Resummation effects in weak SUSY processes

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Topics of this talk

Features of resummation

- Perturbative expansion and resummation of large logs
- > Threshold resummation at NNLL for Drell-Yan processes.

Slepton pair production at aNNLO+NNLL

Electroweakino pair production at aNNLO+NNLL

- Mostly Higgsino scenario
- Mostly gaugino scenario

Conclusions

Resummation

Features of resummation

- Perturbative expansion and resummation of large logs
- > Threshold resummation at NNLL for Drell-Yan processes.
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- Conclusions

Resummation

Heavy particles will be abundantly produced <u>close to threshold</u> and with small transverse momentum. $\begin{array}{c|c} \alpha_s^n \log^m \left(\frac{M^2}{p_T^2} \right) & \\ \alpha_s^n \frac{\log^m (1-z)}{1-z} & z = M^2/\hat{s} \end{array} \end{array}$

The perturbative expansion can be spoiled by the presence of <u>large logarithmic terms</u> (Sudakov Logs) of the form:

A precise calculation of (differential) cross sections for the production of heavy particles requires a consistent treatment of these terms.

A **resummation** to all orders of the large logarithmic contributions is possible through a transformation in Mellin space.

Calulation of LO, NLO, NLO+NLL and aNNLO+NNLL cross sections for SUSY processes are performed using the **RESUMMINO** pacakge.

G. Bozzi, B. Fuks, and M. Klasen, Phys. Rev. D 74, (2006) 015001 Nucl. Phys. B 794, (2007) 46 Nucl. Phys. B 777, (2007) 157-181 J. Debove, B. Fuks, and M. Klasen, Phys. Lett. B 688, (2010) 208 Nucl. Phys. B 842, (2011) 51 Nucl. Phys. B 849, (2011) 64

B. Fuks, M. Klasen, D. R. Lamprea, M. Rothering, JHEP 1210, (2012) 081 Eur. Phys. J. C73, (2013) 2480

Y. L. Dokshitzer, D. Diakonov, and S. I. Troian, Phys. Rept. 58, (1980) 269

> S. Catani and L. Trentadue, Nucl. Phys. B 327 (1989) 323

Resummation

Switch to Mellin space:

$$F(N) = \int_0^1 dy \, y^{N-1} F(y) \qquad \qquad \left[\frac{\ln^m (1-z)}{1-z} \right]_+ \to \ln^{m+1} N + \dots$$

Here the cross section factorizes:

$$\sigma_{ab}^{(\text{res.})}(N, M^2, \mu_R^2, \mu_F^2) = H_{ab}(M^2, \mu_R^2, \mu_F^2) \exp[G_{ab}(N, M^2, \mu_R^2, \mu_F^2)] + \mathcal{O}\left(\frac{1}{N}\right)$$
Hard function:
Independent of N,
but process dependent
$$G_{ab}(N, M^2, \mu_R^2, \mu_F^2) = LG_{ab}^{(1)}(\lambda) + G_{ab}^{(2)}(\lambda, M^2, \mu_R^2, \mu_F^2) + \alpha_s G_{ab}^{(3)}(\lambda, M^2, \mu_R^2, \mu_F^2)$$
Leading Log (LL)
$$Next-to-Leading$$

$$Leading Log (LL)$$

$$Next-to-Leading$$

$$Log (NLL)$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Leading$$

$$Next-to-Next-to$$

$$Leading Log (NLL)$$

Terms in the exponent only depend on the initial state.

For Drell-Yan processes under analysis, we only have quark-antiquark initial state.

 $G_{ab}^{(i)} = g_a^{(i)} + g_b^{(i)}$

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Resummation at NNLL

Necessary ingredient for NNLL resummation:

with $\lambda = \alpha_s b_0 L$ and $L = \ln \overline{N} = \ln (N e^{\gamma_E})$

