

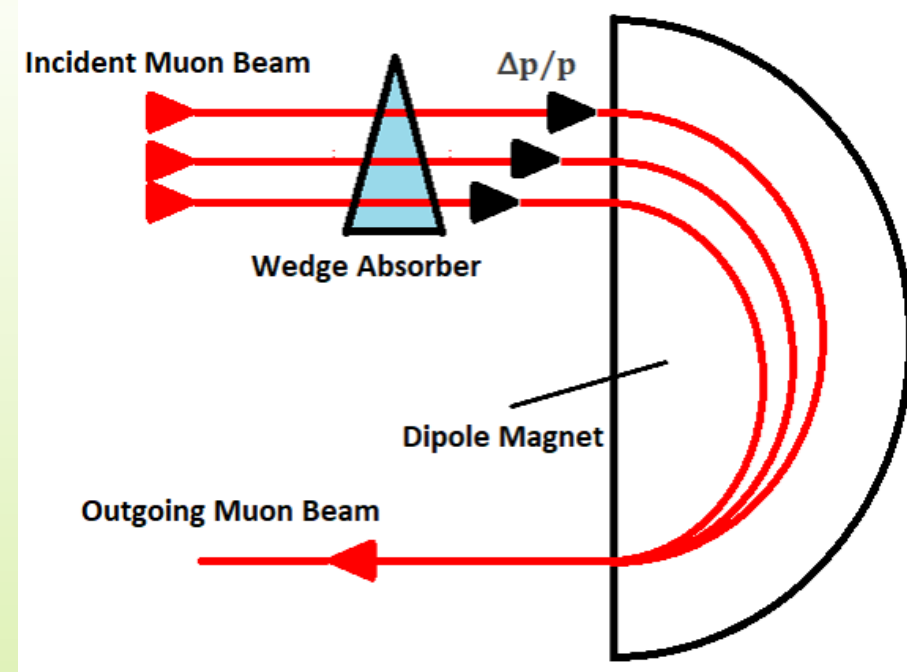
Monte Carlo Simulation of Reverse Emittance Exchange in MICE

Craig Brown, Brunel University, Uxbridge, UK

On behalf of the MICE Collaboration

Reverse Emittance Exchange

- ▶ When produced, **muons occupy large phase-space volume** (their spread in position-momentum space) or conversely the beam has a low phase-space density
- ▶ To create high intensity low-emittance beams **requires cooling** - Ionization cooling only viable process on a shorter timescale than muon lifetime
- ▶ **Ionization Cooling** – muons passed through an **absorber** material (losing momentum) and **then an RF cavity** (restoring longitudinal momentum)

