

Deconfining Phase Boundary of Rapidly Rotating Hot and Dense Matter and Analysis of Moment of Inertia

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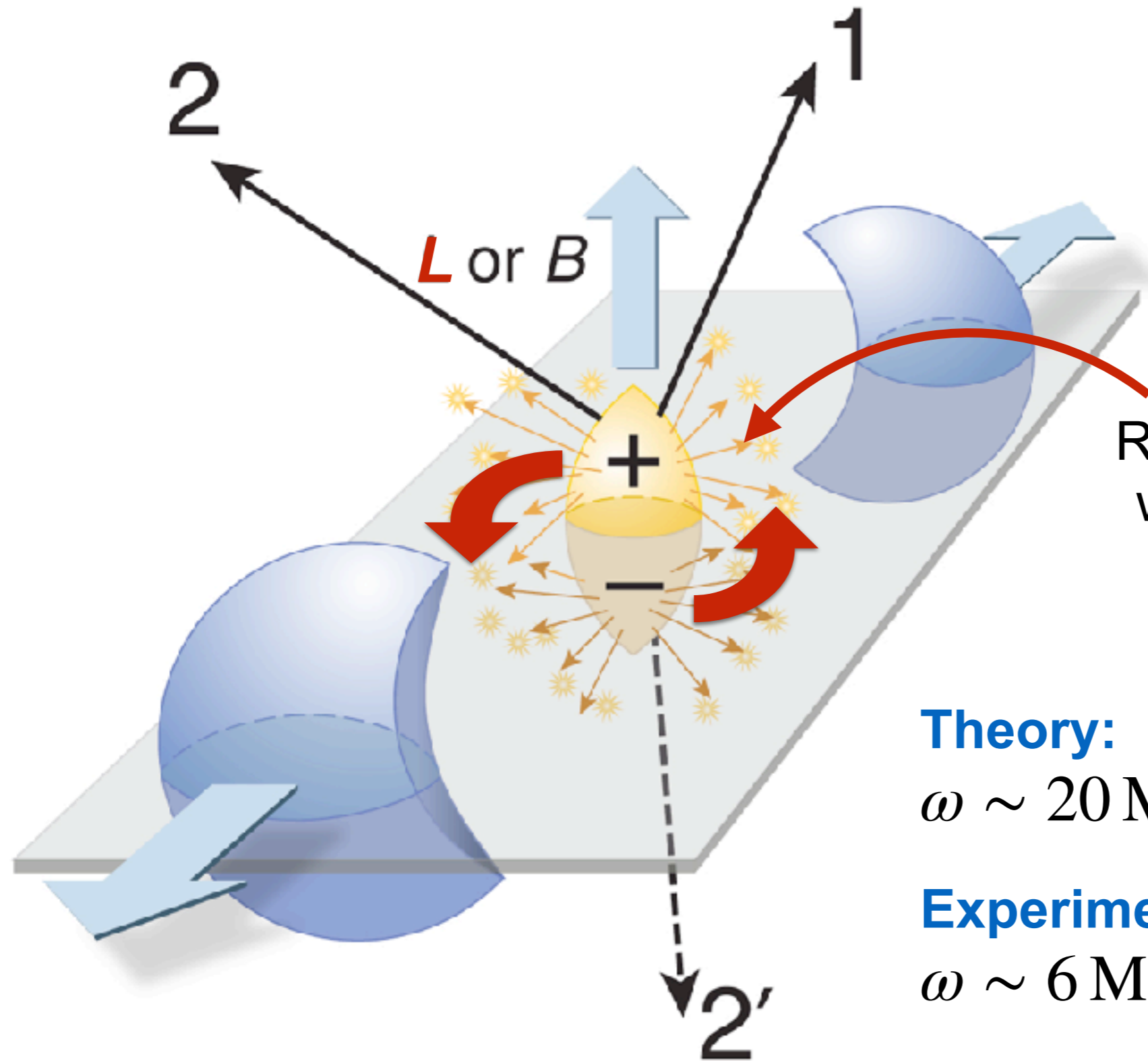
Reference:

Y. Fujimoto, K. Fukushima, Y. Hidaka, “Deconfining Phase Boundary of Rapidly Rotating Hot and Dense Matter and Analysis of Moment of Inertia,” Phys. Lett. B 816 (2021) 136184, arXiv:[2101.09173 \[hep-ph\]](https://arxiv.org/abs/2101.09173).

6 November 2021, ATHIC 2021@Inha Univ.

Rotating quark-gluon matter

Non-central heavy-ion collisions:



Rotating matter is created
with angular momentum

$$L \sim 10^6 \hbar$$

Theory:

$$\omega \sim 20 \text{ MeV}$$

Jiang, Lin, Liao (2016)

