

# Fiber Accelerator: $TVm^{-1}$ Crunch-in Wakefields (Nanometric Wakefield Accelerator)

Aakash Sahai

**Collaborators:** Toshiki Tajima, Vladimir Shiltsev, Peter Taborek, Gerard Mourou



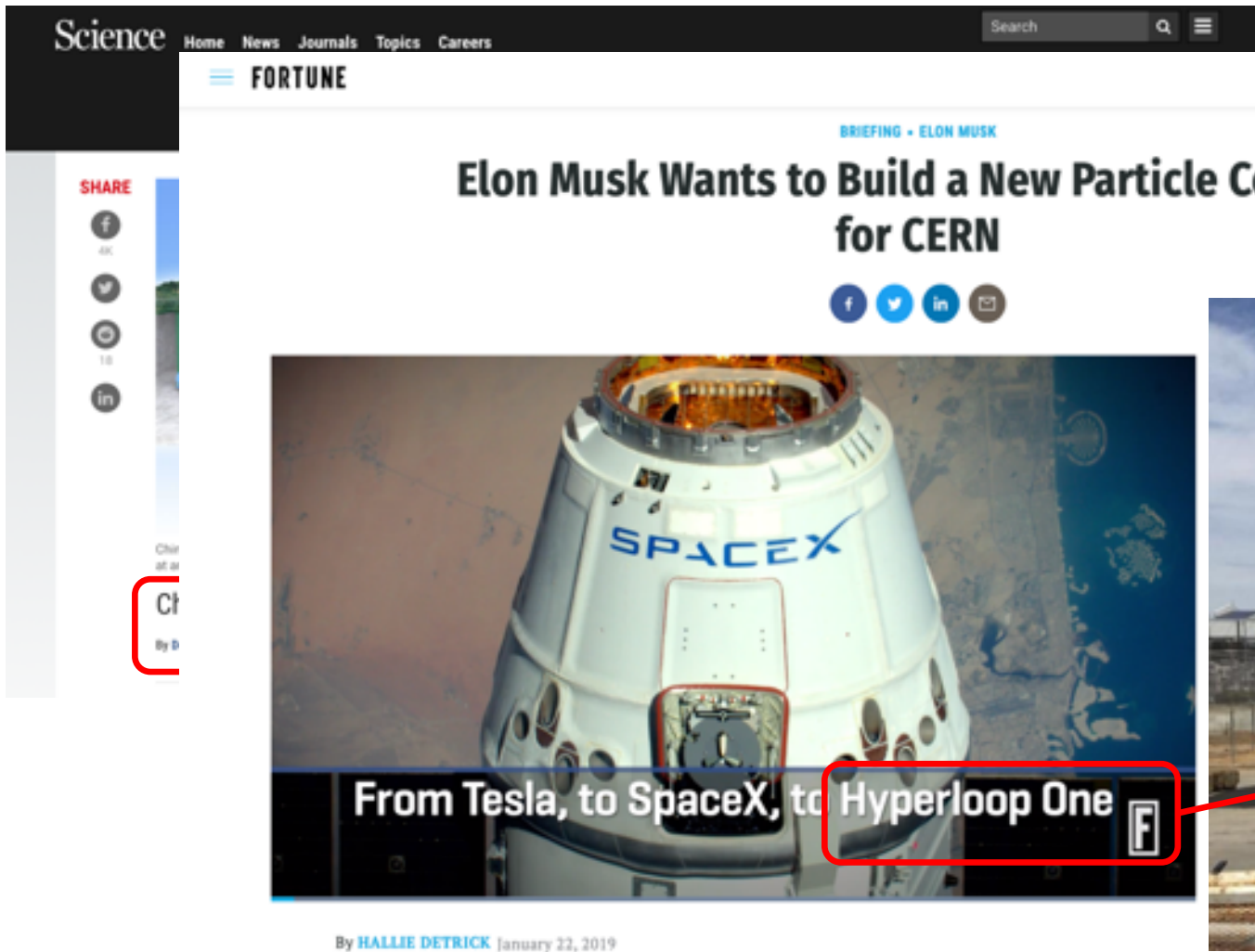
University of Colorado  
Denver



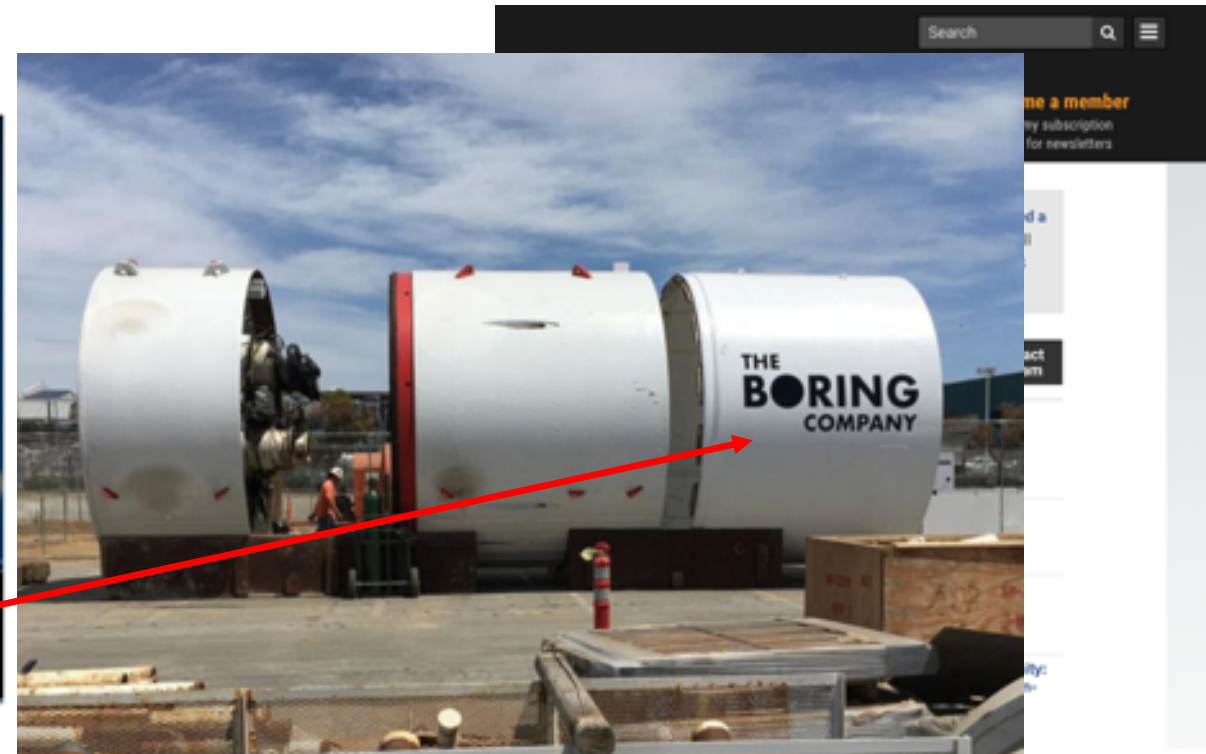
## Outline

- Background & Motivation
- Nanometric “crunch-in” surface wave model
- 3D computational proof-of-principle - GeV in mm
- Nanometric beam envelope oscillations –  $O(100\text{MeV})$  photons
- Conclusion & Future work

