

# Searching for odderon exchange in exclusive $pp \rightarrow pp\phi$ and $pp \rightarrow pp\phi\phi$ reactions at the LHC

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# Searching for odderon ( $C = -1$ partner of pomeron)

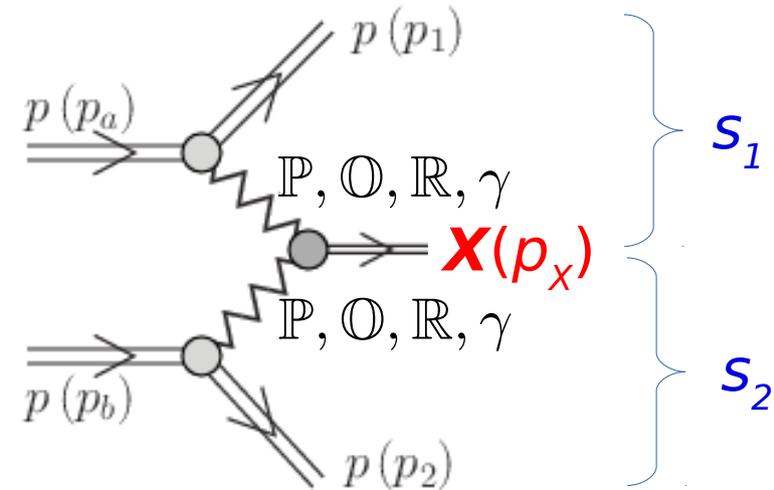
- First introduced in the framework of asymptotic theories  
L. Łukaszuk and B. Nicolescu, Lett. Nuovo Cim. 8 (1973) 405
- Predicted in QCD as a colourless 3-gluon bound state exchange  
J. Kwieciński, M. Praszalowicz, PLB94 (1980) 413  
J. Bartels, Nucl. Phys. B175 (1980) 365  
J. Bartels, L. N. Lipatov, G. P. Vacca, PLB477 (2000) 178
- A hint of the odderon was seen in ISR results (PRL54 (1985) 2180) as a very significant difference between the differential cross sections of elastic  $pp$  and  $p\bar{p}$  scattering in the diffractive dip region at  $\sqrt{s} = 53$  GeV (but non-negligible contribution from reggeons !)
- The D0 observation of a very shallow dip in  $p\bar{p}$  (at 1.96 TeV) (PRD86 (2012) 012009) compared to very pronounced dip measured by TOTEM (at 2.76, 7, and 13 TeV) for  $pp$  elastic scattering (TOTEM Coll., EPJC79 (2019) 785, EPJC80 (2020) 91)  
→ provides evidence for the odderon exchange **see C. Royon talk**
- It is of great importance to study possible odderon effects in other reactions than  $pp$  elastic scattering:
  - central  $J/\Psi$  production in high-energy  $pp$  and  $p\bar{p}$  collisions  
Schafer, Mankiewicz, Nachtmann, PLB272 (1991) 419  
Bzdak et al. PRD75 (2007) 094023
  - photoproduction of  $f_2(1270)$  and  $a_2(1320)$ , exclusive neutral pseudoscalar mesons  
Berger, Donnachie, Dosch, Nachtmann, EPJC14 (2000) 673
  - photoproduction and electroproduction of heavy  $C = +1$  quarkonia
  - observation of charge asymmetry in the  $\pi^+ \pi^-$  production  
Ginzburg, Ivanov, Nikolaev, EPJC5 (2003) 02
  - ultraperipheral proton-ion and ion-ion collisions  
Harland-Lang et al., PRD99 (2019) 034011  
Goncalves et al., EPJC79 (2019) 408  
McNulty et al., arXiv:2002.05031
- Nice review on odderon physics: C. Ewerz, arXiv: 0306137

# Central Exclusive Production (CEP)

in proton-proton collisions at high energies

$$p(p_a) + p(p_b) \rightarrow p(p_1) + \mathbf{X}(p_x) + p(p_2)$$

We require large rapidity gaps between  $p(p_1)$  and  $\mathbf{X}$ ,  $p(p_2)$  and  $\mathbf{X}$ .



Exchange objects:

- $\mathbb{P}$  (C = +1) pomeron, should dominate for large  $s_1, s_2$
- $\mathbb{O}$  (C = -1) odderon
- $\mathbb{R}$  :  $f_{2\mathbb{R}}, a_{2\mathbb{R}}$  (C = +1)  
 $\omega_{\mathbb{R}}, \rho_{\mathbb{R}}$  (C = -1) } reggeons
- $\gamma$  (C = -1) photon

I hope to show you that CEP offers possibilities to study odderon effects.

In my talk I shall consider the exclusive processes:

$$p p \rightarrow p p (\phi \rightarrow K^+ K^-)$$

$$p p \rightarrow p p (\phi \rightarrow \mu^+ \mu^-)$$

$$p p \rightarrow p p K^+ K^- K^+ K^- \text{ (via intermediate } \phi\phi \text{ state)}$$

# Model for soft high-energy scattering: Tensor pomeron and vector odderon

C. Ewerz, M. Maniatis, O. Nachtmann, *Ann. Phys.* 342 (2014) 31

- The main feature of the model is that the pomeron exchange ( $C = +1$ ) is described as effective spin 2 exchange (symmetric rank 2 tensor):

$$i\Delta_{\mu\nu,\kappa\lambda}^{(\mathbb{P})}(s, t) = \frac{1}{4s} \left( g_{\mu\kappa}g_{\nu\lambda} + g_{\mu\lambda}g_{\nu\kappa} - \frac{1}{2}g_{\mu\nu}g_{\kappa\lambda} \right) (-is\alpha'_{\mathbb{P}})^{\alpha_{\mathbb{P}}(t)-1}$$

$$\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}}t, \quad \alpha_{\mathbb{P}}(0) = 1.0808, \quad \alpha'_{\mathbb{P}} = 0.25 \text{ GeV}^{-2}$$

$$i\Gamma_{\mu\nu}^{(\mathbb{P}pp)}(p', p) = -i3\beta_{\mathbb{P}NN}F_1((p' - p)^2) \left\{ \frac{1}{2}[\gamma_{\mu}(p' + p)_{\nu} + \gamma_{\nu}(p' + p)_{\mu}] - \frac{1}{4}g_{\mu\nu}(p' + p) \right\}$$

$$\beta_{\mathbb{P}NN} = 1.87 \text{ GeV}^{-1}$$

- The odderon exchange ( $C = -1$ ) is described as effective vector exchange:

$$i\Delta_{\mu\nu}^{(\mathbb{O})}(s, t) = -ig_{\mu\nu} \frac{\eta_{\mathbb{O}}}{M_0^2} (-is\alpha'_{\mathbb{O}})^{\alpha_{\mathbb{O}}(t)-1}$$

$$i\Gamma_{\mu}^{(\mathbb{O}pp)}(p', p) = -i3\beta_{\mathbb{O}pp} M_0 F_1((p' - p)^2) \gamma_{\mu}$$

where  $\eta_{\mathbb{O}}$  is a parameter with value  $\eta_{\mathbb{O}} = \pm 1$ ;  $M_0 = 1 \text{ GeV}$  is inserted for dimensional reasons;  $\alpha_{\mathbb{O}}(t)$  is the odderon trajectory  $\alpha_{\mathbb{O}}(t) = \alpha_{\mathbb{O}}(0) + \alpha'_{\mathbb{O}}t$

- We take 
$$F_1(t) = \frac{4m_p^2 - 2.79t}{(4m_p^2 - t)(1 - t/m_D^2)^2}, \quad m_D^2 = 0.71 \text{ GeV}^2$$

# Applications

$\gamma p \rightarrow \pi^+ \pi^- p$  *Bolz, Ewerz, Maniatis, Nachtmann, Sauter, Schöning, JHEP 01 (2015) 151*

There will be interference between  $\gamma p \rightarrow (\rho^0 \rightarrow \pi^+ \pi^-) p$  (IP exchange)

and  $\gamma p \rightarrow (f_2(1270) \rightarrow \pi^+ \pi^-) p$  (O exchange) processes and as a consequence  $\pi^+ \pi^-$  charge asymmetries.

## Photoproduction and low x DIS

*Britzger, Ewerz, Glazov, Nachtmann, Schmitt, PRD100 (2019) 114007*

A “vector pomeron” cannot couple in the total photoabsorption cross section  $\sigma_{\gamma p}$ .

## Helicity in proton-proton elastic scattering and the spin structure of the pomeron

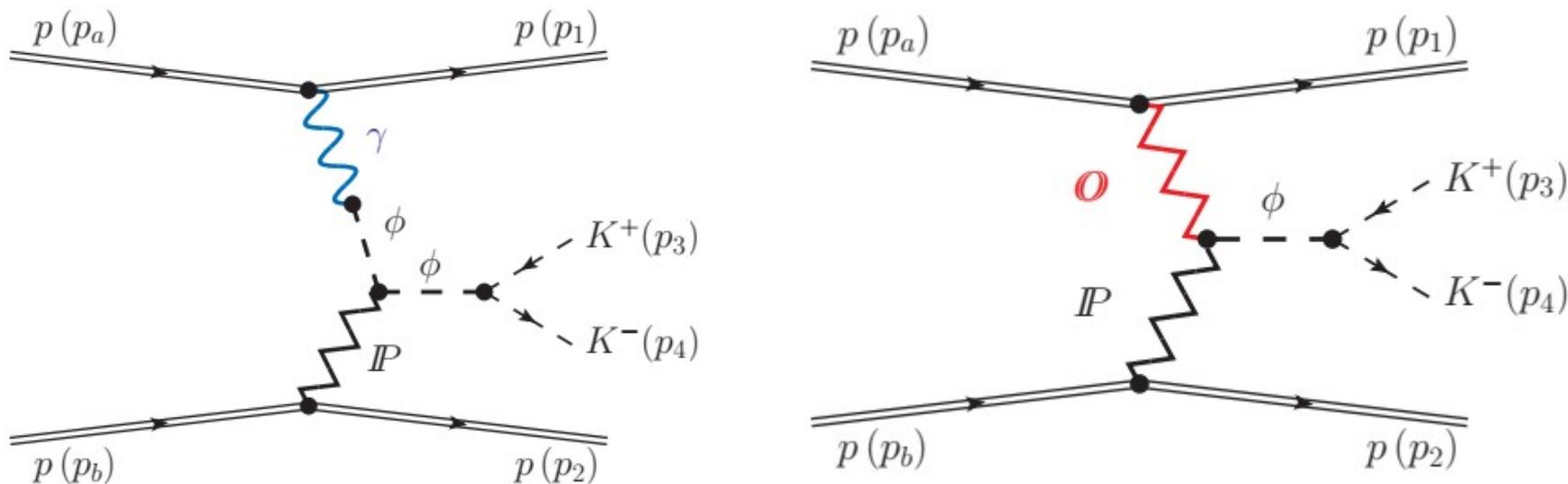
*Ewerz, P.L., Nachtmann, Szczurek, PLB 763 (2016) 382*

Studying the ratio  $r_5$  of single-helicity-flip to non-flip amplitudes we found that the STAR data [L. Adamczyk *et al.*, PLB 719 (2013) 62] are consistent with the tensor pomeron model while they clearly exclude a scalar pomeron. Vector pomeron is in contradiction to the rules of QFT.

