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# An extensive study of dark matter in the Singlet + Triplet Scotogenic Model

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# ABOUT NEUTRINOS AND DARK MATTER

Neutrinos are particles with a mass different from zero [1].

The actual Standard Model cannot explain these results by itself

Many theoretical models try to explain it

85% of the Universe's matter is dark [2]

A particle DM: observations of its gravitational effects on baryonic matter.

The most recent measured of DM abundance by Planck satellite yields that

$$\Omega_{DM} h^2 = 0.1196 \pm 0.0031$$

There are different scenarios about how the abundance was generated and different DM candidates.

[1] Fukuda, Y.; et al. Phys. Rev.Let. 81 (8): 1562–1567 (1998)

[2] Planck Collaboration, 1502.01589

# BORN FROM THE DARK

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- To generate neutrino masses at tree level, a dim-5 operator can be introduced via the **seesaw mechanism** [1] [2] [3]. Neutrino masses can be generated at loop level.
  - The idea of the **Scotogenic Model** was proposed by Ernest Ma [4]
    - His model introduced the possibility of giving mass to neutrinos at One-Loop
    - Also a WIMP-like **Dark Matter (DM)** candidate appears which can be either scalar or fermionic.
      - The stability of the DM particle is ensured by the same  $Z_2$  symmetry that leads to the radiative origin of neutrino masses.
- The Scotogenic Model has been generalized in different ways [5] [6]

[1] R. N. Mohapatra et al Phys. Rev. Lett. 44 (1980) 912.

[2] J. Schechter, José W. F. Valle (1980). Phys. Rev. 22 (9): 2227–2235

[3] B. Bajc and G. Senjanovic, JHEP 0708 (2007) 014

[4] E. Ma, Phys.Rev. D73, 077301 (2006), hep-ph/0601225.

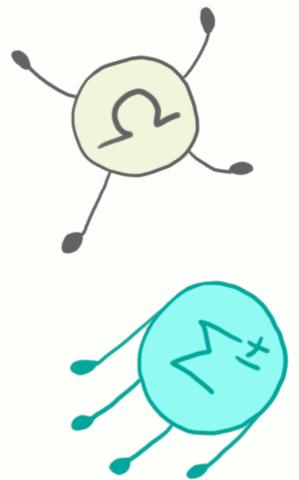
[5] R. Foot et al., Z.Phys. C44 (1989) 441.

[6] M. Hirsch et al., JHEP 1310, 149 (2013), 1307.8134.

# SINGLET+TRIPLET SCOTOGENIC: "A NEW SCOTOGENIC MODEL"

The full particle content of the model is given by the following table

	Standard Model			new fermions		new scalars	
	$L$	$e$	$\phi$	$\Sigma$	$F$	$\eta$	$\Omega$
Generations	3	3	1	1	1	1	1
$SU(3)_C$	1	1	1	1	1	1	1
$SU(2)_L$	2	1	2	3	1	2	3
$U(1)_Y$	-1	-2	1	0	0	1	0
$\mathbb{Z}_2$	+	+	+	-	-	-	+
$L$	1	1	0	0	0	-1	0



The new interactions included in the Lagrangian are

$$\mathcal{L} \subset -Y^{\alpha\beta} L_\alpha e_\beta \phi - Y_F^\alpha (\bar{L}_\alpha \tilde{\eta}) F - \frac{M_F}{2} \bar{F}^c F - Y_\Sigma^\alpha \bar{L}_\alpha^c \Sigma^\dagger \tilde{\eta} - \frac{1}{4} M_\Sigma \text{Tr} (\bar{\Sigma}^c \Sigma) - Y_\Omega \text{Tr} [\bar{\Sigma} \Omega] F + h.c.$$

Simple  
Scotogenic

Triplet  
Scotogenic

Singlet + Triplet  
Scotogenic

$$\tilde{\eta} = i\sigma\eta^*$$

The corresponding scalar potential is

$$\begin{aligned}
 \mathcal{V} = & -m_\phi^2 \phi^\dagger \phi + m_\eta^2 \eta^\dagger \eta - \frac{m_\Omega^2}{2} \text{Tr} (\Omega^\dagger \Omega) \\
 & + \frac{\lambda_1}{2} (\phi^\dagger \phi)^2 + \frac{\lambda_2}{2} (\eta^\dagger \eta)^2 + \frac{\lambda_3}{2} (\phi^\dagger \phi) (\eta^\dagger \eta) + \lambda_4 (\phi^\dagger \eta) (\eta^\dagger \phi) + \frac{\lambda_5}{2} [(\phi^\dagger \eta)^2 + (\eta^\dagger \phi)^2] \\
 & + \mu_1 \phi^\dagger \Omega \phi + \mu_2 \eta^\dagger \Omega \eta \\
 & + \frac{\lambda_1^\Omega}{2} (\phi^\dagger \phi) \text{Tr} (\Omega^\dagger \Omega) + \frac{\lambda_2^\Omega}{4} [\text{Tr} (\Omega^\dagger \Omega)]^2 + \frac{\lambda_\eta^\Omega}{2} (\eta^\dagger \eta) \text{Tr} (\Omega^\dagger \Omega)
 \end{aligned}$$

Singlet + Triplet  
Scotogenic

The conditions for the parameters in the scalar potential are

$$\begin{aligned}
 & \lambda_1 \geq 0, \quad \lambda_2 \geq 0, \quad \lambda_2^\Omega \geq 0, \\
 & \lambda_3 + \sqrt{\lambda_1 \lambda_2} \geq 0, \quad \lambda_3 + \lambda_4 - |\lambda_5| + \sqrt{\lambda_1 \lambda_2} \geq 0, \\
 & \lambda_1^\Omega + \sqrt{2\lambda_1 \lambda_2^\Omega} \geq 0, \quad \lambda_\eta^\Omega + \sqrt{2\lambda_2 \lambda_2^\Omega} \geq 0, \\
 & \sqrt{2\lambda_1 \lambda_2 \lambda_2^\Omega} + \lambda_3 \sqrt{2\lambda_2^\Omega} + \lambda_1^\Omega \sqrt{\lambda_2} + \lambda_\eta^\Omega \sqrt{\lambda_1} + \sqrt{(\lambda_3 + \sqrt{\lambda_1 \lambda_2}) (\lambda_1^\Omega + 2\sqrt{\lambda_1 \lambda_2^\Omega}) (\lambda_\eta^\Omega + \sqrt{\lambda_2 \lambda_2^\Omega})} \geq 0.
 \end{aligned}$$

## ● Scalar sector

The scalar fields presented in the model can be written as follows

$$\eta = \begin{pmatrix} \eta^+ \\ (\eta_R + i\eta_I)/\sqrt{2} \end{pmatrix} \quad \phi = \begin{pmatrix} \varphi^+ \\ (h_0 + v_\phi + i\psi)/\sqrt{2} \end{pmatrix}$$

$$\Omega = \begin{pmatrix} (\Omega_0 + v_\Omega)/\sqrt{2} & \Omega^+ \\ \Omega^- & -(\Omega_0 + v_\Omega)/\sqrt{2} \end{pmatrix}$$

The masses for the neutral scalar are

$$m_{H^\pm}^2 = 2\mu_1 \frac{(v_\phi^2 + v_\Omega^2)}{v_\Omega},$$

$$m_{\eta^\pm}^2 = m_\eta^2 + \frac{1}{2}\lambda_3 v_\phi^2 + \frac{1}{\sqrt{2}}\mu_2 v_\Omega + \frac{1}{2}\lambda_\eta^\Omega v_\Omega^2,$$

$$m_{\eta_R}^2 = m_{\eta^\pm}^2 + \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)v_\phi^2 + \frac{1}{2}\lambda_\eta^\Omega v_\phi^2 - \frac{1}{\sqrt{2}}\mu_2 v_\Omega,$$

$$m_{\eta_I}^2 = m_{\eta^\pm}^2 + \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5)v_\phi^2 + \frac{1}{2}\lambda_\eta^\Omega v_\phi^2 - \frac{1}{\sqrt{2}}\mu_2 v_\Omega.$$

**DM**  
candidate



- Fermionic sector

$$\Sigma = \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} & \Sigma^+ \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} \end{pmatrix}$$

The DM candidate will be the lightest mass eigenstate of the mass matrix

$$\mathcal{M}_\chi = \begin{pmatrix} M_\Sigma & \frac{1}{\sqrt{2}} Y_\Omega v_\Omega \\ \frac{1}{\sqrt{2}} Y_\Omega v_\Omega & M_F \end{pmatrix}$$

