

# DARK MATTER PHENOMENOLOGY

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DEGLI STUDI  
DI TORINO  
  
ALMA UNIVERSITAS  
TAURINENSIS



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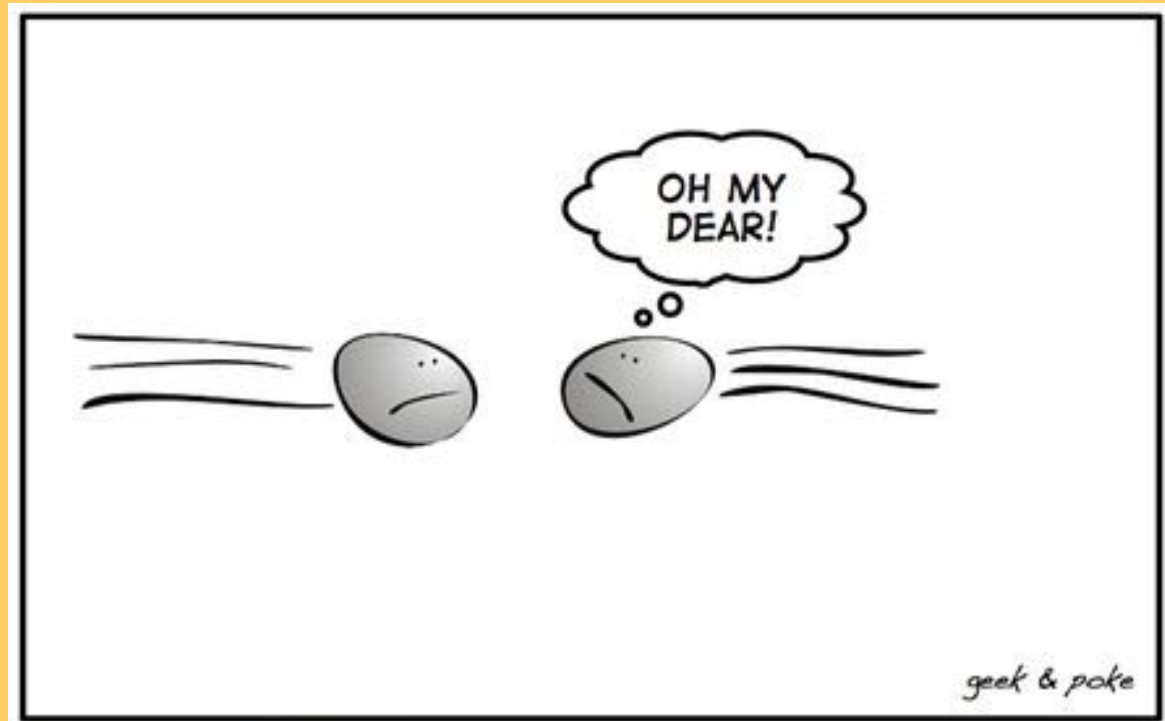
SOUP 20|21: INFN School on Underground Physics

# Dark Matter

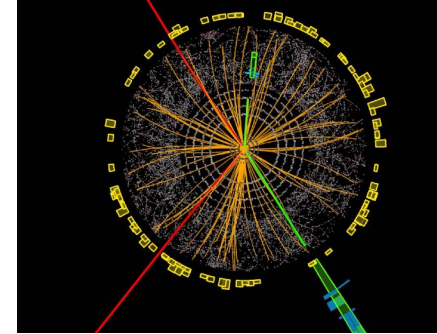
- DM evidence is purely gravitational
  - Galaxy clusters dynamics
  - Rotational curves of spiral galaxies
  - Gravitational lensing
  - Hydrodynamical equilibrium of hot gas in galaxy clusters
  - Energy budget of the Universe
  - The same theory of structure formation
  
- This evidence can be ascribed either to:
  - Modification of the theory of Gravity (difficult to explain all observations)
  - Elementary particle, relic from the early Universe
    - No viable candidate in the SM: **New Physics BSM**
    - However, to demonstrate that DM is a new particle, a non-gravitational signal (due to its particle physics nature) is needed



# NON – GRAVITATIONAL SIGNALS OF PARTICLE DM



# A multiple approach



- Astrophysical signals

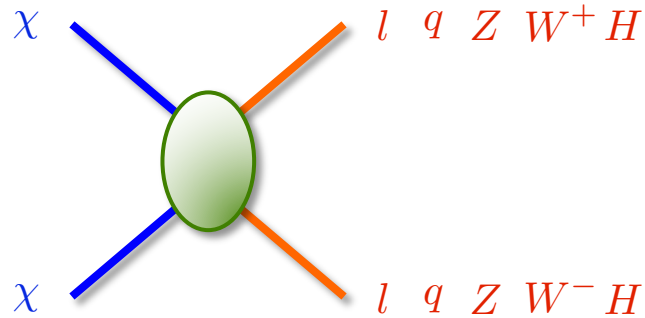
- Tests DM as particle in its environment
- Signals are not produced under our own direct control
- Complex backgrounds
- Multimessenger, multiwavelength, multitechnique strategy

- Accelerator / Lab signals

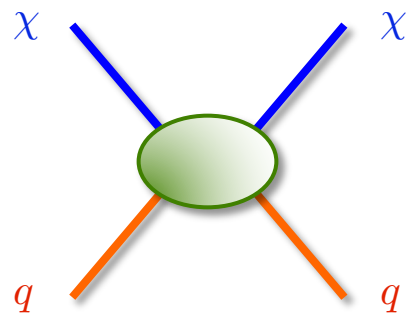
- Produce New Physics states and help in shaping the underlying model
- Allows (hopefully) to identify the physical properties of the DM sector
- Controlled environment

One does not fit all ... profit of all opportunities

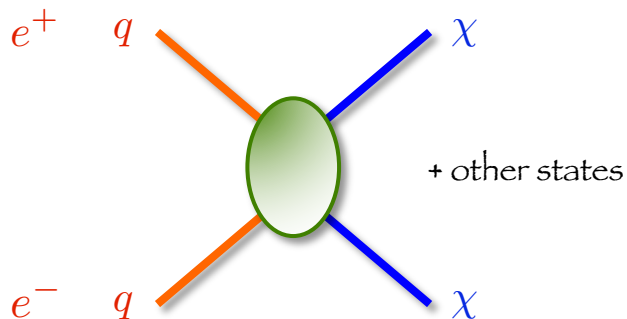
# Mechanisms of DM signal production



Annihilation (or decay)

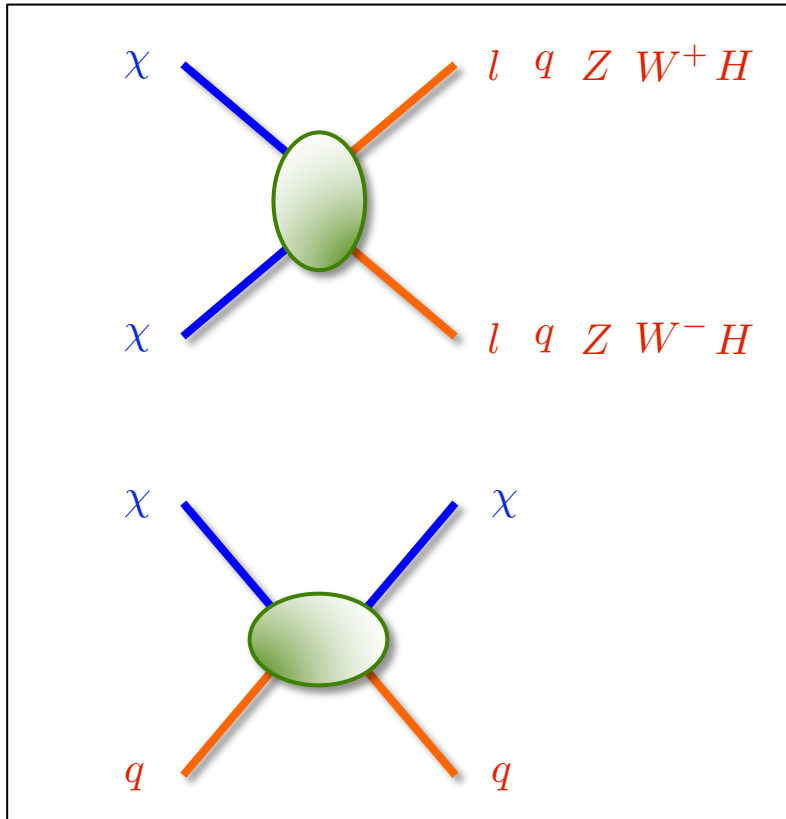


Scattering with ordinary matter



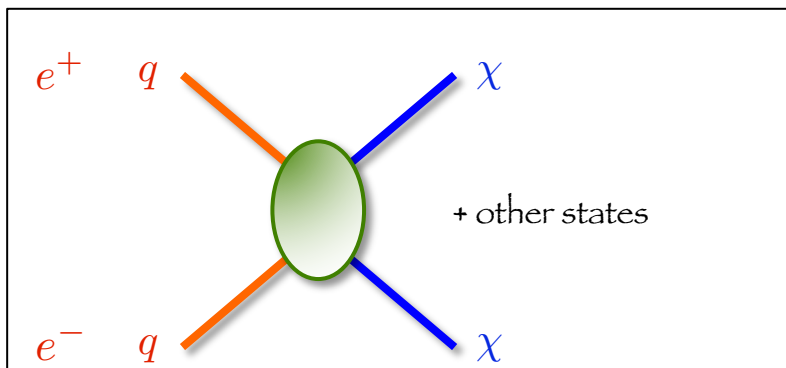
Production at accelerators

# Mechanisms of DM signal production



Signals occur in astrophysical context

Directly test DM the particle-physics nature of DM



Signal produced in accelerators

Directly tests New Physics: compatibility with DM needs to be cross-checked with cosmology and astrophysics

# DM as a particle might ...

Interact with ordinary matter

Inside our detector

Direct detection

Produce effects in astrophysical environments, like in stars

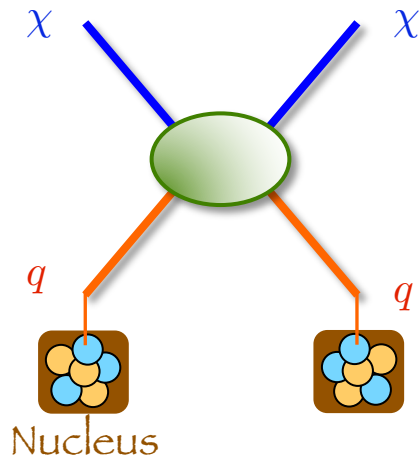
Self annihilate or decay

Send us messengers

Indirect detection

Exotic injections that can alter properties of messengers (e.g. CMB: SZ, reionization; gamma-rays absorption)

# Direct detection signal



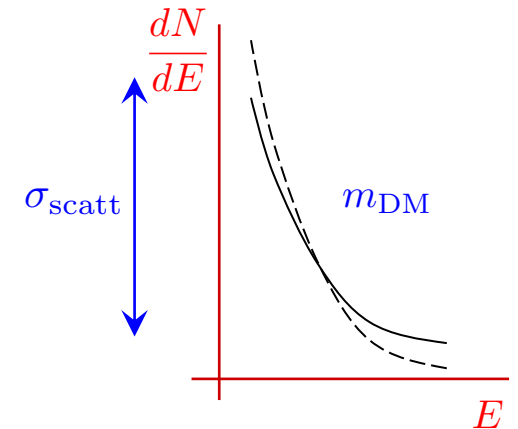
Scattering with ordinary matter

Relevant particle physics properties:

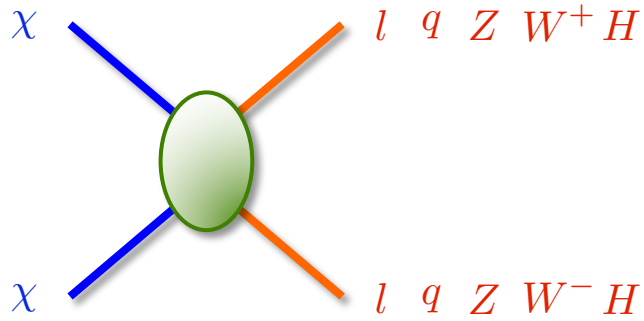
1. Scattering cross section
2. Mass of the DM particle

1 + 2 : Size of the signal

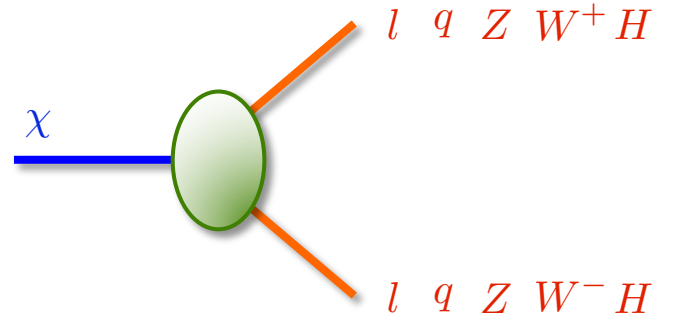
2 : Spectral features of nuclear recoil



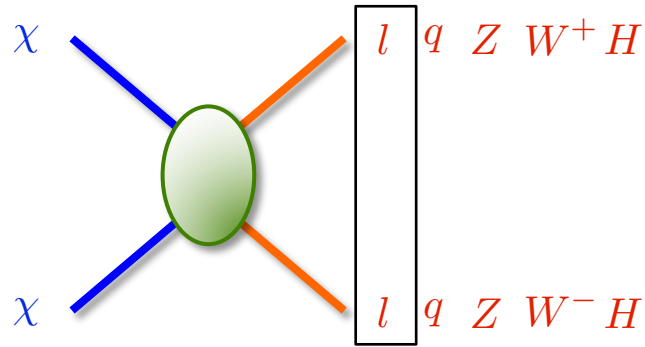
# Indirect astrophysical signals



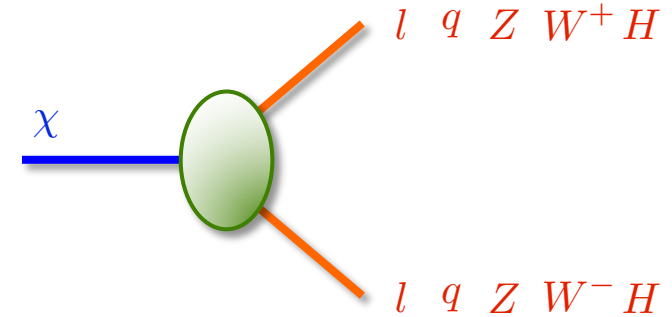
Annihilation  
or decay



# Indirect astrophysical signals



Annihilation  
or decay



$e, \mu, \tau$

$e^\pm$

$\nu_e, \nu_\mu, \nu_\tau$

$\gamma_{\text{FSR}}$

Which channel is open depends on the mass of the non-relativistic DM particle

$m_i < m_{\text{DM}}$  ann

$m_i < m_{\text{DM}}/2$  decay

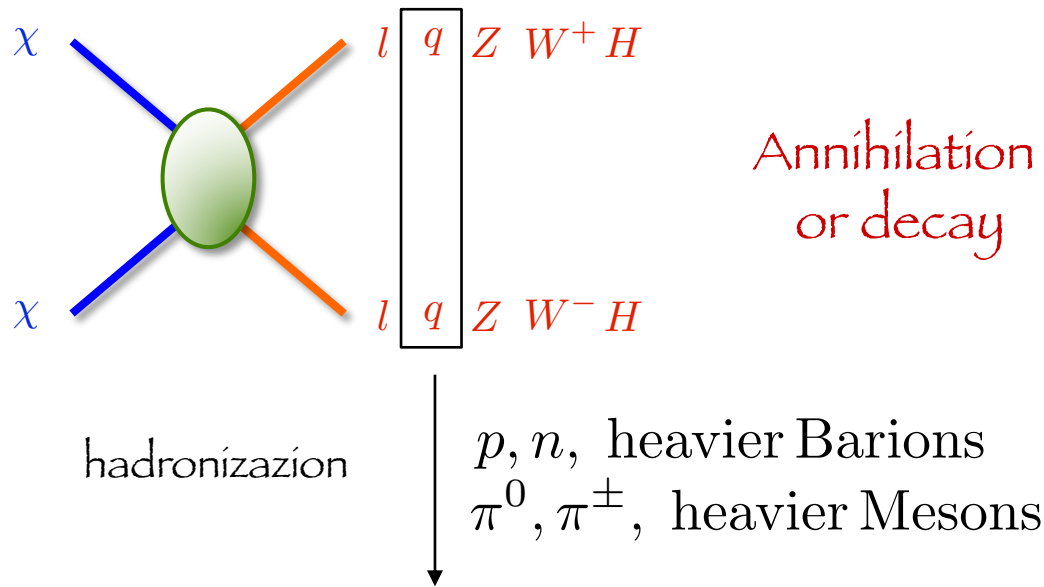
The maximal energy of the final product also depends on the mass of the DM particle

$E < m_{\text{DM}}$  ann

$E < m_{\text{DM}}/2$  decay



# Indirect astrophysical signals



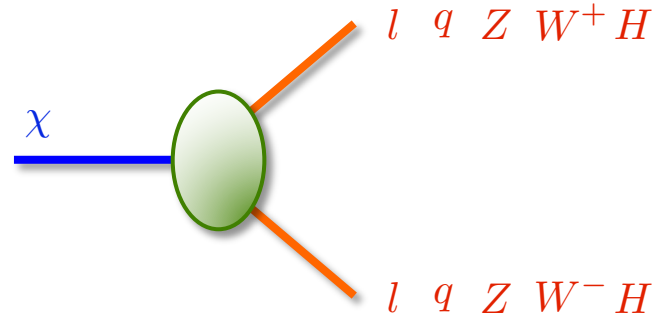
$\bar{p}, \bar{D}, \bar{H}e$

$\gamma$

$e^\pm$

$\nu_e, \nu_\mu, \nu_\tau$

$\gamma_{\text{FSR}}$



Which channel is open depends on the mass of the non-relativistic DM particle

$m_i < m_{\text{DM}}$  ann

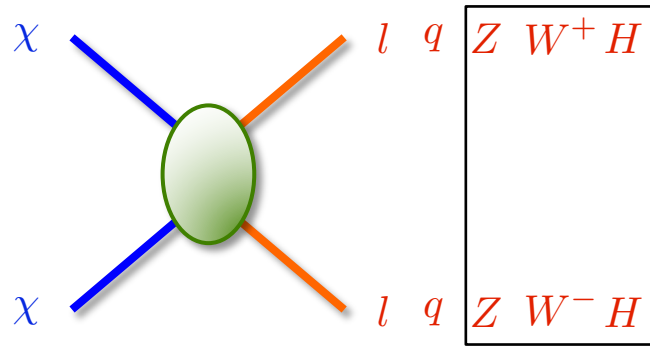
$m_i < m_{\text{DM}}/2$  decay

The maximal energy of the final product also depends on the mass of the DM particle

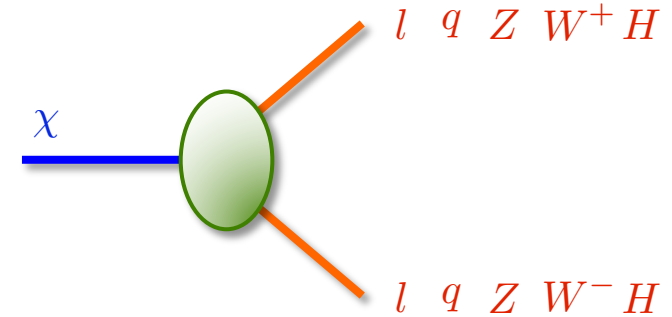
$E < m_{\text{DM}}$  ann

$E < m_{\text{DM}}/2$  decay

# Indirect astrophysical signals



Annihilation  
or decay



Which channel is open depends on  
the mass of the non-relativistic DM  
particle

$m_i < m_{\text{DM}}$	ann
$m_i < m_{\text{DM}}/2$	decay

$\bar{p}, \bar{D}, \bar{H}e$

$\gamma$

$e^\pm$

$\nu_e, \nu_\mu, \nu_\tau$

$\gamma_{\text{FSR}}$

The maximal energy of the final  
product also depends on the mass  
of the DM particle

$E < m_{\text{DM}}$	ann
$E < m_{\text{DM}}/2$	decay

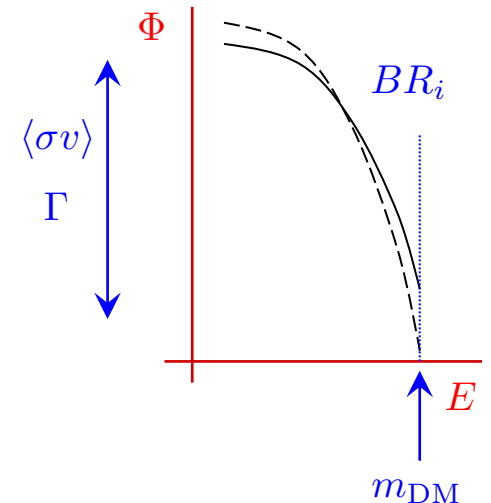
# Indirect astrophysical signals



Relevant particle physics properties:

1. Annihilation cross section (\*) (or decay rate)
2. Mass of the DM particle
3. BR in the different final states

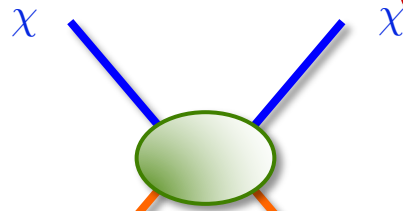
1 + 2 : Size of the signal  
 2 + 3 : Spectral features



(\*) Determines also the cosmological relic abundance (for a thermal DM)

$$\Omega h^2 = 0.11 \iff \langle \sigma_{\text{ann}} v \rangle = 2.3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

# Neutrino signals from Earth and Sun



Scattering with ordinary matter  
Capture



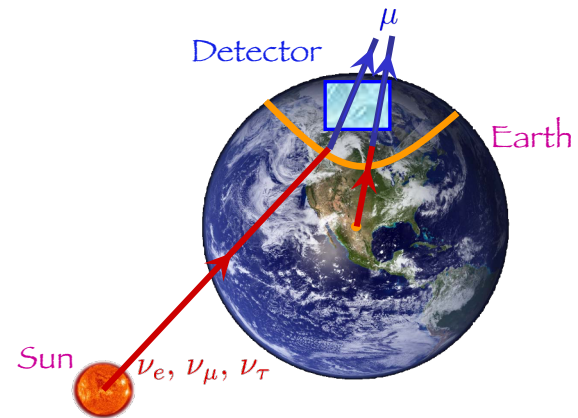
Annihilation (or decay)  
Generation of the neutrino signal



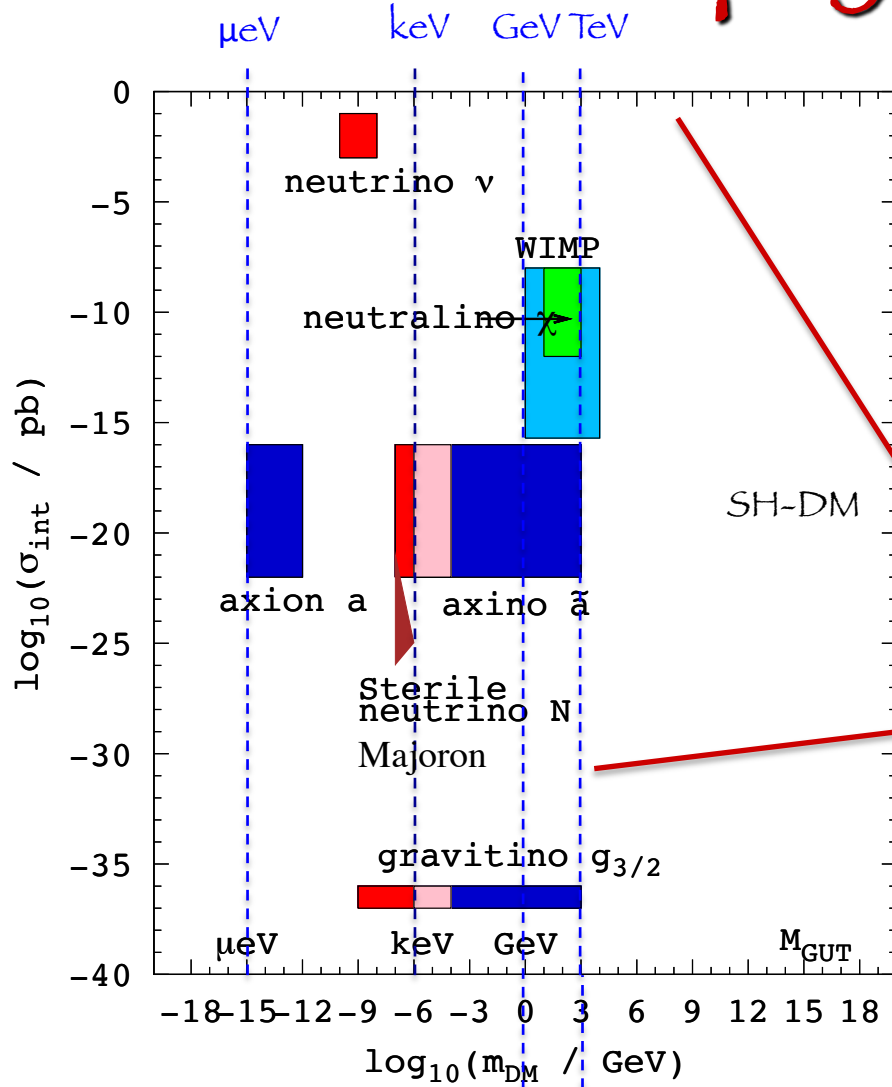
Relevant particle physics properties:

1. Scattering cross section
2. (Annihilation cross section)
3. Mass of the DM particle
4. BR in the different final states

1 + 2 : Size of the signal  
3 + 4 : Spectral features



# Particle physics scales



“Strong (-ish)”

- Self-interacting
- Technicolor DM
- ...

“EM (-ish)”

- Millicharged DM
- Electric/magnetic dipole
- ...

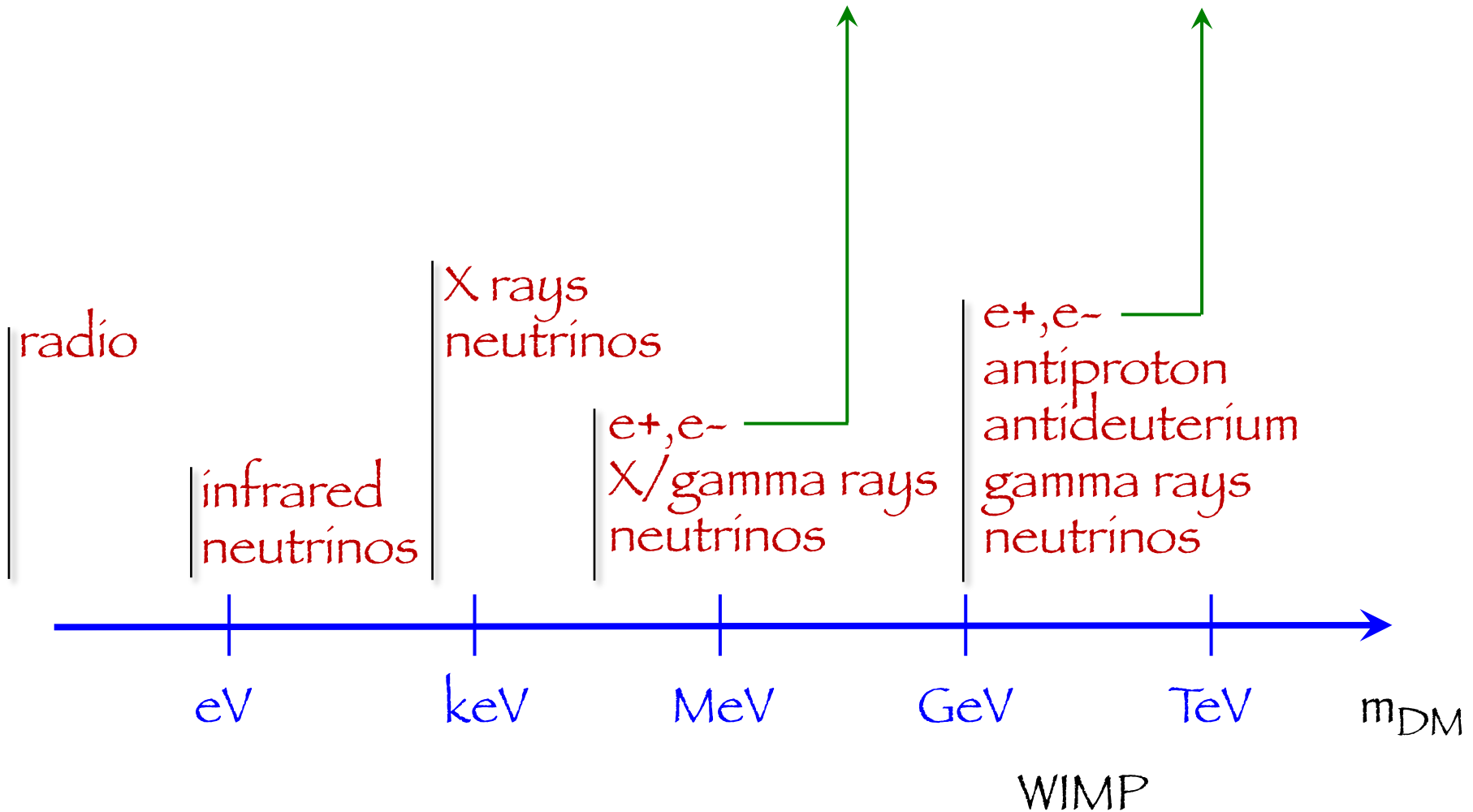
Weak

- WIMP

Gravitational

# The Multimessenger Landscape

X/gamma rays: IC on radiation fields  
radio: synchro on ambient mag fields



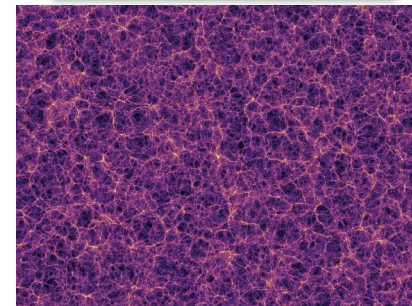
# Multi: messenger/wavelength/technique

	WIMP non WIMP	WIMP non WIMP	WIMP
Photons	radio	IR	X gamma
Cosmic rays	electrons/positrons antiprotons, antideuterium, antinuclei		WIMP, non WIMP WIMP
Neutrinos			WIMP, non WIMP
Gravitational waves		non WIMP (DM = primordial BH)	
Direct detection			WIMP, non WIMP
Accelerator searches for New Physics			WIMP, non WIMP

