

ON WEAK FIELD GRAVITY-MAXWELL SYMMETRIES IN SC FLUCTUATIONS REGIME

Gravity vs. condensed matter physics

Antonio Gallerati

Politecnico di Torino - Dipartimento di Scienza Applicata e Tecnologia

Istituto Nazionale di Fisica Nucleare - Sez. TO

1 Introduction

- 1** **Introduction**

- 2** **Gravito-Maxwell weak field expansion**

- 1** **Introduction**

- 2** **Gravito-Maxwell weak field expansion**

- 3** **The quantum model**

- 1** **Introduction**

- 2** **Gravito-Maxwell weak field expansion**

- 3** **The quantum model**

- 4** **Results**

It is since 1966, with the paper of DeWitt [*Phys. Rev. Lett.* 16 (1966)], that there is great interest in the interplay between the theory of gravitation and superconductivity

It is since 1966, with the paper of DeWitt [*Phys. Rev. Lett.* 16 (1966)], that there is great interest in the interplay between the theory of gravitation and superconductivity

- Podkletnov and Nieminen declared to have observed a gravitational shielding in a rotating disk of YBaCuO (YBCO) [*Physica C: Superconductivity* 203 (1992)].

It is since 1966, with the paper of DeWitt [*Phys. Rev. Lett.* 16 (1966)], that there is great interest in the interplay between the theory of gravitation and superconductivity

- Podkletnov and Nieminen declared to have observed a gravitational shielding in a rotating disk of YBaCuO (YBCO) [*Physica C: Superconductivity* 203 (1992)].
- In 1996 Modanese proposed a theoretical explanation [*EPL* 35 (1996)] in the frame of a quantum field formulation.

It is since 1966, with the paper of DeWitt [*Phys. Rev. Lett.* 16 (1966)], that there is great interest in the interplay between the theory of gravitation and superconductivity

- Podkletnov and Nieminen declared to have observed a gravitational shielding in a rotating disk of YBaCuO (YBCO) [*Physica C: Superconductivity* 203 (1992)].
- In 1996 Modanese proposed a theoretical explanation [*EPL* 35 (1996)] in the frame of a quantum field formulation.
- It is instructive to explore a weak field expansion for nearly flat spacetime configurations (generalization of Maxwell equations).



- ① Classical framework: impossible to extract experimental evidences.

- 1 Classical framework: impossible to extract experimental evidences.
- 2 Quantum picture: observable effects are possible

- 1 **Classical framework**: impossible to extract experimental evidences.
- 2 **Quantum picture**: observable effects are possible
 - the probability of a graviton excitation of a medium particle is suppressed;

- ① **Classical framework**: impossible to extract experimental evidences.

- ② **Quantum picture**: observable effects are possible
 - the probability of a graviton excitation of a medium particle is suppressed;

 - possible interaction of the gravitational field with some particular state of matter, like a Bose condensate or a more general superfluid:

- 1 **Classical framework**: impossible to extract experimental evidences.
- 2 **Quantum picture**: observable effects are possible
 - the probability of a graviton excitation of a medium particle is suppressed;
 - possible interaction of the gravitational field with some particular state of matter, like a Bose condensate or a more general superfluid:

$$\mathcal{L}_{\text{int}} \propto h^{\mu\nu} \partial_{\mu} \phi_0^* \partial_{\nu} \phi_0,$$

- 1 **Classical framework**: impossible to extract experimental evidences.
- 2 **Quantum picture**: observable effects are possible
 - the probability of a graviton excitation of a medium particle is suppressed;
 - possible interaction of the gravitational field with some particular state of matter, like a Bose condensate or a more general superfluid:

$$\mathcal{L}_{\text{int}} \propto h^{\mu\nu} \partial_{\mu} \phi_0^* \partial_{\nu} \phi_0, \quad \mathcal{L}_0 = -\frac{1}{2} \partial_{\mu} \phi_0^* \partial^{\mu} \phi_0 + \frac{1}{2} m^2 |\phi_0|^2,$$

- 1 **Classical framework**: impossible to extract experimental evidences.
- 2 **Quantum picture**: observable effects are possible
 - the probability of a graviton excitation of a medium particle is suppressed;
 - possible interaction of the gravitational field with some particular state of matter, like a Bose condensate or a more general superfluid:

$$\mathcal{L}_{\text{int}} \propto h^{\mu\nu} \partial_{\mu} \phi_0^* \partial_{\nu} \phi_0, \quad \mathcal{L}_0 = -\frac{1}{2} \partial_{\mu} \phi_0^* \partial^{\mu} \phi_0 + \frac{1}{2} m^2 |\phi_0|^2,$$

where $g_{\mu\nu} \simeq \eta_{\mu\nu} + h_{\mu\nu}$, $\phi_0 = \langle 0|\phi|0\rangle$.