$$g_{q}^{(3)}(\lambda) = \frac{A^{(1)}b_{1}^{2}}{2\pi b_{0}^{4}} \frac{1}{1-2\lambda} \Big[2\lambda^{2} + 2\lambda \ln(1-2\lambda) + \frac{1}{2}\ln^{2}(1-2\lambda) \Big] \qquad \lambda = \alpha_{s}b_{0}L \text{ and } L = \ln \bar{N} = \ln(Ne^{\gamma_{L}} + \frac{A^{(1)}b_{2}}{2\pi b_{0}^{3}} \Big[2\lambda + \ln(1-2\lambda) + \frac{2\lambda^{2}}{1-2\lambda} \Big] + \frac{2A^{(1)}}{\pi} \zeta_{2} \frac{\lambda}{1-2\lambda} - \frac{\lambda}{2\pi^{2}b_{0}} \frac{\lambda}{1-2\lambda} - \frac{A^{(2)}b_{1}}{(2\pi)^{2}b_{0}^{3}} \frac{1}{1-2\lambda} \Big[2\lambda^{2} + 2\lambda + \ln(1-2\lambda) \Big] + \frac{A^{(3)}}{\pi^{3}b_{0}^{2}} \frac{\lambda^{2}}{1-2\lambda} - \frac{D^{(2)}}{2\pi^{2}b_{0}} \frac{\lambda}{1-2\lambda} + \frac{A^{(1)}b_{1}}{2\pi b_{0}^{2}} \frac{1}{1-2\lambda} \Big[2\lambda + \ln(1-2\lambda) \Big] \ln \left(\frac{M^{2}}{\mu_{R}^{2}}\right) + \frac{A^{(1)}}{2\pi} \Big[\frac{\lambda}{1-2\lambda} \ln^{2} \left(\frac{M^{2}}{\mu_{R}^{2}}\right) - \lambda \ln^{2} \left(\frac{\mu_{F}^{2}}{\mu_{R}^{2}}\right) \Big] - \frac{A^{(2)}}{2\pi^{2}b_{0}} \Big[\frac{\lambda}{1-2\lambda} \ln \left(\frac{M^{2}}{\mu_{R}^{2}}\right) - \lambda \ln \left(\frac{\mu_{F}^{2}}{\mu_{R}^{2}}\right) \Big]$$
A. Vogt.
Phys. Lett. B497 (2001) 228-234

$$\begin{aligned} A^{(1)} &= 2C_F, \\ A^{(2)} &= 2C_F \left[C_A \left(\frac{67}{18} - \zeta_2 \right) - \frac{5}{9} n_f \right], \\ A^{(3)} &= \frac{1}{2} C_F \left[C_A^2 \left(\frac{245}{24} - \frac{67}{9} \zeta_2 + \frac{11}{6} \zeta_3 + \frac{11}{5} \zeta_2^2 \right) + C_F n_f \left(2\zeta_3 - \frac{55}{24} \right) \right. \\ &+ C_A n_f \left(\frac{10}{9} \zeta_2 - \frac{7}{3} \zeta_3 - \frac{209}{108} \right) - \frac{n_f^2}{27} \right] \end{aligned}$$

$$D^{(2)} = 2C_F \left[C_A \left(-\frac{101}{27} + \frac{11}{3}\zeta_2 + \frac{7}{2}\zeta_3 \right) + n_f \left(\frac{14}{27} - \frac{2}{3}\zeta_2 \right) \right]$$

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Resummation at NNLL

Hard matching coefficients:

 $H_{ab}(M^2, \mu_R^2, \mu_F^2) = \sigma_{ab}^{(0)} \mathcal{C}_{ab}(M^2, \mu_R^2, \mu_F^2) \quad \nabla$

They can be expanded as:

$$\mathcal{C}_{ab}^{(n)}(M^2,\mu_R^2,\mu_F^2) = \left(\frac{2\pi}{\alpha_s}\right)^n \left[\frac{\sigma_{ab}^{(n)}}{\sigma_{ab}^{(0)}}\right]_{\text{N-ind}}$$

with
$$\mathcal{C}_{ab}(M^2, \mu_R^2, \mu_F^2) = \sum_{n=0}^{\infty} \left(\frac{\alpha_s}{2\pi}\right)^n \mathcal{C}_{ab}^{(n)}(M^2, \mu_R^2, \mu_F^2)$$

NNLO DY cross section from literature: N. Kidonakis, Int.J.Mod.Phys. A19 (2004) 1793-1821 N. Kidonakis, Phys.Rev. D77 (2008) 053008

