

Pileup and Underlying Event Mitigation with Iterative Constituent Subtraction

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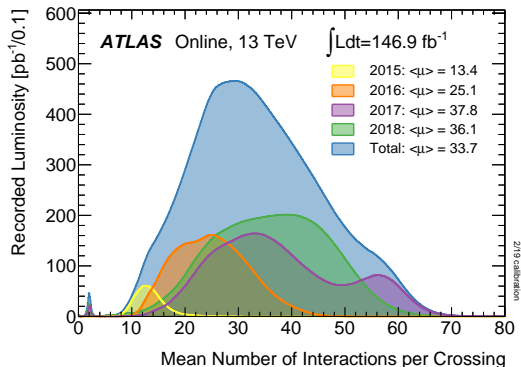
This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 797520

1. Pileup at the LHC
2. Constituent Subtraction
3. Newest developments: Iterative Constituent Subtraction

Pileup at the LHC

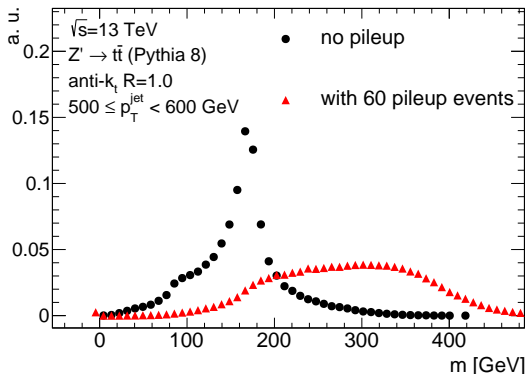
Pileup at the LHC

- Pileup = simultaneous proton-proton collisions in one bunch crossing (or in neighboring bunch crossings)
- Higher instantaneous luminosity \implies higher pileup
 - LHC Run2: up to ~ 70 interactions per bunch crossing,
 - future LHC running: up to 200 interactions per bunch crossing.



Pileup effects for jets

- Pileup randomly adds energy deposits to calorimeter
 - 20 pileup events adds ~ 50 GeV additional p_T under an anti- k_t $R=1.0$ jet,
 - jet shape variables (mass, width,...) may change significantly.
- Necessity to mitigate pileup effects



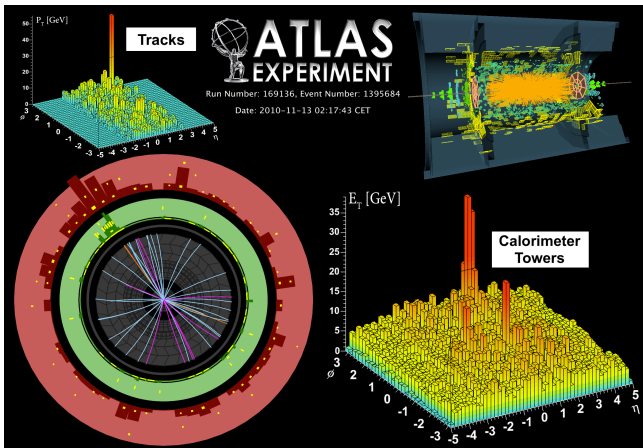
large- R jets containing top quarks

Selection of pileup mitigation methods for jets

- Area Subtraction - [arXiv:0707.1378](#), [arXiv:0802.1188](#)
 - used by LHC experiments in ~ 600 physics measurements
- **Constituent Subtraction** - [arXiv:1403.3108](#)
 - better performance than Area Subtraction
 - already used in 12 physics measurements
- SoftKiller (SK) - [arXiv:1407.0408](#)
- PUPPI - [arXiv:1407.6013](#)
 - used at the CMS experiment
- **Iterative Constituent Subtraction** - [arXiv:1905.03470](#)

Heavy-ion collisions

- Underlying event in heavy-ion collisions \approx pileup in proton-proton collisions
 \Rightarrow same methods to correct jets can be used



ATLAS experiment, heavy-ion collision with dijet event

<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/EventDisplayHeavyIonCollisions>

Constituent Subtraction

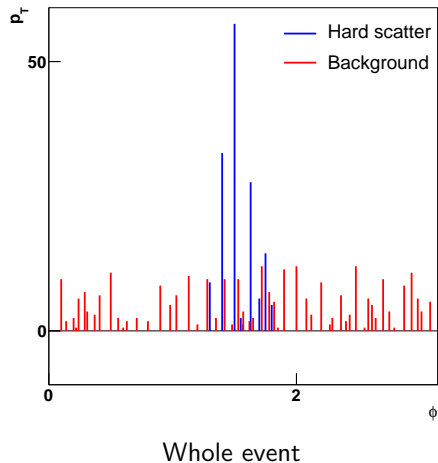
Constituent Subtraction (CS)