# Where to search for a signal

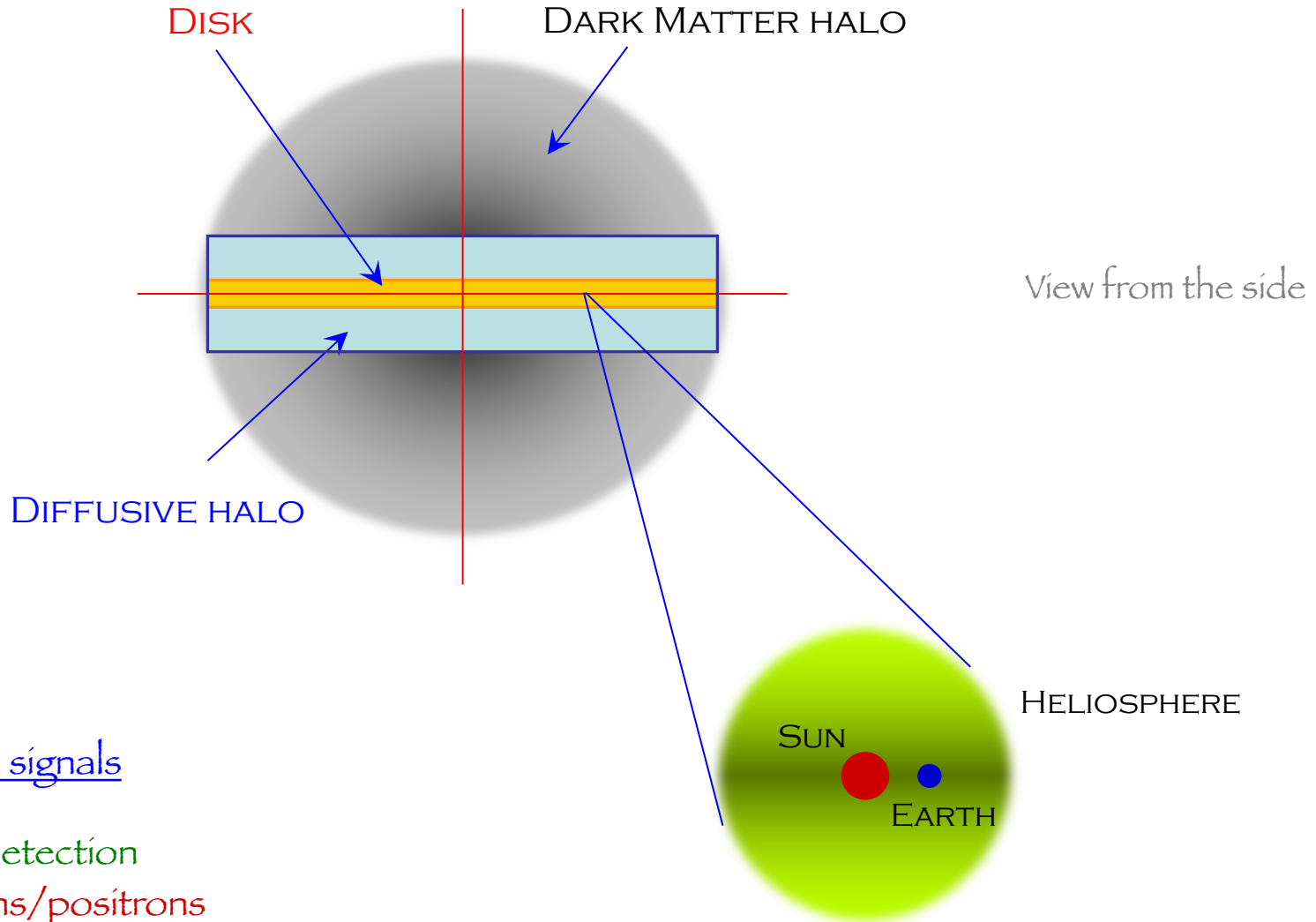
DM is present in:

- Our Galaxy
  - smooth component
  - subhalos
- Satellite galaxies (dwarfs)
- Galaxy clusters
  - smooth component
  - individual galaxies
  - galaxies subhalos
- “Cosmic web”





# Galactic environment



## Galactic signals

Direct detection

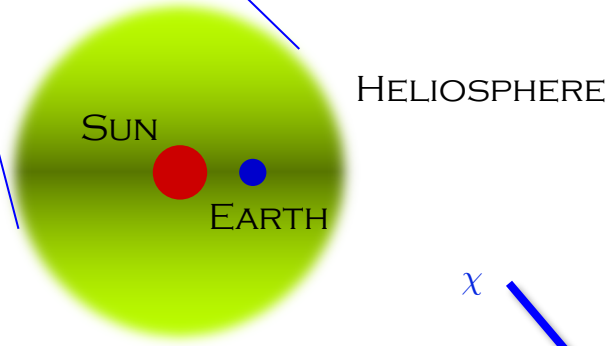
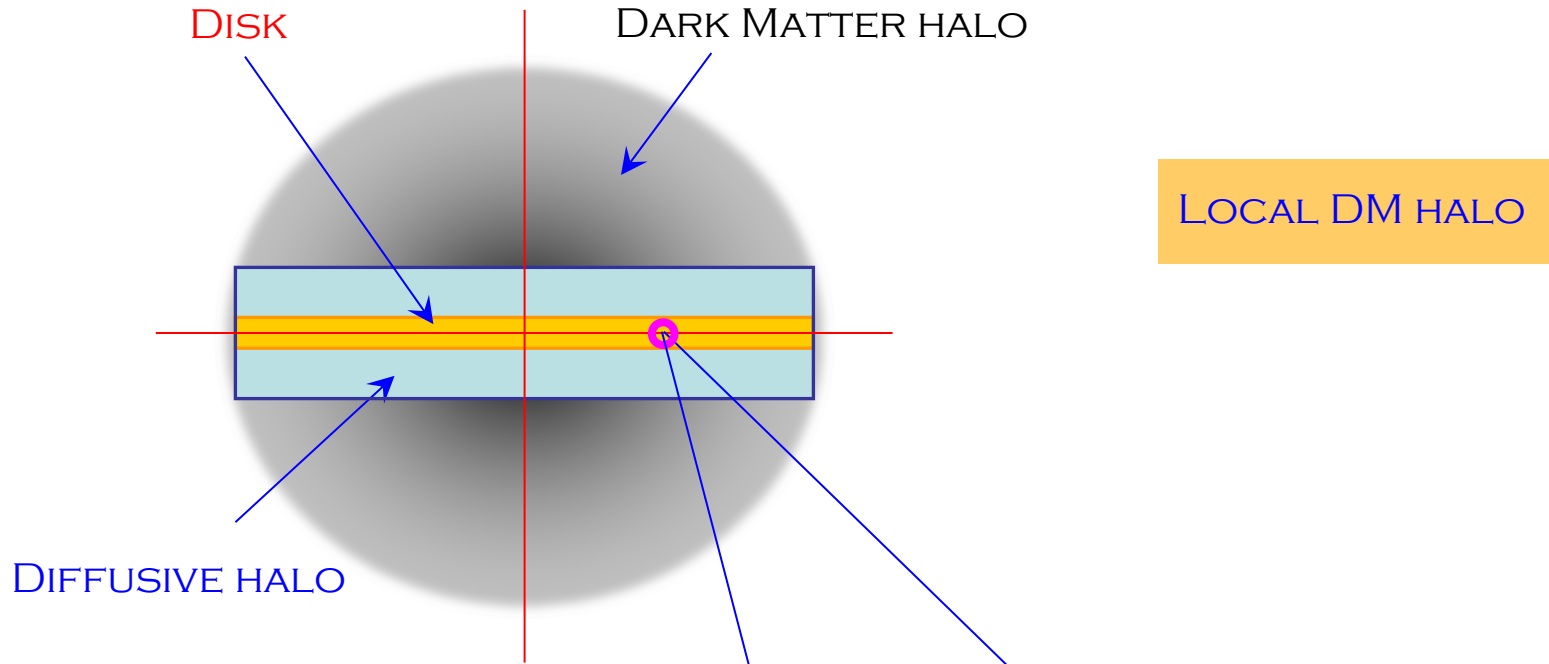
Electrons/positrons

Antiprotons

Antideuterons

Photons (from radio to gamma rays)

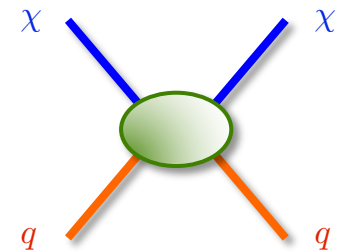
neutrinos

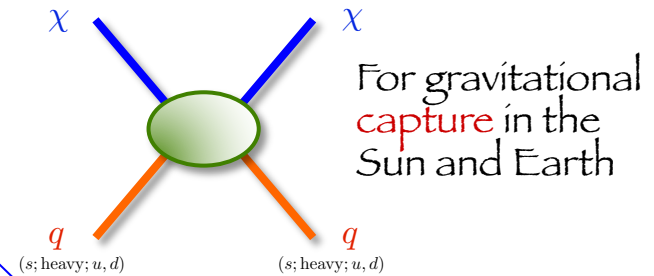
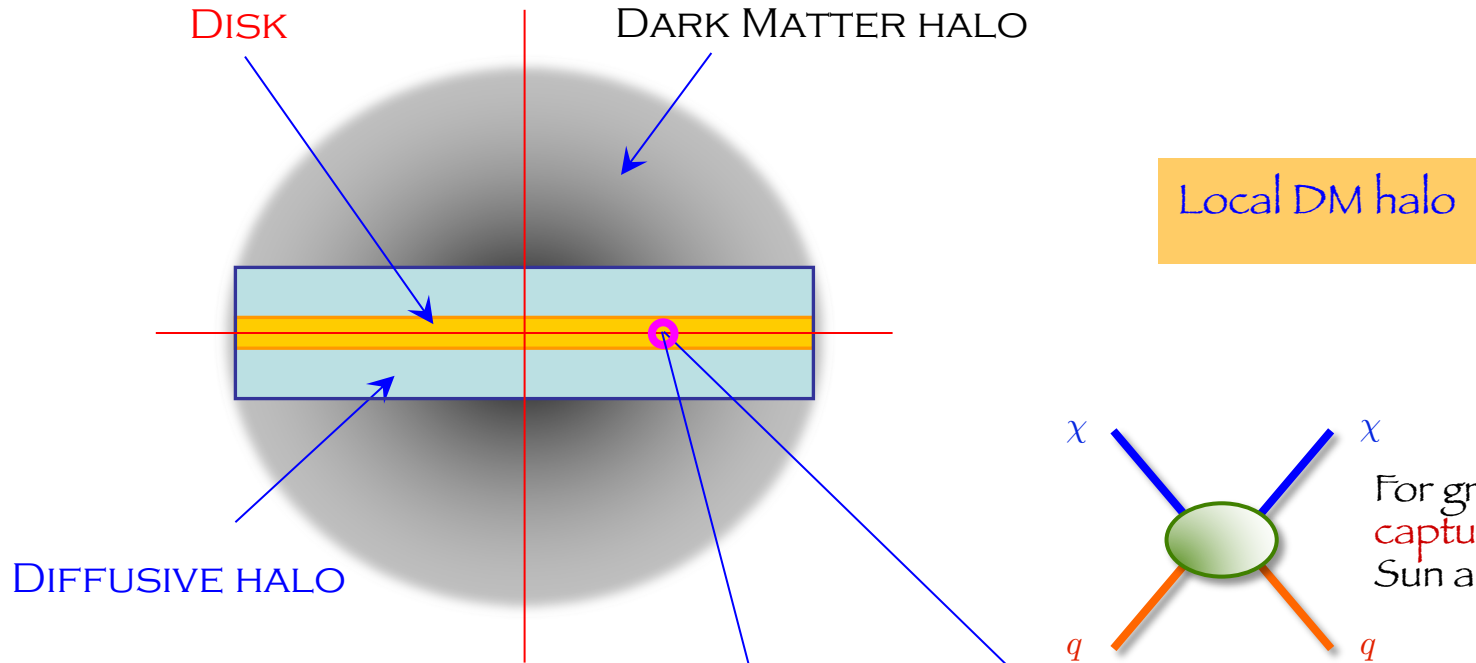


Galactic signals

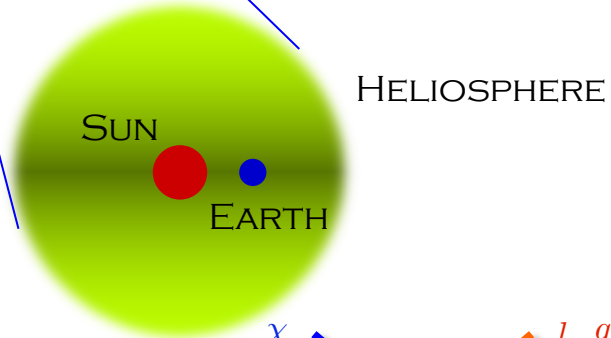
Direct detection

Feels only the local DM density  
 Feels how DM is locally distributed in velocity space





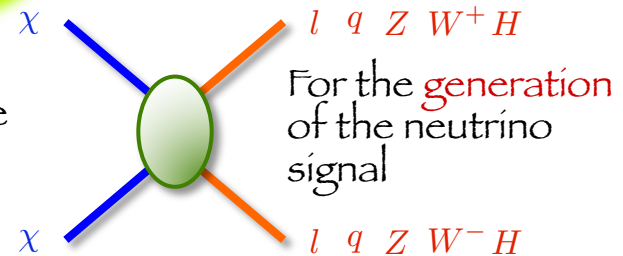
For gravitational capture in the Sun and Earth



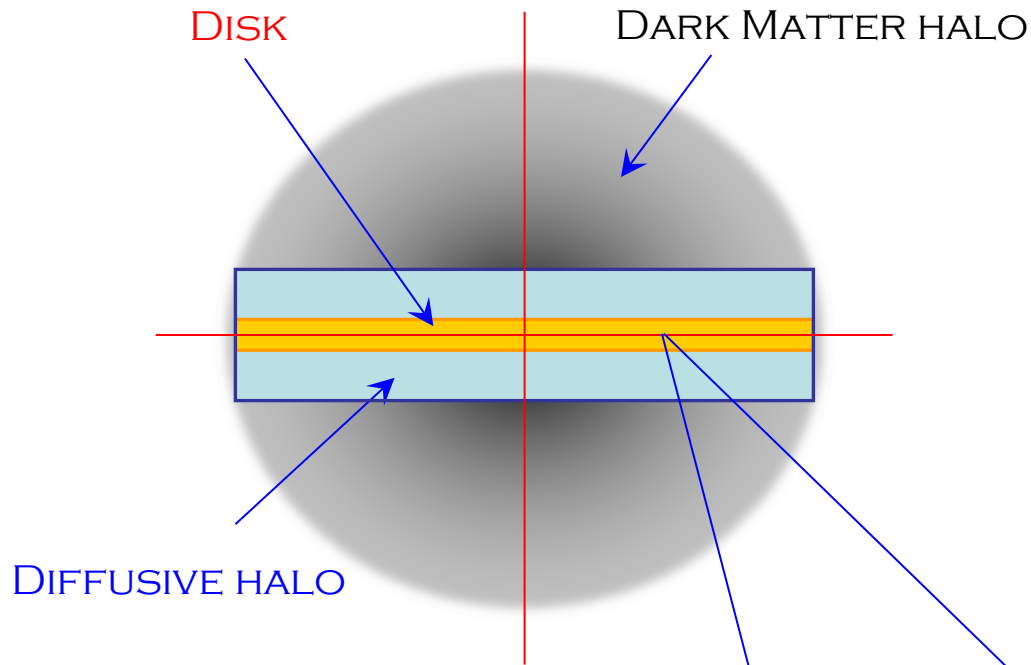
Galactic signals

Neutrinos from earth and sun

Feels only the local DM density  
 Feels (somehow) how DM is locally distributed in velocity space



For the generation of the neutrino signal

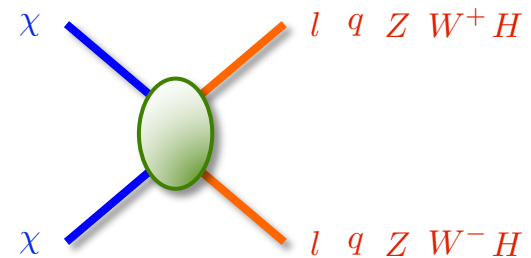
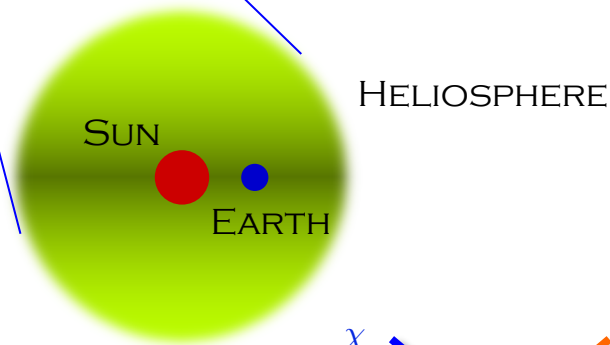


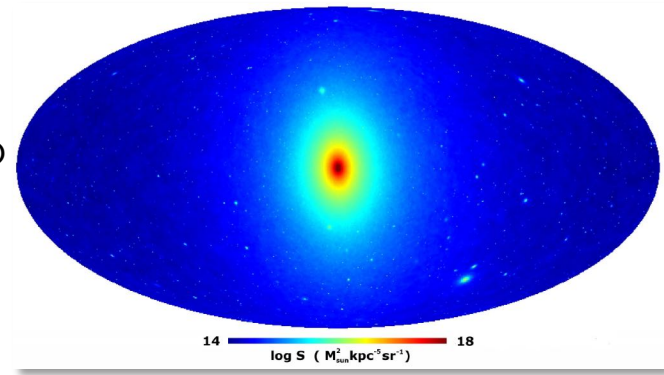
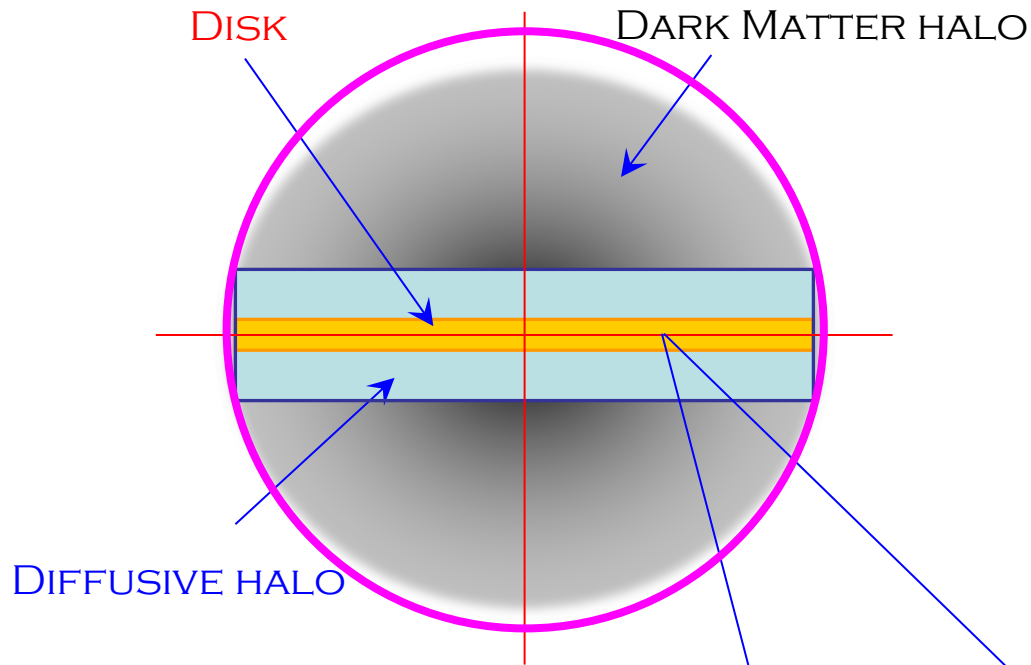
DM HALO PROFILE  
SUBSTRUCTURES

Galactic signals

Direct detection

- Electrons/positrons
- Antiprotons
- Antideuterons
- Photons (from radio to gamma rays)
- Neutrinos from the Galaxy





Gamma rays  
 prompt ( $\pi^0$  decay)  
 IC from  $e^+/e^-$  on ISRF

Radio  
 synchrotron emission from  
 $e^+/e^-$  on galactic  $B$

Galactic signals

Direct detection

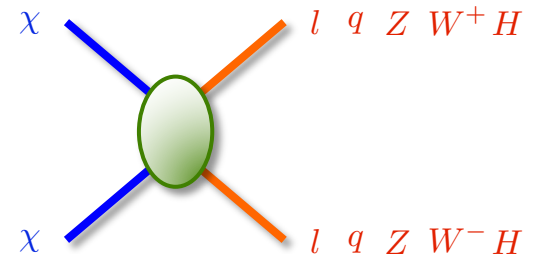
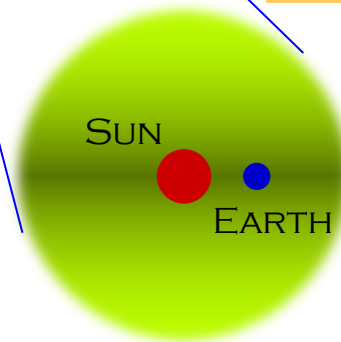
Electrons/positrons

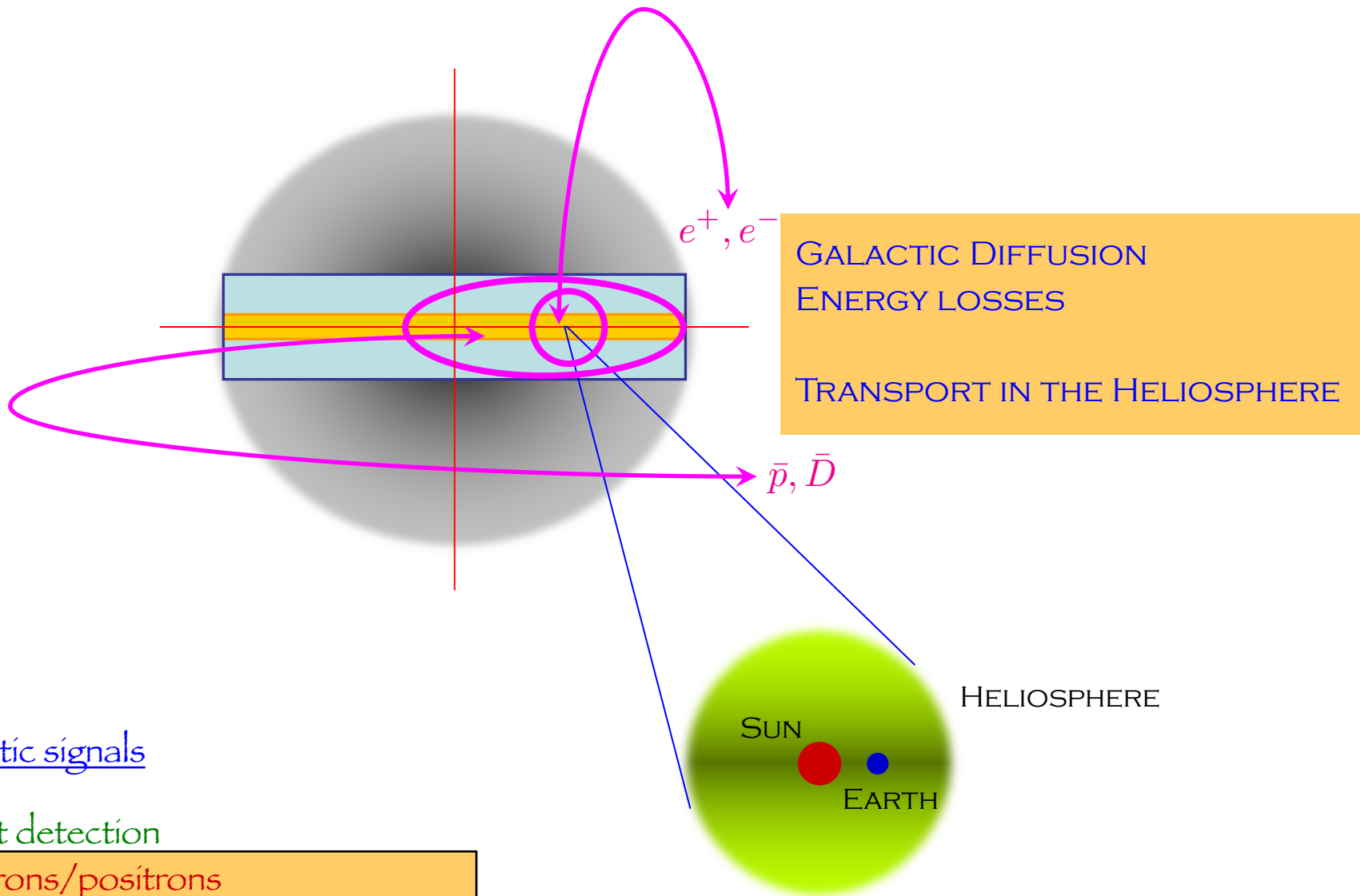
Antiprotons

Antideuterons

Photons (from radio to gamma rays)

Neutrinos from the Galaxy





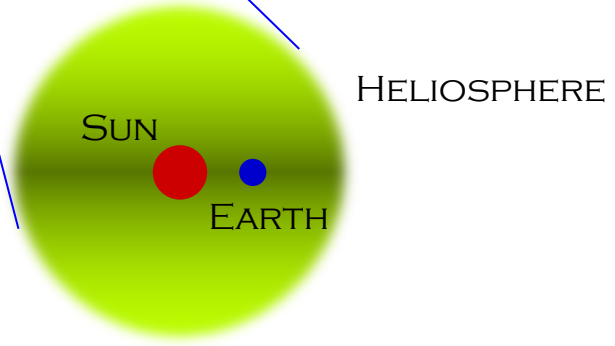
GALACTIC DIFFUSION  
 ENERGY LOSSES  
 TRANSPORT IN THE HELIOSPHERE

Galactic signals

Direct detection

- Electrons/positrons
- Antiprotons
- Antideuterons

Photons (from radio to gamma rays)  
 Neutrinos from the Galaxy



HELIOSPHERE

SUN

EARTH

# Extra-galactic environment

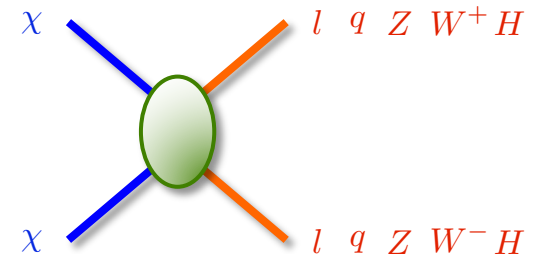
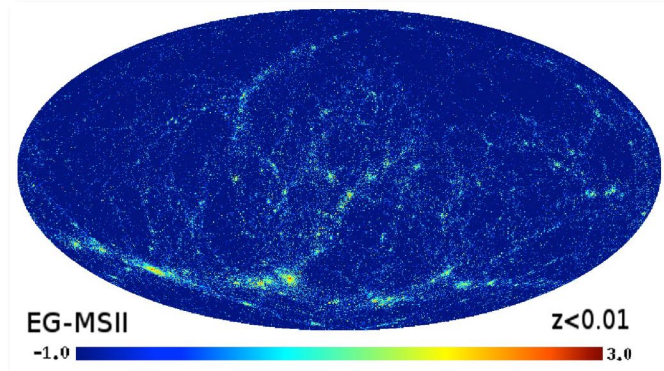
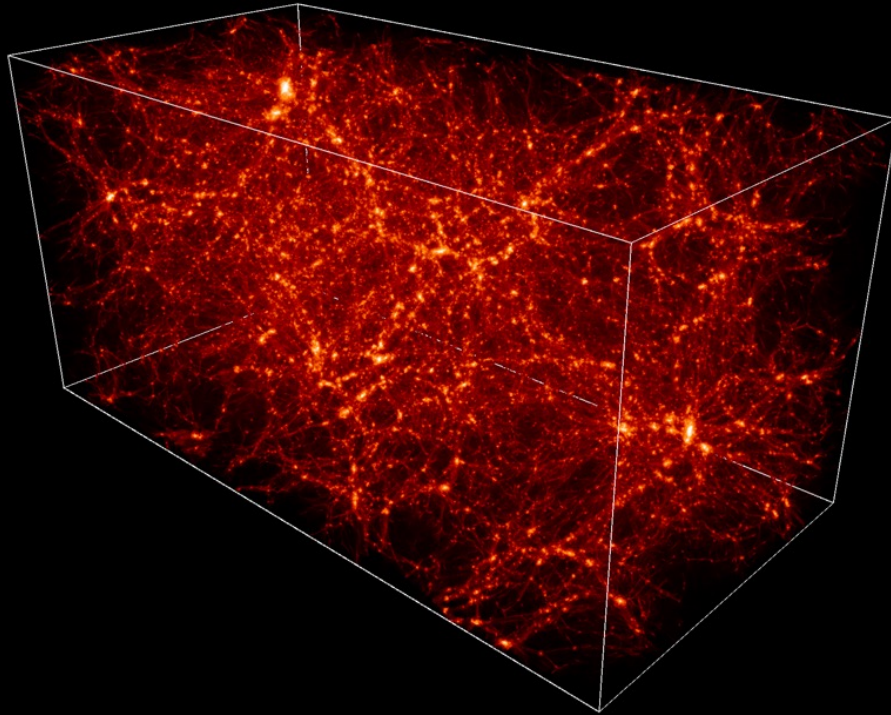
## Extragalactic signals

Photons: gamma,  $\chi$ , radio

Neutrinos

Sunyaev-Zeldovich effect on CMB

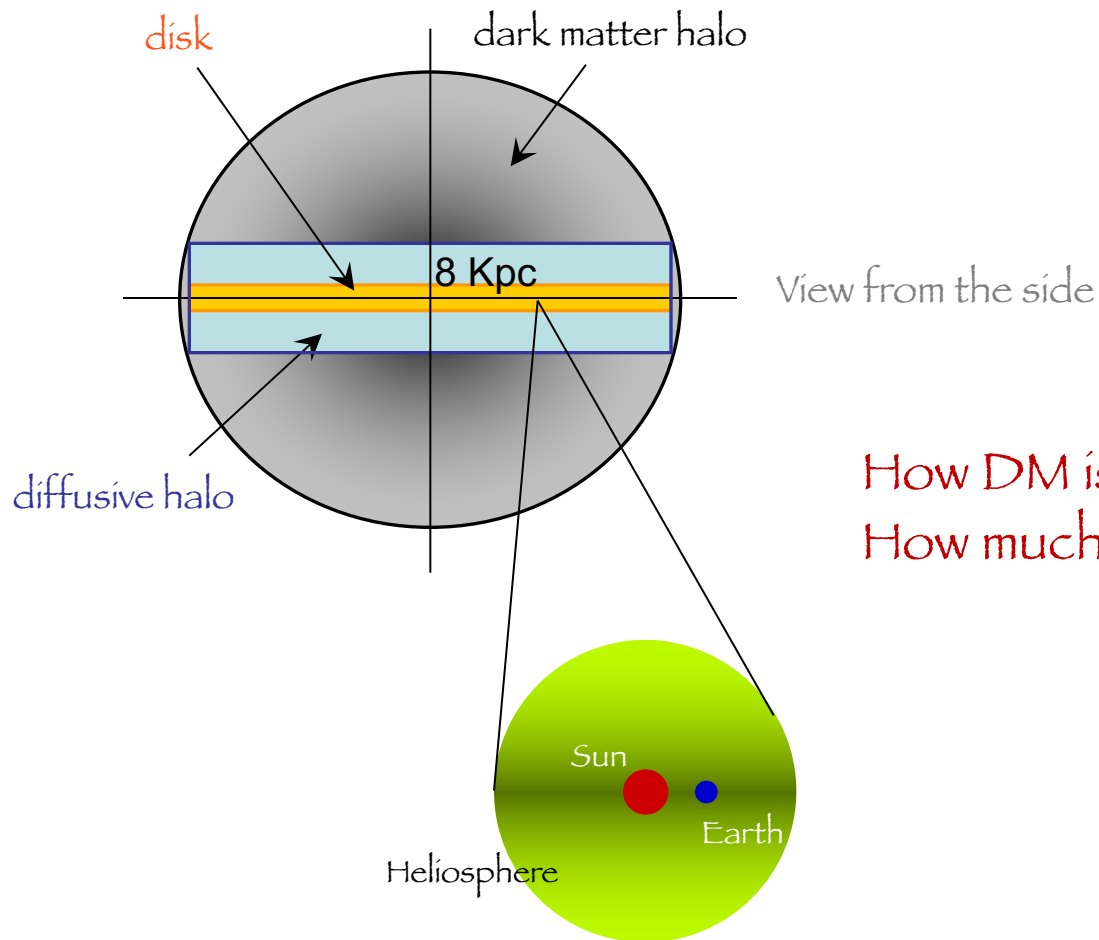
Optical depth of the Universe



# DM DISTRIBUTION IN GALAXIES



# Galactic environment



How DM is distributed in the Galaxy?  
How much DM is there?