The fermion masses generated at tree level

$$m_\chi^\pm = M_\Sigma,$$

$$m_{\chi_1^0} = \frac{1}{2} \left( M_\Sigma + M_F - \sqrt{(M_\Sigma - M_F)^2 + 4(2Y_\Omega v_\Omega)^2} \right)$$

$$m_{\chi_2^0} = \frac{1}{2} \left( M_\Sigma + M_F + \sqrt{(M_\Sigma - M_F)^2 + 4(2Y_\Omega v_\Omega)^2} \right)$$

$$\tan(2\theta) = \frac{4Y_\Omega v_\Omega}{M_\Sigma - M_F}$$

# NEUTRINO MASS GENERATION

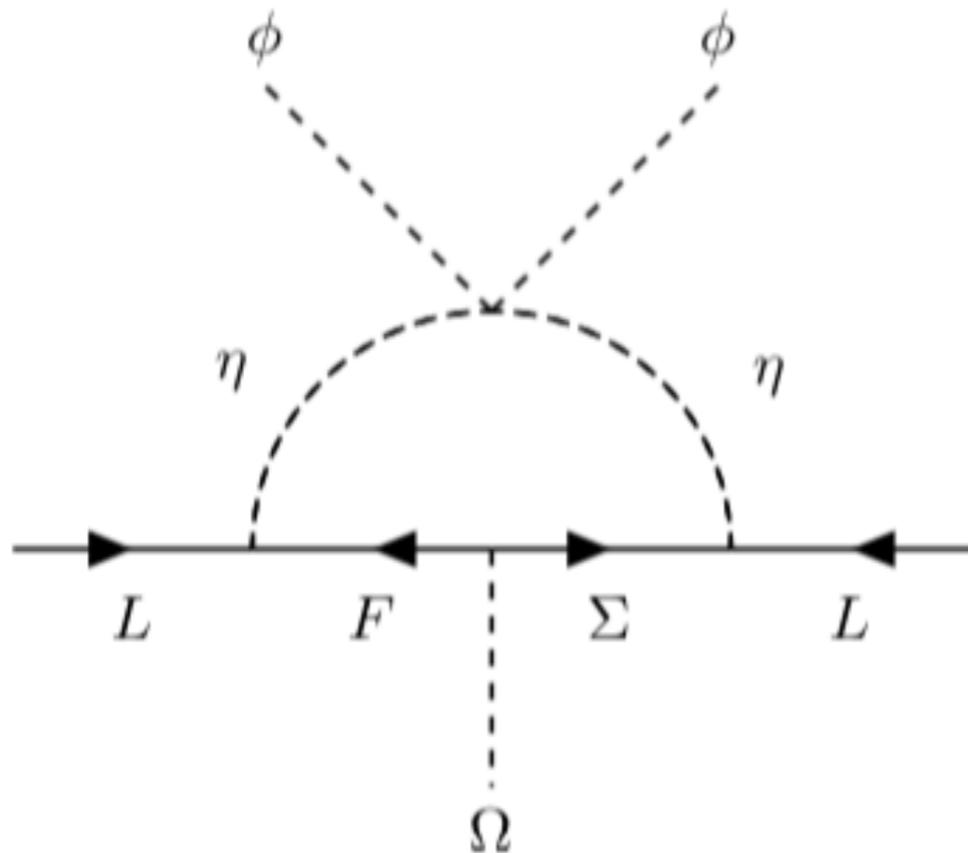
$$\mathcal{M}_{\alpha\beta}^{\nu} = \sum_{\sigma=1,2} \frac{Y_{\alpha\sigma}^{\nu} Y_{\beta\sigma}^{\nu}}{32\pi^2} m_{\chi_{\sigma}} \left( \frac{m_{\eta_R}^2}{m_{\eta_R}^2 - m_{\chi_{\sigma}}^2} \ln \left( \frac{m_{\eta_R}^2}{m_{\chi_{\sigma}}^2} \right) - \frac{m_{\eta_I}^2}{m_{\eta_I}^2 - m_{\chi_{\sigma}}^2} \ln \left( \frac{m_{\eta_I}^2}{m_{\chi_{\sigma}}^2} \right) \right)$$

$$Y^{\nu} = \begin{pmatrix} Y_{\Sigma}^1 & Y_F^1 \\ Y_{\Sigma}^2 & Y_F^2 \\ Y_{\Sigma}^3 & Y_F^3 \end{pmatrix} \cdot V(\theta).$$

$$Y_{\alpha\beta}^{\nu} = U_{\nu} \sqrt{m_{\nu}} \rho \sqrt{\mathcal{F}}^{-1},$$

[J. A. CASAS AND A. IBARRA, NUCL. PHYS. B618, 171 (2001), HEP-PH/0103065]

One neutrino will be massless



# Constraints

For our analysis the following constraints have been considered

- Lepton Flavor Violation  $\mu \rightarrow e\gamma < 4.2 \times 10^{-13}$  [Baldini+ (MEG), EPJC 2016]  
 $\mu \rightarrow 3e < 1.0 \times 10^{-12}$  [Bellgardt+ (SINDRUM), NPB 1988]  
[Rocha-Morán+ arxiv:1605.01915]  
 $CR(\mu - e, Au) < 7.10^{-13}$  [Bertl+ (SINDRUM II), EPJC 2006]
- Neutrino oscillation parameters [de Salas+ PLB, 2018 ]
- Electroweak precision tests  $-0.00018 \leq \delta\rho \leq 0.00096(3\sigma)$
- DM and cosmological observations
- Invisible Higgs decay of the Higgs boson  $BR(h^0 \rightarrow inv) \leq 24\%$   
 $0.62 \leq BR(h^0 \rightarrow \gamma\gamma)/BR(h^0 \rightarrow \gamma\gamma)_{SM} \leq 1.7$
- Colliders  $80GeV \leq m_{H^\pm} \leq 1TeV$   $122GeV \leq m_{h^0} \leq 128GeV$   
 $m_H \leq 1TeV$

# Tools

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For the montecarlo simulation we develop our own python code.

For our analysis we use numerical tools.

- **SARAH**: model implementation, computation off all the vertices, mass matrices, one loop correction for tadpole and self-energies.
- **SPHENO**: computation of the physical particle spectrum and low energy observables
- **MicrOMEGAS**: computation of the thermal component to the DM relic abundance and the DM-nucleon scattering cross section.
- **MadGraph**: computation of the cross section.
- **Checkmate**: test our results with the last results given by the LHC.

