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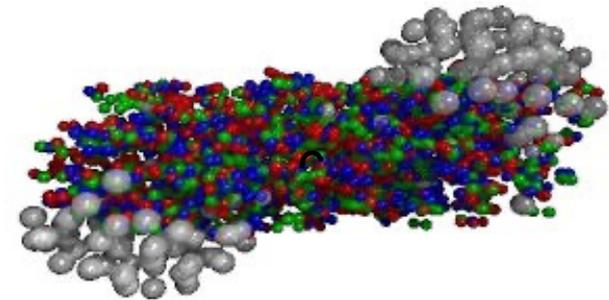
Geometry and Dynamics in Heavy-ion Collisions Seen by the Femtoscopy Method in the STAR experiment

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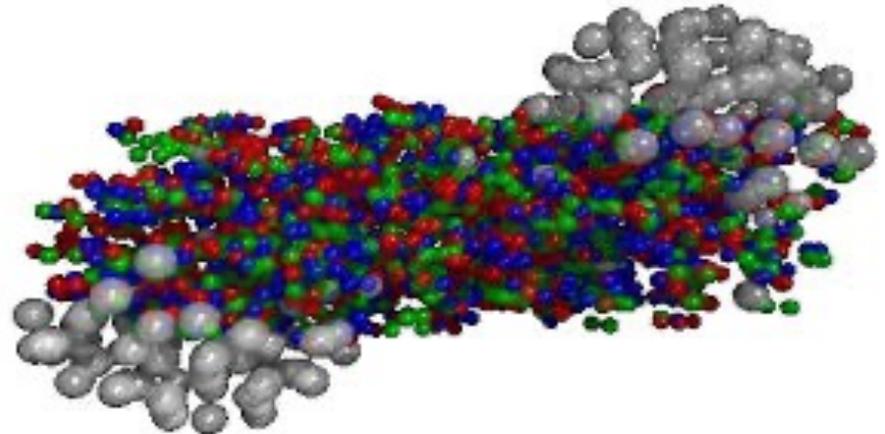
Outline

Introduction

- HIC and HBT method
- Correlation femtoscopy: method, frames, correlations, measures, ...
- RHIC / STAR

Results

- Strong **interactions** between (anti)baryons
- Femtoscopy of strange baryons
- Beam Energy Scan Program (BES):
 - identical pion femtoscopy
 - **geometry**: centrality dependencies
energy dependencies
system (of pair) dependencies
 - **dynamics**: centrality dependencies
energy dependencies
system (of pair) dependencies

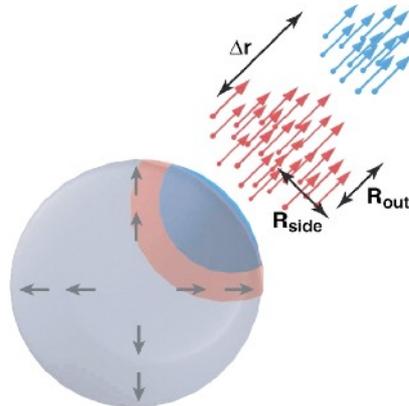
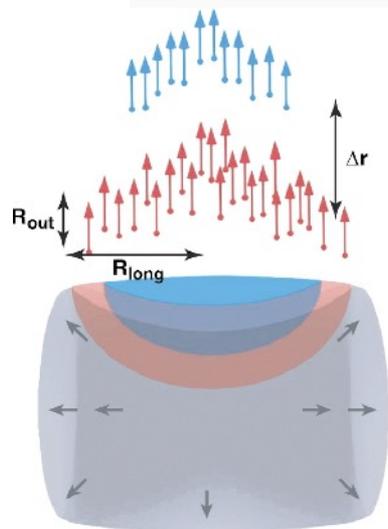
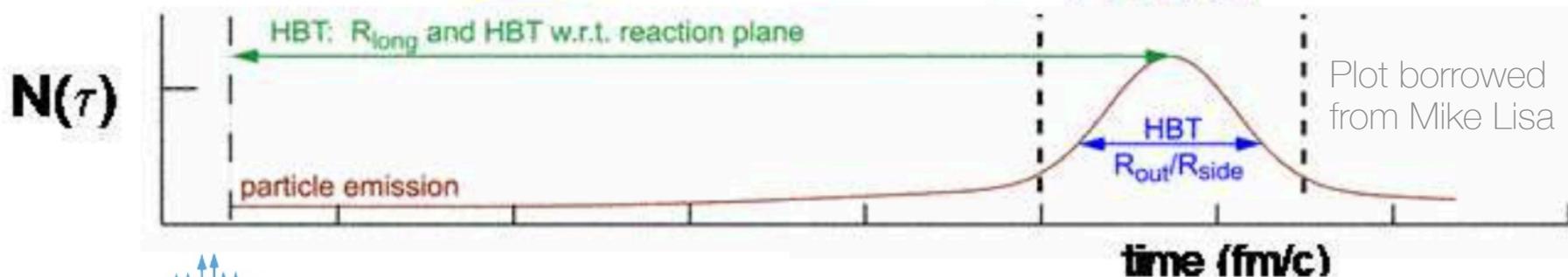
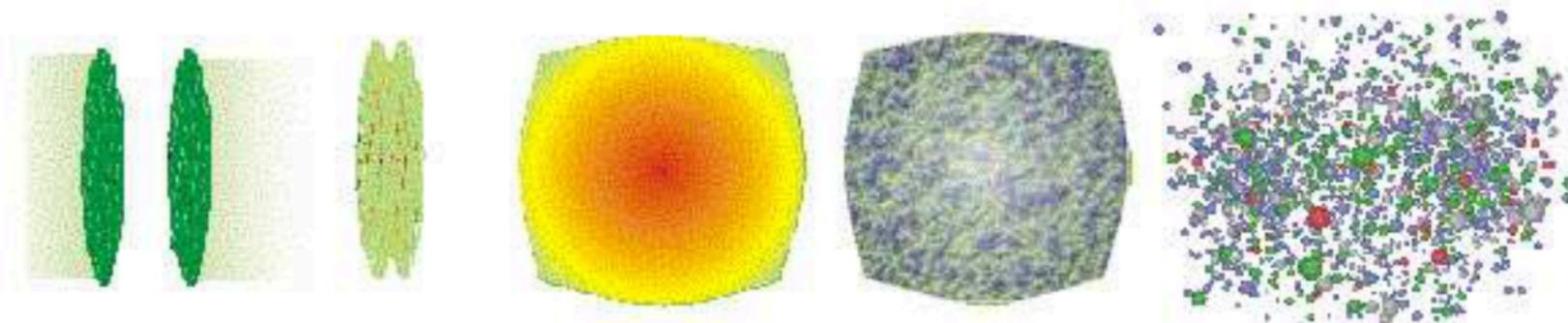


Conclusions



Introduction

Heavy-Ion collision and **HBT** method



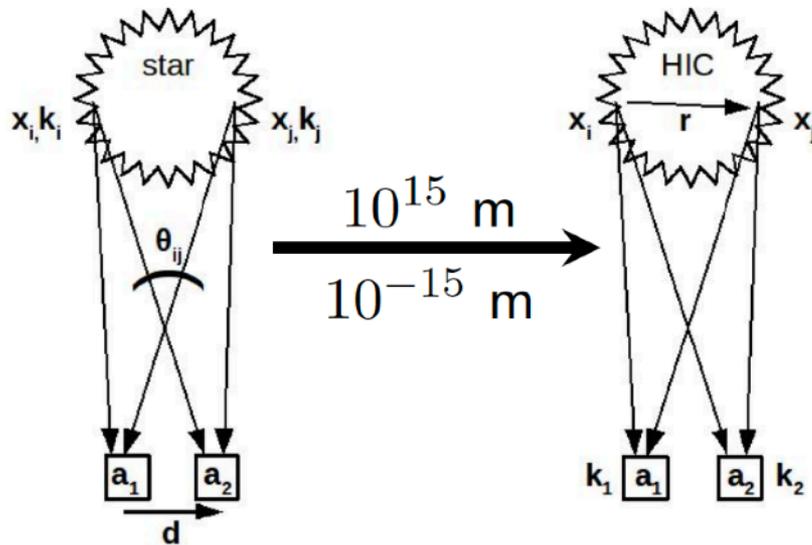
long - beam axis
out - pair transverse \mathbf{p}
side - perpendicular to out and long

Correlation **femtosc**copy



Size: $\sim 10^{-15}$ m (**fm**)
Time: $\sim 10^{-23}$ s

**Impossible
to measure directly!**



Femtoscscopy (**HIC**) inspired by **H**anbury **B**rown and **T**wiss interferometry method (**A**stronomy)

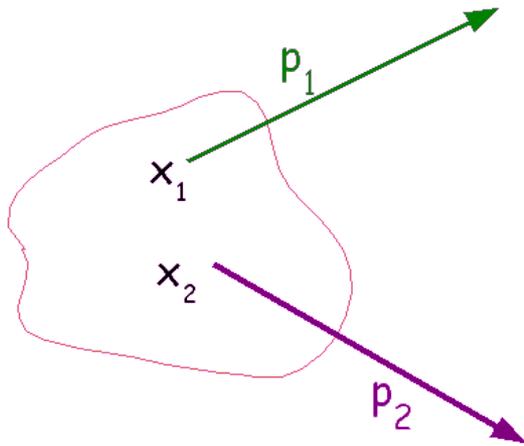
but!

- different scales,
- different measured quantities
- different determined quantities

Femtoscopic correlations and correlation function

$S(x,p)$ – emission function:

the distribution of source density
probability of finding particle with x and p



x_1, x_2 - space-time sizes and dynamics

(**can not** be measured directly) →

Close velocity correlations

(**HBT + FSI**) ←

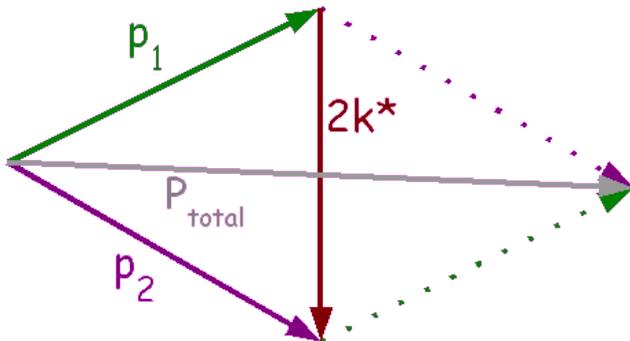
p_1, p_2 - momenta and momentum difference

(**can** be measured directly)

Single- and two-particle distributions

$$P_1(p) = E \frac{dN}{d^3 p} = \int d^4 x S(x, p)$$

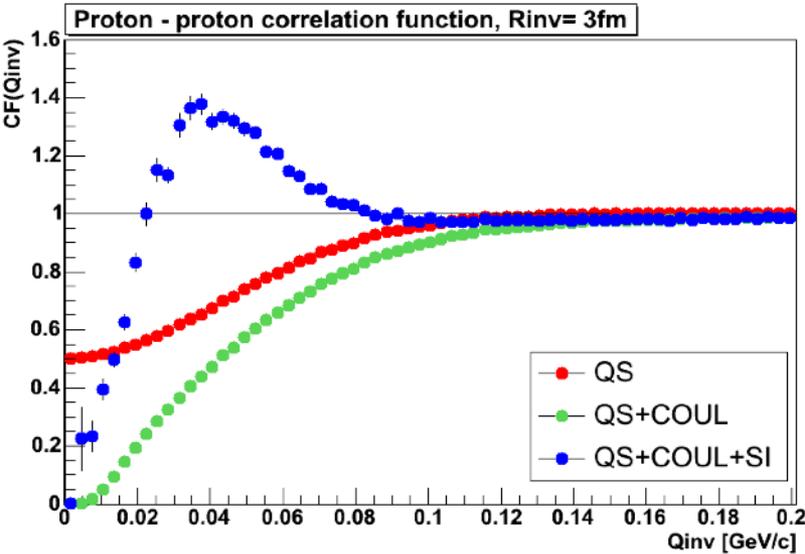
$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3 p_1 d^3 p_2} = \int d^4 x_1 S(x_1, p_1) d^4 x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$