- Pileup subtraction method at the level of inputs
- Generalization of the Area Subtraction
 - exploits the background p_T density (ρ)
- ρ = amount of p_T from pileup particles per unit area in the rapidity - azimuth ($y - \phi$) space
- Two possibilities of usage:
 - **jet-by-jet** - jet clustering first, then correction of individual jets
 - **event-wide** - correction of the whole event first, then jet clustering
 - jet clustering is less biased

Physics results with Constituent Subtraction

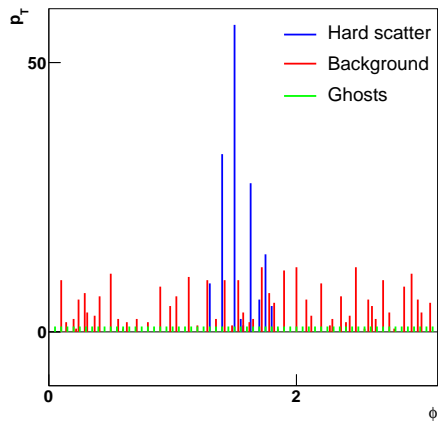
- **ALICE** publications:
 - Measurements of jet fragmentation and jet substructure with ALICE, arXiv:1909.03066
 - Role of Coherence Effects on Jet Quenching in Pb-Pb, arXiv:1705.03383
 - Exploring jet substructure with jet shapes in ALICE, arXiv:1704.05230
 - First measurement of jet mass in Pb-Pb and p-Pb collisions, arXiv:1702.00804
 - Jet shapes in pp and Pb-Pb collisions at ALICE, arXiv:1512.07882
- **ATLAS** publication:
 - Measurement of $Z(\rightarrow b\bar{b})\gamma$ differential cross section, arXiv:1907.07093
- **CMS** publications:
 - Evidence for top quark production in nucleus-nucleus collisions, CMS-PAS-HIN-19-001
 - Measurement of Jet Nuclear Modification Factor in PbPb Collisions, CMS-PAS-HIN-18-014
 - Measurement of the groomed jet mass in PbPb and pp collisions, arXiv:1805.05145
 - Splitting function in pp and PbPb collisions, arXiv:1708.09429
- **STAR** publication:
 - Jet sub-structure and parton shower evolution in p+p and Au+Au collisions at STAR, arXiv:1906.05129

1 Estimation of ρ



Event-wide CS

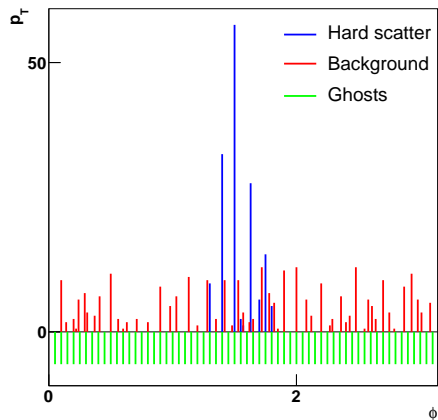
- 1 Estimation of ρ
- 2 **Adding ghosts to the whole event**



Whole event

Event-wide CS

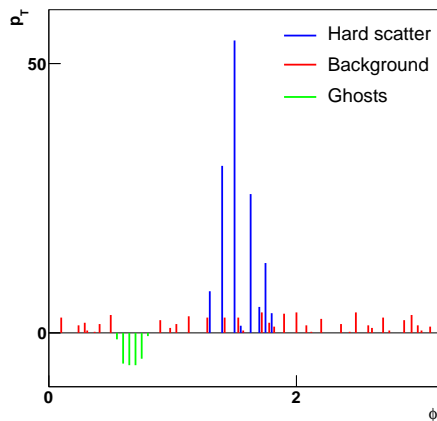
- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 **Setting ghosts p_T to negative value corresponding to ρ**