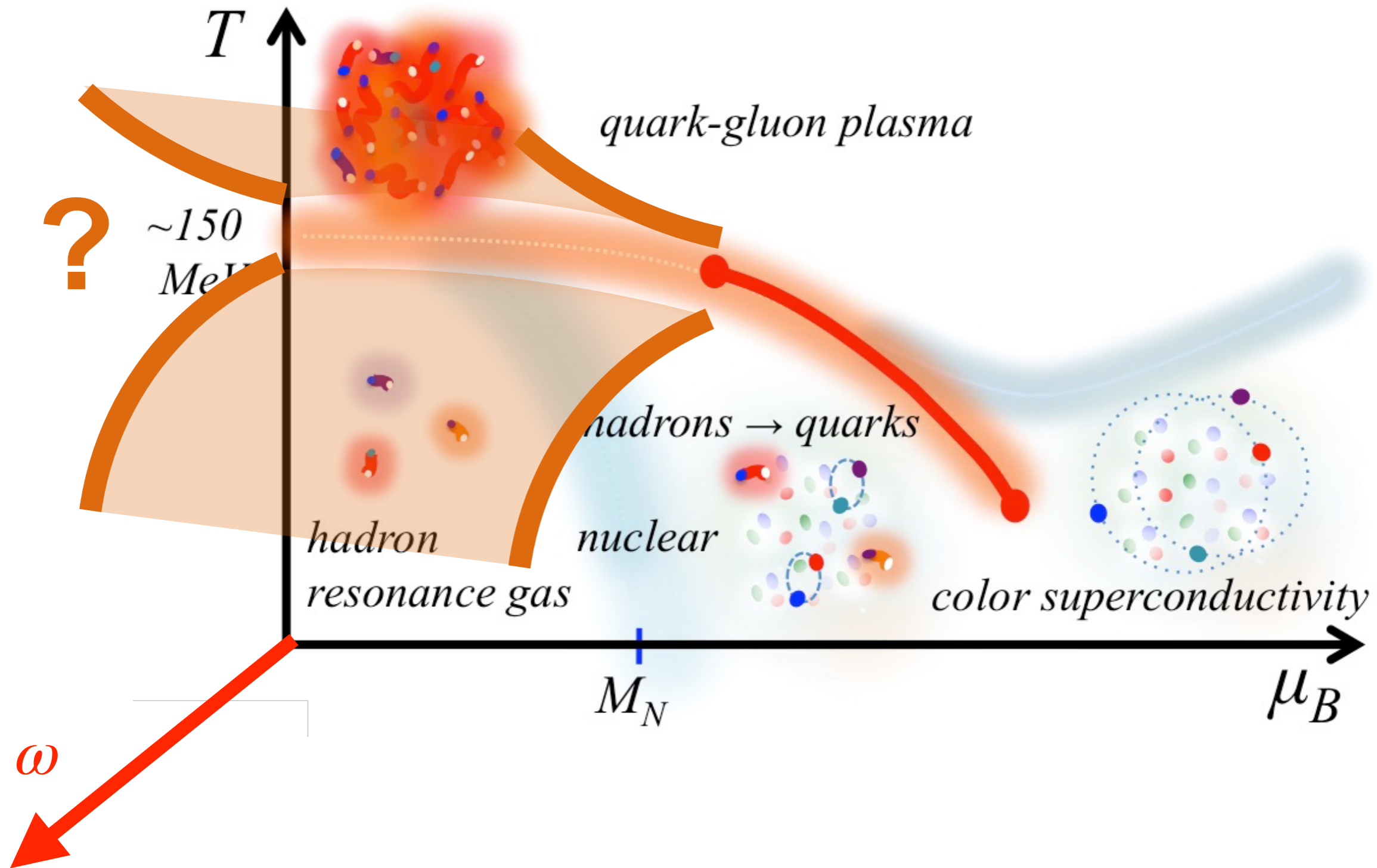
Experiment (global Λ polarization):

$$\omega \sim 6 \text{ MeV}$$

STAR collaboration (2017)

QCD phase diagram under rotation

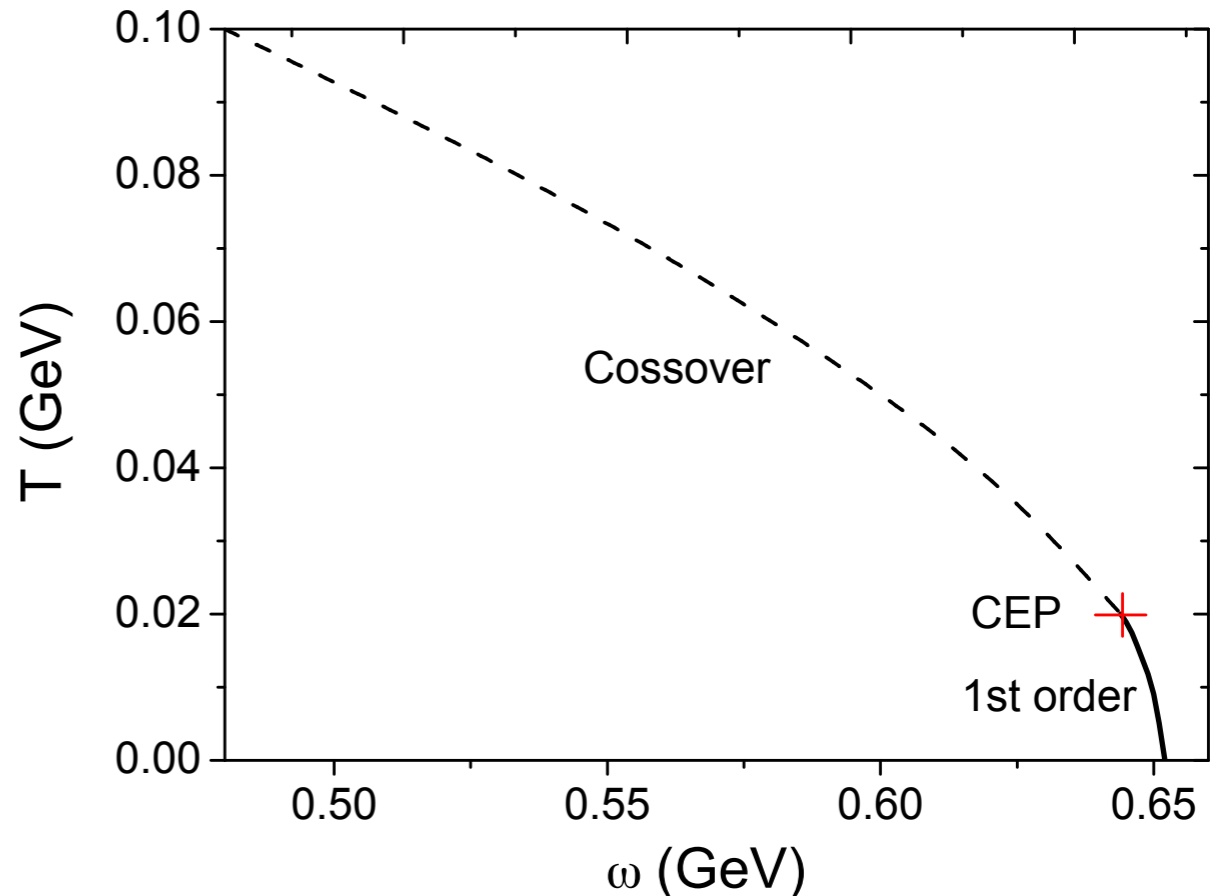
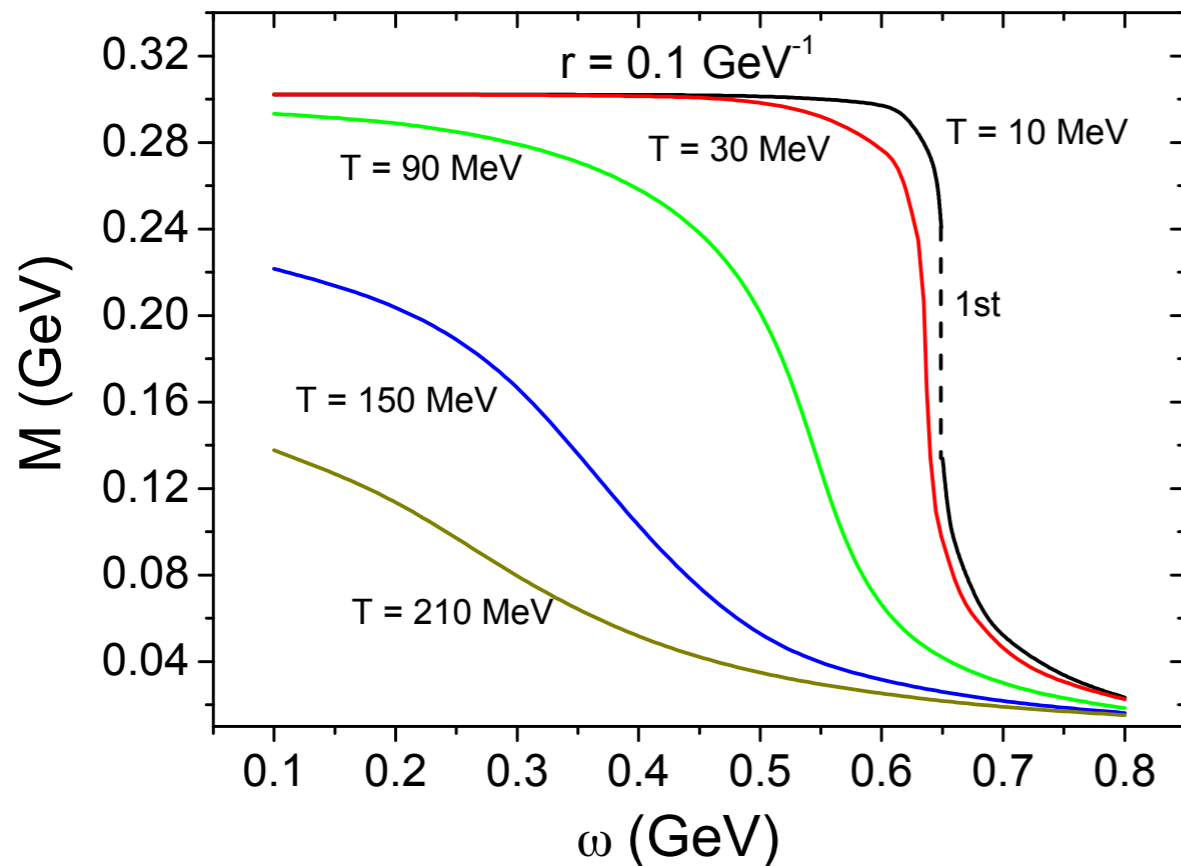
Taken from: Baym, Hatsuda, Kojo, Powell, Song, Takatsuka (2017)



