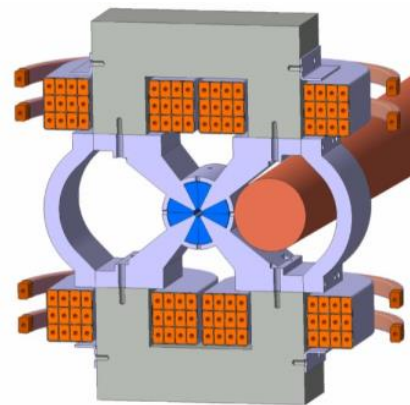
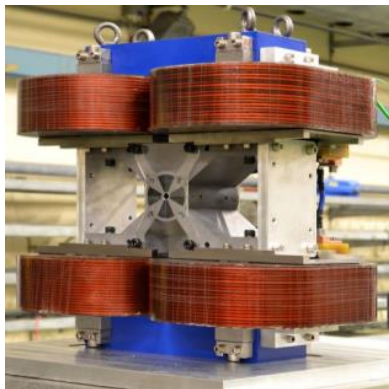


**Supermendur**

## Design and Manufacture of a Hybrid Final Focus Quadrupole Model for CLIC

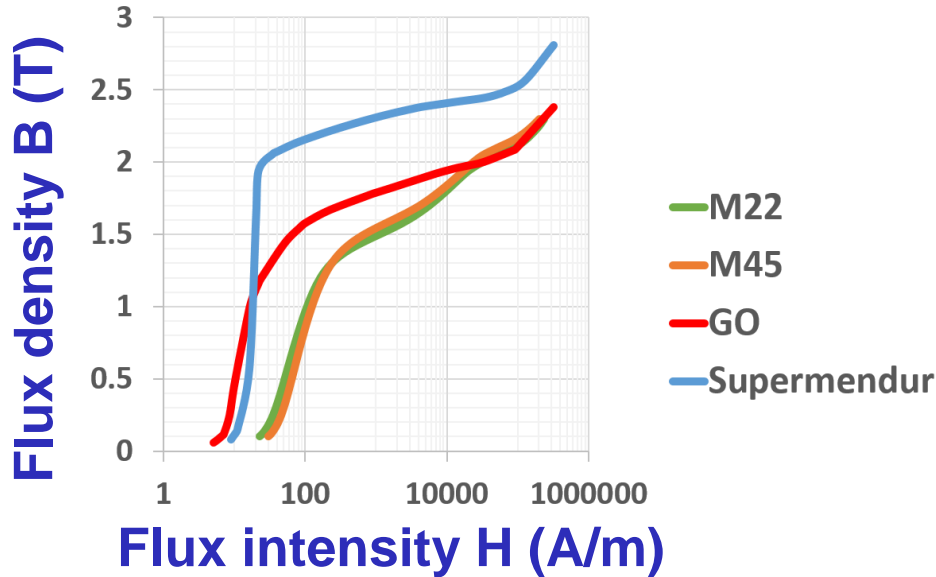
Alexey Vorozhtsov, Michele Modena, and Davide Tommasini