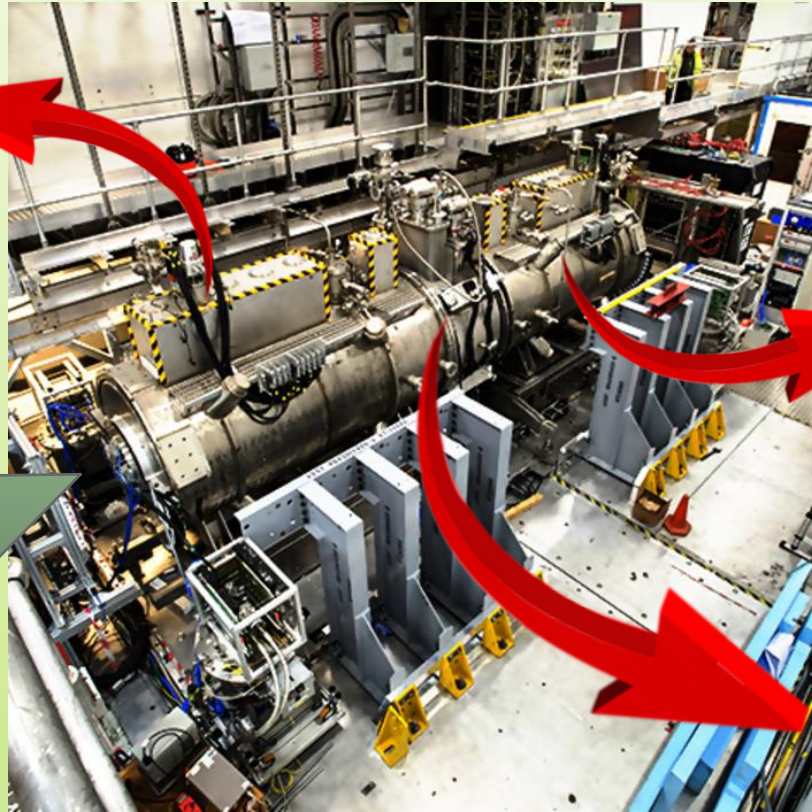


- ▶ **Emittance Exchange** allows **manipulation** of **transverse and longitudinal phase-spaces**
- ▶ In Reverse Emittance Exchange, the beam is passed through a wedge (e.g. lower right picture) creating a position-momentum correlation, and then through a dipole magnet.
- ▶ The resulting beam has a higher transverse phase-space density and lower longitudinal phase-space density
- ▶ **Repeated manipulation** of the beam along **with repeated transverse ionization cooling** increases the phase-space density of the beam allowing for the **creation of a beam of the desired intensity**



Muon Ionization Cooling Experiment (MICE)

Measure muon position and momentum upstream



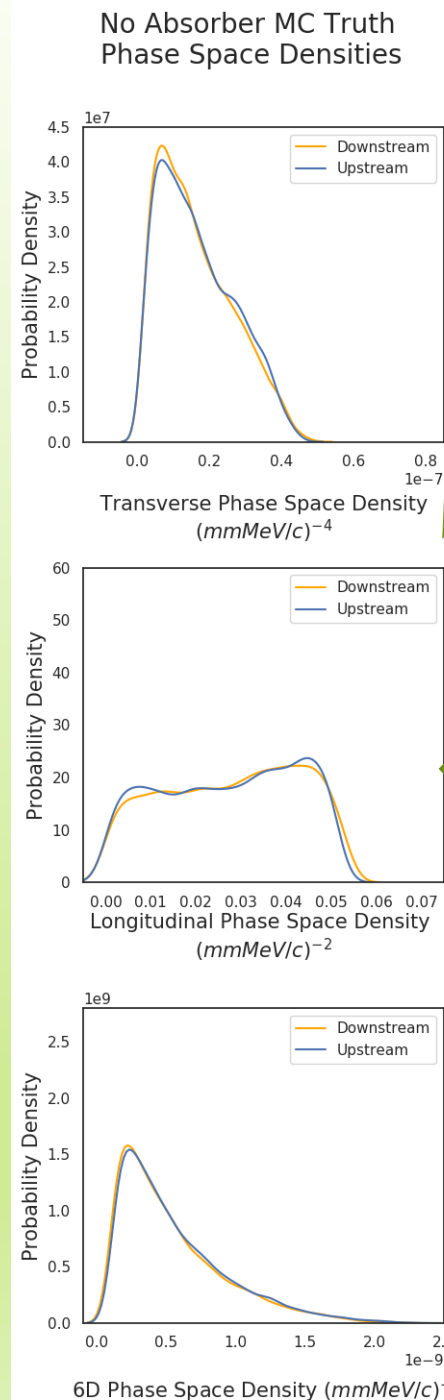
Measure muon position and momentum downstream

Cool the muon beam using LiH, LH₂, or polyethylene wedge absorbers

Beam

Monte Carlo Simulation of Phase-Space Density Change

- ▶ Liouville => Phase-Space density for a distribution of particles remains constant (unless acted upon by a dissipative force)
- ▶ Measure x, y, z, p_x, p_y and p_z upstream and downstream (i.e. before and after wedge)
- ▶ Calculate phase-space density of the beam
- ▶ No Absorber – Conservation of 6D density
- ▶ Wedge – Longitudinal density has been reduced
- ▶ Some biases still need to be taken account of e.g. transmission losses
- ▶ **6D density conservation in No Absorber case** shows this analysis will be able to quantify the cooling performance of the wedge
- ▶ **Future => Apply to MICE data**



No Wedge ←

Wedge →



No Absorber =
Phase-space density
conservation

Wedge = Lower
longitudinal and
6D phase-space
density