Chiral transition of rotating matter

Jiang,Liao (2016)

NJL model analysis shows...



↑ Rotation suppresses the chiral condensate

More or less accepted consensus:

Critical temperature T_c drops with increasing ω

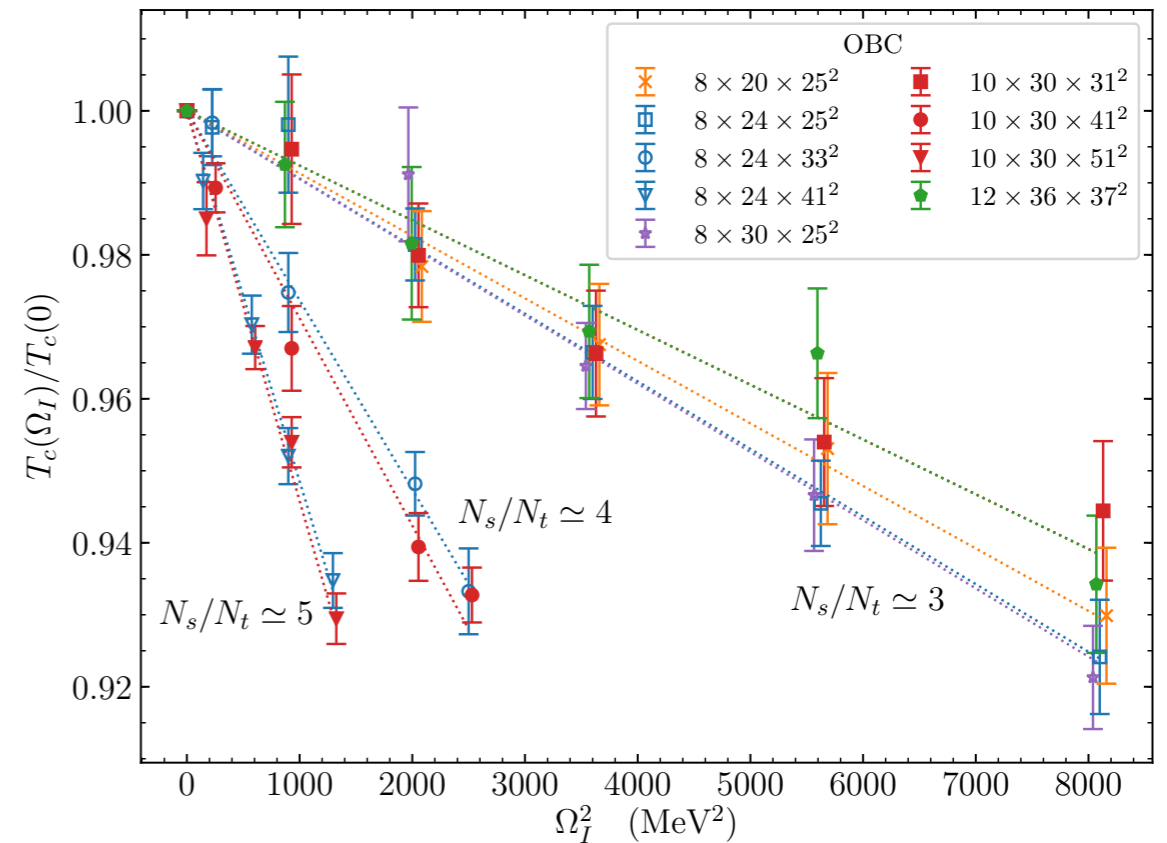
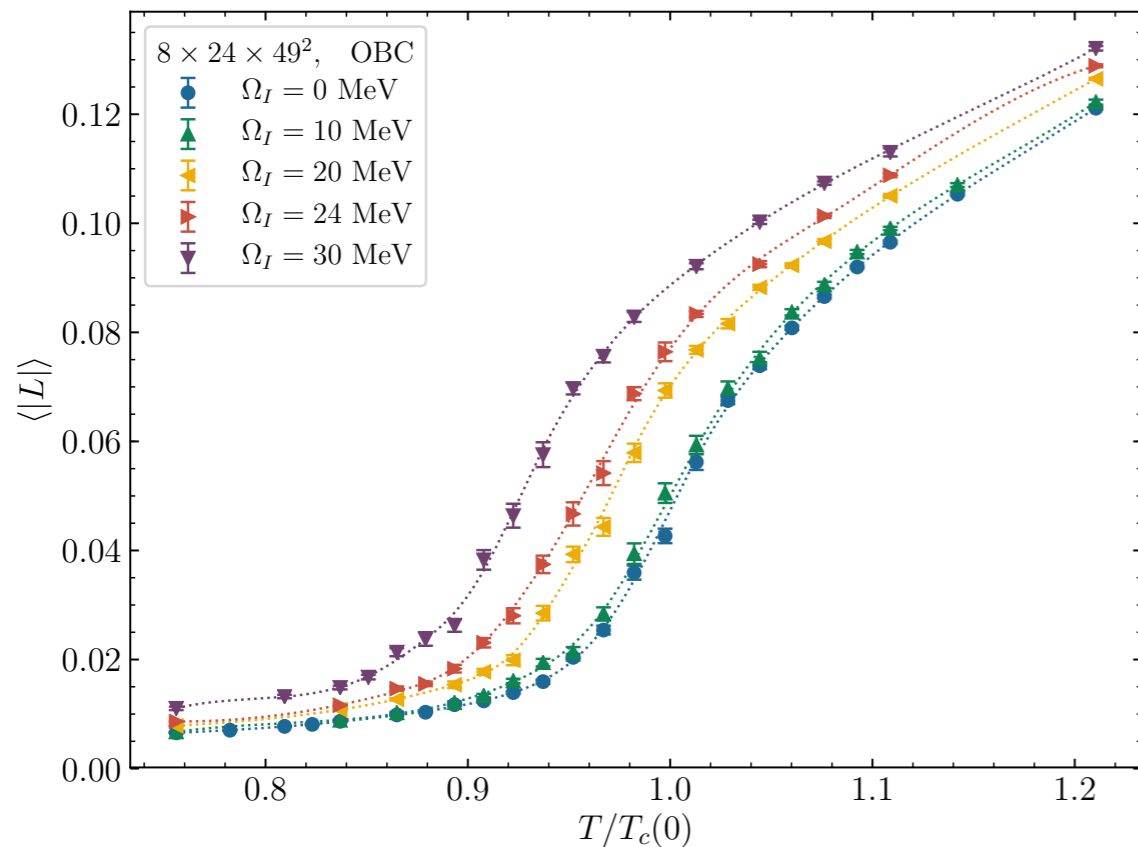
Other studies: Ebihara,Fukushima,Mameda (2016); Chernodub,Gongyo (2016); Wang,Wei,Li,Huang (2018); Zhang,Hou,Liao (2018); ...