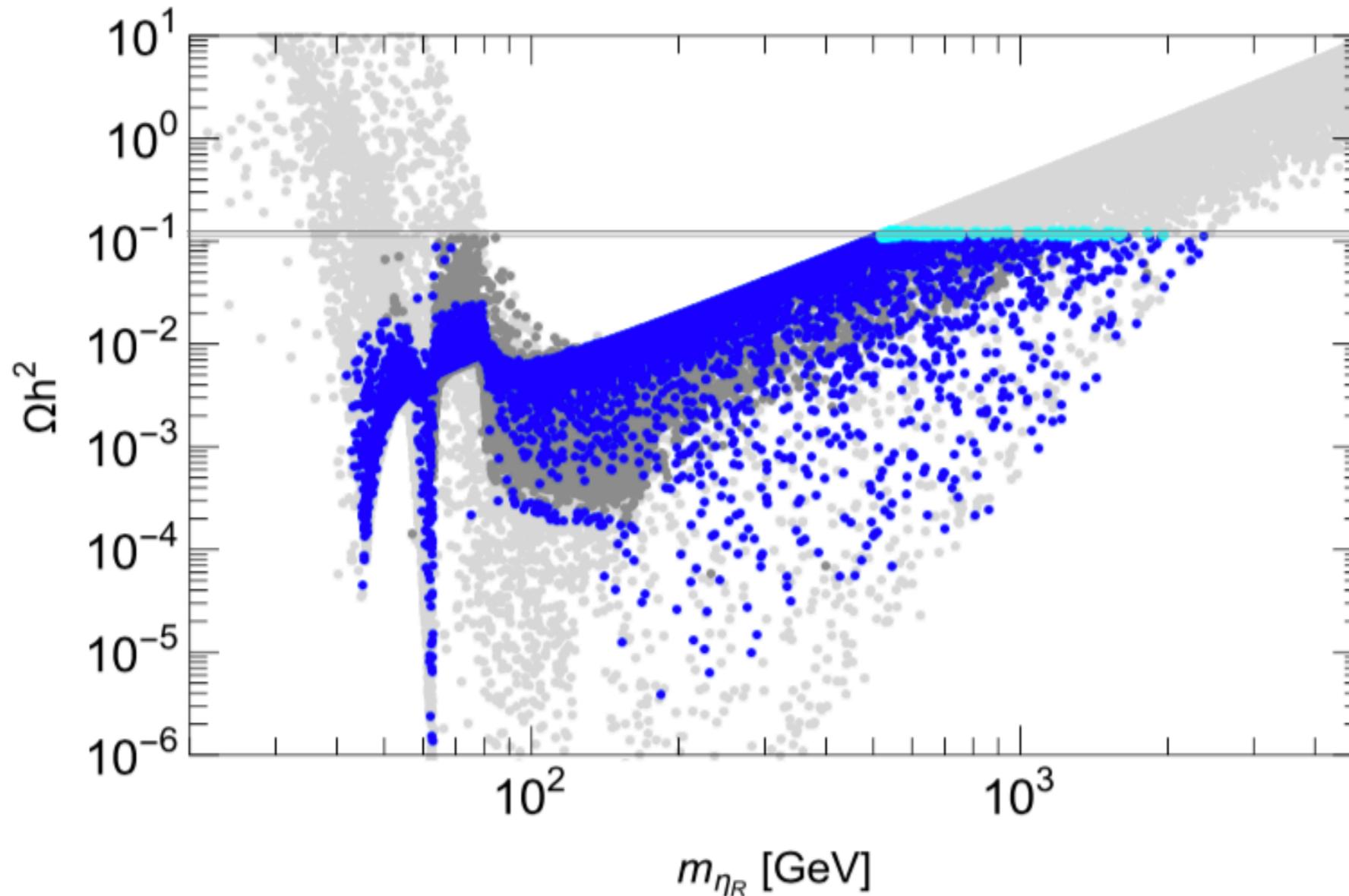
# Numerical scan

The values for the main parameter considered in the analysis are

Parameter	Range
$M_N$	$[5 \cdot 10^3, 10^4]$ (GeV)
$M_\Sigma$	$[5 \cdot 10^3, 10^4]$ (GeV)
$m_\eta^2$	$[100, 5000]$ (GeV <sup>2</sup> )
$\mu_{1,2}$	$[10^{-8}, 5 \cdot 10^3]$ (GeV)
$v_\Omega$	$[10^{-5}, 5]$ (GeV)
$ \lambda_i , i = 1 \dots 4$	$[10^{-8}, 1]$
$ \lambda_5 $	$[10^{-5}, 1]$
$ \lambda_{1,2}^\Omega $	$[10^{-8}, 1]$
$ \lambda_\eta^\Omega $	$[10^{-8}, 1]$
$ Y_\Omega $	$[10^{-8}, 1]$

# RELIC DENSITY

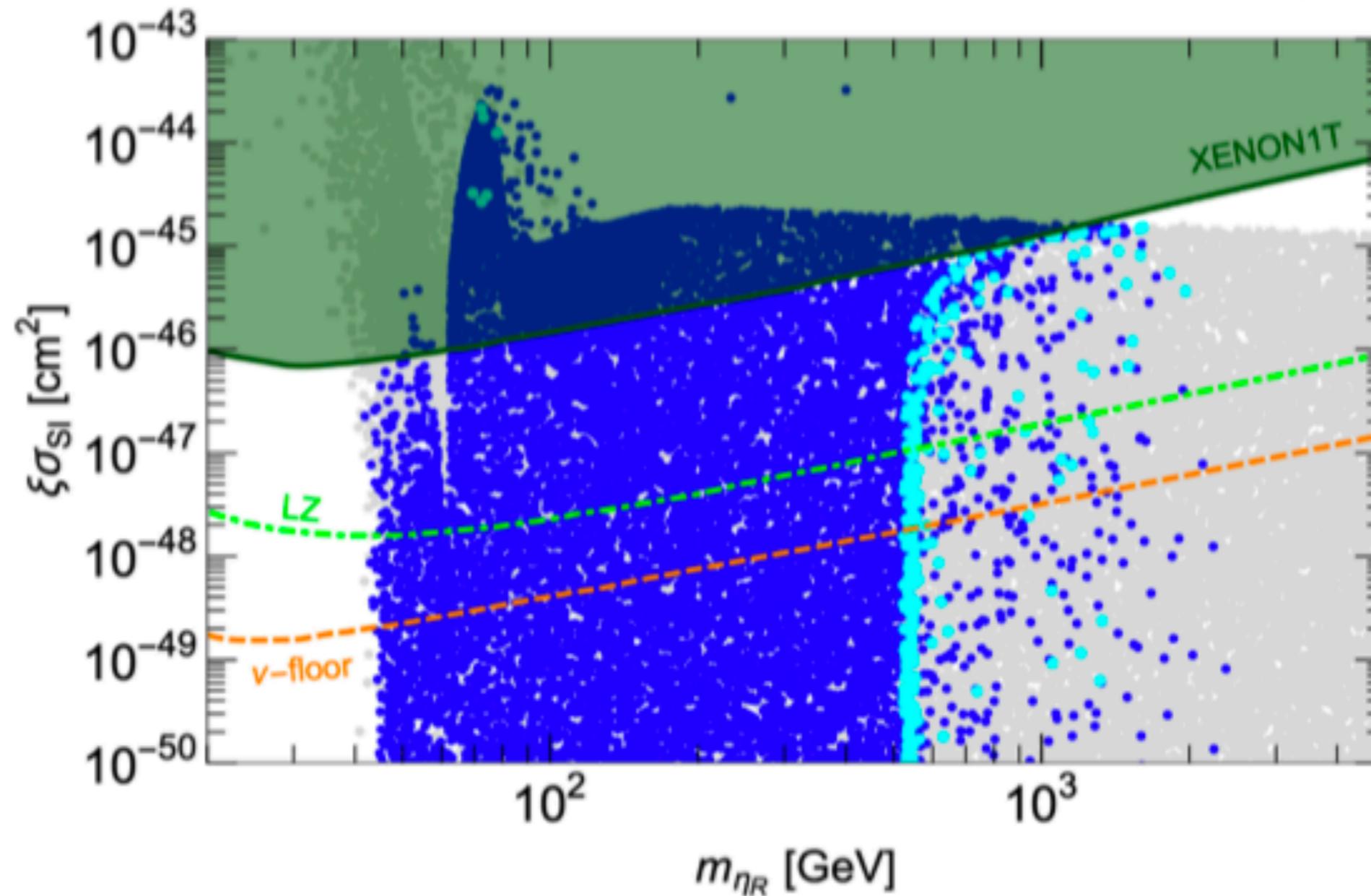
[arXiv:1910.08422]



Relic abundance  $\Omega_{\eta_R} h^2$  as a function of the  $\eta_R$  mass. Cyan points are solutions that fall exactly within the  $3\sigma$  C.L. cold DM measurement by the Planck collaboration. Dark grey points are solutions in conflict with the current limit on WIMP-nucleon SI elastic scattering cross section set by XENON1T

[Planck Collaboration, 1502.01589]