Whole event before correction

Event-wide CS

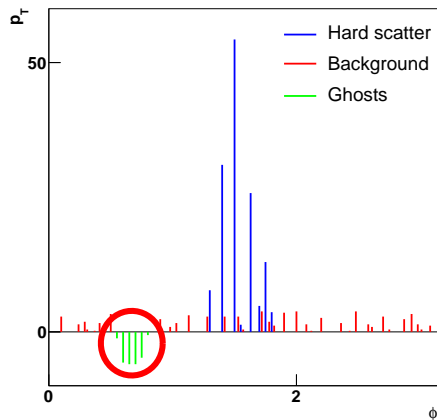
- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 Setting ghosts p_T to negative value corresponding to ρ
- 4 **Matching ghosts to particles**
 - Matching algorithm based on the ΔR distance between particles and ghosts
 - Matching particle-ghost pairs with $\Delta R < \Delta R^{\max}$, where ΔR^{\max} is a free parameter



Whole event after correction

Event-wide CS

- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 Setting ghosts p_T to negative value corresponding to ρ
- 4 Matching ghosts to particles
 - Matching algorithm based on the ΔR distance between particles and ghosts
 - Matching particle-ghost pairs with $\Delta R < \Delta R^{\max}$, where ΔR^{\max} is a free parameter
 - **With finite ΔR^{\max} , some ghosts can be unmatched**
 - discussed later



Whole event after correction

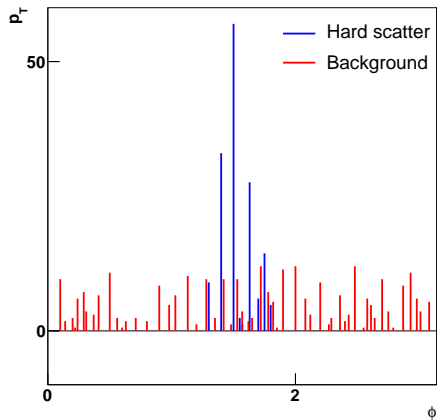
Newest developments: Iterative Constituent Subtraction

Iterative Constituent Subtraction (ICS)

- P. Berta, L. Masetti, D. W. Miller and M. Spousta
JHEP 08 (2019) 175
- New pileup mitigation method for jets
 - supersedes the original Constituent Subtraction method
- Main idea: application of the Event-wide CS several times
 - After each CS application, the remaining unsubtracted p_T in ghosts is redistributed
 - For each iteration, different CS parameters can be used
- Software implementation available in FastJet Contrib since v1.041

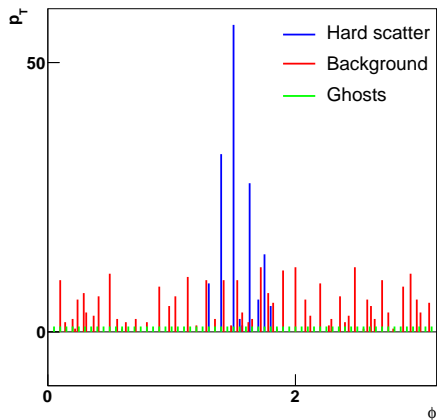
ICS - example with two iterations

1 Estimation of ρ



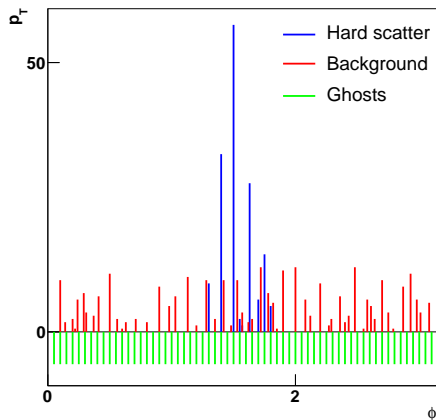
ICS - example with two iterations

- 1 Estimation of ρ
- 2 **Adding ghosts to the whole event**



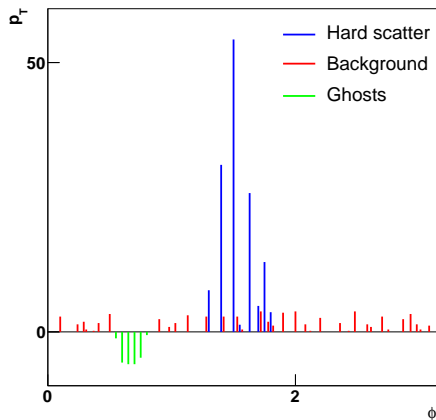
ICS - example with two iterations

- 1 Estimation of ρ
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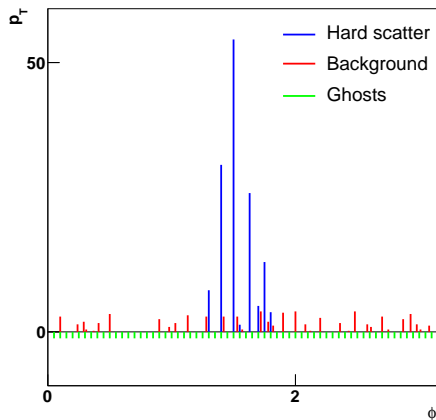
ICS - example with two iterations

- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 Setting ghosts p_T to negative value corresponding to ρ
- 4 **1. iteration: matching of ghosts to particles**



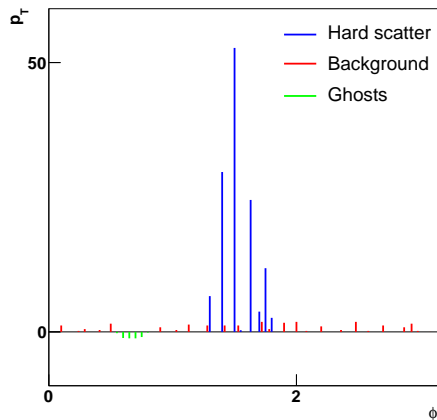
ICS - example with two iterations

- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 Setting ghosts p_T to negative value corresponding to ρ
- 4 1. iteration: matching of ghosts to particles
- 5 **Redistribution of remaining p_T**

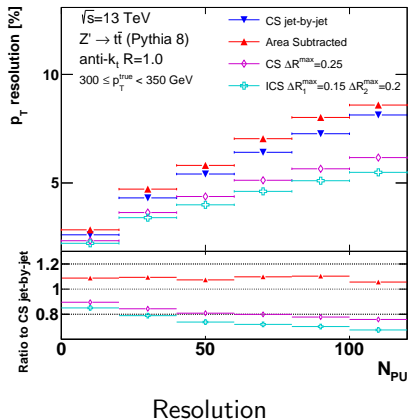
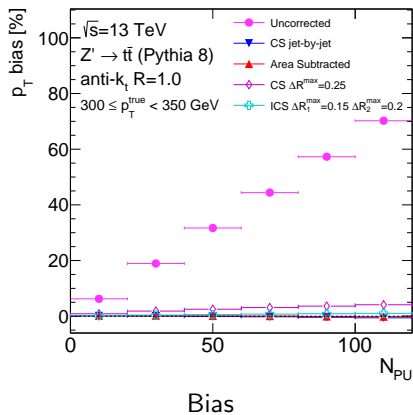


ICS - example with two iterations

- 1 Estimation of ρ
- 2 Adding ghosts to the whole event
- 3 Setting ghosts p_T to negative value corresponding to ρ
- 4 1. iteration: matching of ghosts to particles
- 5 Redistribution of remaining p_T
- 6 **2. iteration: matching of ghosts to particles**

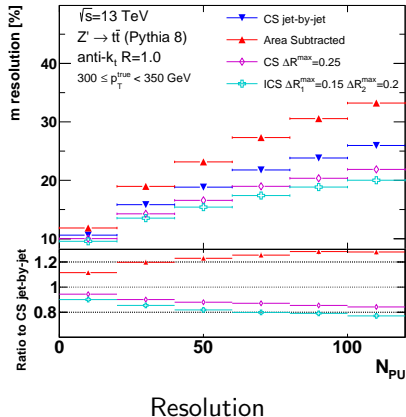
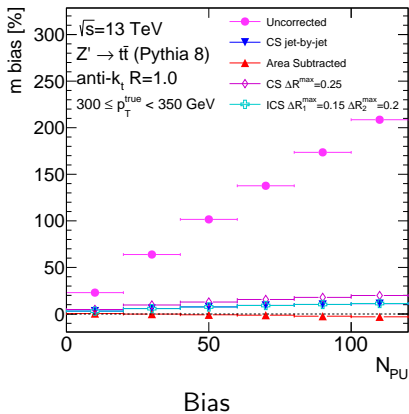


Iterative CS - performance for jet p_T



- ICS improves the jet p_T resolution

Iterative CS - performance for jet mass



- ICS improves the jet mass resolution

- Constituent Subtraction
 - competitive pileup mitigation method
- Iterative Constituent Subtraction
 - new method
 - large improvement in resolution keeping the bias well controlled
 - experiments are encouraged to test it