Deconfinement of rotating matter

Lattice formulation of imaginary rotation: Yamamoto, Hirono (2013)

Braguta, Kotov, Kuznedeleev, Roenko (2020, 21)

Lattice result of the Polyakov loop in pure QCD under imaginary rotation $\Omega_I = -i\omega$:



Deconfinement temperature T_c **rises**
with increasing ω

$$\frac{T_c(\Omega_I)}{T_c(0)} = 1 - C\Omega_I^2$$

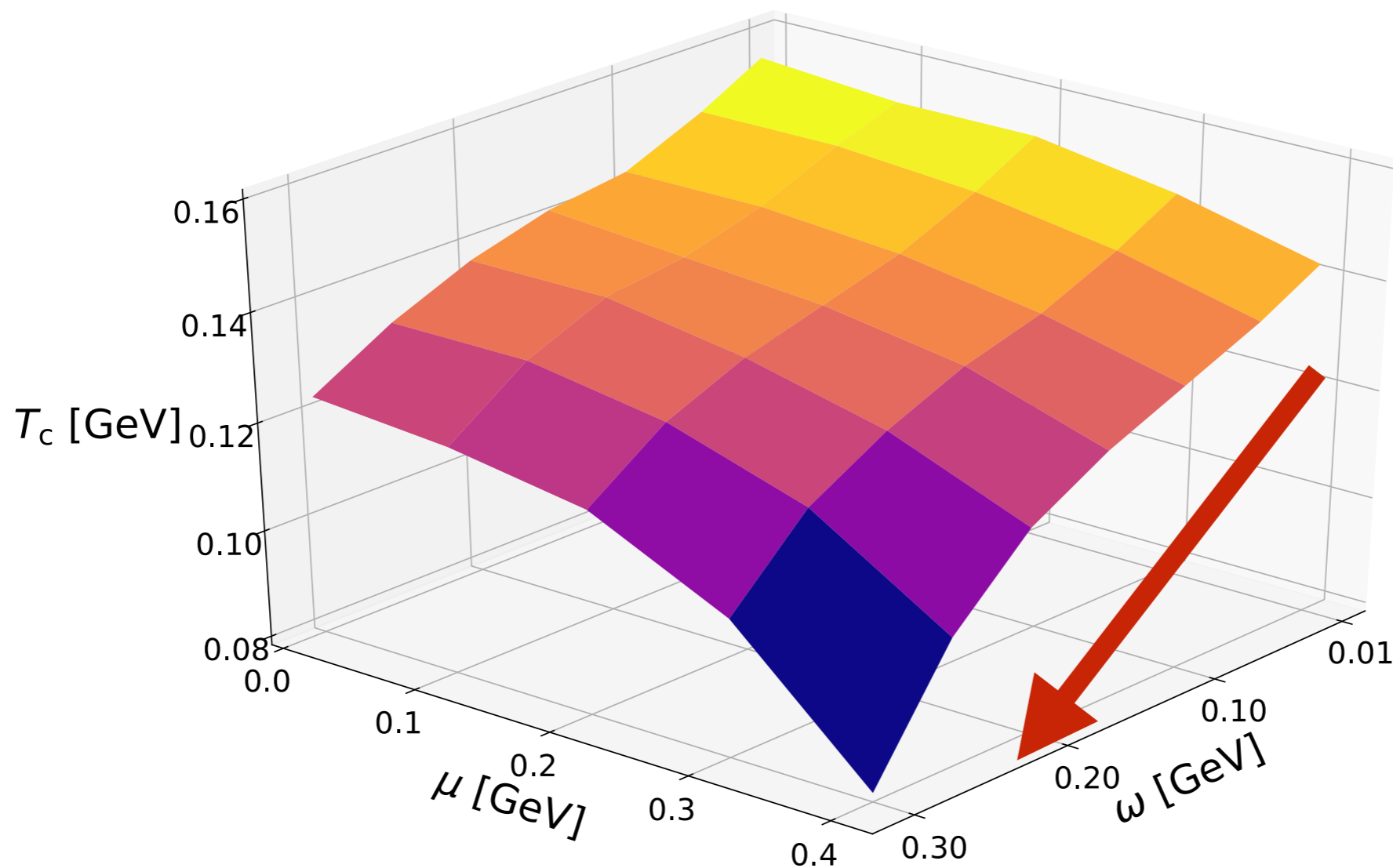
At odds with chiral transition!?