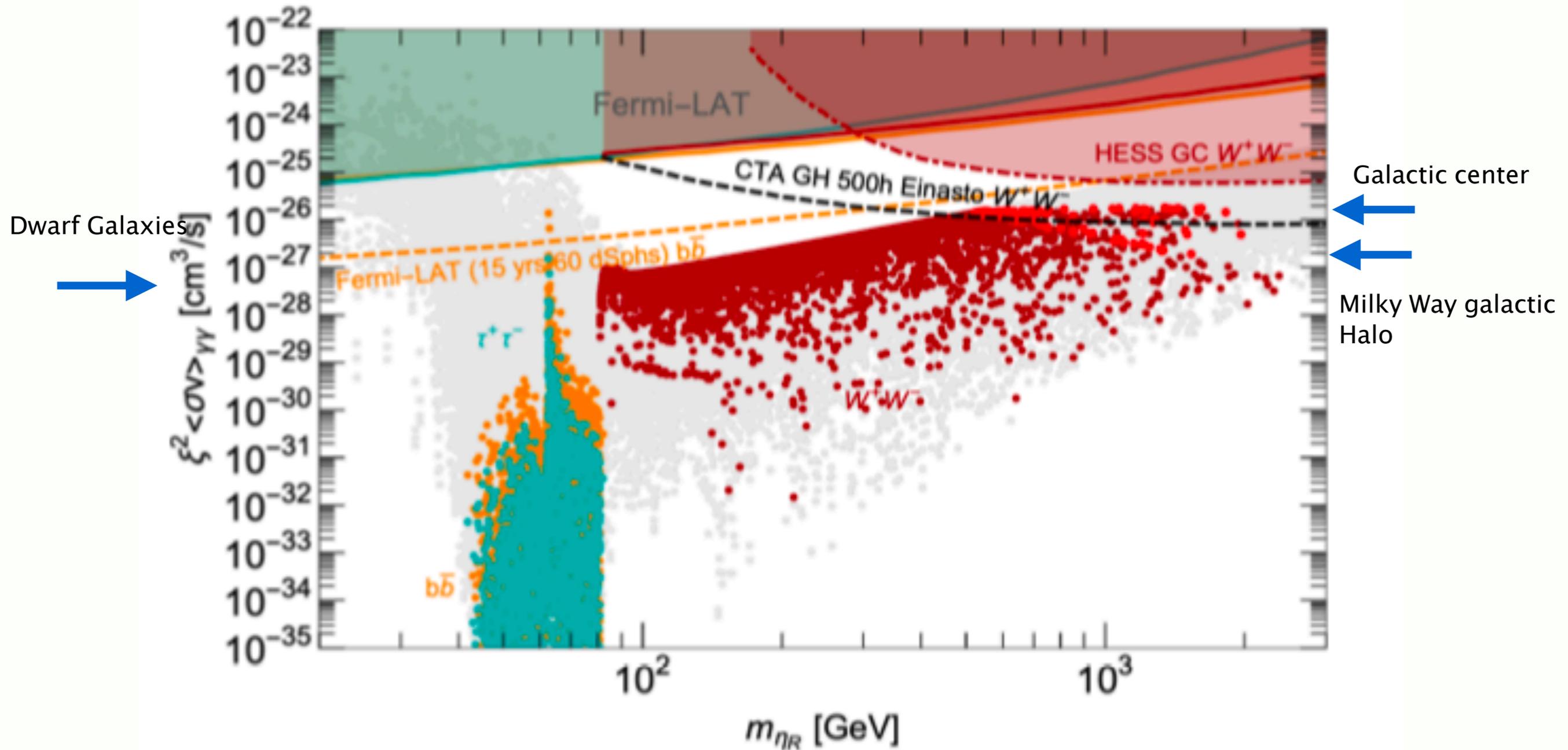
[Xenon1T collaboration arXiv:1805.12562v2 [astro-ph.CO]]



Spin-independent  $\eta_R$ -nucleon elastic scattering cross section versus the  $\eta_R$  mass. The dark green line denotes the most recent upper bound from XENON1T. The dashed orange line correspond to the neutrino floor limit from coherent elastic neutrino nucleus scattering.

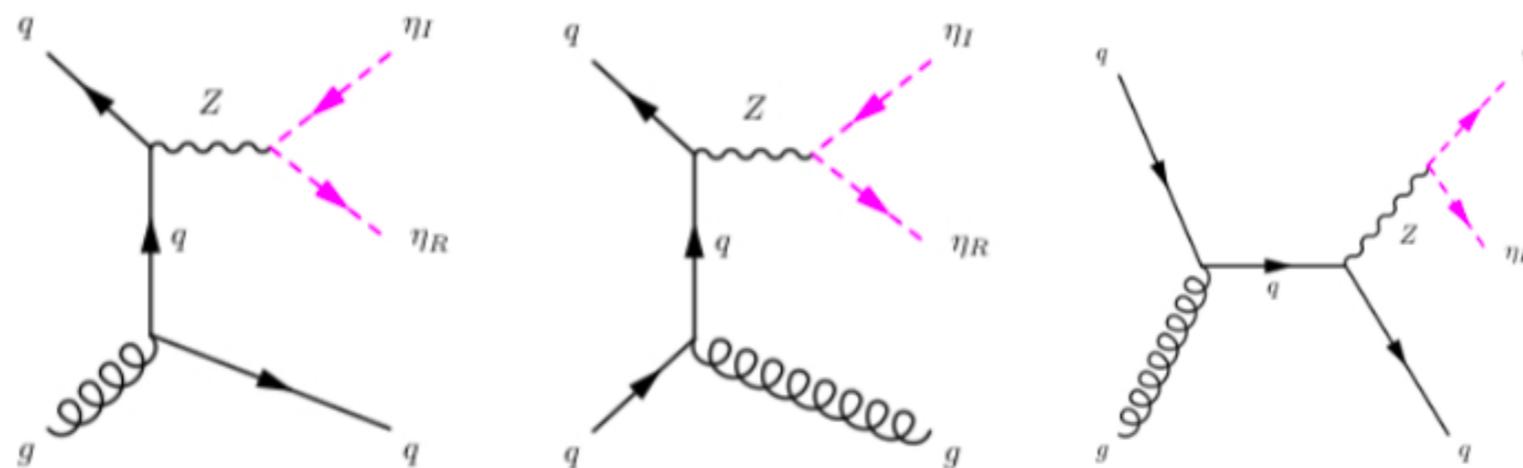
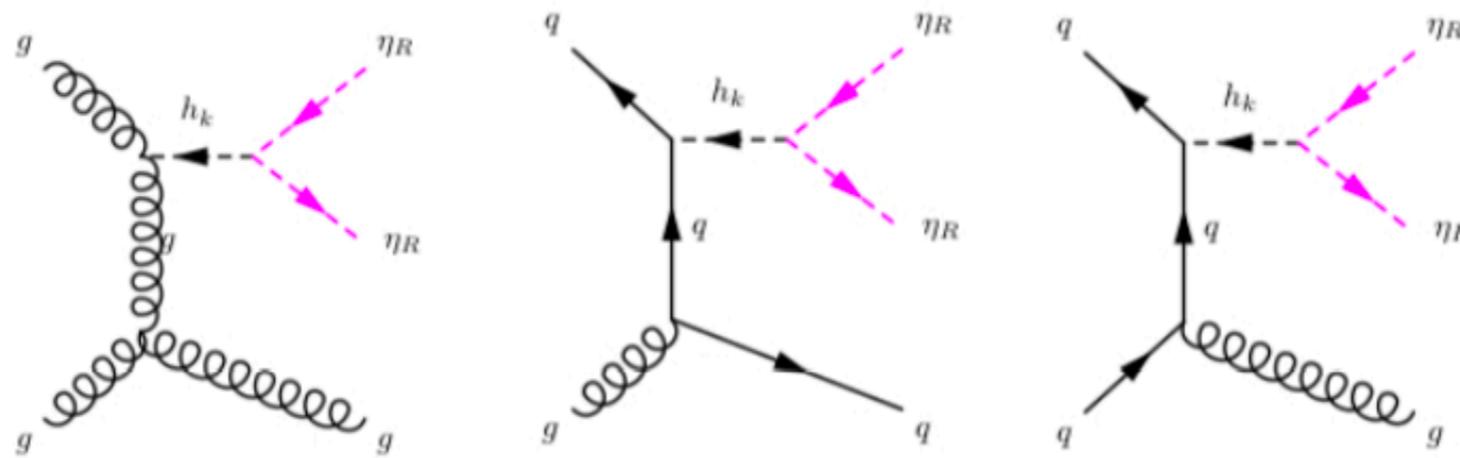
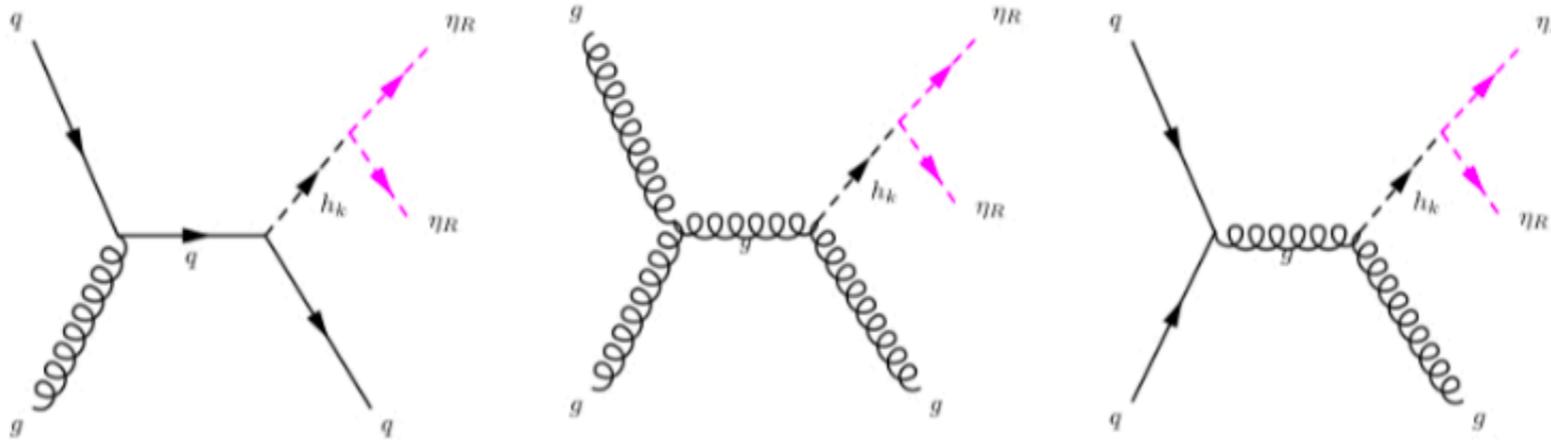
# INDIRECT DETECTION