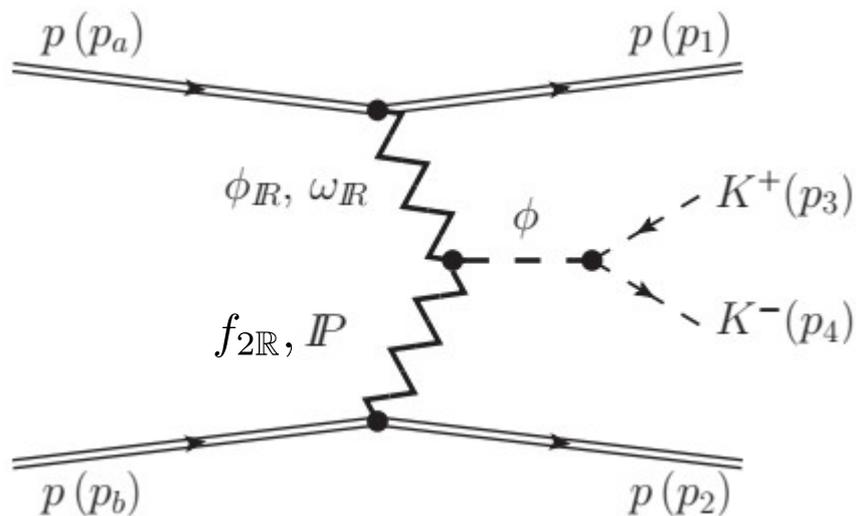
## CEP, $p p \rightarrow p p$ **X**, *P.L., Nachtmann, Szczurek*:

<b>X</b> : $\eta, \eta', f_0$	<i>Ann. Phys. 344 (2014) 301</i>
$\rho^0$	<i>PRD91 (2015) 074023</i>
$\pi^+ \pi^-, f_0, f_2$	<i>PRD93 (2016) 054015</i>
$\pi^+ \pi^- \pi^+ \pi^-, \rho^0 \rho^0$	<i>PRD94 (2016) 034017</i>
$\rho^0$ with proton diss.	<i>PRD95 (2017) 034036</i>
$p\bar{p}$	<i>PRD97 (2018) 094027</i>
$K^+ K^-$	<i>PRD98 (2018) 014001</i>
$K^+ K^- K^+ K^-, \phi\phi$	<i>PRD99 (2019) 094034</i> ← <b>this talk</b>
$f_2 \rightarrow \pi^+ \pi^-$	<i>PRD101 (2020) 034008</i>
$\phi \rightarrow K^+ K^-, \mu^+ \mu^-$	<i>PRD101 (2020) 094012</i> ← <b>this talk</b>
$f_1(1285), f_1(1420)$	← <b>see O. Nachtmann talk</b>

# The reaction $pp \rightarrow pp (\phi \rightarrow K^+ K^-)$



at high energies (LHC) we expect this reaction to be dominated by the processes



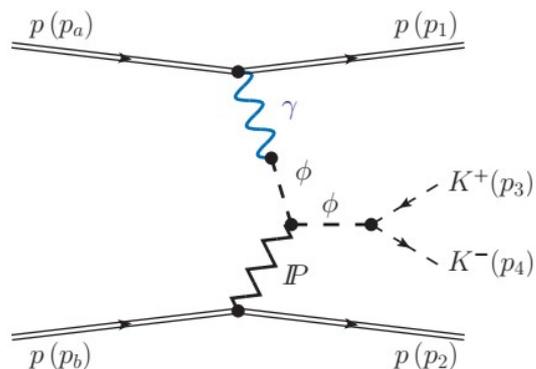
important at lower energies (WA102)

# Photon-pomeron fusion

- 2 → 4 exclusive reaction

$$p(p_a, \lambda_a) + p(p_b, \lambda_b) \rightarrow p(p_1, \lambda_1) + [\phi(p_{34}) \rightarrow K^+(p_3) + K^-(p_4)] + p(p_2, \lambda_2)$$

where  $p_{a,b}$ ,  $p_{1,2}$  and  $\lambda_{a,b}$ ,  $\lambda_{1,2} = \pm \frac{1}{2}$  denote the four-momenta and helicities of the protons and  $p_{3,4}$  denote the four-momenta of the  $K$  mesons, respectively



- Kinematic variables

$$p_{34} = p_3 + p_4, \quad q_1 = p_a - p_1, \quad q_2 = p_b - p_2,$$

$$s = (p_a + p_b)^2 = (p_1 + p_2 + p_{34})^2,$$

$$t_1 = q_1^2, \quad t_2 = q_2^2,$$

$$s_1 = (p_1 + p_{34})^2, \quad s_2 = (p_2 + p_{34})^2$$

- Born-level amplitude

$$\begin{aligned} \mathcal{M}_{pp \rightarrow pp K^+ K^-}^{(\gamma \mathbb{P})} &= (-i) \bar{u}(p_1, \lambda_1) i \Gamma_{\mu}^{(\gamma pp)}(p_1, p_a) u(p_a, \lambda_a) \\ &\quad \times i \Delta^{(\gamma) \mu \sigma}(q_1) i \Gamma_{\sigma \nu}^{(\gamma \rightarrow \phi)}(q_1) i \Delta^{(\phi) \nu \rho_1}(q_1) i \Gamma_{\rho_2 \rho_1 \alpha \beta}^{(\mathbb{P} \phi \phi)}(p_{34}, q_1) i \Delta^{(\phi) \rho_2 \kappa}(p_{34}) i \Gamma_{\kappa}^{(\phi K K)}(p_3, p_4) \\ &\quad \times i \Delta^{(\mathbb{P}) \alpha \beta, \delta \eta}(s_2, t_2) \bar{u}(p_2, \lambda_2) i \Gamma_{\delta \eta}^{(\mathbb{P} pp)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

Model is formulated in terms of effective propagators and vertices.

The vertices are derived from Lagrangians for the couplings.

Inclusion of photons is straightforward and gauge invariance is guaranteed.

The Regge factors are incorporated in the effective propagators.

- Effective propagator and proton vertex function for the tensor pomeron

$$i\Delta_{\mu\nu,\kappa\lambda}^{(\mathbb{P})}(s, t) = \frac{1}{4s} \left( g_{\mu\kappa}g_{\nu\lambda} + g_{\mu\lambda}g_{\nu\kappa} - \frac{1}{2}g_{\mu\nu}g_{\kappa\lambda} \right) (-is\alpha'_{\mathbb{P}})^{\alpha_{\mathbb{P}}(t)-1}$$

$$i\Gamma_{\mu\nu}^{(\mathbb{P}pp)}(p', p) = -i3\beta_{\mathbb{P}NN}F_1(t) \left\{ \frac{1}{2} [\gamma_{\mu}(p' + p)_{\nu} + \gamma_{\nu}(p' + p)_{\mu}] - \frac{1}{4}g_{\mu\nu}(p' + p) \right\}$$

where  $\beta_{\mathbb{P}NN} = 1.87 \text{ GeV}^{-1}$

$$\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}}t$$

$$\alpha_{\mathbb{P}}(0) = 1.0808, \quad \alpha'_{\mathbb{P}} = 0.25 \text{ GeV}^{-2}$$

- For the  $\mathbb{P}\phi\phi$  vertex we have (in analogy to  $f_2\gamma\gamma$  vertex)

$$i\Gamma_{\mu\nu\kappa\lambda}^{(\mathbb{P}\phi\phi)}(k', k) = iF_M((k' - k)^2) \left[ 2a_{\mathbb{P}\phi\phi} \Gamma_{\mu\nu\kappa\lambda}^{(0)}(k', -k) - b_{\mathbb{P}\phi\phi} \Gamma_{\mu\nu\kappa\lambda}^{(2)}(k', -k) \right]$$

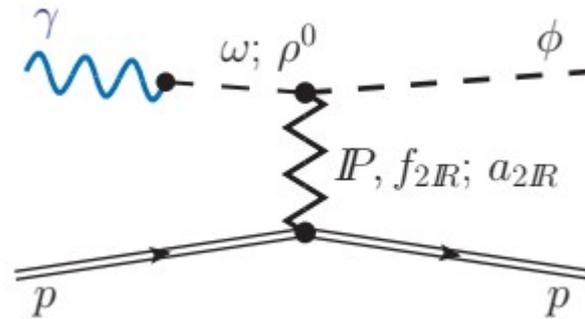
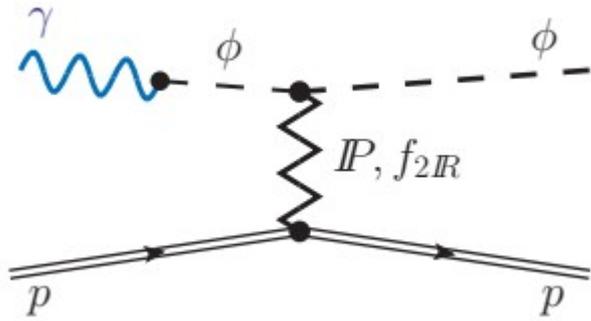
$$\Gamma_{\mu\nu\kappa\lambda}^{(0)}(k_1, k_2) = \left[ (k_1 \cdot k_2)g_{\mu\nu} - k_{2\mu}k_{1\nu} \right] \left[ k_{1\kappa}k_{2\lambda} + k_{2\kappa}k_{1\lambda} - \frac{1}{2}(k_1 \cdot k_2)g_{\kappa\lambda} \right]$$

$$\begin{aligned} \Gamma_{\mu\nu\kappa\lambda}^{(2)}(k_1, k_2) = & (k_1 \cdot k_2)(g_{\mu\kappa}g_{\nu\lambda} + g_{\mu\lambda}g_{\nu\kappa}) + g_{\mu\nu}(k_{1\kappa}k_{2\lambda} + k_{2\kappa}k_{1\lambda}) \\ & - k_{1\nu}k_{2\lambda}g_{\mu\kappa} - k_{1\nu}k_{2\kappa}g_{\mu\lambda} - k_{2\mu}k_{1\lambda}g_{\nu\kappa} - k_{2\mu}k_{1\kappa}g_{\nu\lambda} \\ & - [(k_1 \cdot k_2)g_{\mu\nu} - k_{2\mu}k_{1\nu}]g_{\kappa\lambda} \end{aligned}$$

C. Ewerz, M. Maniatis, O. Nachtmann,  
Ann. Phys. 342 (2014) 31

The coupling parameters  $a_{\mathbb{P}\phi\phi}$ ,  $b_{\mathbb{P}\phi\phi}$  and the cut-off parameter  $\Lambda_{0,\mathbb{P}\phi\phi}^2$  in  $F_M(t) = \frac{1}{1-t/\Lambda_{0,\mathbb{P}\phi\phi}^2}$  are fixed from the process  $\gamma p \rightarrow \phi p$ .