# current RF Acc. workhorse of HEP



22 Billion €



# CPA laser electron accelerator

Giant strides in Laser Wake-Field Acceleration (LWFA) of electron beams

VOLUME 43, NUMBER 4

PHYSICAL REVIEW LETTERS

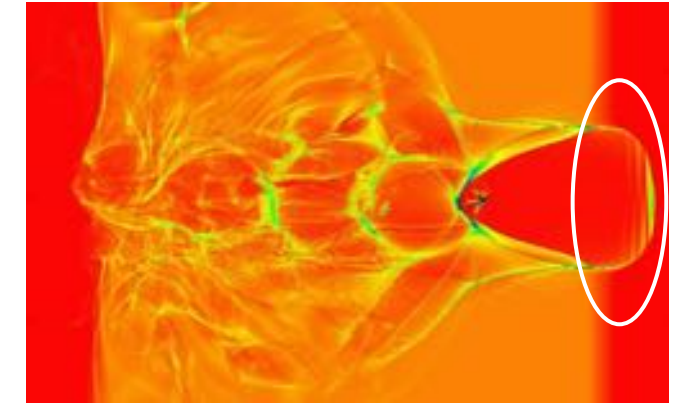
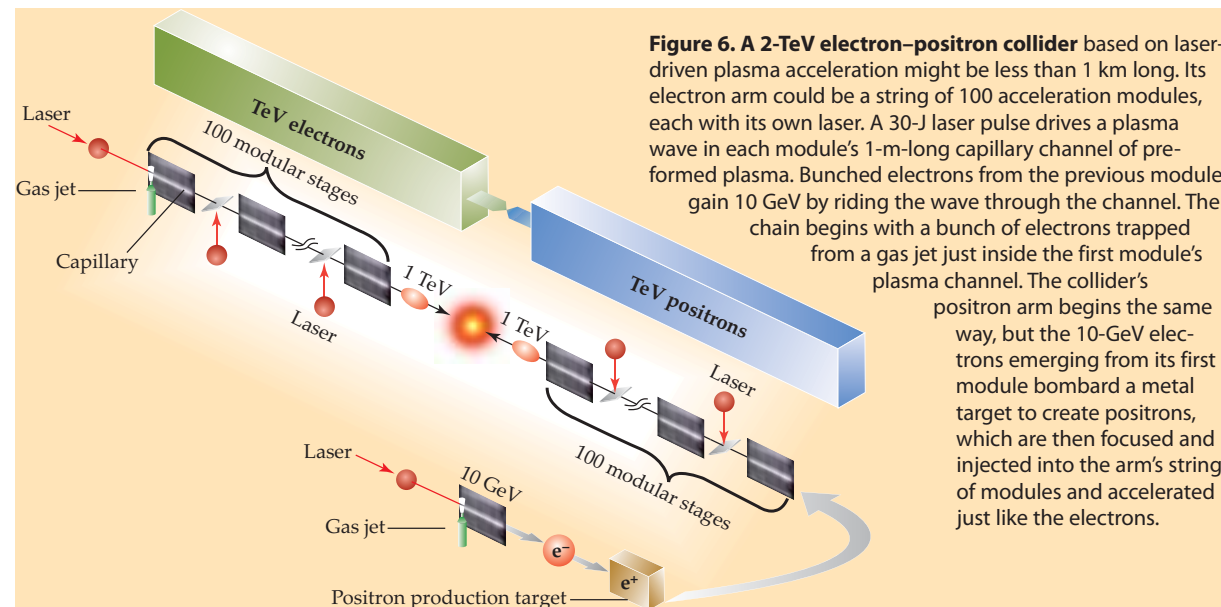
23 JULY 1979

1979

## Laser Electron Accelerator

T. Tajima and J. M. Dawson

Department of Physics, University of California, Los Angeles, California 90024



electron density of strongly nonlinear LWFA

Laser-Plasma Collider effort

## Laser-driven plasma-wave electron accelerators

Wim Leemans and Eric Esarey

Citation: *Phys. Today* **62**(3), 44 (2009); doi: 10.1063/1.3099645

View online: <http://dx.doi.org/10.1063/1.3099645>



# Nanostructures electron dynamics

# Proposed Solid-state plasma

## Gaseous Plasma

electron density,  $n_0 < 10^{21} \text{ cm}^{-3}$   
(ionization required)

**No Breakdown**

Density - easier to control

Structure – quite difficult

## Nanostructured “plasma”

$n_0 > 10^{21} \text{ cm}^{-3}$

**now** nanofabrication allows  
**tunable** properties  
nanostructured solids (*few atom layers*)

CB Fermi  $e^-$  gas: plasmon, surface  
plasmon, SP-polariton etc.

free  $e^-$ : nonlinear & relativistic  
collective oscillations

## Time & Spatial scales

$$\omega_{pe}^{-1} = [4\pi n_0 e^2 m_e^{-1}]^{-1/2}$$

$$\lambda_{pe} = 2\pi c \omega_{pe}^{-1}$$

### Gaseous Plasma

time scale :

$$17.7(n_0[10^{18}\text{cm}^{-3}])^{-1/2} \text{ femtoseconds}$$

spatial scale :

$$33.3(n_0[10^{18}\text{cm}^{-3}])^{-1/2} \mu\text{m}$$

CPA laser & phase-space gym  
made possible wakefield excitation

### Solid-state Plasma

time scale :

$$177(n_0[10^{22}\text{cm}^{-3}])^{-1/2} \text{ attoseconds}$$

spatial scale :

$$333(n_0[10^{22}\text{cm}^{-3}])^{-1/2} \text{ nm}$$

now experimentally realizable

# Energy density

Tajima-Dawson limit  
(or) Wavebreaking limit

$$E_{wb} = \frac{m_e c \omega_{pe}}{e}$$

Energy density of  
collective oscillations

$$\tilde{\mathcal{E}} = \frac{E_{wb}^2}{8\pi}$$

ultrashort laser pulse

$$\left. \begin{array}{l} \text{energy density of} \\ \text{ultrashort } (\sigma_r, \sigma_z \sim \lambda_{pe}) \\ \text{laser pulse} \end{array} \right\} \tilde{\mathcal{E}} = \frac{I}{2c}$$

$$\tilde{\mathcal{E}} = \frac{N_p E_p}{(2\pi)^{3/2} (2\pi c / \omega_{pe})^3}$$

relativistic particle beam

$$\left. \begin{array}{l} \text{field of ultrashort} \\ (\sigma_r, \sigma_z \sim \lambda_{pe}) \\ \text{particle bunch} \end{array} \right\} E_{\text{beam}} = \frac{e N_b}{2\pi (2\pi c / \omega_{pe})^2}$$

$$\left. \begin{array}{l} \text{energy density of} \\ \text{particle bunch} \end{array} \right\} \tilde{\mathcal{E}} = \frac{E_{\text{beam}}^2}{8\pi}$$

# minimum particle number

## Gaseous Plasma

$$E_{wb} \simeq 96(n_0[10^{18}\text{cm}^{-3}])^{1/2} \text{ GVm}^{-1}$$

## Solid-state Plasma

$$E_{wb} \simeq 9.6(n_0[10^{22}\text{cm}^{-3}])^{1/2} \text{ TVm}^{-1}$$

need relativistic momentum of oscillation

Energy density considerations:

10 Joule class optical lasers ( $a_0 > 1$ )

~ nC charge in 30  $\mu\text{m}$  beam

Energy density considerations:

mJ class keV x-ray lasers ( $a_0 > 1$ )