$$= 1 + C\omega^2$$

Deconfinement of rotating matter

Fujimoto, Fukushima, Hidaka (2021)

Our result based on the hadron resonance gas model:



Deconfinement temperature T_c **drops**
with increasing ω

See also: Holography approach: Chen, Zhang, Li, Hou, Huang (2020)

Compact QED approach: Cherdodub (2020)

these works also give the same behavior as ours

Our phenomenological approach

Hadron resonance gas (HRG) model

total pressure: $p(T, \mu) = \sum_i p_i^{\text{ideal}}$

Only control parameter (T, μ) ;
Parameter free (fixed by experiments)

Each particle's contribution is very small,
but in total, it becomes big

$$p_i^{\text{ideal}} = \pm \frac{T}{8\pi^2} \int dk_r^2 \int dk_z (2S_i + 1) \\ \times \log \left\{ 1 \pm \exp \left[-\frac{E_{k,i} - \mu_i}{T} \right] \right\}$$

i : particle specie (e.g., π , K , p , n , ...); $E_{k,i} = \sqrt{k^2 + m_i^2}$

Rotating reference frame

General coordinate transformation:

\bar{x}^μ : non-rotating \rightarrow x^μ : rotating

$$\begin{aligned} \bar{x} &\rightarrow x = +\bar{x} \cos \omega t + \bar{y} \sin \omega t \\ \bar{y} &\rightarrow y = -\bar{x} \sin \omega t + \bar{y} \cos \omega t \end{aligned}$$

$$g_{\mu\nu} = \eta_{ab} \frac{\partial \bar{x}^a}{\partial x^\mu} \frac{\partial \bar{x}^b}{\partial x^\nu} = \begin{pmatrix} 1 - (x^2 + y^2)\omega^2 & y\omega & -x\omega & 0 \\ y\omega & -1 & 0 & 0 \\ -x\omega & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

Energy spectrum: $\varepsilon \rightarrow \varepsilon - (\ell + s)\omega$

($s = -S, -S + 1, \dots, S - 1, S$ for spin- S particles)

Rotating hadron resonance gas model

$$p(T, \mu, \omega) = \sum_i p_i^{\text{rot}}$$
$$p_i^{\text{rot}} = \pm \frac{T}{8\pi^2} \int dk_r^2 \int dk_z \sum_{\ell=-\infty}^{\infty} \sum_{\nu=\ell}^{\ell+2S_i} J_\nu^2(k_r r) \times \log \left\{ 1 \pm \exp \left[-\frac{E_{k,i} - (\ell + S_i)\omega - \mu_i}{T} \right] \right\}$$

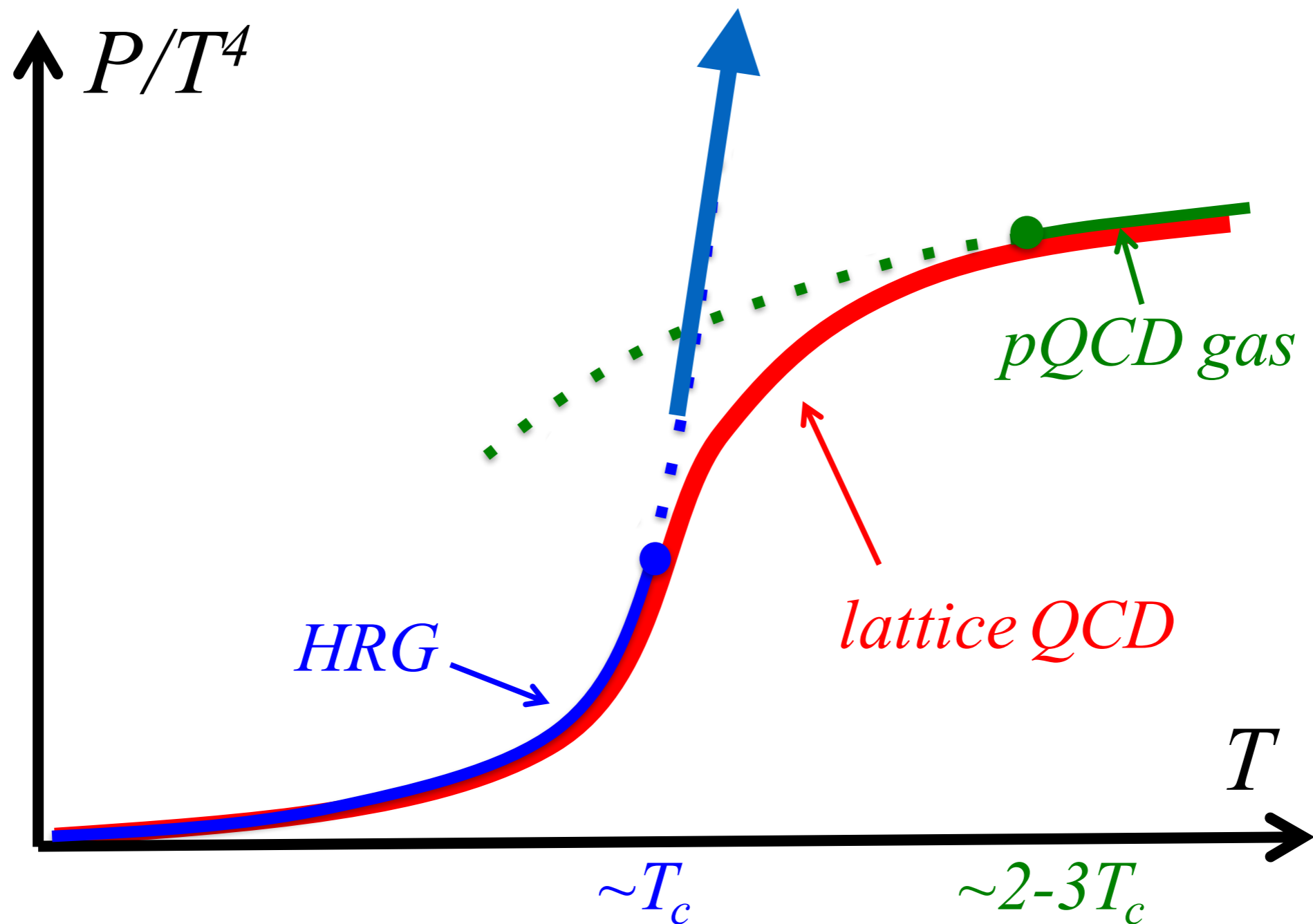
Compare with non rotating expression:

$$p_i^{\text{ideal}} = \pm \frac{T}{8\pi^2} \int dk_r^2 \int dk_z (2S_i + 1) \times \log \left\{ 1 \pm \exp \left[-\frac{E_{k,i} - \mu_i}{T} \right] \right\}$$

**HRG model is purely hadronic model,
but how can it capture the deconfinement of quarks?**

Deconfinement in hadron resonance gas

HRG blow up \rightarrow Signal for deconfinement



Taken from: Baym, Hatsuda, Kojo, Powell, Song, Takatsuka (2017)

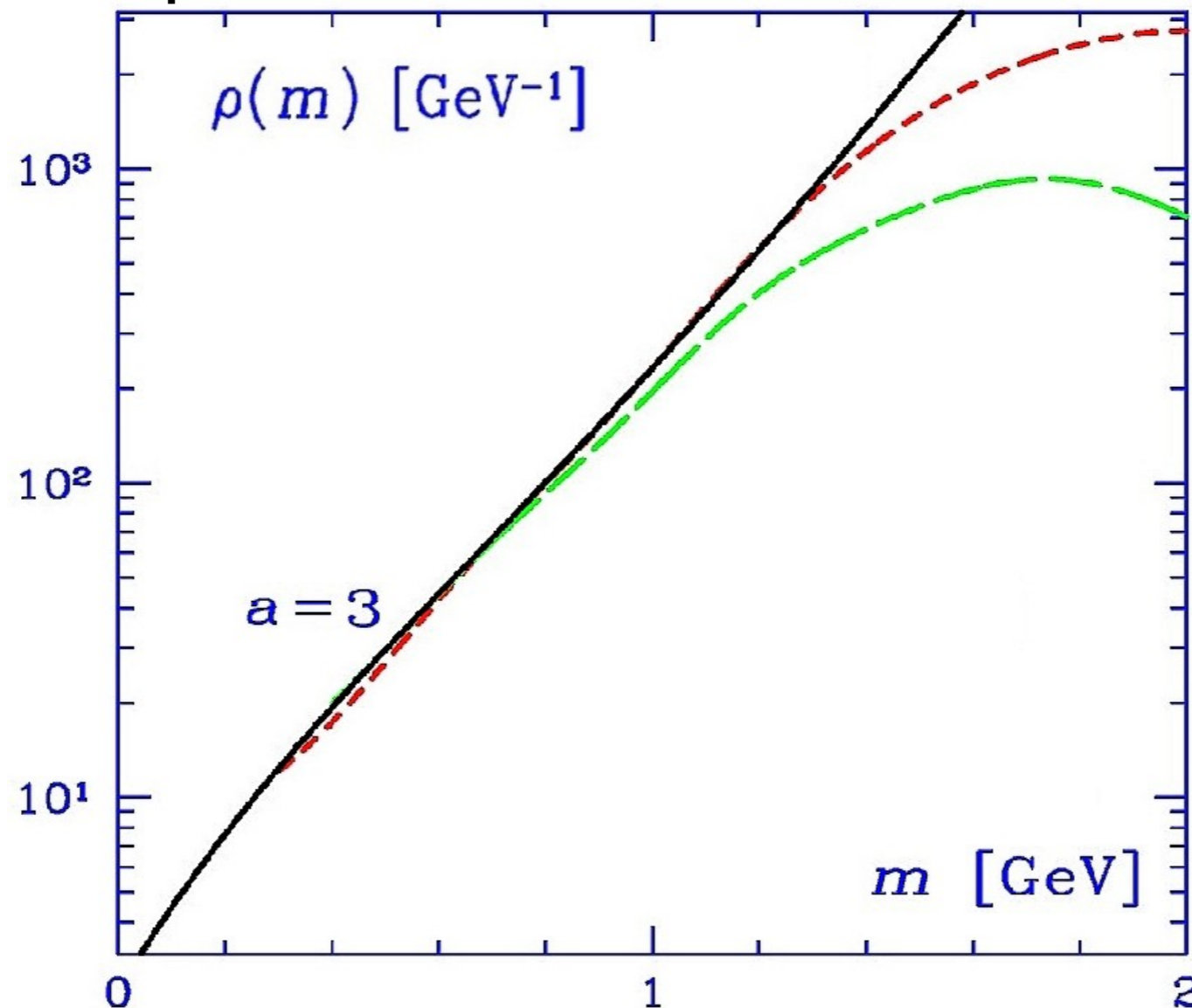
Deconfinement in hadron resonance gas

$$Z = N \int dm \rho(m) e^{-m/T}, \quad \rho(m) \propto e^{m/T_H}$$

Hagedorn (1965)

T_H : Hagedorn's limiting temperature

hadron mass spectrum:



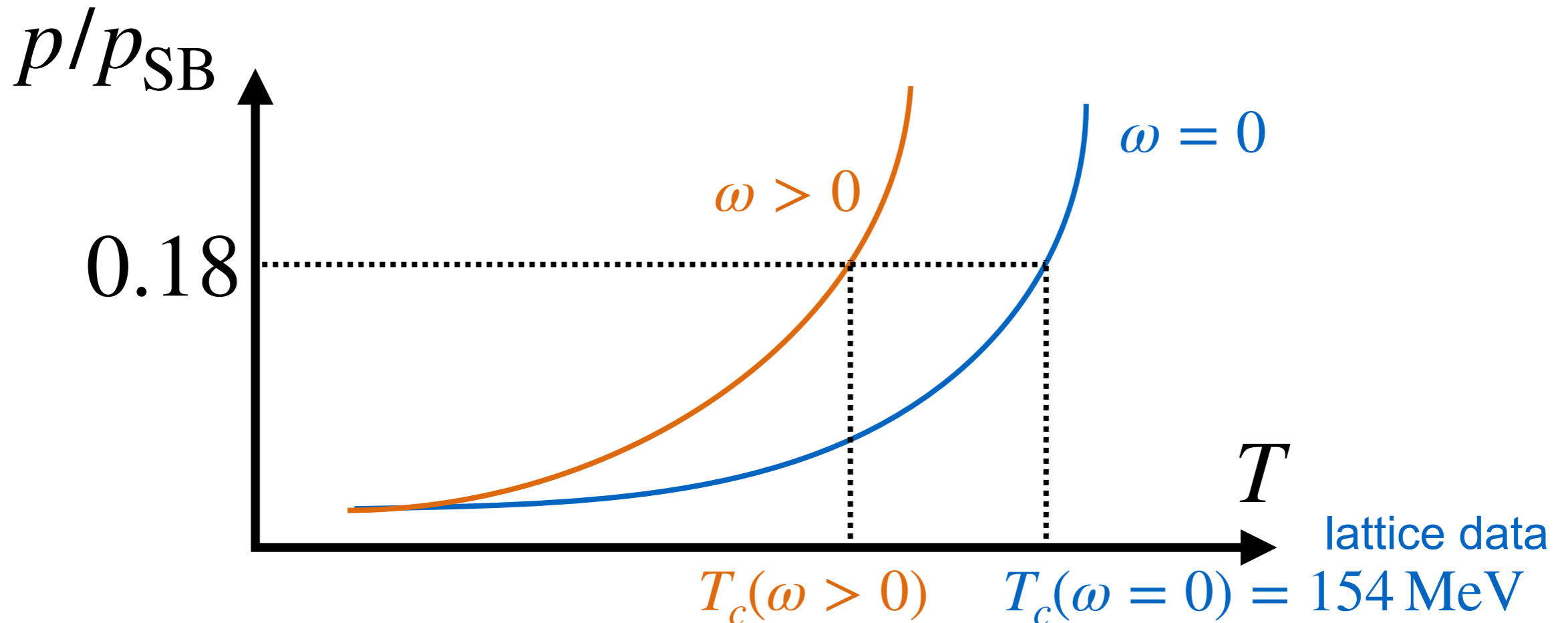
Taken from Rafelski (2016)

Our criterion of deconfinement

For each given (μ, ω) , we identify T that satisfies the following condition as T_c :

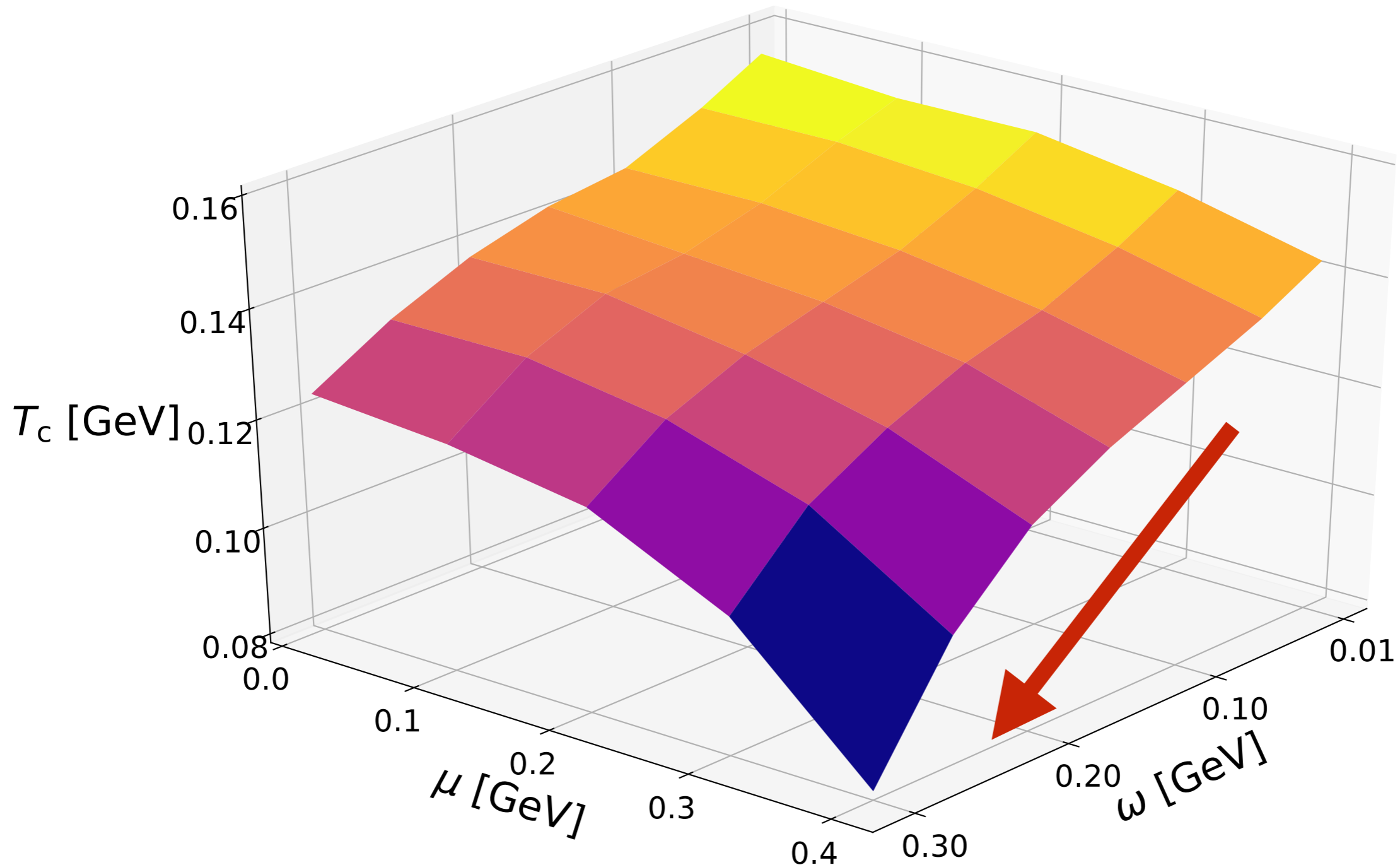
$$\frac{p}{p_{\text{SB}}}(T = T_c, \mu, \omega) = 0.18$$

$$p_{\text{SB}} \equiv (N_c^2 - 1)p_{\text{gluon}} + N_c N_f (p_{\text{quark}} + p_{\text{antiquark}})$$