1 pc = 3.26 ly

# The vanilla model: isothermal sphere

$$v_0^2 \equiv v_{\text{rot}}^2(R_\odot) = \frac{G}{R_\odot} [M_{\text{vis}} + M_{\text{DM}}]$$

\*  $\rho_{\text{DM}}(r) = \frac{v_0}{4\pi G} \frac{1}{r^2} \longrightarrow \frac{v_0}{4\pi G} \frac{r^2 + 3R_c^2}{(r^2 + R_c^2)^2}$   
unphysical at small  $r$

\*  $f(v) = N \exp(-v^2/v_0^2)$

# Numerical simulations

Cold Dark Matter

N-body

Gas coolings, photo-ionization

Star formation, ISM model

Stellar evolution

Stellar feedback (winds)

Black holes and SMBH feedback

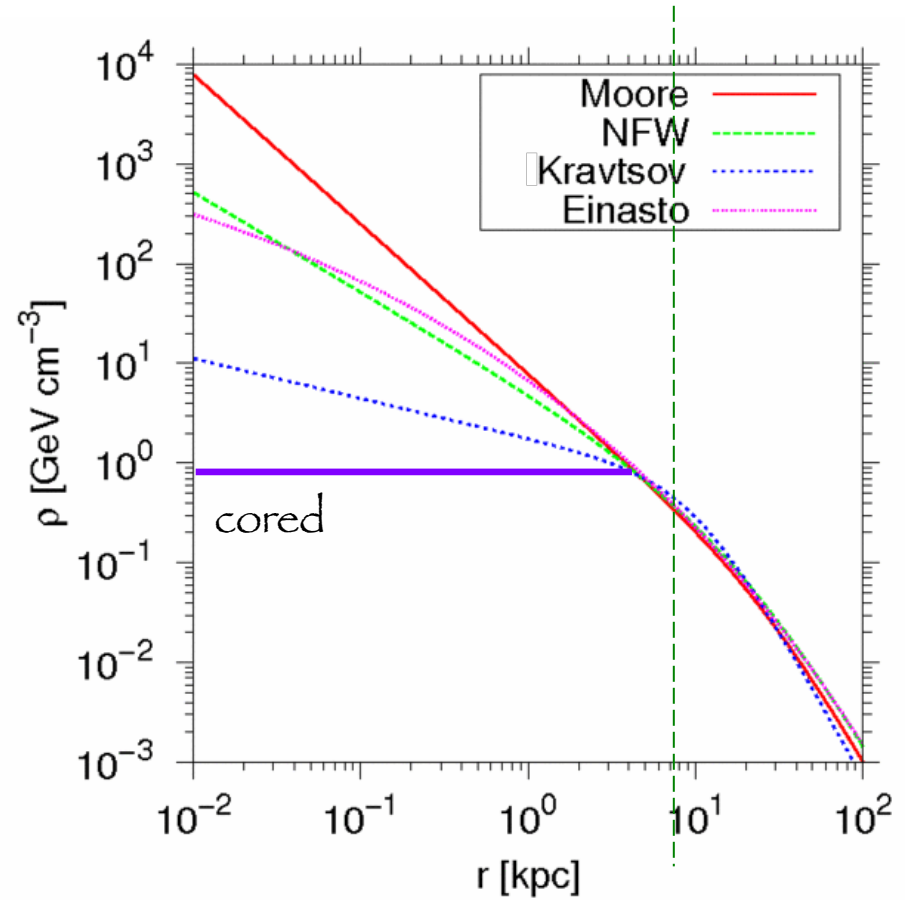
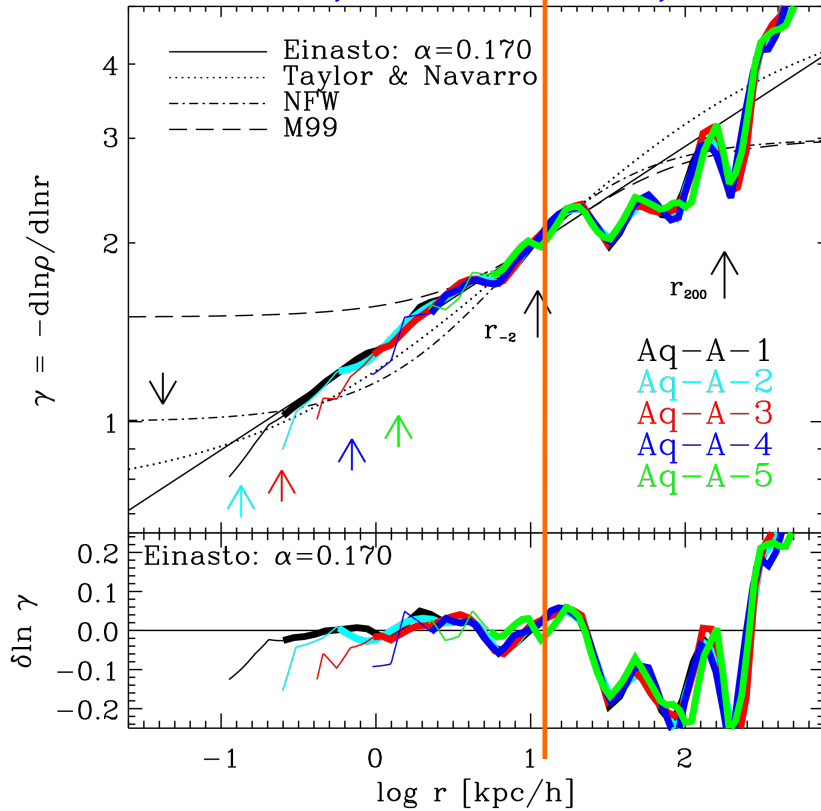
Hydrodinamical

Volume:  $(100 \text{ Mpc})^3$

DM particles/cells:  $10^9 - 10^{10}$

# Density profile: smooth component

## Log-slope of density profile



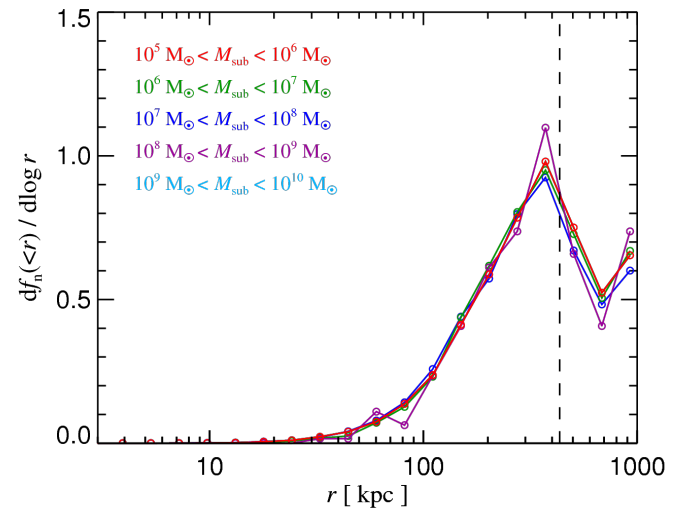
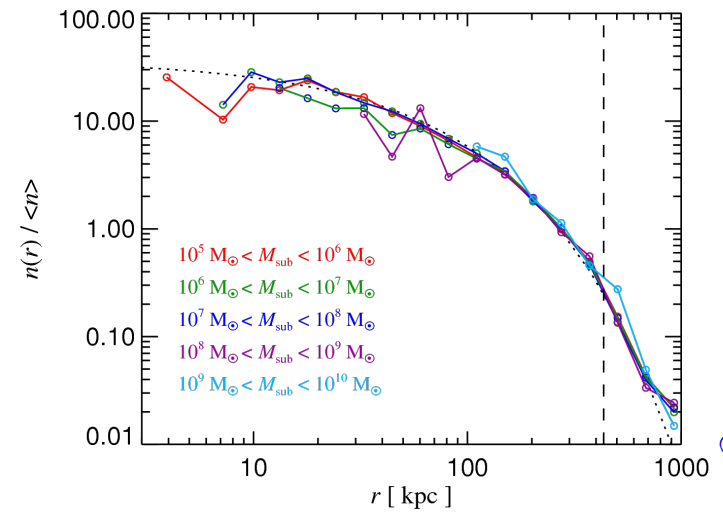
From numerical simulations

Navarro et al., arXiv:0810.1522

# CDM: Subhalos

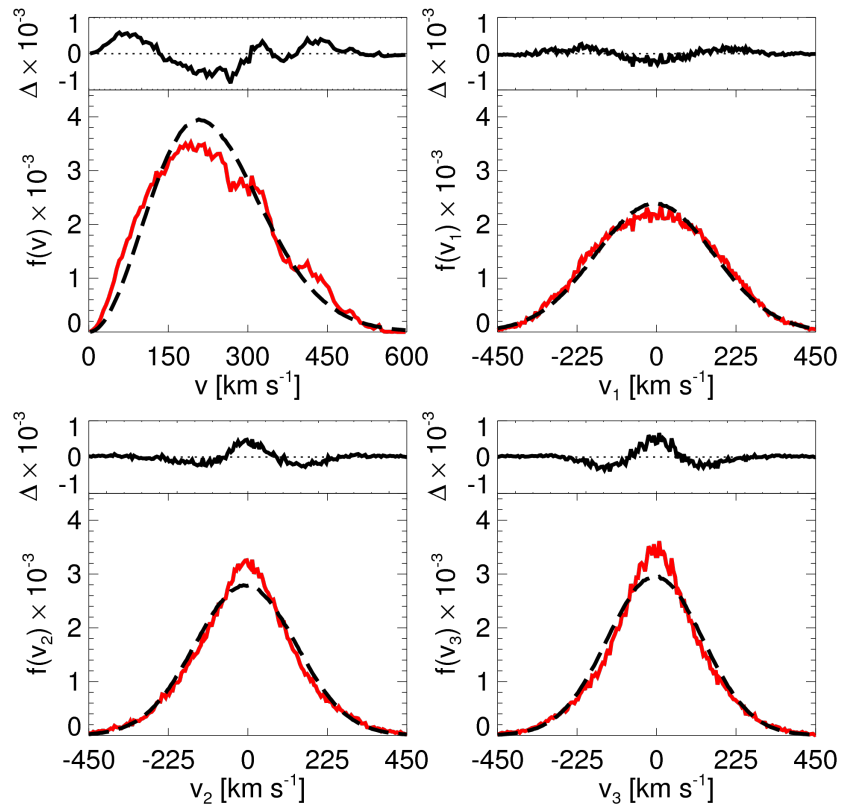


The Aquarius Project

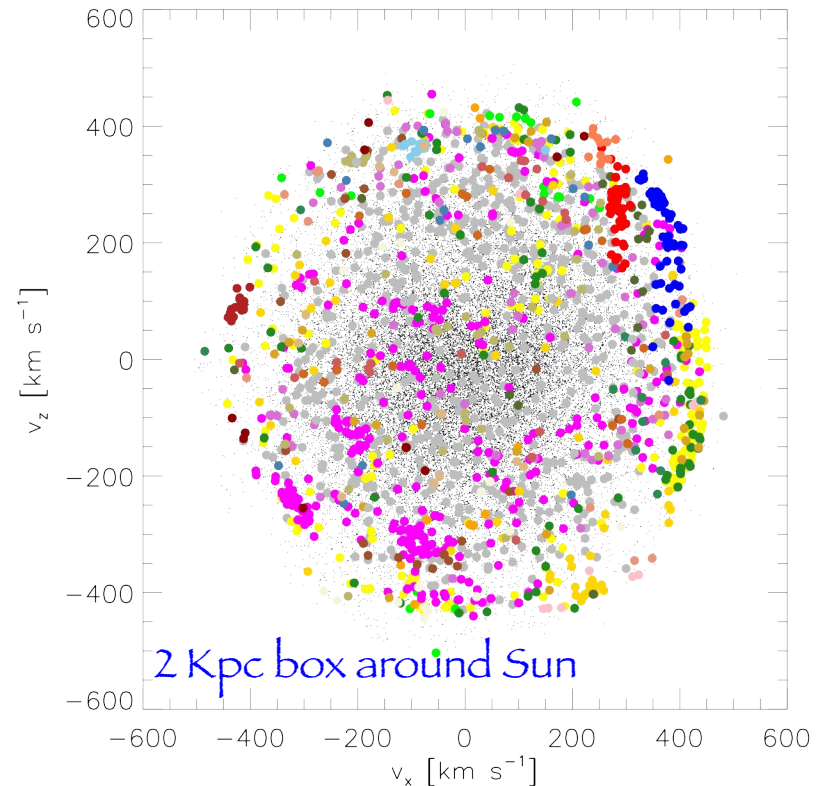


Most subhalos are in the outer halo

# Velocity distribution (at Sun's position)



Velocity streams



From numerical simulations

# “Canonical” halo

$$\rho(r) \longrightarrow \rho_0 = 0.3 \text{ GeV cm}^{-3}$$

$$\rho(r) \longrightarrow r^{-1} \quad [r \rightarrow 0]$$

Some determinations [1-3]

[1]  $\rho_0 = 0.385 \pm 0.027 \text{ GeV cm}^{-3}$  (Einasto)  
 $\rho_0 = 0.389 \pm 0.025 \text{ GeV cm}^{-3}$  (NFW)

[2]  $\rho_0 = 0.43(11)(10) \text{ GeV cm}^{-3}$

$$f(\vec{v}) = N \exp(-v^2/v_0^2)|_{v_{\text{esc}}}$$

$$v_0 = (220 \pm 50) \text{ km s}^{-1}$$

$$v_{\text{esc}} = (450 \div 650) \text{ km s}^{-1}$$

[1] Catena, Ullio, arXiv:0907.0018

[2] Salucci et al. arXiv:1003.3101

[3] Pato et al., arXiv:1006.1322

# “Canonical” halo

$$\rho(r) \longrightarrow \rho_0 = 0.3 \text{ GeV cm}^{-3}$$

*Debated whether cuspy or cored  
Effect of baryons unclear*

$$\rho(r) \longrightarrow r^{-1} [r \rightarrow 0]$$

*Substructures likely are present  
(although sparsely distributed, mostly in  
the outer parts (anti-biased))*

$$f(\vec{v}) = N \exp(-v^2/v_0^2)|_{v_{\text{esc}}}$$

$$v_0 = (220 \pm 50) \text{ km s}^{-1}$$

$$v_{\text{esc}} = (450 \div 650) \text{ km s}^{-1}$$

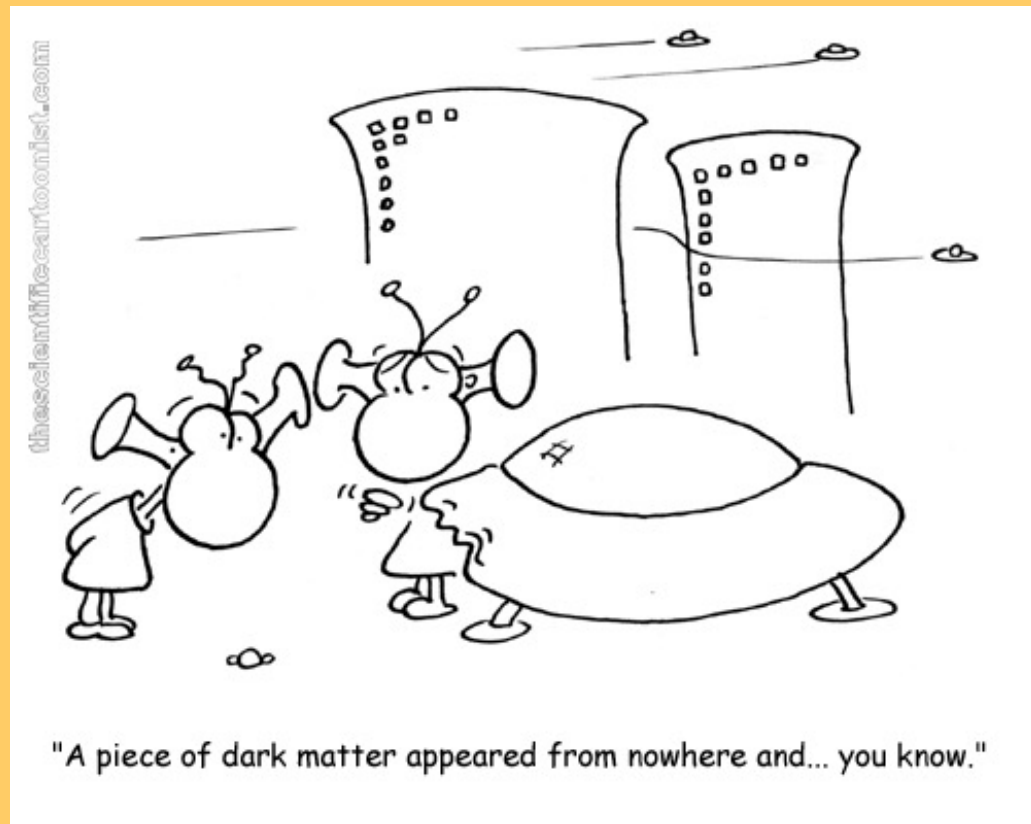
*Anisotropies may be present*

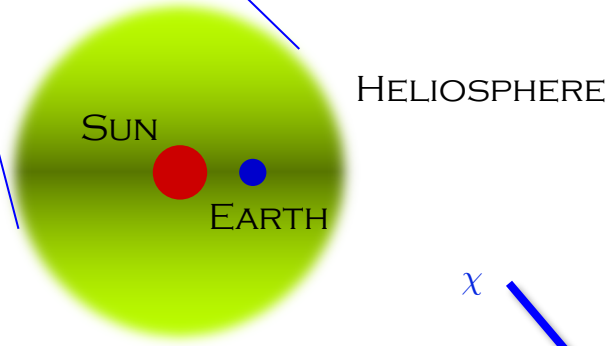
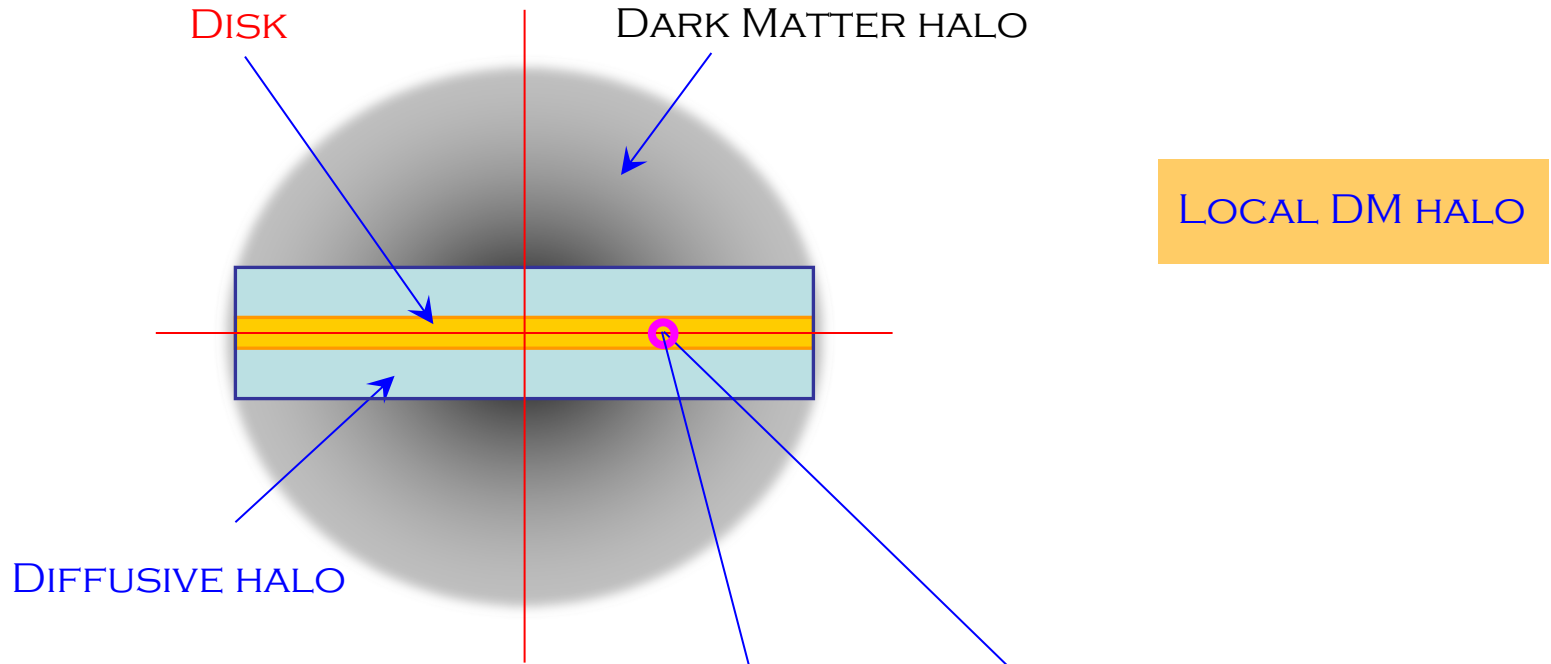
*The high- $v$  tail may not be fully “thermal”*

*Streams may have impact*



# DIRECT DETECTION OF DM

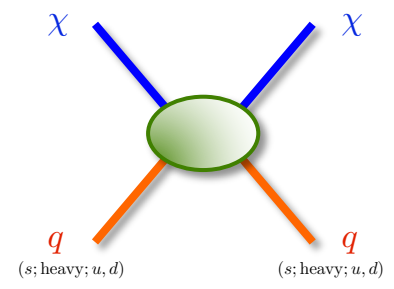




GALACTIC SIGNALS

DIRECT DETECTION

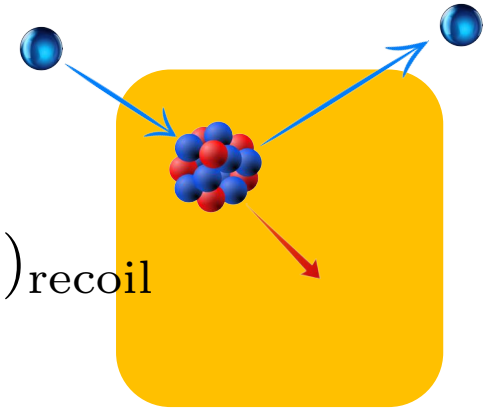
Feels only the local DM density  
 Feels how DM is locally distributed in velocity space



# Direct detection signal

Typical process for WIMP DM

$$\chi + \mathcal{N}(A_{\mathcal{N}}, Z_{\mathcal{N}})_{\text{at rest}} \rightarrow \chi + \mathcal{N}(A_{\mathcal{N}}, Z_{\mathcal{N}})_{\text{recoil}}$$



Recoil rate

$$\frac{dR}{dE_R} = \frac{\xi_{\mathcal{N}}}{m_{\mathcal{N}}} \frac{\rho_{\odot}}{m_{\chi}} \int_{v_{\min}(E_R)}^{v_{\text{esc}}} d^3v v f_E(\vec{v}) \frac{d\sigma_{\mathcal{N}}}{dE_R}(v, E_R)$$

For non-WIMP (keV, MeV) DM: interaction on electrons

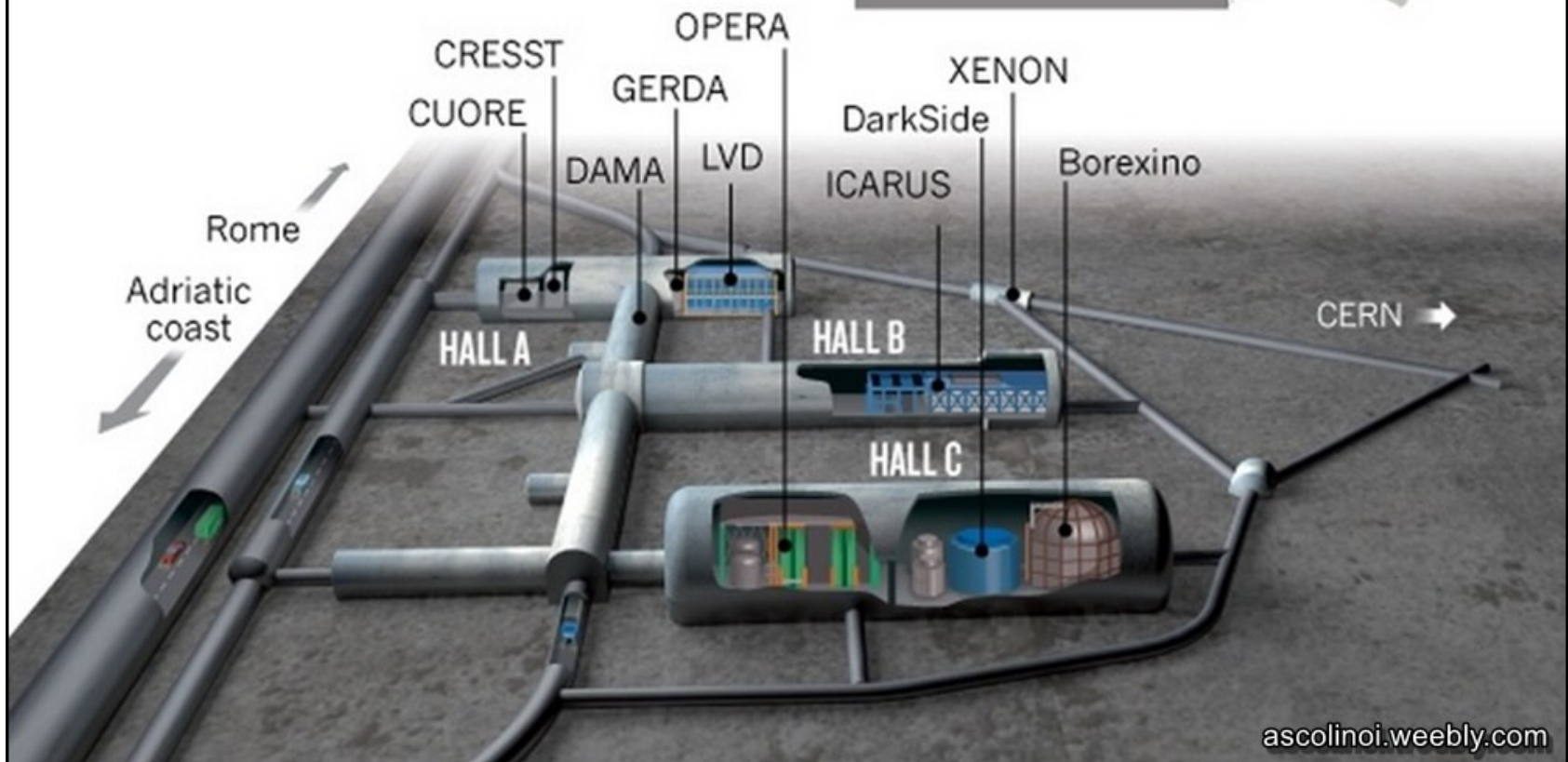
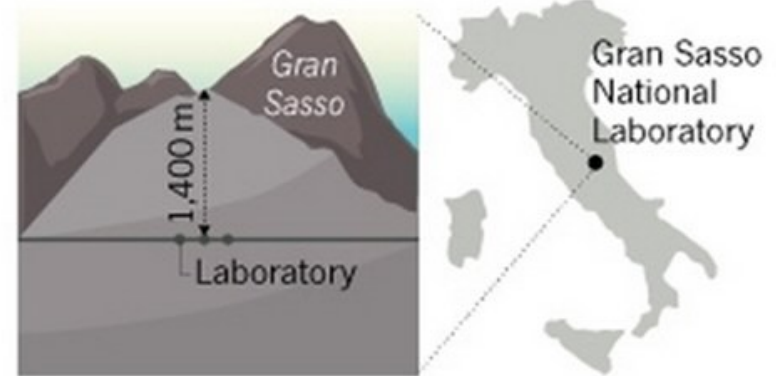
# Underground Labs



# LNGS – Gran Sasso Lab (INFN)

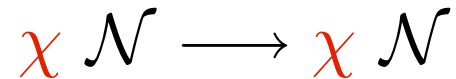
## THE A, B AND C OF GRAN SASSO

Experiments at the Gran Sasso National Laboratory are housed in and around three huge halls carved deep inside the mountain, where they are shielded from cosmic rays by 1,400 metres of rock.



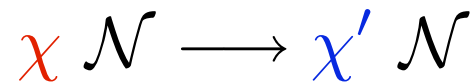
# Interaction mechanisms

- Elastic scattering with nuclei



- Coherent coupling to nucleons
- Coupling the nucleus spin
- Long-range mediators
- Electric/magnetic dipole-moment interactions
- ...

- Inelastic scattering with nuclei



- Scatter requires a mass difference between  $\chi$  and  $\chi'$  of the order of 1-100 keV

- Scattering on electrons

# Interaction mechanisms

- Elastic scattering with nuclei

WIMP DM (GeV-TeV<sup>+</sup>)

$$E_R = \mu_{\mathcal{N}}^2 v^2 (1 - \cos \theta) / m_{\mathcal{N}}$$

$$\langle E_R \rangle \sim \text{KeV} \left( \frac{m_{\mathcal{N}}}{\text{GeV}} \right) \left( \frac{m_{\chi}}{m_{\chi} + m_{\mathcal{N}}} \right)^2 \quad E_R > \text{few KeV}$$

- Inelastic scattering with nuclei

WIMP DM (GeV-TeV<sup>+</sup>)

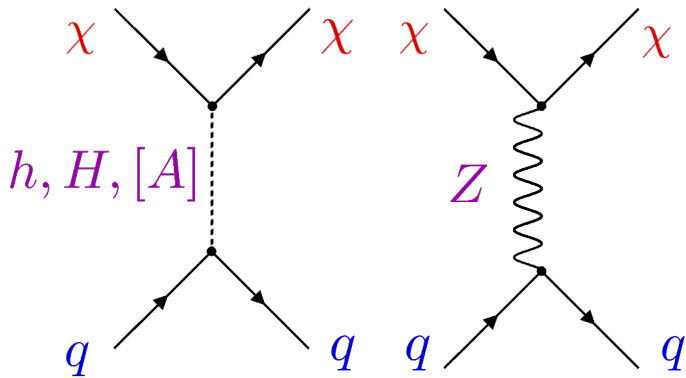
- Scattering on electrons

Light (keV) [pseudo]scalars



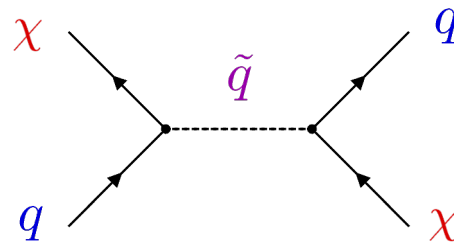
# Example: Neutralino-quark scattering

$\chi q \rightarrow \chi q$	$\tilde{q}_L, \tilde{q}_R$	s channel
	$Z, h, H, A$	t channel
	$\tilde{q}_L, \tilde{q}_L$	u channel

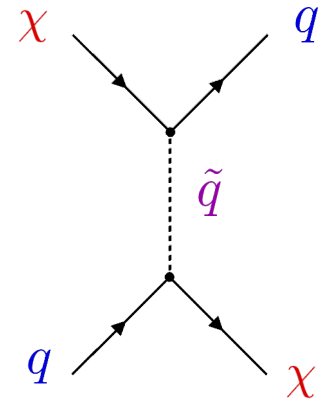


coherent

spin



coherent  
spin



coherent  
spin



# Cross section

$$\mathcal{L}_{\text{eff}} = \sum_i \bar{\alpha}_i (\bar{q} O q) (\bar{\chi} O' \chi)_i$$

$$\mathcal{L}_{\text{eff}} \longrightarrow \langle N | \bar{q} O q | N \rangle \propto \bar{\psi}_N O \psi_N \longrightarrow \langle \mathcal{N} | \bar{\psi}_N O \psi_N | \mathcal{N} \rangle$$

$$\begin{aligned} \mathcal{M} &= \langle \mathcal{N}, \chi | \mathcal{L}_{\text{eff}} | \mathcal{N}, \chi \rangle \\ &= \sum_i \langle \mathcal{N} | \bar{\psi}_N O \psi_N | \mathcal{N} \rangle \langle \chi | \bar{\chi} O' \chi | \chi \rangle_i \end{aligned}$$

# Cross section

Scattering amplitude on nucleon n

$$\mathcal{M}_n = \sum_{i=1}^{16} c_i^n(\lambda, m_\chi) \mathcal{O}_i^{\text{NR}}$$

Basis of 16 non-relativistic operators

$\lambda$ : parameters of the underlying non-relativistic theory  
(mediator masses, couplings, ...)

# Set of operators

$$\hat{O}_1 = \mathbb{1}_{\chi N} \text{ scalar}$$

$$\hat{O}_3 = i\hat{\mathbf{S}}_N \cdot \left( \frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N \text{ spin}$$

$$\hat{O}_5 = i\hat{\mathbf{S}}_\chi \cdot \left( \frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_6 = \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left( \hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_7 = \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp$$

$$\hat{O}_8 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp$$

$$\hat{O}_9 = i\hat{\mathbf{S}}_\chi \cdot \left( \hat{\mathbf{S}}_N \times \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_{10} = i\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}$$

$$\hat{O}_{11} = i\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}$$

$$\hat{O}_{12} = \hat{\mathbf{S}}_\chi \cdot \left( \hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_{13} = i \left( \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp \right) \left( \hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_{14} = i \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left( \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_{15} = - \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left[ \left( \hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp \right) \cdot \frac{\hat{\mathbf{q}}}{m_N} \right]$$

$$\hat{O}_{17} = i \left( \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp \right)$$

$$\hat{O}_{18} = i \left( \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N \right)$$

Catena, JCAP 1407 (2014) 055  
 Arina, Del Nobile, Panci, PRL 114 (2015) 011301  
 Scopel, Yoon, JCAP 1507 (2015) 041  
 Catena, Gondolo, JCAP 08 (2015) 022  
 Gluscevic et al, JCAP 12 (2015) 057  
 Catena, Ibarra, Wild JCAP 05 (2016) 039  
 Kalhofer, Wild, arXiv:1607.04418  
 (...)