BACKUP

Background density ρ

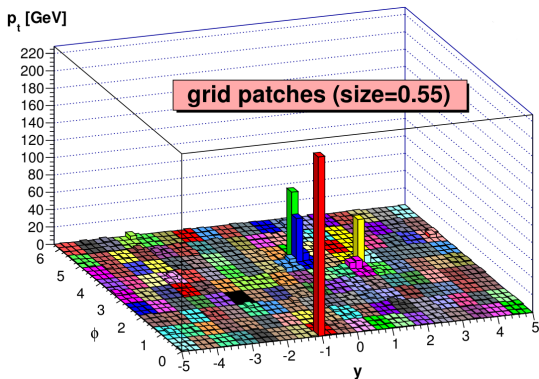
- ρ - amount of p_T from pileup particles per unit area in the rapidity - azimuth ($y - \phi$) space
- many possibilities how to estimate ρ . One of them:

- 1 event divided into rectangular patches in the ($y - \phi$) space; p_T of each patch:

$$p_{T\text{patch}} = \sum_{i \in \text{patch}} p_{Ti}$$

- 2 the estimated pileup p_T density:

$$\rho = \text{median}_{\text{patches}} \left\{ \frac{p_{T\text{patch}}}{A_{\text{patch}}} \right\}$$



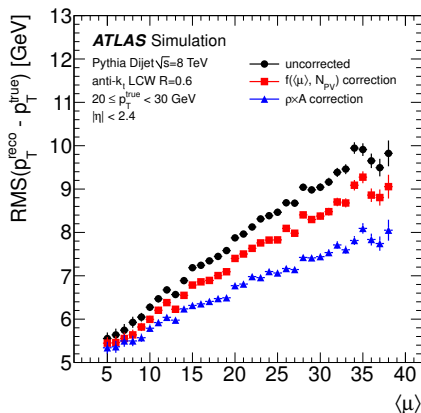
Slides from G. Soyez (BOOST2012 conference)

Pileup mitigation for jets - other methods

- SoftKiller - [arXiv:1407.0408](#)
 - removes particles up to certain p_T threshold
 - the p_T threshold estimated based on the pileup activity in the event
- PUPPI - [arXiv:1407.6013](#)
 - used in CMS
- Grooming:
 - removal of particles within large- R jets
 - makes the signal-to-background separation better (e.g. top quarks vs QCD jets)
 - several methods:
 - trimming - [arXiv:0912.1342](#)
 - SoftDrop - [arXiv:1402.2657](#)
 - pruning - [arXiv:0903.5081](#)
 - ...

Jet Area Subtraction

- Current pileup mitigation method for 8 TeV and 13 TeV data in ATLAS
- Correction of jet 4-momentum
- Basic ingredients:
 - pileup p_T density (ρ)
 - concept of jet area



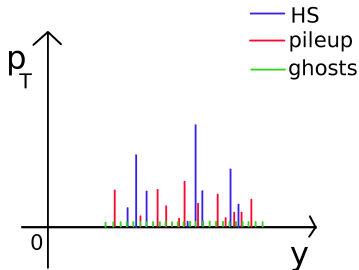
Jet p_T resolution for the Area Subtraction method ($\rho \times A$ correction),
[arXiv:1510.03823](https://arxiv.org/abs/1510.03823)

- ghosts - important ingredient to the “pileup p_T density” methods
- ghosts - infinitesimally soft massless particles uniformly distributed in the $y - \phi$ space. The 4-momentum of ghost k is:

$$g_{\mu,k} = p_T^g \cdot [\cos \phi_k^g, \sin \phi_k^g, \sinh y_k^g, \cosh y_k^g], \quad (1)$$

p_T^g - ghost transverse momentum

- each ghost occupies an area A_g in the $y - \phi$ space,
- the ghosts may be clustered into the jet with arbitrary jet algorithm,
- **ghosts mimic pileup \implies they can be used to subtract pileup.**



Area Subtraction for 4-momentum

- 4-momentum of jet with pileup:

$$[p^x, p^y, p^z, E]. \quad (2)$$

- corrected jet 4-momentum:

$$p_{\text{CORR}}^\mu = [p^x - \rho A^x, p^y - \rho A^y, p^z - \rho A^y, E - \rho A^E]. \quad (3)$$

where area 4-vector A^μ is defined:

$$A^\mu = \frac{A_g}{p_T^g} \sum_{k \in \text{ghosts}} g_{\mu,k} \quad (4)$$

- 1 Adding ghosts to the whole event
- 2 Setting ghosts p_T to negative value corresponding to ρ