• Photoproduction process

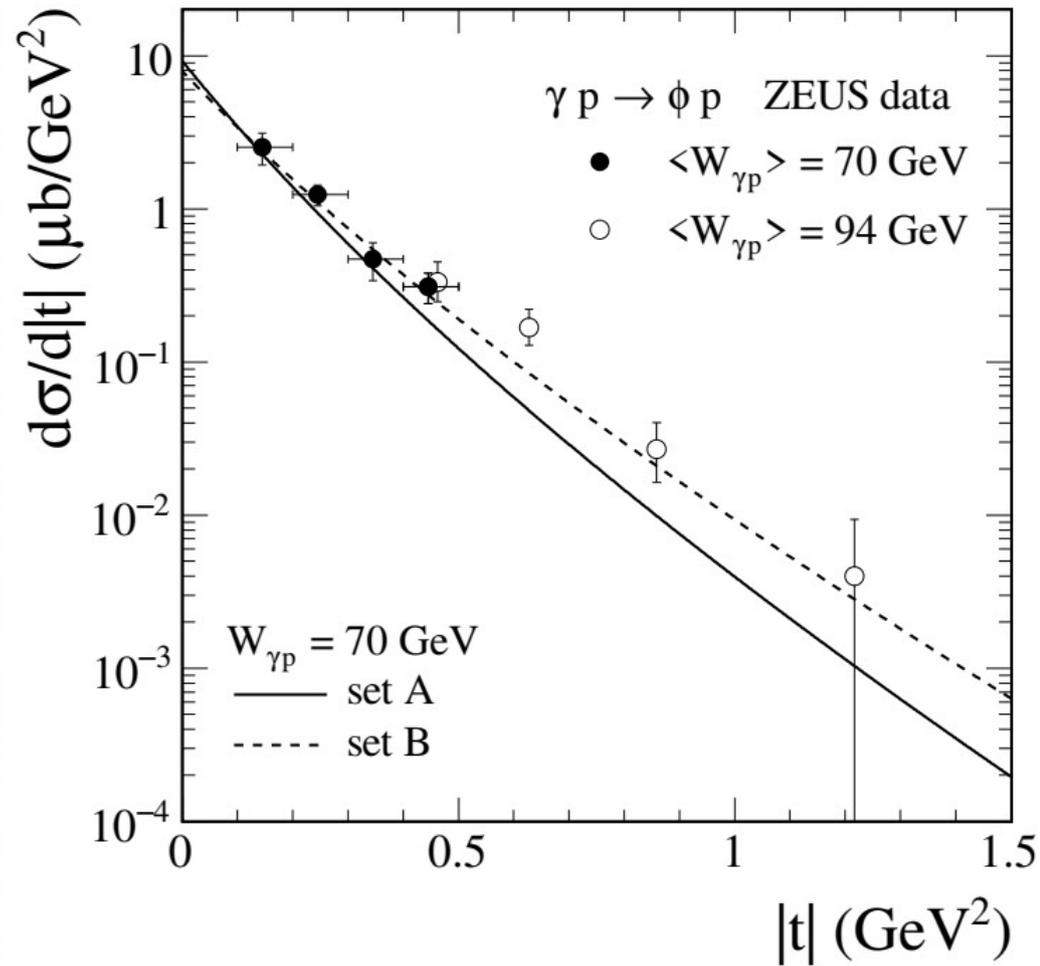
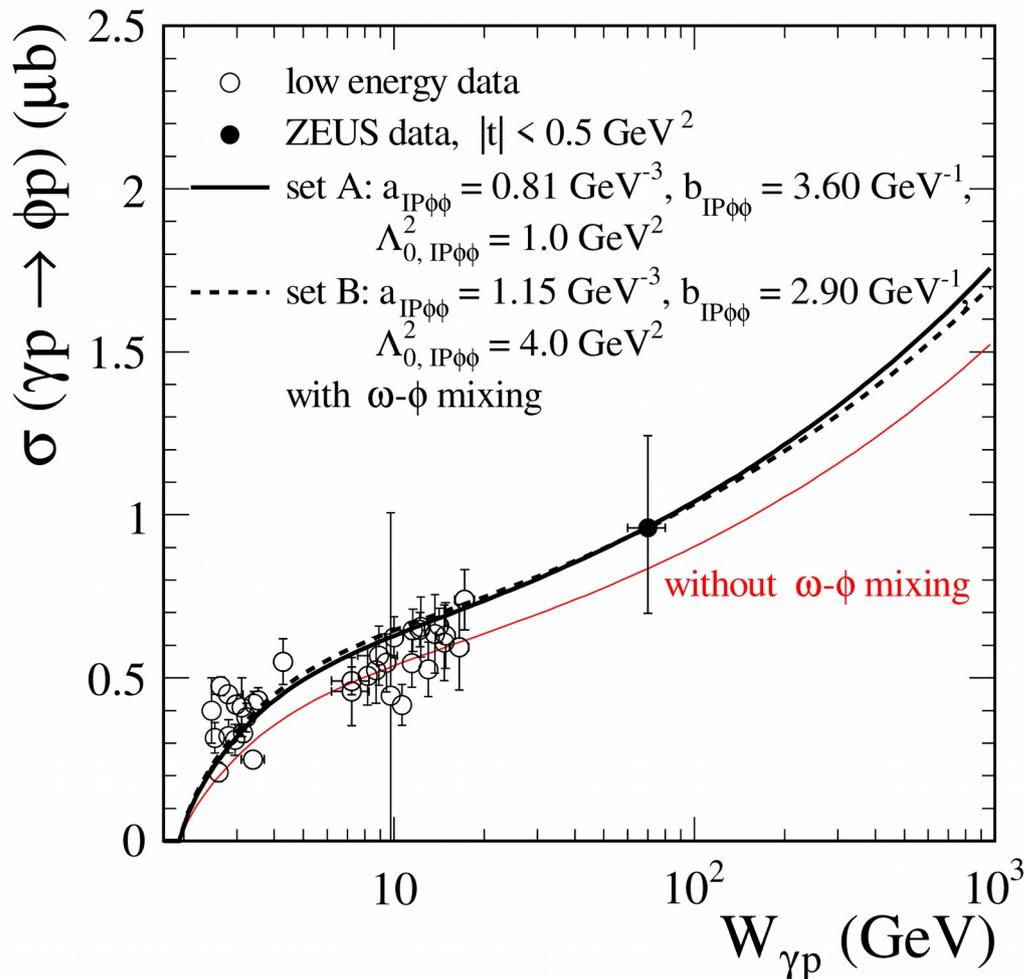


$\omega$ - $\phi$  mixing effect included

$$b_{\mathbb{P}\omega\phi} = -b_{\mathbb{P}\omega\omega} \tan(\Delta\theta_V)$$

$$b_{\mathbb{P}\omega\omega} = 7.04 \text{ GeV}^{-1}$$

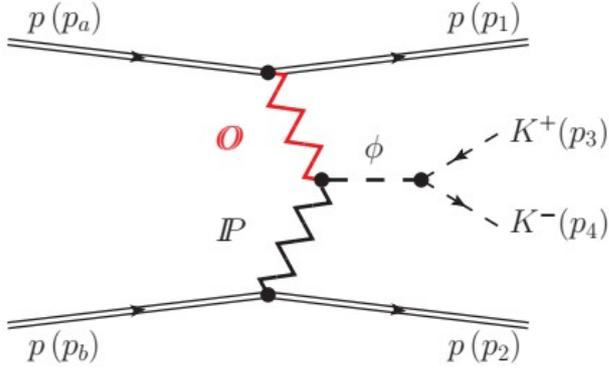
$$\Delta\theta_V = 3.7^\circ$$



# Odderon-pomeron fusion

Born-level amplitude:

$$\begin{aligned} \mathcal{M}_{pp \rightarrow pp K^+ K^-}^{(\odot \mathbb{P})} &= (-i) \bar{u}(p_1, \lambda_1) i\Gamma_{\mu}^{(\odot pp)}(p_1, p_a) u(p_a, \lambda_a) \\ &\times i\Delta^{(\odot) \mu\rho_1}(s_1, t_1) i\Gamma_{\rho_1\rho_2\alpha\beta}^{(\mathbb{P}\odot\phi)}(-q_1, p_{34}) i\Delta^{(\phi) \rho_2\kappa}(p_{34}) i\Gamma_{\kappa}^{(\phi KK)}(p_3, p_4) \\ &\times i\Delta^{(\mathbb{P}) \alpha\beta, \delta\eta}(s_2, t_2) \bar{u}(p_2, \lambda_2) i\Gamma_{\delta\eta}^{(\mathbb{P}pp)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$



Effective propagator of  $C = -1$  odderon and the  $O\phi\phi$  vertex

$$i\Delta_{\mu\nu}^{(\odot)}(s, t) = -ig_{\mu\nu} \frac{\eta_{\odot}}{M_0^2} (-is\alpha'_{\odot})^{\alpha_{\odot}(t)-1}$$

$$i\Gamma_{\mu}^{(\odot pp)}(p', p) = -i3\beta_{\odot pp} M_0 F_1((p' - p)^2) \gamma_{\mu}$$

In our calculations we shall choose as default values:

$$\alpha_{\odot}(0) = 1.05, \quad \alpha'_{\odot} = 0.25 \text{ GeV}^{-2}, \quad \eta_{\odot} = -1$$

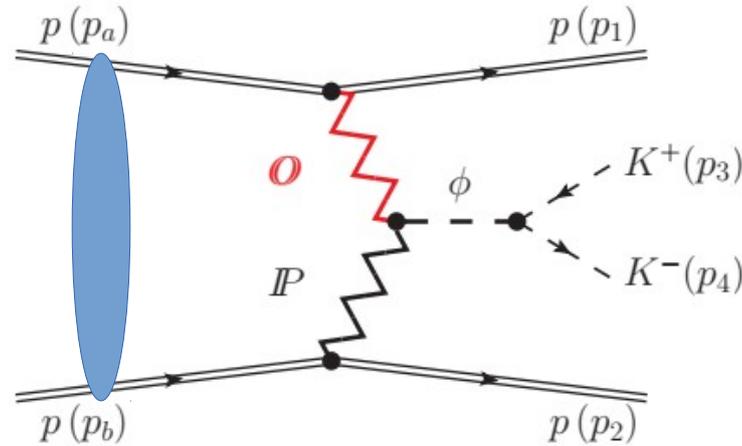
$$\beta_{\odot pp} = 0.1 \times \beta_{\mathbb{P}NN} \simeq 0.18 \text{ GeV}^{-1}$$

For the  $\mathbb{P}\odot\phi$  vertex we use an ansatz analogous to the  $\mathbb{P}\phi\phi$  vertex:

$$\begin{aligned} i\Gamma_{\rho_1\rho_2\alpha\beta}^{(\mathbb{P}\odot\phi)}(-q_1, p_{34}) &= i \left[ 2 a_{\mathbb{P}\odot\phi} \Gamma_{\rho_2\rho_1\alpha\beta}^{(0)}(p_{34}, -q_1) - b_{\mathbb{P}\odot\phi} \Gamma_{\rho_2\rho_1\alpha\beta}^{(2)}(p_{34}, -q_1) \right] \\ &\times F_M(q_2^2) F_M(q_1^2) F^{(\phi)}(p_{34}^2) \end{aligned}$$

The coupling parameters  $a_{\mathbb{P}\odot\phi}$ ,  $b_{\mathbb{P}\odot\phi}$  and the cut-off parameter  $\Lambda_{0, \mathbb{P}\odot\phi}^2$  in  $F_M(t) = \frac{1}{1-t/\Lambda_{0, \mathbb{P}\odot\phi}^2}$  could be adjusted to experimental data.