IEEE TRANSACTIONS ON APPLIED SUPERCONDUCTIVITY, VOL. 22, NO. 3, JUNE 2012

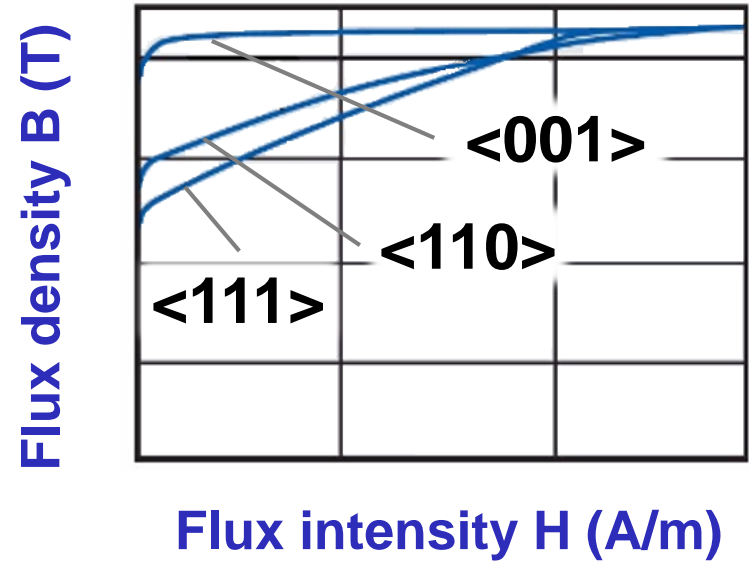


- Permendur**
- 1010 steel**
- Nb<sub>2</sub>Fe<sub>14</sub>B**

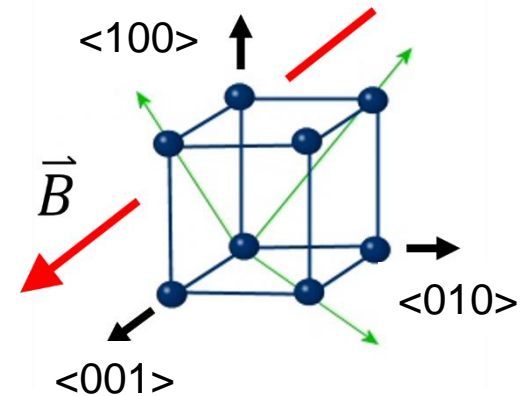
## BH curves



## BH curves of crystal orientations



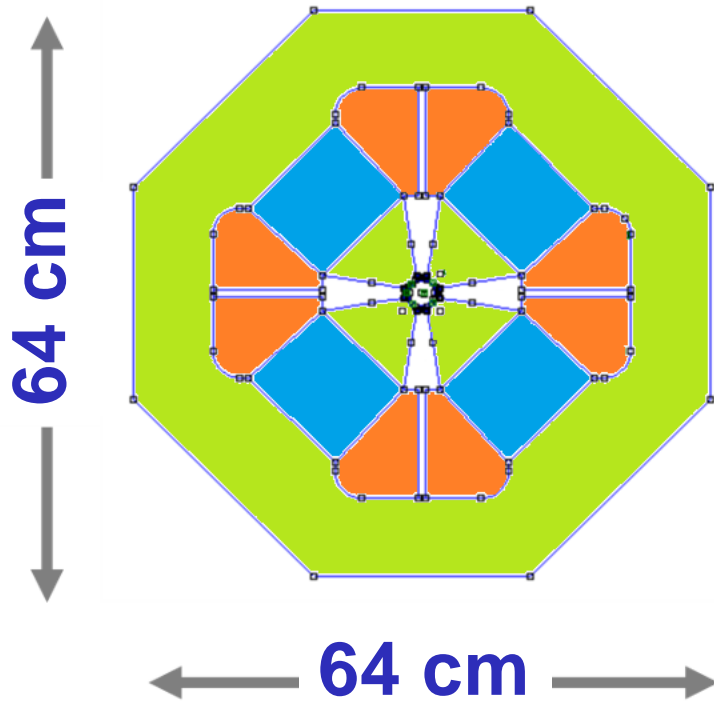
## Crystal structure of Si



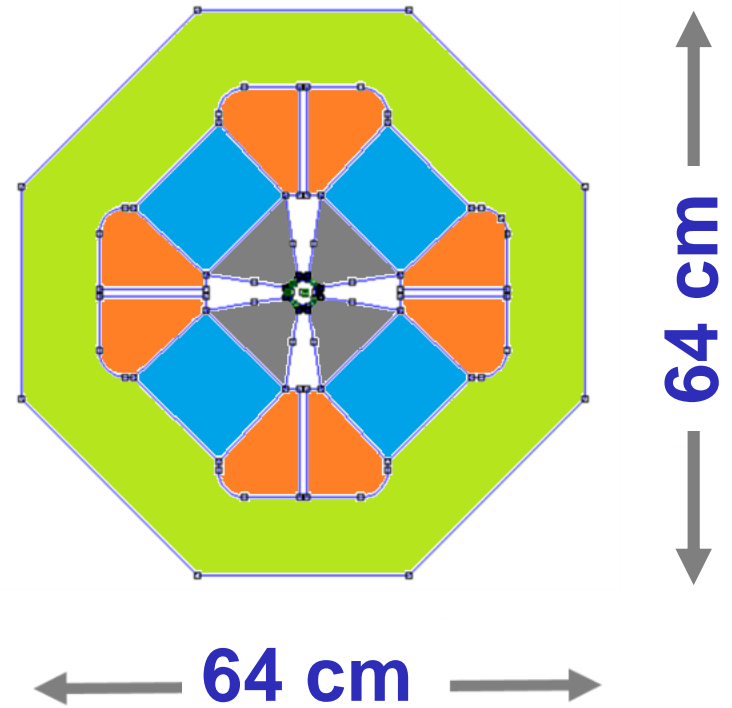
## Hysteresis effect $P_{loss} = C_m B^\alpha f^\beta$