The general Einstein equations are written as

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8\pi G_N T_{\mu\nu} .$$

The general Einstein equations are written as

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8\pi G_N T_{\mu\nu} .$$

- Let us now consider a nearly flat spacetime configuration where the metric can be expanded as $g_{\mu\nu} \simeq \eta_{\mu\nu} + h_{\mu\nu}$ and introduce then the tensors

$$\bar{h}_{\mu\nu} = h_{\mu\nu} - \frac{1}{2} \eta_{\mu\nu} h, \quad \mathcal{G}_{\mu\nu\rho} \simeq \partial_{[\nu} \bar{h}_{\rho]\mu},$$

having imposed the gauge condition $\partial^\mu \bar{h}_{\mu\nu} \simeq 0$;

The general Einstein equations are written as

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8\pi G_N T_{\mu\nu} .$$

- Let us now consider a nearly flat spacetime configuration where the metric can be expanded as $g_{\mu\nu} \simeq \eta_{\mu\nu} + h_{\mu\nu}$ and introduce then the tensors

$$\bar{h}_{\mu\nu} = h_{\mu\nu} - \frac{1}{2} \eta_{\mu\nu} h, \quad \mathcal{G}_{\mu\nu\rho} \simeq \partial_{[\nu} \bar{h}_{\rho]\mu},$$

having imposed the gauge condition $\partial^\mu \bar{h}_{\mu\nu} \simeq 0$;

- in first-order approximation, the Einstein equations can be then rewritten as

$$G_{\mu\nu} = \partial^\rho \mathcal{G}_{\mu\nu\rho} = 8\pi G_N T_{\mu\nu} .$$



- Now, let us introduce the new fields

$$\mathbf{E}_g \equiv E_i = -\frac{1}{2} \mathcal{G}_{00i} = -\frac{1}{2} \partial_{[0} \bar{h}_{i]0} ,$$

$$\mathbf{A}_g \equiv A_i = \frac{1}{4} \bar{h}_{0i} , \quad \mathbf{B}_g \equiv B_i = \frac{1}{4} \varepsilon_i{}^{jk} \mathcal{G}_{0jk} ,$$

- Now, let us introduce the new fields

$$\mathbf{E}_g \equiv E_i = -\frac{1}{2} \mathcal{G}_{00i} = -\frac{1}{2} \partial_{[0} \bar{h}_{i]0} ,$$

$$\mathbf{A}_g \equiv A_i = \frac{1}{4} \bar{h}_{0i} , \quad \mathbf{B}_g \equiv B_i = \frac{1}{4} \varepsilon_i{}^{jk} \mathcal{G}_{0jk} ,$$

- it is then possible to write the set of equations:

$$\nabla \cdot \mathbf{E}_g = \frac{\rho_g}{\varepsilon_g} ; \quad \nabla \cdot \mathbf{B}_g = 0 ;$$

$$\nabla \times \mathbf{E}_g = -\frac{\partial \mathbf{B}_g}{\partial t} ; \quad \nabla \times \mathbf{B}_g = \mu_g \mathbf{j}_g + \frac{1}{c^2} \frac{\partial \mathbf{E}_g}{\partial t} ,$$

- Now, let us introduce the new fields

$$\mathbf{E}_g \equiv E_i = -\frac{1}{2} \mathcal{G}_{00i} = -\frac{1}{2} \partial_{[0} \bar{h}_{i]0} ,$$

$$\mathbf{A}_g \equiv A_i = \frac{1}{4} \bar{h}_{0i} , \quad \mathbf{B}_g \equiv B_i = \frac{1}{4} \varepsilon_i{}^{jk} \mathcal{G}_{0jk} ,$$

- it is then possible to write the set of equations:

$$\nabla \cdot \mathbf{E}_g = \frac{\rho_g}{\varepsilon_g} ; \quad \nabla \cdot \mathbf{B}_g = 0 ;$$

$$\nabla \times \mathbf{E}_g = -\frac{\partial \mathbf{B}_g}{\partial t} ; \quad \nabla \times \mathbf{B}_g = \mu_g \mathbf{j}_g + \frac{1}{c^2} \frac{\partial \mathbf{E}_g}{\partial t} ,$$

having defined $\rho_g \equiv -T_{00}$, $\mathbf{j}_g \equiv T_{0i}$.