[arXiv:1910.08422]



Predicted DM annihilation cross section into  $\gamma$  rays (weighted by the relative abundance) for annihilations to  $b\bar{b}$  (orange),  $\tau^+\tau^-$  (dark cyan) and  $W^+W^-$  (dark and light red) final states (left panel). The dark cyan, red and orange lines are the current limit set by Fermi-LAT satellite. The dot dashed red line is the current limit for HESS telescope. Current limits lie a couple of orders of magnitude above the predicted signals but future data offer promising prospects.

# $\cancel{E}_T$ + jet signal (mono-jet)



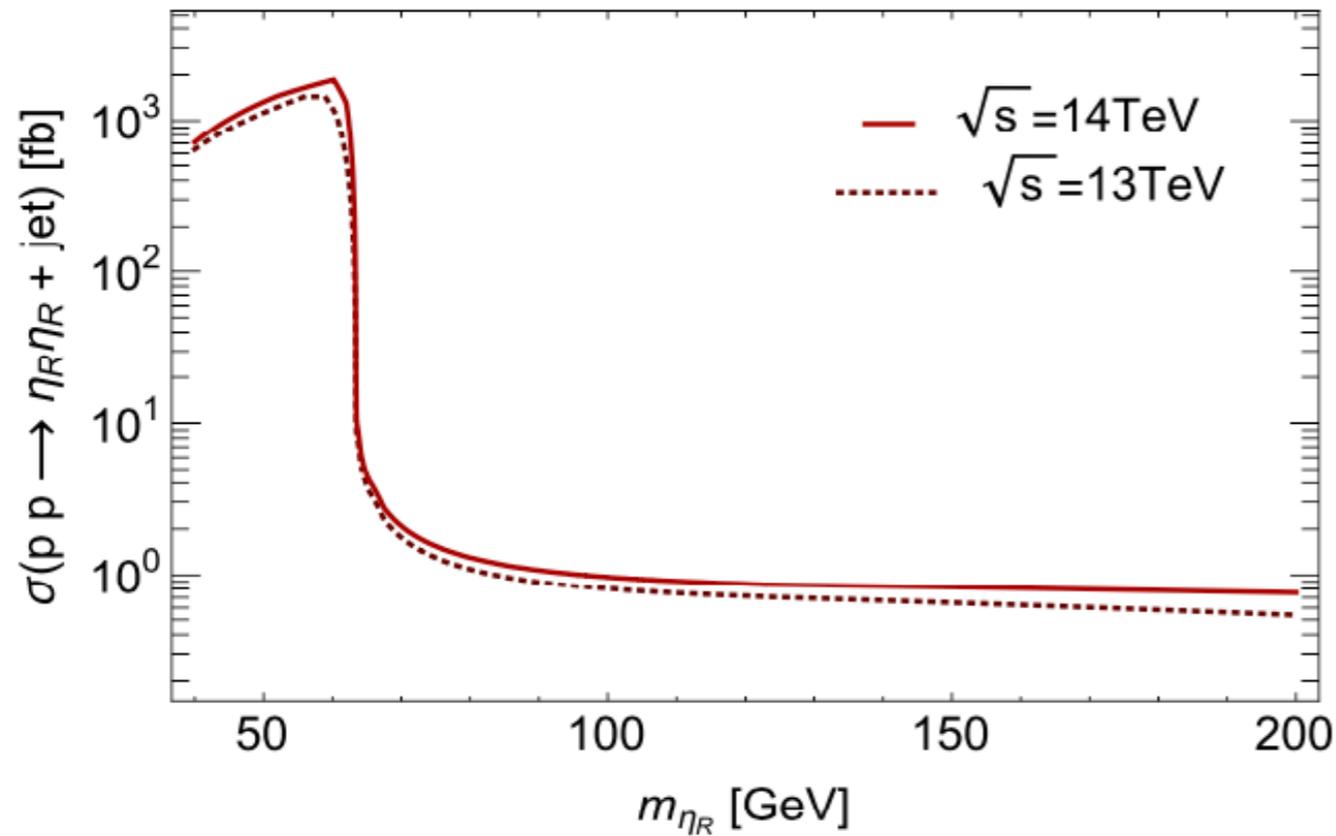


Parameters	Benchmark 1	Benchmark 2	Units
$\lambda_3$	$3.64 \times 10^{-5}$	$-1.64 \times 10^{-5}$	-
$\lambda_4$	$7.02 \times 10^{-7}$	$-3.29 \times 10^{-7}$	-
$\lambda_5$	$-1.8 \times 10^{-2}$	$-1.45 \times 10^{-2}$	-
$\lambda_\eta^\Omega$	$-1.32 \times 10^{-5}$	$-7.11 \times 10^{-6}$	-
$\mu_2$	$-4.57 \times 10^{-8}$	$-1.59 \times 10^{-1}$	[GeV]
$v_\Omega$	$2.43 \times 10^{-4}$	$9.21 \times 10^{-1}$	[GeV]
$m_\eta^2$	3678.17	2851.39	[GeV] <sup>2</sup>
<b>Scalar masses</b>			
$m_{\eta_R}$	55.92	49.09	[GeV]
$m_{\eta_I}$	65.04	57.38	[GeV]
$m_{h^0}$	124.68	125.54	[GeV]
$m_H$	425.9	834.45	[GeV]
<b>Constraints</b>			
$\Omega h^2$	0.0107	0.0129	-
BR( $h^0 \rightarrow inv.$ )	0.155489	0.12939	-
BR( $\mu \rightarrow e\gamma$ )	$7.33 \times 10^{-29}$	$8.55 \times 10^{-32}$	-
BR( $\mu \rightarrow eee$ )	$3.75 \times 10^{-30}$	$1.01 \times 10^{-30}$	-
CR( $\mu^-, Au \rightarrow e^-, Au$ )	$3.88 \times 10^{-29}$	$1.40 \times 10^{-29}$	-
BR( $h^0 \rightarrow \gamma\gamma$ )	0.00226748	0.00212008	-
$\Delta a_\mu$	$2.18 \times 10^{-14}$	$2.15 \times 10^{-14}$	-
$\sigma_{SI}$	$5.953 \times 10^{-10}$	$4.862 \times 10^{-10}$	cm <sup>2</sup>