~ 100pC charge in ~100 nm beam

need relativistic intensity drive bunch

CPA laser & phase-space gym  
made possible wave-breaking fields

now experimentally realizable

RC

Relativistic  
Compression

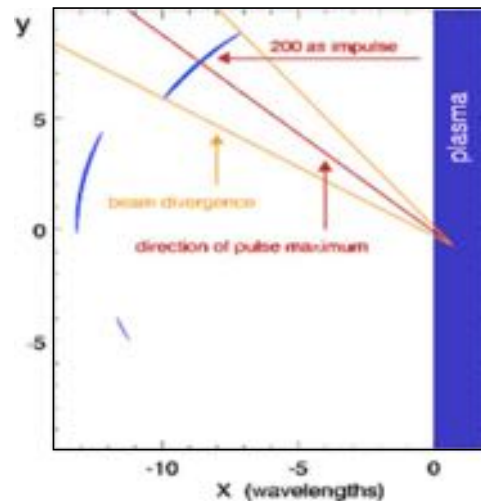
TFC

Thin-film  
Compression

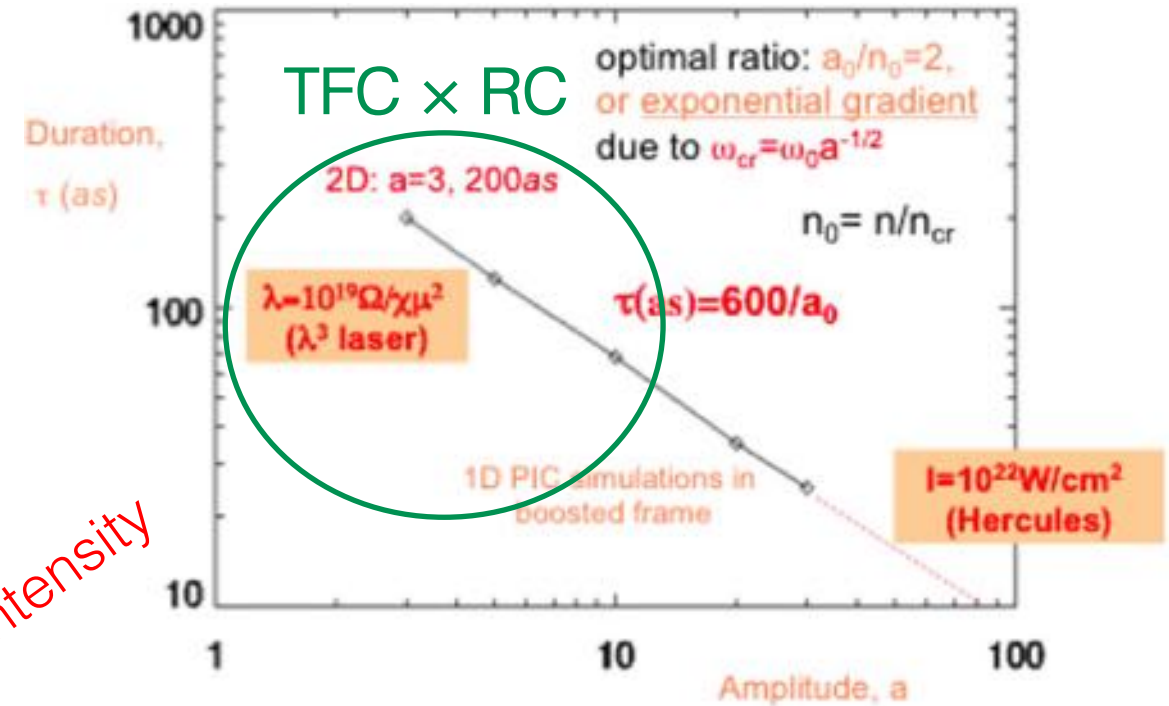
# Mourou's attosecond x-ray laser



**Fig. 5a.** Interaction of few cycle pulse in the relativistic  $\gamma$  regime. It shows the shaped mirror created by the enormous light pressure. In this time scale only the electrons have the time to move. The ions are too slow to follow.



**Fig. 5b.** The reflection of an ultra relativistic pulse by a high Z target will broadcast the beam in specific way. The pulse is compressed by a factor proportional to  $a_0$ . The pulses will be easily isolated.



Relativistic Intensity  
x-ray laser

Eur. Phys. J. Special Topics **223**, 1181–1188 (2014)  
© EDP Sciences, Springer-Verlag 2014  
DOI: [10.1140/epjst/e2014-02171-5](https://doi.org/10.1140/epjst/e2014-02171-5)

THE EUROPEAN  
PHYSICAL JOURNAL  
SPECIAL TOPICS

Naumova, N. M., Nees, J. A., Sokolov, I. V., Hou, B., Mourou, G. A., *Relativistic Generation of Isolated Attosecond Pulses in a  $\lambda^3$  Focal Volume*, *Phys. Rev. Lett.* **92**, 063902 (2004)



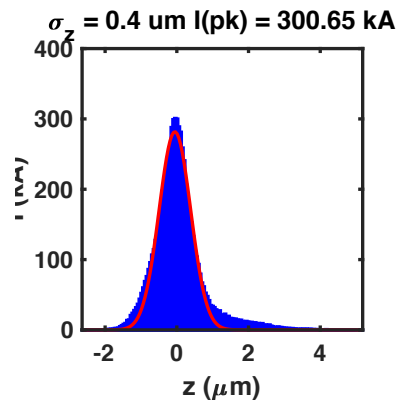
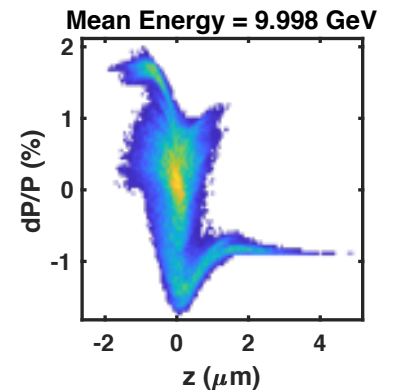
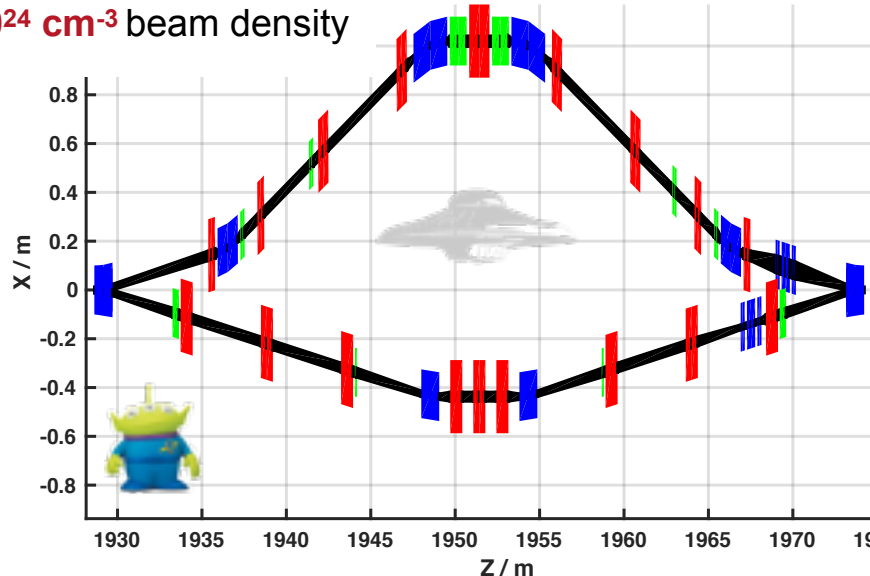
# Submicron near solid e<sup>-</sup> bunch

Phase-space gymnastics – 100nm compression - bunch length

## FACET-II Beam will Access New Regimes

Low-emittance (state of the art photoinjector) and ultra-short (improved compression) beam will generate:

- >300 kA peak current (~0.4  $\mu\text{m}$  long)
- ~100 nm focus by plasma ion column
- ~ $10^{12}$  V/cm radial electric field ( $E_s = 1.3 \times 10^{16}$  V/cm)
- ~ $10^{24}$  cm<sup>-3</sup> beam density



Parameter	[Unit]	NPQED Collider	FACET-II	ILC	CLIC
Beam energy	[GeV]	125	10	250	1500
Bunch charge	[nC]	0.14–1.4	1.2	3.2	0.6
Peak current	[kA]	1700	300	1.3	12.1
Energy spread (rms)	[%]	0.1	0.85	0.12	0.34
Bunch length (rms)	[ $\mu\text{m}$ ]	0.01–0.1	0.48	300	44
Bunch size (rms)	[ $\mu\text{m}$ ]	0.01	3	0.47	0.045
Pulse rate $\times$	[Hz] $\times$	100 $\times$	30 $\times$	5 $\times$	50 $\times$
Bunches/pulse	$N_{\text{bunch}}$	1	1	1312	312
Beamstrahlung	$\chi_{\text{av}}$	969		0.06	5
Parameter	$\chi_{\text{max}}$	1721		0.15	12
Disruption	$D_{x,y}$	0.001–0.1		0.3	0.15
Parameters		0.001–0.1		24.4	6.8
Peak electric field	[TV/m]	4500	3.2	0.2	2.7
Beam power	[MW]	0.002–0.02	$10^{-4}$	5	14
Luminosity	[cm <sup>-2</sup> s <sup>-1</sup> ]	$6 \times 10^{30}$ $-4 \times 10^{32}$		$10^{34}$	$10^{34}$

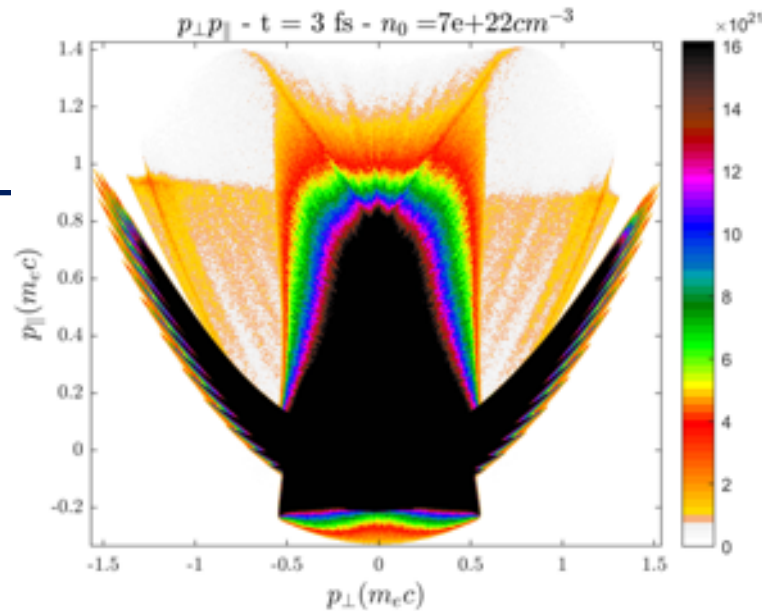
PHYSICAL REVIEW LETTERS **122**, 190404 (2019)