Then, we introduce the generalized fields and potentials

$$\mathbf{E} = \mathbf{E}_e + \frac{m}{e} \mathbf{E}_g ; \quad \mathbf{B} = \mathbf{B}_e + \frac{m}{e} \mathbf{B}_g ;$$

$$\phi = \phi_e + \frac{m}{e} \phi_g ; \quad \mathbf{A} = \mathbf{A}_e + \frac{m}{e} \mathbf{A}_g .$$

Then, we introduce the generalized fields and potentials

$$\mathbf{E} = \mathbf{E}_e + \frac{m}{e} \mathbf{E}_g ; \quad \mathbf{B} = \mathbf{B}_e + \frac{m}{e} \mathbf{B}_g ;$$

$$\phi = \phi_e + \frac{m}{e} \phi_g ; \quad \mathbf{A} = \mathbf{A}_e + \frac{m}{e} \mathbf{A}_g .$$

The *generalized Maxwell equations* for the above fields become:

$$\nabla \cdot \mathbf{E} = \left(\frac{1}{\varepsilon_g} + \frac{1}{\varepsilon_0} \right) \rho ; \quad \nabla \cdot \mathbf{B} = 0 ;$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} ; \quad \nabla \times \mathbf{B} = (\mu_g + \mu_0) \mathbf{j} + \frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} .$$

Then, we introduce the generalized fields and potentials

$$\mathbf{E} = \mathbf{E}_e + \frac{m}{e} \mathbf{E}_g ; \quad \mathbf{B} = \mathbf{B}_e + \frac{m}{e} \mathbf{B}_g ;$$

$$\phi = \phi_e + \frac{m}{e} \phi_g ; \quad \mathbf{A} = \mathbf{A}_e + \frac{m}{e} \mathbf{A}_g .$$

The *generalized Maxwell equations* for the above fields become:

$$\nabla \cdot \mathbf{E} = \left(\frac{1}{\varepsilon_g} + \frac{1}{\varepsilon_0} \right) \rho ; \quad \nabla \cdot \mathbf{B} = 0 ;$$

$$\nabla \times \mathbf{E} = - \frac{\partial \mathbf{B}}{\partial t} ; \quad \nabla \times \mathbf{B} = (\mu_g + \mu_0) \mathbf{j} + \frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} .$$

[AG, *Eur.Phys.J. C77 (2017)*, *Symmetry 11 (2019)*]



The fluctuation regime can be described using the time-dependent Ginzburg-Landau equations that, for $T > T_c$, read

$$\Gamma \left(\hbar \frac{\partial}{\partial t} - 2ie\phi \right) \psi = \frac{1}{2m} (\hbar \nabla - 2ie\mathbf{A})^2 \psi + \alpha \psi.$$

The fluctuation regime can be described using the time-dependent Ginzburg-Landau equations that, for $T > T_c$, read

$$\Gamma \left(\hbar \frac{\partial}{\partial t} - 2ie\phi \right) \psi = \frac{1}{2m} (\hbar \nabla - 2ie\mathbf{A})^2 \psi + \alpha \psi.$$

- First, we look for a solution of the form

$$\psi(\mathbf{x}, t) = f(\mathbf{x}, t) \exp(i g(\mathbf{x}, t));$$

The fluctuation regime can be described using the time-dependent Ginzburg-Landau equations that, for $T > T_c$, read

$$\Gamma \left(\hbar \frac{\partial}{\partial t} - 2ie\phi \right) \psi = \frac{1}{2m} (\hbar \nabla - 2ie\mathbf{A})^2 \psi + \alpha \psi.$$

- First, we look for a solution of the form

$$\psi(\mathbf{x}, t) = f(\mathbf{x}, t) \exp(i g(\mathbf{x}, t));$$

- one then finds for the superfluid speed

$$\mathbf{v}_s = \frac{1}{m} \left(\hbar \nabla g + 2 \frac{e}{c} \mathbf{A} \right),$$

The fluctuation regime can be described using the time-dependent Ginzburg-Landau equations that, for $T > T_c$, read

$$\Gamma \left(\hbar \frac{\partial}{\partial t} - 2 i e \phi \right) \psi = \frac{1}{2m} (\hbar \nabla - 2 i e \mathbf{A})^2 \psi + \alpha \psi.$$