	$C_m \times 10^{-3}$	$\alpha$	$\beta$
GO Si	1.2	2.3	1.5
AISI M22	8.2	2.2	1.3
AISI M45	13.5	1.8	1.3

## RCS1



## RCS2



- M22 Si steel
- 3% GO Si steel
- Copper wire
- Supermendur

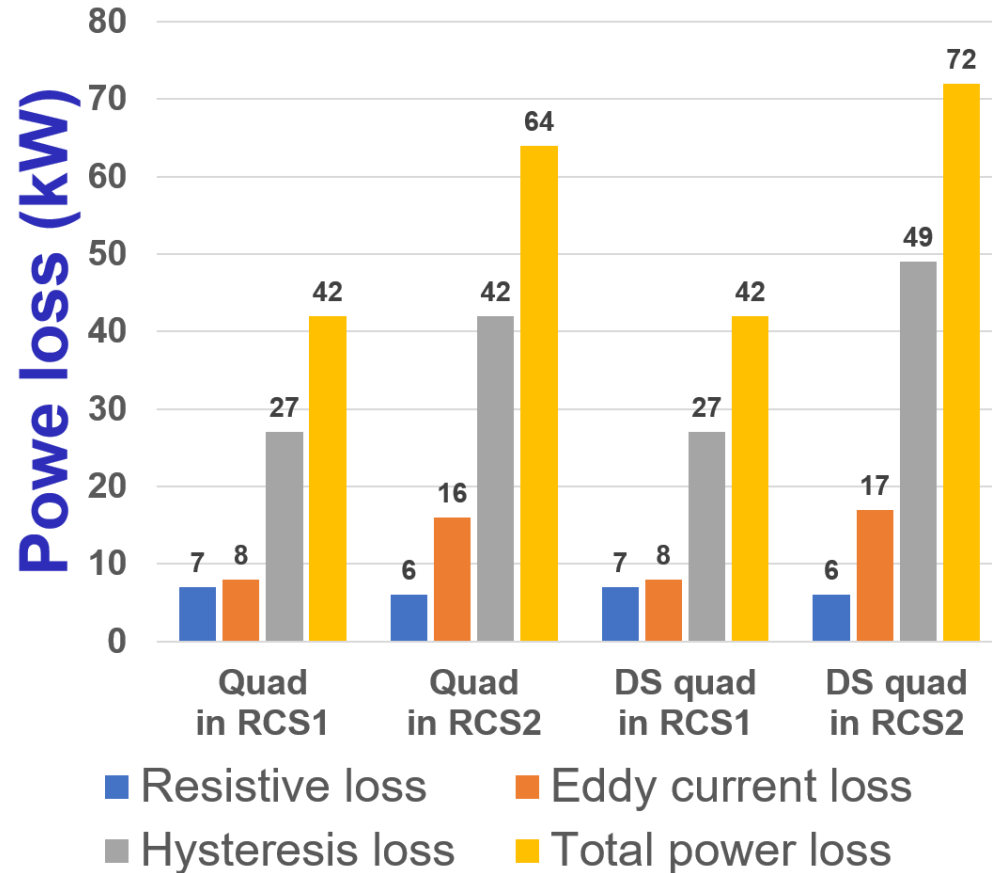


## Extra Quadrupole scheme

	Quad in RCS1	Quad in RCS2	DS quad in RCS1	DS quad in RCS2
Ramping rate (Hz)	135	180	135	180
Gradient (T/m)	57.6	96	57.6	103.6
Aperture size (mm)	38	28	38	28
Pole tip field (T)	0.8	1.34	0.8	1.45
Current (A)	<b>8820</b>	<b>7740</b>	<b>8820</b>	<b>8600</b>
Efficiency (%)	<b>98</b>	<b>96</b>	<b>98</b>	<b>93</b>
Field quality $\Delta g/g$ in $\frac{2}{3}R$	<b><math>6 \times 10^{-4}</math></b>	<b><math>5 \times 10^{-4}</math></b>	<b><math>6 \times 10^{-4}</math></b>	<b><math>5 \times 10^{-4}</math></b>