By their means, we can easily obtain the n-th order cross section in Mellin space:

$$\begin{aligned} \mathcal{C}_{ab}^{(0)} &= 1, \\ \mathcal{C}_{ab}^{(1)} &= C_F \left[\frac{4}{3} (\pi^2 - 6) - 3 \log \left(\frac{\mu_F^2}{M^2} \right) \right], \\ \mathcal{C}_{ab}^{(2)} &= \frac{C_F}{720} \bigg\{ 5 (-4605C_A + 4599C_F + 762n_f) + 20\pi^2 (188C_A - 297C_F - 32n_f) \\ &- 92\pi^4 (C_A - 6C_F) + 180 (11C_A + 18C_F - 2n_f) \log^2 \left(\frac{\mu_F^2}{M^2} \right) \\ &- 160 (11C_A - 2n_f) (6 - \pi^2) \log \left(\frac{\mu_R^2}{M^2} \right) + 80 (151C_A - 135C_F + 2n_f) \zeta_3 \\ &+ 20 \log \left(\frac{\mu_F^2}{M^2} \right) \bigg[- 51C_A + 837C_F + 6n_f - 4\pi^2 (11C_A + 27C_F - 2n_f) \\ &+ (-198C_A + 36n_f) \log \left(\frac{\mu_R^2}{M^2} \right) + 216 (C_A - 2C_F) \zeta_3 \bigg] \bigg\} \end{aligned}$$

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Resummation at NNLL

Next step requires the matching of resummed and fixed order results to avoid double counting:

$$\begin{split} \sigma_{ab} &= \sigma_{ab}^{(\text{res.})} + \sigma_{ab}^{(\text{f.o.})} - \sigma_{ab}^{(\text{exp.})} \\ \text{Expand the resummed cross section at given fixed order:} \\ \sigma_{ab}^{(\text{exp.})}(N, M^2, \mu_R^2, \mu_F^2) &= \sigma_{ab}^{(0)} \mathcal{C}_{ab}(M^2, \mu_R^2, \mu_F^2) \exp[G_{ab}(N, M^2, \mu_R^2, \mu_F^2)] \\ &= \sigma_{ab}^{(0)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \mathcal{C}_{ab}^{(1)} + \left(\frac{\alpha_s}{2\pi}\right)^2 \mathcal{C}_{ab}^{(2)} + \dots \right] \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \mathcal{K}^{(1)} + \left(\frac{\alpha_s}{2\pi}\right)^2 \mathcal{K}^{(2)} + \dots \right] \\ &= \sigma_{ab}^{(0)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(1)} \right) + \left(\frac{\alpha_s}{2\pi}\right)^2 \left(\mathcal{C}_{ab}^{(2)} + \mathcal{K}^{(2)} + \mathcal{C}_{ab}^{(1)} \mathcal{K}^{(1)} \right) + \dots \right] \\ &= \sigma_{ab}^{(0)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(1)} \right) + \left(\frac{\alpha_s}{2\pi}\right)^2 \left(\mathcal{C}_{ab}^{(2)} + \mathcal{K}^{(2)} + \mathcal{C}_{ab}^{(1)} \mathcal{K}^{(1)} \right) + \dots \right] \\ &= \sigma_{ab}^{(0)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(1)} \right) + \left(\frac{\alpha_s}{2\pi}\right)^2 \left(\mathcal{C}_{ab}^{(2)} + \mathcal{K}^{(2)} + \mathcal{C}_{ab}^{(1)} \mathcal{K}^{(1)} \right) + \dots \right] \\ &= \sigma_{ab}^{(0)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(2)} \right) \right]^2 \left(\mathcal{C}_{ab}^{(2)} + \mathcal{K}^{(2)} + \mathcal{C}_{ab}^{(1)} \mathcal{K}^{(1)} \right) + \dots \right] \\ &= \sigma_{ab}^{(1)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(2)} \right) \right]^2 \left(\mathcal{C}_{ab}^{(2)} + \mathcal{K}^{(2)} + \mathcal{C}_{ab}^{(1)} \mathcal{K}^{(1)} \right) + \dots \right] \\ &= \sigma_{ab}^{(1)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{C}_{ab}^{(1)} + \mathcal{K}^{(2)} \right) \right] \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(1)} \right) \right] \\ &= \sigma_{ab}^{(1)} \left[1 + \left(\frac{\alpha_s}{2\pi}\right) \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \right] \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(1)} \right) \right] \\ &= \mathcal{L}_{ab}^{(1)} \left[1 + \mathcal{L}_{ab}^{(1)} \right] \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(1)} \right) \right] \\ &= \sigma_{ab}^{(1)} \left[1 + \mathcal{L}_{ab}^{(1)} \right] \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \right) \left(\mathcal{L}_{ab}^{(1)} \right) \right] \\ &= \mathcal{L}_{ab}^{(1)} \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(1)} + \mathcal{L}_{ab}^{(2)} \right) \right) \left(\mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(2)} + \mathcal{L}_{ab}^{(2)} \right) \left(\mathcal{L}_{ab}^{(2)} + \mathcal{L}_{ab}^{(2)} \right) \right) \left(\mathcal{L}_{ab}^{(2)} + \mathcal{L}_{ab}^{(2)} \right) \right) \left(\mathcal{L}_{ab}^{(2)} + \mathcal$$