Fitzpatrick et al, JCAP 1302 (2013) 004  
 Fitzpatrick et al, arXiv:1211.2818  
 Anand et al, PRC 89 (2014) 065501  
 Dent et al, PRD 92 (2015) 063515

# Cross section

Scattering amplitude on nucleon  $n$

$$\mathcal{M}_n = \sum_{i=1}^{16} c_i^n(\lambda, m_\chi) \mathcal{O}_i^{\text{NR}}$$

Basis of 16 non-relativistic operators

$\lambda$ : parameters of the underlying non-relat. theory  
(mediator masses, couplings, ...)

Transition probability on nucleus  $\mathcal{N}$

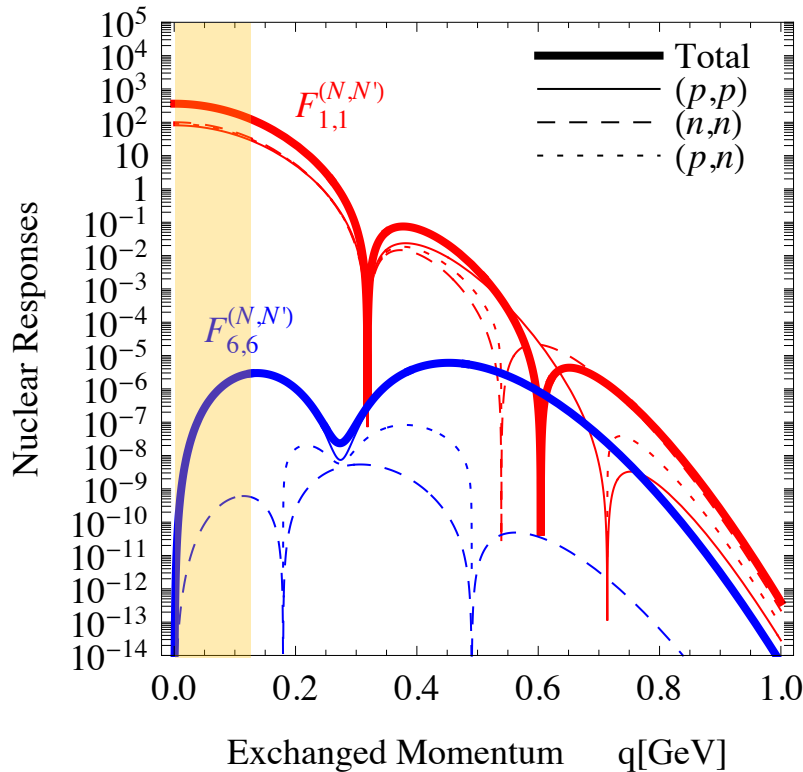
$$\overline{|\mathcal{M}_{\mathcal{N}}|^2} = \frac{m_{\mathcal{N}}^2}{m_n^2} \sum_{i,j=1}^{16} \sum_{n,n'=p,n} c_i^n c_j^{n'} F_{i,j}^{(n,n')}(\nu, E_R | \mathcal{N})$$

nuclear response functions

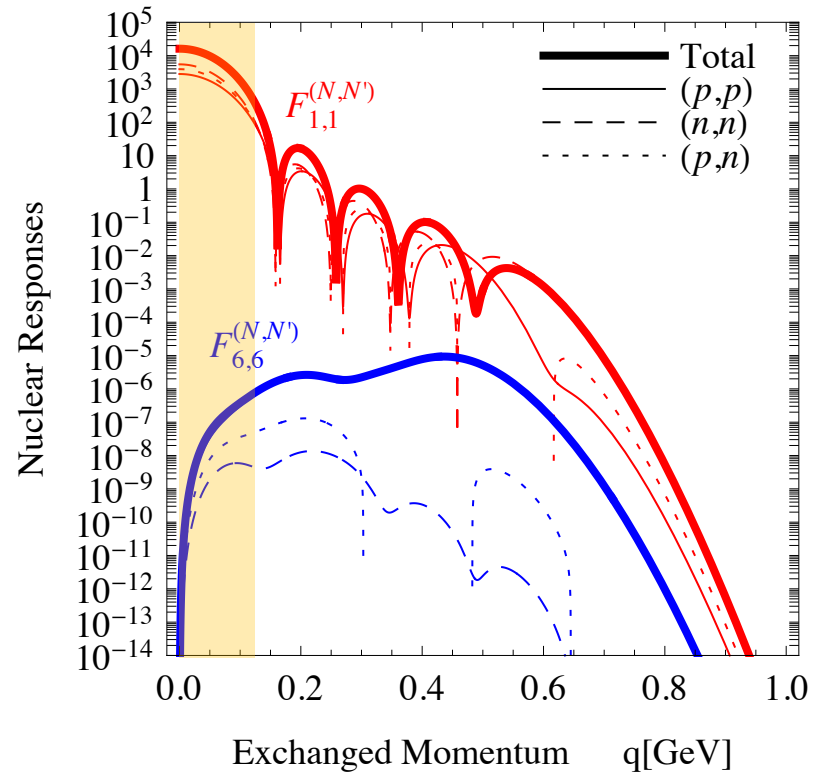
Fitzpatrick et al, JCAP 1302 (2013) 004

# Nuclear response functions

fluorine



iodine




(1,1):  $\mathcal{O}_1^{\text{NR}} = \mathbb{1}$

“Vanilla” coherent scattering  
 $A^2$  enhanced

(6,6):  $\mathcal{O}_6^{\text{NR}} = (\vec{s}_\chi \cdot \vec{q})(\vec{s}_n \cdot \vec{q})$  e.g., pseudo-scalar mediator scattering on p dominant (no unpaired n on F and I)

# Cross section

Cross section on nucleus  $\mathcal{N}$

$$\frac{d\sigma_{\mathcal{N}}}{dE_R}(v, E_R) = \frac{1}{32\pi} \frac{1}{m_{\chi}^2 m_{\mathcal{N}}} \frac{1}{v^2} |\mathcal{M}_{\mathcal{N}}|^2$$


Non-relativistic scattering on nucleons  $\rightarrow$  nucleus

Relevant quantities:

$\vec{v}$  DM velocity

$\vec{q}$  Exchanged momentum

$\vec{s}_n$  Nucleon spin

$\vec{s}_{\chi}$  DM spin

$m_{\chi}$  DM mass

$m_n$  nucleon mass

$m_{\mathcal{N}}$  nucleus mass

# Summarizing

$$\frac{dR_{\mathcal{N}}}{dE_R} = K \rho_{\odot} \xi_{\mathcal{N}} \sum_{i,j=1}^{16} \sum_{n,n'=p,n} c_i^n(\lambda, m_{\chi}) c_j^{n'}(\lambda, m_{\chi}) \mathcal{F}_{i,j}^{(n,n')}(E_R, \mathcal{N})$$

$$\mathcal{F}_{i,j}^{(n,n')}(E_R, \mathcal{N}) = \int_{v_{\min}(E_R)}^{v_{\text{esc}}} d^3v \frac{1}{v} f_G(\vec{v} + \vec{v}_E(t)) F_{i,j}^{(n,n')}(v, E_R, \mathcal{N})$$

Structure of the interaction

Nuclear response

Galactic modeling

Local motions

Sun/Earth revolution in the Galaxy

Earth revolution around the Sun

Earth rotation around its axis

stationary boost

annual periodicity

diurnal periodicity

# Interaction rate (WIMP ; scalar interaction)

$$\hat{O}_1 = \mathbb{1}_{\chi N}$$

$$\frac{dR}{dE_R} = N_T \frac{\rho_0}{m_\chi} \frac{m_N}{2\mu_1^2} A^2 \left[ \sigma_{\text{scalar}}^{(\text{nucleon})} \right] F^2(E_R) \mathcal{I}(v_{\min})$$

$$\mathcal{I}(v_{\min}) = \int_{w \geq v_{\min}} d^3w \frac{f_{\text{ES}}(\vec{w})}{w}$$

$$f_{\text{ES}}(\vec{w}) = f(\vec{w} + \vec{v}_\oplus) |_{[v_{\text{rot}}; v_{\text{esc}}]}$$

$$v_{\min} = [m_N E_R / (2\mu_A^2)]^{1/2}$$



# Interaction rates

Spin-independent (scalar)  $\hat{O}_1 = \mathbb{1}_{\chi N}$

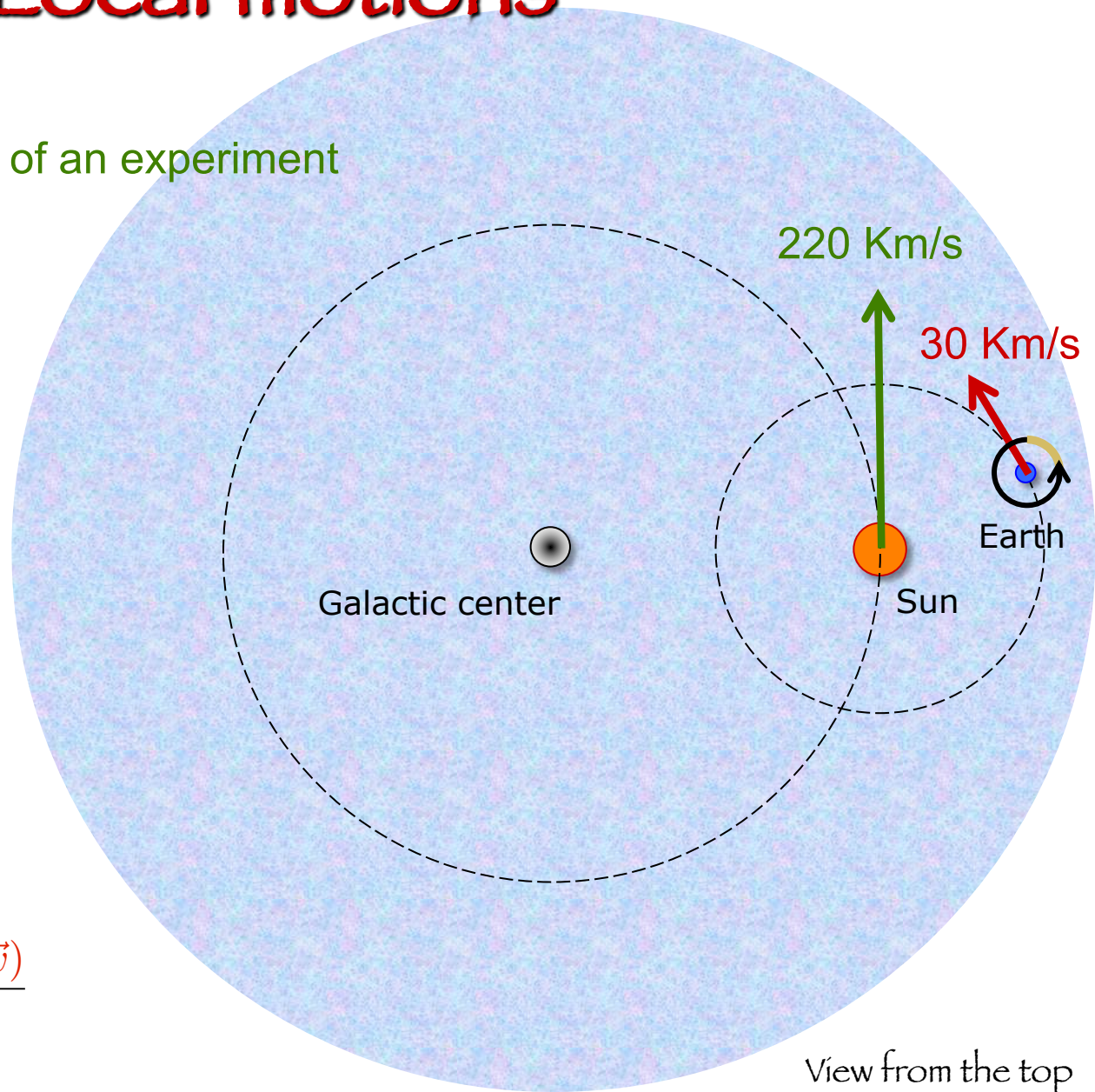
$$\frac{dR}{dE_R} = N_T \frac{\rho_0}{m_\chi} \frac{m_N}{2\mu_1^2} A^2 \left[ \sigma_{\text{scalar}}^{(\text{nucleon})} \right] F^2(E_R) \mathcal{I}(v_{\text{min}})$$

Spin-dependent  $\hat{O}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N$

$$\frac{dR}{dE_R} = N_T \frac{\rho_0}{m_\chi} \frac{2m_N}{\mu_1^2} \lambda J(J+1) \left[ \sigma_{\text{spin}}^{(\text{nucleon})} \right] F^2(E_R) \mathcal{I}(v_{\text{min}})$$

# Local motions

Stationary over the lifetime of an experiment  
Directional boost

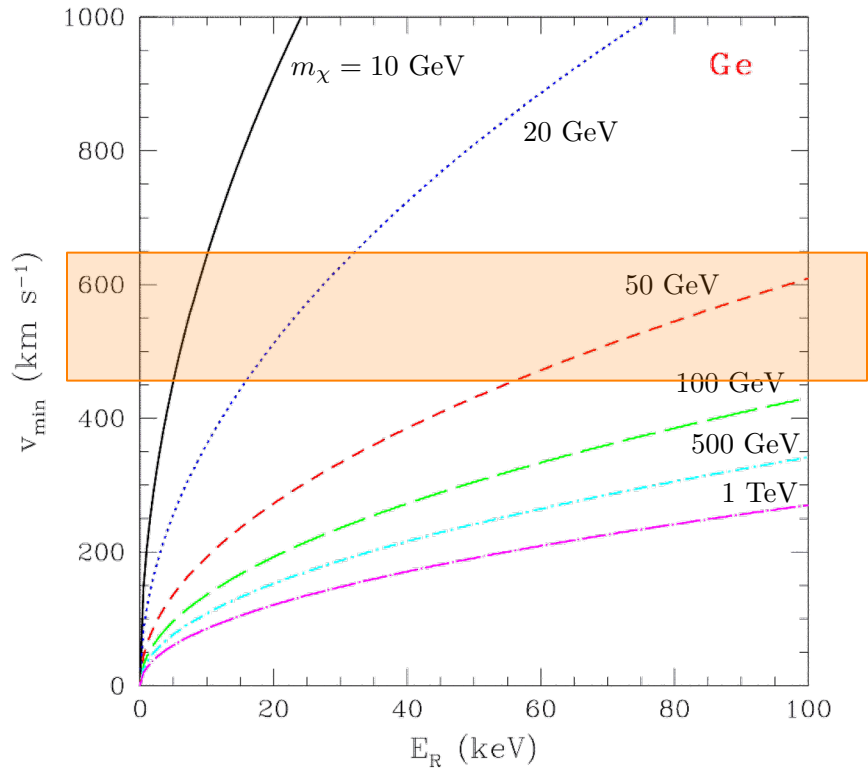


View from the top

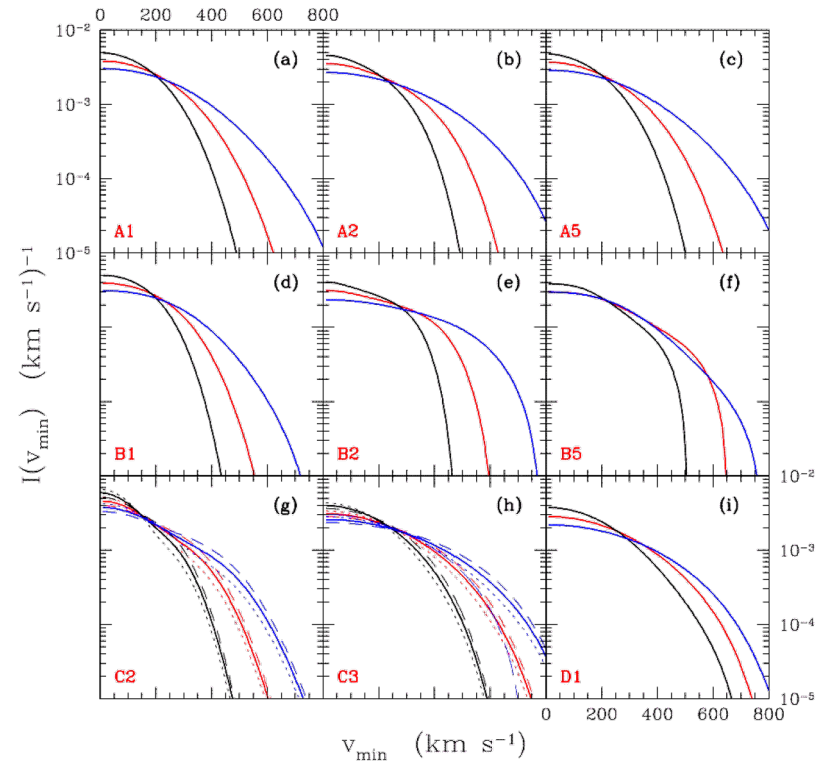
$$\mathcal{I}(v_{\min}) = \int_{w \geq v_{\min}} d^3 w \frac{f_{\text{ES}}(\vec{w})}{w}$$

$$f_{\text{ES}}(\vec{w}) = f(\vec{w} + \vec{v}_{\oplus})|_{[v_{\text{rot}}; v_{\text{esc}}]}$$

# Response function

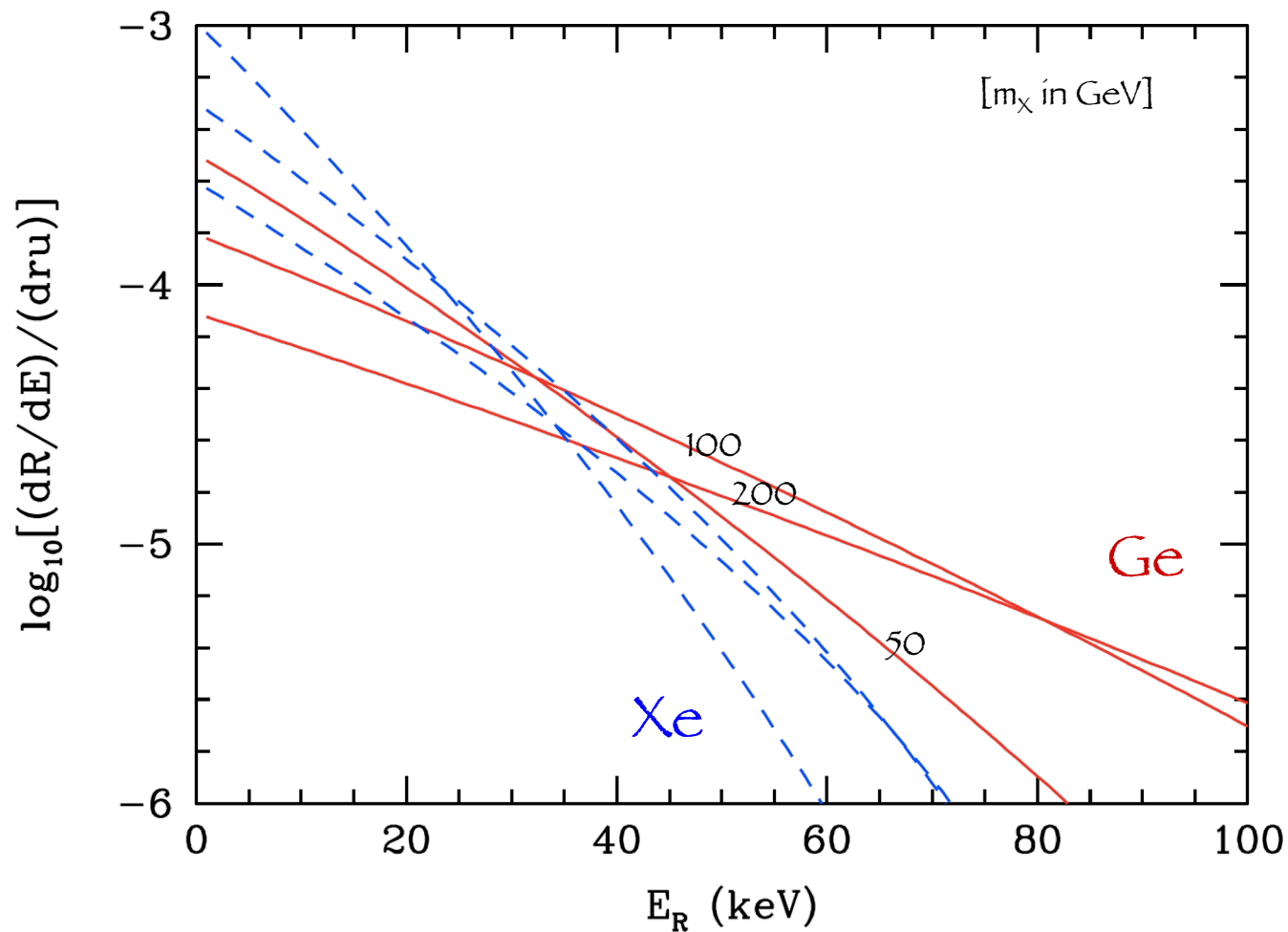


$$v_{\min} = [m_N E_R / (2\mu_A^2)]^{1/2}$$



$$I(v_{\min}) = \int_{w \geq v_{\min}} d^3 w \frac{f_{\text{ES}}(\vec{w})}{w}$$

# Differential Rate ~ Energy Dependence

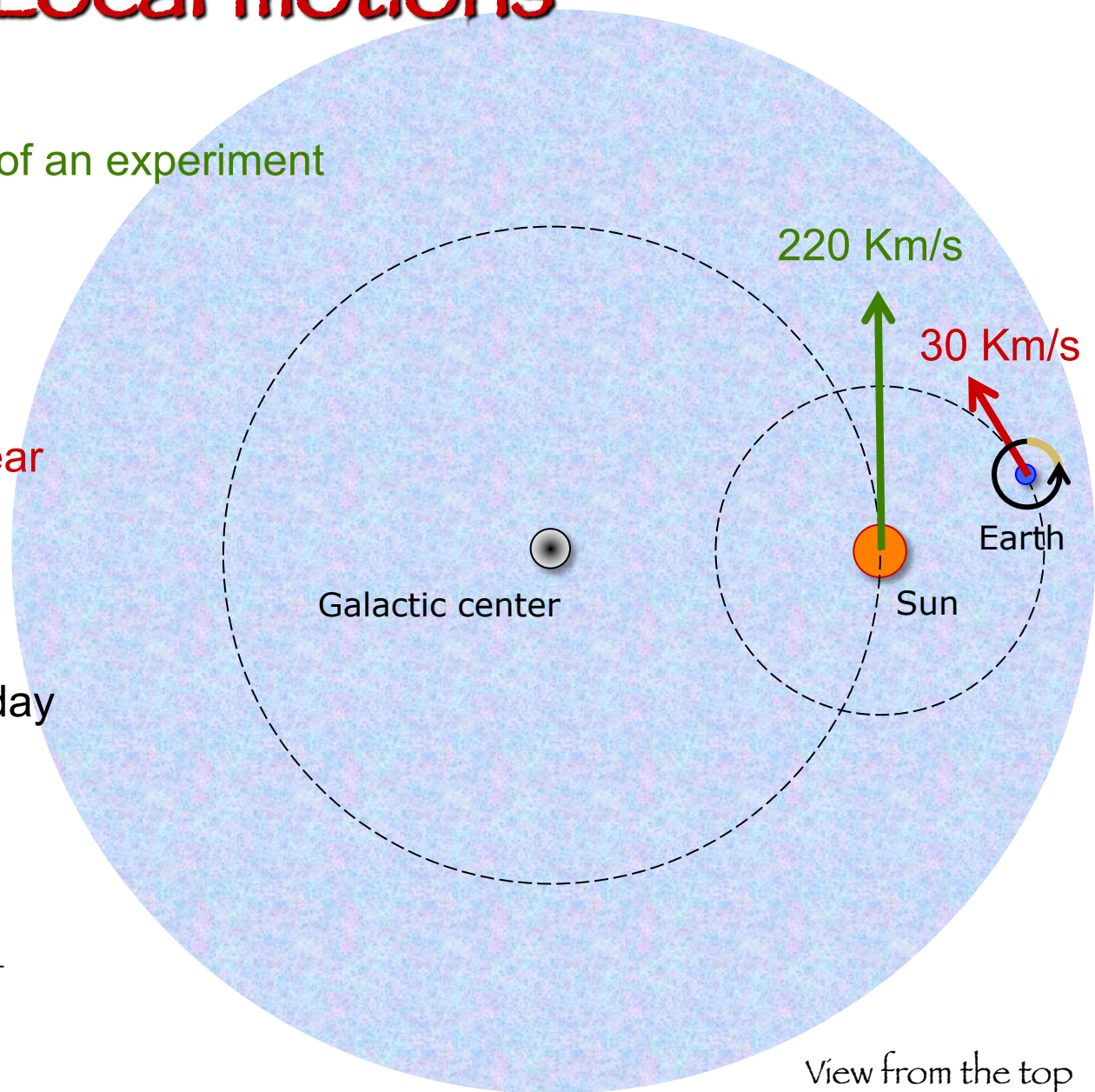


# Local motions

Stationary over the lifetime of an experiment  
Directional boost

Orbital motion - Period: 1 year

Diurnal rotation - Period: 1 day



$$\mathcal{I}(v_{\min}) = \int_{w \geq v_{\min}} d^3w \frac{f_{\text{ES}}(\vec{w})}{w}$$

$$f_{\text{ES}}(\vec{w}) = f(\vec{w} + \vec{v}_{\oplus})|_{[v_{\text{rot}}; v_{\text{esc}}]}$$

# Typical signatures of direct detection

Stationary over the lifetime of an experiment

Directional boost

*Directionality*

$$\vec{v}$$

Orbital motion - Period: 1 year

*Annual modulation*

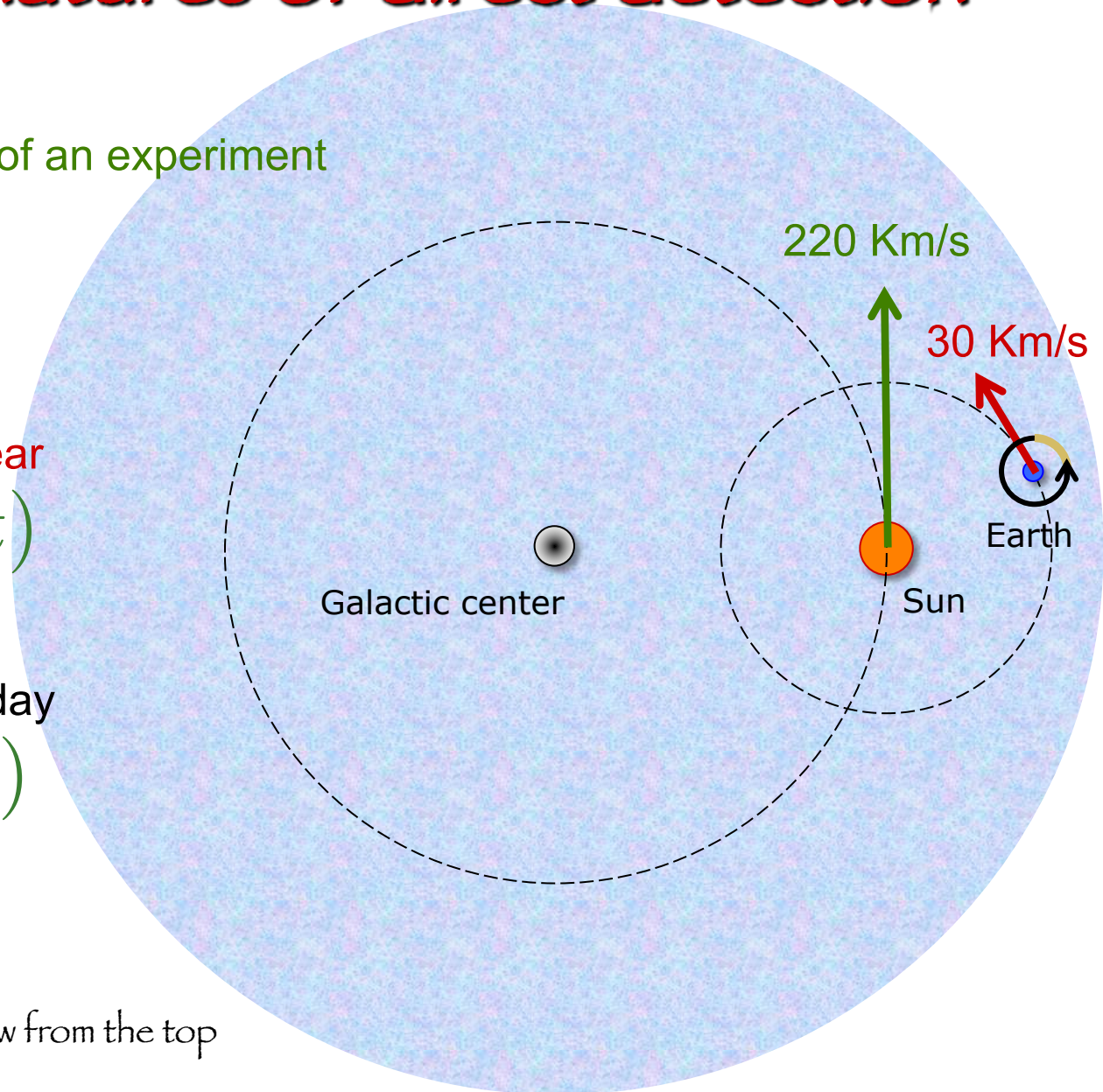
$$\vec{v}(t)$$

Diurnal rotation - Period: 1 day

*Diurnal modulation*

$$\vec{v}(t)$$

View from the top

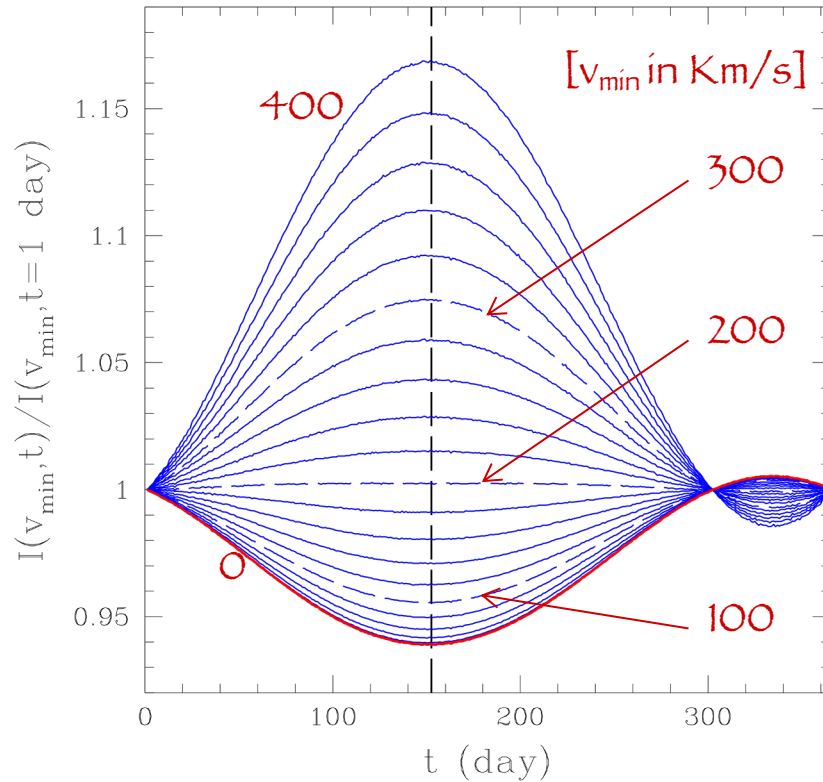


# Annual Modulation of the rate

$$\begin{aligned}\frac{dR}{dE_R}[\eta(t)] &= \frac{dR}{dE_R}[\eta_0] + \frac{\partial}{\partial \eta} \left( \frac{dR}{dE_R} \right)_{\eta=\eta_0} \Delta\eta \cos[\omega(t - t_0)] \\ &= S_0(E_R) + S_m(E_R) \cos[\omega(t - t_0)]\end{aligned}$$

