

Inflaton Dark Matter

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This talk is based on:

O. Lebedev and J.-H. Yoon, "Challenges for Inflaton Dark Matter", 2105.05860



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Bergen, Norway, 29 Nov

Introduction

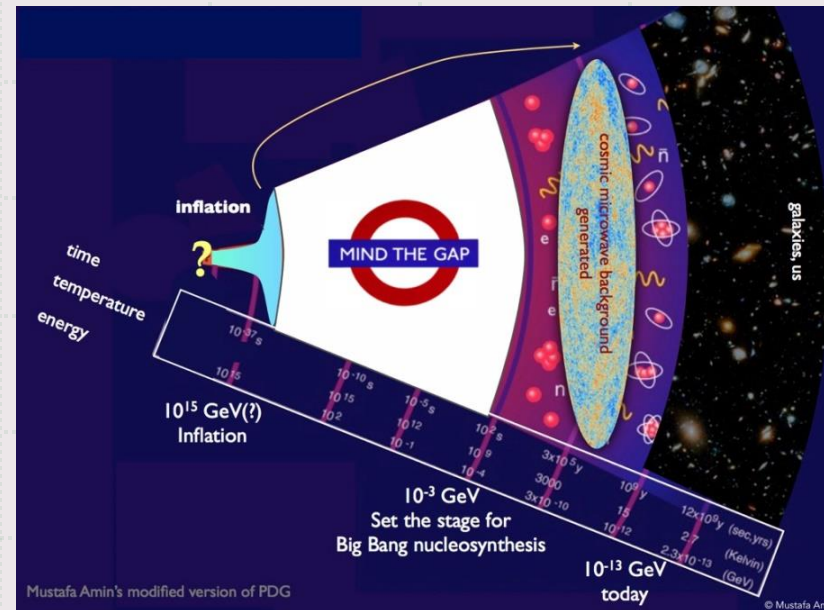
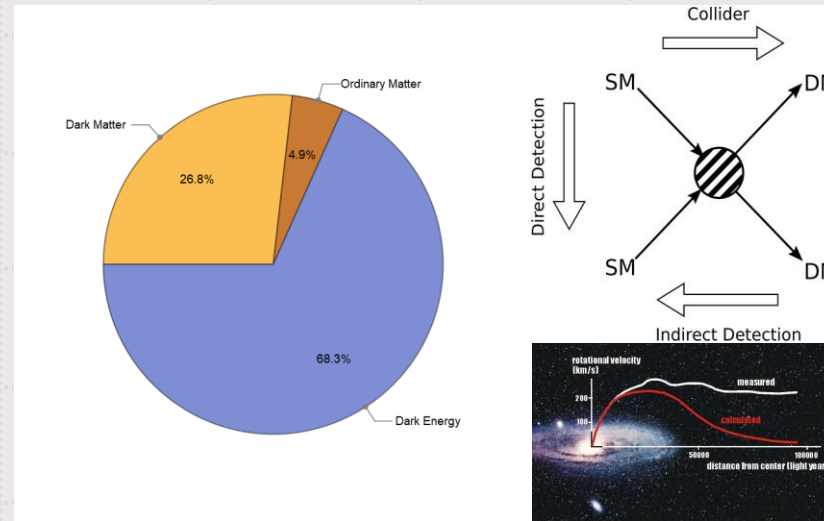
Dark Matter (Zwicky, 1933)

Cosmic Inflation (Guth, 1979)

