





Lepton Flavor Violation at the LHC

Olcyr Sumensari

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Based on [Angelescu, Faroughy, OS. 2002.05684]

Outline:

- Motivation
- Probing flavor at high-p_T
- Low vs. high-energy probes of LFV

Flavor physics

- Gauge sector of the SM entirely fixed by symmetry:
 - \Rightarrow Only a handful of parameters.

3+2 parameters (flavor symmetric)

$$\mathcal{L}_{SM} = \mathcal{L}_{gauge} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yuk}$$

- Flavor sector loose:
 - → 13 parameters (masses and quark mixing) fixed by data.

$$M_{u,d,e} = \left(egin{array}{cccc} & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & &$$

⇒ Striking hierarchy [does not look accidental...]. Hints of a flavor theory?

Our goal: Search for signals of BSM flavor dynamics in precision observables.

LFV is a very clean probe of New Physics:

Forbidden in the SM by an accidental symmetry: $U(1)_e \times U(1)_\mu \times U(1)_\tau$

... which **must be broken** (neutrinos oscillate)! But LFV rates in charged processes are **unobservable** if there is no new dynamics beyond m_{ν_i} (since $\Delta m_{\nu_i}^2 \ll m_W^2$).

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Experimental prospects are very **promising**:

Leptonic probes: Belle-II, COMET, Mu2E, MEG2...

$$\mu \to e\gamma \qquad \mu \to 3e$$

$$\tau \to e\gamma \qquad \tau \to 3\mu \qquad \mu N \to eN$$

$$\tau \to \mu \gamma \qquad \dots$$

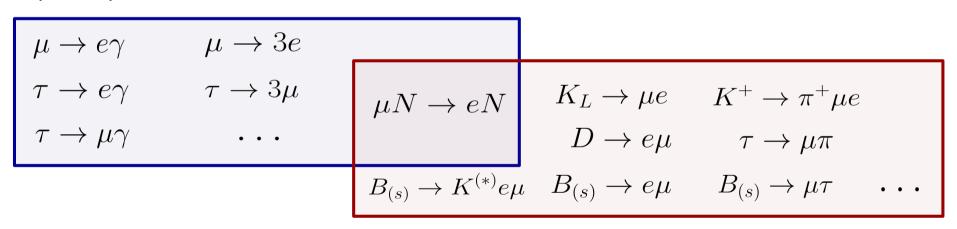
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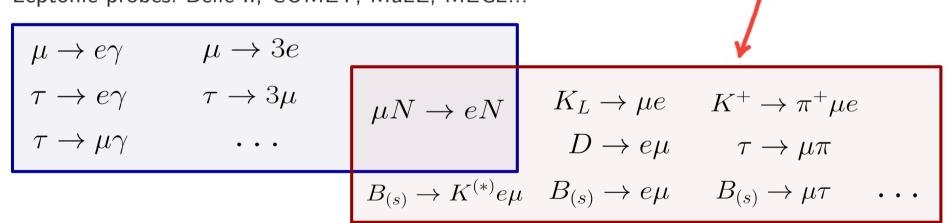
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Hadronic probes: NA62, KOTO, BES-III, LHCb, Belle-II...

LHC can be **useful** here too!

This talk: Constraining **LFV** with $pp \to \ell_i \ell_j$ at **high-p**_T

Lepton Flavor Universality (LFU)

A further motivation... See talks by Amhis, Benito, Borsato, Garcia, Georg, Gerick, Neshatpour, Soni...

Renewed interest on by discrepancies observed in B-hadron decays:

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \to D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \to D^{(*)} \ell \bar{\nu})} \& R_{D^{(*)}}^{\exp} > R_{D^{(*)}}^{\text{SM}}$$

See also:

$$R_{J/\psi}$$

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \to K^{(*)} \mu \mu)}{\mathcal{B}(B \to K^{(*)} ee)} \bigg|_{q^2 \in [q_{\min}^2, q_{\max}^2]} \& R_{K^{(*)}}^{\exp} < R_{K^{(*)}}^{\text{SM}}$$

 R_{pK}

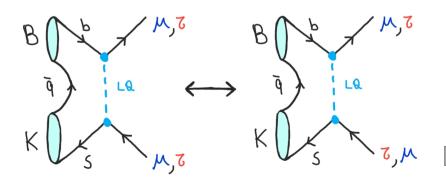
⇒ Flavorful New Physics at the O(TeV) scale?

See talk by Becirevic

LFUV

 Lepton Flavor Violation?

[Glashow et al. '14]



Large effects in $b \to s\mu\tau$ is a prediction of the viable New Physics explanations.