$$\eta(t) = v(t)/v_0$$

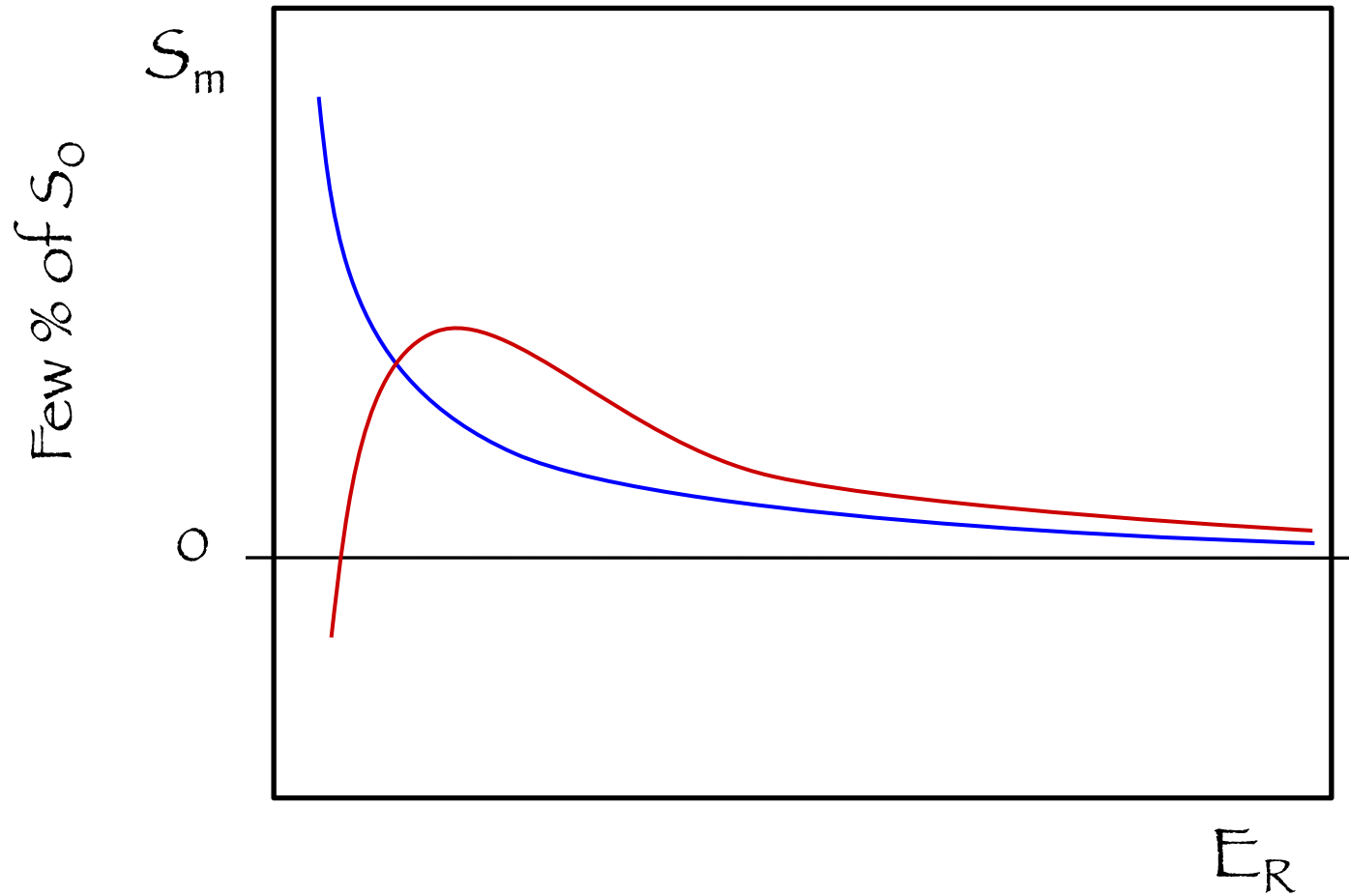
# Annual modulation



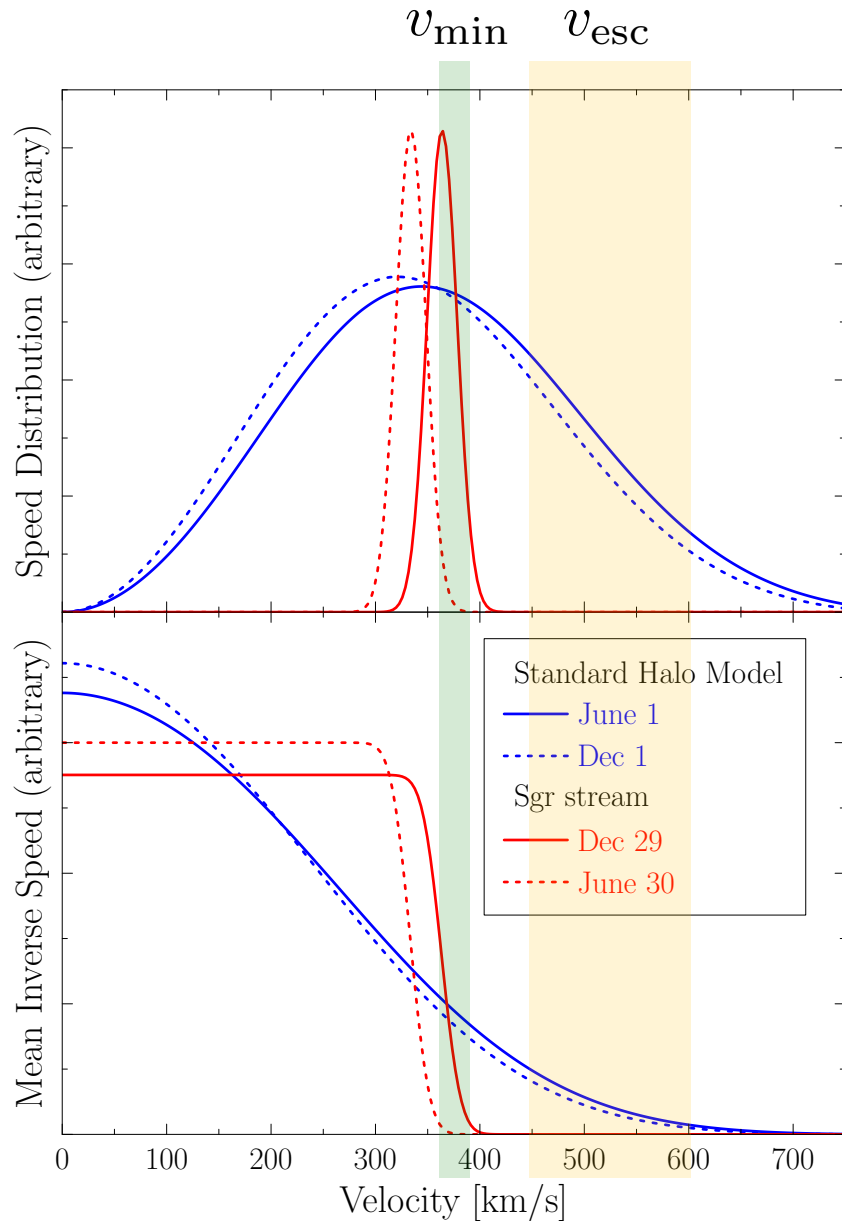
$f(v)$ : isotropic maxwellian



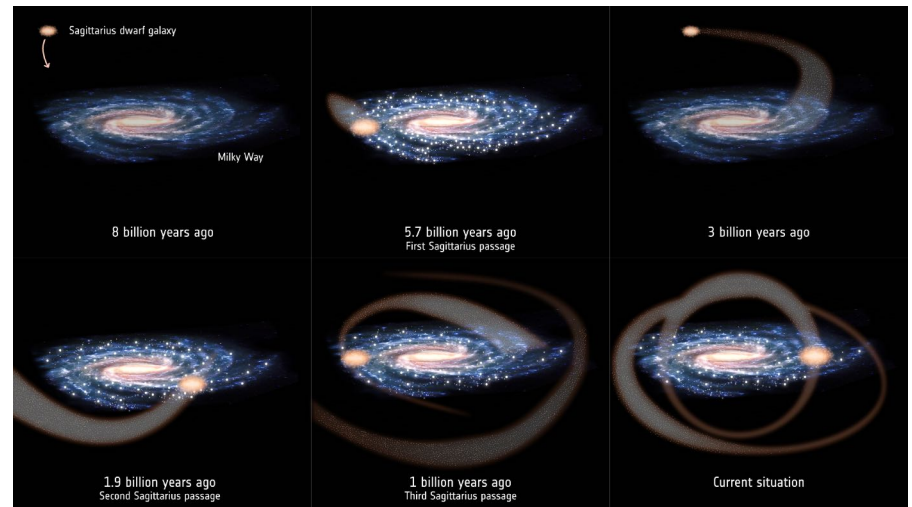
# Modulation amplitude - energy dependence



# DM velocity distribution: streams?



## Sagittarius stream

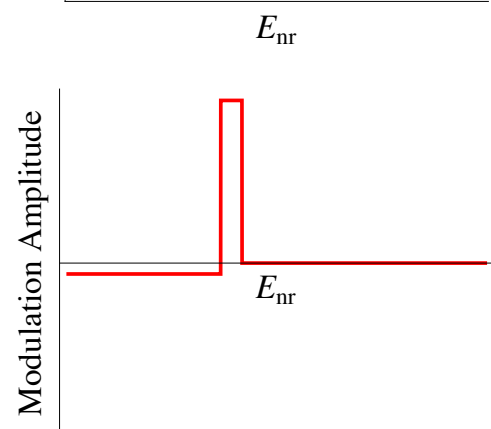
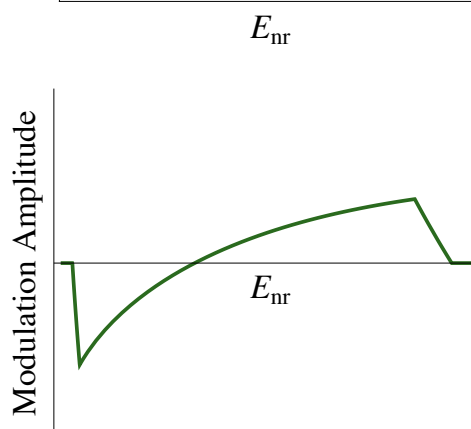
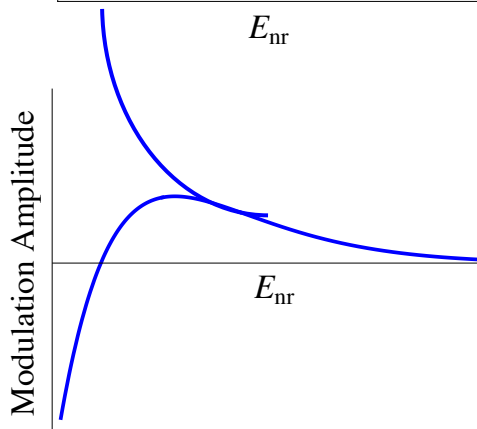
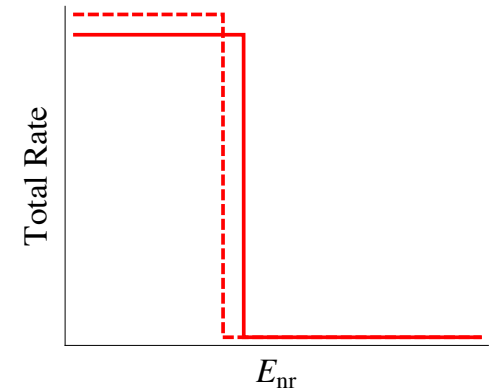
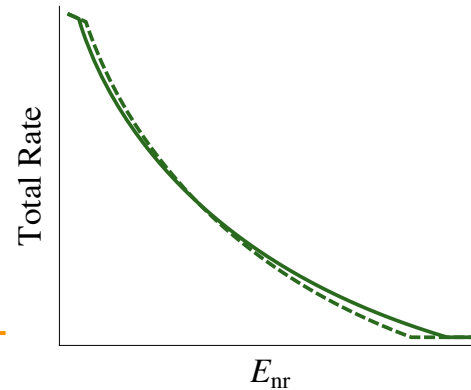
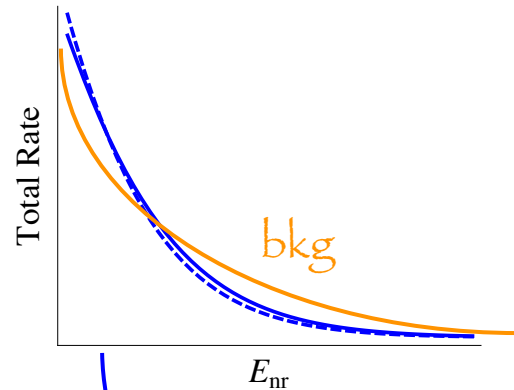


# DM velocity distribution

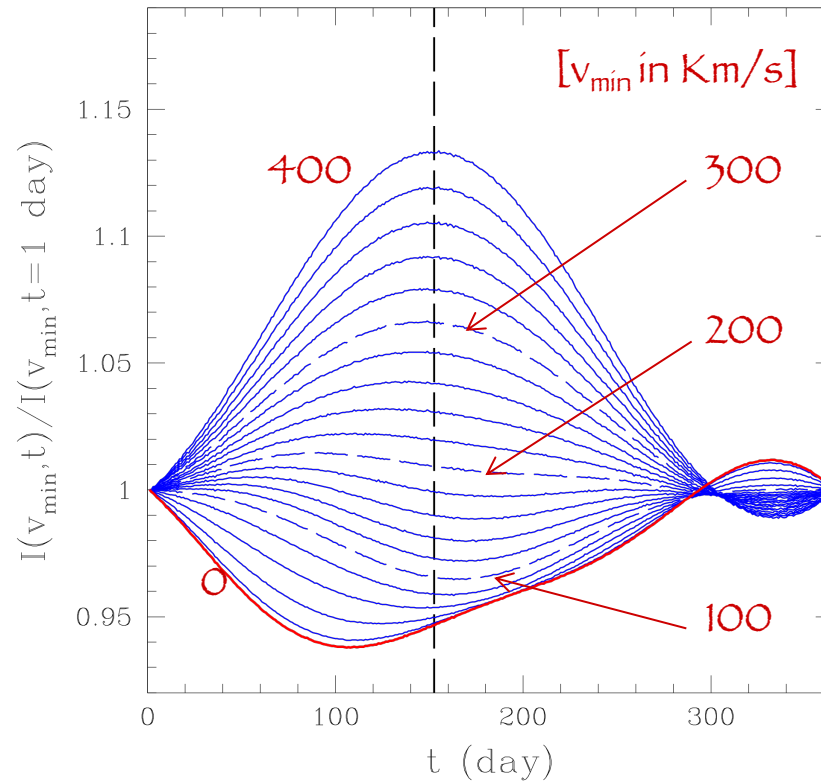
SHM

Debris Flow

Stream



# Annual modulation: effect of anisotropies



$f(v)$ : anisotropic maxwellian

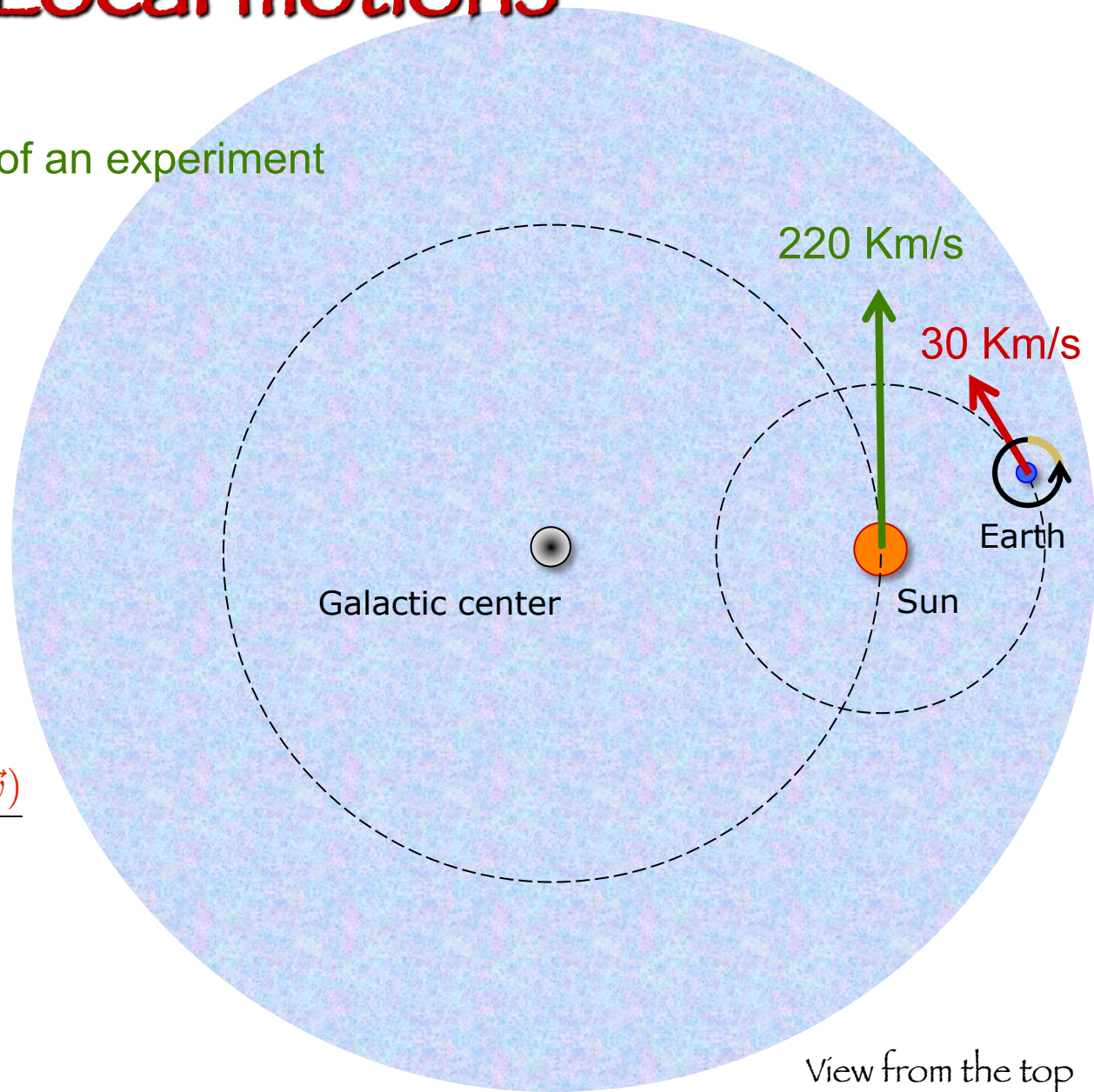
# Local motions

Stationary over the lifetime of an experiment

Directional boost

*Directionality*

$\vec{v}$

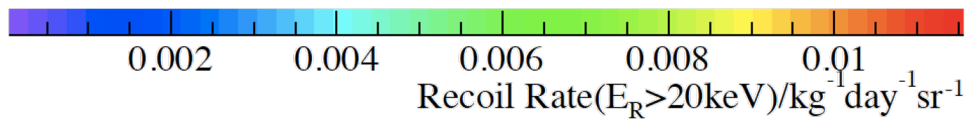
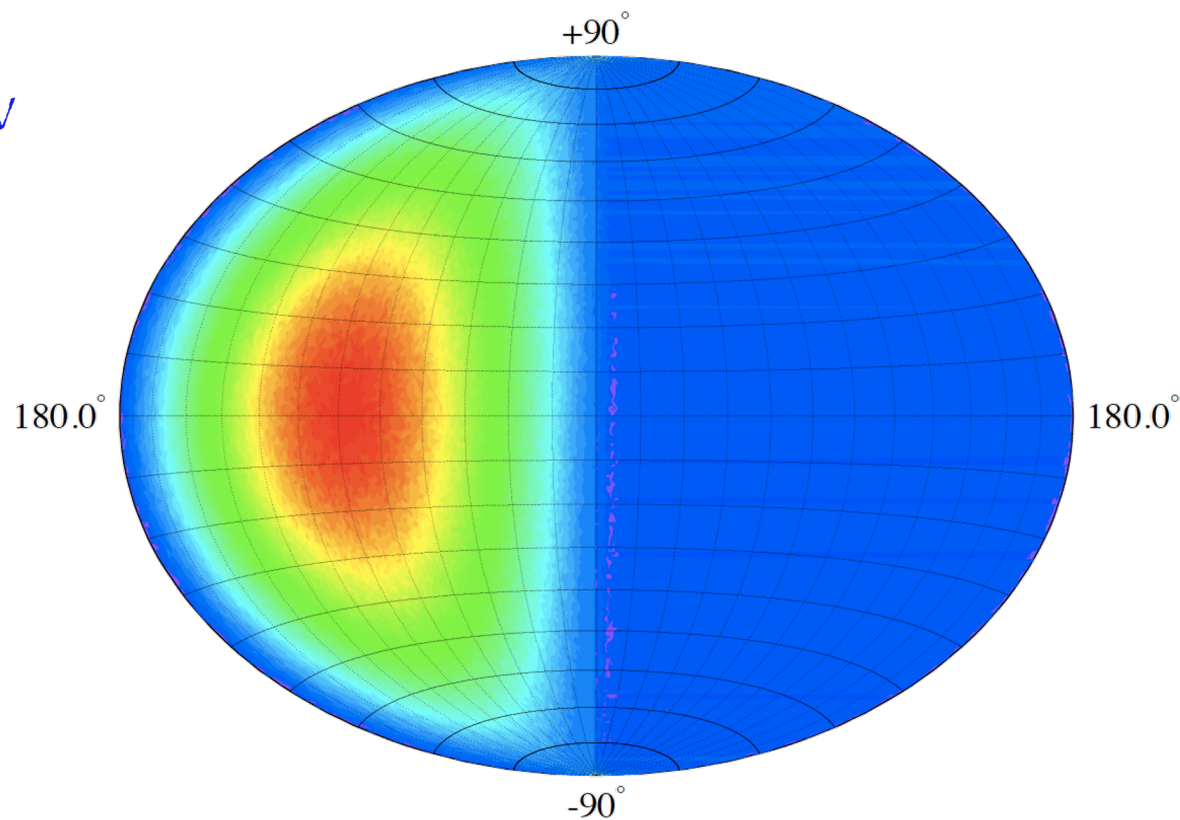


$$\mathcal{I}(v_{\min}) = \int_{w \geq v_{\min}} d^3w \frac{f_{\text{ES}}(\vec{w})}{w}$$

$$f_{\text{ES}}(\vec{w}) = f(\vec{w} + \vec{v}_{\oplus})|_{[v_{\text{rot}}; v_{\text{esc}}]}$$

# Directionality of the recoil

$m_\chi = 100 \text{ GeV}$



# DM particle features extraction

$$\frac{dR}{dE_R} = N_T \frac{\rho_0}{m_\chi} \frac{m_N}{2\mu_1^2} A^2 \left[ \sigma_{\text{scalar}}^{(\text{nucleon})} \right] F^2(E_R) \mathcal{I}(v_{\min})$$



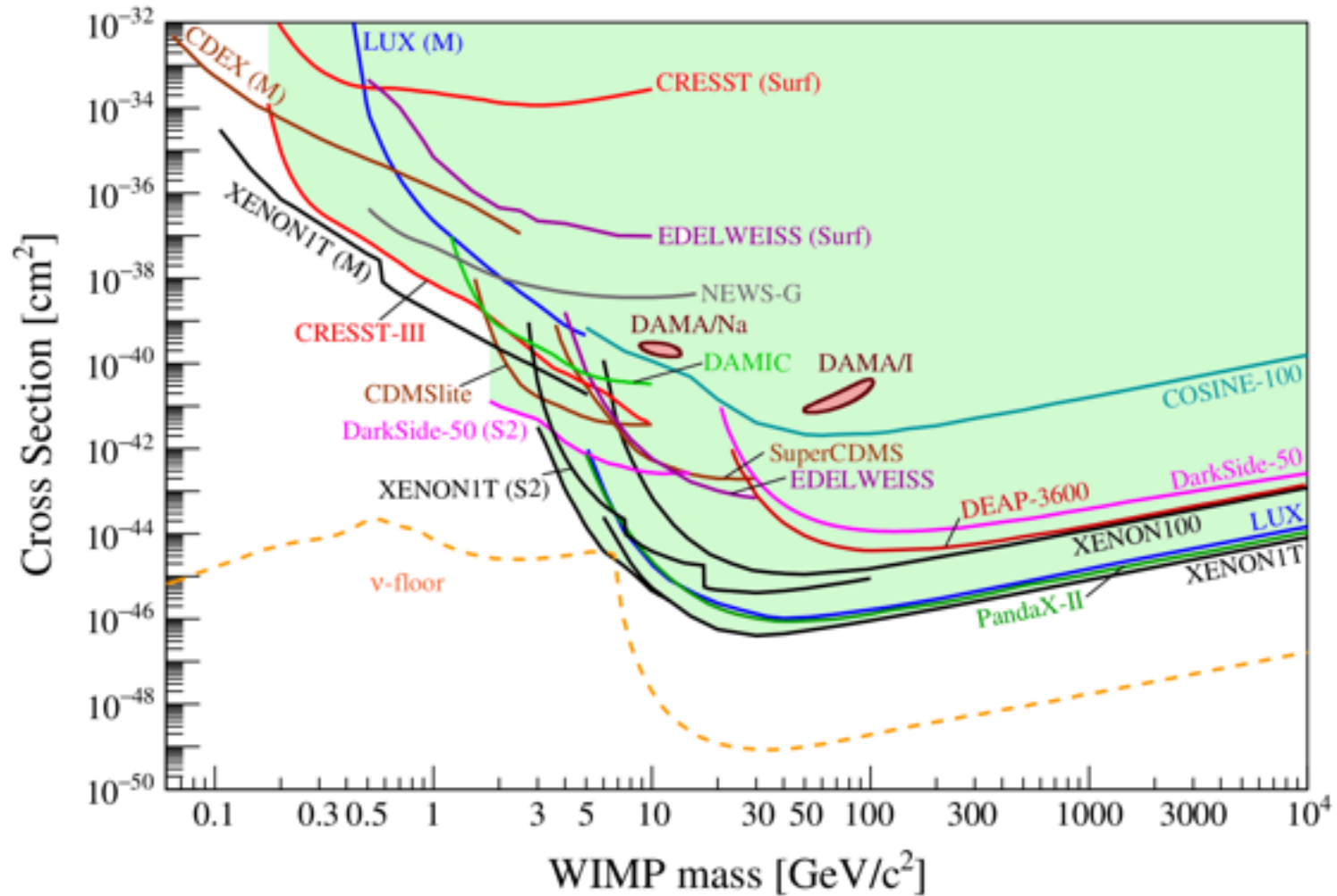
$$\mathcal{I}(v_{\min}) = \int_{w \geq v_{\min}} d^3w \frac{f_{\text{ES}}(\vec{w})}{w}$$

$$f_{\text{ES}}(\vec{w}) = f(\vec{w} + \vec{v}_\oplus) |_{[v_{\text{rot}}; v_{\text{esc}}]}$$

$$v_{\min} = [m_N E_R / (2\mu_A^2)]^{1/2}$$

$$E_R \rightarrow E_{\text{det}}$$
$$E_{\text{ee}} = q(E) E_R$$

# Current status (Spin-independent = $O_1$ operator)



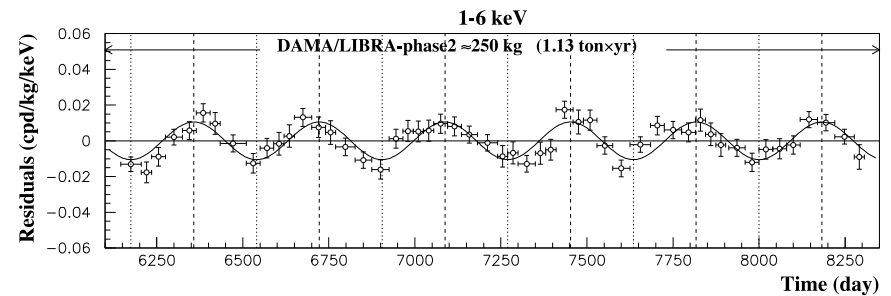
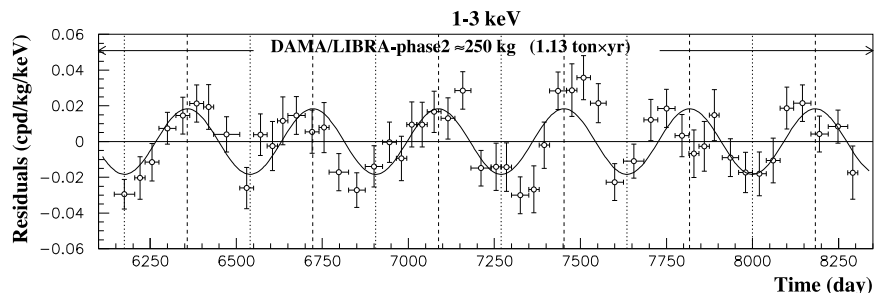
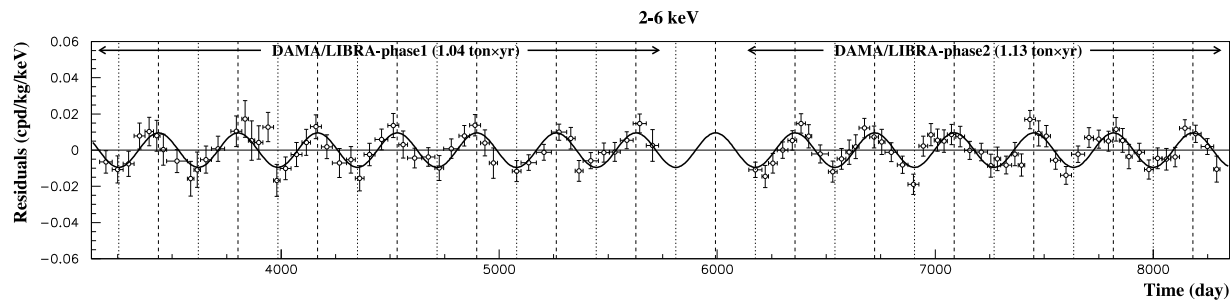
APPEC Committee Report, arXiv:2104.07634