Correlation function

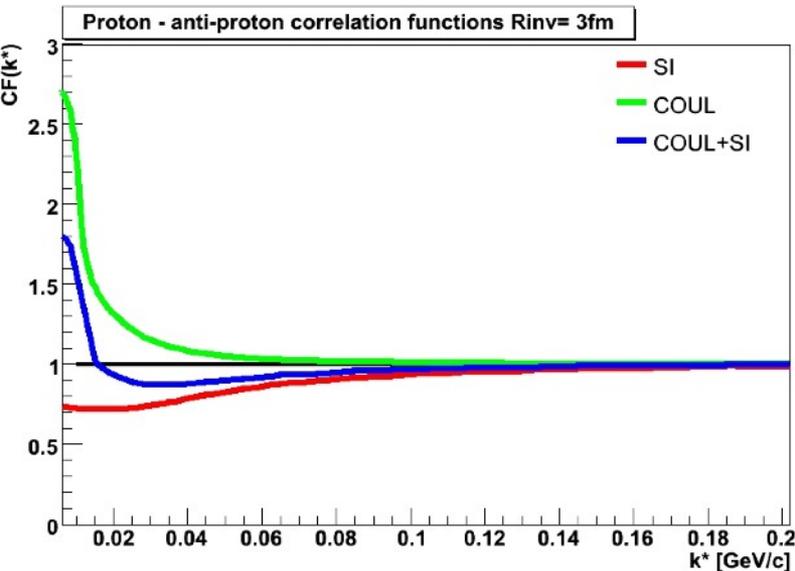
$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1) P_1(p_2)}$$

Effects and interactions



Identical pairs:

- Quantum Statistics- **QS**
- Final State Interactions- **FSI**: Coulomb, Strong

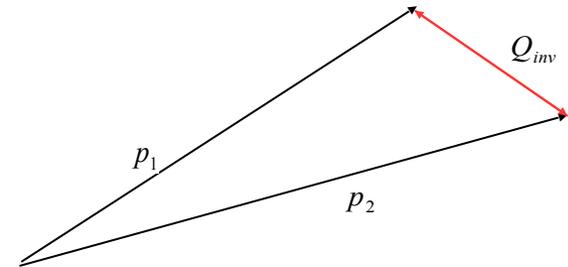


Non-identical pairs:

- Final State Interactions- **FSI**: Coulomb, Strong

Longitudinal Co-Moving System - **LCMS**

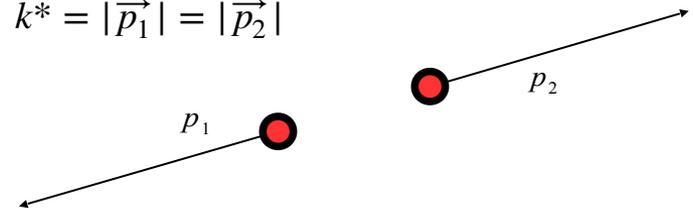
$$\vec{p}_{1,L} + \vec{p}_{2,L} = 0$$



$$Q_{inv} = \sqrt{(p_1 - p_2)^2 - (E_1 - E_2)^2} \text{ if } m_1 = m_2$$

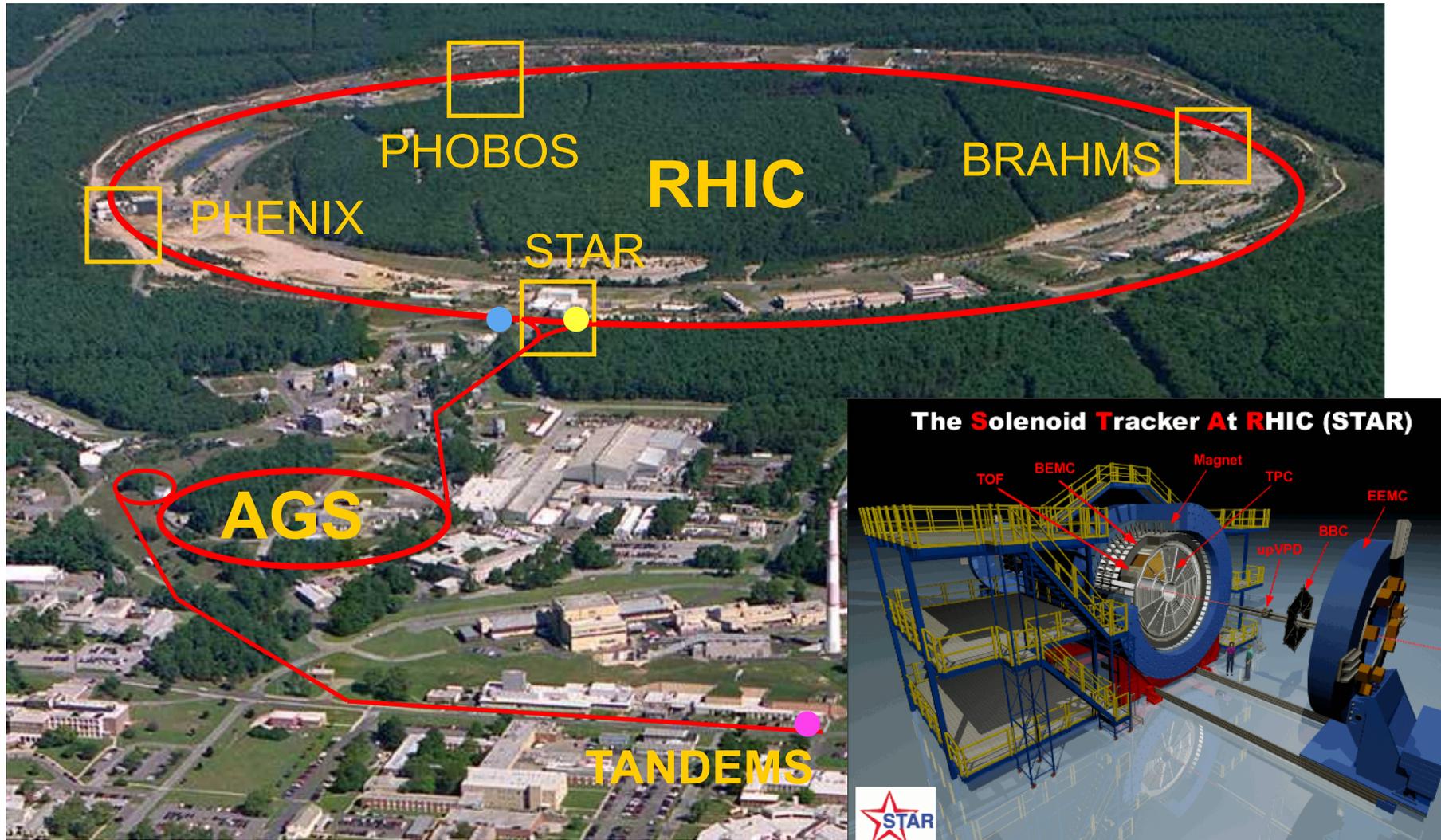
Pair Rest Frame - **PRF**

$$k^* = |\vec{p}_1| = |\vec{p}_2|$$



$$Q_{inv} = 2k^* \text{ if } m_1 = m_2$$

Relativistic Heavy Ion Collider (**RHIC**) Brookhaven National Laboratory (**BNL**), Upton



- 2 concentric rings of 1740 superconducting magnets
- 3.8 km circumference



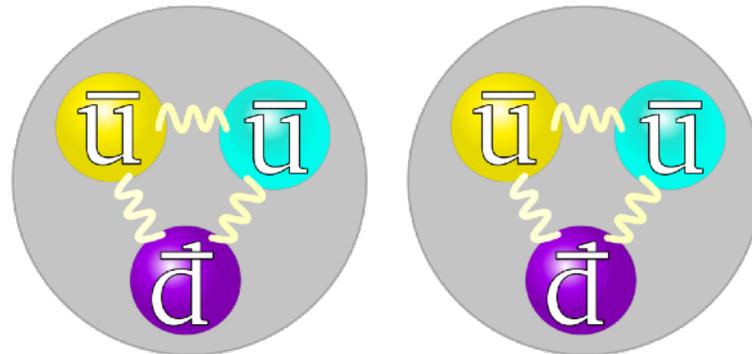
Results

a) Proton Femtoscopy @200 GeV

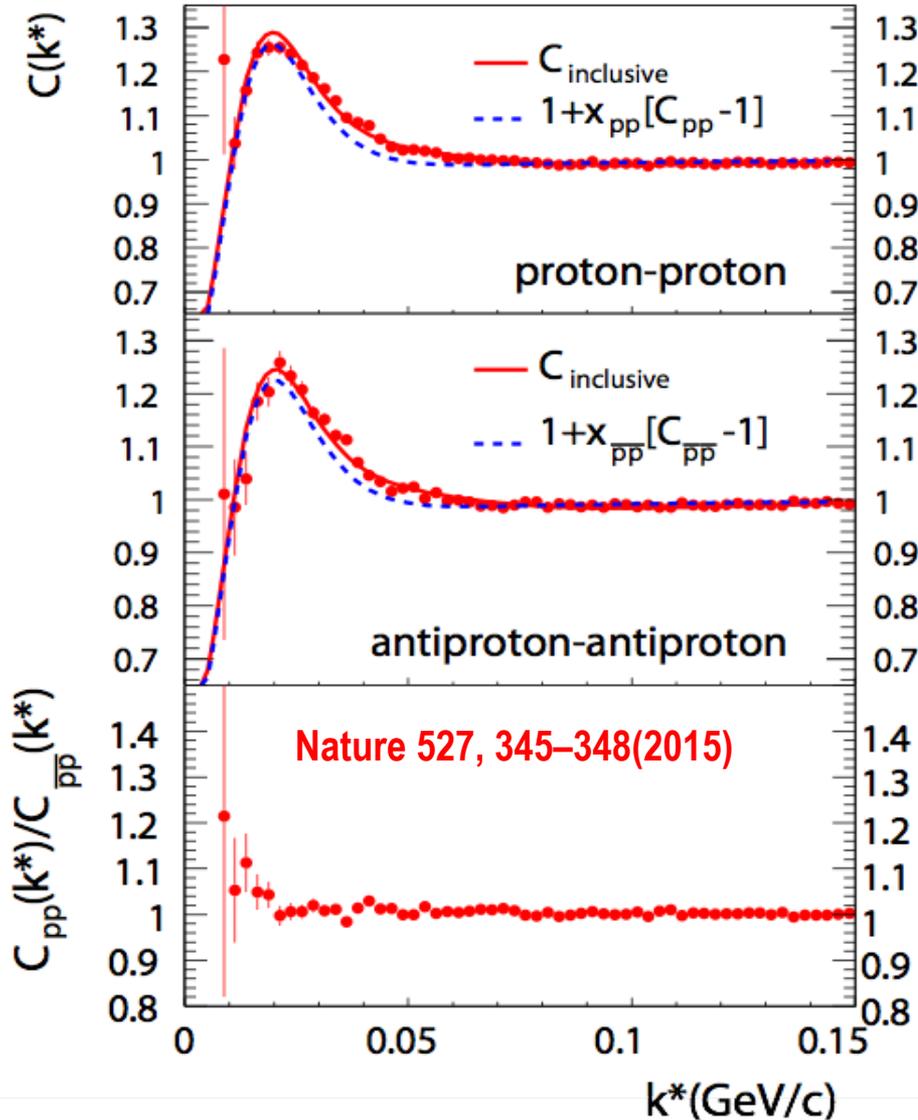
So far, the knowledge on **nuclear force** has been derived from studies made on **nucleon** or / and **nuclei**.