# relativistic solid density electron “plasma”

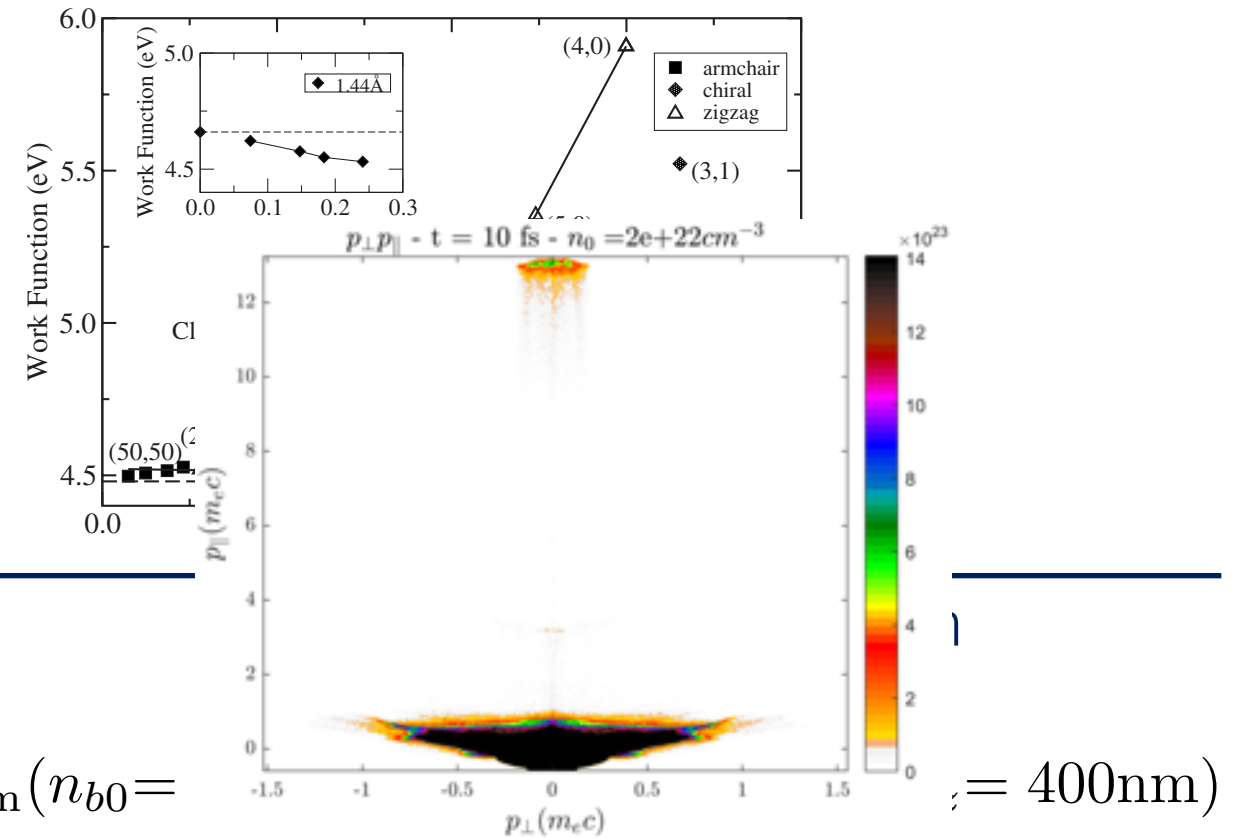
nanostructured tube

work function  $\sim 5\text{eV}$

PHYSICAL REVIEW B **76**, 235413 (2007)



$$\rightarrow a_0 \sim 3$$



$$E_{\text{beam}}(n_{b0} = \simeq 0.1 \text{ TV/m})$$

$$V_{\text{beam}}(\text{inter - atomic}) = E_{\text{beam}} \times 10 \text{ \AA} = 100 \text{ V}$$

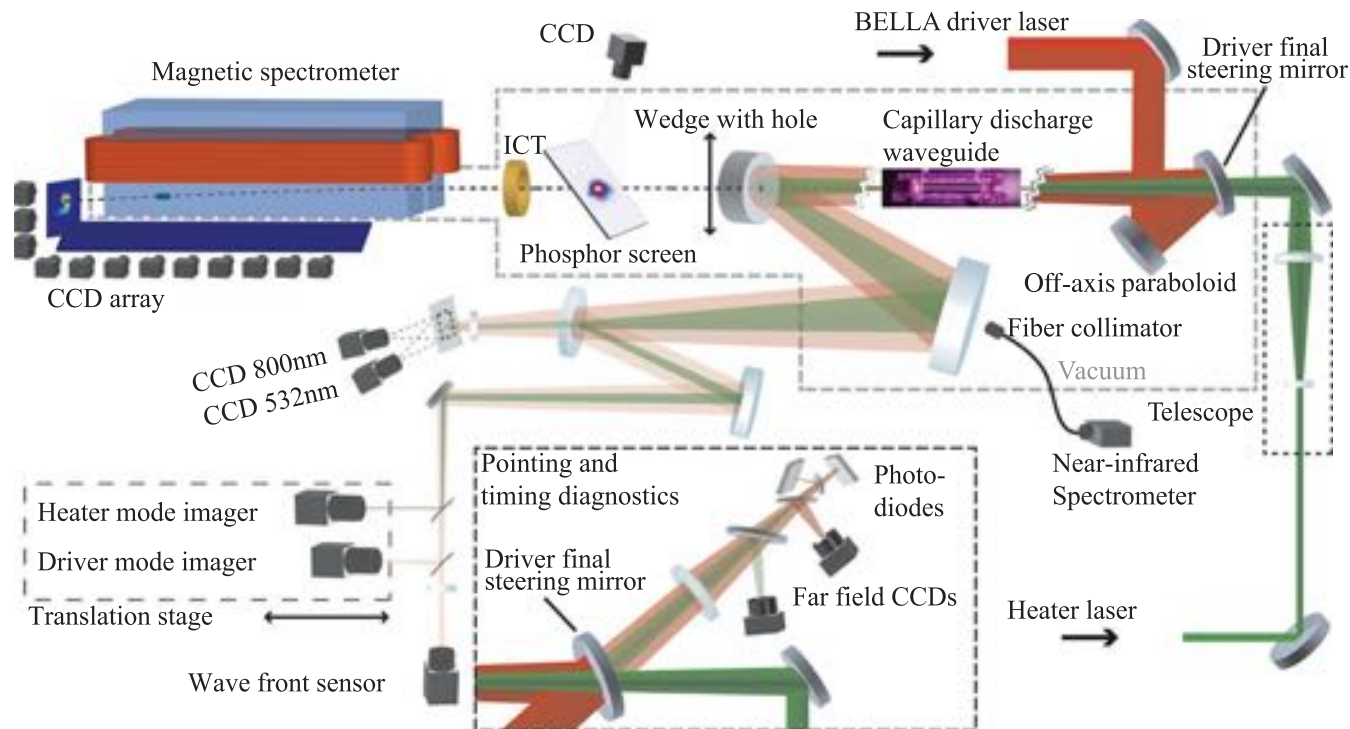
structured “plasma”

# hollow gaseous fiber accelerator

D. C., Kurki-Suonio, T., Tajima, T., *Laser Self-Trapping for the Plasma Fiber Accelerator*, *IEEE Transactions on Plasma Science*, **15**, iss.2, April 1987

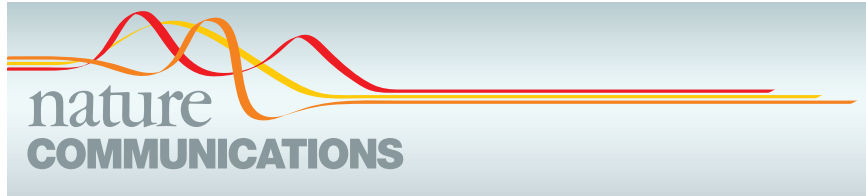
PHYSICAL REVIEW LETTERS **122**, 084801 (2019)

Petawatt Laser Guiding and Electron Beam Acceleration to 8 GeV in a Laser-Heated Capillary Discharge Waveguide