[Angelescu, Becirevic, Faroughy, **OS**, '18]

[Bordone et al. '18], [Di Luzio et al. '18], [Crivellin et al. '20]

LHC is a flavorful experiment

LHC collides five quark-flavors:

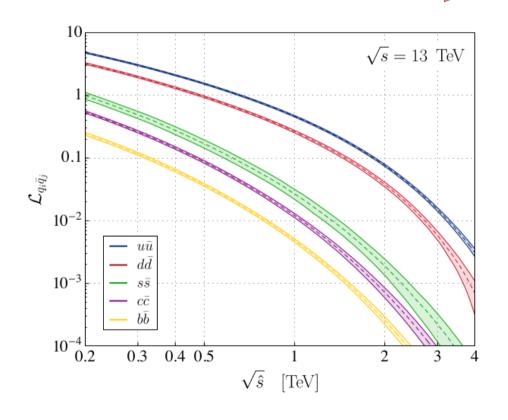
 $\sigma(pp \to \ell\ell') = \sum_{ij} \int \frac{\mathrm{d}\tau}{\tau} \mathcal{L}_{q_i \bar{q}_j}(\tau) \,\hat{\sigma}(q_i \bar{q}_j \to \ell\ell')_{\hat{s}=s\tau} \qquad \hat{s} = m_{\ell\ell'}^2$

Partonic cross-section

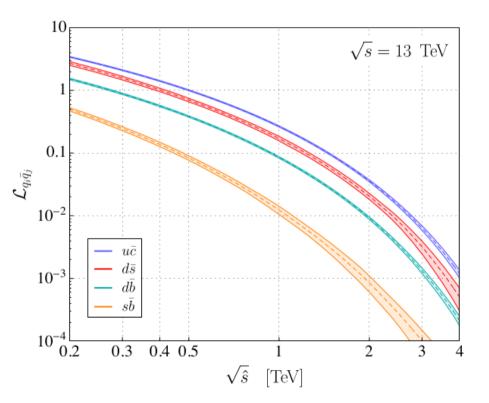
$$\tau = \hat{s}/s$$
$$\hat{s} = m_{\ell\ell'}^2$$

$$\sqrt{s} = 13 \text{ TeV}$$

Parton luminosities:

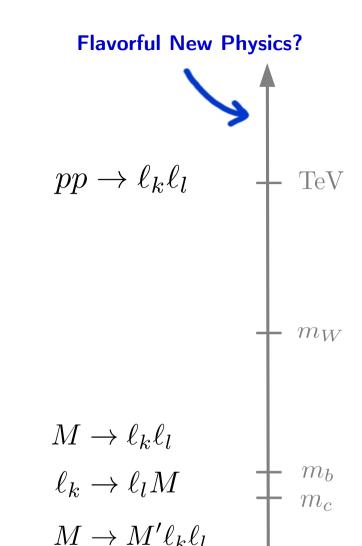


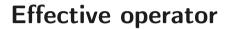


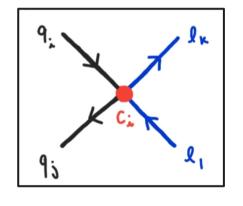


[PDF4LHC15 nnlo mc]

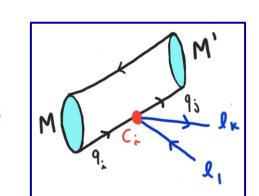
Low vs. high-energy searches







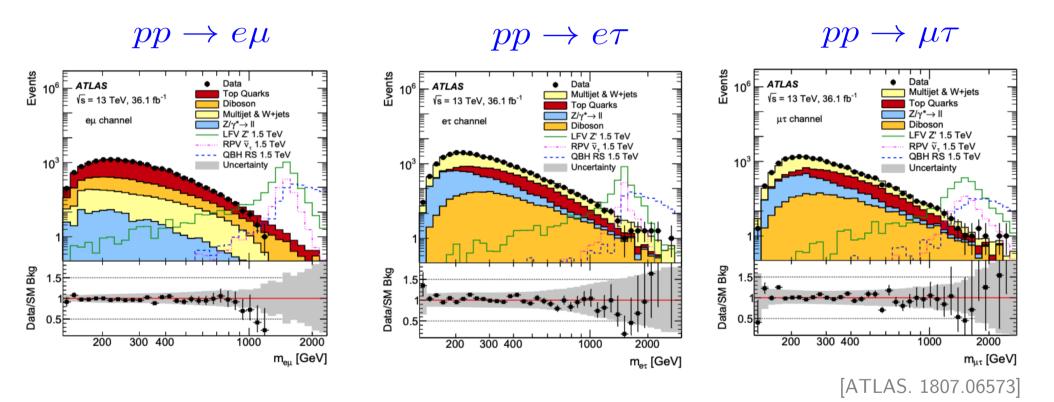




High-p_T searches (CMS and ATLAS) can probe the same operators directly constrained

Strategy

Recast LFV di-lepton searches and look for New Physics effects in the tails of the invariant mass-distribution (where S/B is large).