Nuclear force between **anti-nucleons** is studied for the first time.

The knowledge of **interaction** between two **anti-protons** is fundamental to understand the properties of more sophisticated anti-nuclei.



a) Strong interactions between anti-nucleons



Fit results:

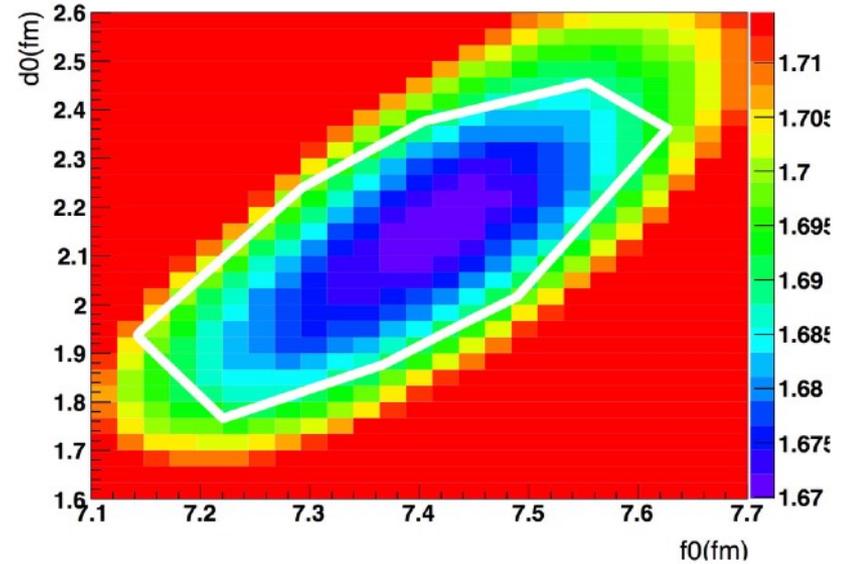
p-p CF,

$R=2.75\pm 0.01\text{fm}$; $\chi^2/\text{NDF} = 1.66$;

antiproton-antiproton CF,

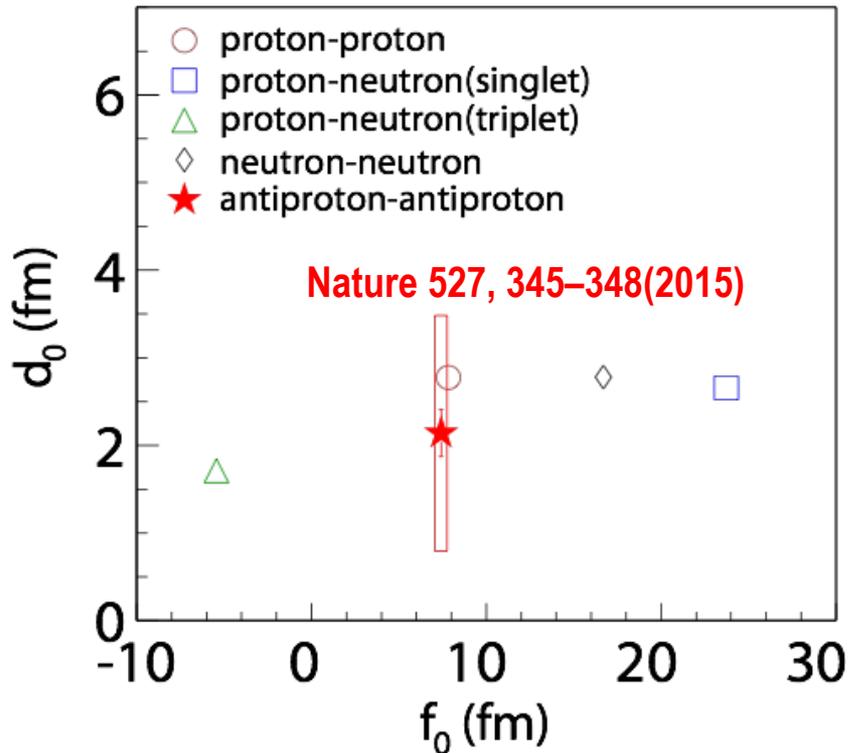
$R=2.80\pm 0.02\text{fm}$, $f_0=7.41\pm 0.19\text{fm}$,

$d_0=2.14\pm 0.27\text{fm}$; $\chi^2/\text{NDF}=1.61$



$\chi^2/\text{NDF}(f_0, d_0)$ map of the results between measured function and fitted one to find the best values of f_0 , d_0 parameters

a) Strong interactions between anti-nucleons



- f_0 and d_0 for the antiproton-antiproton interaction consistent with parameters for the proton-proton interaction.
- Descriptions of the interaction among antimatter (based on the simplest systems of anti-nucleons) determined.
- A quantitative verification of matter-antimatter symmetry in context of the forces responsible for the binding of (anti)nuclei.

The scattering length f_0 : determines low-energy scattering.

The elastic cross section, σ_e , (at low energies) determined solely by the scattering length, $\lim_{k \rightarrow 0} \sigma_e = 4\pi f_0^2$

d_0 - the effective range of strong interaction between two particles.

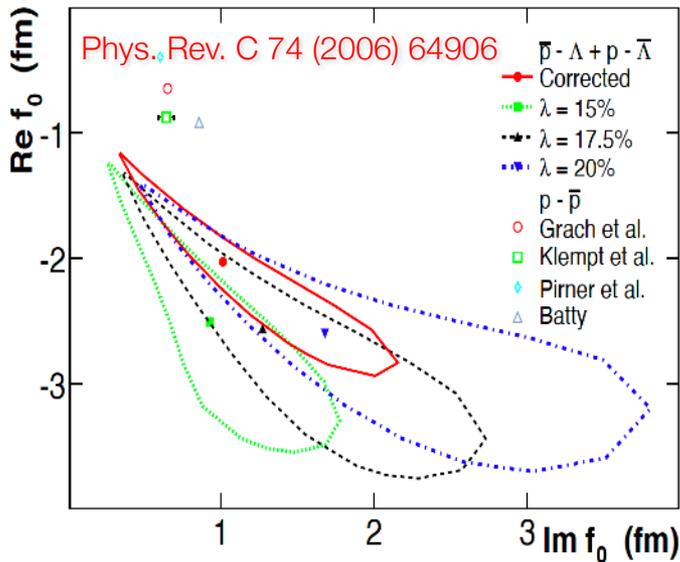
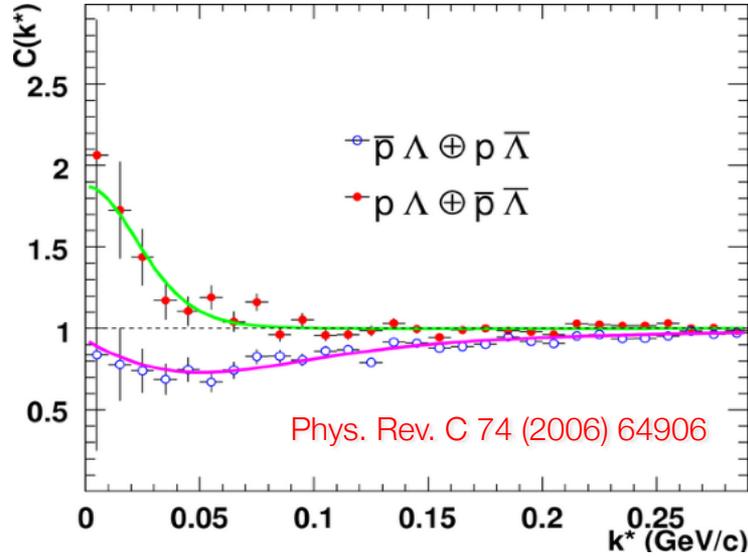
It corresponds to the range of the potential in an extremely simplified scenario - the square well potential.

f_0 and d_0 - two important parameters of strong interaction between two particles.

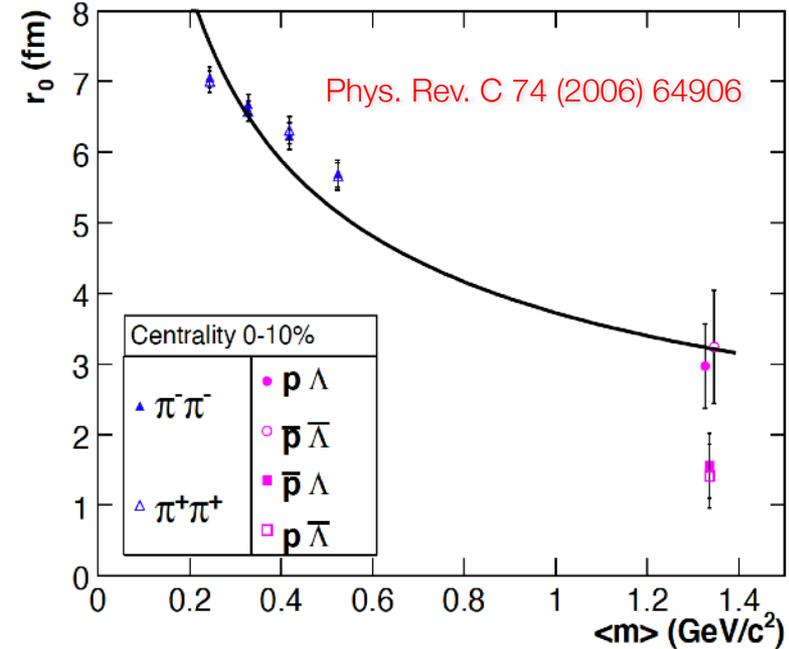
Theoretical correlation function depends on: source size, k^* , f_0 and d_0 .

b) Strange Baryon Correlations (Including Λ Hyperons)

$p - \Lambda$ correlations:
sensitive to the Strong FSI only



System	r_0 (fm)
$p - \Lambda$	$2.97 \pm 0.34^{+0.19}_{-0.25} \pm 0.2$
$\bar{p} - \bar{\Lambda}$	$3.24 \pm 0.59^{+0.24}_{-0.14} \pm 0.2$
$p - \Lambda \oplus \bar{p} - \bar{\Lambda}$	$3.09 \pm 0.30^{+0.17}_{-0.25} \pm 0.2$
$\bar{p} - \Lambda$	$1.56 \pm 0.08^{+0.10}_{-0.14} \pm 0.3$
$p - \bar{\Lambda}$	$1.41 \pm 0.10 \pm 0.11 \pm 0.3$
$\bar{p} - \Lambda \oplus p - \bar{\Lambda}$	$1.50 \pm 0.05^{+0.10}_{-0.12} \pm 0.3$



$p - \Lambda$ correlations: contain contributions from
Residual feed-down Correlations (RC)