# DAMA/Libra

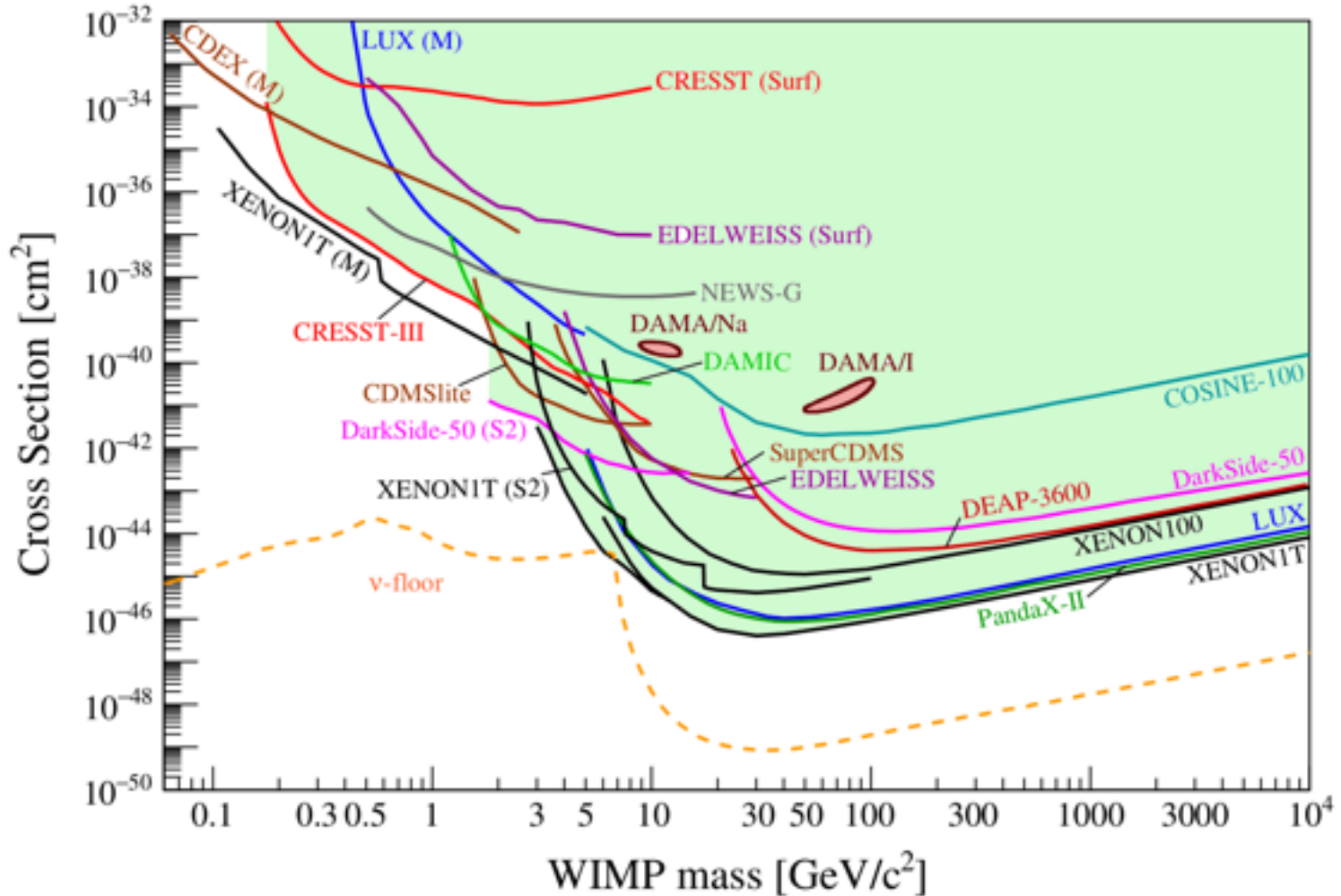
The data of DAMA/LIBRA phase1+phase2 favor the presence of a modulation with proper features at 12.9s CL (2.46 ton × yr)

$$S_m = (0.0103 \pm 0.0008) \text{ cpd/kg/keV}$$



# Current status (Spin-independent = $O_1$ operator)

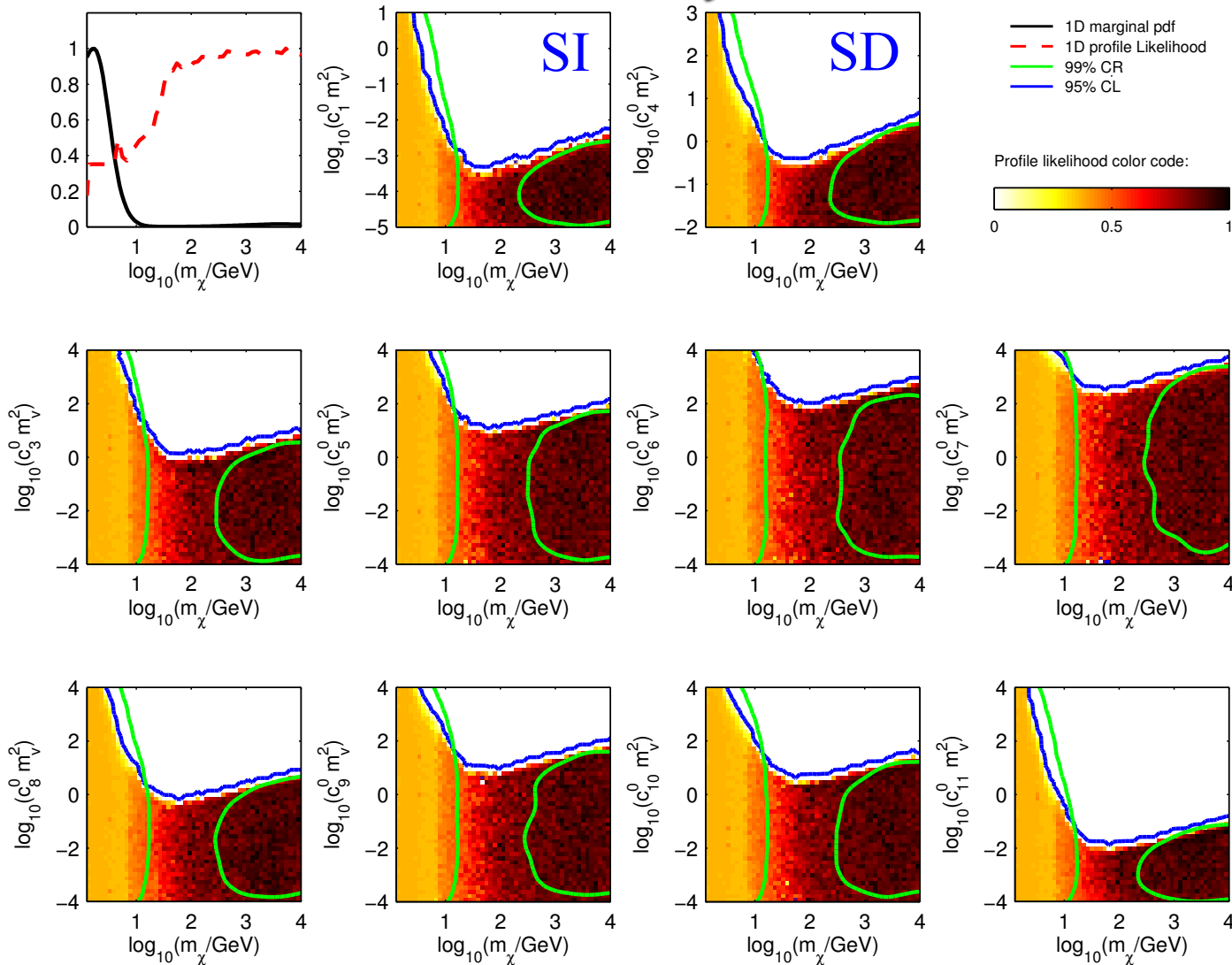
$$\frac{dR}{dE_R} = N_T \frac{\rho_0}{m_\chi} \frac{m_N}{2\mu_1^2} A^2 \left[ \sigma_{\text{scalar}}^{(\text{nucleon})} \right] F^2(E_R) \mathcal{I}(v_{\text{min}})$$



# Full set of operators

Catena, Gondolo, JCAP 09 (2014) 045

See also: Scheck et al (SuperCDMS), PRD 91 (2015) 092004



Combined analysis of  
CDMS, XENON, LUX, COUPP, PICASSO, SIMPLE

# Light WIMPs - Migdal effect

When the nucleus recoils, electrons do not 'rigidly' follow, but can have transition to a different energy level or to the continuum, resulting in:

excitation

ionization

with e.m. released in addition to the recoil signal

Transition to the continuum: emission of radiation

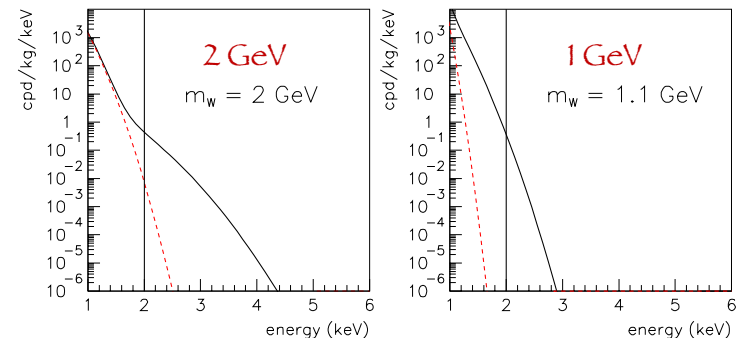
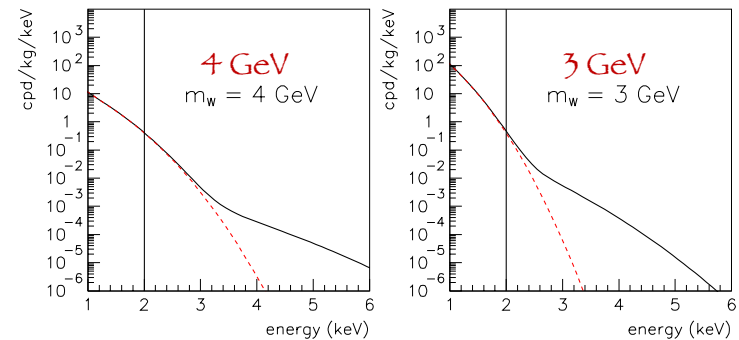
Rearrangement of atomic shells

Emission of radiation

Meitner-Auger electrons<sup>(\*)</sup>

Relevant especially for light WIMPs

(\*) Filling the inner shell vacancy, energy is transferred to another electron which is then emitted



# Very light DM

- Very light DM (down to the warm regime):
  - Available kinetic energy can be as low as meV (for KeV DM)
  - Too low deposited energy on nuclear target
- Possibilities:
  - Nuclear interactions on light targets, e.g. liquid He
  - Electron recoils

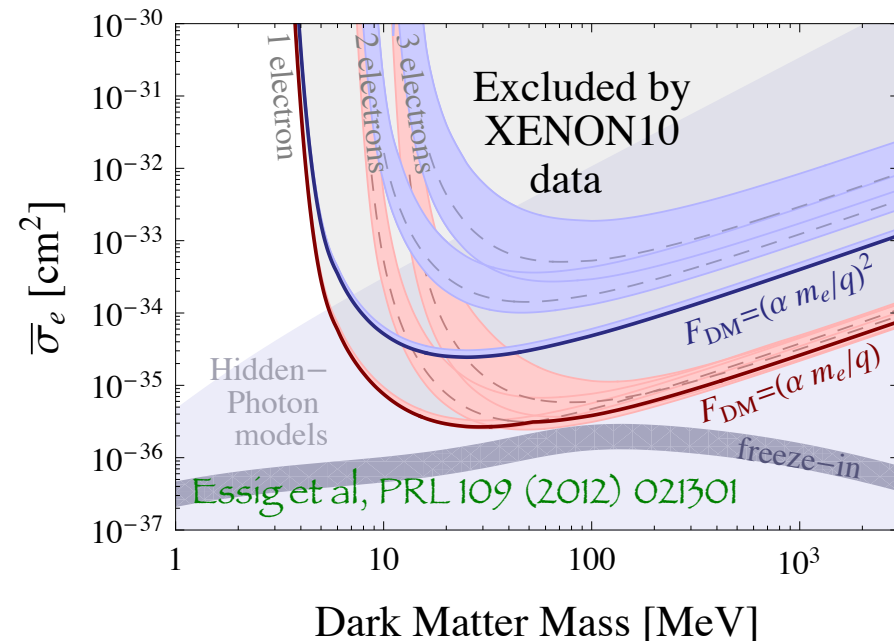
Essig et al, PRD 85 (2012) 076007

Essig et al, 1509.01598

Agnese et al (SuperCDMS) PRL 112 (2014) 041302

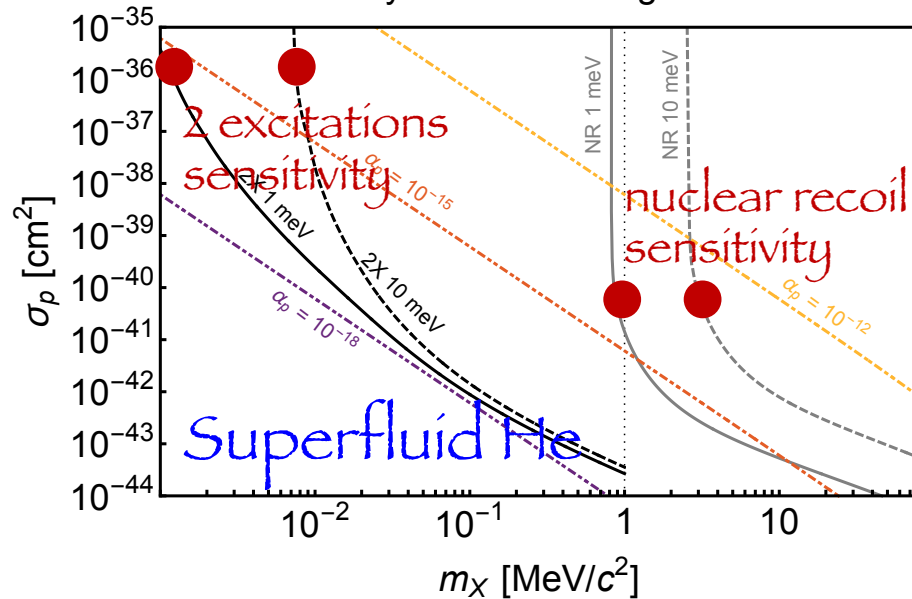
Essig et al, PRL 109 (2012) 021301

Guo, McKinsey, PRD 87 (2013) 115001

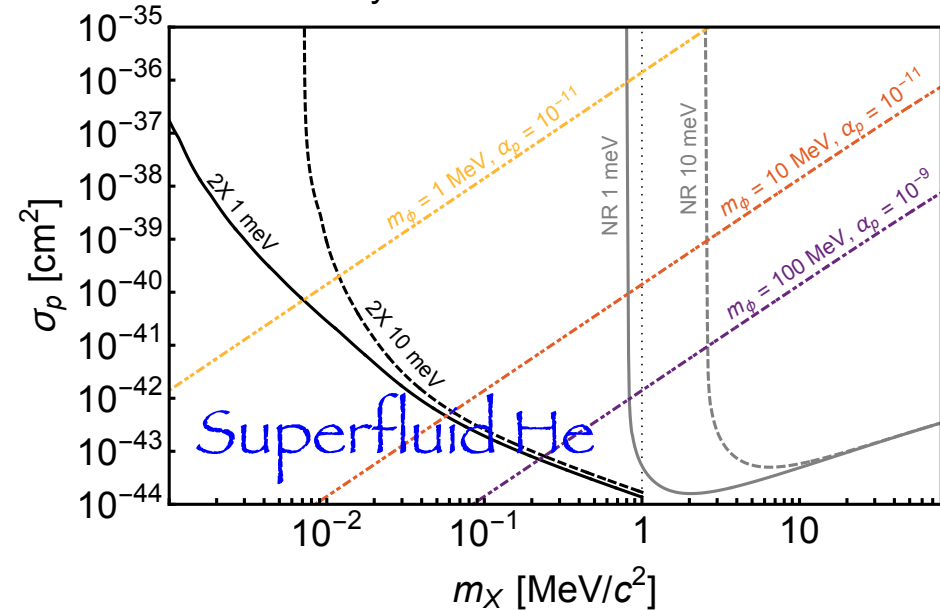


# Super light DM

Sensitivity to DM via a Light Mediator



Sensitivity to DM via a Massive Mediator



To go below 10 MeV DM: conversion of the full tiny energy needed

» Superconductors

Hochberg et al, 1512.04533

Hochberg et al, PRL 116 (2016) 011301

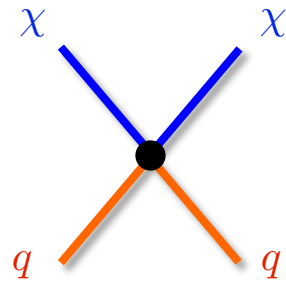
electron interactions

» Superfluid He

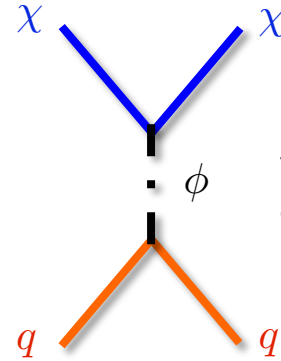
Schutz, Zurek, 1604.08206

nuclear interactions

# Other type of interactions: e.g. long range



contact



long-range

very light mediator  
e.g. dark photon or mirror photon

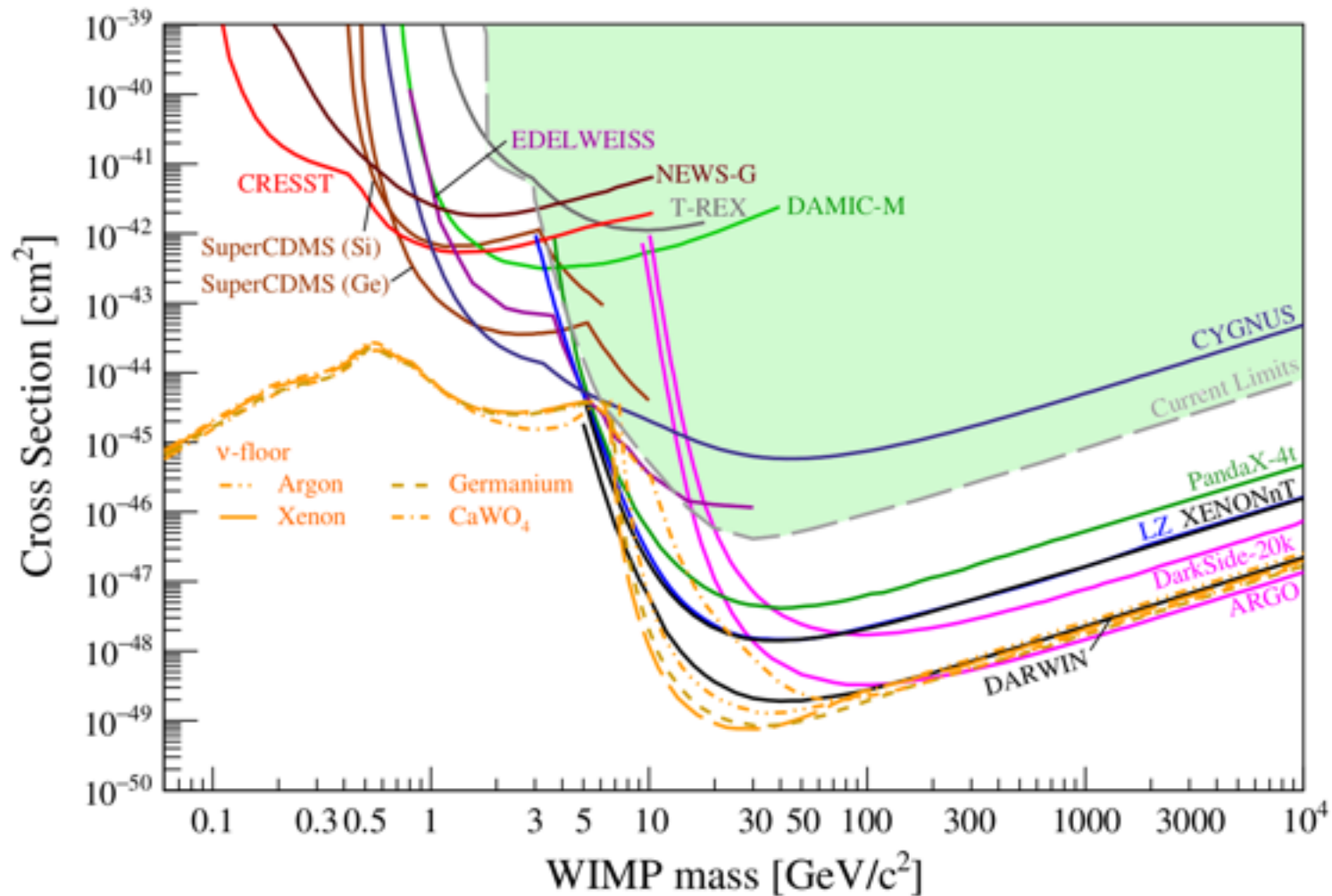
$$\frac{d\sigma(v, E_R)}{dq^2} = \frac{2m_N \lambda}{(q^2 + m_\phi^2)^2} \frac{1}{v^2} F^2(E_R)$$

$q^2 = 2m_N E_R$  momentum transfer  
 $m_\phi$  mass of the mediator

$$\frac{d\sigma(v, E_R)}{dE_R} = \frac{m_N}{2\mu_{\chi p}^2} \frac{1}{v^2} Z^2 \sigma_{\phi\gamma} F^2(E_R) \quad m_\phi^2 \gg q^2$$

$$\frac{d\sigma(v, E_R)}{dE_R} = \frac{\lambda}{E_R^2} \frac{1}{v^2} F^2(E_R) \propto E_R^{-2} \quad m_\phi^2 \ll q^2$$

# Prospects: Projected Sensitivities





# Prospects

- Annual modulation: ANAIS  
KIMS + DM Ice = COSINE 100  
SABRE
- Diurnal modulation: DAMA with larger mass might access it
- Directionality:
  - Nuclear emulsion (NEWS)
  - Gas TPC (CYGNO)
  - Negative Ion Time Expansion Chamber
  - Carbon nanotubes, grafene
  - Anysotropic crystals (ADAMO)
  - DRIFT
  - MIMAC, DMTPC, NEWAGE, D3, ...

# NEUTRINO SIGNAL

# Neutrino signals from DM

- Neutrino flux produced by DM annihilation (or decay) *inside the Sun/Earth*, where DM may be gravitationally captured
  - Because of capture, the flux may have a detectable size
  - Directionality (point source)
- Diffuse emission from DM annihilation (or decay) *in the galactic halo*
  - Size of signal is low (target for next-generation neutrino telescopes)
  - Possible correlation with diffuse galactic gamma rays

# Neutrinos from Earth and Sun

- Capture:

- Galactic DM particles that cross the Earth and the Sun, can interact with the nuclei in these bodies and lose enough energy to remain gravitationally captured

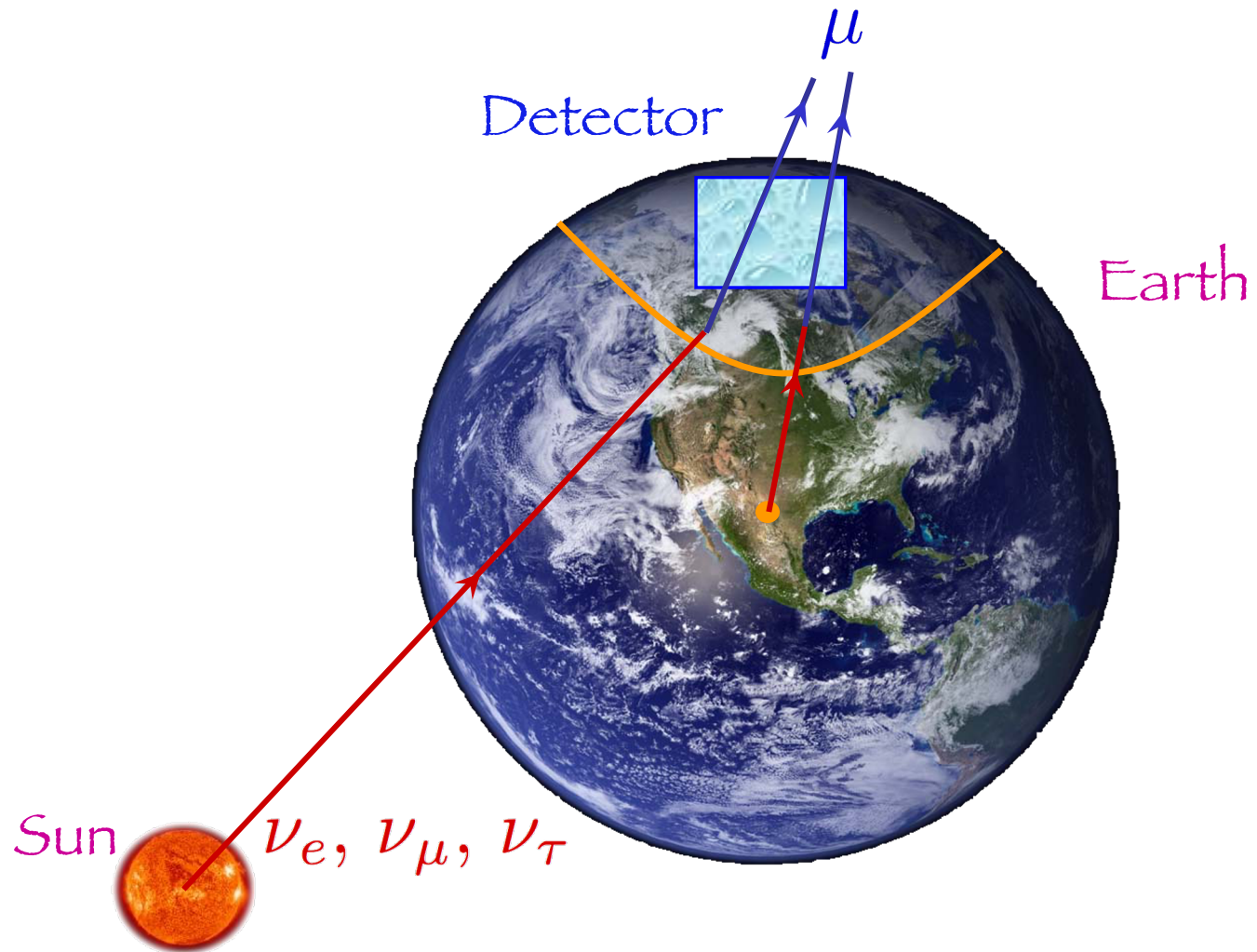
- Accumulation:

- After subsequent interactions they tend to drop into the innermost parts of the Earth and the Sun, where they accumulate

- Annihilation:

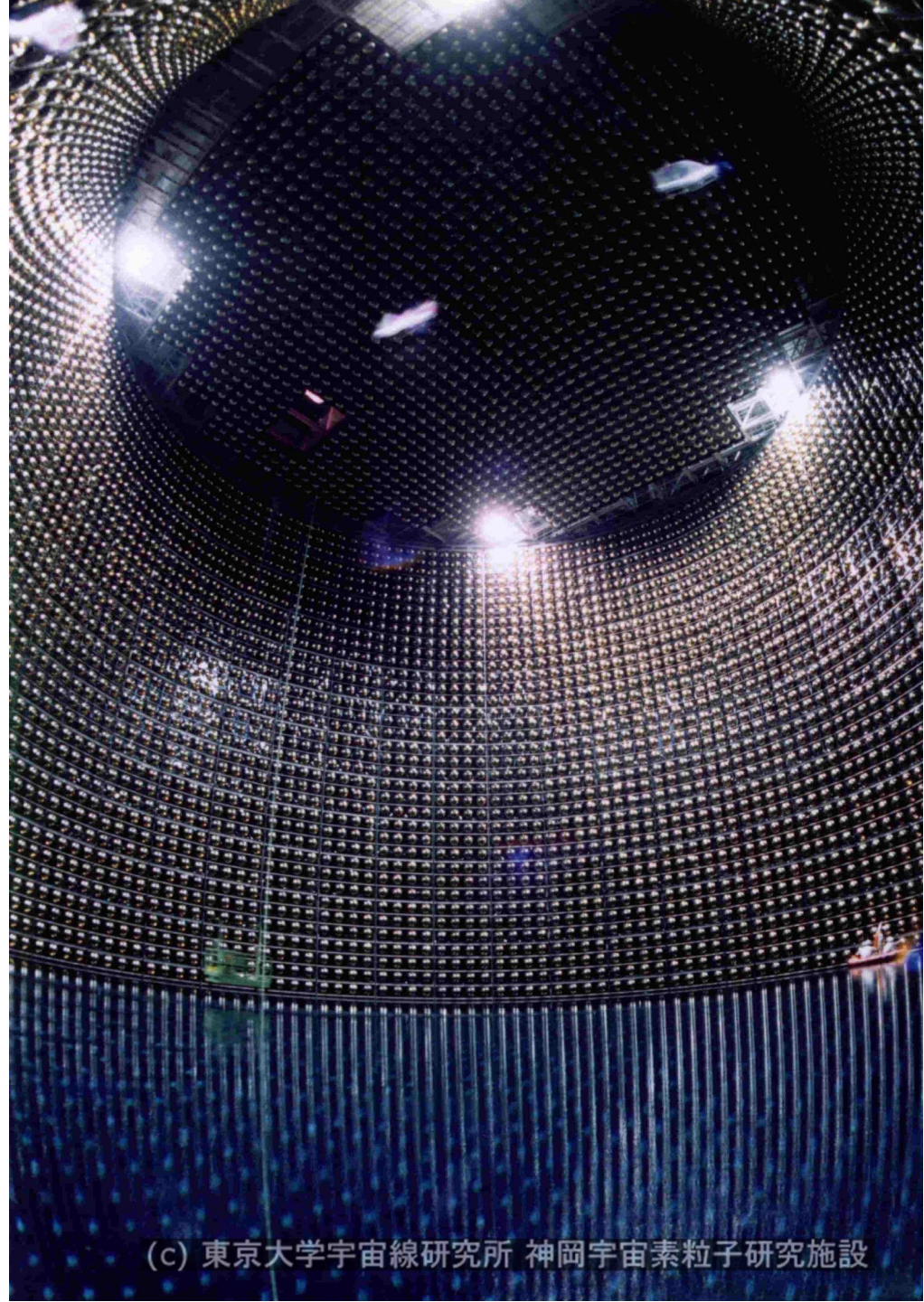
- When the energy density in the inner parts of the Earth and the Sun increases enough, they may start to annihilate

neutrino flux



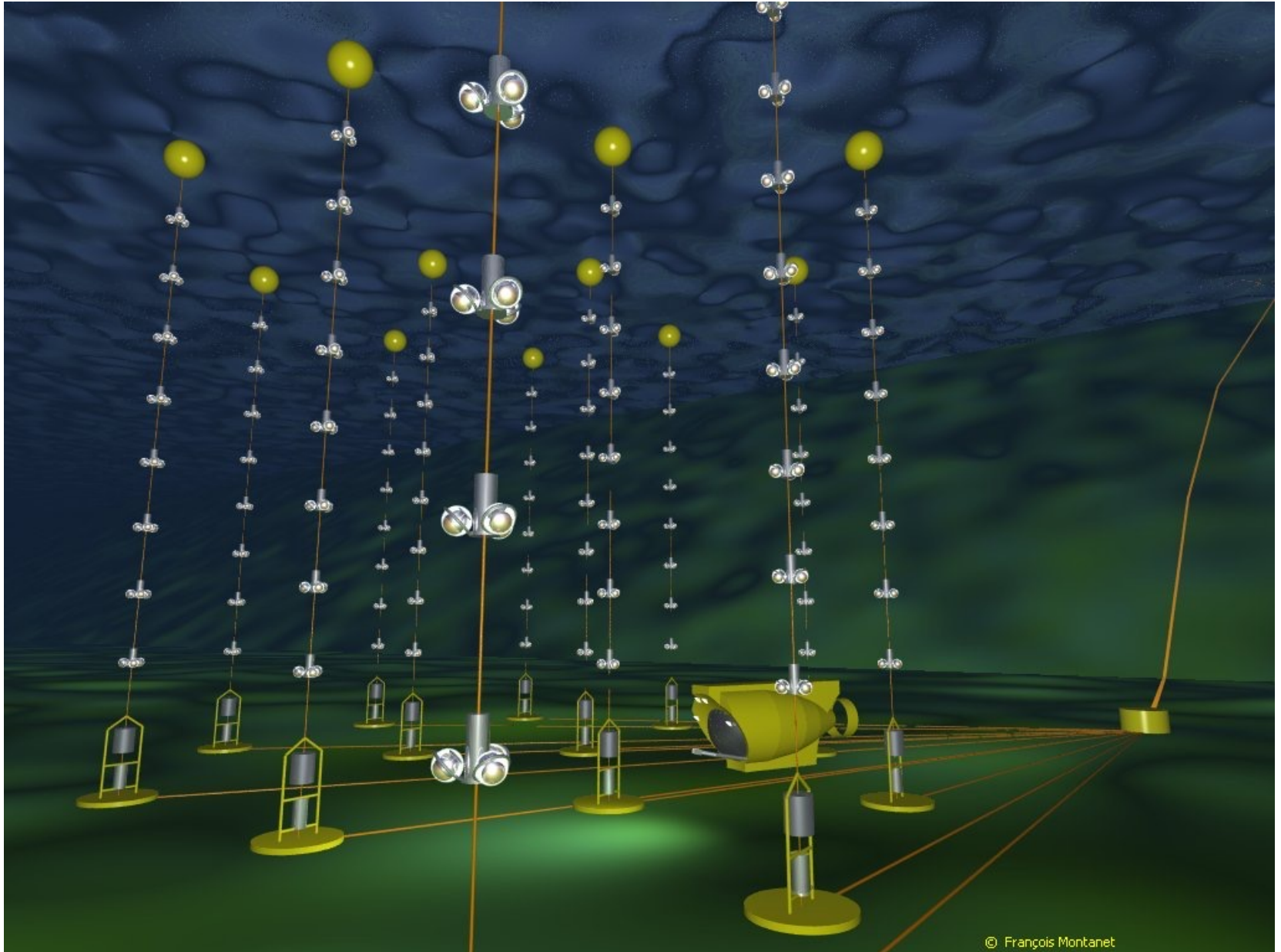


# Super Kamiokande

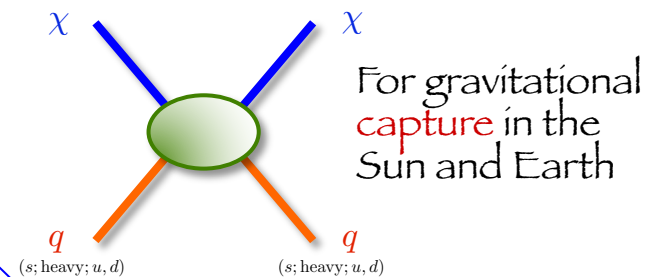
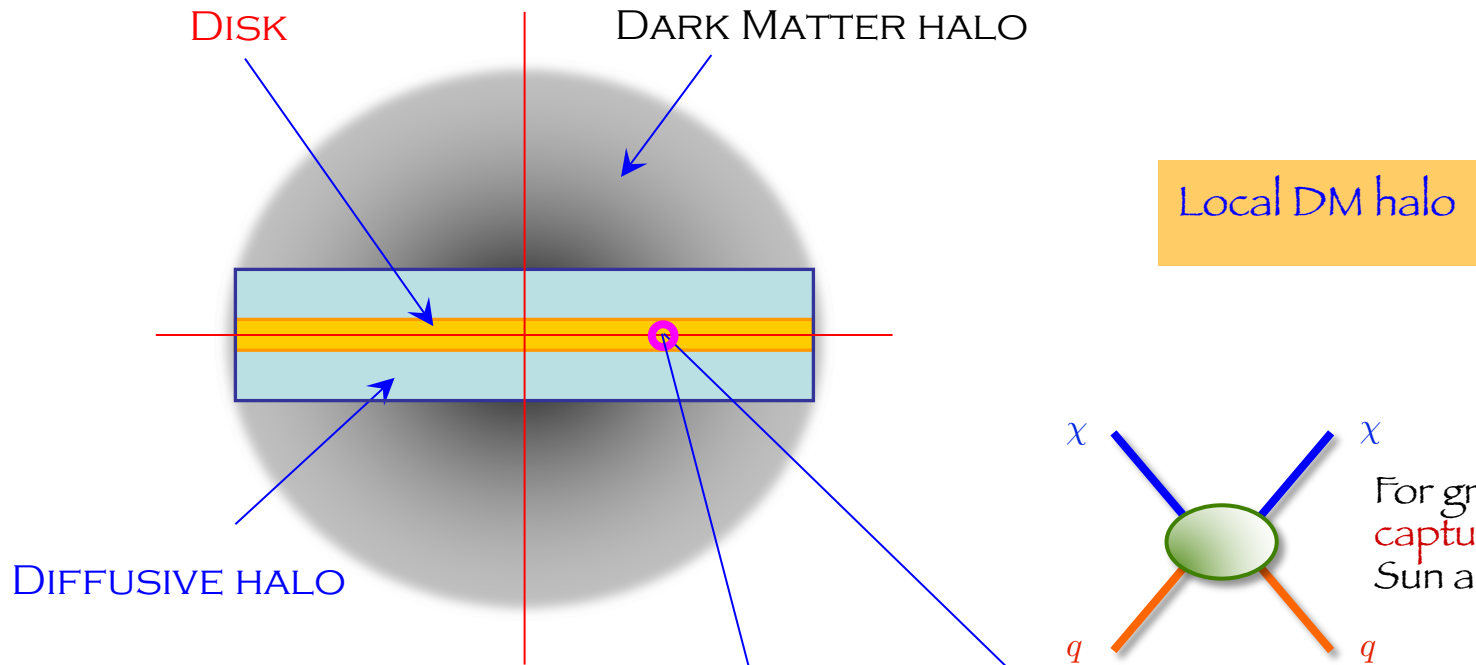