# Absorption effects



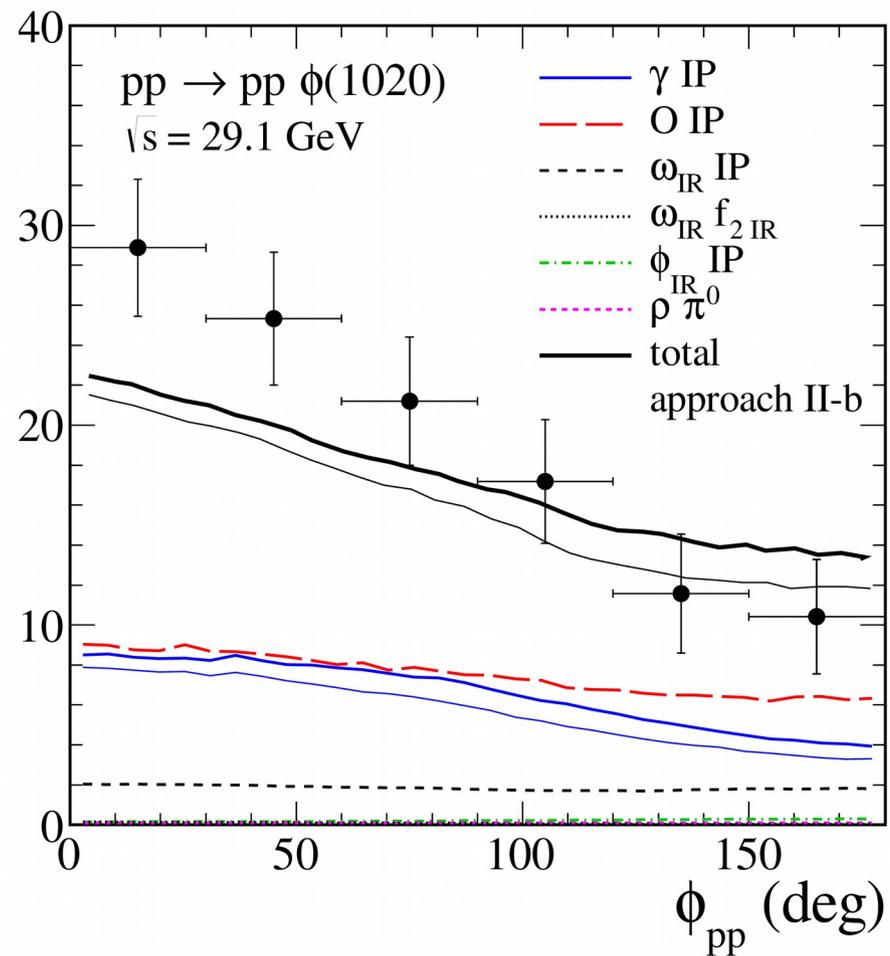
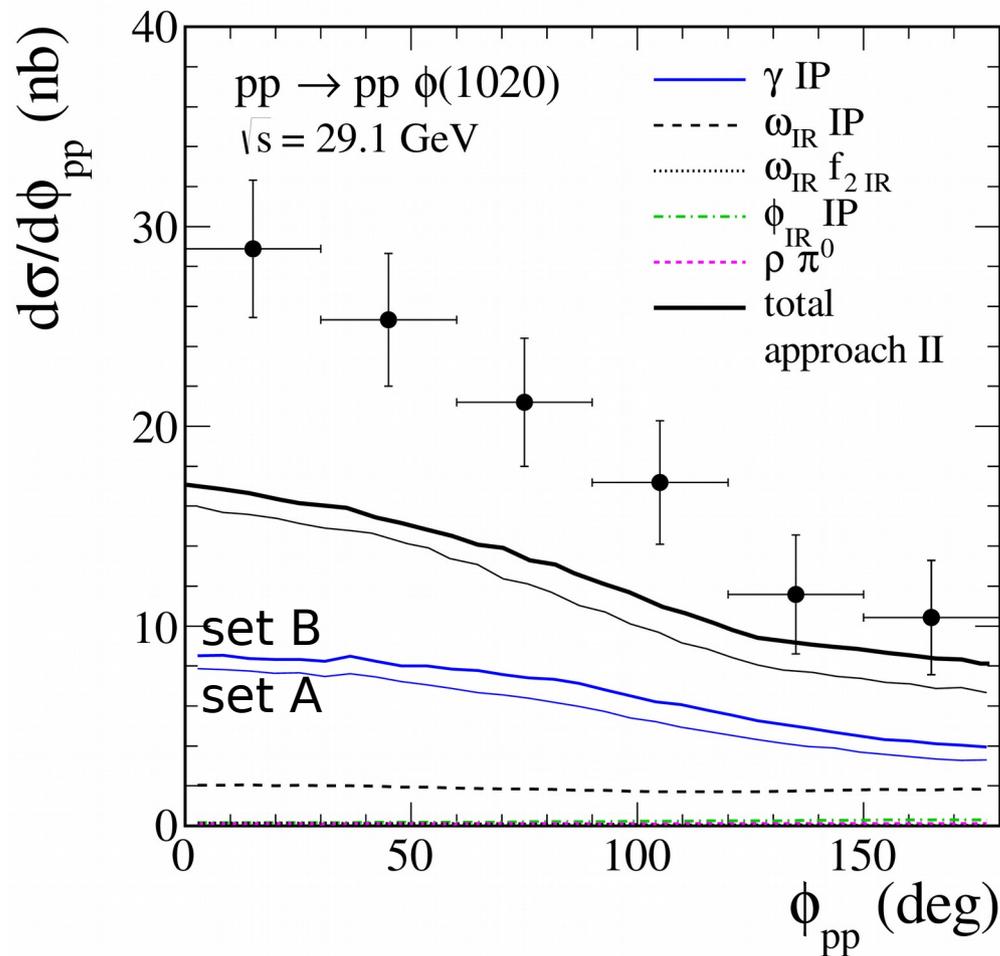
$$\mathcal{M} = \mathcal{M}^{Born} + \mathcal{M}^{pp-rescattering}$$

$$\mathcal{M}^{pp-rescattering}(s, \vec{p}_{1\perp}, \vec{p}_{2\perp}) = \frac{i}{8\pi^2 s} \int d^2 \vec{k}_{\perp} \mathcal{M}^{Born}(s, \vec{p}_{1\perp} - \vec{k}_{\perp}, \vec{p}_{2\perp} + \vec{k}_{\perp}) \mathcal{M}_{pp \rightarrow pp}^{IP-exch.}(s, -\vec{k}_{\perp}^2)$$

here  $\vec{k}_{\perp}$  is the transverse momentum carried around the loop

These corrections (called as soft survival factor,  $\langle S^2 \rangle$ ) plays a crucial role, reduce the value of cross section and change, e.g., the  $\phi_{pp}$  dependence

# Comparison with WA102 data

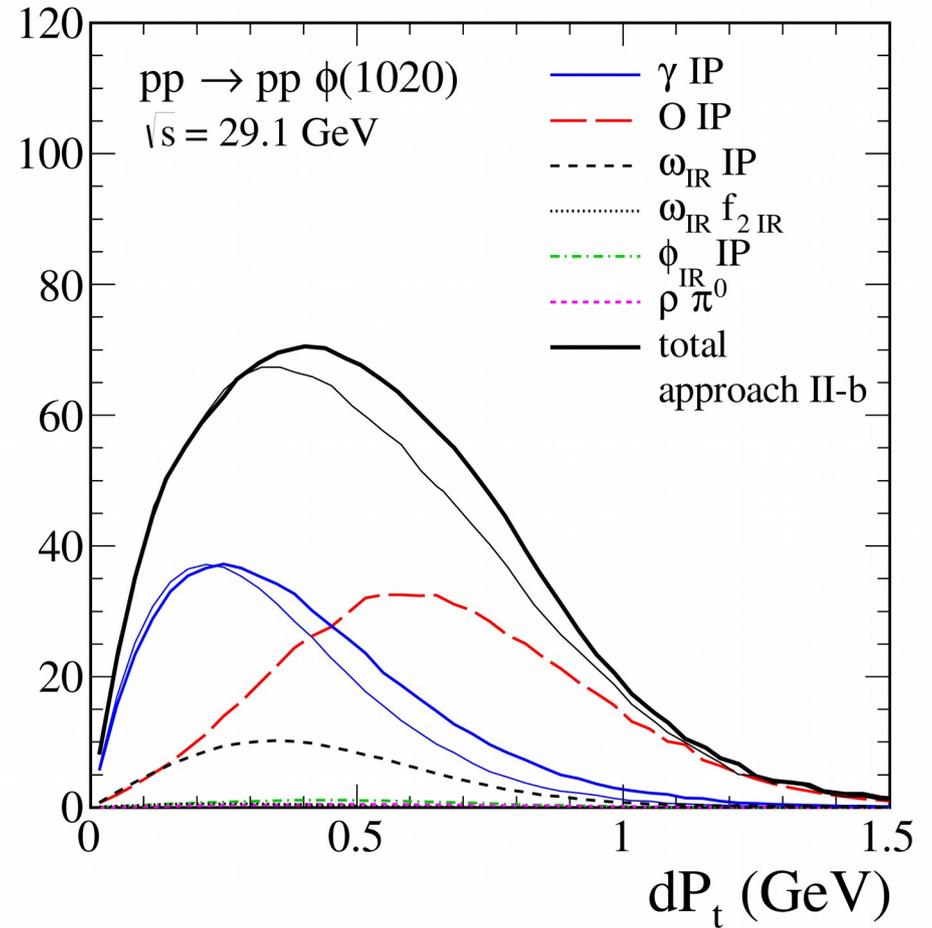
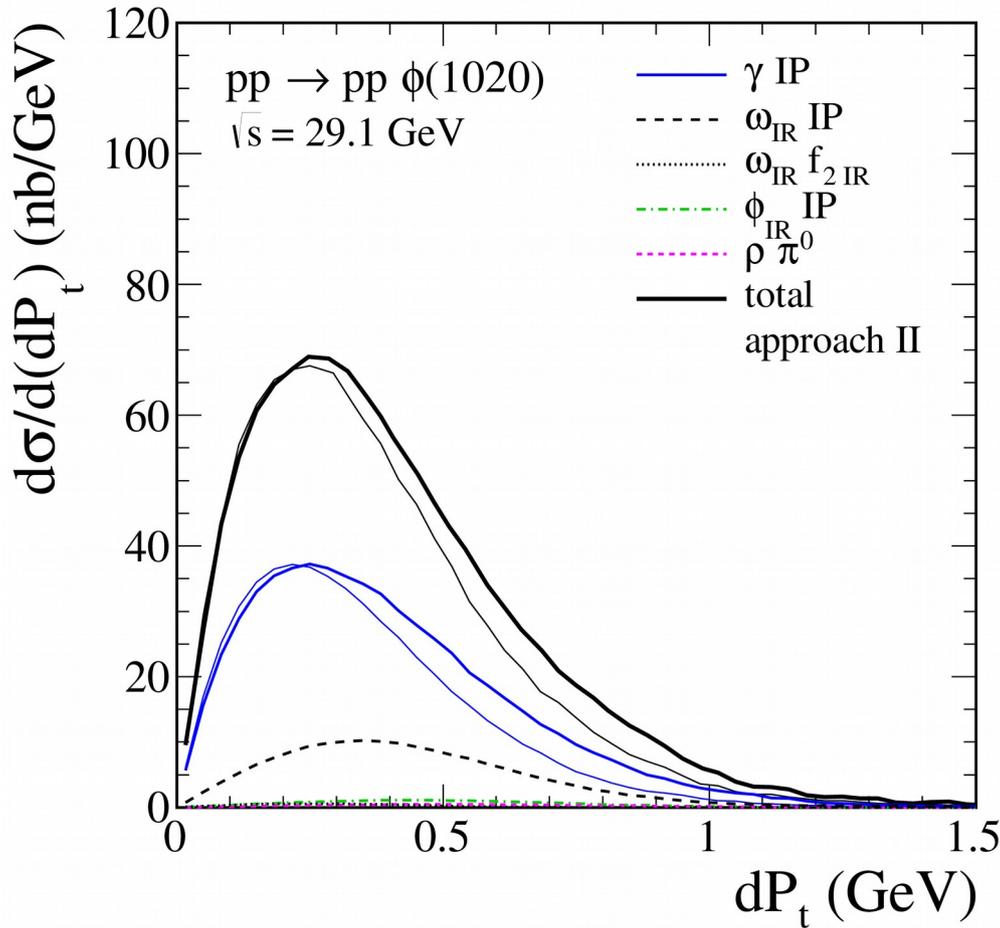