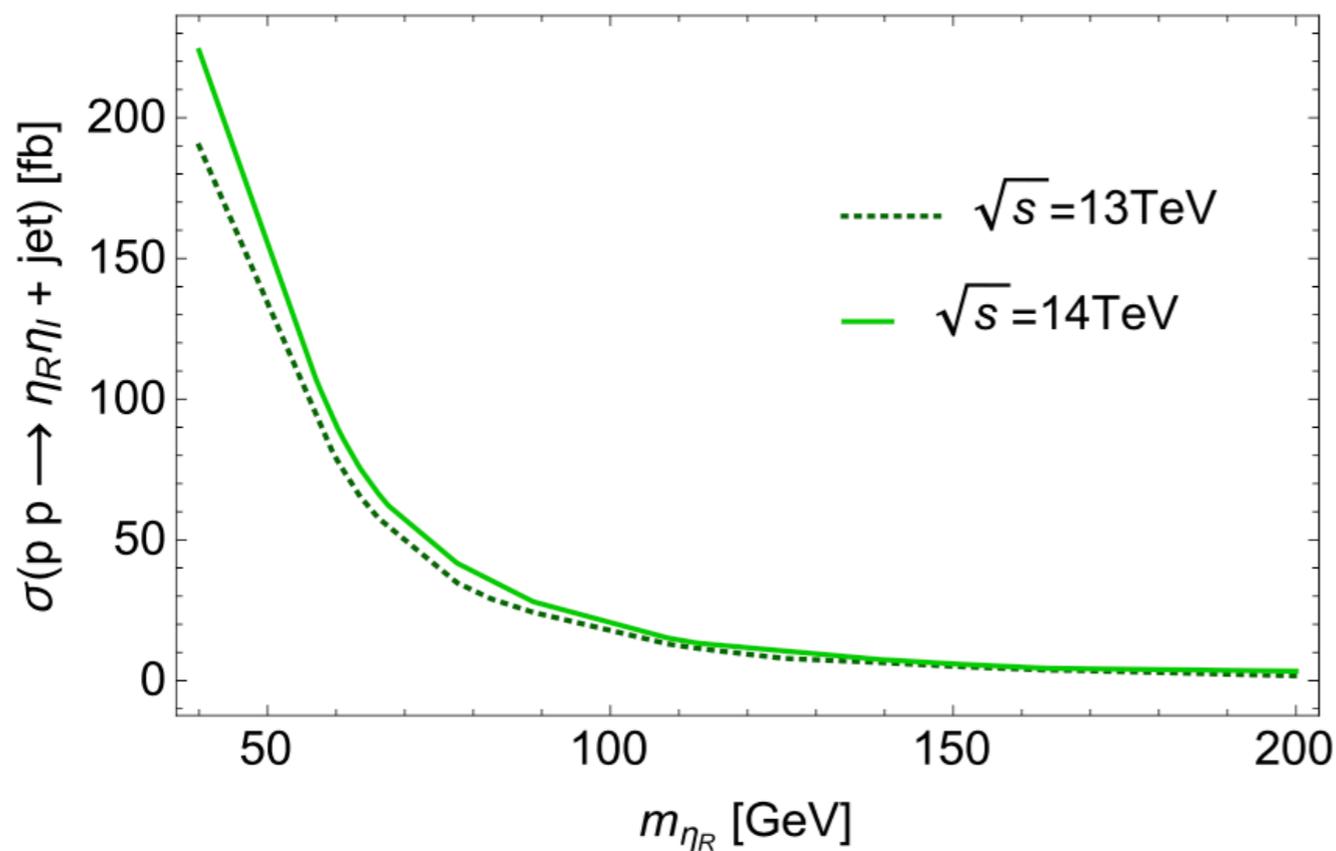
Quantity	Benchmark 1
$\sigma \perp d\sigma$ [fb]	787.791
<b>Norm. Events (<math>\mathcal{L} \times \sigma</math>)</b>	28439.2
<b>Cuts Eff. (<math>\mathcal{A} \times \epsilon</math>)</b>	0.00574
$S \pm dS$	$163.241 \pm 6.814$
$B + dB$	$4680.0 \pm 160.0$
$r$	0.220
<b>Signal Region</b>	<b>IM6</b>

$$r_{\text{BSP}_1} = 0.220$$

$$\lambda_{345} = [-0.2, 0.9]$$



Cross section of  $pp \rightarrow \eta_R \eta_R + \text{jet}$  at LHC  $\sqrt{s} = 13(14)$  TeV. The maximum value of the cross section is  $\sim 1400$  ( $1800$ ) fb for 13 ( $14$ ) TeV respectively, both values are below those in the last analysis presented by ATLAS.



Cross section for the  $pp \rightarrow \eta_R \eta_I$  jet production at LHC  $\sqrt{s} = 13(14)$  TeV.

# SUMMARY AND OUTLOOK

# Thanks!

$\nabla \cdot \vec{D} = \rho$

$(SU(3) \times SU(2) \times U(1))$

$\frac{d}{dt} \left( \frac{\partial \mathcal{L}}{\partial \dot{\theta}} \right) - \frac{\partial \mathcal{L}}{\partial \theta} = 0$

$dU = TdS - PdV$

$\nabla \cdot \vec{B} = 0$

$\sigma_x \sigma_p \geq \frac{\hbar}{2}$

$S = k_B \ln \Omega$

$\oint \vec{E} \cdot d\vec{S} = qV/\epsilon_0$

$\mathcal{L}_D = i\hbar c \bar{\psi} \not{\partial} \psi - m c^2 \bar{\psi} \psi$

$\vec{F} = q\vec{E}$

$C = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

$\vec{\nabla} \times \vec{B} = \mu_0 \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$

$\vec{v} = \vec{r}/t$

$Y(t) = y_0 + v_0 t + \frac{1}{2} a t^2$

$\vec{E} = \epsilon_0 \vec{\nabla} \phi$

$\vec{F} = q\vec{E}$

$\vec{v} = \vec{r}/t$

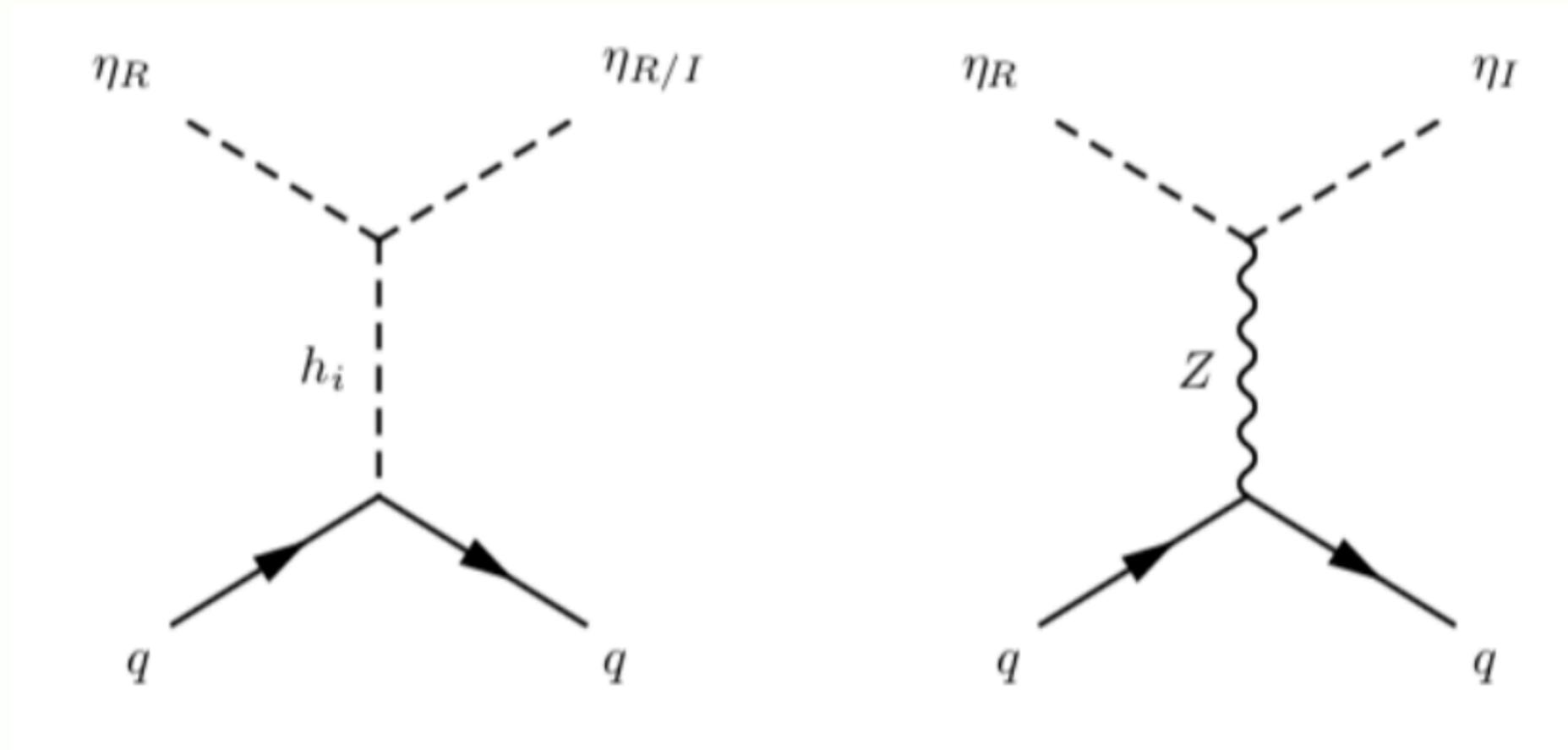
$T-U$



IMA acknowledges partial financial support by CONICyT, Doctorado Nacional 2015 (21151255).