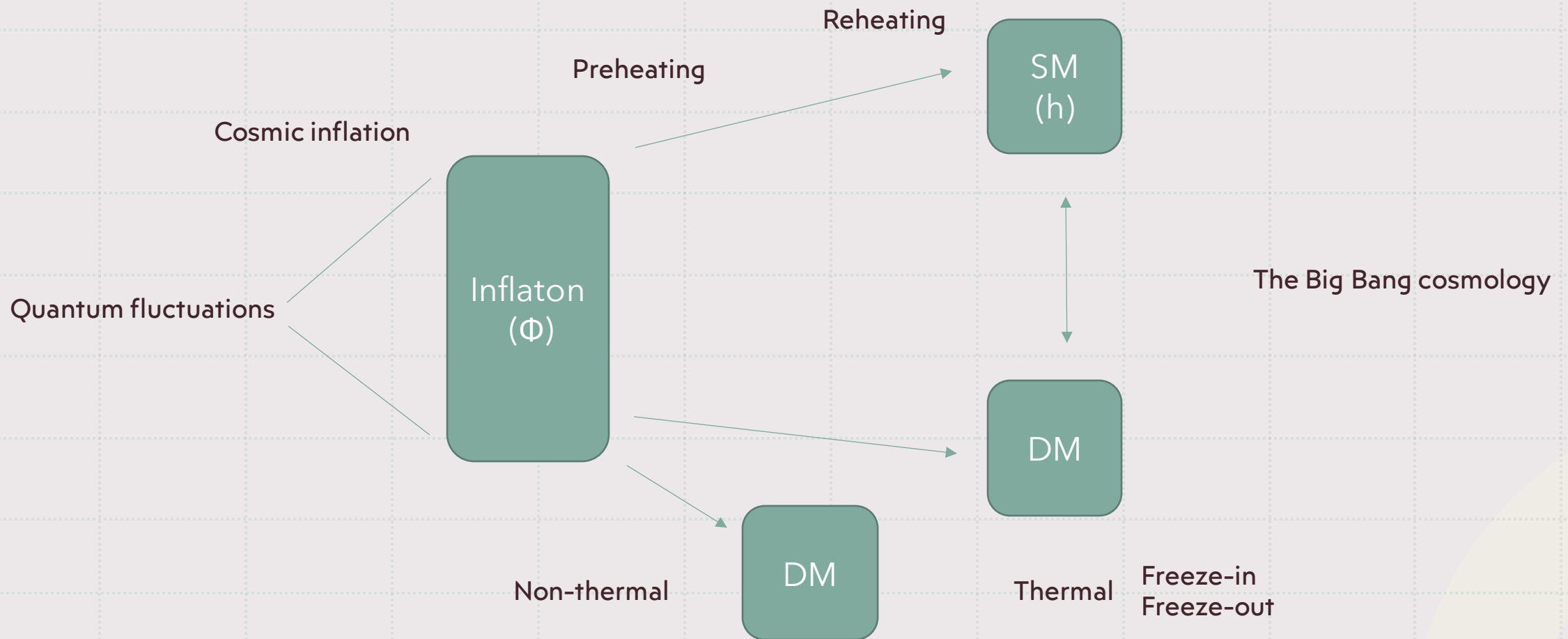
- New Inflation, Slow-roll, Chaotic, etc.

(Linde, etc., 1982~)

- A real scalar field, "Inflaton"