**DS: dispersion suppression**

## Power loss of a quad



## Estimation for both rings

	RCS1	RCS2
Number of quads	192	192
Weight (tonne)	784	782
$P_{loss}$ (MW)	10	11
Overall Weight (tonne)	1564	
Overall $P_{loss}$ (MW)	<b>21</b>	

- **A hybrid material design**
- **Target gradients of B-field achieved**
- **The average Field quality is  $6 \times 10^{-4}$**
- **Total weight is 1564 tonnes**
- **Total power loss of quads is 21 MW**

# Radiation Considerations

## Student Design Project

**Carlo Mussolini**

# How do radiation regulations work?

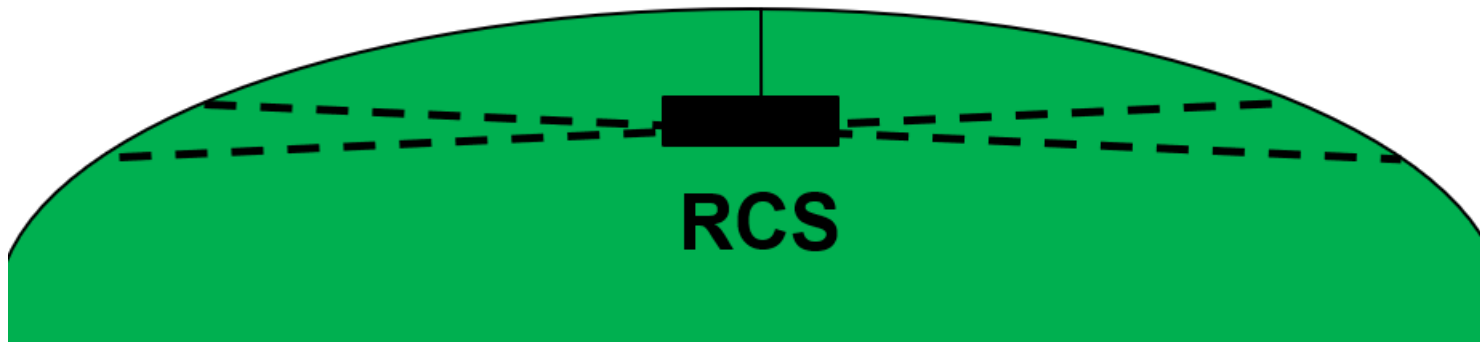
- The Sievert (Sv) is a unit describing the effects of radiation on an organism
- The regulations we are interested in are aimed towards the protection of individuals, so in Sv
- The limits to the general population are 0.3 mSv for people and 1mSv for the environment

Chest X-ray	0.1 mSv
Average background exposure in one year	3 mSv
Abdominal X-ray	4 mSv
Living on the Colorado Plateau for one year	4.5 mSv
Typical yearly dose for a uranium miner	5-10 mSv
Full-body CT scan	10 mSv
Lowest dose for any statistical risk of cancer	50 mSv

# The Neutrino Problem

# The neutrino problem (!?)

- Muon decays produce neutrinos each with about  $1/3$  of the muon's energy
- Travel straight through the Earth and emerge in a cone in the plane of the accelerator
- The radiation is highly focused in straight sections