backup

# DIRECT DETECTION



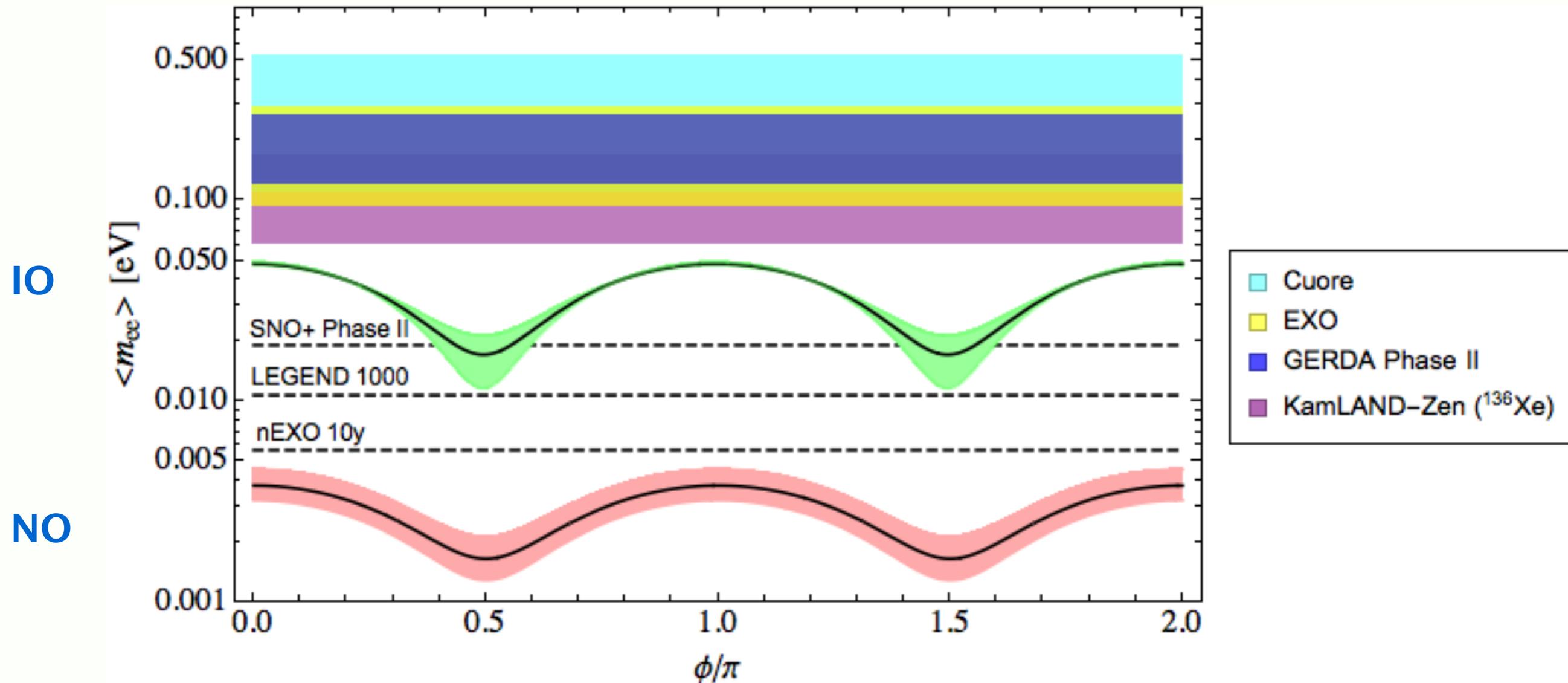
The tree-level spin independent DM nucleon interaction is through the Higgs and Z portals. If the mass difference of mass between the CP-odd particle and the DM is small, the interaction through the Z boson appear.

# 0ν2β

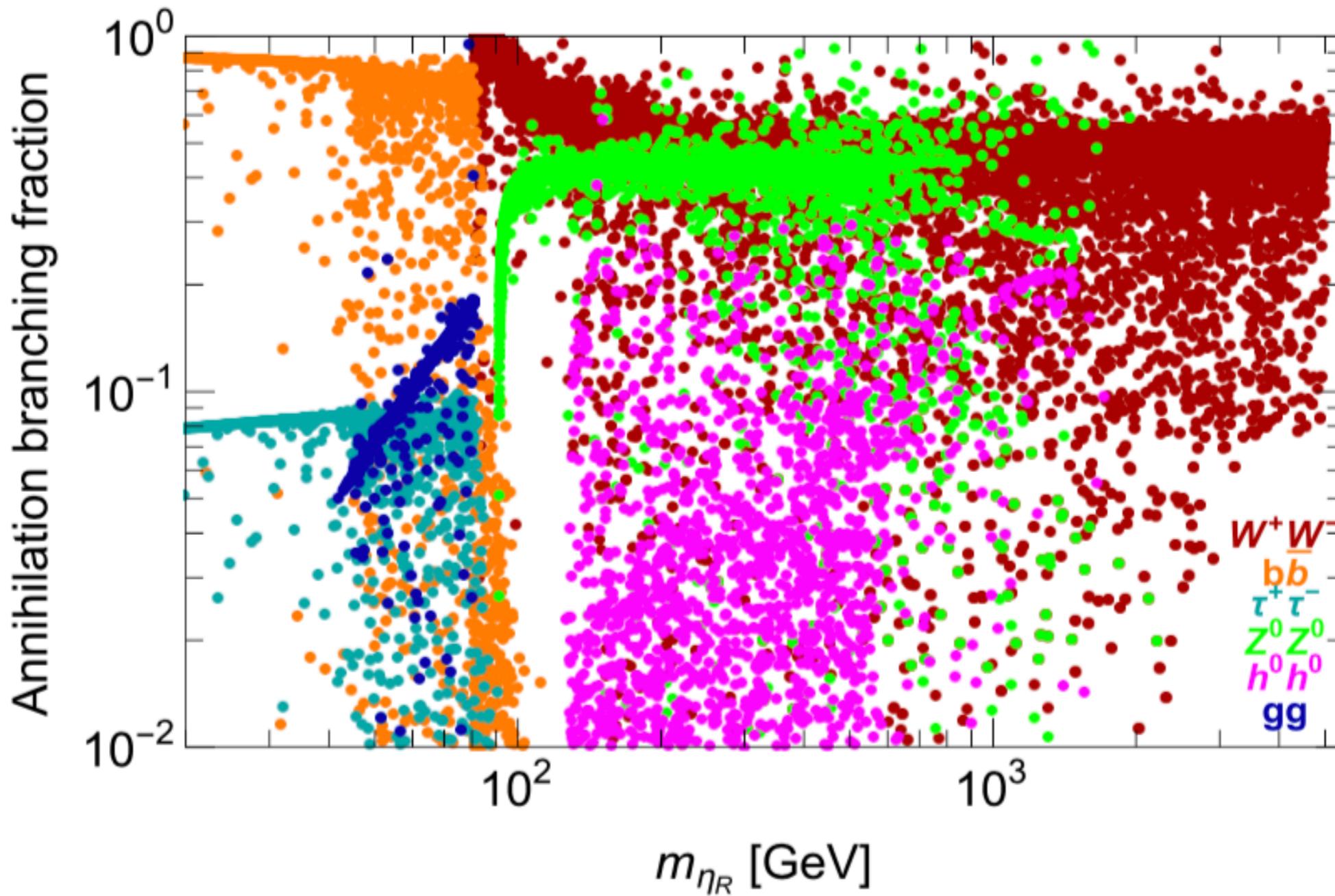
[arXiv:1910.08422]

The Effective 0ν2β Majorana mass parameter expression is

$$\langle m_{ee} \rangle = \left| \sum_j U_{\nu,ej}^2 m_j \right| = \left| \cos \theta_{12}^2 \cos \theta_{13}^2 m_1 + \sin \theta_{12}^2 \cos \theta_{13}^2 m_2 e^{2i\phi_{12}} + \sin \theta_{13}^2 m_3 e^{2i\phi_{13}} \right|$$



The effective mass parameter characterizing the amplitude for neutrinoless double beta (0ν2β) decay has a lower limit



Main branching fractions of the annihilation cross section of  $\eta_R$  into SM final states versus the mass of  $\eta_R$ .

# CHECKMATE

This code allows to determine whether our model is excluded or not at 95% C.L. by comparing to recent experimental analyses in the same final states.