- WA102 data from [PLB489 \(2000\) 29](#),  $\sigma_{\text{exp.}} = (60 \pm 21) \text{ nb}$
- Different fusion processes were considered. Large interference effects. The  $\phi_{pp}$  distribution allow us to determine the respective coupling constants

$$a_{\text{PO}\phi} = -0.8 \text{ GeV}^{-3}, \quad b_{\text{PO}\phi} = 1.6 \text{ GeV}^{-1}, \quad \Lambda_{0,\text{PO}\phi}^2 = 0.5 \text{ GeV}^2$$

- We obtain the gap survival factor  $\langle S^2 \rangle = 0.8$  for the photoproduction term and  $\langle S^2 \rangle = 0.4$  for the hadronic diffractive terms

# Comparison with WA102 data



$$dP_t = |d\mathbf{P}_t|, \quad d\mathbf{P}_t = \mathbf{q}_{t,1} - \mathbf{q}_{t,2} = \mathbf{p}_{t,2} - \mathbf{p}_{t,1}$$

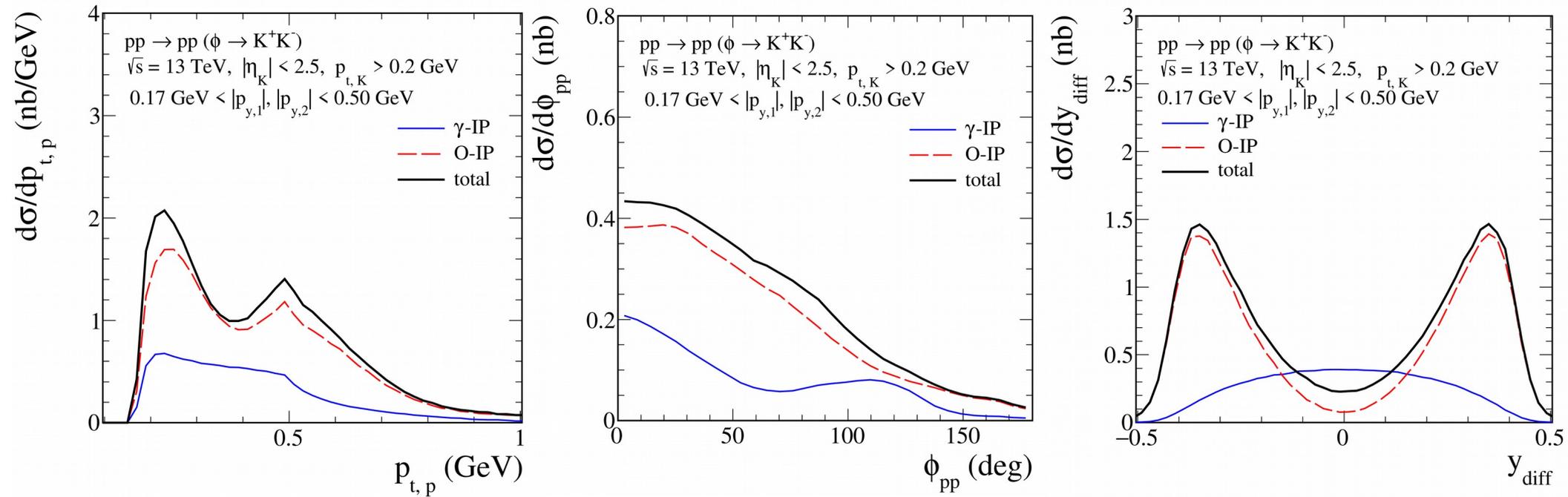
$$R = \frac{d\sigma/d(dP_t \leq 0.2 \text{ GeV})}{d\sigma/d(dP_t \geq 0.5 \text{ GeV})}$$

**WA102 experiment:**  $R_{\text{exp.}} = 0.18 \pm 0.07$

$R = 0.71$  (no odderon),  $R = 0.27$  (with odderon)

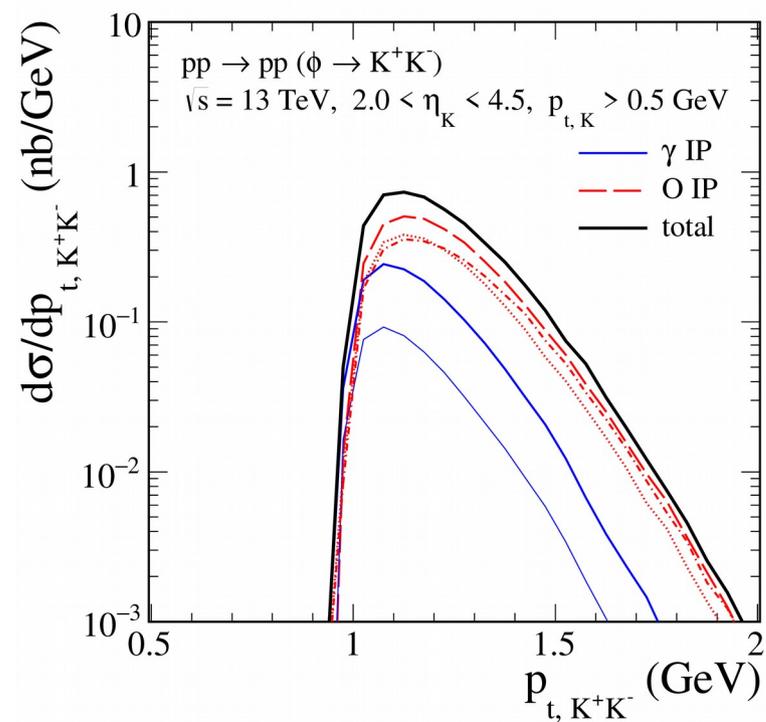
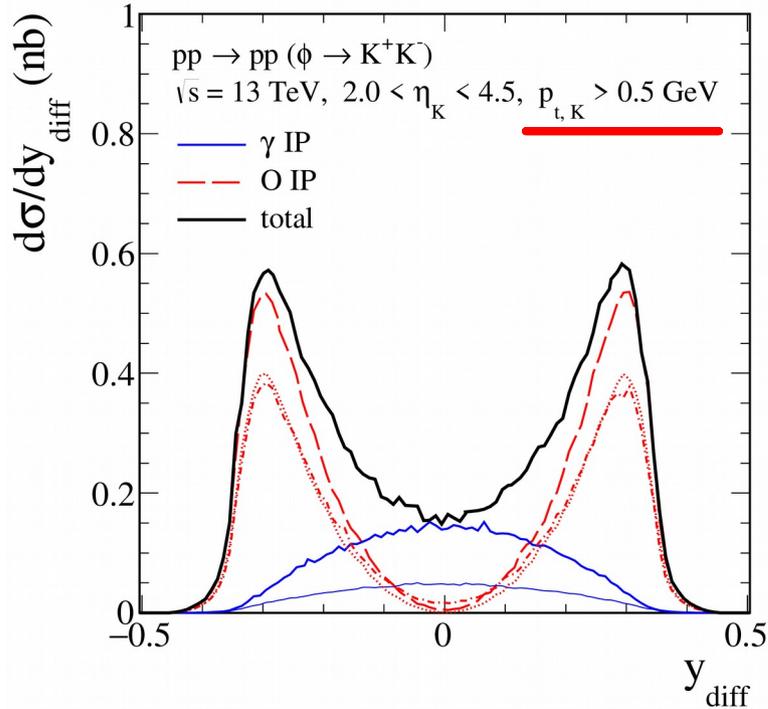
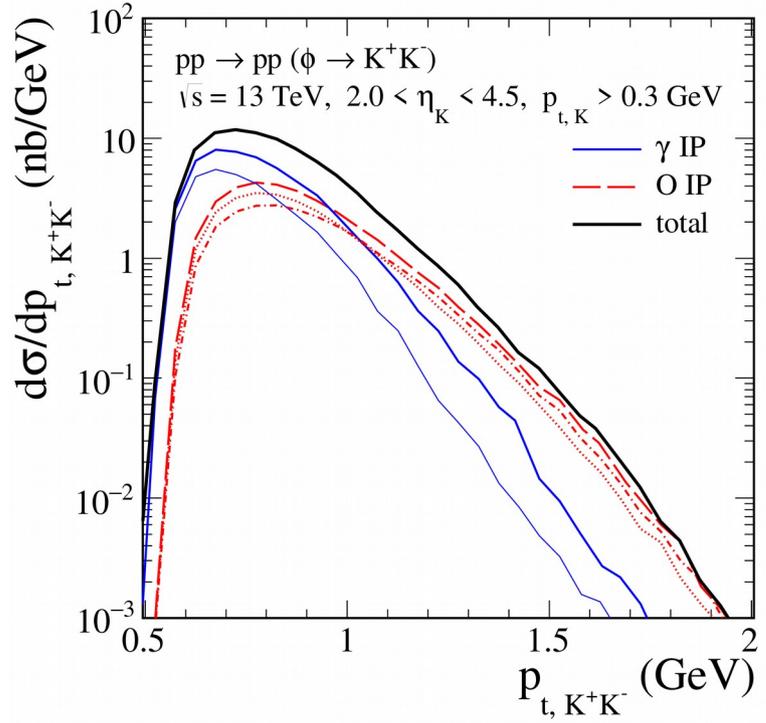
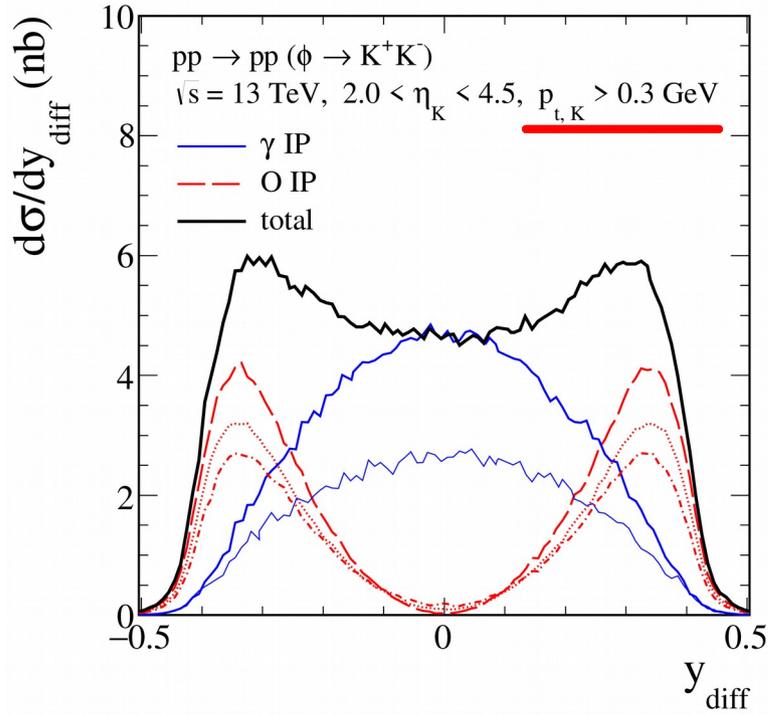
- We find that two couplings  $a_{\text{IPO}\phi}$  and  $b_{\text{IPO}\phi}$  are needed to describe  $\phi_{\text{pp}}$  and  $dP_t$
- The WA102 data support the existence of odderon exchange !
- It would be very useful to measure the outgoing protons at the LHC

# Predictions for the $pp \rightarrow pp K^+K^-$ reaction (ATLAS + ALFA)



- Different behaviour is seen for  $\gamma$ IP and OIP contributions.
- Due to the ALFA cuts on the leading protons the photoproduction term is strongly suppressed
- For the ATLAS-ALFA kinematics the absorption effects lead to a large damping of the cross section both for the purely diffractive and for the photoproduction mechanisms.
- This effect could be verified in experiments at the LHC (ATLAS-ALFA, CMS-TOTEM) when both protons are measured.
- For the OIP-fusion process the complete result indicates a large (destructive) interference effect of the two type of couplings, a and b, in the IPO  $\phi$  vertex  $\rightarrow$  minimum at  $y_{\text{diff}} = y_3 - y_4 = 0$

# Predictions for the $pp \rightarrow pp K^+K^-$ reaction (LHCb)

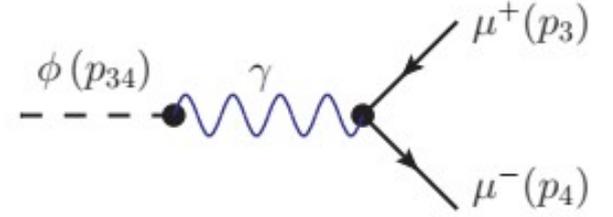


# The reaction $pp \rightarrow pp \mu^+ \mu^-$

The amplitudes for the  $pp \rightarrow pp \mu^+ \mu^-$  reaction through  $\phi$  resonance production can be obtained from the  $pp \rightarrow pp K^+ K^-$  amplitudes with  $i\Gamma_{\kappa}^{(\phi K K)}(p_3, p_4)$  replaced by  $\bar{u}(p_4, \lambda_4) i\Gamma_{\kappa}^{(\phi \mu \mu)}(p_3, p_4) v(p_3, \lambda_3)$ .