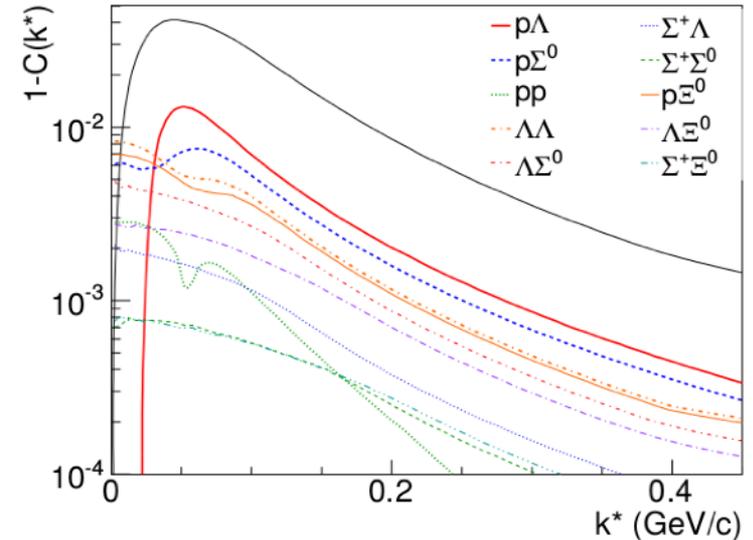
b) Strange Baryon Correlations (Including Λ Hyperons)

$$C^{XY \rightarrow p\bar{\Lambda}}(k_{p\bar{\Lambda}}^*) = \frac{\int C^{XY\bar{Y}}(k_{XY}^*) W(k_{XY}^*, k_{p\bar{\Lambda}}^*) dk_{XY}^*}{\int W(k_{XY}^*, k_{p\bar{\Lambda}}^*) dk_{XY}^*}$$

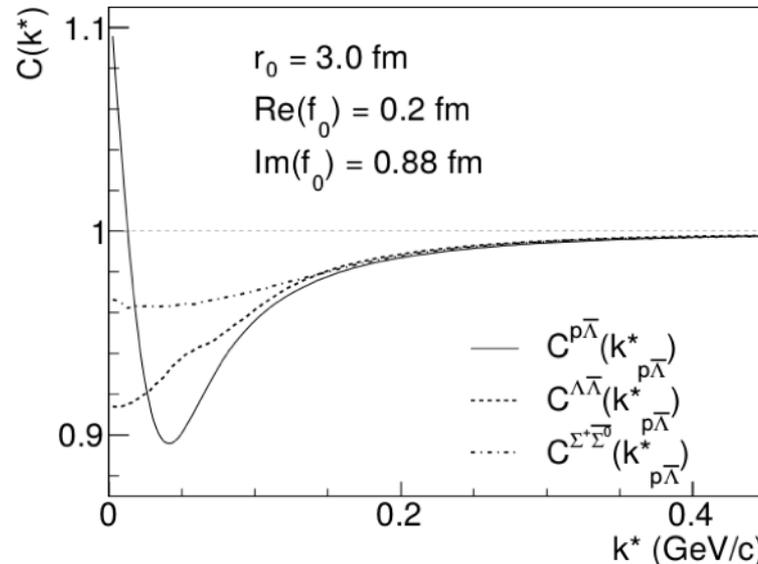
$$C(k_{p\bar{\Lambda}}^*) = 1 + \lambda_{p\Lambda} \left(C^{p\bar{\Lambda}}(k_{p\bar{\Lambda}}^*) - 1 \right) + \sum_{XY} \lambda_{XY} \left(C^{XY\bar{Y}}(k_{p\bar{\Lambda}}^*) - 1 \right)$$

$p - \Lambda$ correlations: contain contributions from **Residual** feed-down **Correlations (RC)**

Removing residual contribution pure correlation signal leads to **similar source sizes** in case of $p - \Lambda$ and $p - \bar{\Lambda}$



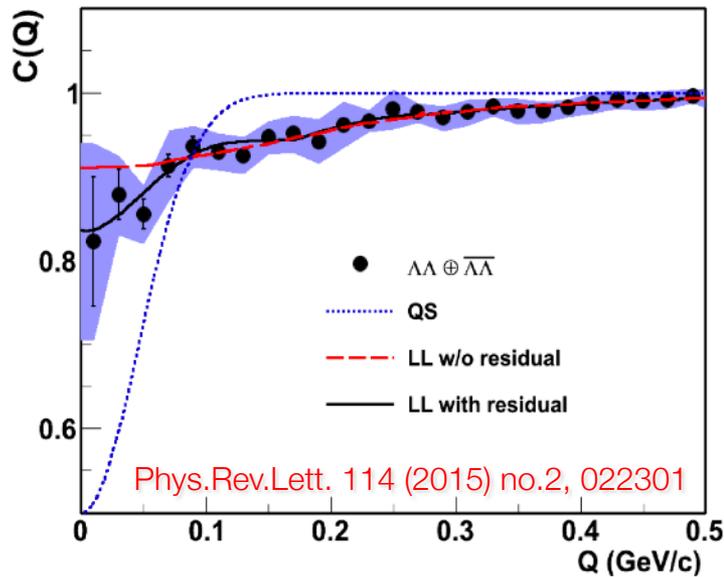
Phys.Rev. C89 (2014) no.5, 054916
HZ, A. Kisiel, M. Szymański



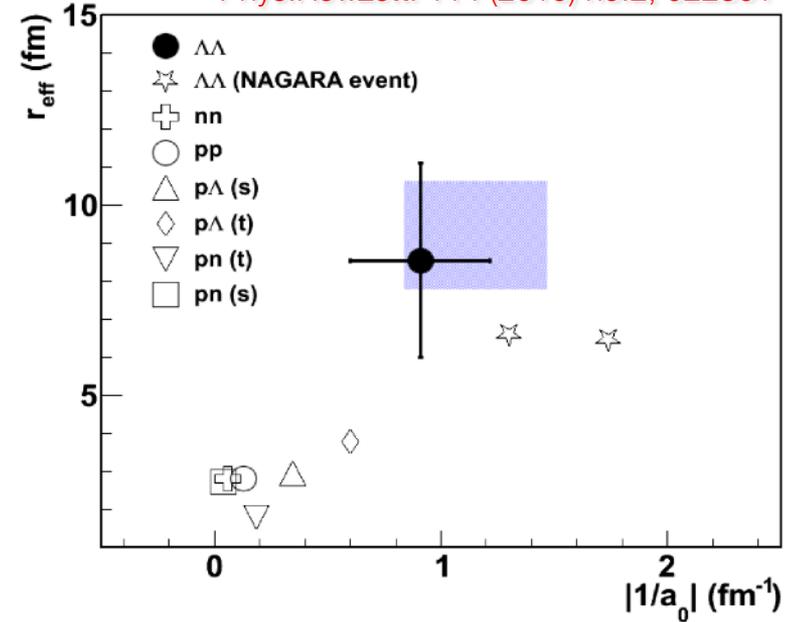
b) Strange Baryon Correlations (Including Λ Hyperons)

$\Lambda - \Lambda$ correlations:
sensitive to the Quantum Statistical
effects and Strong FSI

lambda-lambda correlations: contain contributions
from **Residual** feed-down **Correlations (RC)**



Phys.Rev.Lett. 114 (2015) no.2, 022301



- strength of the $\Lambda - \Lambda$ interaction is weak;
- nonexistence of a $\Lambda\Lambda$ resonance
- limit on the yield of a deuteron-like bound **H**-dibaryon is also reported.

b) Strange Baryon Correlations (including $p\text{-}\Omega$)

Binding energy E_{bin} [MeV]

Scattering length a_0 [fm]

Effective range r_{eff} [fm]

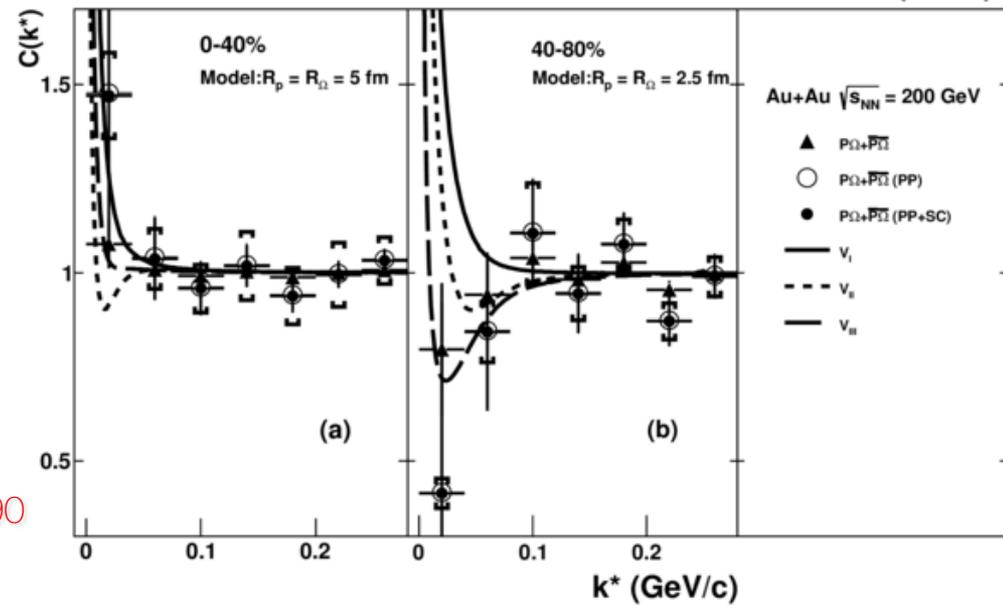
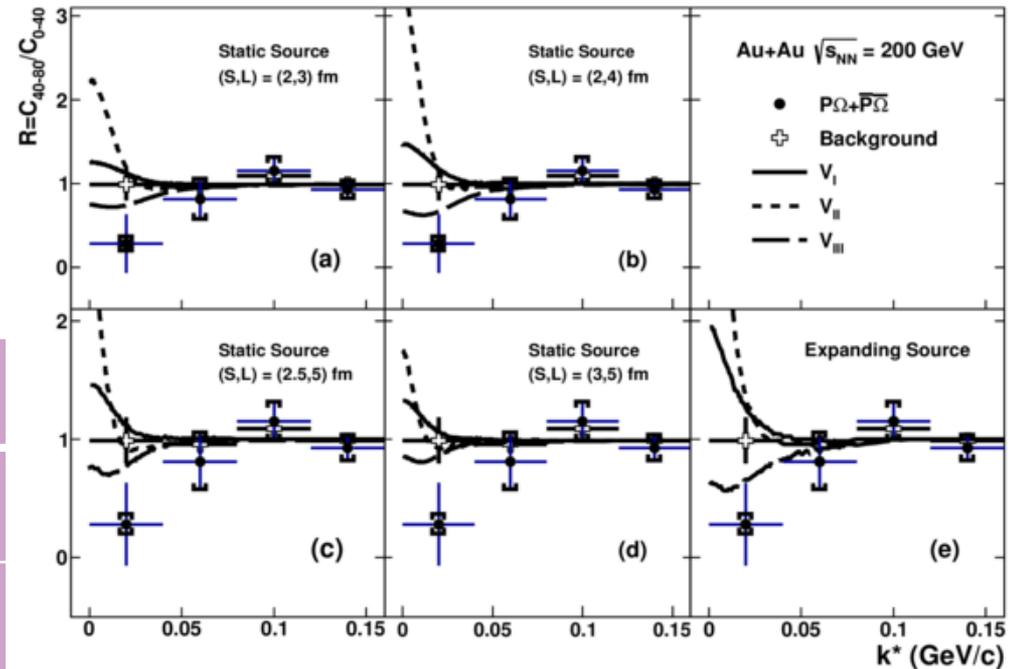
for 3 scenarios:

K. Morita et al. Phys. Rev. C 94, 031901 (2016)

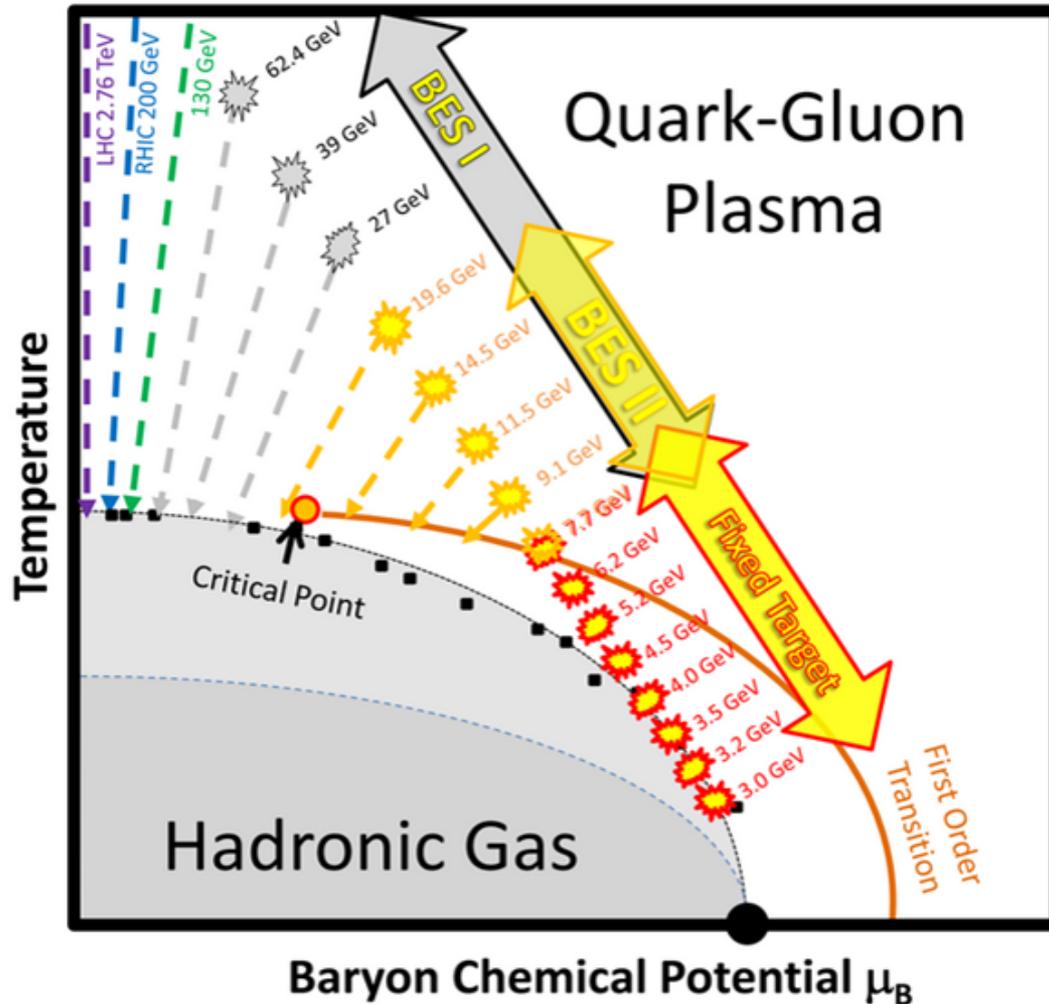
	V_1	V_2	V_3
E_{bin} [MeV]	-	6.3	26.9
a_0 [MeV]	-1.12	5.79	1.29
r_{eff} [MeV]	-1.16	0.96	0.65

A comparison of the measured correlation functions from Au+Au collisions with theoretical predictions

Scattering length is positive and favor $p\Omega$ bound state hypothesis



c) Program **B**eam **E**nergy **S**can



RHIC **T**op **E**nery

p+p, p+Al, p+Au, d+Au,
 $^3\text{He}+\text{Au}$, Cu+Cu, Cu+Au,
Ru+Ru, Zr+Zr, Au+Au, U+U
QCD at high energy
density/temperature
Properties of QGP, EoS

Beam **E**nergy **S**can

Au+Au 7.7-62 GeV

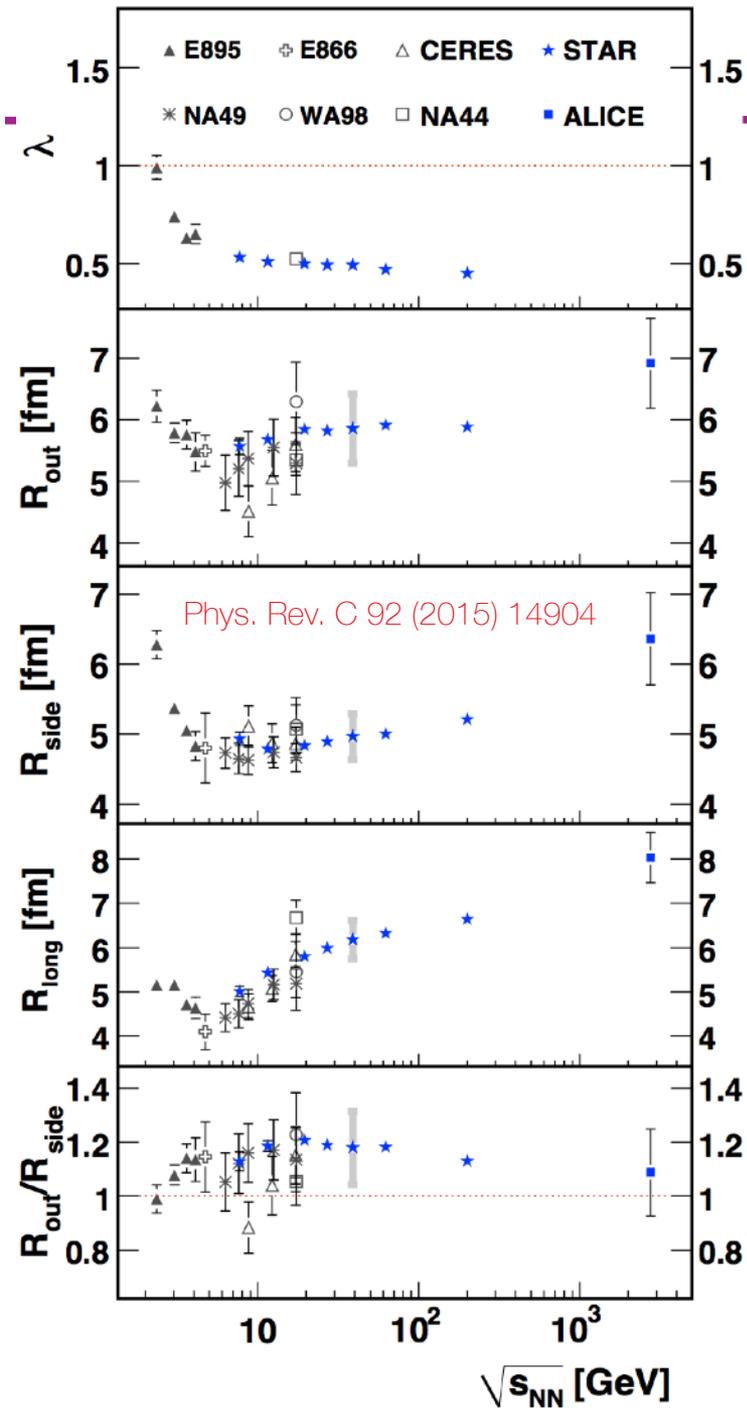
- QCD phase transition
- Search for critical point
- Turn-off of QGP signatures
- Chiral symmetry restoration

Fixed-**T**arget Program

Au+Au =3.0-7.7 GeV

High baryon density regime
with 420-720 MeV

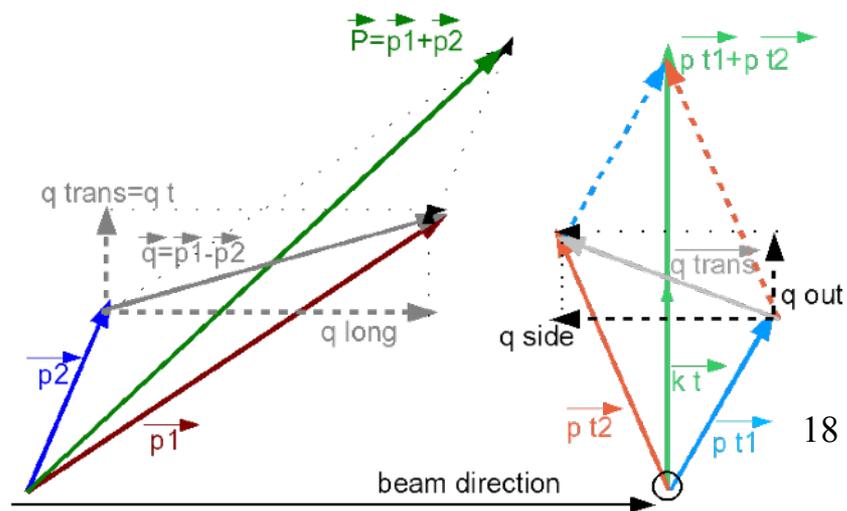
Program BES



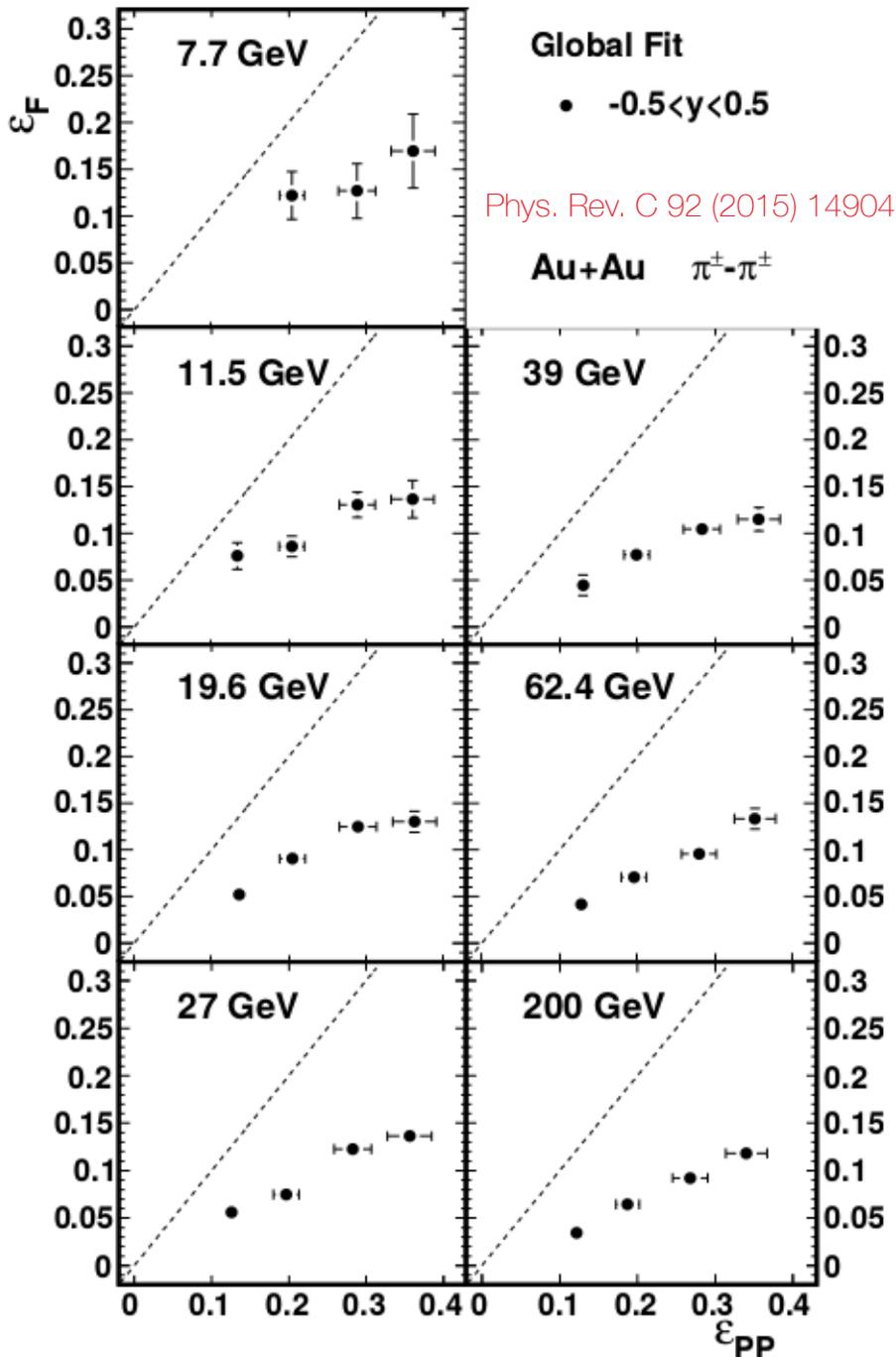
- R_{side} spatial source evolution in the transverse direction
- R_{out} related to spatial and time components
- R_{out}/R_{side} (before!) signature of phase transition
- $R_{out}^2 - R_{side}^2 = \Delta\tau^2 \beta_t^2$; $\Delta\tau$ – emission time
- R_{long} temperature of kinetic freeze-out and source lifetime