Introduction



Introduction

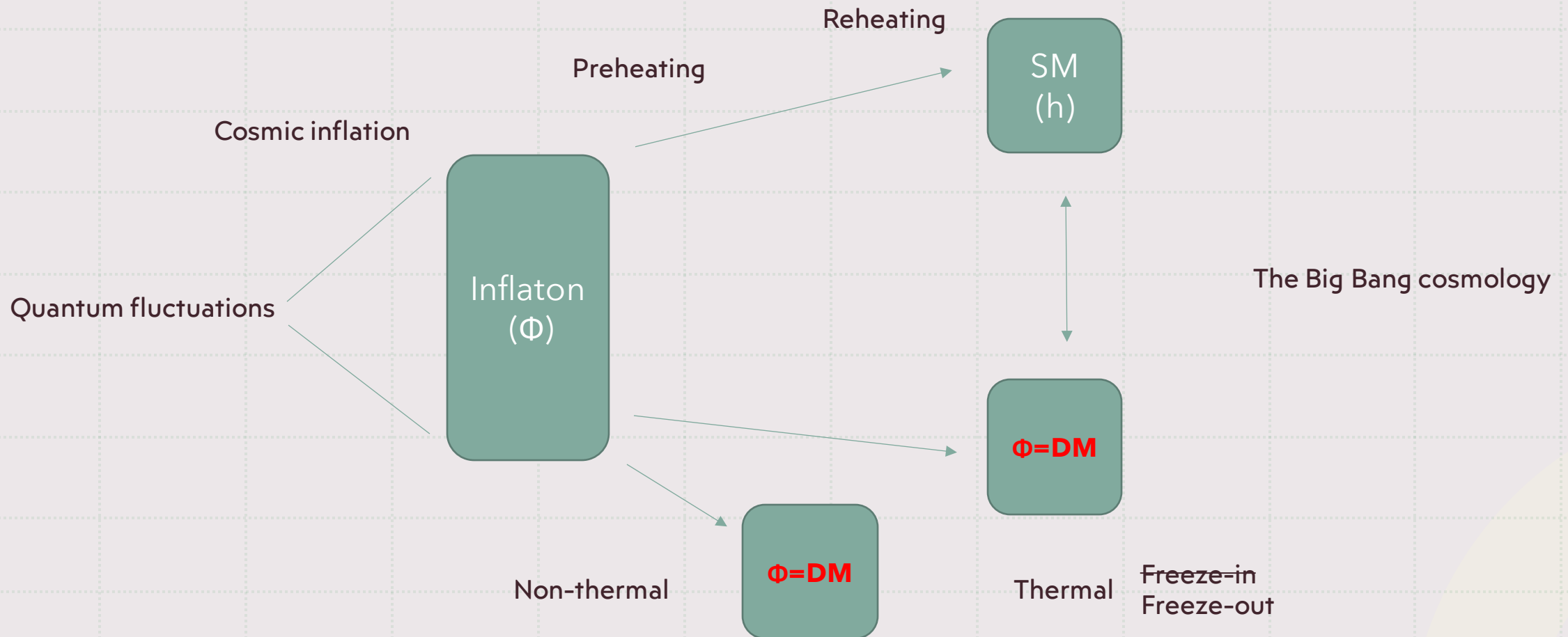
Inflaton and Dark Matter

- **'Inflaton = Dark Matter'**

- 'Inflaton \neq Dark Matter'

- 'Inflaton \rightarrow Dark Matter'

'Inflaton = Dark Matter' model



Exp. constraints

Monomial potentials were ruled out
(Planck, 2013)

$$V(\phi, h) = \frac{1}{4}\lambda_h h^4 + \frac{1}{4}\lambda_{\phi h} h^2 \phi^2 + \frac{1}{4}\lambda_{\phi} \phi^4 + \frac{1}{2}m_h^2 h^2 + \frac{1}{2}m_{\phi}^2 \phi^2$$

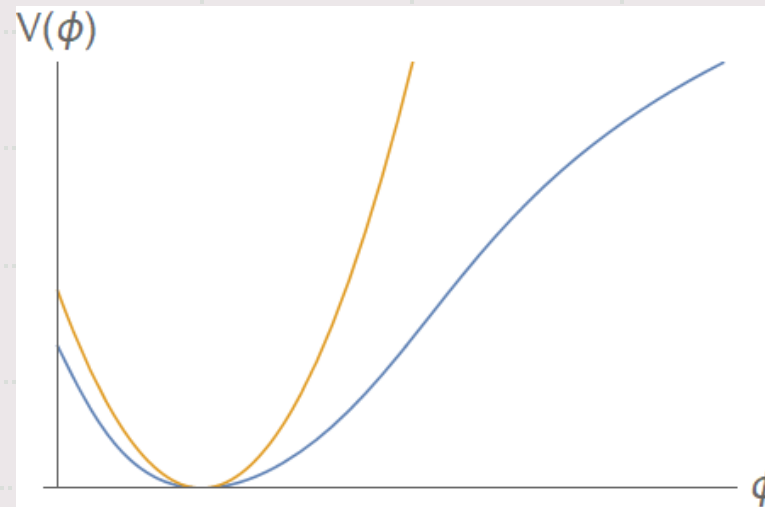
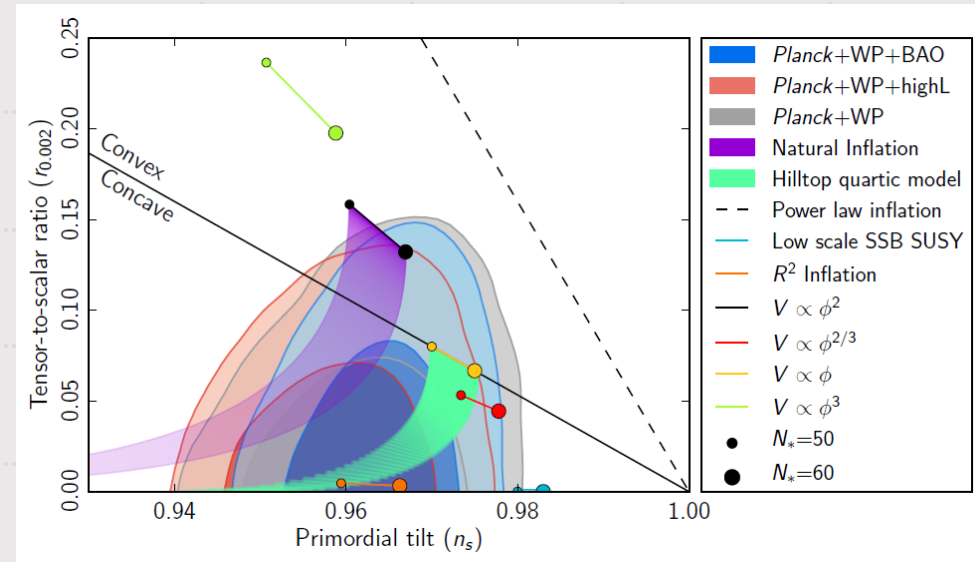
→ Non-minimal coupling to gravity

$$\mathcal{L}_J = \sqrt{-\hat{g}} \left(-\frac{1}{2}\Omega \hat{R} + \frac{1}{2}\partial_{\mu}\phi\partial^{\mu}\phi + (D_{\mu}H)^{\dagger}D^{\mu}H - V(\phi, H) \right)$$

$$\Omega = 1 + \xi_h h^2 + \xi_{\phi} \phi^2$$

$$g_{\mu\nu} = \Omega \hat{g}_{\mu\nu}$$

$$V_E = \frac{\lambda_{\phi}}{4\xi_{\phi}^2} \left(1 + \exp\left(-\frac{2\gamma\chi'}{\sqrt{6}}\right) \right)^{-2}$$