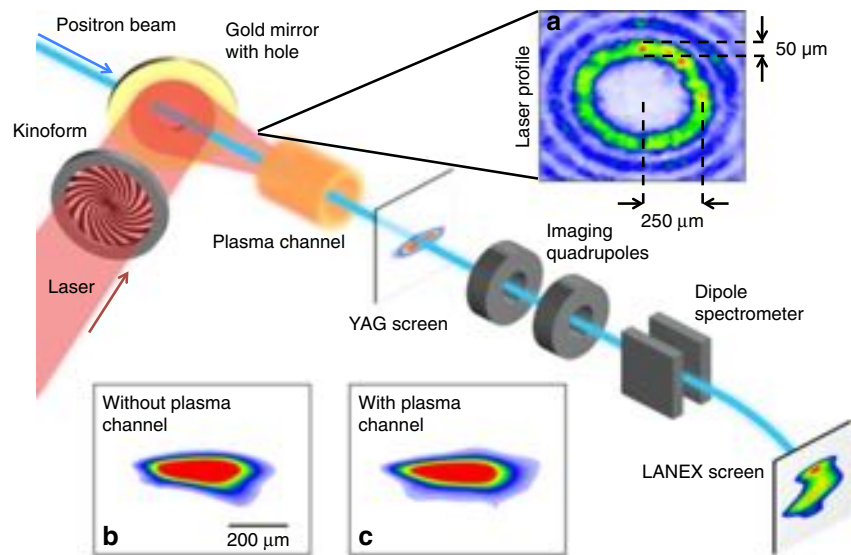
- hollow tube in gaseous plasma
- guide & self-focus high-intensity laser pulse
- difficult to create such channels
- But, higher energies need good quality channels

# beam-driven hollow channel plasma



## ARTICLE

Received 17 Nov 2015 | Accepted 27 Apr 2016 | Published 2 Jun 2016



un-ionized gas within the channel

## PURELY EM mode

$e^+$ -beam -driven

$$r_{ch} = 16 c/\omega_{pe}$$

$$n_b = 1.3 n_0$$

$$\sigma_z = 1.5 c/\omega_{pe}$$

$$\sigma_r = 0.3 c/\omega_{pe}$$

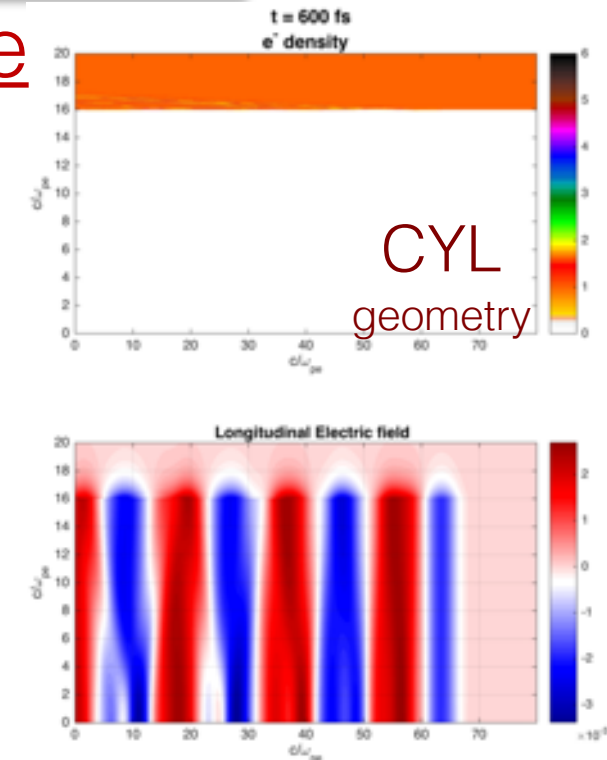
$$\gamma_b = 1000$$

**NO focusing forces**

currents in the wall

EM acc. fields leak into the channel

$$10^{-2} E_{WB}$$

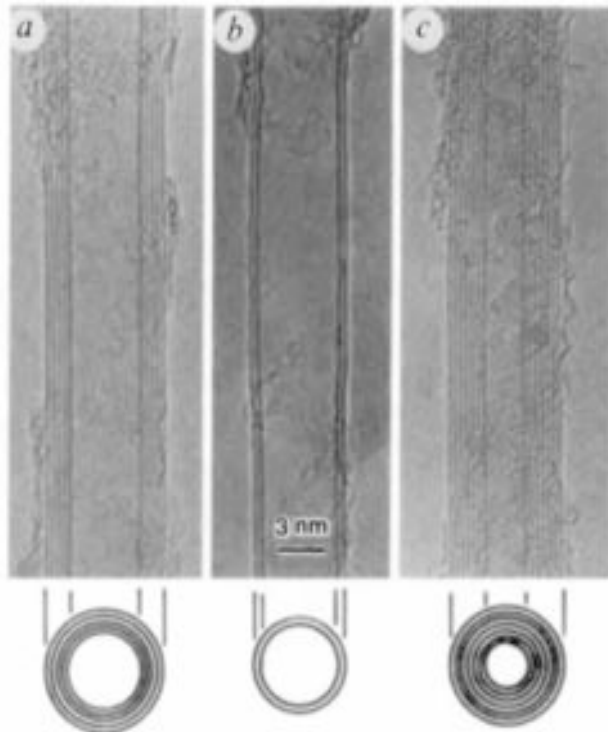


$$n_0 = 8 \times 10^{16} \text{ cm}^{-3}$$

obs. field = **220MV/m**

**WB field ~ 20 GV/m**

# nano-tubes – hollow crystal channels



LETTERS TO NATURE

## Helical microtubules of graphitic carbon

Sumio Iijima

NEC Corporation, Fundamental Research Laboratories,  
34 Miyukigaoka, Tsukuba, Ibaraki 305, Japan

NATURE · VOL 354 · 7 NOVEMBER 1991

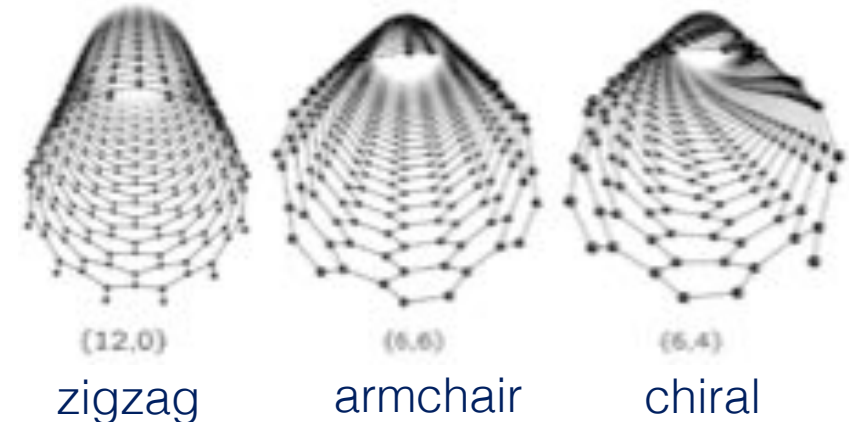
density  $\sim 10^{21} - 10^{22} \text{ cm}^{-3}$

FIG. 1 Electron micrographs of microtubules of graphitic carbon. Parallel dark lines correspond to the (002) lattice images of graphite. A cross-section of each tubule is illustrated. *a*, Tube consisting of five graphitic sheets, diameter 6.7 nm. *b*, Two-sheet tube, diameter 5.5 nm. *c*, Seven-sheet tube, diameter 6.5 nm, which has the smallest hollow diameter (2.2 nm).

$\lambda_{\text{mfp}} \simeq \mu m$  collision-less  $e^-$  over few ten fs

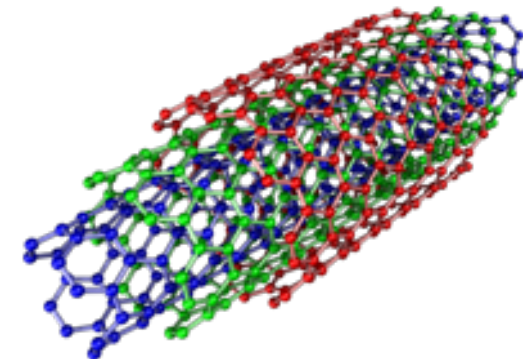
PRL 98, 186808 (2007)

single-walled nanotubes (SWNT)



SWNT diameter – 0.3nm to 4nm

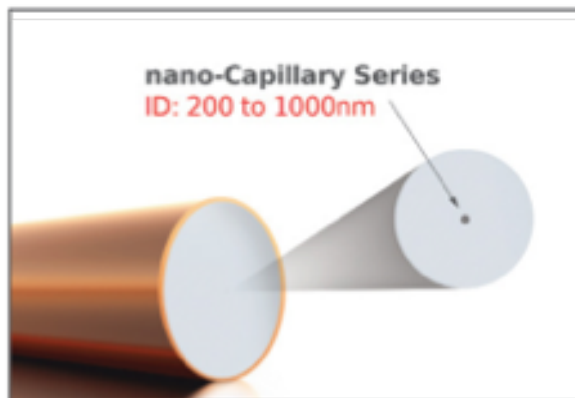
multi-walled nanotubes (MWNT)