- First, we look for a solution of the form

$$\psi(\mathbf{x}, t) = f(\mathbf{x}, t) \exp(i g(\mathbf{x}, t));$$

- one then finds for the superfluid speed

$$\mathbf{v}_s = \frac{1}{m} \left(\hbar \nabla g + 2 \frac{e}{c} \mathbf{A} \right),$$

while the associated current density has the form

$$\mathbf{j}_s = -2 \frac{e}{m} |\psi|^2 \left(\hbar \nabla g + 2 \frac{e}{c} \mathbf{A} \right) = -2 e f^2 \mathbf{v}_s.$$

Using fluctuations theory, we can calculate the supercurrent $j_s(t)$ for three-dimensional samples with dimensions greater than the correlation length.

Using fluctuations theory, we can calculate the supercurrent $\mathbf{j}_s(t)$ for three-dimensional samples with dimensions greater than the correlation length.

- The potential vector $\mathbf{A}(x, y, z, t)$ can be then extracted from:

$$\mathbf{A}(x, y, z, t) = \frac{1}{4\pi} \int \frac{\mathbf{j}_s(t) \, dx' \, dy' \, dz'}{\sqrt{(x - x')^2 + (y - y')^2 + (z - z')^2}} ,$$

when the time variations of external fields are small.

Using fluctuations theory, we can calculate the supercurrent $\mathbf{j}_s(t)$ for three-dimensional samples with dimensions greater than the correlation length.

- The potential vector $\mathbf{A}(x, y, z, t)$ can be then extracted from:

$$\mathbf{A}(x, y, z, t) = \frac{1}{4\pi} \int \frac{\mathbf{j}_s(t) \, dx' \, dy' \, dz'}{\sqrt{(x - x')^2 + (y - y')^2 + (z - z')^2}} ,$$

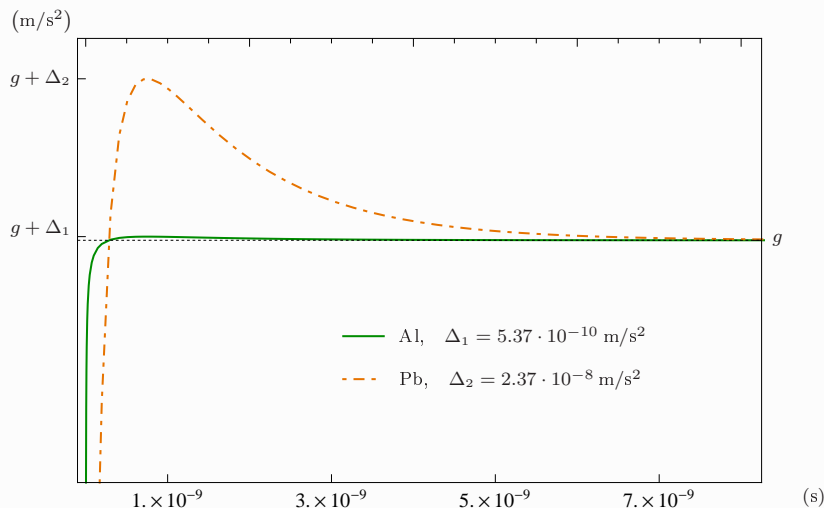
when the time variations of external fields are small.

- The generalized electric field $\mathbf{E}(x, y, z, t)$ can be then written as

$$\mathbf{E}(x, y, z, t) = -\frac{1}{c} \frac{\partial \mathbf{A}}{\partial t} + \frac{m}{e} \mathbf{g} = -\frac{1}{c} \frac{\partial \mathbf{j}_s(t)}{\partial t} \mathcal{C}(x, y, z) + \frac{m}{e} \mathbf{g} ,$$