$$C(\vec{q}) = (1 - \lambda) + K_{Coul}(q_{inv})\lambda$$

$$\times \exp(-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 - 2q_o q_s R_{os}^2 - 2q_o q_l R_{ol}^2)$$



Program BES

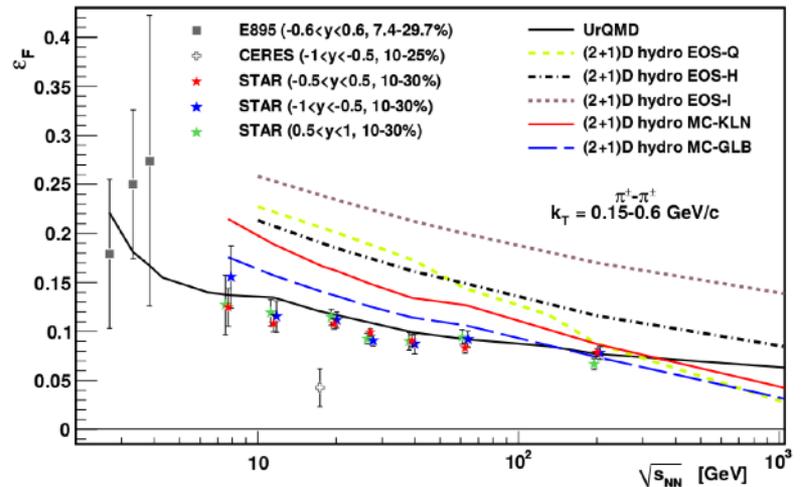


$$\varepsilon_{PP} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_x^2 + \sigma_y^2}, \quad \varepsilon_F = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

$$\sigma_x^2 = \{x^2\} - \{x\}^2 \text{ and } \sigma_y^2 = \{y^2\} - \{y\}^2$$

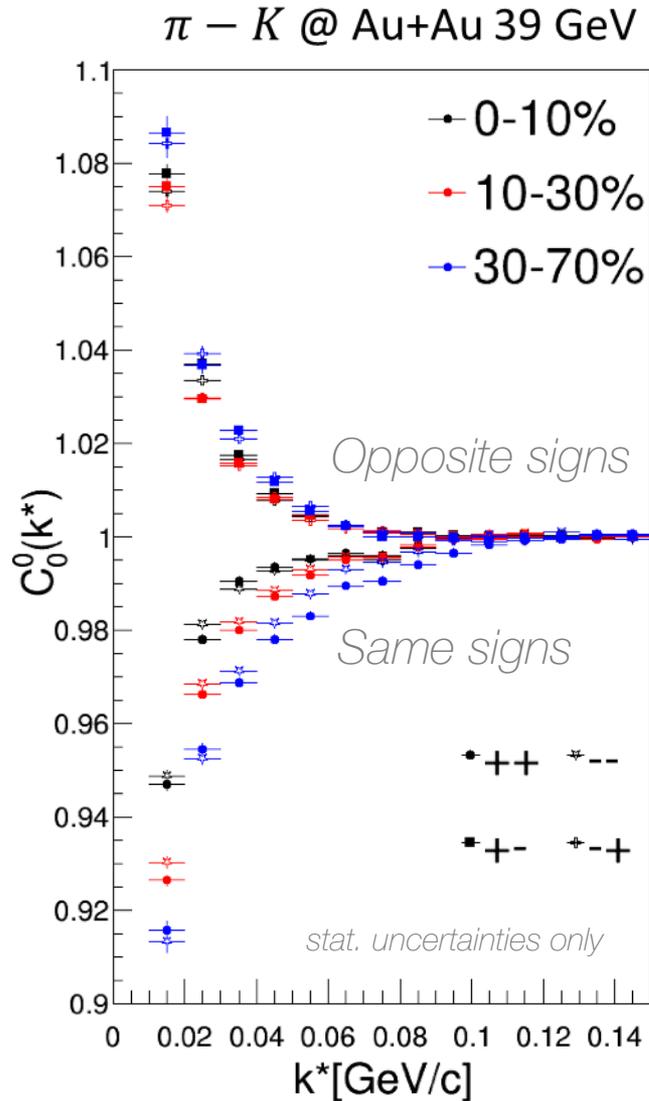
$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6,\dots} R_{\mu,n}^2 \cos(n\Phi) \quad (\mu = o, s, l, ol)$$

$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6,\dots} R_{\mu,n}^2 \sin(n\Phi) \quad (\mu = os)$$

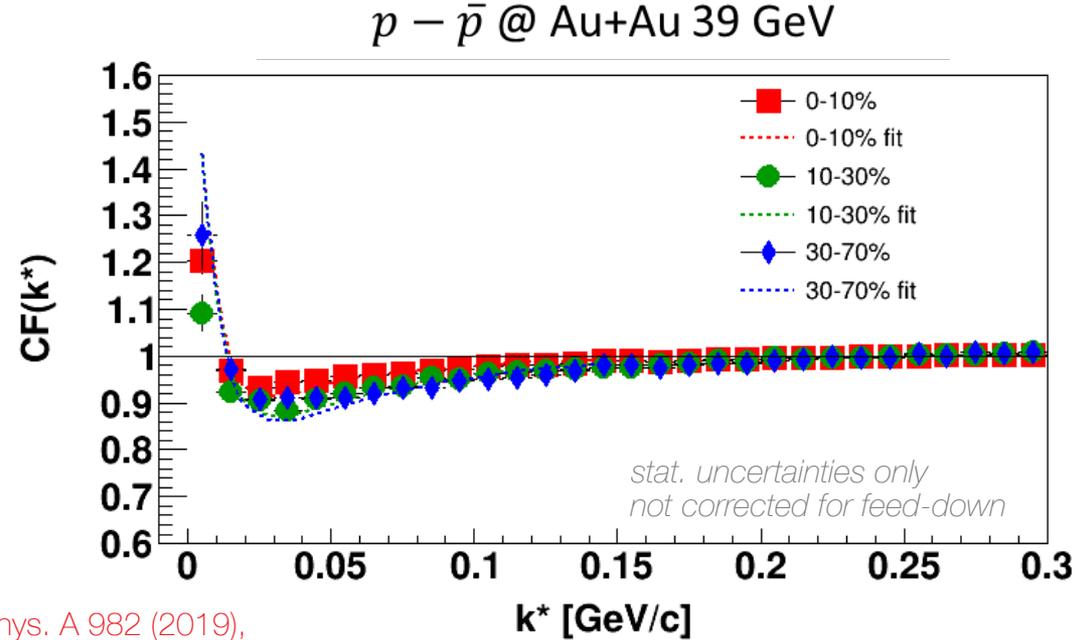


System evolves faster in the reaction plane than in the direction perpendicular to it

Geometry: dependence on collision centrality



Nucl. Phys. A 982 (2019),
359-362



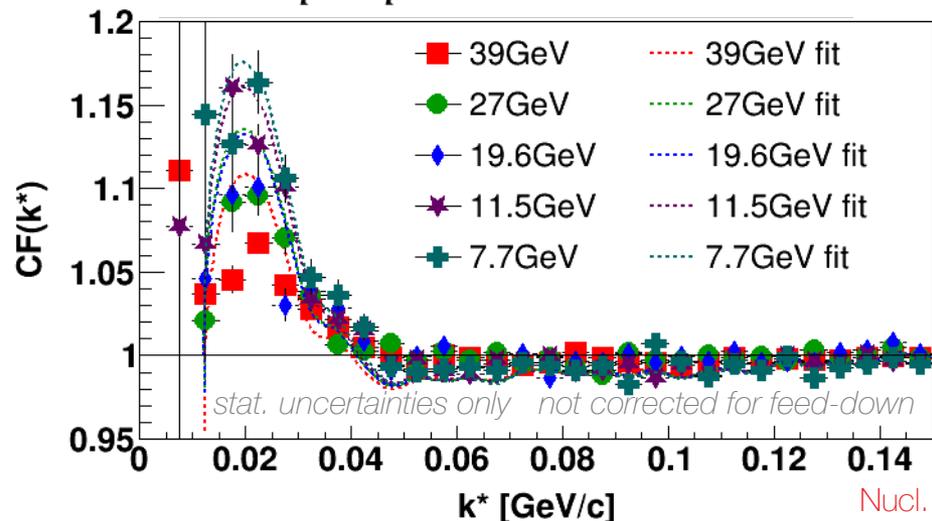
Clear centrality dependence

$$R(0-10\%) > R(10-30\%) > R(30-70\%)$$

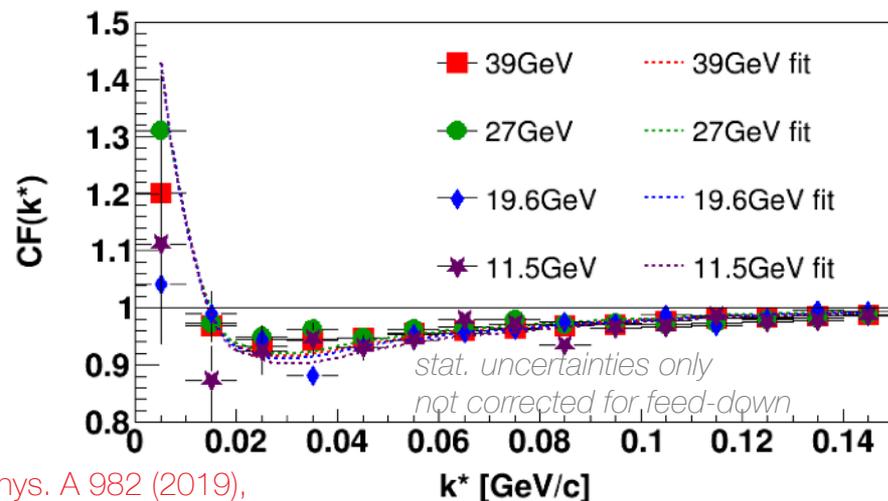
centrality	$R_{inv} p - \bar{p}$ [fm]
0-10%	$3.39 \pm 0.12 \pm 0.14$
10-30%	$2.69 \pm 0.10 \pm 0.12$
30-70%	$2.56 \pm 0.09 \pm 0.12$