- **Problems arise with muon colliders as the energy frontier**
- **As the energy of the accelerator is increased the neutrino beam becomes more focused**
- **Flux and energy are high enough that with the conversion tables the effects are significant**

$$\theta \sim \sqrt{\epsilon/\gamma\beta} + 1/\gamma$$

$$\log(C) = 2 \log(E) - 15$$

Emittance:  $\epsilon \sim 25 \mu\text{m}$

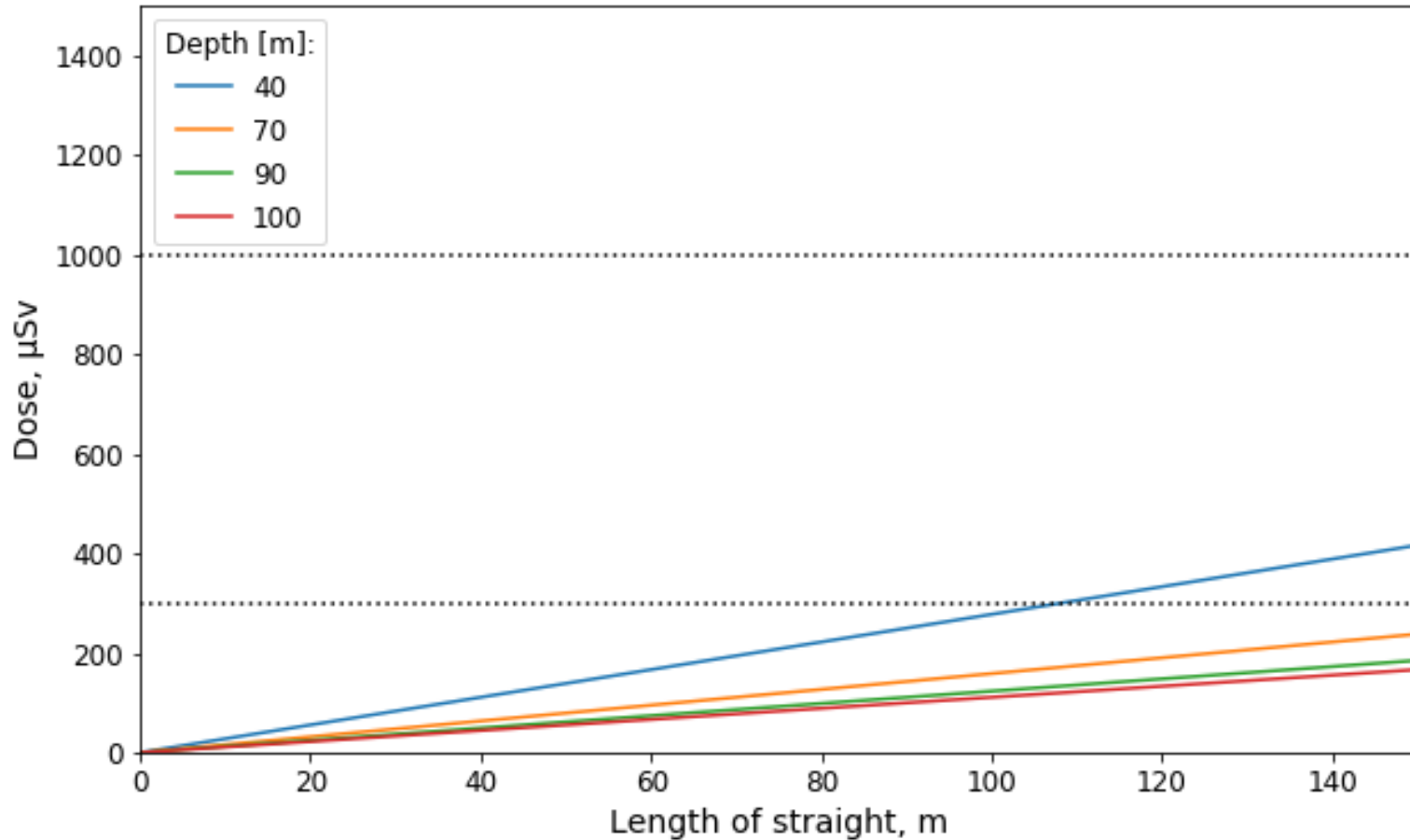
Beta function:  $\beta \sim 350\text{m}$

Rel. Gamma:  $\gamma \sim 1000 - 15000$



# The neutrino problem

Dose Produced from Straight Sections  
at an Energy of 100-900 GeV for a Circumference of 6.9 km