(c) 東京大学宇宙線研究所 神岡宇宙素粒子研究施設

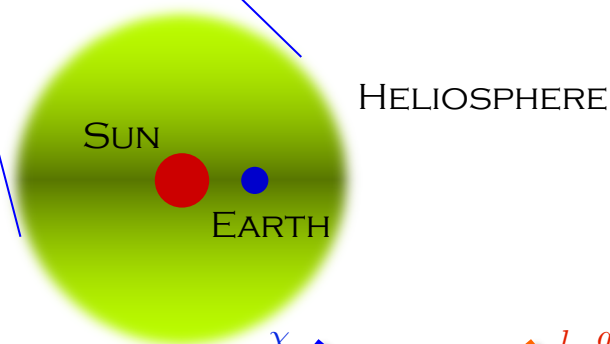
# ANTARES



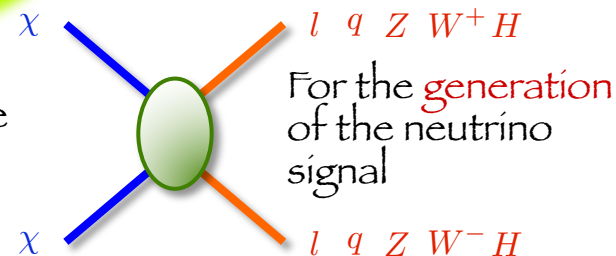




Galactic signals  
Neutrinos from earth and sun



Feels only the local DM density  
Feels (somehow) how DM is locally distributed in velocity space





# Capture Rate

- Elastic scattering of the DM particle with a nucleus  $i$  in a spherical shell at a distance  $r$  from the center of the Earth (or Sun)
- In order to be captured, the velocity of the DM particle after the interaction must be smaller than the escape velocity at the shell

$$v_{\text{esc}}^{\text{Sun}} = 618 \text{ Km s}^{-1}$$

at the surface

$$v_{\text{esc}}^{\text{Earth}} = 11.2 \text{ Km s}^{-1}$$

$$\langle v \rangle \sim 300 \text{ Km s}^{-1}$$

mean DM particle velocity

# Capture Rate

$$C = \sum_i \left( \frac{8}{3\pi} \right)^{1/2} \left[ \sigma_i \frac{\rho_\chi \bar{v}}{m_\chi} \right] \left[ \frac{M_i}{m_i} \right] \left[ \frac{3v_{esc}^2}{2\bar{v}^2} \langle \phi \rangle_i \right] \xi(\infty) S_i$$

interaction rate of a flux of DM particle with a nucleus in free space

number of nuclei of type  $i$  in the body

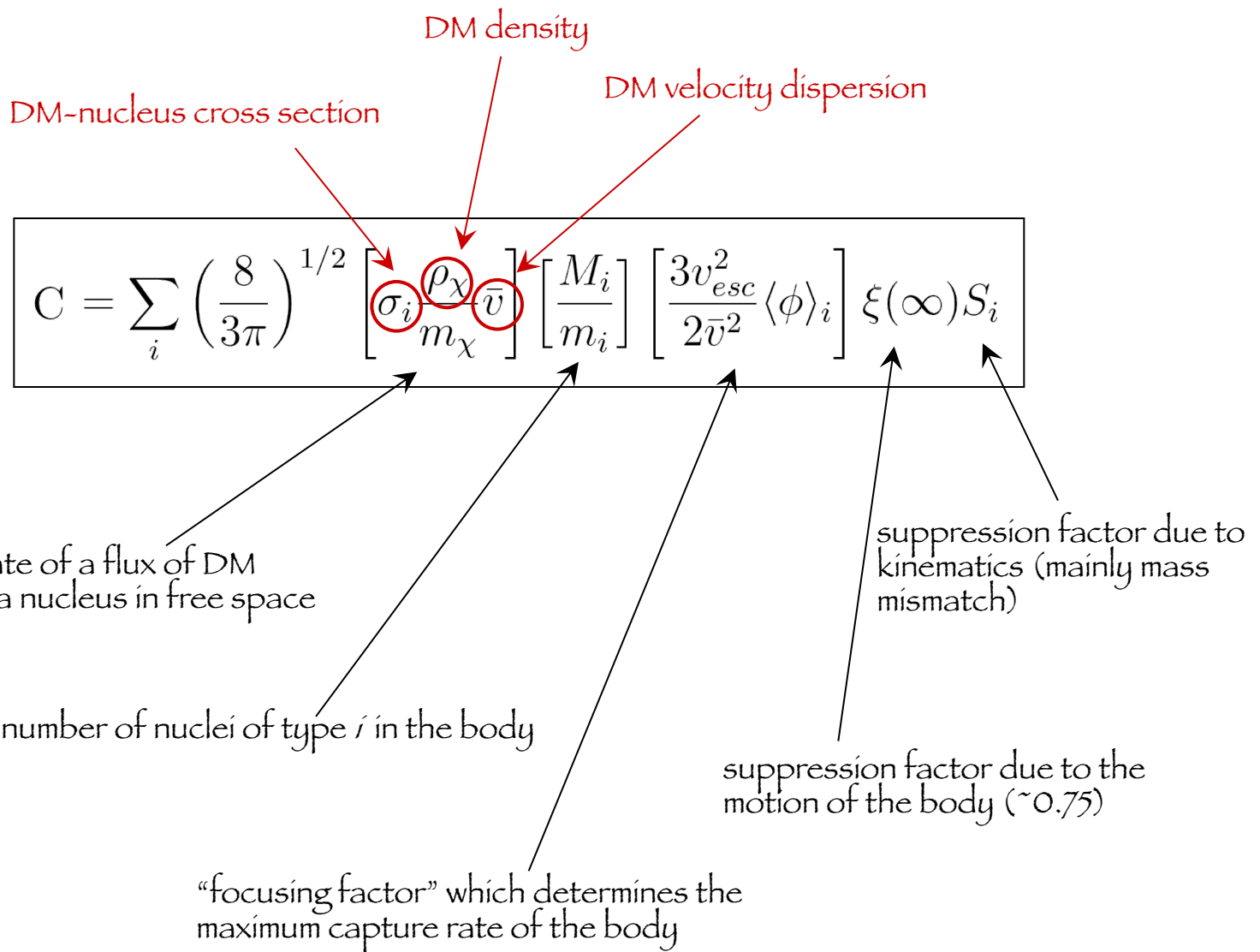
“focusing factor” which determines the maximum capture rate of the body

suppression factor due to the motion of the body ( $\sim 0.75$ )

suppression factor due to kinematics (mainly mass mismatch)

$M_i$  Total mass in terms of element  $i$

$\langle \phi \rangle_i$  Gravitational potential averaged over the mass distribution of element  $i$



$M_i$  Total mass in terms of element  $i$

$\langle \phi \rangle_i$  Gravitational potential averaged over the mass distribution of element  $i$

# Capture Rate

$$C = \sum_i \left( \frac{8}{3\pi} \right)^{1/2} \left[ \sigma_i \frac{\rho_\chi}{m_\chi} \bar{v} \right] \left[ \frac{M_i}{m_i} \right] \left[ \frac{3v_{esc}^2}{2\bar{v}^2} \langle \phi \rangle_i \right] \xi(\infty) S_i$$

Sun

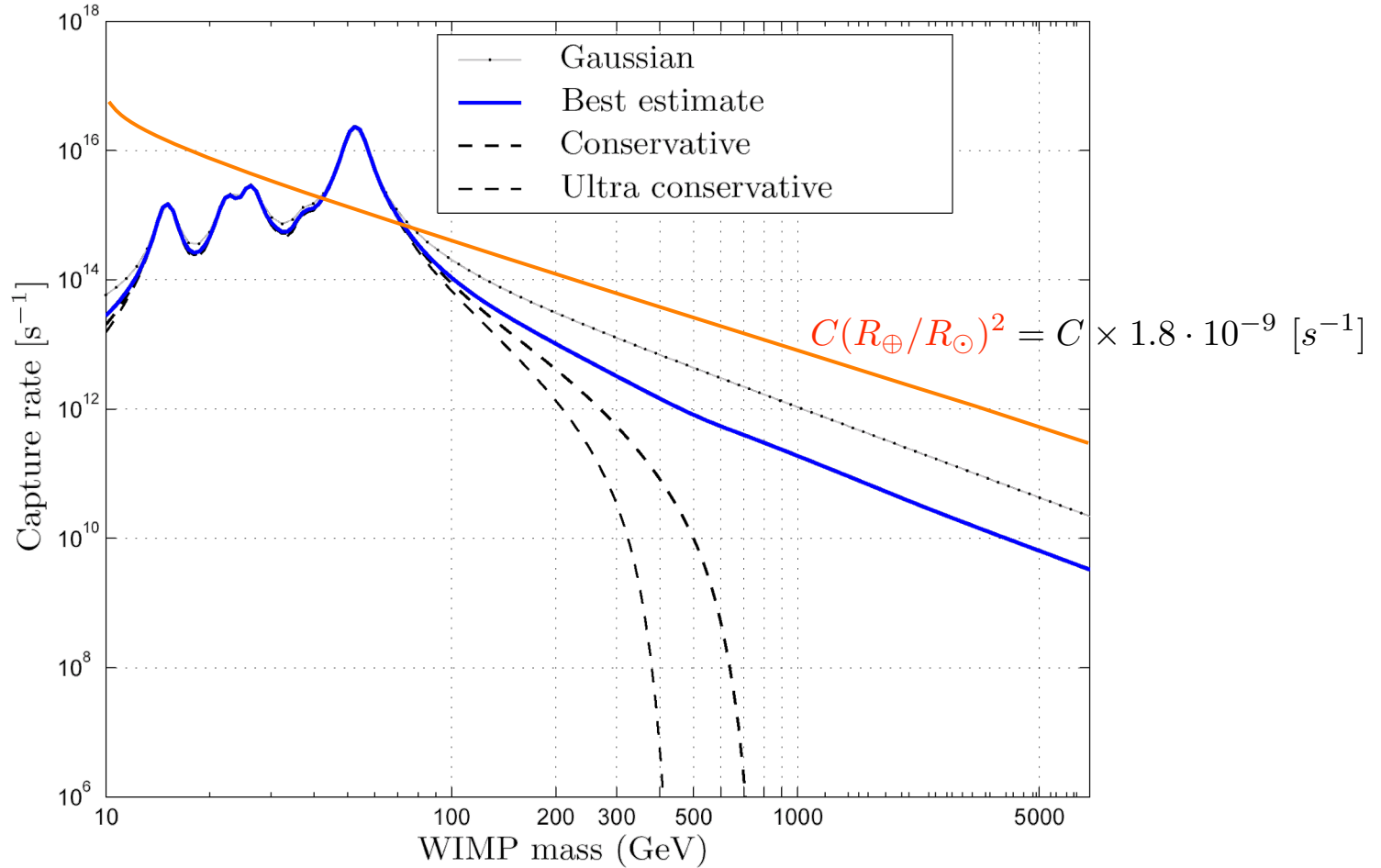
Nuc	H	He	O	C	Ne	Fe	N	Si	Mg
f	0.77	0.21	$8 \cdot 10^{-3}$	$4 \cdot 10^{-3}$	$1 \cdot 10^{-3}$	$1 \cdot 10^{-3}$	$9 \cdot 10^{-4}$	$8 \cdot 10^{-4}$	$7 \cdot 10^{-4}$
A	1	4	16	12	20	56	14	28	24

nuclei of type  $i$  in the body

Earth

	core			mantle					
Nuc	Fe	Si	Ni	O	Si	Mg	Fe	Ca	Al
f	0.24	0.05	0.03	0.30	0.15	0.14	0.06	0.02	0.01
A	56	32	59	16	28	24	56	40	27

# Capture rate on the Earth



# Solar bound orbits

- Numerical simulation of Near Earth Asteroids show that many of these have life times in the solar system less than 2 Myr
- After that, they are either:
  - Driven into the Sun
  - Escape the solar system
- If this would occur also to the DM particles, this would significantly reduce the number of these particles bound to the solar system, and therefore reduce the capture rate on Earth

and consequently the neutrino signal

# Accumulation and concentration

- DM particles which have been captured inside Earth or Sun can suffer subsequent scatterings
- This may lead to:
  - Concentration in the innermost parts of the Earth or Sun
  - Development of an equilibrium distribution of these particles

distribution  $n(r) = n_0 e^{-\alpha_B m_\chi r^2}$

$n_0$  central density

$$\alpha_B = 2\pi G \rho_0 / (3T_0)$$

Earth  $R_{\text{prod}} \sim 500 \text{ km} \sqrt{100 \text{ GeV} / m_{\text{DM}}}$

Sun  $R_{\text{prod}} \sim 0.01 R_\odot \sqrt{100 \text{ GeV} / m_{\text{DM}}}$

# Annihilation rate

Evolution equation

$$\frac{dN}{dt} = C - 2\Gamma_A$$

Total number of captures DM particles

$$N = C \tau_A \tanh(t_0/\tau_A)$$

Annihilation rate

$$\Gamma_A = \frac{1}{2} \langle \sigma_{\text{ann}v} \rangle \int d^3r n^2(r)$$

$$\Gamma_A = \frac{C}{2} \tanh^2 \left( \frac{t_0}{\tau_A} \right)$$

Capture rate

$C$

Age of the body

$t_0 = 4.6 \text{ Gyr}$

Relaxation time

$\tau_A = [CC_A]^{-1/2}$

$$C_A = \langle \sigma_{\text{ann}v} \rangle_0 V_2 / V_1^2$$

$$V_j = c_B (j m_\chi / 10 \text{ GeV})^{-3/2} \text{ cm}^3$$

$$c_B = 1.8 \cdot 10^{25} / 6.6 \cdot 10^{28}$$

Earth

Sun

Effective volumes of DM concentrations  
More concentrated for larger masses



# Neutrino flux

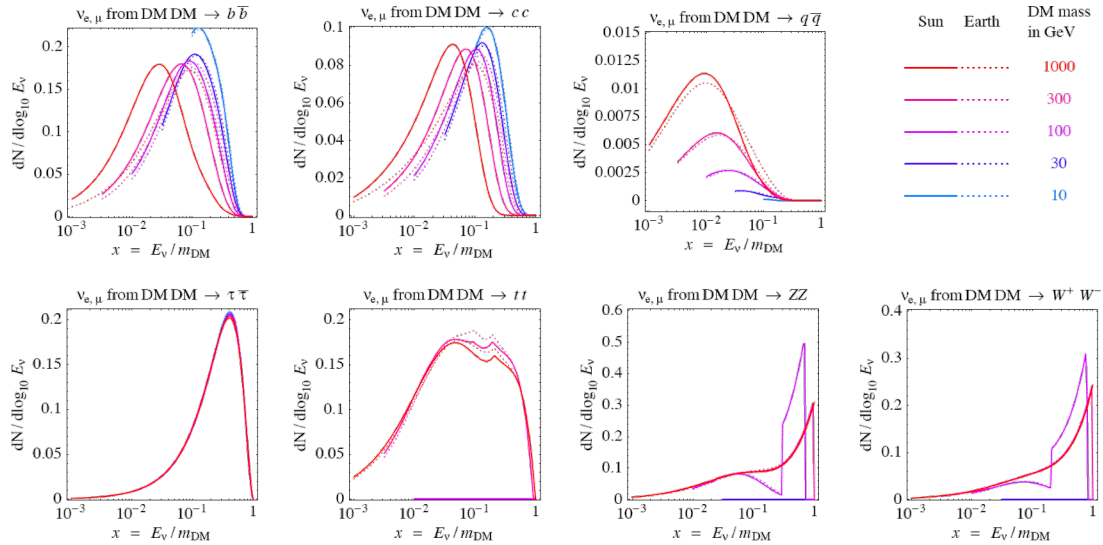
$$\frac{dN_\nu}{dE_\nu} = \frac{\Gamma_A}{4\pi R^2} \sum_{\mathcal{F}} \text{BR}(\chi\chi \rightarrow \mathcal{F}) \frac{dN_\nu^{\mathcal{F}}}{dE_\nu}$$

# Neutrino Production

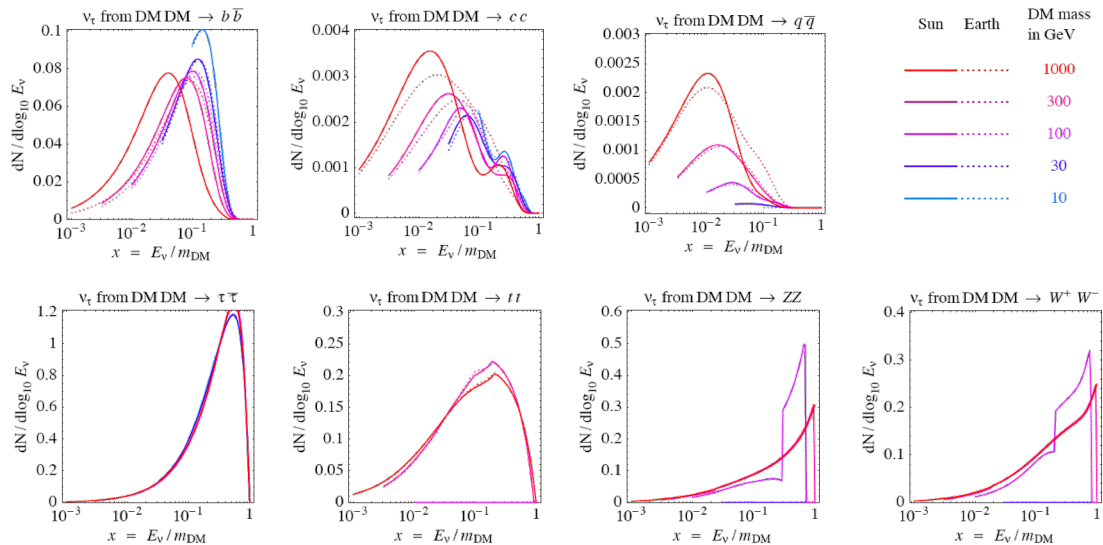
- Neutrinos are produced by DM annihilation
  - Available channels depend on mass threshold
$$\chi\chi \rightarrow \nu\nu, \ell\bar{\ell}, q\bar{q}, W^+W^-, ZZ, \text{Higgses}, \text{Higgs} + \text{gauge}$$
  - Quark hadronize  $\rightarrow$  neutrinos from hadron decay
- Productions in Earth
  - Muons: stopped before decay  $\rightarrow$  neutrinos below typical thresholds
  - Taus: decay almost as in vacuum
  - Light hadrons: typically stopped before decay
  - Heavy hadrons: typically decay before losing significant energy
- Production in Sun
  - Leptons: stopping power of medium is stronger  $\rightarrow$  softer neutrino spectra
  - Light hadrons: typically stopped before decay
  - Heavy hadrons: energy losses important, need modeling

# Spectra at production

$\nu_e, \nu_\mu$



$\nu_\tau$



# Neutrino Propagation

## Density matrix evolution

$$\frac{d\rho}{dr} = -i[\mathbf{H}, \rho] + \left. \frac{d\rho}{dr} \right|_{\text{CC}} + \left. \frac{d\rho}{dr} \right|_{\text{NC}} + \left. \frac{d\rho}{dr} \right|_{\text{in}}$$

$$\rho = \sum_j p_j |\psi_j\rangle \langle \psi_j| \quad i = e, \mu, \tau$$

diag( $\rho$ ): population of flavour  $i$   
non-diag( $\rho$ ): superposition of flavour  $i$  and  $j$

mixing, oscillations, decoherence

# Neutrino Propagation

## Density matrix evolution

$$\frac{d\rho}{dr} = -i[\mathbf{H}, \rho] + \left. \frac{d\rho}{dr} \right|_{\text{CC}} + \left. \frac{d\rho}{dr} \right|_{\text{NC}} + \left. \frac{d\rho}{dr} \right|_{\text{in}}$$

Vacuum oscillation  
MSW matter effect

CC interactions  
(absorption and  $\nu_\tau$  regeneration)

NC scatterings  
(absorption and re-injection)

source

# Neutrino Propagation

Density matrix evolution

$$\frac{d\rho}{dr} = -i[\mathbf{H}, \rho] + \left. \frac{d\rho}{dr} \right|_{\text{CC}} + \left. \frac{d\rho}{dr} \right|_{\text{NC}} + \left. \frac{d\rho}{dr} \right|_{\text{in}}$$

source

Vacuum oscillations and MSW matter effect

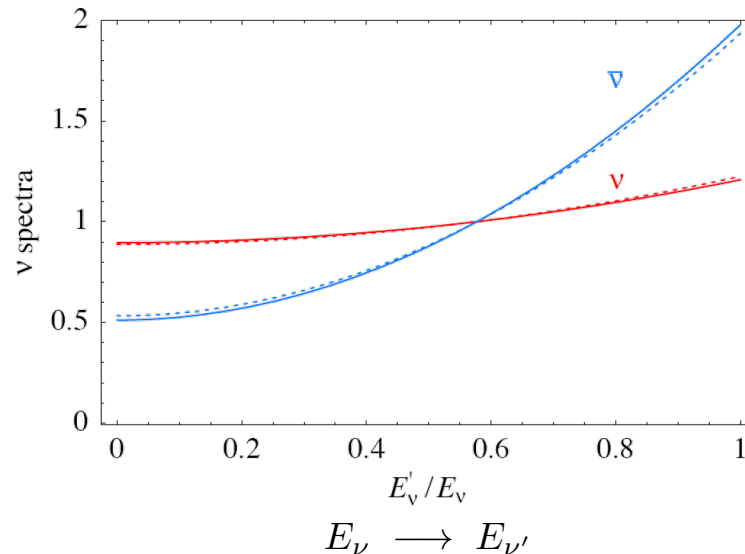
$$\mathbf{H} = \frac{\mathbf{m}^\dagger \mathbf{m}}{2E_\nu} + \sqrt{2}G_{\text{F}} \left[ N_e \text{diag}(1, 0, 0) - \frac{N_n}{2} \text{diag}(1, 1, 1) \right]$$

# NC scatterings

$$\left. \frac{d\rho}{dr} \right|_{\text{NC}} = - \int_0^{E_\nu} dE'_\nu \frac{d\Gamma_{\text{NC}}}{dE'_\nu}(E_\nu, E'_\nu) \rho(E_\nu) + \int_{E_\nu}^{\infty} dE'_\nu \frac{d\Gamma_{\text{NC}}}{dE'_\nu}(E'_\nu, E_\nu) \rho(E'_\nu)$$

absorption
re-injection

$$\Gamma_{\text{NC}}(E_\nu, E'_\nu) = N_p(r) \text{diag } \sigma(\nu_{\ell p} \rightarrow \nu'_\ell X) + N_n(r) \text{diag } \sigma(\nu_{\ell n} \rightarrow \nu'_\ell X)$$



# CC absorptions and $\nu_\tau$ regeneration

$\begin{aligned} \nu_\tau &\rightarrow \tau^- \rightarrow X \nu_\tau \\ &\rightarrow e^- \bar{\nu}_e \nu_\tau \\ &\rightarrow \mu^- \bar{\nu}_\mu \nu_\tau \end{aligned}$	$\begin{aligned} \bar{\nu}_\tau &\rightarrow \tau^+ \rightarrow X \bar{\nu}_\tau \\ &\rightarrow e^+ \nu_e \bar{\nu}_\tau \\ &\rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau \end{aligned}$
---	---

$$\left. \frac{d\rho}{dr} \right|_{\text{CC}} = -\frac{\{\mathbf{\Gamma}_{\text{CC}}, \rho\}}{2} + \int \frac{dE_\nu^{\text{in}}}{E_\nu^{\text{in}}} \left[ \mathbf{\Pi}_\tau \rho_{\tau\tau}(E_\nu^{\text{in}}) \mathbf{\Gamma}_{\text{CC}}^\tau(E_\nu^{\text{in}}) f_{\tau \rightarrow \tau}(E_\nu^{\text{in}}, E_\nu) \right. \\ \left. + \mathbf{\Pi}_{e,\mu} \bar{\rho}_{\tau\tau}(E_\nu^{\text{in}}) \bar{\mathbf{\Gamma}}_{\text{CC}}^\tau(E_\nu^{\text{in}}) f_{\bar{\tau} \rightarrow e,\mu}(E_\nu^{\text{in}}, E_\nu) \right],$$

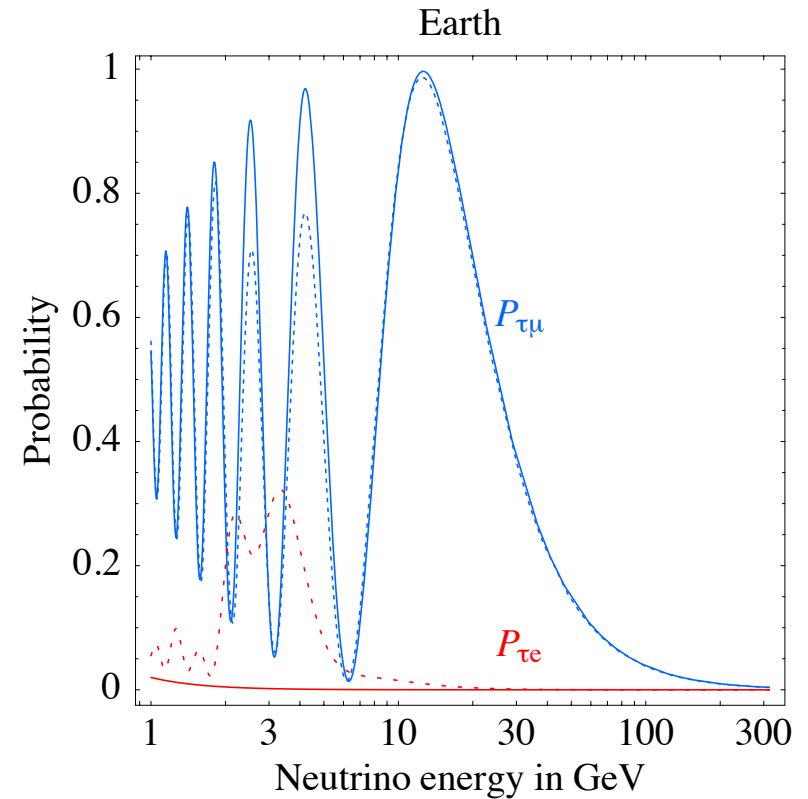
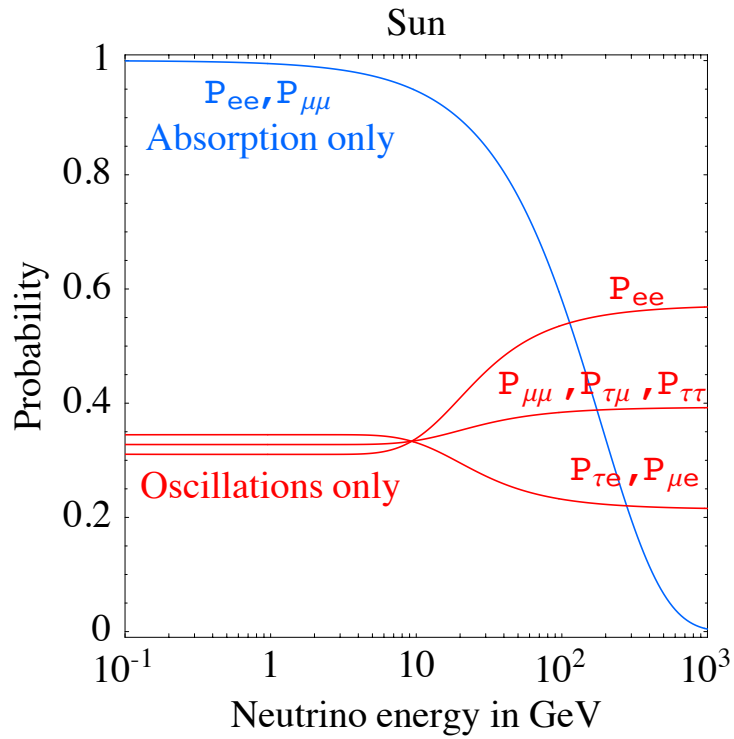
$$\left. \frac{d\bar{\rho}}{dr} \right|_{\text{CC}} = -\frac{\{\bar{\mathbf{\Gamma}}_{\text{CC}}, \bar{\rho}\}}{2} + \int \frac{dE_\nu^{\text{in}}}{E_\nu^{\text{in}}} \left[ \mathbf{\Pi}_\tau \bar{\rho}_{\tau\tau}(E_\nu^{\text{in}}) \bar{\mathbf{\Gamma}}_{\text{CC}}^\tau(E_\nu^{\text{in}}) f_{\bar{\tau} \rightarrow \bar{\tau}}(E_\nu^{\text{in}}, E_\nu) \right. \\ \left. + \mathbf{\Pi}_{e,\mu} \rho_{\tau\tau}(E_\nu^{\text{in}}) \mathbf{\Gamma}_{\text{CC}}^\tau(E_\nu^{\text{in}}) f_{\tau \rightarrow \bar{e},\bar{\mu}}(E_\nu^{\text{in}}, E_\nu) \right].$$

$$\mathbf{\Gamma}_{\text{CC}}(E_\nu) = \text{diag}(\Gamma_{\text{CC}}^e, \Gamma_{\text{CC}}^\mu, \Gamma_{\text{CC}}^\tau), \quad \mathbf{\Gamma}_{\text{CC}}^\ell = N_p(r) \sigma(\nu_\ell p \rightarrow \ell X) + N_n(r) \sigma(\nu_\ell n \rightarrow \ell X)$$