3 Matching of ghosts to particles

- Evaluate distances between each particle-ghost pair.
 - Distance between particle i and ghost k :

$$\Delta R_{i,k} = p_{Ti}^\alpha \cdot \sqrt{(y_i - y_k^g)^2 + (\phi_i - \phi_k^g)^2}$$

- Combine each ghost-particle pair starting from lowest $\Delta R_{i,k}$:

$$\text{If } p_{Ti} \geq p_{Tk}^g : \quad p_{Ti} \rightarrow p_{Ti} - p_{Tk}^g \quad \text{otherwise:} \quad p_{Ti} \rightarrow 0$$
$$p_{Tk}^g \rightarrow 0 \quad \quad \quad p_{Tk}^g \rightarrow p_{Tk}^g - p_{Ti}$$

- Procedure stops for $\Delta R_{i,k} > \Delta R^{\max}$

Jet-by-jet CS - detailed description

- for each event
 - 1 estimate the pileup p_T density, ρ , in the event,
 - 2 add ghosts (infinitesimally small p_T^g) among particles in the event and apply jet clustering algorithm to all particles and ghosts \Rightarrow the jets are composited from particles and ghosts,
- for each jet in the event
 - 3 set for each ghost $p_T^g = \rho A_g$
 - 4 evaluate distance $\Delta R_{i,k}$ between particle i and ghost k for each possible particle-ghost pair and sort them in ascending order:

$$\Delta R_{i,k} = p_{Ti}^\alpha \cdot \sqrt{(y_i - y_k^g)^2 + (\phi_i - \phi_k^g)^2}. \quad (5)$$

α - free parameter

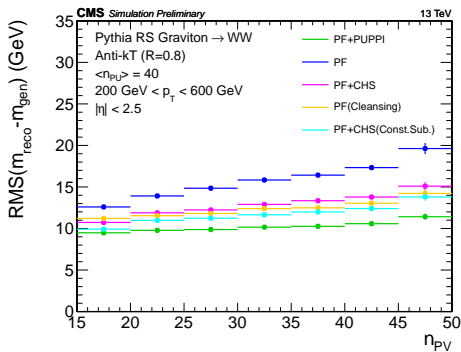
- 5 iteratively change transverse momenta by applying the following procedure for each ghost-particle pair until no more pairs remain or $\Delta R_{i,k} > \Delta R^{\max}$:

$$\begin{aligned} \text{If } p_{Ti} \geq p_{Tk}^g : \quad & p_{Ti} \rightarrow p_{Ti} - p_{Tk}^g, & \text{otherwise:} \quad & p_{Ti} \rightarrow 0, \\ & p_{Tk}^g \rightarrow 0; & & p_{Tk}^g \rightarrow p_{Tk}^g - p_{Ti}. \end{aligned} \quad (6)$$

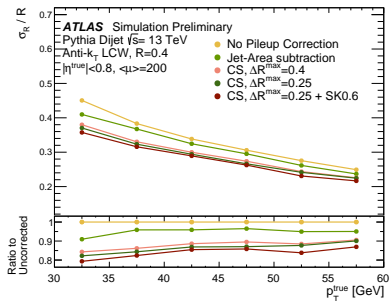
- 6 after the iterative process, discard all particles with zero transverse momentum.

CS performance in ATLAS and CMS (pp collisions)

- CMS performance CMS-PAS-JME-14-001
- ATLAS low p_T performance in ATLAS-CONF-2017-065
- ATLAS large- R jets performance in ATL-PHYS-PUB-2017-020
- Improved performance compared to the Area Subtraction



CMS-PAS-JME-14-001



ATLAS-CONF-2017-065

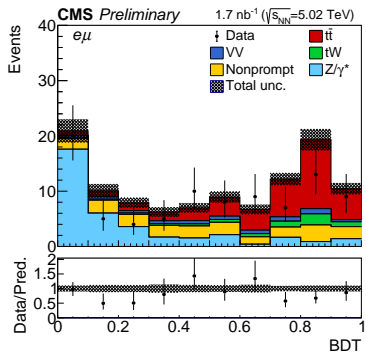
New developments - setup for performance studies