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• Features of resummation

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- > Threshold resummation at NNLL for Drell-Yan processes.

Slepton pair production at aNNLO+NNLL

- Electroweakino pair production at aNNLO+NNLL
 - Mostly Higgsino scenario
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- Conclusions

Slepton signatures



First & second generation sleptons



Strong dependence on the neutralino mass. (Loss of experimental sensitivity in the degenerate scenario.)

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- Resummation effects at NLL are more important at production threshold.
- K-factor increases from 4.5% to 11%
- > The increase from NLO+NLL to aNNLO+NNLL is about 1%

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- > These cross sections correspond to:
 - more than 10 events at 700 GeV at current integrated luminosity of 139 fb⁻¹;
 - 3 events at 1 TeV for LHC Run 3 goal of 300 fb⁻¹;
 - Few events at 1.5 TeV for HL-LHC goal of 3 ab⁻¹
- aNNLO(+NNLL) corrections increase the NLO(+NLL) prediction by 1% 2%.
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- > Weak dependence from the strong SUSY > Visible threshold behaviour from the sector, as K-factor varies between 1.170 to 1.186, i.e. less than 2%.
- triangle loop, as the squarks masses cross the slepton mass set at 1 TeV.

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Electroweakino pair production

• Features of resummation

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- Mostly gaugino scenario
- Conclusions

Electroweakinos signatures







Mostly gaugino: pp → *some* τs + MET



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Mostly Higgsino Electroweakinos



For a massless light neutralino, chargino masses are <u>excluded</u> below 450 GeV for the production of the lightest-chargino pairs assuming W-boson-mediated decays

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For a massless light neutralino, chargino masses are excluded below *1 TeV* for the production of the lightest-chargino pairs assuming slepton-mediated decays.

Electroweakinos spectra

Interpretation of experimental results is performed within the **pMSSM**.

Mass spectra are obtained with SPheno providing the following input:

Following the indications in:

B. Fucks, M. Klasen, S. Schmiemann, M. Sunder Eur. Phys. J. C78 (2018) 209

Mostly Higgsino electroweakinos:

 $M_1 = M_2 \gg \mu$ mild dependence on $\tan \beta$

 $\tan\beta = 30$ $M_1 = M_2 = 1000 \text{ GeV}$ $\mu \in [100 - 500] \text{ GeV}$

$$\begin{split} M_{\chi_2^0} &\simeq \mu \\ M_{\chi_2^0} - M_{\chi_1^\pm} &\simeq M_{\chi_1^\pm} - M_{\chi_1^0} \simeq 5 - 10 \text{ GeV} \end{split}$$

Electroweakinos > 98% Higgsinos

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Mostly gaugino electroweakinos:

 $\mu > M_2 > M_1$ mild dependence on $\tan \beta$

 $\tan\beta = 5$ $\mu = 3000 \text{ GeV}$ $M_1 = 100 \,\,{\rm GeV}$ $M_2 \in [1000 - 2600] \text{ GeV}$

$$\begin{array}{l} M_{\chi_2^0}\simeq M_{\chi_1^\pm}\simeq M_2\\ M_{\chi_1^0}\simeq M_1 \end{array}$$

Electroweakinos > 98% gauginos



- > NLO corrections enhance the LO cross section by about 30%.
- NLL corrections enhance the NLO cross section by another 3-5%.
- aNNLO+NNLL give another ±2 % correction to the NLO+NLL cross section.