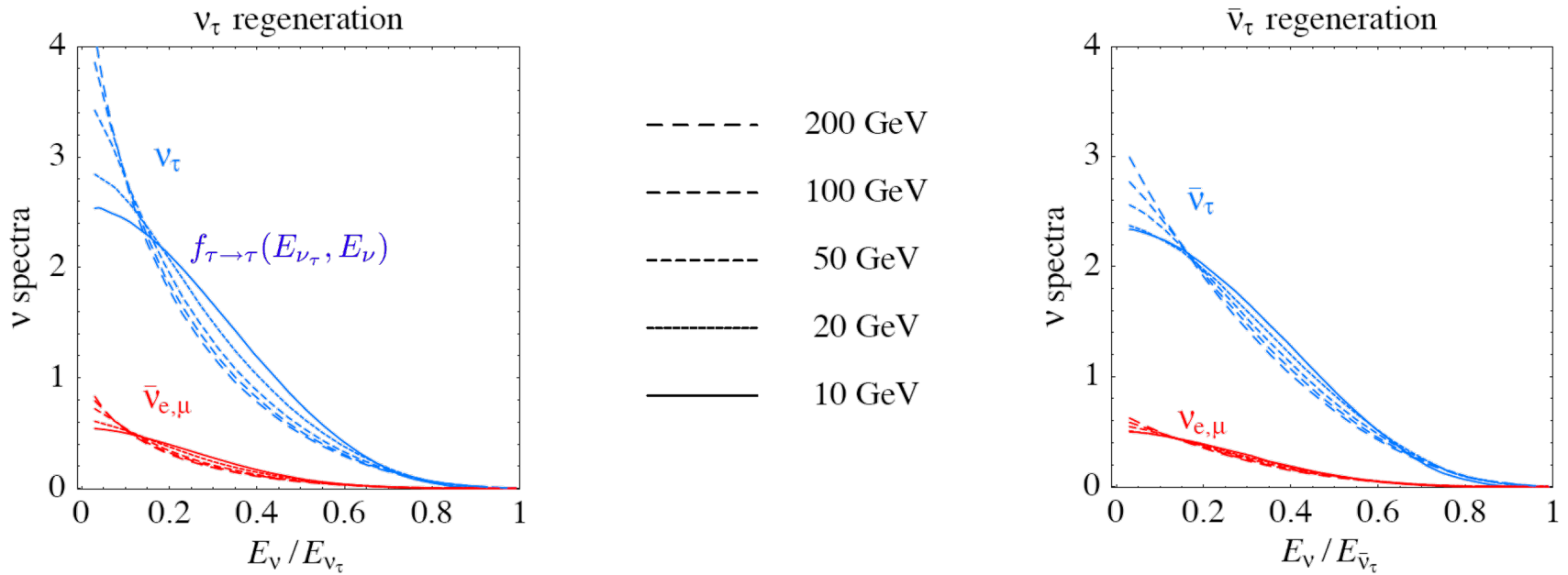
$$\bar{\mathbf{\Gamma}}_{\text{CC}}(E_\nu) = \text{diag}(\bar{\Gamma}_{\text{CC}}^e, \bar{\Gamma}_{\text{CC}}^\mu, \bar{\Gamma}_{\text{CC}}^\tau), \quad \bar{\mathbf{\Gamma}}_{\text{CC}}^\ell = N_p(r) \sigma(\bar{\nu}_\ell p \rightarrow \bar{\ell} X) + N_n(r) \sigma(\bar{\nu}_\ell n \rightarrow \bar{\ell} X)$$



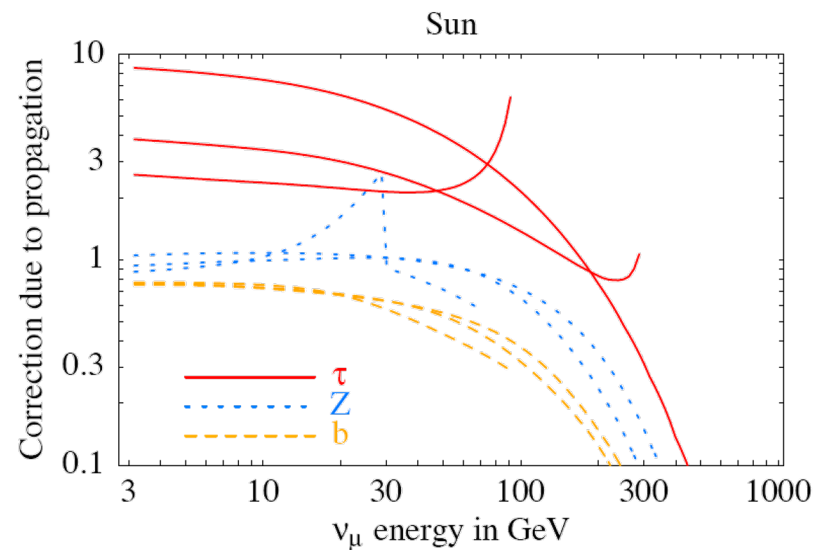
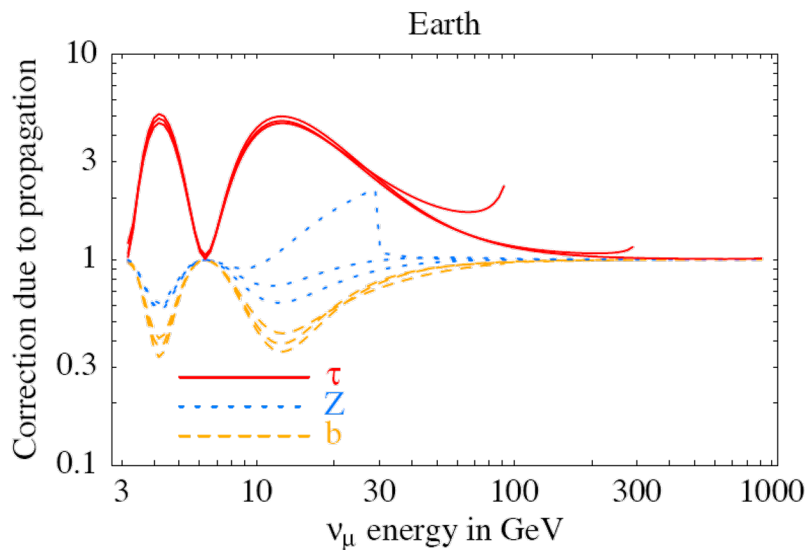
# Oscillations probabilities and absorption



# Tau-neutrino regeneration



# Effect of propagation



## Earth:

- Affected only by “atmospheric” oscillation  $\nu_\mu \leftrightarrow \nu_\tau$  at  $E < 100$  GeV

## Sun:

- Affected by average “solar” and “atmospheric” oscillations
- Absorption suppresses neutrinos for  $E > 100$  GeV (partially converted to lower energy neutrinos (by NC and regeneration))

# Signal at Neutrino Telescopes: upgoing muons

$$\frac{d^2 N_\mu^{(\nu)}}{dE_\mu dE_\nu} = N_A \frac{dN_\nu}{dE_\nu} \int_0^X dX \int_{E_\mu}^{E_\nu} dE'_\mu \frac{d\sigma_\nu(E_\nu, E'_\mu)}{dE'_\mu} \cdot g(E_\mu, E'_\mu; X)$$

neutrino flux

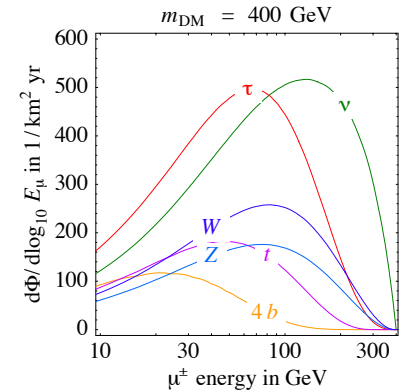
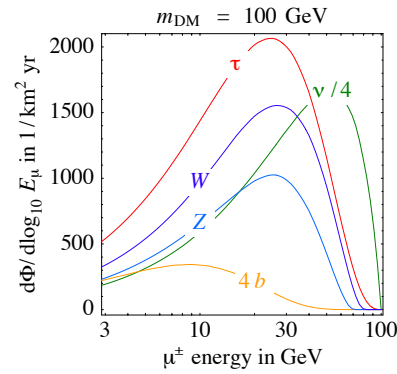
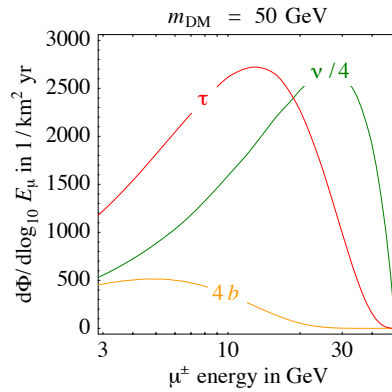
muon pathlength in rock

CC cross section neutrino-nucleus

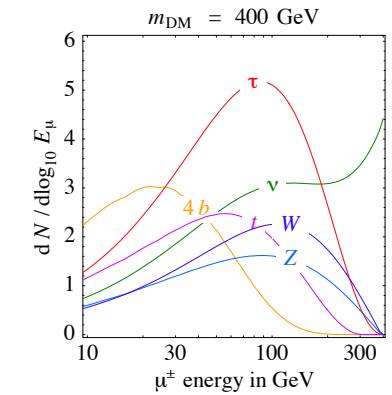
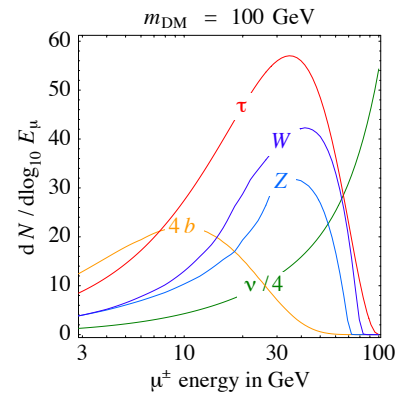
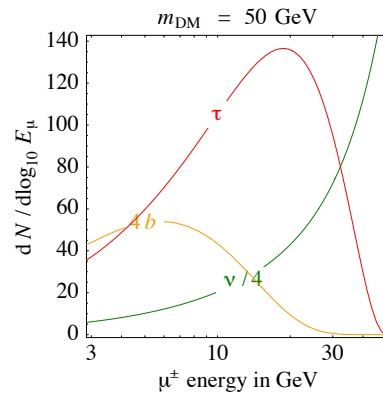
Probability that a muon with energy  $E'_\mu$  emerges with energy  $E_\mu$  after traveling a path  $X$  in rock

# Neutrino telescope signal from the Sun

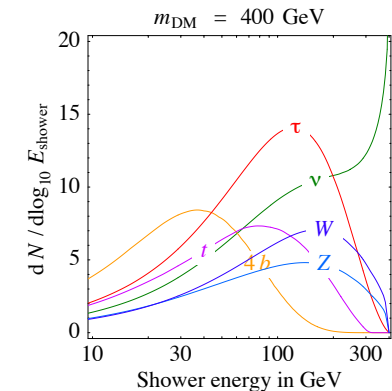
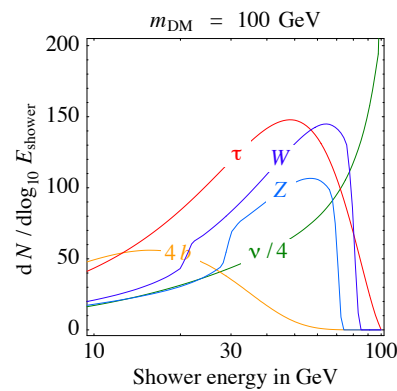
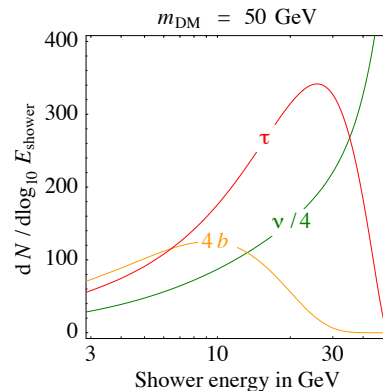
Thru-going muons



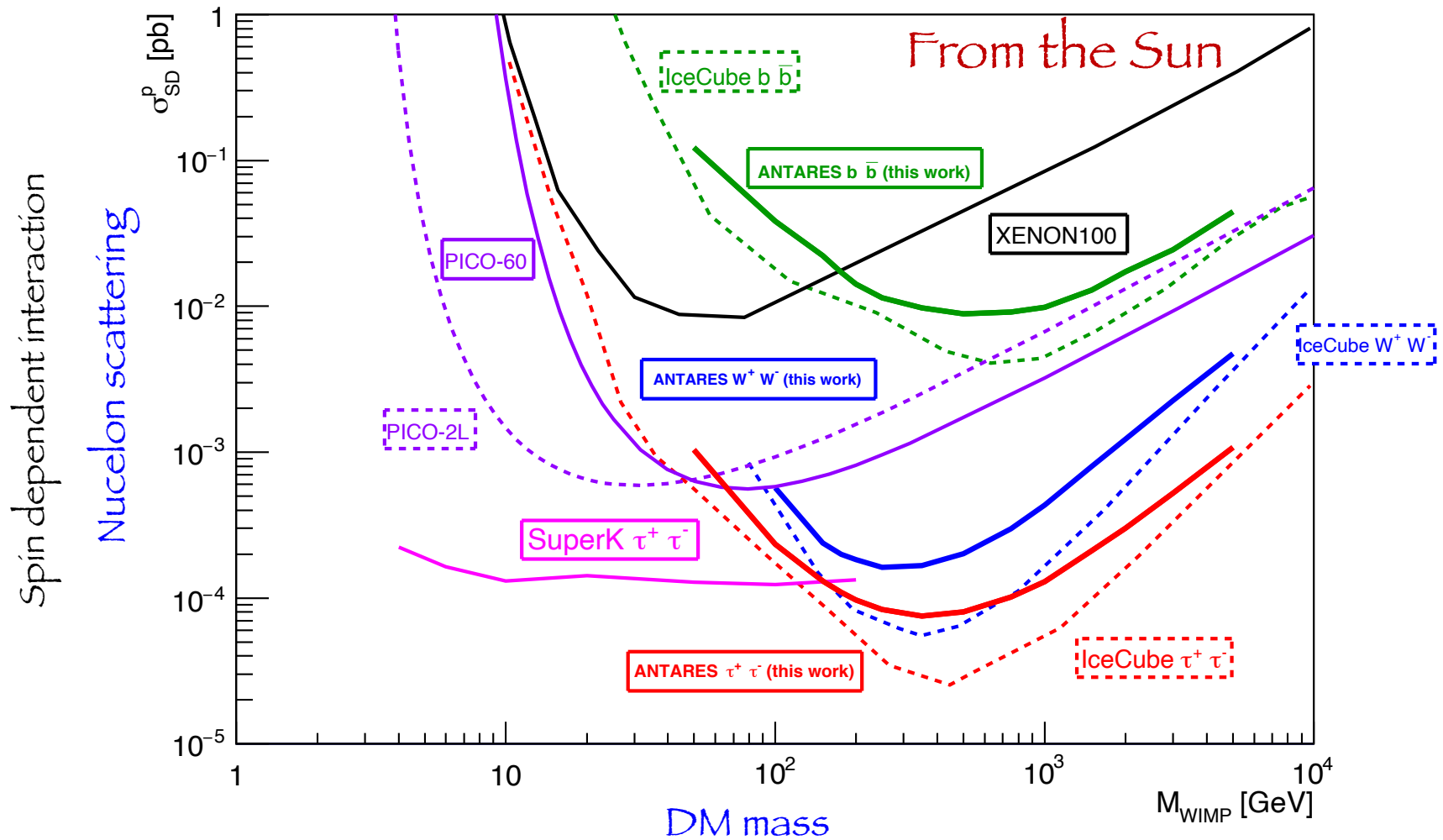
Fully-contained muons



“Showers”



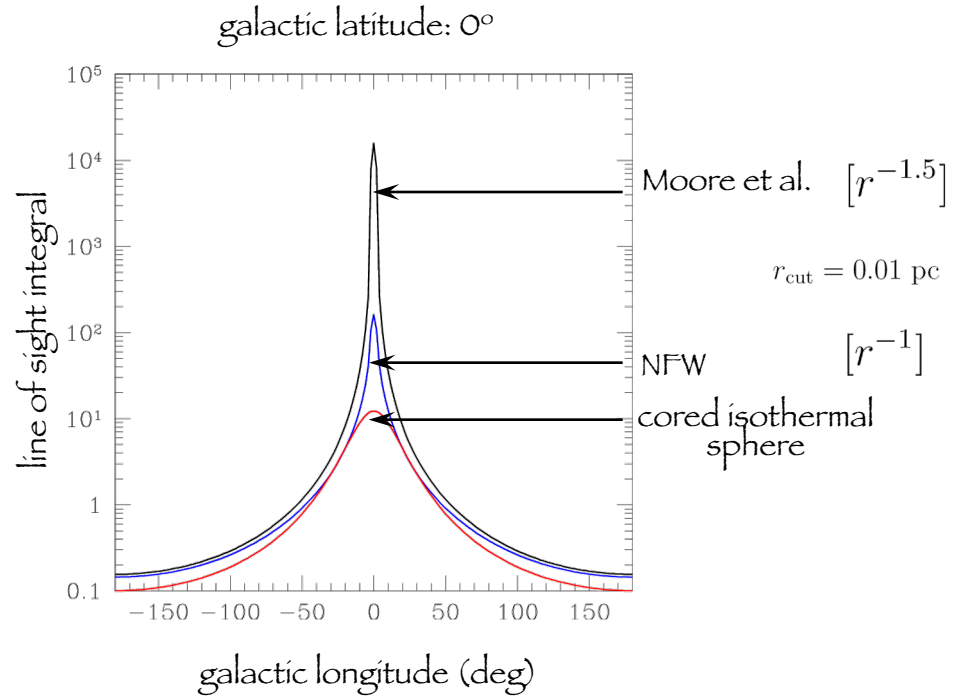
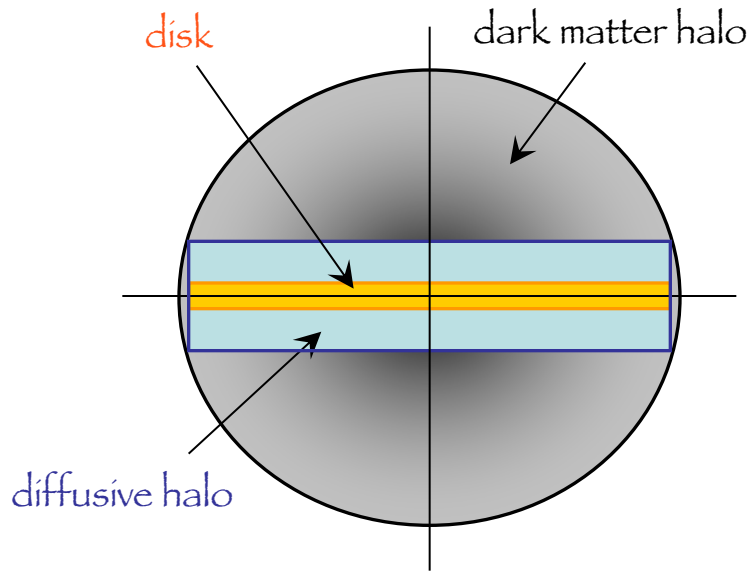
# Bounds on capture cross section



ANTARES Collab, PLB 759 (2016) 69

Warning: bounds are typically derived under the assumption of perfect equilibration between capture and annihilation (and contact interactions)

# Annihilation in the galactic halo



DM signal

$$\chi\chi \longrightarrow (\dots) \longrightarrow \nu\bar{\nu}$$

The flux is sensitive to the DM density profile

# Flux from galactic DM

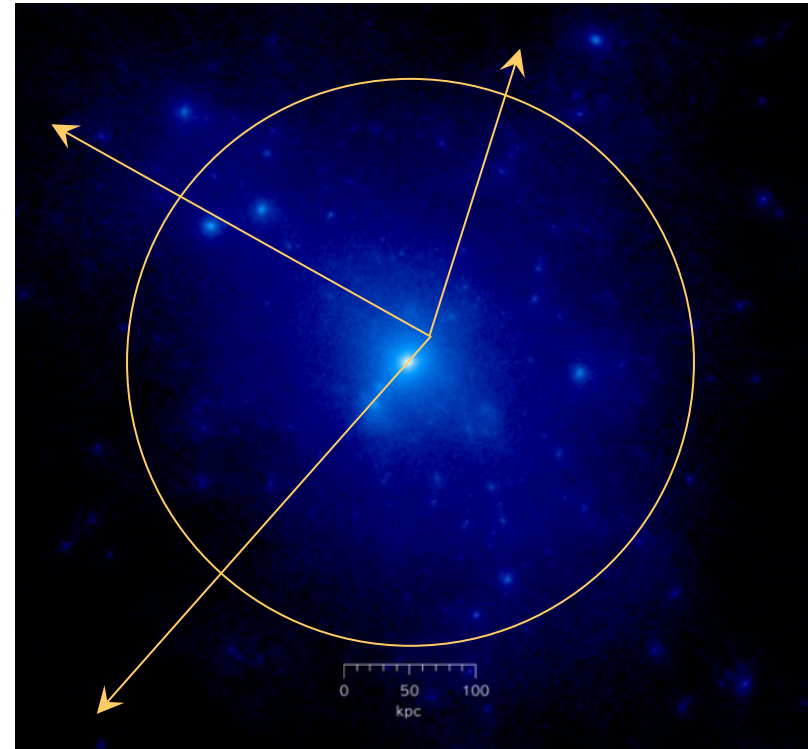
Flux:

$$\Phi_{\gamma}^{\text{DM}}(E_{\gamma}, \psi) = \frac{1}{4\pi} \frac{\langle \sigma_{\text{ann}} v \rangle_0}{2m_{\chi}^2} g_{\gamma}(E_{\gamma}) I(\psi)$$

$$I(\psi) = \int_{\text{l.o.s.}} \rho^2(r(\lambda, \psi)) d\lambda$$

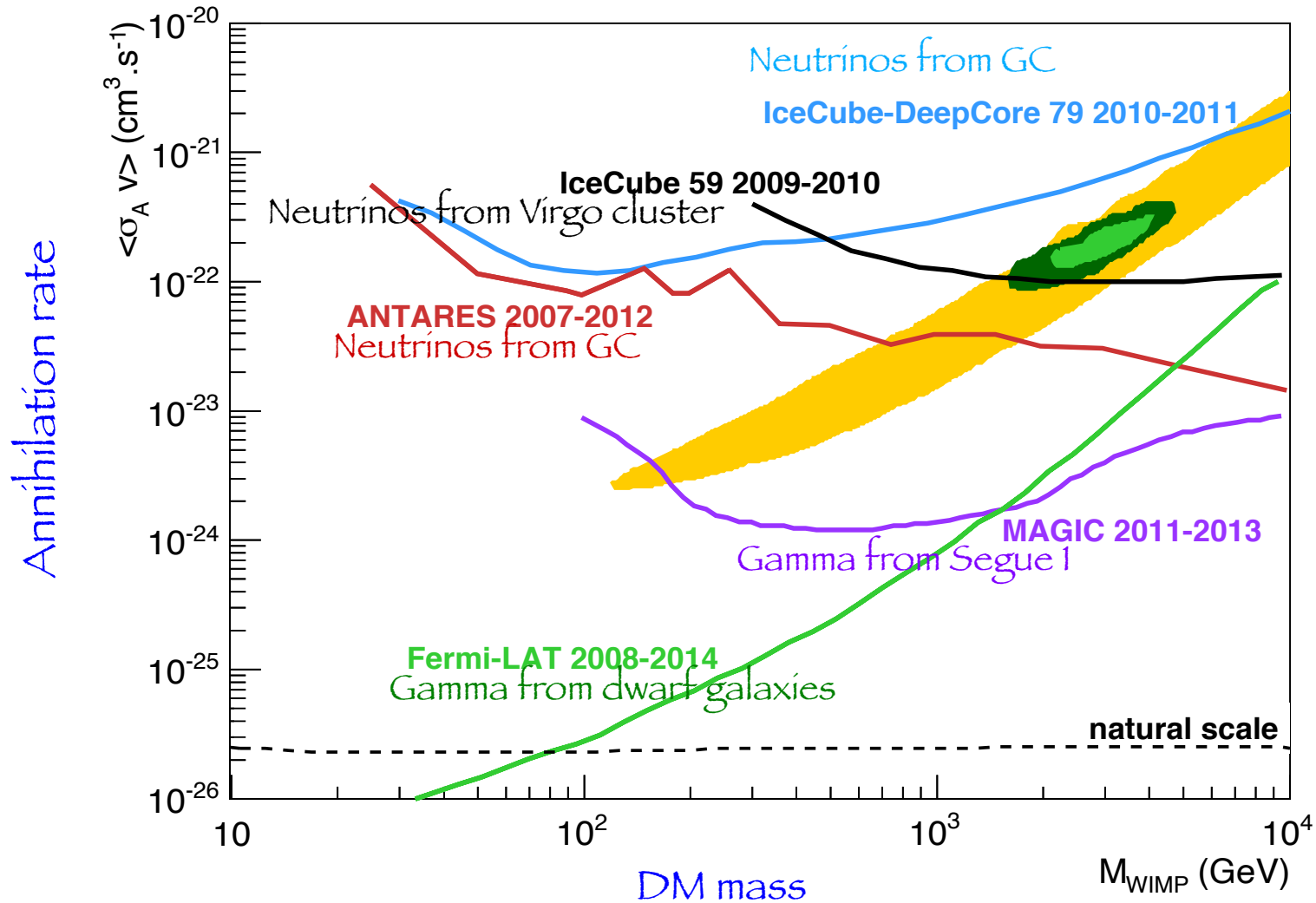
$$\rho(\vec{r}) = \rho_{\text{halo}}(\vec{r}) + \sum_i \rho_{\text{sub}}(\vec{r}_s) \vec{r}$$

$$g(E) = \sum_{\mathcal{F}} \text{BR}(\chi\chi \rightarrow \mathcal{F}) \left( \frac{dN}{dE} \right)_{\mathcal{F}}$$

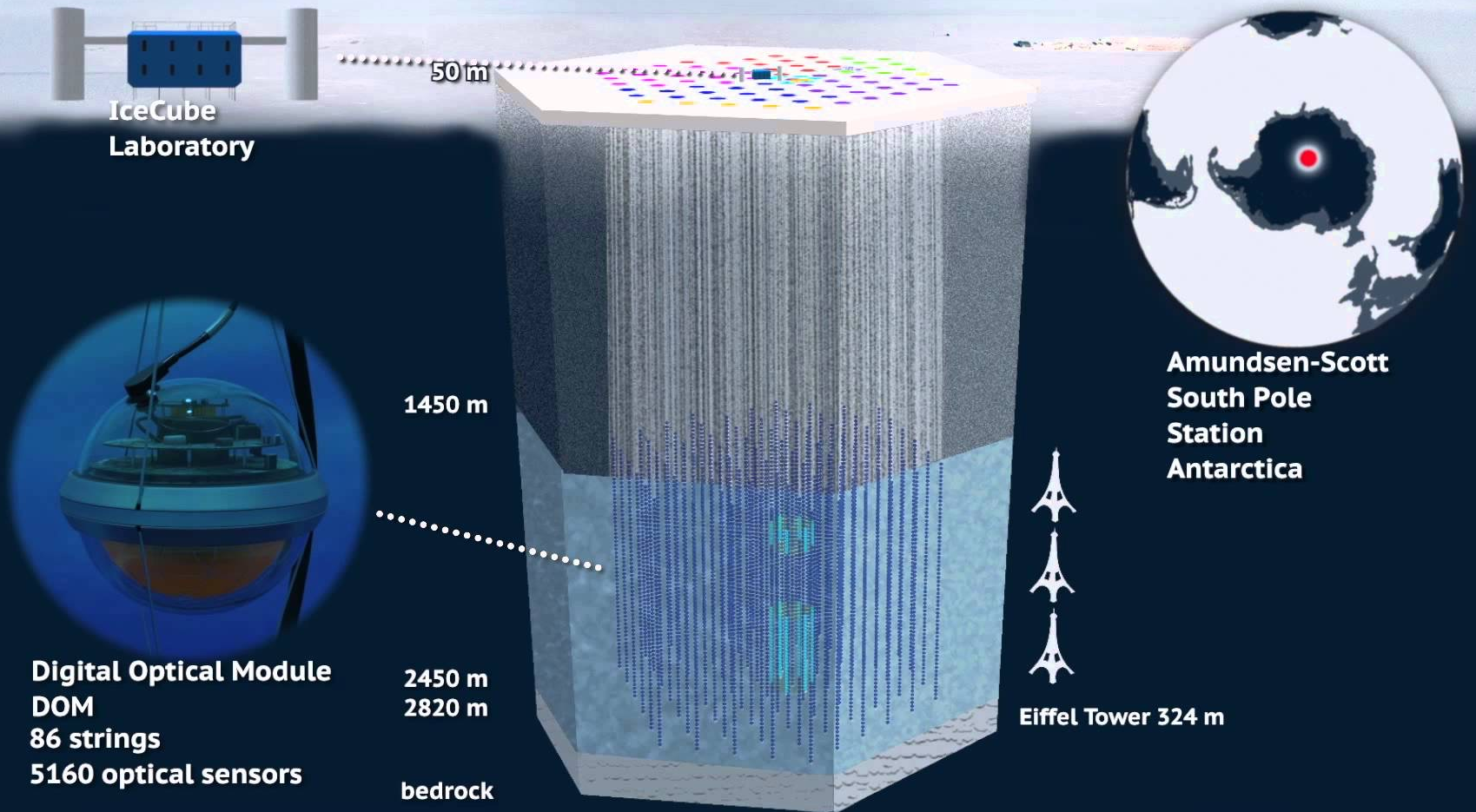




# Bounds on annihilation cross section



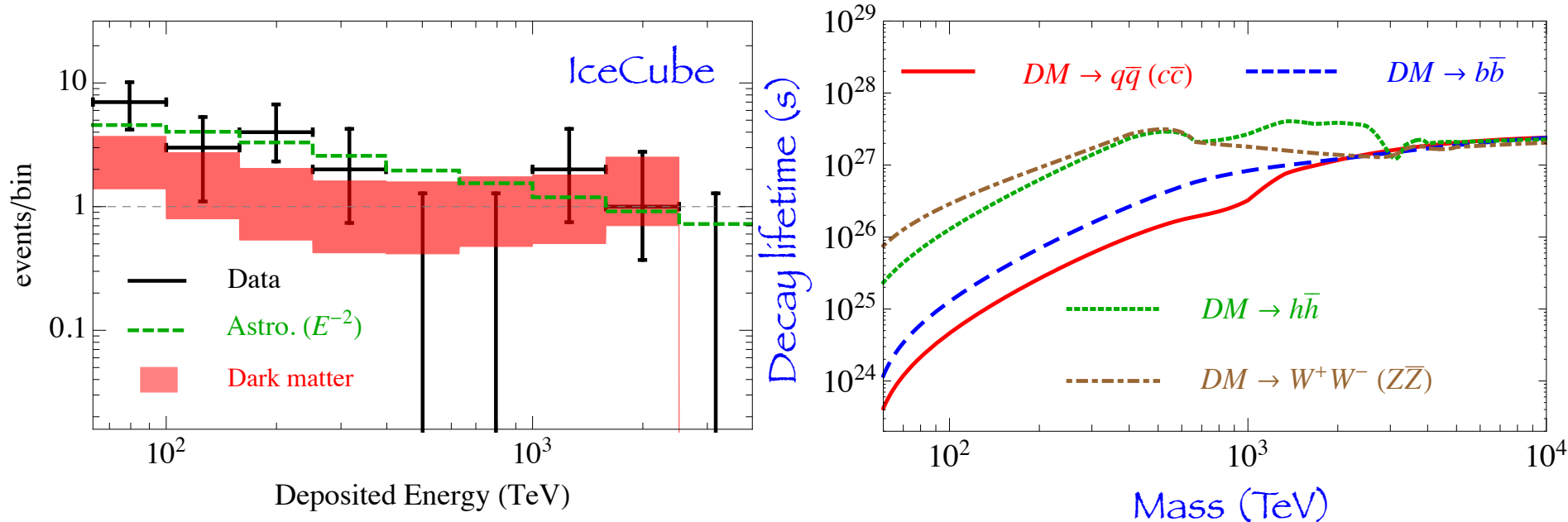
# IceCube



# IceCube PeV neutrinos

The spectral feature of the IceCube PeV events could refer to decaying very heavy DM: PeV scale

e.g.  $m_{\text{DM}} = 4 \text{ PeV}$  lifetime  $= 10^{28} \text{ s}$





# Km<sup>3</sup>NET