Dimension-6 operators:

$$\mathcal{L}_{\mathrm{eff}} \supset \frac{C_{\mathrm{eff}}}{\Lambda^2} \mathcal{O}^{(6)} \stackrel{(s \ll \Lambda)}{\Longrightarrow} \sigma \propto \frac{s}{\Lambda^4} |C_{\mathrm{eff}}|^2$$

Energy-growth can overcome heavy-flavor PDF suppression!

Effective Field Theory

(i,j,k,l = flavor indices)

Dimension-6 operators:

$$\mathcal{L} = \sum_{\alpha} \frac{C_{\alpha}}{v^2} \, \mathcal{O}_{\alpha}$$

| | Eff. coeff. | Operator | SMEFT |
|--------|---------------------|--|--|
| | $C_{V_{LL}}^{ijkl}$ | $ig(\overline{q}_{Li}\gamma_{\mu}q_{Lj}ig)ig(ar{\ell}_{Lk}\gamma^{\mu}\ell_{Ll}ig)$ | $\mathcal{O}_{lq}^{(1)}, \mathcal{O}_{lq}^{(3)}$ |
| | $C_{V_{RR}}^{ijkl}$ | $ig(ar{q}_{Ri}\gamma_{\mu}q_{Rj}ig)ig(ar{\ell}_{Rk}\gamma^{\mu}\ell_{Rl}ig)$ | $\mathcal{O}_{ed}, \mathcal{O}_{eu}$ |
| Vector | $C_{V_{LR}}^{ijkl}$ | $\left(\overline{q}_{Li}\gamma_{\mu}q_{Lj} ight)\left(ar{\ell}_{Rk}\gamma^{\mu}\ell_{Rl} ight)$ | ${\cal O}_{qe}$ |
| | $C_{V_{RL}}^{ijkl}$ | $\left(\overline{q}_{Ri}\gamma_{\mu}q_{Rj} ight)\left(ar{\ell}_{Lk}\gamma^{\mu}\ell_{Ll} ight)$ | $\mathcal{O}_{lu}, \mathcal{O}_{ld}$ |
| Scalar | $C_{S_R}^{ijkl}$ | $(\overline{q}_{Ri}q_{Lj})(\overline{\ell}_{Lk}\ell_{Rl}) + \text{h.c.}$ | \mathcal{O}_{ledq} |
| | $C_{S_L}^{ijkl}$ | $\left(\overline{q}_{Li}q_{Rj} ight)\left(ar{\ell}_{Lk}\ell_{Rl} ight) + \mathrm{h.c.}$ | $\mathcal{O}_{lequ}^{(1)}$ |
| Tensor | C_T^{ijkl} | $(\overline{q}_{Li}\sigma_{\mu\nu}q_{Rj})(\overline{\ell}_{Lk}\sigma^{\mu\nu}\ell_{Rl}) + \text{h.c.}$ | $\mathcal{O}_{lequ}^{(3)}$ |

Effective Field Theory

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Vector

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Scalar

Tensor

Partonic cross-section:

$$\sigma(q_{i}\bar{q}_{j} \to \ell_{k}^{-}\ell_{l}^{+}) = \begin{bmatrix} \hat{s} \\ 144\pi v^{4} \end{bmatrix} \sum_{\alpha} M_{\alpha} |C_{\alpha}|^{2} \qquad M_{\alpha} = \begin{cases} 1, & \alpha = V_{X,Y} \\ \frac{3}{4}, & \alpha = S_{X} \\ 4, & \alpha = T \end{cases}$$

Energy enhancement!

Overall factors (no interference!):

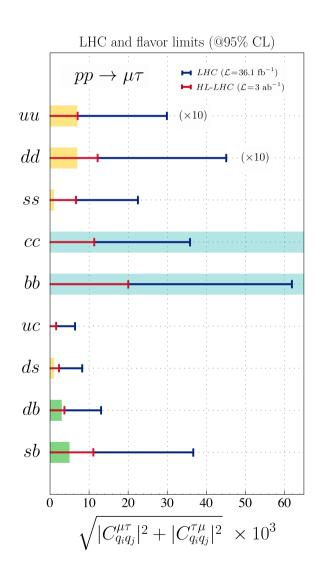
$$M_{lpha} = egin{cases} 1 \,, & & lpha = V_{X,Y} \ rac{3}{4} \,, & & lpha = S_X \ 4 \,, & & lpha = T \end{cases}$$

Limits on different operators are related via the M_{α} coefficients.