Here we describe the transition  $\phi \rightarrow \gamma \rightarrow \mu^+ \mu^-$  by an effective vertex:

$$i\Gamma_{\kappa}^{(\phi \mu \mu)}(p_3, p_4) = ig_{\phi \mu^+ \mu^-} \gamma_{\kappa}$$



The decay rate  $\phi \rightarrow \mu^+ \mu^-$  is calculated from the diagram

$$\Gamma(\phi \rightarrow \mu^+ \mu^-) = \frac{1}{12\pi} |g_{\phi \mu^+ \mu^-}|^2 m_{\phi} \left(1 + \frac{2m_{\mu}^2}{m_{\phi}^2}\right) \left(1 - \frac{4m_{\mu}^2}{m_{\phi}^2}\right)^{1/2}$$

From the experimental values (PDG)

$$m_{\phi} = (1019.461 \pm 0.016) \text{ MeV},$$

$$\Gamma(\phi \rightarrow \mu^+ \mu^-) / \Gamma_{\phi} = (2.86 \pm 0.19) \times 10^{-4},$$

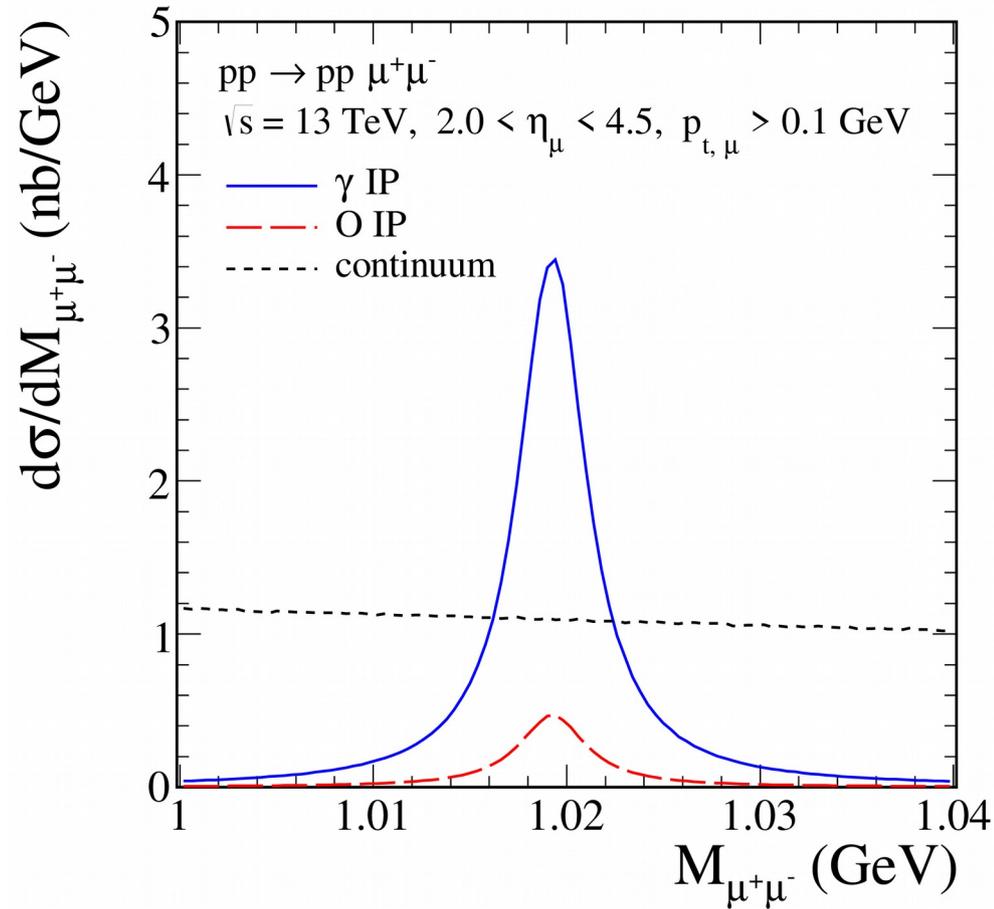
$$\Gamma_{\phi} = (4.249 \pm 0.013) \text{ MeV}$$

we get  $g_{\phi \mu^+ \mu^-} = (6.71 \pm 0.22) \times 10^{-3}$

Using VMD model we get  $g_{\phi \mu^+ \mu^-} = -e^2 \frac{1}{\gamma_{\phi}}, \quad \gamma_{\phi} < 0, \quad 4\pi/\gamma_{\phi}^2 = 0.0716 \pm 0.0017$

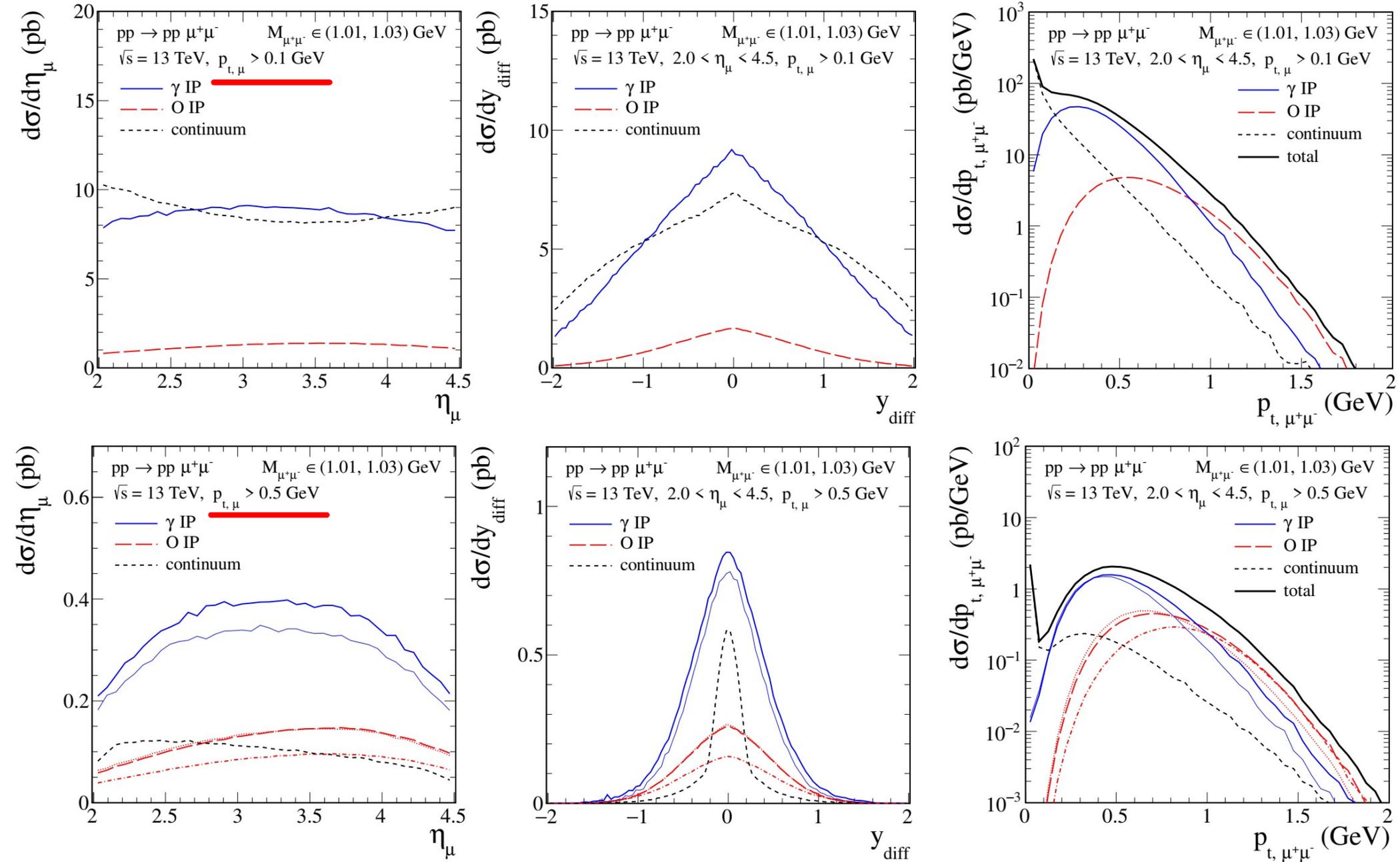
$$g_{\phi \mu^+ \mu^-} = (6.92 \pm 0.08) \times 10^{-3}$$