MWNT diameter – 1.5nm to 100nm



# Commercial Silica Capillaries

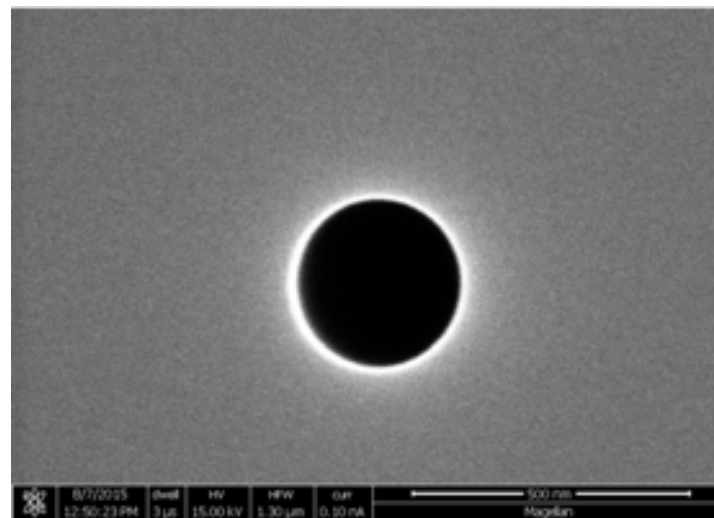


Polymicro nano-Capillary Tubing

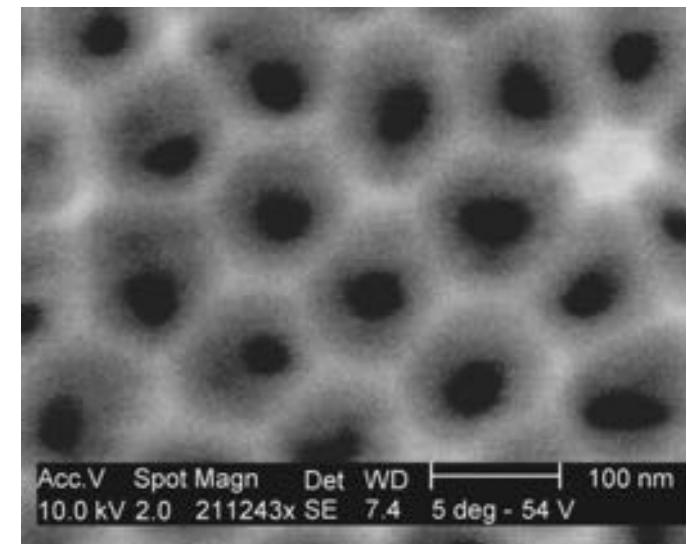
**Polymicro**  
**nano-Capillary**  
**Fused Silica Capillary Tubing**



Polymicro Fused Silica Capillary Diagram



*SEM characterization*  
courtesy: P. Taborek



Lazarowich, R. J., Taborek, P., Yoo, B. Y., Myung, N. V.,  
*Fabrication of porous alumina on quartz crystal micro-*  
*balances* *J. Appl. Phys.* **101**, 104909 (2007)

Materials Today • Volume 17, Number 5 • June 2014  
**A brief review of atomic layer deposition:  
from fundamentals to applications**

of three or more elements by ALD is very useful in optoelectronic materials such as photovoltaics as it enables a means to controllably vary properties as band gap, density, conductivity, energy band levels, and morphology. An example of this is the ALD-

# Nanostructured material wakefield model

## solid-state nanostructured tube wakefield

- Tunable density, structure, composition
- Collisions can be controlled
- guided and focused - x-ray laser and particle beam
- Nonlinear & Relativistic Surface Plasmon Polariton
- wave-breaking fields accessible

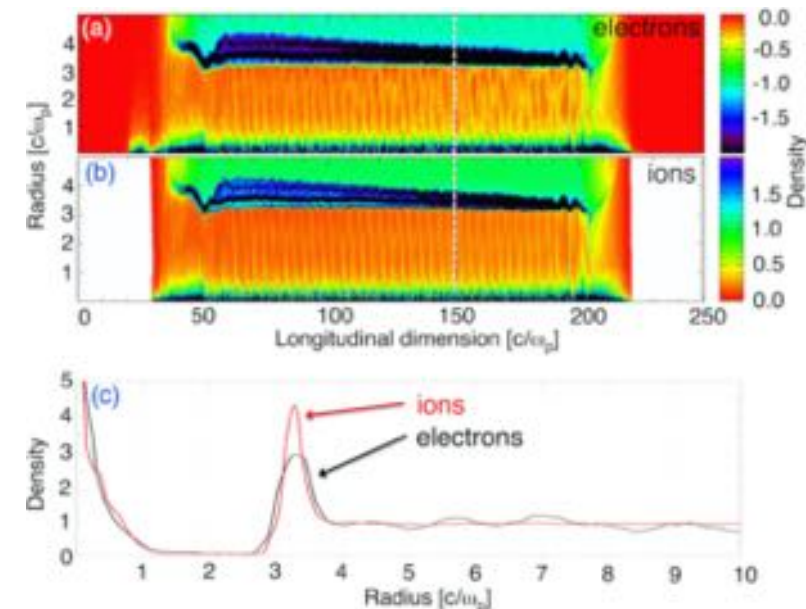
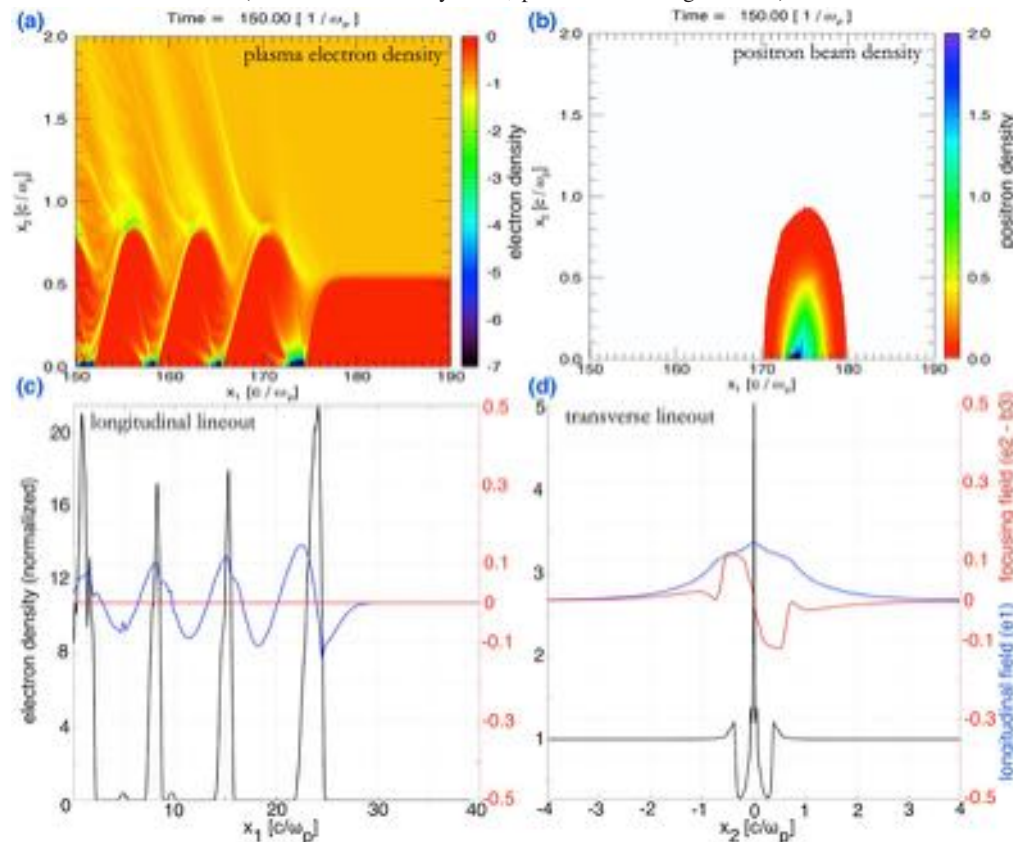
# beam-driven crunch-in surface mode

PHYSICAL REVIEW ACCELERATORS AND BEAMS **20**, 081004 (2017)