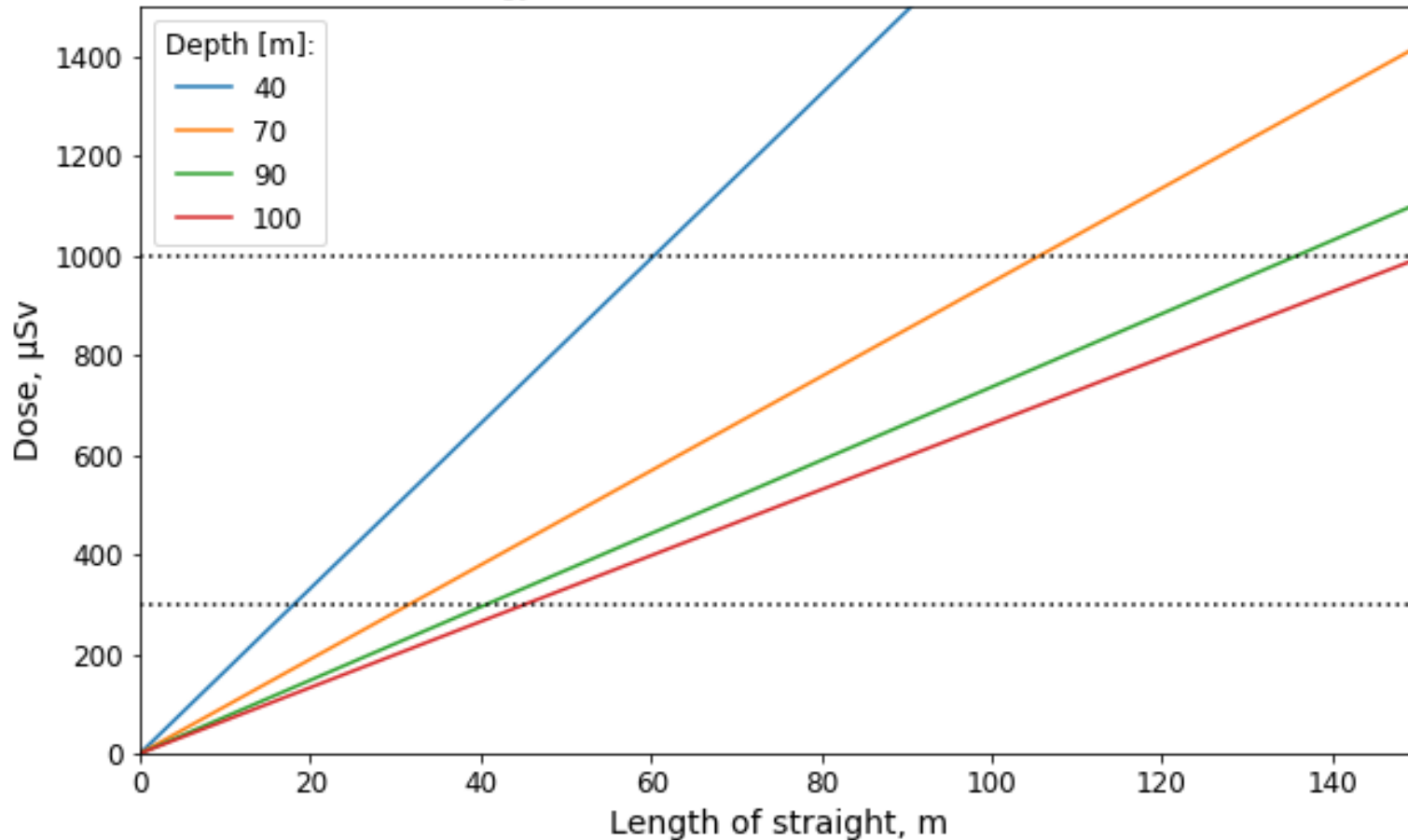


**Depth SPS: 40 m**

**Length of straights in RCSs: 130 m**

# The neutrino problem

Dose Produced from Straight Sections  
at an Energy of 900-1500 GeV for a Circumference of 6.9 km



**Depth SPS: 40 m**

**Length of straights in RCSs: 130 m**

## The parameters that affect the radiation:

- Time the accelerator is ran for
- Depth of accelerator
- Emittance of the beam
- Length of straights
- Number of muons being accelerated