How to light up the Dark Universe

The universe was full of Inflaton in the beginning

If Inflaton-DM fails to transfer its energy to SM enough, we would end up with DM-dominated universe

✂ Force ourselves to fragment Inflaton as much as possible through its Higgs coupling

Non-thermal v.s. Thermal DM production



Non-thermal Dark Matter

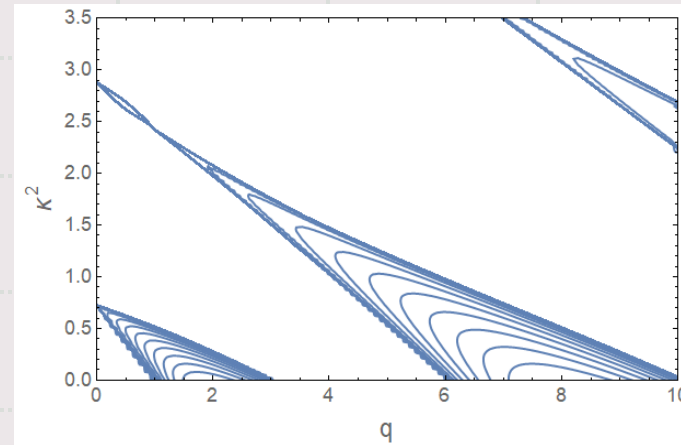
Inflaton field oscillates coherently (homogeneous) \rightarrow Parametric resonance

EOM: $\ddot{\phi} + 3H\dot{\phi} + \lambda_{\phi}\phi^3 = 0$

$$\phi(t) = \frac{\Phi_0}{a(t)} \operatorname{cn}\left(x, \frac{1}{\sqrt{2}}\right)$$

$$X_k'' + \left[\kappa^2 + \frac{\lambda_{\phi} h}{2\lambda_{\phi}} \operatorname{cn}^2\left(x, \frac{1}{\sqrt{2}}\right) \right] X_k = 0$$

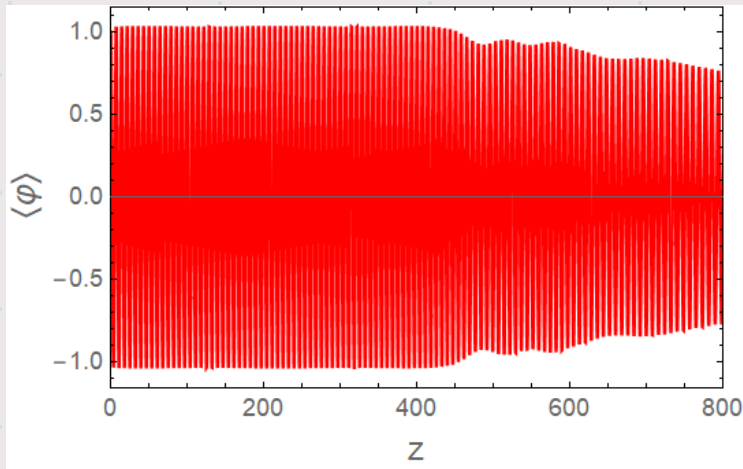
\uparrow
q parameter



Modes inside bands grow exponentially

Non-thermal Dark Matter

Fast Higgs decay \rightarrow No B.E. condensation \rightarrow Perturbative computation



$$\Gamma_{\phi}^{\text{pert}} = C \frac{\lambda_{\phi h}^2}{16\pi} \frac{\Phi_0}{a(t)\sqrt{\lambda_{\phi}}}$$

Inflaton bck. decays alone
and produces its quanta

Decay into Higgs is much slower than decay into inflaton quanta

\rightarrow We are left with too much inflaton DM

Non-thermal Dark Matter

Slow Higgs decay \rightarrow B.E. condensation \rightarrow Resonance

- Parametric resonance
- How long? When does it end?