(see back-up for full expressions)

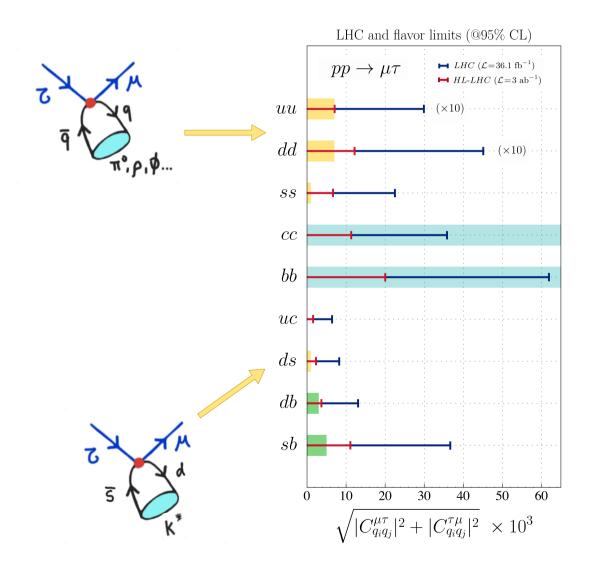
Flavor vs. LHC

Benchmark scenario:
$$\mathcal{L}_{\text{eff}} = \sum \frac{C_{q_i q_j}^{\ell_k \ell_l}}{v^2} \left(\bar{q}_{Li} \gamma^{\mu} q_{Lj} \right) \left(\bar{\ell}_{Lk} \gamma_{\mu} \ell_{Ll} \right)$$



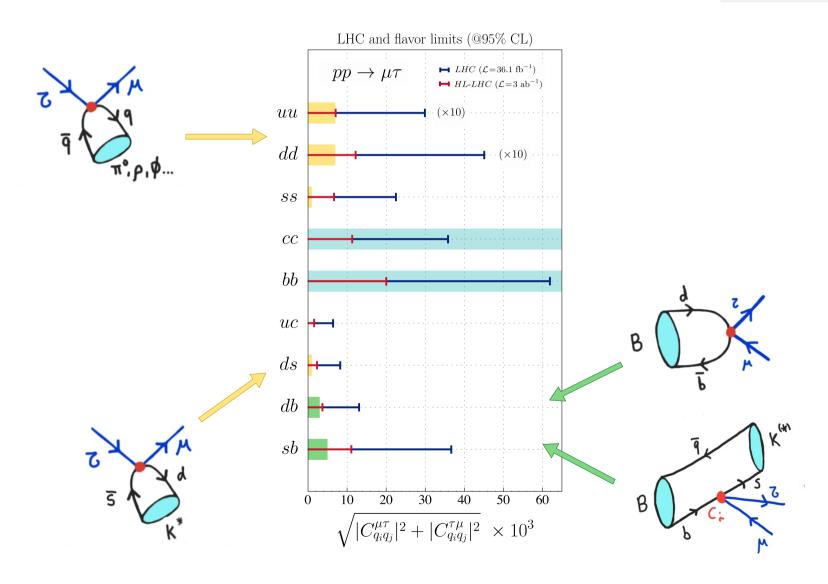
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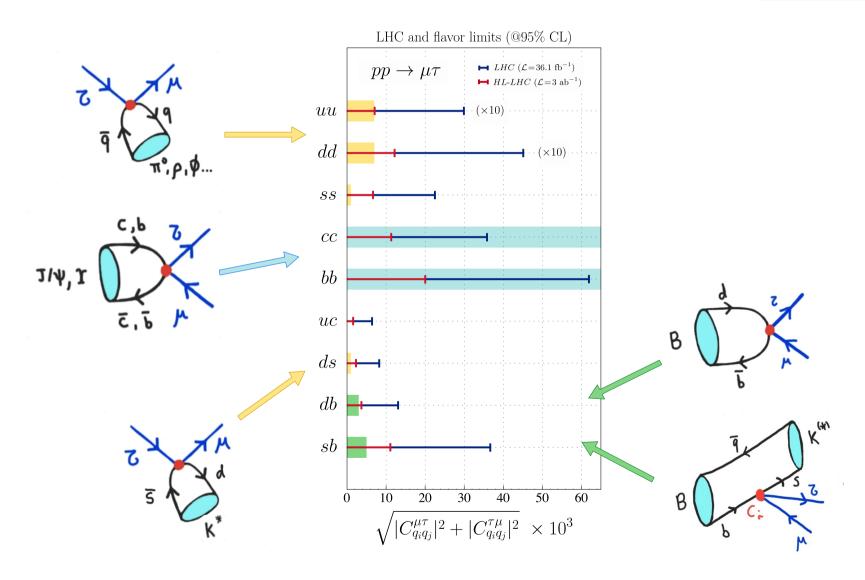
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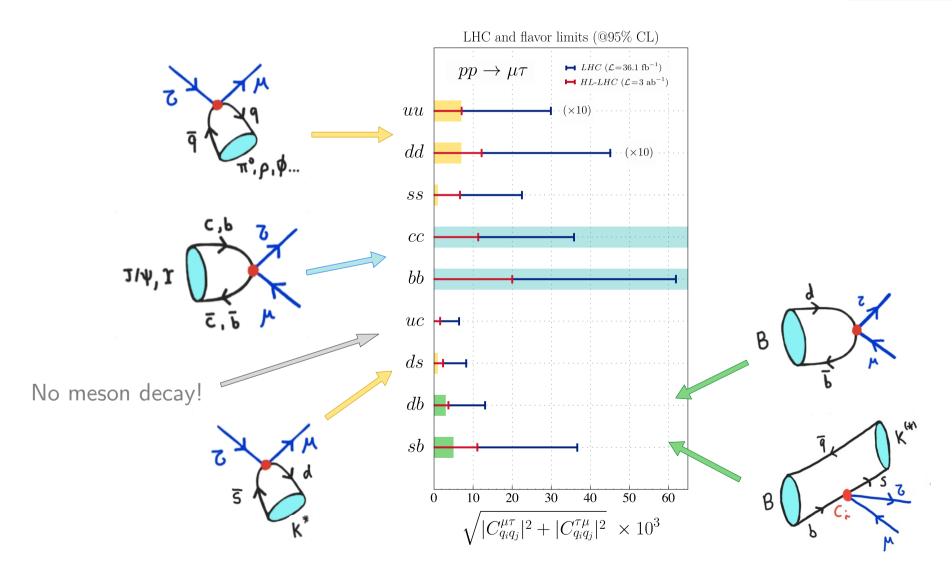
Flavor vs. LHC