## Excitation of a nonlinear plasma ion wake by intense energy sources with applications to the crunch-in regime

Aakash A. Sahai\*

Department of Physics, Blackett Laboratory and John Adams Institute for Accelerator Sciences,  
Imperial College London, London, SW7 2AZ, United Kingdom,  
and Department of Electrical Engineering, Duke University, Durham, North Carolina 27708, USA  
(Received 5 February 2017; published 23 August 2017)



coherent radial oscillations  
e<sup>-</sup> collapse to the channel axis

Coherent acc. fields  $\sim 0.4 E_{WB}$

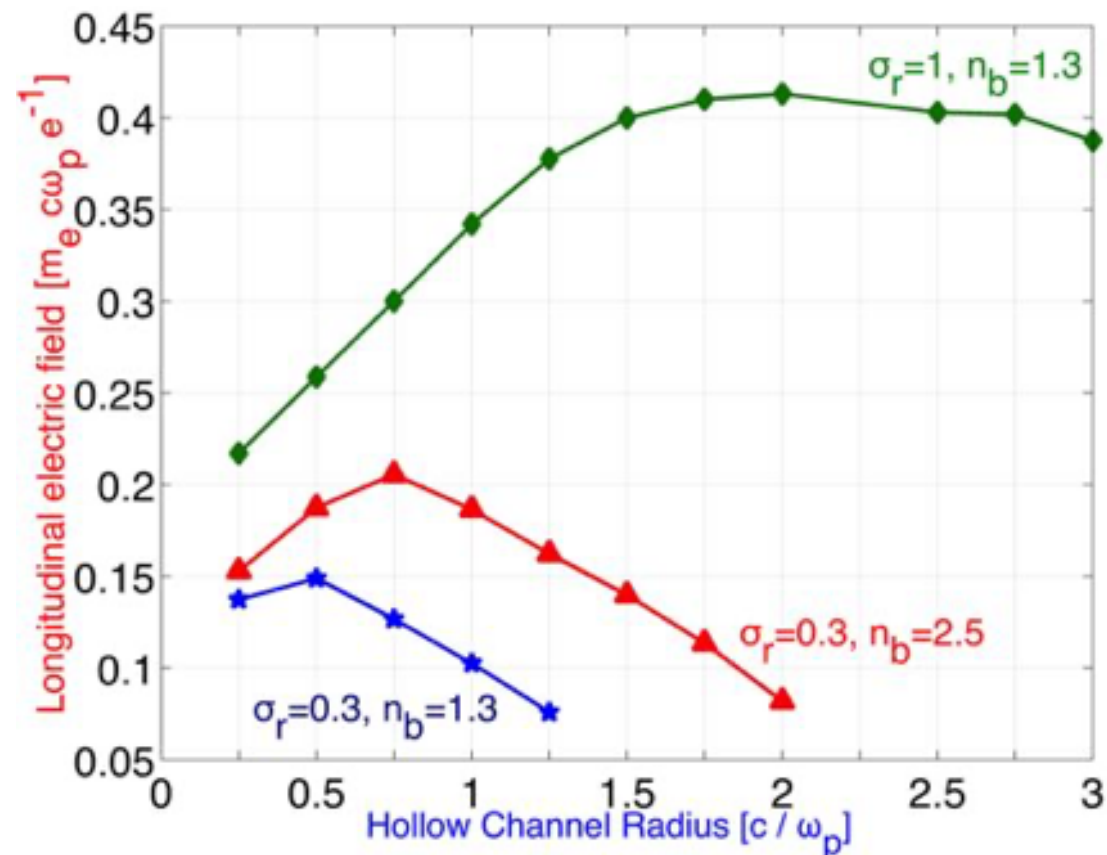
## Chapter 8

Sahai, A. A., *On Certain Non-linear and Relativistic Effects in Plasma-based Particle Acceleration*, Ph.D. dissertation submitted to the Duke university graduate school, July 2015

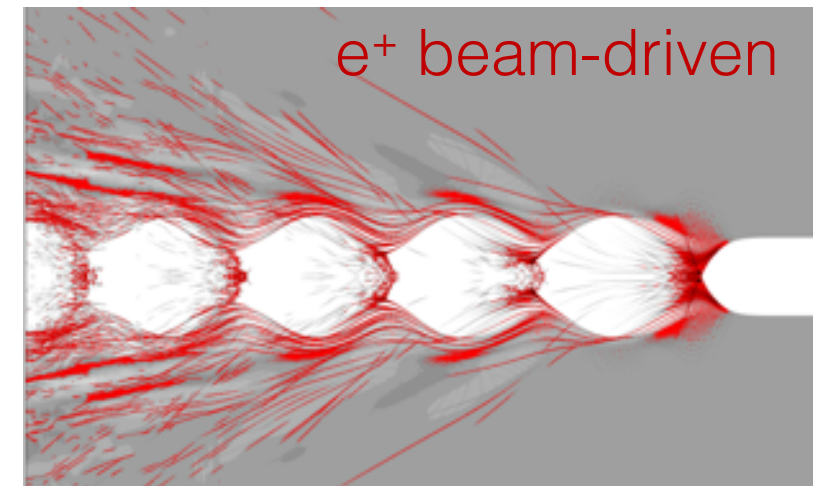
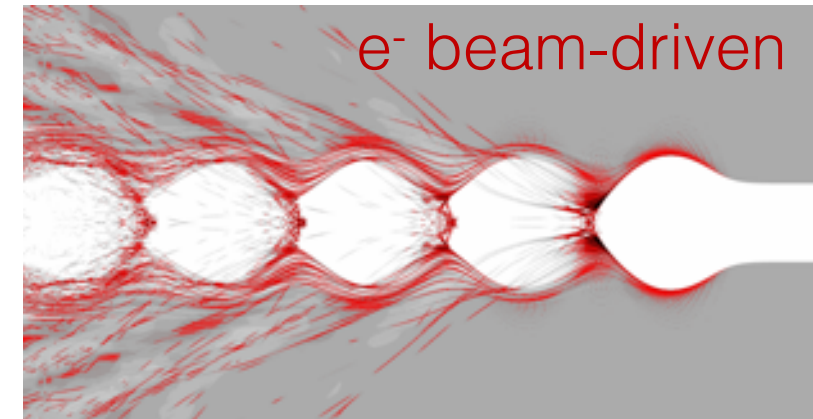
# beam-driven crunch-in surface mode

## Chapter 8

Sahai, A. A., *On Certain Non-linear and Relativistic Effects in Plasma-based Particle Acceleration*, Ph.D. dissertation submitted to the Duke university graduate school, July 2015



## cartesian CRUNCH-IN mode





# x-ray laser tube crunch-in mode

PHYSICAL REVIEW ACCELERATORS AND BEAMS **19**, 101004 (2016)

## Particle-in-cell simulation of x-ray wakefield acceleration and betatron radiation in nanotubes

Xiaomei Zhang,<sup>1,2</sup> Toshiki Tajima,<sup>2</sup> Deano Farinella,<sup>2</sup> Youngmin Shin,<sup>3</sup> Gerard Mourou,<sup>4</sup> Jonathan Wheeler,<sup>4</sup> Peter Taborek,<sup>2</sup> Pisin Chen,<sup>5</sup> Franklin Dollar,<sup>2</sup> and Baifei Shen<sup>1</sup>