- Pythia8 simulation of signal and pileup events
- Number of pileup events, N_{PU} , is uniformly distributed in range $[0,120]$ (LHC Run 3)
- Particles grouped into massless towers of size 0.1×0.1 in $y - \phi$ space
- CS correction of whole event up to $|\eta| < 5$
- Using CS parameter $\alpha = 0$
- Using ρ rescaling (rapidity dependence)
- Figures of merit:

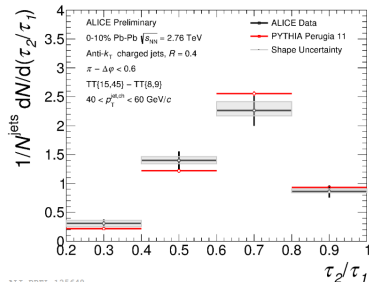
- Bias = $\frac{\langle x - x^{\text{true}} \rangle}{\langle x^{\text{true}} \rangle}$ - **the closer to zero, the better**

- Resolution = $\frac{\text{RMS}(x - x^{\text{true}})}{\langle x^{\text{true}} \rangle}$ - **the smaller, the better**

Physics results with Constituent Subtraction



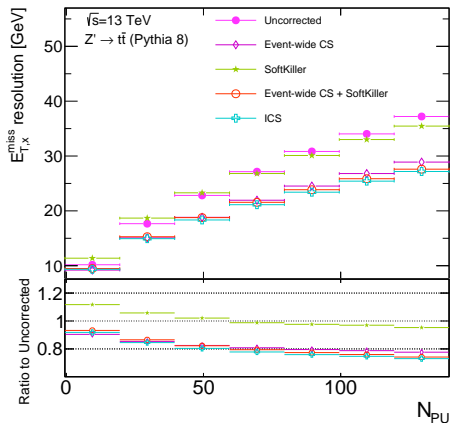
Evidence for top quark production in heavy-ion collisions,
CMS-PAS-HIN-19-001



Measurement of jet substructure variable τ_{21} in heavy-ion collisions ,
[arXiv:1705.03383](https://arxiv.org/abs/1705.03383)

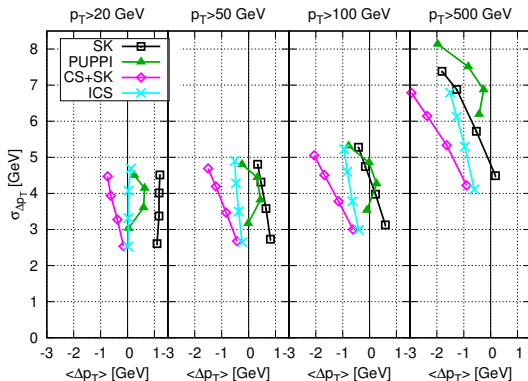
- Heavy-ion community extensively uses Constituent Subtraction for physics results

ICS - missing transverse energy



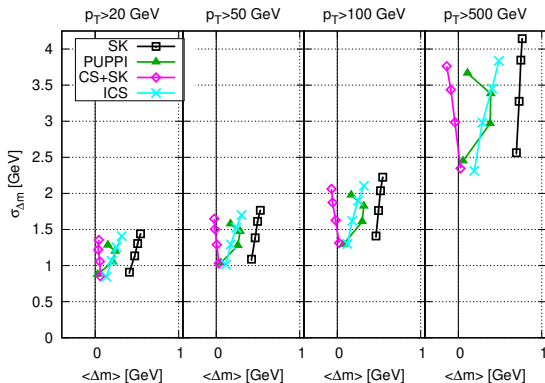
- ICS improves MET resolution

ICS - Comparison with other methods



- Using framework from [Pileup workshop in 2014](#)
- Jet p_T resolution vs jet p_T bias
- Each panel corresponds to dijet sample with certain jet p_T threshold
- The 4 points on each curve correspond to $N_{PU} = 30, 60, 100$ and 140 from bottom to top
- ICS brings improved resolution while keeping the bias low

ICS - Comparison with other methods



- Using framework from [Pileup workshop in 2014](#)
- Jet mass resolution vs jet mass bias
- Each panel corresponds to dijet sample with certain jet p_T threshold
- The 4 points on each curve correspond to $N_{PU} = 30, 60, 100$ and 140 from bottom to top
- ICS brings improved resolution while keeping the bias low