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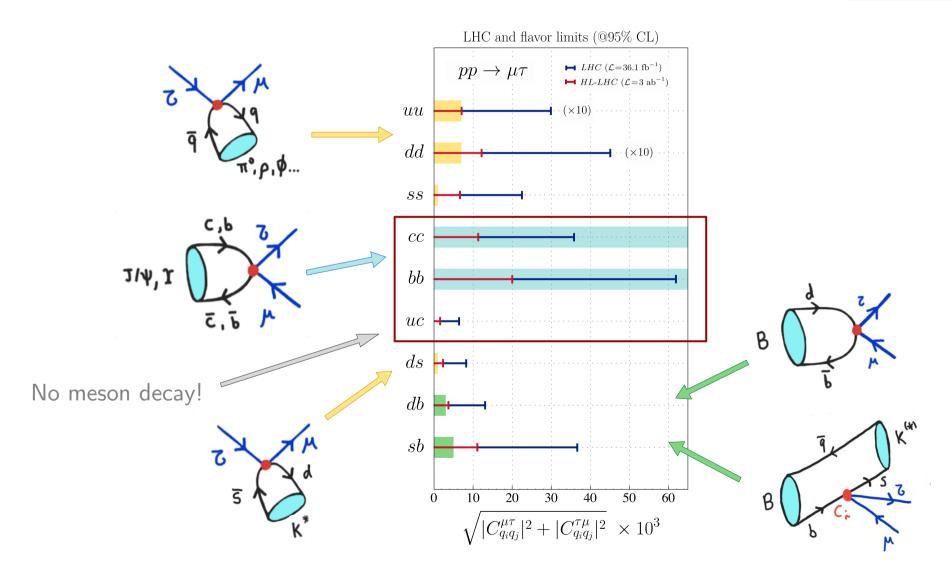
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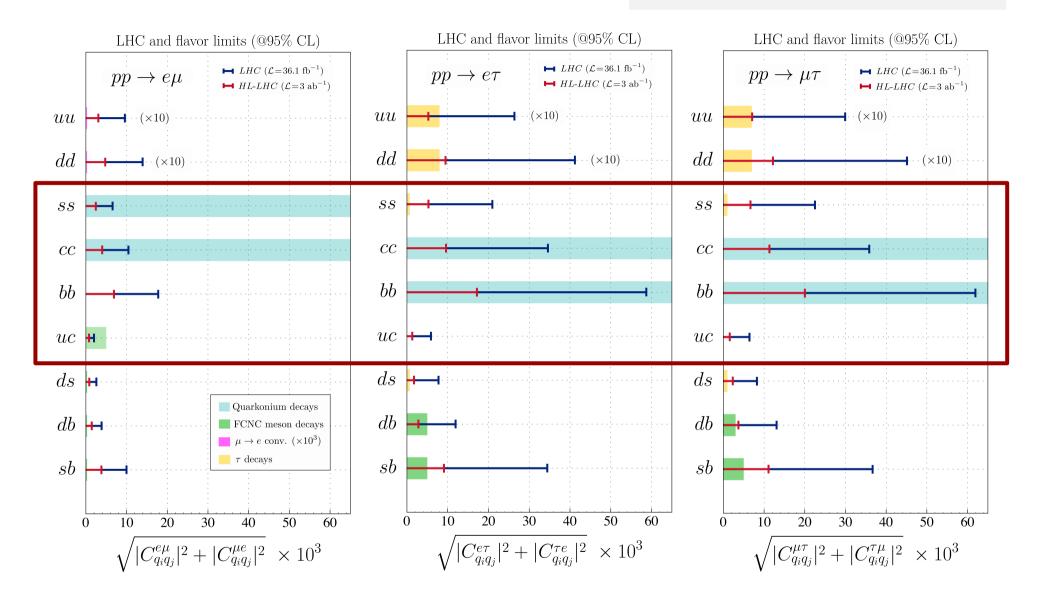
(i.e. $O_{V_{LL}}$)