Non-thermal Dark Matter

Produced particles can re-scatter off background field

→ Inflaton is no longer dominant

→ Linear regime breaks down

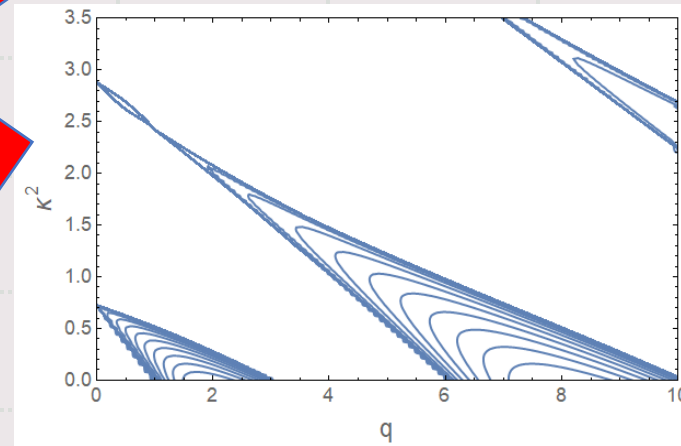
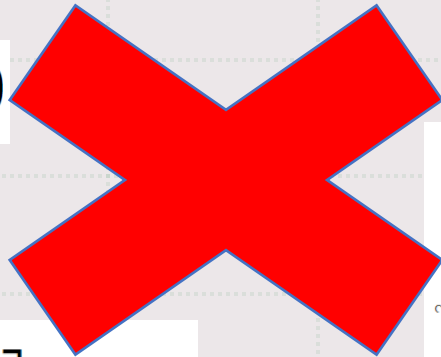
Non-thermal Dark Matter

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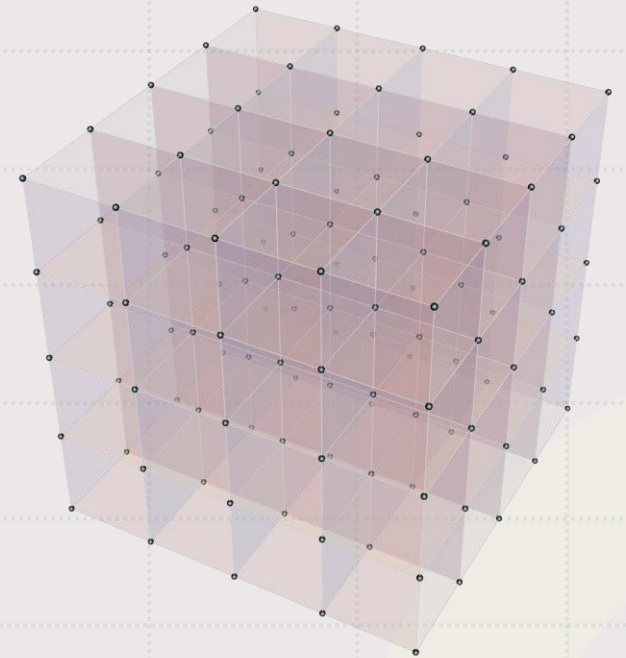
Modes inside bands grow exponentially

Non-thermal Dark Matter

Backreaction and Rescattering → Non-perturbative description

Lattice simulations

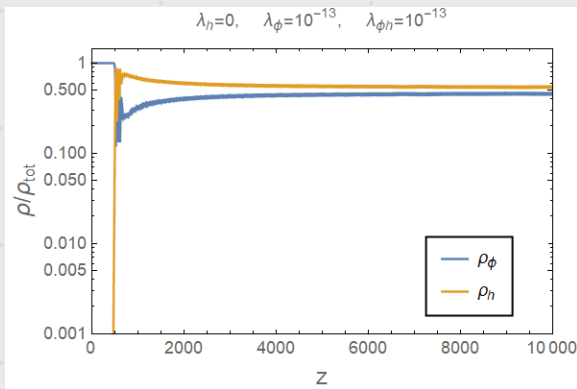
- solve equations of motion at each space point
- LATTICEEASY, CosmoLattice, etc.
- Parallel computation on cluster computers



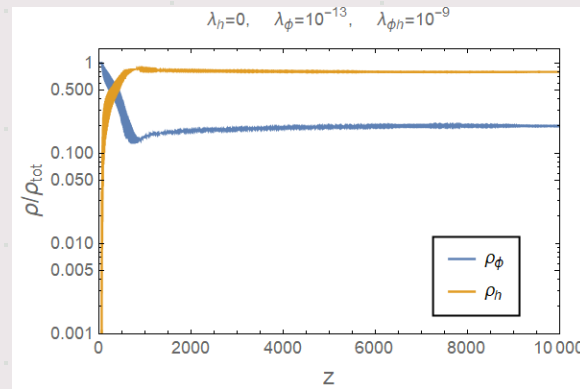
Non-thermal Dark Matter

Zero v.s. Non-zero for the Higgs self-interaction coupling

$$\lambda_h = 0$$



$\lambda = 10^{-13}$



Stronger interaction

Democratic energy distribution

→ Quasi-equilibrium $\frac{\rho_\phi}{\rho_{\text{tot}}} \sim \frac{1}{\text{\#d.o.f.}}$