Dependence on collision energy

$p - p$: Au+Au 0-10%

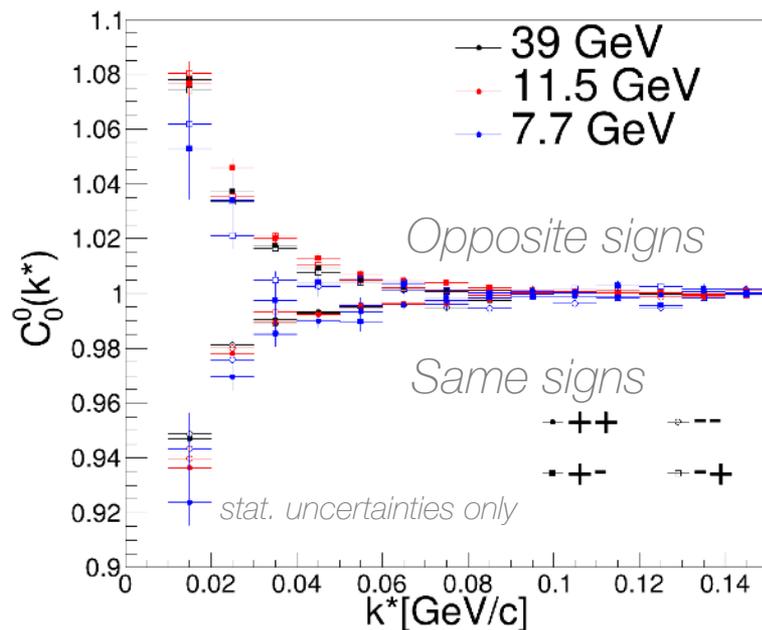


$p - \bar{p}$: Au+Au 0-10%



Nucl. Phys. A 982 (2019),
359-362

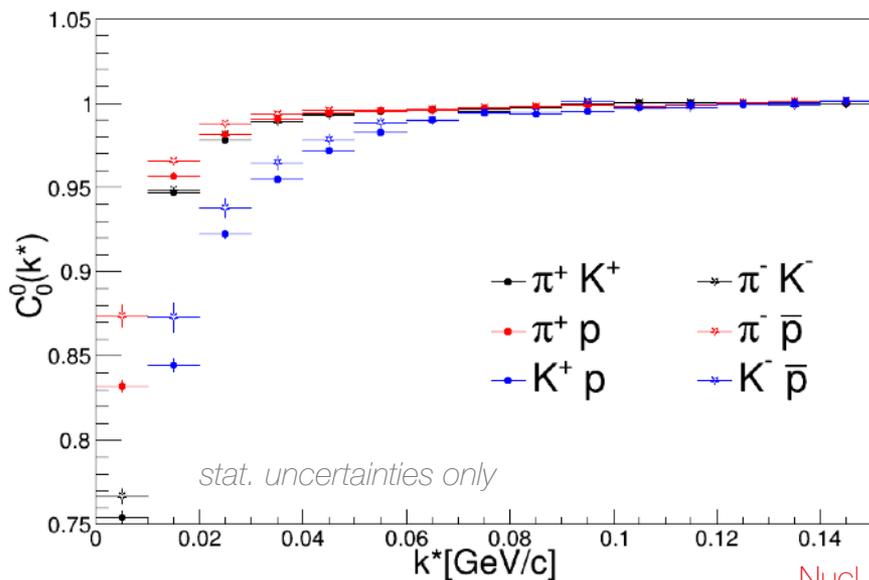
$\pi - K$: Au+Au 0-10 %



energy	$R_{inv} p - p$ [fm]	$R_{inv} p - \bar{p}$ [fm]
7.7 GeV	$3.59 \pm 0.16 \pm 0.19$	
11.5 GeV	$3.66 \pm 0.08 \pm 0.05$	$3.30 \pm 0.42 \pm 0.28$
19.6 GeV	$3.82 \pm 0.15 \pm 0.06$	$3.32 \pm 0.25 \pm 0.13$
27 GeV	$3.80 \pm 0.12 \pm 0.08$	$3.49 \pm 0.25 \pm 0.16$
39 GeV	$4.00 \pm 0.15 \pm 0.02$	$3.39 \pm 0.12 \pm 0.14$

Dependence on interacting **system**

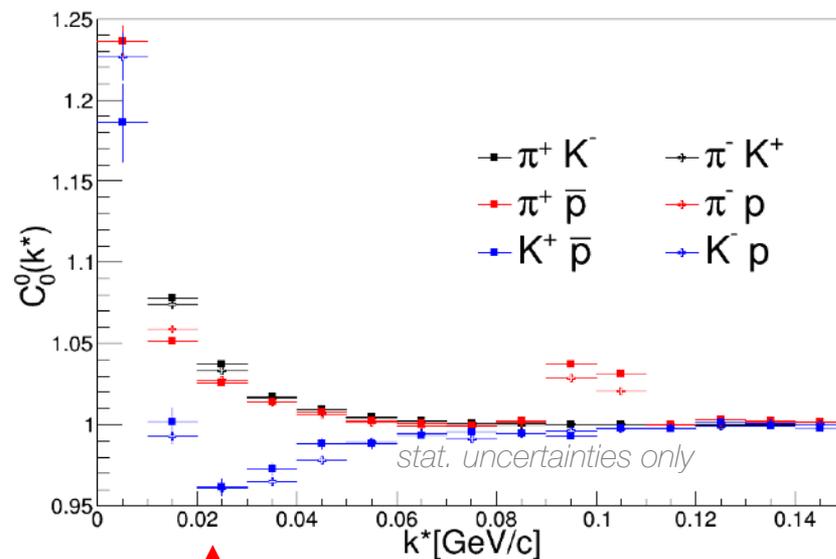
Same charges 0-10% @ Au+Au 39 GeV



Nucl. Phys. A 982 (2019),
359-362

Determined by **Coulomb** Interactions

Opposite charges 0-10% @ Au+Au 39 GeV



$C_0^0(K-p)$ different shape due to strong interaction

Determined by full **FSI: Coulomb** and **Strong** interactions (kaon-proton)

Spherical harmonics

$$C(q) = \sum_{l,m} C_l^m(q) Y_l^m(\theta, \phi)$$

$$C_l^m(q) = \int_{\Omega} C(q, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

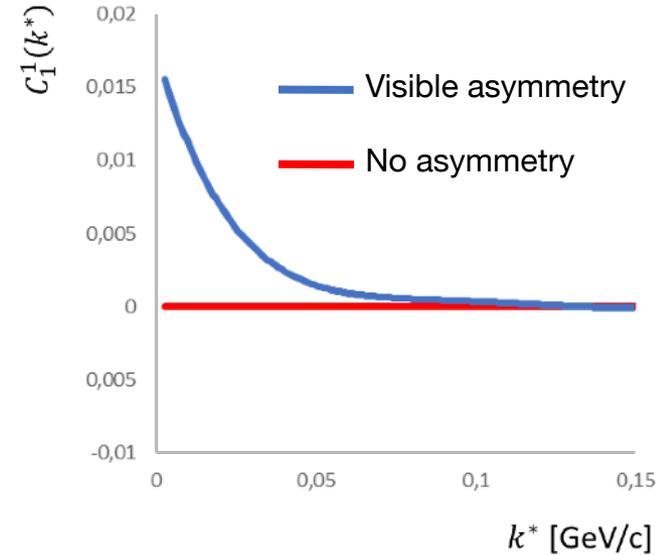
Ω – full solid angle

$Y_l^m(\theta, \phi)$ – spherical harmonic function

$q = |\mathbf{q}|, \theta, \phi$ – spherical coordinates

C00 → source size

C11 → space-time asymmetry

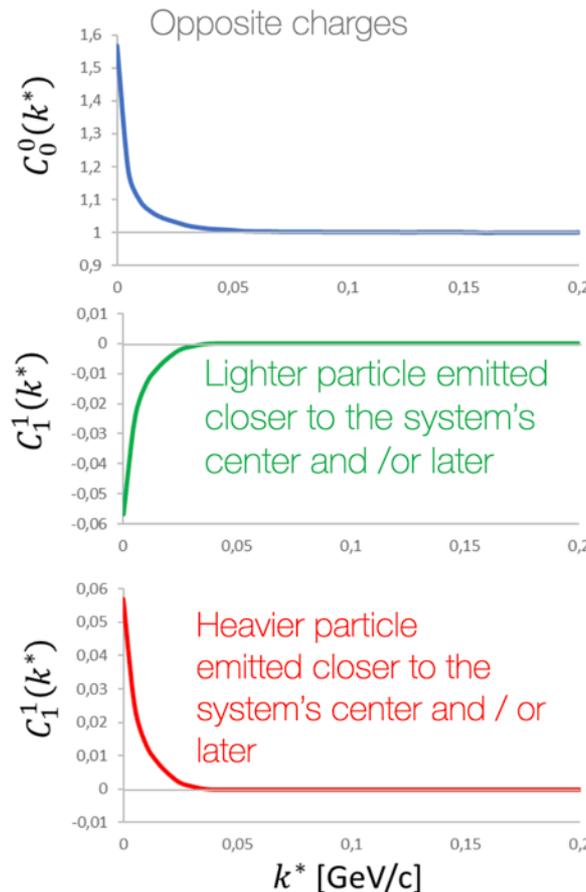
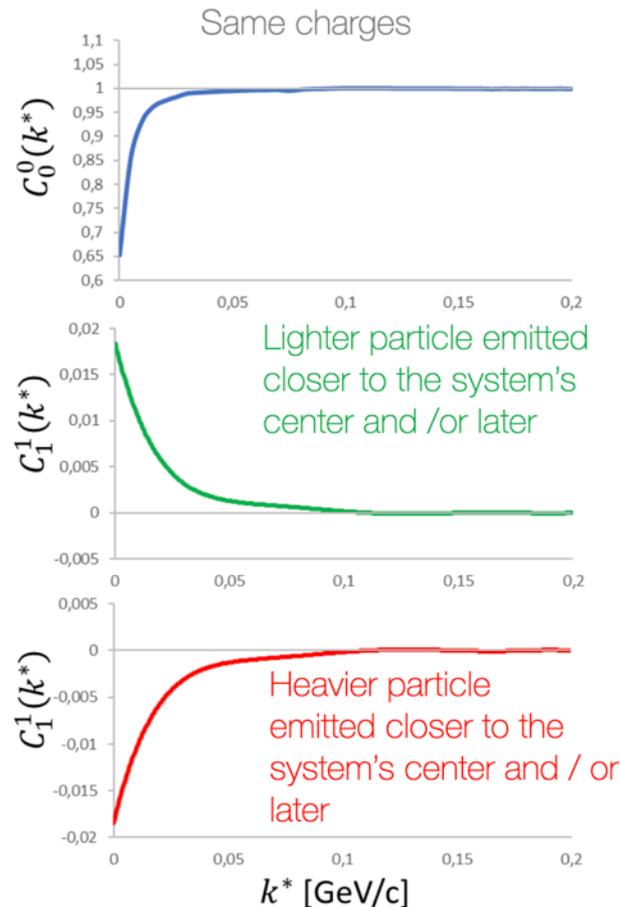