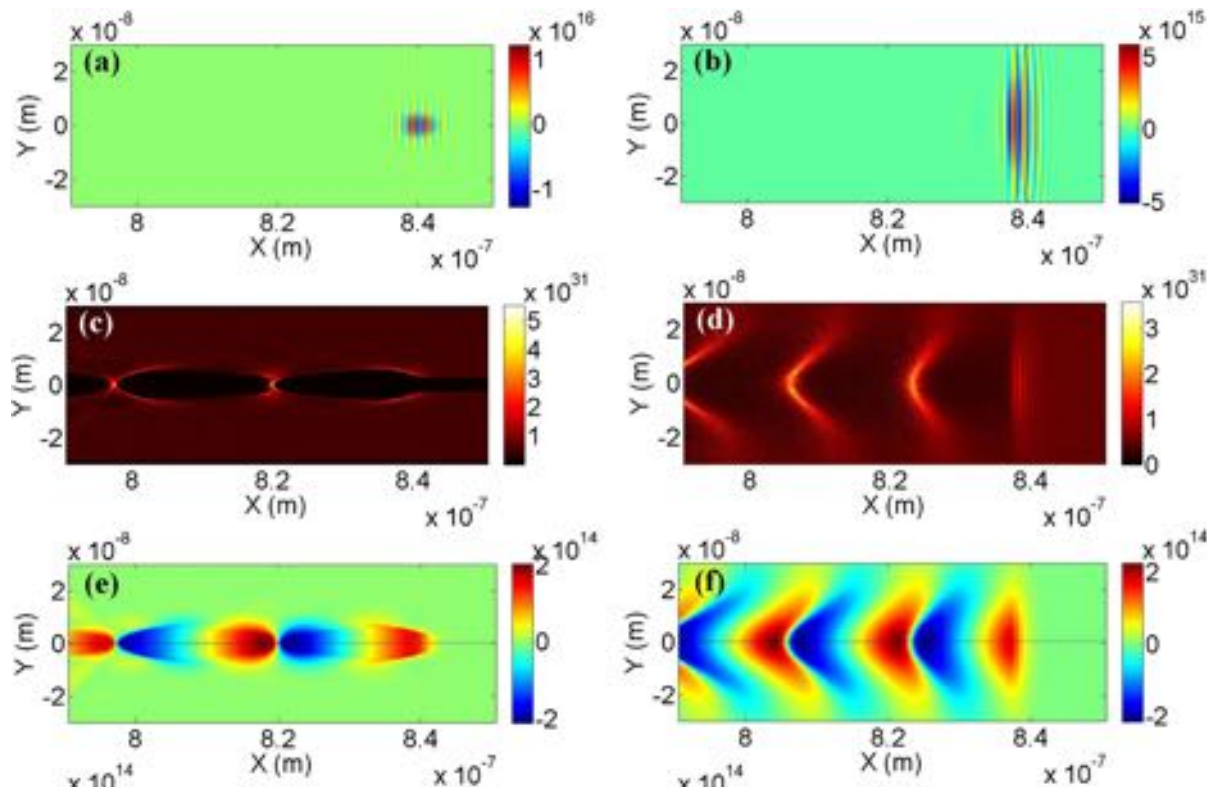
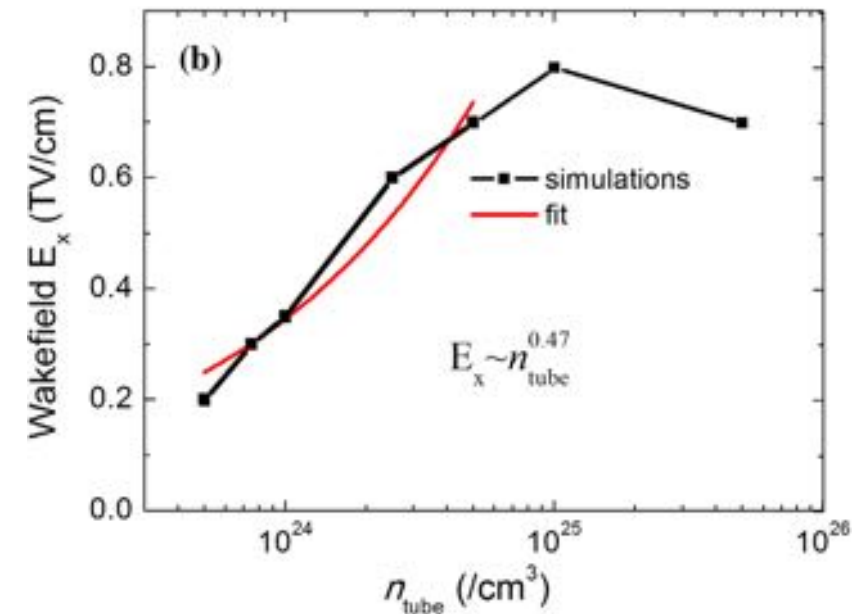


TABLE I. Summary of the laser and plasma parameters for our base case.

Laser wavelength $\lambda_L$	Peak amplitude $a_0$	Width radius $\sigma_L$	Length radius $\sigma_x$	Plasma density $n_{\text{tube}}$	Tube radius $\sigma_{\text{tube}}$
1 nm	4	5 nm	3 nm	$5 \times 10^{24}$ W/cm <sup>3</sup>	2.5 nm/0 nm
1 $\mu\text{m}$	4	5 $\mu\text{m}$	3 $\mu\text{m}$	$5 \times 10^{18}$ W/cm <sup>3</sup>	2.5 $\mu\text{m}$ /0 $\mu\text{m}$





# Nanometric wakefield model

# crunch-in kinetic theoretical model - IV

Tube wakefield  
peak radial field

$$E_{t-r}(\xi_{r-min}) 2\pi r_{min} dz = 4\pi \delta Q_{max}$$

$$E_{t-r}(\xi_{r-min}) = -\alpha n_t 2\pi r_t \left( \frac{en_{b0} 2\pi\sigma_r^2}{n_t\pi(r_t + \Delta w)^2 - n_{b0} 2\pi\sigma_r^2} \right)$$

Panofsky-Wenzel  
theorem

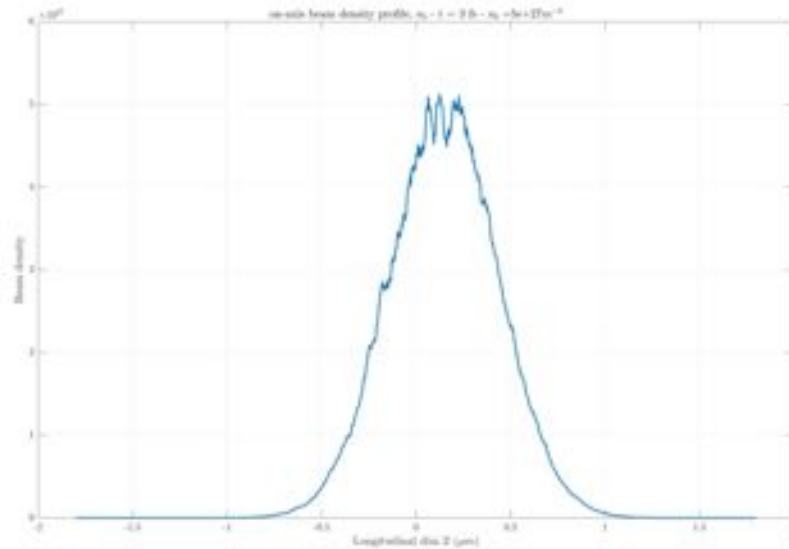
$$\frac{E_{t-r}}{\Delta\xi} = \frac{E_{t-z}}{\Delta r}$$

$$E_{t-z} = \frac{E_{t-r}}{\Delta\xi} \Delta r = E_{t-r} \frac{r_{min}}{\kappa 2\pi c} \frac{\omega_{pe}(n_t)}{\sqrt{\gamma_e}}$$

Tube wakefield  
peak acc. field

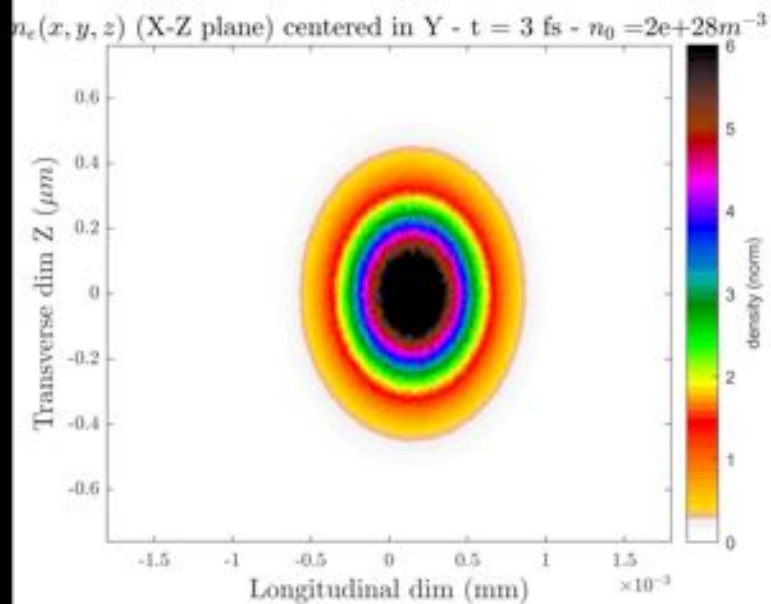
$$E_{t-z} = -\frac{2.03}{\kappa} \frac{\sqrt{n_t[10^{22}\text{cm}^{-3}]}}{\sqrt{r_t[100\text{nm}]}} \sqrt{Q_b[\text{pC}]} \frac{\sigma_r}{\sigma_z} \left( \left( \frac{r_t + \Delta w}{r_t} \right)^2 - 2 \frac{n_{b0}}{n_t} \frac{\sigma_r^2}{r_t^2} \right)^{-1} \frac{\text{TV}}{\text{m}}$$

# 3D Particle-In-Cell modeling



3D PIC simulation  
on-axis beam density profile

initialized Gaussian



2D slice density profile

# Conclusion & Future Work

## Nanometric Wakefield Acceleration

- Ready to be prototyped:  
1 GeV in  $\sim 100 \mu\text{m}$
- Several **related details** being characterized:  
attosecond ionization, ion motion, etc.
- Extend the **module** to higher energies
- Self-focusing & nano-modulation  
of ultra-relativistic beam
- controlled  $O(100\text{MeV})$  photon production

Towards

**TeV on a Chip !**

**Gamma-ray**

**FEL on a Chip !!**