→ Over-abundance

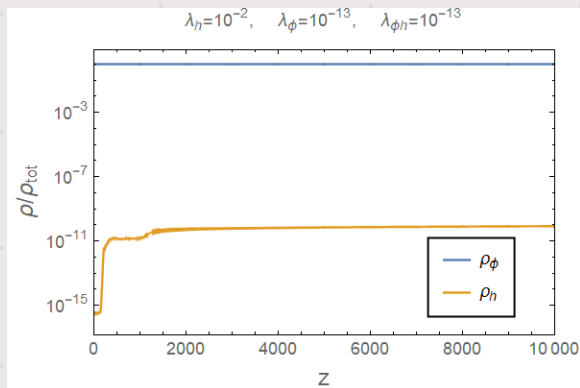
$$Y = n_\phi / s_{\text{SM}} \gtrsim 10^{-3}$$

$$Y_{\text{obs}} = 4 \times 10^{-10} \text{ GeV}/m_\phi$$

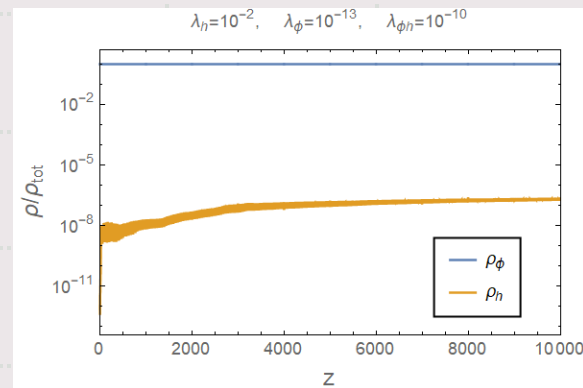
Non-thermal Dark Matter

Zero v.s. Non-zero for the Higgs self-interaction coupling

$$\lambda_h = 0.01$$



$\lambda = 10^{-13}$



Stronger interaction

Higgs production is hindered by backreaction (large effective mass)

$$\lambda_\phi \phi^2 \sim \lambda_h \langle h^2 \rangle$$

$$\rho_\phi \gg \rho_{\text{SM}}$$

for the same reason in Fast Higgs decay scenario

Thermal Dark Matter

Experimental constraint and RG equation \rightarrow Breaks Unitarity

$$\lambda_{\phi h}(1 \text{ TeV}) \gtrsim 0.25$$

$$16\pi^2 \frac{d\lambda_{\phi}}{dt} = 2\lambda_{\phi h}^2 + 18\lambda_{\phi}^2$$

Non-minimal coupling to gravity corresponds to Dim-5 operator

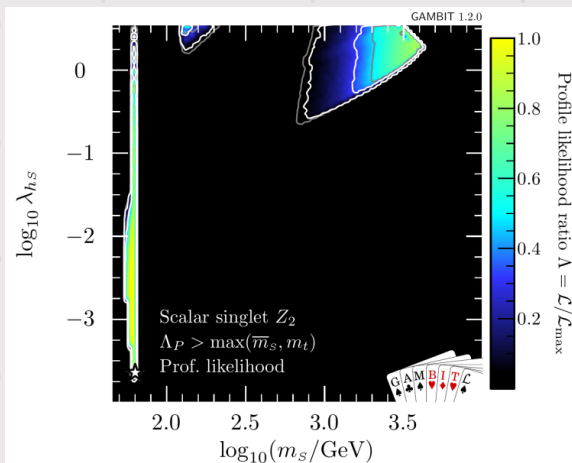
- Cut-off scale in EFT $\Lambda \sim 1/\xi_{\phi}$

Inflationary energy scale can't be larger than the cut-off scale

$$(\lambda_{\phi}/4\xi_{\phi}^2)^{1/4}$$

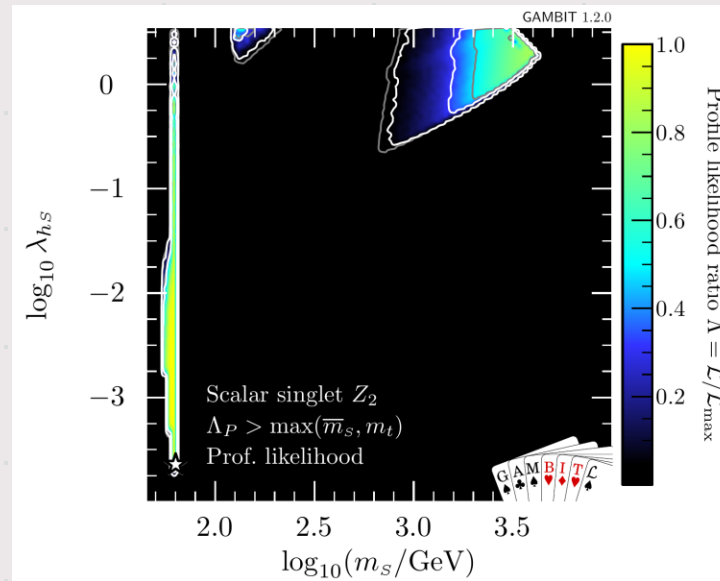
$$\lambda_{\phi}(H) < 4 \times 10^{-5}$$