# Predictions for the $pp \rightarrow pp \mu^+\mu^-$ reaction (LHCb)



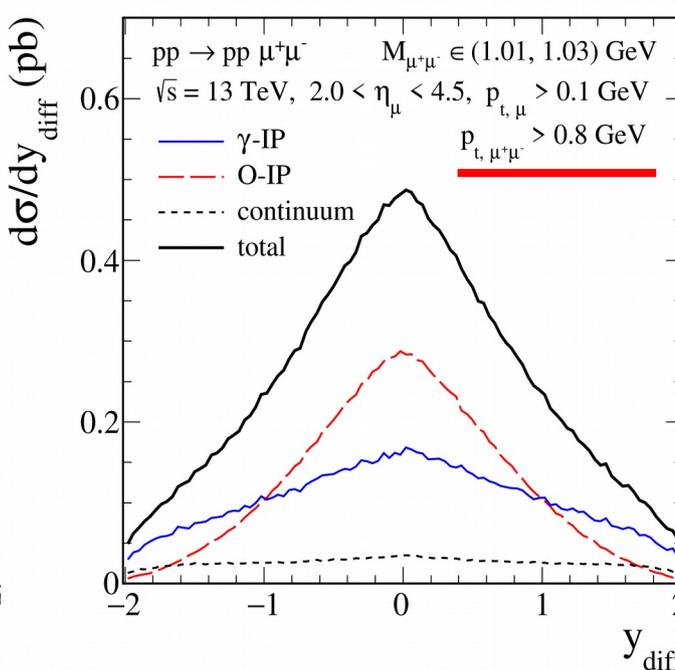
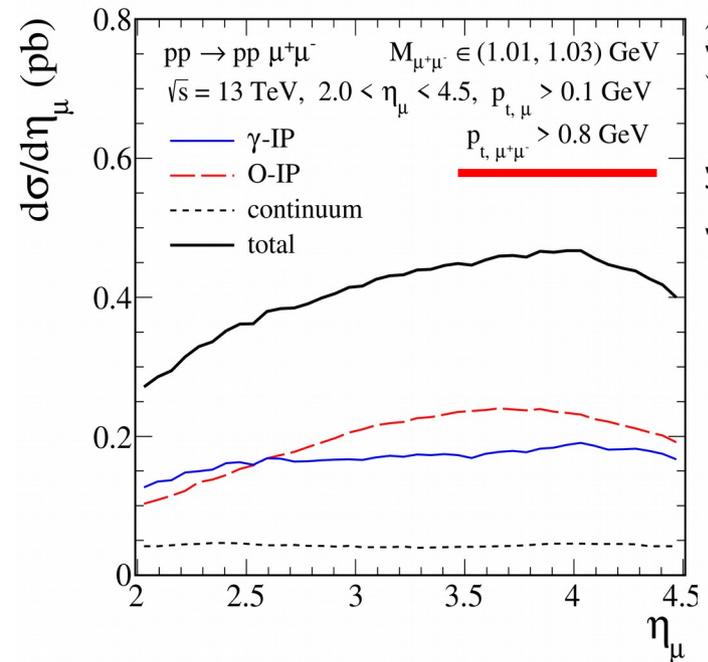
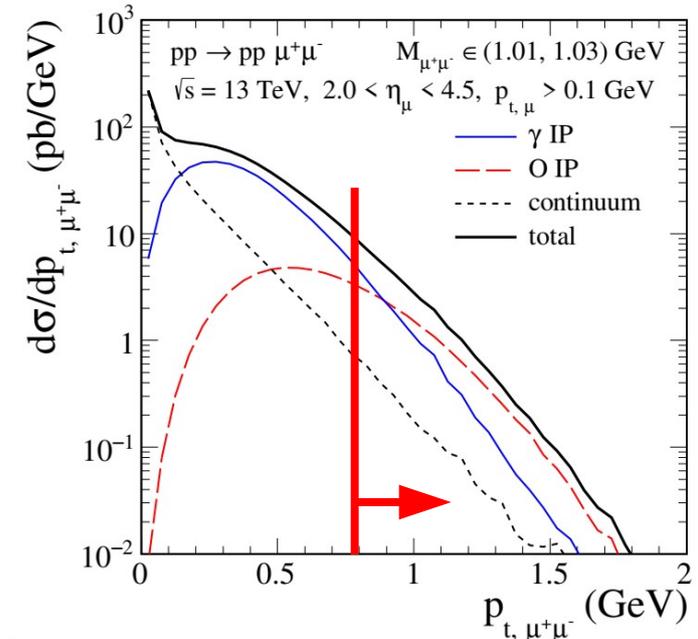
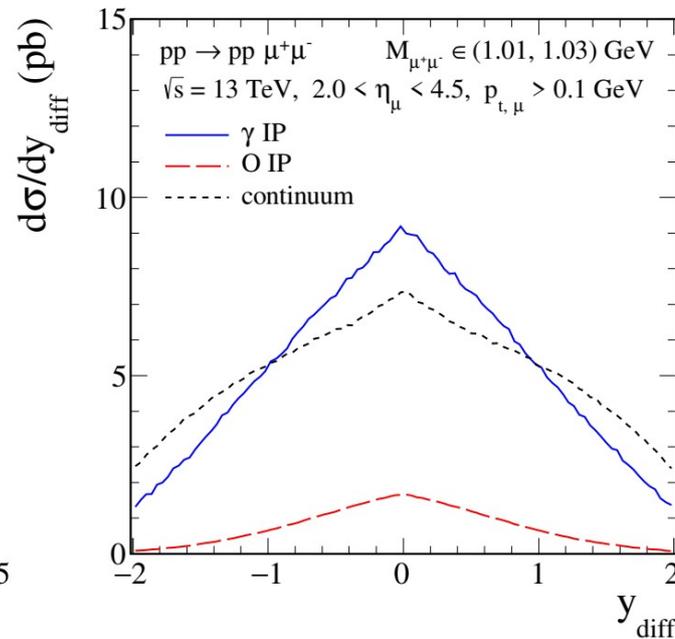
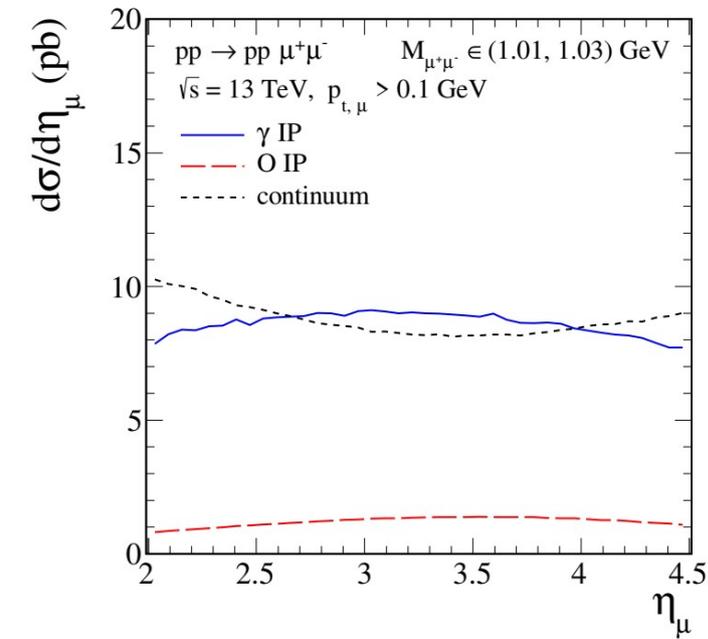
We show the contributions from the  $\gamma\mathbb{P}$ - and  $\mathbb{O}\mathbb{P}$ -fusion processes and the continuum  $\gamma\gamma \rightarrow \mu^+\mu^-$  term.

# Predictions for the $pp \rightarrow pp \mu^+\mu^-$ reaction (LHCb)



- (bottom panels) Larger  $p_{t,\mu}$  can be helpful to reduce the  $\gamma\gamma \rightarrow \mu^+\mu^-$  continuum

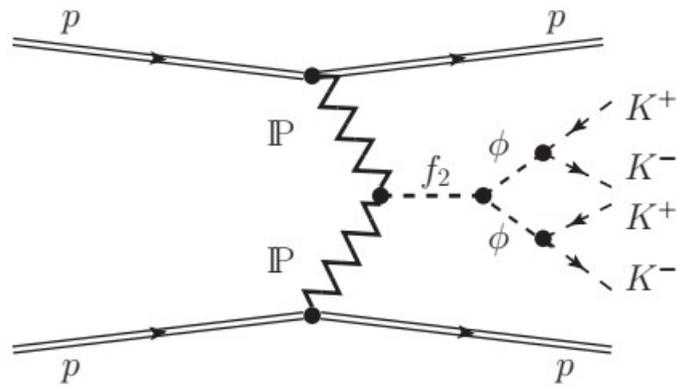
# Predictions for the $pp \rightarrow pp \mu^+\mu^-$ reaction (LHCb)



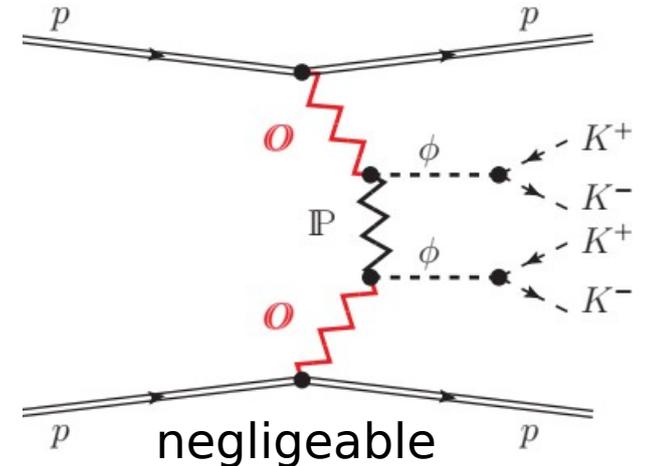
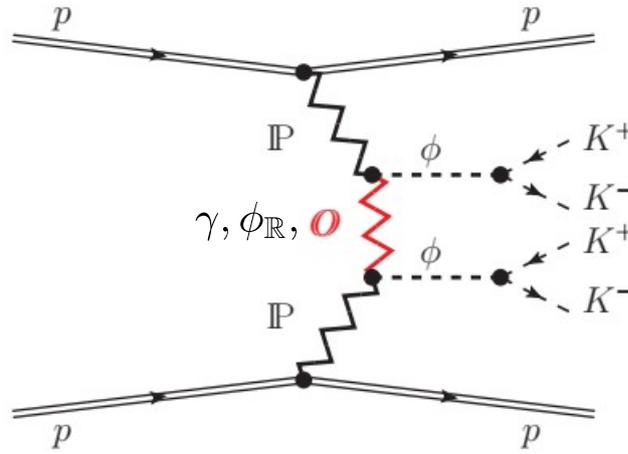
- $p_{t,\mu^+\mu^-} > 0.8$  GeV cut can be helpful to reduce the  $\gamma\gamma \rightarrow \mu^+\mu^-$  continuum and  $\gamma$  IP-fusion contribution
- In this case the absolute normalization of the cross section or detailed studies of shapes of distributions should provide a hint whether one observes the O effect

# The reaction $pp \rightarrow pp(\phi\phi \rightarrow K+K-K+K-)$

P.L., O. Nachtmann, A. Szczurek, PRD99 (2019) 094034



$f_2(2340)$  resonance;  
tensor glueball production



Some modifications are needed to simulate  $2 \rightarrow 6$  reaction  
(e.g. smearing of  $\phi$  masses due to their resonance distribution)

$$\sigma_{2 \rightarrow 6} = [\mathcal{B}(\phi \rightarrow K^+ K^-)]^2 \int_{2m_K} \int_{2m_K} \sigma_{2 \rightarrow 4}(\dots, m_{X_3}, m_{X_4}) f_\phi(m_{X_3}) f_\phi(m_{X_4}) dm_{X_3} dm_{X_4}$$

- At high energies we expect this reaction to be dominated by IPIP fusion processes
- We can expect resonances at low  $M_{\phi\phi}$  and Regge **C = -1** exchanges at high  $M_{\phi\phi}$

Contributions:

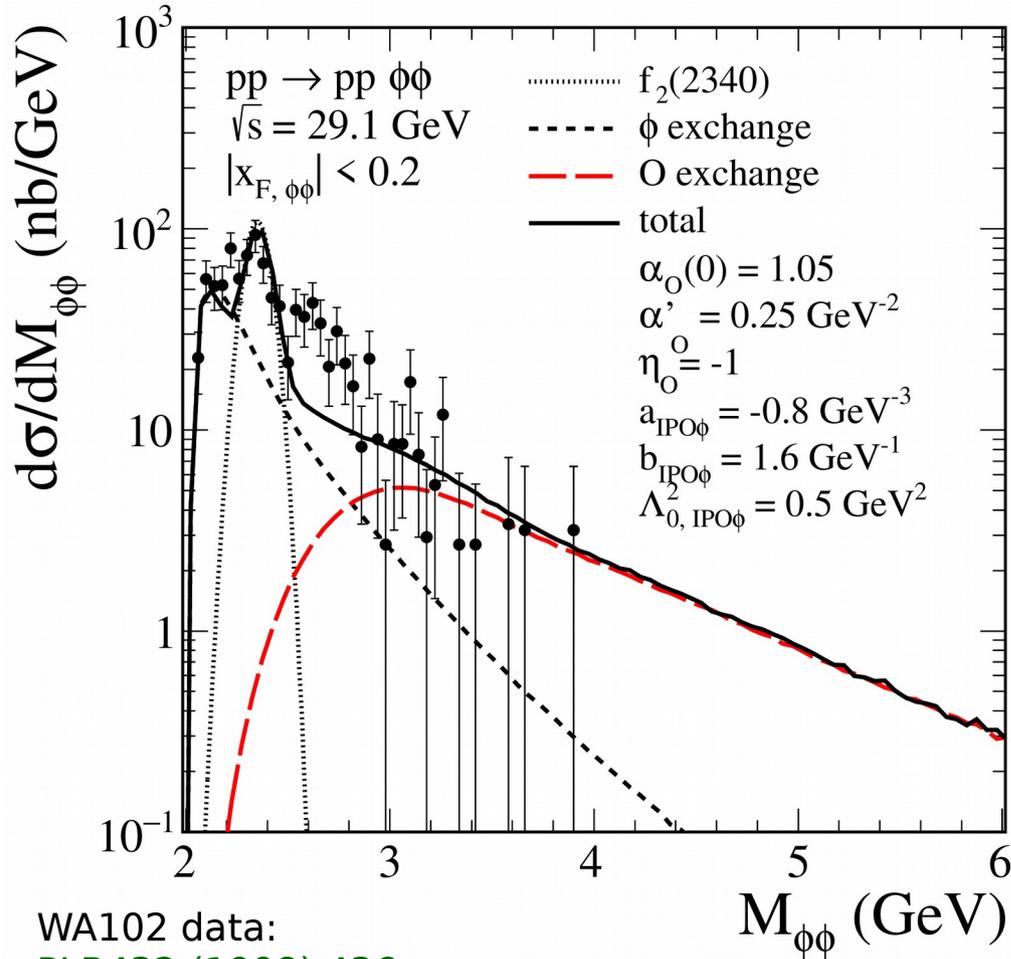
$\gamma$  : negligeable

$$\phi_{\mathbb{R}} : \propto (M_{\phi\phi}^2)^{\alpha_\phi(\hat{t})-1}, \quad \alpha_\phi(\hat{t}) = 0.1 + 0.9\hat{t}$$

$$\mathbb{O} : \propto (M_{\phi\phi}^2)^{\alpha_{\mathbb{O}}(\hat{t})-1}, \quad \alpha_{\mathbb{O}}(0) \approx 1.0 \quad ?$$

If  $\alpha_{\mathbb{O}}(0) \approx 1.0$ , then  $\mathbb{O}$  exchange will win for large  $M_{\phi\phi}$ .

## Comparison with WA102

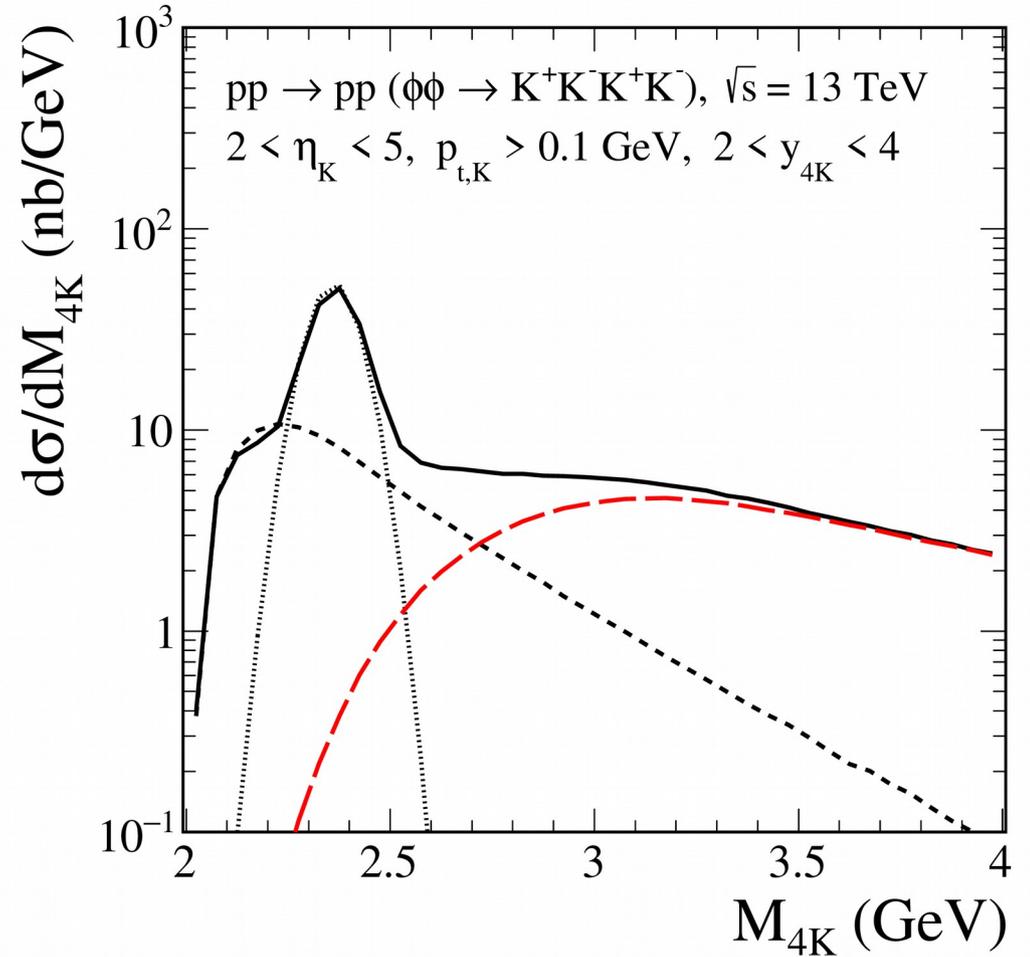


WA102 data:

PLB432 (1998) 436

PLB489 (2000) 29

## Predictions for LHCb



The small intercept of the  $\phi$  reggeon exchange,  $\alpha_\phi(0) = 0.1$  makes the  $\phi$ -exchange contribution steeply falling with increasing  $M_{4K}$  (and also  $|Y_{\text{diff}}|$ ). Therefore, an odderon with an intercept  $\alpha_O(0) \approx 1$  should be clearly visible in these distributions if  $\mathbb{P}\mathbb{O}\phi$  coupling is of reasonable size.

# Conclusions

I have shown you some applications of the **tensor-pomeron** and **vector-odderon** model to CEP. It is effective model where some parameters have to be determined from experiment. All amplitudes are formulated in terms of effective vertices and propagators for the exchanged objects respecting the standard crossing and charge conjugation relations of QFT and the power-law ansätze from the Regge model.

## $pp \rightarrow pp \phi$

- WA102 data give an indication for odderon-exchange contribution
- We have presented distributions which are sensitive to the O-exchange contributions ( $p_{t,K+K'}$ ,  $y_{\text{diff}}$  rapidity distance between the  $K^+$  and  $K^-$ )
- To observe a sizeable deviation from photoproduction a  $p_{t,\mu^+\mu^-} > 0.8$  GeV cut on transverse momentum of the  $\mu^+\mu^-$  pair seems necessary

## $pp \rightarrow pp \phi\phi$

- The  $\phi\phi$  invariant mass distribution has a rich structure (resonances at low  $M_{\phi\phi}$ , continuum terms at higher  $M_{\phi\phi}$ , interference effects)
- The O-exchange contribution should be distinguishable from other contributions in the region of large four-kaon invariant masses and for large rapidity distance between the  $\phi$  mesons

In principle CEP of  $\phi$  and  $\phi\phi$  offers the possibility to determine the  $\text{IPO}\phi$  coupling (at least, to derive an upper limit on the odderon contribution).

We are looking forward to many checks of the model in CEP at the LHC. Comparison with 'exclusive' data expected from LHC experiments should be very valuable for clarifying the status of the odderon.

# Cross sections in nb for CEP of single $\phi$ in $pp$ collisions

Table 1: The integrated cross sections in nb for the CEP of single  $\phi$  mesons in  $pp$  collisions with the subsequent decays  $\phi \rightarrow K^+K^-$  or  $\phi \rightarrow \mu^+\mu^-$ . The results have been calculated for  $\sqrt{s} = 13$  TeV in the dikaon/dimuon invariant mass region  $M_{34} \in (1.01, 1.03)$  GeV and for some typical experimental cuts. The ratios of full and Born cross sections  $\langle S^2 \rangle$  (the gap survival factors) are shown.

Cuts	Contributions	$\sigma^{(\text{Born})}$ (nb)	$\sigma^{(\text{full})}$ (nb)	$\langle S^2 \rangle$
$pp \rightarrow pp K^+K^-$ $ \eta_K  < 2.5, p_{t,K} > 0.1$ GeV	$\gamma\mathbb{P}$ fusion	60.07	55.09	0.9
	$\mathbb{O}\mathbb{P}$ fusion	21.40	6.44	0.3
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		58.58	
$ \eta_K  < 2.5, p_{t,K} > 0.2$ GeV, $0.17$ GeV $<  p_{y,1} ,  p_{y,2}  < 0.5$ GeV	$\gamma\mathbb{P}$ fusion	1.07	0.24	0.2
	$\mathbb{O}\mathbb{P}$ fusion	2.10	0.61	0.3
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		0.70	
$2.0 < \eta_K < 4.5, p_{t,K} > 0.1$ GeV	$\gamma\mathbb{P}$ fusion	43.18	40.07	0.9
	$\mathbb{O}\mathbb{P}$ fusion	16.73	4.70	0.3
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		43.28	
$2.0 < \eta_K < 4.5, p_{t,K} > 0.3$ GeV	$\gamma\mathbb{P}$ fusion	3.09	2.57	0.8
	$\mathbb{O}\mathbb{P}$ fusion	6.57	1.64	0.3
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		4.24	
$2.0 < \eta_K < 4.5, p_{t,K} > 0.5$ GeV	$\gamma\mathbb{P}$ fusion	$0.93 \times 10^{-1}$	$0.66 \times 10^{-1}$	0.7
	$\mathbb{O}\mathbb{P}$ fusion	0.88	0.16	0.2
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		0.24	
$pp \rightarrow pp \mu^+\mu^-$ $2.0 < \eta_\mu < 4.5, p_{t,\mu} > 0.1$ GeV	$\gamma\mathbb{P}$ fusion	$23.93 \times 10^{-3}$	$20.96 \times 10^{-3}$	0.9
	$\mathbb{O}\mathbb{P}$ fusion	$10.06 \times 10^{-3}$	$3.02 \times 10^{-3}$	0.3
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		$21.64 \times 10^{-3}$	
$2.0 < \eta_\mu < 4.5, p_{t,\mu} > 0.5$ GeV	$\gamma\mathbb{P}$ fusion	$1.21 \times 10^{-3}$	$0.85 \times 10^{-3}$	0.7
	$\mathbb{O}\mathbb{P}$ fusion	$1.49 \times 10^{-3}$	$0.45 \times 10^{-3}$	0.2
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		$1.07 \times 10^{-3}$	
$2.0 < \eta_\mu < 4.5, p_{t,\mu} > 0.1$ GeV, <u><math>p_{t,\mu^+\mu^-} &gt; 0.8</math> GeV</u>	$\gamma\mathbb{P}$ fusion	$0.70 \times 10^{-3}$	$0.41 \times 10^{-3}$	0.6
	$\mathbb{O}\mathbb{P}$ fusion	$2.46 \times 10^{-3}$	$0.51 \times 10^{-3}$	0.2
	$\gamma\mathbb{P}$ and $\mathbb{O}\mathbb{P}$		$0.91 \times 10^{-3}$	