Low and high-energy observables are complementary!

Our results: $e\mu$, $e\tau$, $\mu\tau$

$$O_{V_{LL}}^{ijkl} = (\bar{q}_{Li}\gamma^{\mu}q_{Lj})(\bar{\ell}_{Lk}\gamma_{\mu}\ell_{Ll})$$

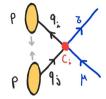


LHC data is **more constraining** for **flavor-conserving** transitions (ss, cc and bb), as well as for the **charm sector** (cu).

Physical observables: $\mu\tau$

$O_{V_{LL}}^{ijkl} = (\bar{q}_{Li}\gamma^{\mu}q_{Lj})(\bar{\ell}_{Lk}\gamma_{\mu}\ell_{Ll})$

Selected results



Our high- p_{τ} constraints

| Decay mode | Current (36 fb^{-1}) | Future (3 ab^{-1}) |
|---|----------------------------------|------------------------------|
| $	au 	o \mu \phi$ | 3.5×10^{-5} | 3.2×10^{-6} |
| $J/\psi \to \tau^{\pm}\mu^{\mp}$ | 6.8×10^{-11} | 6.4×10^{-12} |
| $B_d \to \tau^{\pm} \mu^{\mp}$ | 2.4×10^{-4} | 1.8×10^{-5} |
| $B^+ \to \pi^+ \tau^{\pm} \mu^{\mp}$ | 3.1×10^{-4} | 2.4×10^{-5} |
| $B_s \to \tau^{\pm} \mu^{\mp}$ | 2.9×10^{-3} | 2.5×10^{-4} |
| $B^+ \to K^+ \tau^{\pm} \mu^{\mp}$ | 3.5×10^{-3} | 3.1×10^{-4} |
| $\Upsilon(3S) \to \tau^{\pm} \mu^{\mp}$ | 1.0×10^{-7} | 1.2×10^{-8} |

Direct limits at low-energies

| Decay mode | Exp. limit | Future prospects |
|---|----------------------|------------------------------|
| $	au 	o \mu \phi$ | 1.1×10^{-7} | $\approx 2 \times 10^{-9}$ |
| $J/\psi 	o 	au^{\pm} \mu^{\mp}$ | 2.6×10^{-6} | _ |
| $B_d 	o 	au^{\pm} \mu^{\mp}$ | 1.4×10^{-5} | $\approx 1.3 \times 10^{-5}$ |
| $B^+ \to \pi^+ \tau^{\pm} \mu^{\mp}$ | 9.4×10^{-5} | _ |
| $B_s 	o 	au^{\pm} \mu^{\mp}$ | 4.2×10^{-5} | - |
| $B^+ \to K^+ \tau^{\pm} \mu^{\mp}$ | 6.2×10^{-5} | $\approx 3.3 \times 10^{-6}$ |
| $\Upsilon(3S) \to \tau^{\pm} \mu^{\mp}$ | 4.0×10^{-6} | - |

Take-home:

- High-p_T observables are much more constraining than quarkonia decays!
- LHCb and Belle-II remain the best experiments to look for the decay channels motivated by the *B*-physics anomalies: $B_s \to \mu \tau$ and $B \to K^{(*)} \mu \tau$.

- High-p_T limits can be easily rescaled from vector to scalar/tensor eff. coefficients
 - overall factors of 1, $\frac{3}{4}$ and 4 for the cross-sections (see previous slides).