$$\lambda_{\phi}(H) \gtrsim 10^{-3}$$



Thermal Dark Matter

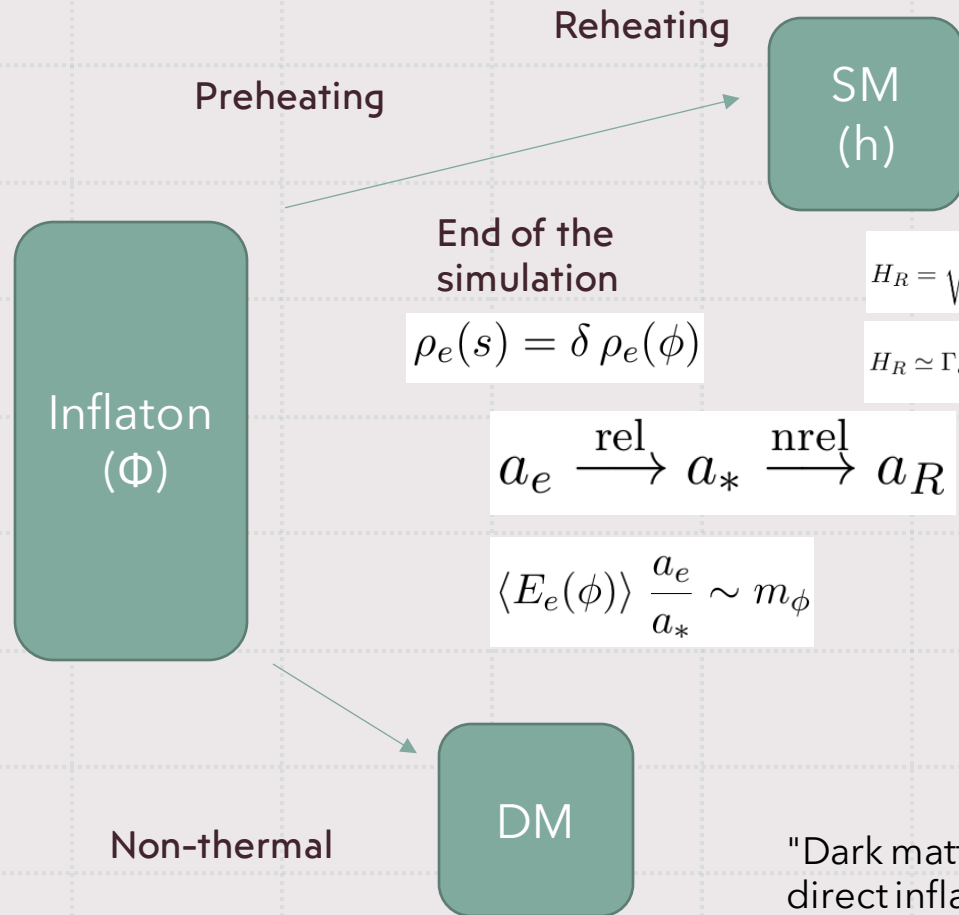
Higgs resonance $\phi\phi \rightarrow h \rightarrow \text{SM}$



$$m_\phi \simeq m_{h_0}/2$$

→The mass of inflaton DM should be equal to half Higgs mass

'Inflaton \neq Dark Matter' model



Reheating

SM
(h)