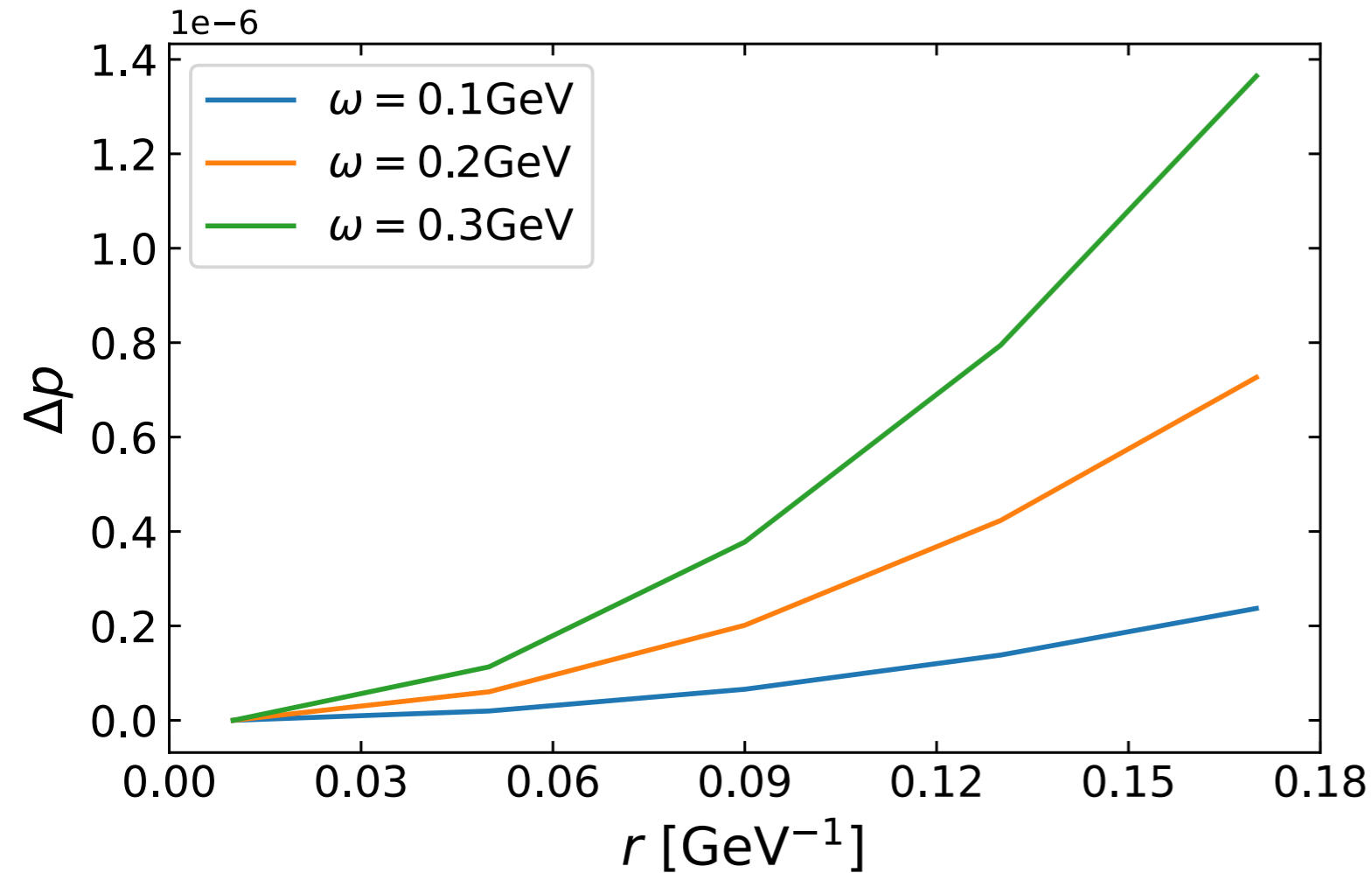
Deconfining boundary

Fujimoto, Fukushima, Hidaka (2021)

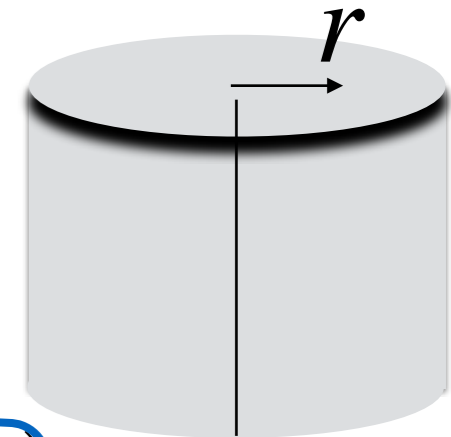


Deconfinement temperature T_c **drops**
with increasing ω

Discussion: radial dependence



$$\langle j \rangle(r) = \frac{\partial p(r)}{\partial \omega}$$



$$\langle j \rangle(r) dV \simeq dI(r)\omega$$

moment of inertia $\propto r^2$

$$p(r) = p(0) + \Delta p(r)$$

$$\Delta p(r) \simeq \frac{\sigma}{2} T^4 r^2 \omega^2$$

$$p_i^{\text{rot}} = \pm \frac{T}{8\pi^2} \int dk_r^2 \int dk_z \sum_{\ell=-\infty}^{\infty} \sum_{\nu=\ell}^{\ell+2S_i} J_\nu^2(k_r r) \times \log \left\{ 1 \pm \exp \left[-\frac{E_{k,i} - (\ell + S_i)\omega - \mu_i}{T} \right] \right\}$$

r -dependence originates here

Summary

- Estimated the rotation effect on the deconfinement transition in QCD:
the critical temperature T_c **drops** with increasing rotation
- We used the **Hadron Resonance Gas model**: a phenomenological and parameter-free approach
- Still there is a tension between our and the lattice result; the lattice result only includes gluon. We are looking for the thermodynamics at finite rotation on lattice.
- Radial dependent pressure may be interesting to see in the future analysis.