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- Flavor observables can change significantly though:
 - i. QCD (+EW) RGE effects: [Gonzaléz-Alonso et al., '17], [Feruglio, Paradisi, OS. '18]

e.g.,
$$C_{S_L}(2 \text{ GeV}) \approx 2.1 C_{S_L}(\text{TeV}) - 0.5 C_T(\text{TeV})$$

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ii. Chiral-enhancement at low-energies:

*keeping only two eff. coeffs. for illustration!

e.g.,
$$\mathcal{B}(D^0 \to \mu^- e^+) = \frac{\tau_{D^0} f_D^2 m_{D^0}}{64\pi v^4} \frac{m_\mu^2}{m_\mu^2} \beta_\mu^2 \left| C_{V_{LL}}^{uce\mu} + \frac{m_{D_0}^2}{m_\mu m_c} C_{S_L}^{uce\mu} \right|^2$$

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For this example (LHC vs meson decays):

$$O_{V_{LL}} = (\bar{u}_L \gamma^\mu c_L) (\bar{e}_L \gamma^\mu \mu_L)$$

High-p_T: $|C_{V_{I,I}}^{uce\mu}| \lesssim 2 \times 10^{-3}$

Flavor: $|C_{V_{LL}}^{uce\mu}| \lesssim 5 \times 10^{-3}$

$$O_{S_L} = (\bar{u}_L c_R)(\bar{e}_L \mu_R) + \text{h.c.}$$

High-p_T: $|C_{S_L}^{uce\mu}| \lesssim 2.3 \times 10^{-3}$

Flavor: $|C_{S_L}^{uce\mu}| \lesssim 8 \times 10^{-5}$

Summary and perspectives

• Semileptonic effective operators can modify the tails of $pp \to \ell\ell'$ currently studied at CMS and ATLAS.

PDF suppression can be partially compensated by cross-section energy-growth.

• High- p_T observables are more constraining than flavor experiments for quark-flavor conserving operators (ss, cc, bb) and they are useful in the charm sector (cu).

High- p_{T} searches are complementary to flavor-physics experiments.

Non-resonant high-p_⊤ searches offer plenty of new possibilities for flavor physics:

$$pp o \ell\ell'$$
 $pp o \ell\ell$ $pp o \ell\nu$ [Greljo et al. '17] [Greljo et al. '18] [Fuentes-Martin et al., '20]

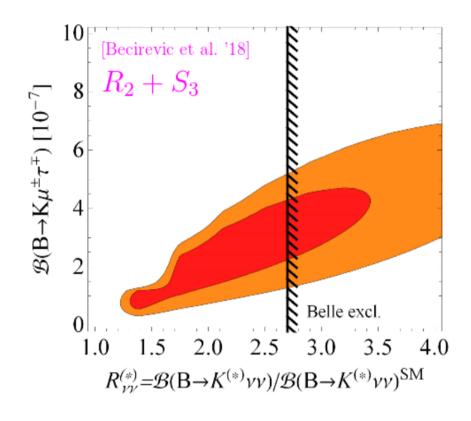
Combining low and high-energy searches is fundamental in the quest for New Physics!

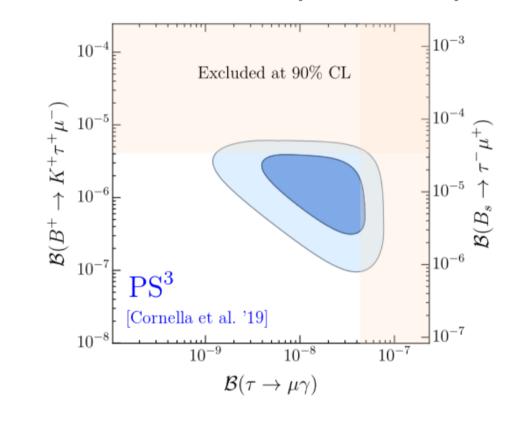
Thank you!

Back-up

From LFUV to LFV

Large effects in $b \to s \mu \tau$ are a common prediction of the minimal solutions to the LFU anomalies [Glashow et al. '14]





i) If purely
$$(V - A) \times (V - A)$$
:

$$\frac{\mathcal{B}(B_s \to \mu \tau)}{\mathcal{B}(B \to K \mu \tau)} \simeq 0.8, \quad \frac{\mathcal{B}(B \to K^* \mu \tau)}{\mathcal{B}(B \to K \mu \tau)} \simeq 1.8 \qquad \frac{\mathcal{B}(B_s \to \mu \tau)}{\mathcal{B}(B \to K^{(*)} \mu \tau)} \gg 1$$

ii) If scalar operators are present:

$$\frac{\mathcal{B}(B_s \to \mu \tau)}{\mathcal{B}(B \to K^{(*)}\mu \tau)} \gg 1$$

[Becirevic, OS, Zukanovich. '16]