- First, we generate Monte Carlo events for our model with Madgraph.
- CheckMATE 2 determines whether the model is excluded or not at 95% C.L. by comparing to many recent experimental analyses.

$$r \equiv \frac{S - 1.96\Delta S}{S_{exp}^{95}}$$

According the algorithm definitions

a result is excluded  $r \geq 1.5$

a result is compatible  $r \leq 0.67$

a result is “potentially excluded”  $0.67 < r < 1.5$

[arXiv:1812.05186]

Integrate luminosity of  $36.1 \text{ fb}^{-1}$

between the missing transverse momentum direction and each selected jet

Leading jet with  $p_T > 250 \text{ GeV}$  and  $|\eta| < 2.4$

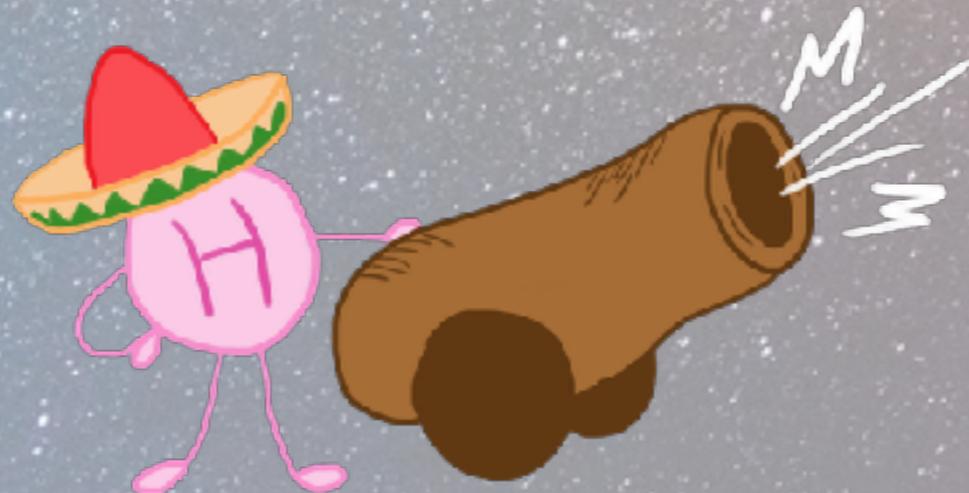
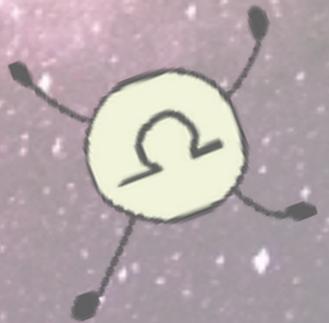
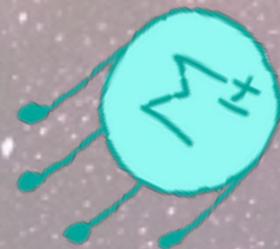
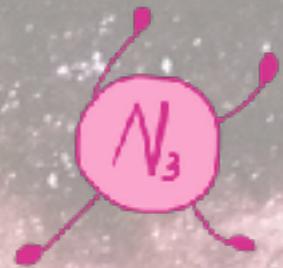
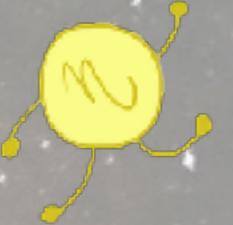
Separation in the azimuthal plane of  $\Delta\phi(\text{jet}, p_T^{\text{miss}}) > 0.4$

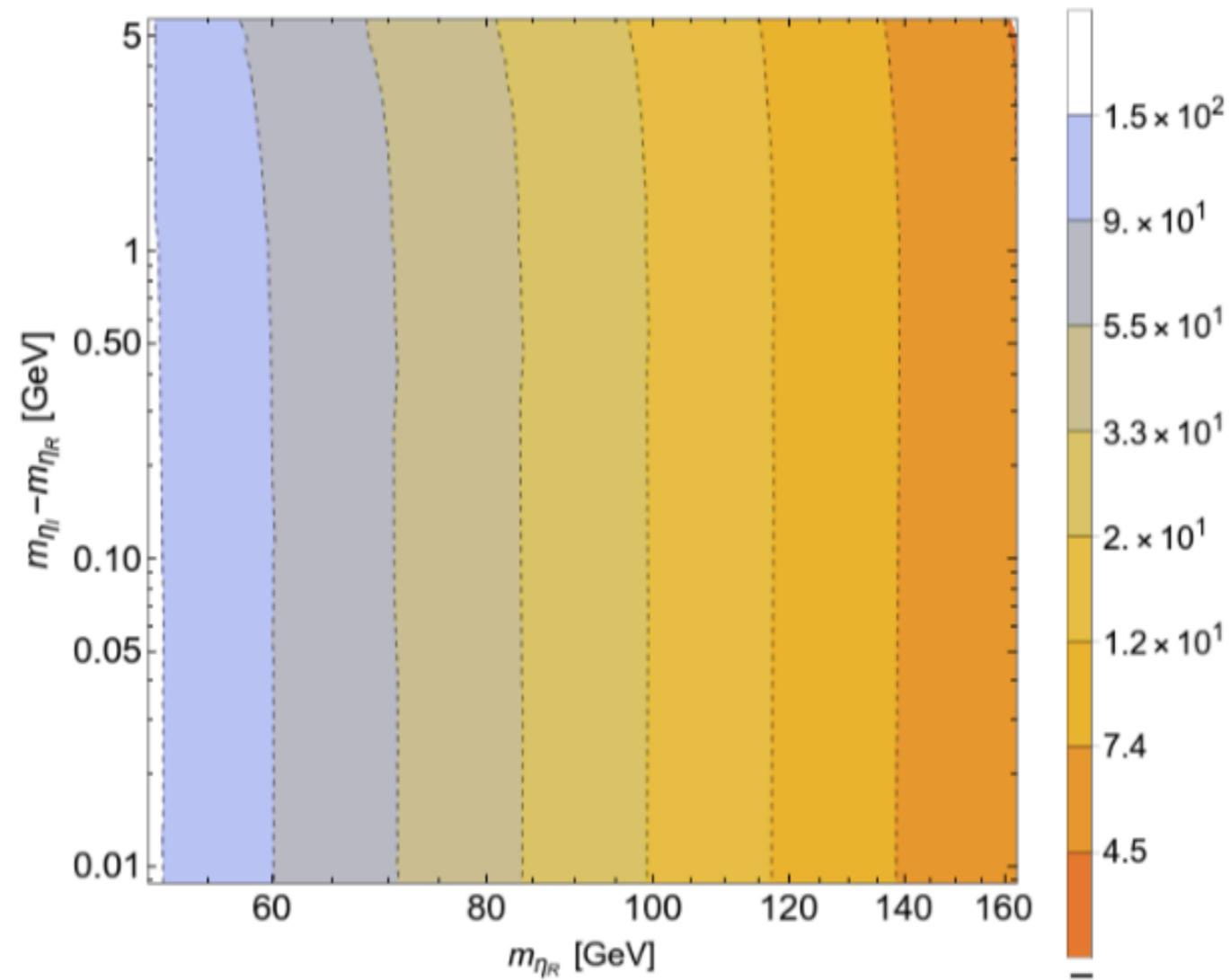
Events with identify muons with  $p_T > 10 \text{ GeV}$  or electrons with  $p_T > 20 \text{ GeV}$  ✗

Quantity	Benchmark 1	Benchmark 2
$\sigma \perp d\sigma$ [fb]	787.791	1074.62
<b>Norm. Events (<math>\mathcal{L} \times \sigma</math>)</b>	<b>28439.2</b>	<b>38793.7</b>
<b>Cuts Eff. (<math>\mathcal{A} \times \epsilon</math>)</b>	<b>0.00574</b>	<b>0.01086</b>
$S \pm dS$	$163.241 \pm 6.814$	$421.3 \pm 12.784$
$B + dB$	$4680.0 \pm 160.0$	$12720.0 \pm 340.0$
$r$	0.220	0.263
<b>Signal Region</b>	<b>IM6</b>	<b>IM5</b>

# Outline

- INTRODUCTION
- SCOTOGENIC MODELS
  - \* SIMPLEST SCOTOGENIC MODEL
  - \* TRIPLET SCOTOGENIC MODEL
  - \* SINGLET + TRIPLET SCOTOGENIC
- CONSTRAINTS
- NUMERICAL SCAN
- RESULTS
- SUMMARY





Mass difference  $m_{\eta_I} - m_{\eta_R}$  as a function of  $m_{\eta_R}$  in mono-jet events mediated by the Z boson,  $pp \rightarrow \eta_R \eta_I + \text{jet}$ . The color shades represent values of the cross section in fb.