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NLL corrections reduce the NLO cross section by 1% to 2%.

(Scale uncertainties are not so small, because of the relatively light Higgsino masses)

ANNLO+NLL corrections increase the NLO+NLL cross section by up to 5% for low higgsino masses.



- Weak dependence from the strong SUSY sector, as K-factor varies between 1.174 to 1.175, i.e. ~ 0.1%.
- The gradient is along the diagonal and slightly steeper when the squark and gluino masses are still relatively close to those of the Higgsinos.

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- > NLL corrections increase the cross section between 5% to 10%.
- > A decrease for all invariant masses is observed from NLO+NLL to aNNLO+NNLL.
- This behavior is correlated with <u>large t- and u- channel contributions and large</u> <u>cancellations of the squared s- channel contribution with its interference terms</u>.

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- > NLL corrections increase the NLO cross section by up to 5%.
- aNNLO+NLL corrections reduce the NLO+NLL cross section by up to 4% for high gaugino masses.

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 Weak dependence the gluino mass, which enters only at NLO, and very strong dependence on the squark mass. Large contribution at NLO mainly (but not only) from onshell production of intermediate squarks in the final state that subsequently decay into the observed gauginos, plus some resonant contribution in virtual box diagrams when the squark threshold is crossed.

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Conclusions

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 - Mostly gaugino scenario

Conclusions

Conclusions

- Updated calculations of threshold resummation for <u>slepton</u> and <u>electroweakinos</u> pair production (in their mostly <u>Higgsino</u> and <u>gaugino</u> compisition) at the LHC with **NNLL** accuracy, matched to **approximate NNLO** QCD corrections.
- Review of the formalism and highlights of analytical results for resummation at **NNLL** accuracy matched to fixed order calculation at **aNNLO**.
- Sleptons:
 - Small enhancement (< 2%) of invariant-mass distributions and total cross sections with respect to previous calculations with NLO+NLL precision.
 - <u>Significant reductions on the renormalisation and factorisation scale dependences</u> now at the permil level.
 - Very small dependence on squark and gluino masses (< 2%) and on bottom squark mixing (~ 1%).
- Electroweakinos (mostly Higgsino):
 - Moderate modifications (< ±5%) of the differential and total cross sections with respect to previous calculations with NLO+NLL precision.
 - Further <u>reduction of scale uncertainties</u> now ≤ 2%.
 - Small dependence on squark and gluino masses (~0.1%) and on bottom squark mixing (< 1.5%).
- Electroweakinos (mostly gaugino):
 - Moderate reduction (< 4%) of the differential and total cross sections with respect to previous calculations with NLO+NLL precision.
 - <u>Significant reductions of scale dependences</u> for light electroweakinos down to permil level. For heavy electroweakinos scale uncertainty is as large as NLO+NLL result.
 - Very large resonant increase of cross sections observed in the gluino-squark mass plane, as squark mass crosses the electroweakinos mass threshold. Very small dependence on bottom squark mixing (<0.1%).

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31/07/2020 **26**

Thank you!



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Sleptons



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Upper limit on direct stau pair production is set to $\sigma \times Br^2 = 132 \ fb$ for a stau mass of 125 *GeV* and lightest neutralino mass of 1 *GeV*.

In the degenerate case both left- and right-handed staus are produced. Mass limits vary between *90 GeV* and *150 GeV*.

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Mostly Higgsino Electroweakinos



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Similar results in other final states.

In pp collisions, absolute size of the total cross section larger for positively charged final states, and intermediate for neutral final state.

Experimental signatures

Sleptons searches:

1st & 2nd generation:



3rd generation:



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Electroweakinos searches:

Mostly Higgsino:



 $pp \rightarrow some \ \tau s + MET$

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Mostly gauginos Electroweakinos



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In pp collisions, absolute size of the total cross section larger for positively charged final states, and intermediate for neutral final state.

Much larger aNNLO+NNLL corrections amount to up to -8% and -15% with respect to the NLO+NLL predictions for neutral and positive charged final state respectively.

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