New results: $\mathcal{B}(B_s \to \mu^{\pm} \tau^{\mp}) < 4.2 \times 10^{-5}$ $\mathcal{B}(B^+ \to K^+ \mu^- \tau^+) < 4.5 \times 10^{-5}$ [LHCb, '19, '20]

$$\mathcal{B}(B^+ \to K^+ \mu^- \tau^+) < 4.5 \times 10^{-5}$$
 [LHCb,

Partonic cross-section

$$\mathcal{L} = \sum_{\alpha} \frac{C_{\alpha}}{v^2} \, \mathcal{O}_{\alpha}$$

| Eff. coeff. | Operator | SMEFT |
|---------------------|--|--|
| $C_{V_{LL}}^{ijkl}$ | $\left(\overline{q}_{Li}\gamma_{\mu}q_{Lj} ight)\left(\overline{\ell}_{Lk}\gamma^{\mu}\ell_{Ll} ight)$ | $\mathcal{O}_{lq}^{(1)}, \mathcal{O}_{lq}^{(3)}$ |
| $C_{V_{RR}}^{ijkl}$ | $ig(\overline{q}_{Ri} \gamma_{\mu} q_{Rj} ig) ig(ar{\ell}_{Rk} \gamma^{\mu} \ell_{Rl} ig)$ | $\mathcal{O}_{ed}, \mathcal{O}_{eu}$ |
| $C_{V_{LR}}^{ijkl}$ | $ig(ar{q}_{Li}\gamma_{\mu}q_{Lj}ig)ig(ar{\ell}_{Rk}\gamma^{\mu}\ell_{Rl}ig)$ | \mathcal{O}_{qe} |
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| $C_{S_L}^{ijkl}$ | $\left(\overline{q}_{Li}q_{Rj} ight)\left(ar{\ell}_{Lk}\ell_{Rl} ight) + 	ext{h.c.}$ | $\mathcal{O}_{lequ}^{(1)}$ |
| C_T^{ijkl} | $(\bar{q}_{Li}\sigma_{\mu\nu}q_{Rj})(\bar{\ell}_{Lk}\sigma^{\mu\nu}\ell_{Rl}) + \text{h.c.}$ | $\mathcal{O}_{lequ}^{(3)}$ |

$$\frac{d\hat{\sigma}}{d\hat{t}}(q_{i}\bar{q}_{j} \to \ell_{k}^{-}\ell_{l}^{+}) = \frac{(\hat{s}+\hat{t})^{2}}{48\pi v^{4}\hat{s}^{2}} \left\{ \left[|C_{V_{LL}}|^{2} + |C_{V_{LR}}|^{2} + (L \leftrightarrow R) \right] + \frac{\hat{s}^{2}}{4(\hat{s}+\hat{t})^{2}} \left[|C_{S_{L}}|^{2} + |C_{S_{R}}|^{2} \right] + \frac{4(\hat{s}+2\hat{t})^{2}}{(\hat{s}+\hat{t})^{2}} |C_{T}|^{2} - \frac{2\hat{s}(\hat{s}+2\hat{t})}{(\hat{s}+\hat{t})^{2}} \operatorname{Re}\left(C_{S_{L}}C_{T}^{*}\right) \right\}$$

where

$$C_{V_{X,Y}} \to C_{V_{X,Y}}^{ijkl}$$

$$C_{S_X} \to \sqrt{\left|C_{S_X}^{ijkl}\right|^2 + \left|C_{S_X}^{jilk}\right|^2}$$

$$C_T \to \sqrt{\left|C_T^{ijkl}\right|^2 + \left|C_T^{jilk}\right|^2}$$

High-p₊ limits from current (future) LHC data:

$$\sqrt{|C_{q_i q_j}^{\ell_k \ell_l}|^2 + |C_{q_j q_i}^{\ell_l \ell_k}|^2}$$

$$\mathcal{L}_{\text{eff}} = \sum \frac{C_{q_i q_j}^{\ell_k \ell_l}}{v^2} \left(\bar{q}_{Li} \gamma^{\mu} q_{Lj} \right) \left(\bar{\ell}_{Li} \gamma^{\mu} \ell_{Lj} \right)$$

| $C_{ m eff} \left(imes 10^3 ight)$ | $e\mu$ | e	au | $\mu \tau$ |
|---------------------------------------|-----------|-----------|------------|
| uu | 1.0 (0.3) | 2.6 (0.5) | 3.0 (0.7) |
| dd | 1.4 (0.5) | 4.1 (0.9) | 4.5 (1.2) |
| ss | 6.5 (2.4) | 21 (5.3) | 22 (6.7) |
| cc | 10 (4.0) | 35 (9.5) | 36 (11) |
| bb | 18 (6.8) | 59 (17) | 62 (21) |
| uc | 2.0 (0.7) | 5.8 (1.2) | 6.4 (1.6) |
| ds | 2.5 (0.9) | 7.6 (1.7) | 8.2 (2.2) |
| db | 3.9 (1.4) | 12 (2.8) | 13 (3.6) |
| sb | 9.9 (3.7) | 34 (9.0) | 37 (11) |

[Angelescu, Faroughy, OS. '20]