Not sensible to change

Add small bends or wigglers

Change from the MAP scheme to the LEMMA scheme

# The Electron Problem

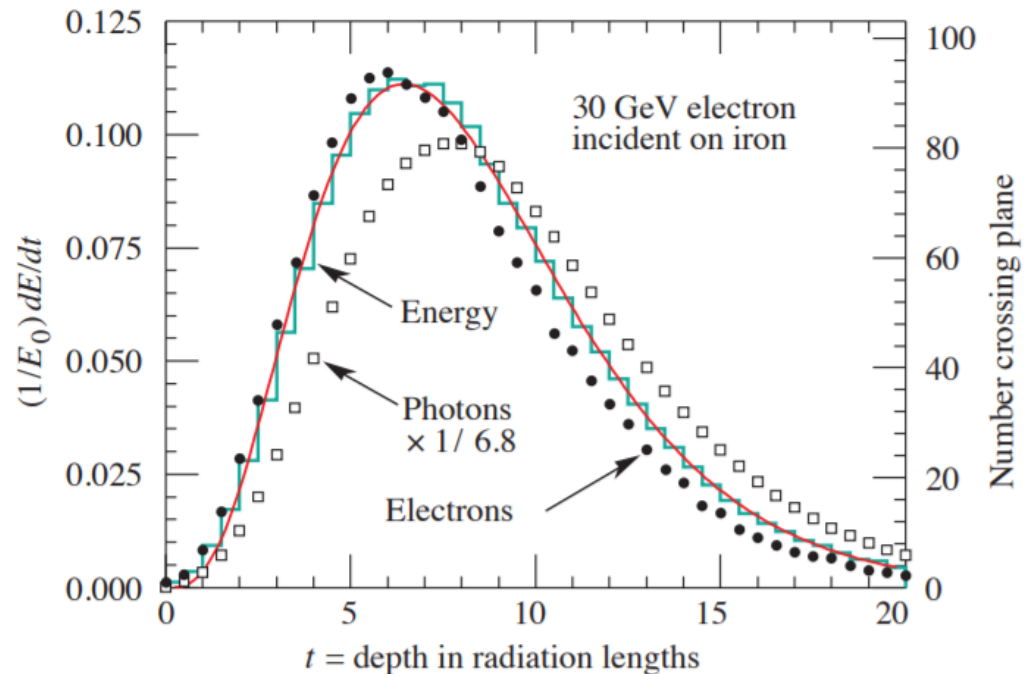
- **As the muons decay, electrons are produced**
- **These electrons do not have the right energy to go around the accelerator**
- **They fall out of the bunches, depositing energy in the accelerator**

**Why is this important and how do we evaluate the effects of the electrons on the machine itself?**

# The electron problem

There are no simulations available for the desired energy range – Especially not in geometries we are interested in

Assuming about 12 cm of material, which is 6 radiation lengths, 25% of energy is deposited in machine



Accelerator	Energy Deposited per Year
RCS1	1.4 TJ
RCS2	1.1 TJ
LEP	0.1 MJ

- **LEP** ran for 11 years and was one order of magnitude below significant radiation damage
- **Clearly if nothing is done about the electrons, the components of the accelerators would be damaged extremely quickly**

- **There are designs for shielding for a Higgs factory and for magnets to reduce energy deposition**
- **Would need to check the efficacy of these at higher energies**
- **It may be possible to extract the electrons, since these act differently in the magnets compared to the muons**
- **Minimising materials used can also help to minimise the energy deposited**



- **Difficult quantities to investigate**
- **Clearly there is the need for more in depth studies**
- **The effects of neutrinos are surprisingly significant and may prove to limit the energies a muon collider can reach**
- **Electron damage needs to be investigated to ensure the accelerator would be functional for a sensible length of time**
- **While these issues are significant, they are not insolvable and muon colliders still offer a unique opportunity to probe the high energy frontier**

# Conclusion

## Student Design Project

- **A lattice that works for all energy ranges, with zero suppression sections and with low tune shift has been designed**
- **Longitudinal dynamics and collective effects to first order are acceptable and further RF optimisation may reduce the already low losses**
- **Existing magnets already provide enough bending but further studies may increase the field strength and further reduce power losses**
- **Radiation and energy deposition are issues that must be carefully considered but can be mitigated**
- **All of this was achieved with the constraint of using the SPS tunnel to significantly lower costs**

**Thank you to Emmanuel and Ciprian  
for their help**

**Thank you for listening**