Preheating

End of the simulation

$$\rho_e(s) = \delta \rho_e(\phi)$$

$$H_R = \sqrt{\frac{\pi^2 g_*}{90}} T_R^2$$

$$H_R \simeq \Gamma_{\phi \rightarrow hh}, \quad \Gamma_{\phi \rightarrow hh} = \frac{\sigma_{\phi h}^2}{8\pi m_\phi}$$

$$a_e \xrightarrow{\text{rel}} a_* \xrightarrow{\text{nrel}} a_R$$

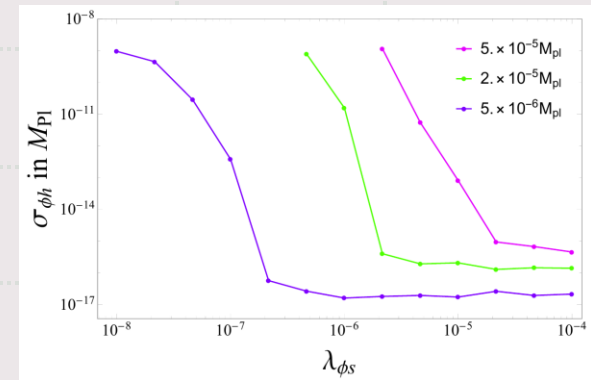
$$Y_\infty = 4.4 \times 10^{-10} \left(\frac{\text{GeV}}{m_s} \right)$$

$$\langle E_e(\phi) \rangle \frac{a_e}{a_*} \sim m_\phi$$

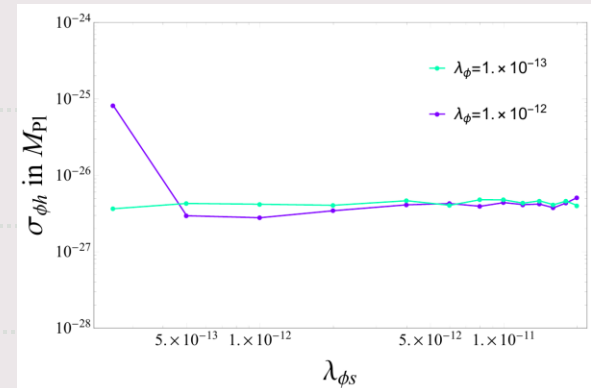
Non-thermal

DM

"Dark matter production and reheating via direct inflaton couplings: collective effects", 2107.06292



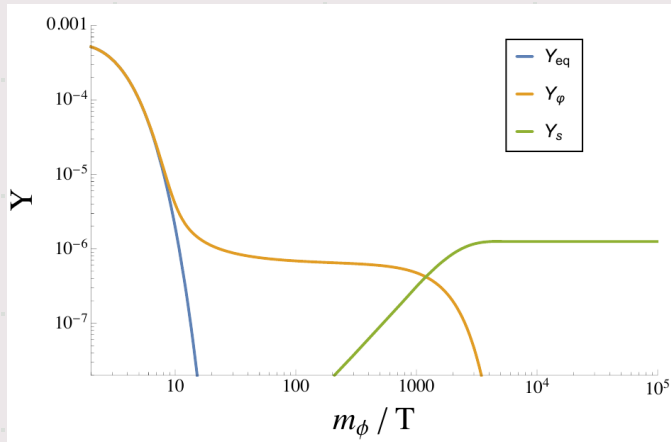
$$V_\phi = \frac{m_\phi^2}{2} \phi^2$$



$$V_\phi = \frac{1}{4} \lambda_\phi \phi^4$$

'Inflaton → Dark Matter' model

Inflaton freeze-out

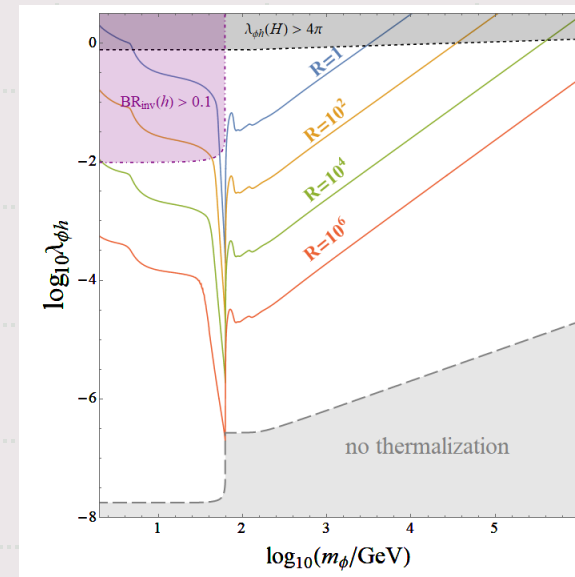


$$Y_s = Y_\phi^{\text{FO}} \times 2 \text{BR}(\phi \rightarrow ss)$$

$$Y_s = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_s}, \quad Y_\phi^{\text{FO}} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_\phi} \times R,$$

$$\frac{m_\phi}{R} = 2m_s \text{BR}(\phi \rightarrow ss).$$

Allowed parameter space



Summary

We find the interplay of Inflaton and Dark matter fun

Non-linear effects are important in the post-inflationary universe

We have studied "Inflaton Dark Matter model" in a minimalistic framework

- Non-thermal DM remains too much to match current observations
- Thermal DM threatens the unitarity condition → Mass should be fine-tuned