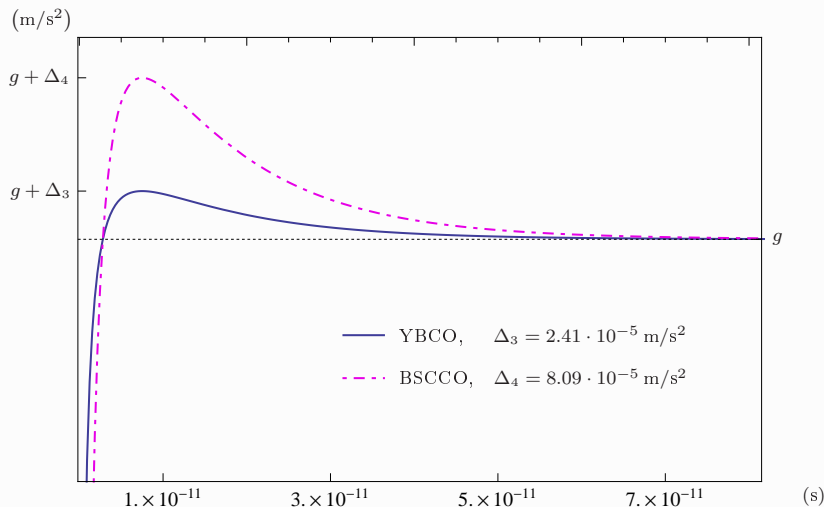
where we have considered the static weak (Earth-surface) gravitational field contribution, and where $\mathcal{C}(x, y, z)$ is a geometrical factor.





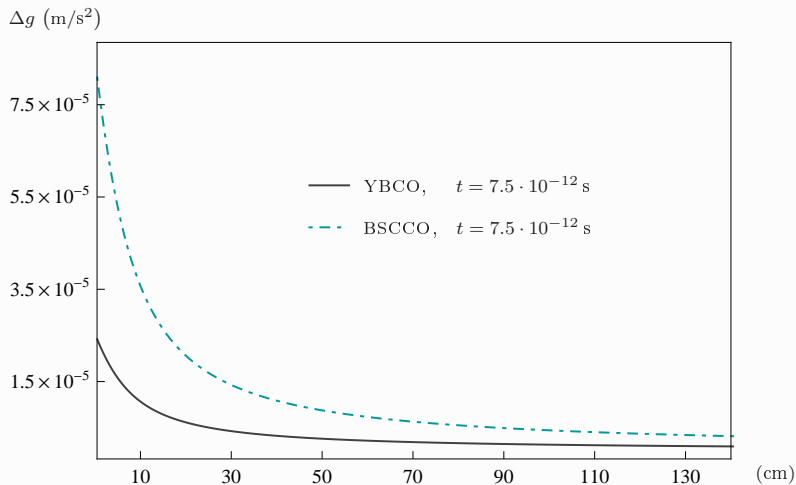
Disk with $R = 10 \text{ cm}$, $h = 1 \text{ cm}$, bases parallel to the ground; the corrections are calculated at a fixed distance $d = 0.5 \text{ cm}$ from the base surface [AG, *Symmetry 11* (2019)].





Disk with $R = 10 \text{ cm}$, $h = 1 \text{ cm}$, bases parallel to the ground; the corrections are calculated at a fixed distance $d = 0.5 \text{ cm}$ from the base surface [AG, *Symmetry 11* (2019)].





Field variation measured along the axis of the disk, at fixed time $t = \tau_0$ that maximizes the effect [AG, *Symmetry 11* (2019)].

- 1 In a very short initial time interval, the gravitational field is reduced w.r.t. its unperturbed value; after that, it increases up to a maximum value and then decreases to the standard external value.

- 1 In a very short initial time interval, the gravitational field is reduced w.r.t. its unperturbed value; after that, it increases up to a maximum value and then decreases to the standard external value.
- 2 The value of the maximum variation Δ is in principle measurable (especially in high- T_c superconductors), while the problem lies in the short time intervals in which the perturbation manifests itself.

- 1 In a very short initial time interval, the gravitational field is reduced w.r.t. its unperturbed value; after that, it increases up to a maximum value and then decreases to the standard external value.
- 2 The value of the maximum variation Δ is in principle measurable (especially in high- T_c superconductors), while the problem lies in the short time intervals in which the perturbation manifests itself.
- 3 It is possible to show that $\tau_0 \propto (T - T_c)^{-1}$, so it is fundamental to be very close to the critical temperature in order to increase the time range in which the effect takes place.

- 1 In a very short initial time interval, the gravitational field is reduced w.r.t. its unperturbed value; after that, it increases up to a maximum value and then decreases to the standard external value.
- 2 The value of the maximum variation Δ is in principle measurable (especially in high- T_c superconductors), while the problem lies in the short time intervals in which the perturbation manifests itself.
- 3 It is possible to show that $\tau_0 \propto (T - T_c)^{-1}$, so it is fundamental to be very close to the critical temperature in order to increase the time range in which the effect takes place.
- 4 The maximum value of the correction is obtained for $t = \tau_0$ and is proportional to $\xi(T)^{-1}$: this means that the effect is larger in high- T_c superconductors, having the latter small coherence length.



Thank you for listening!