P. Danielewicz and S.Pratt.
Phys. Lett. B618: 60 2005

P. Danielewicz and S.Pratt.
Phys. Rev. C75:034907 2007

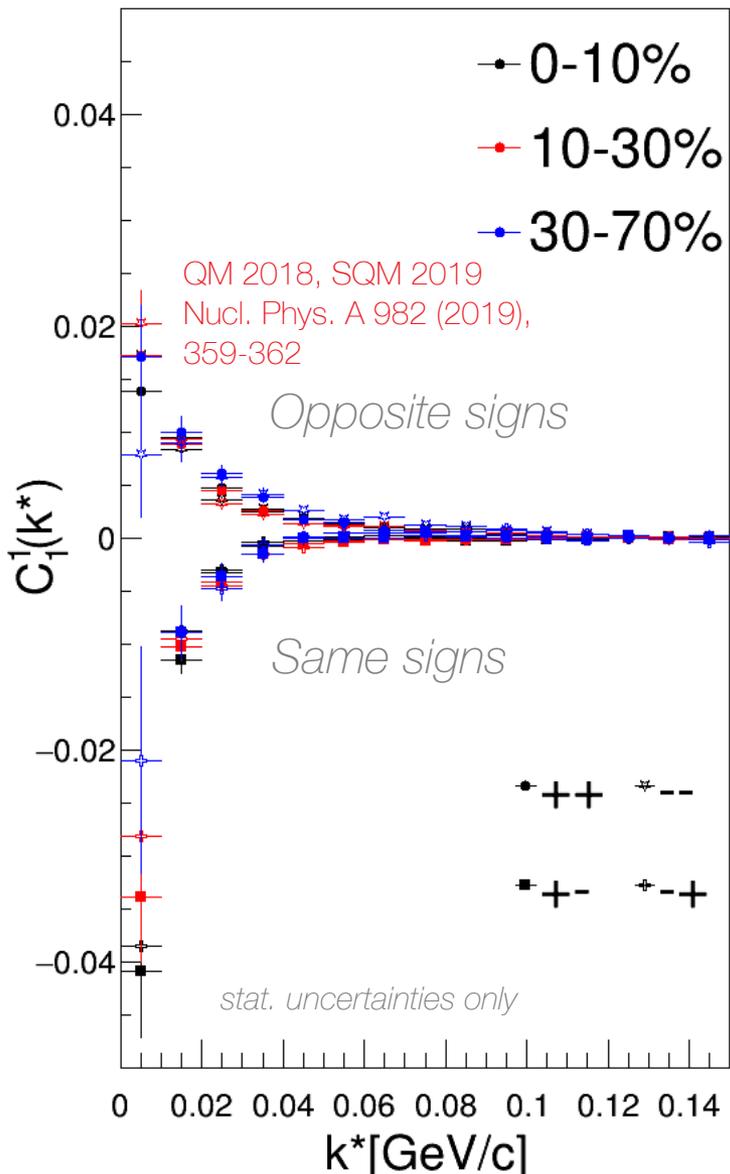
A. Kisiel
Phys. Rev. C81:064906 2010

A. Kisiel and D. A. Brown
Phys. Rev. C80:064911 2009



Source dynamics: **centrality** and **energy** dependencies

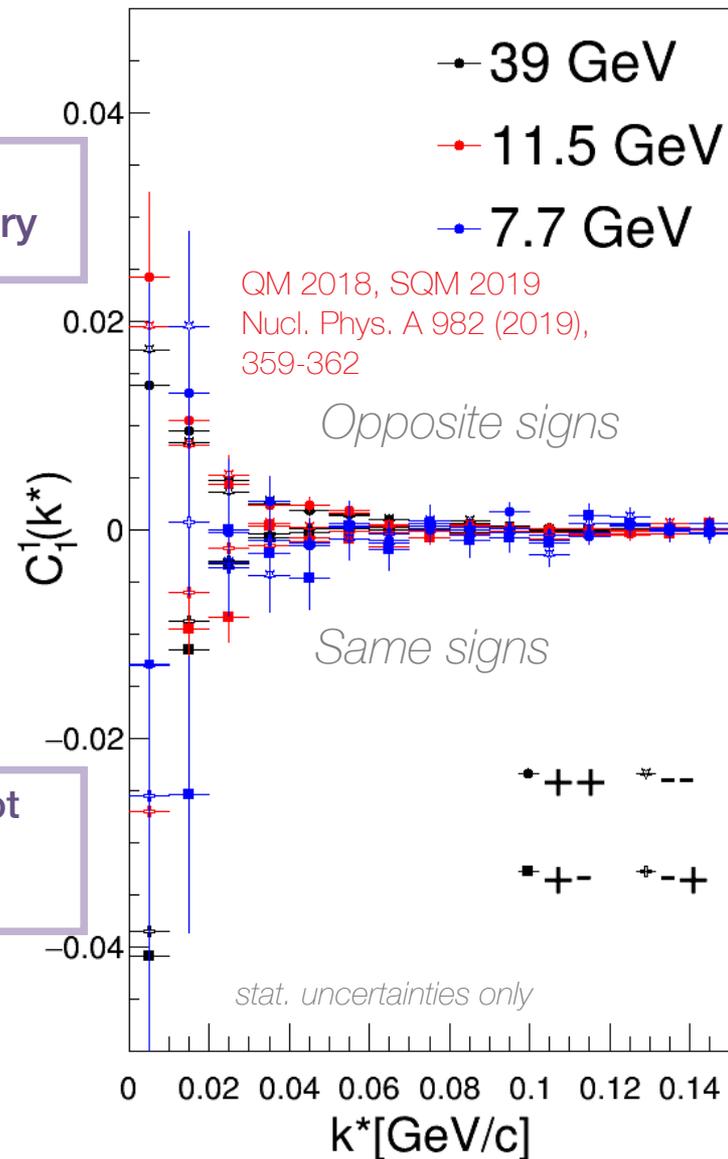
$\pi - K$ @ Au+Au 39 GeV



Clear signal of emission asymmetry

Asymmetry does not disappear in lower energies

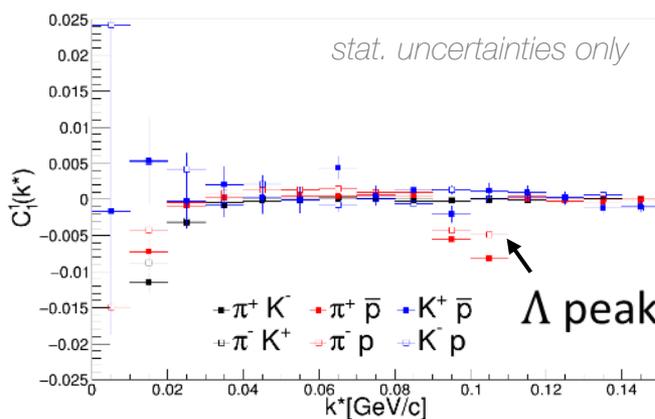
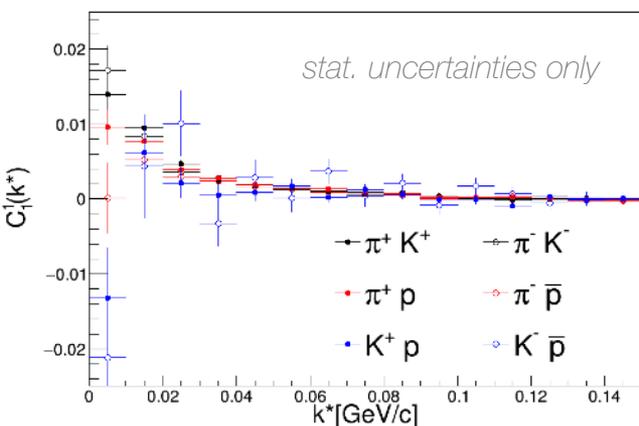
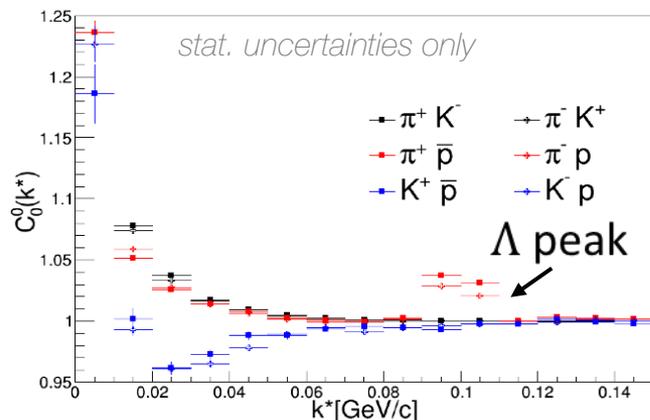
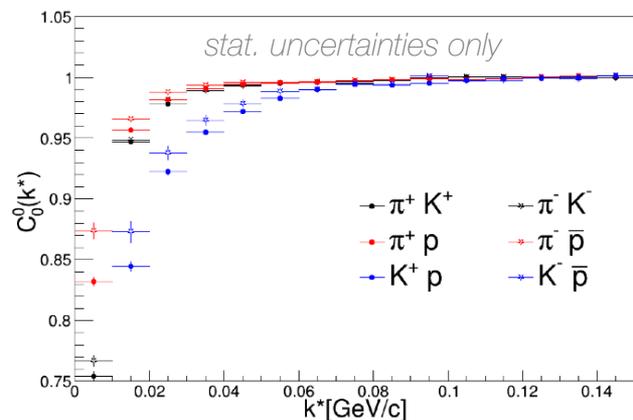
$\pi - K$: Au+Au 0-10%



Source dynamics: **system** dependence

Like-sign 0-10% @ Au+Au 39 GeV

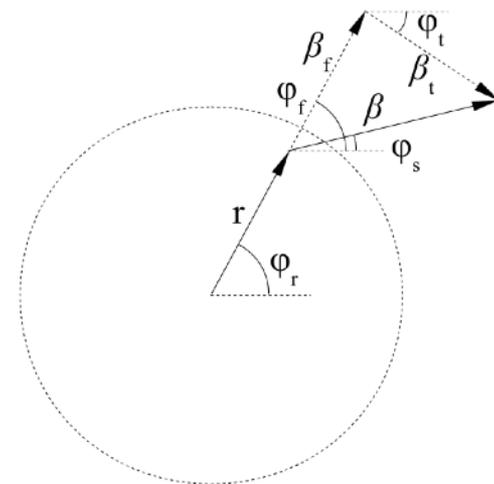
Unlike-sign 0-10% @ Au+Au 39 GeV



Heavier particles directed towards edge of the source.

Heavier particles freeze-out earlier

Phys. Rev. C81:064906 2010



$$\langle x_{out} \rangle = \frac{\langle r \beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0 \beta_0 \beta}{\beta_0^2 + T/m_t}$$

β_f - the same for both particles

$\beta_t \sim 1/m_T$ - smaller for heavier particles

QM 2018, SQM 2019
Nucl. Phys. A 982 (2019),
359-362



Conclusions & Summary

Summary

Correlation **femtoscscopy** probes the system:

- **interaction:**

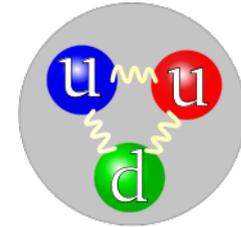
- First attempt to determine strong forces responsible for binding anti-nuclei;
- A quantitative verification of matter-antimatter symmetry (forces responsible for the binding of anti-nuclei);
- Strong interaction between strange (Λ , Ω) particles is investigated;

- **geometry:**

- Pure geometrical information: source parametrized in 3D space (out-side-long), also seen w.r.t. reaction plane;
- Source's lifetime, particle duration, temperature of kinetic freeze-out, etc..;

- **dynamics:**

- emission sequence (particle of which type is emitted earlier or later);
- collectivity seen through homogeneity region.



Thank you for Your attention