

Electroweak Phase Transitions with BSM Fermions

[arXiv:2107.09617]

Martin Gabelmann, M. Margarete Mühlleitner, Jonas Müller | 26. August 2021

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- 1 Motivation
- 2 The 2HDM + Electroweakinos
- 3 Strength of the Electroweak Phasetransition in the 2HDM+EWinos

1 Motivation

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3 Strength of the Electroweak Phase Transition in the 2HDM+EWinos

Experimental constraints on...

Electroweakinos

(i.e. weak fermions)

Extended Higgs sectors

(e.g. MSSM inspired 2HDM)

Coloured Scalars

(e.g. stops)

$$m_{\chi_1^0} \gtrsim 50\text{-}200 \text{ GeV}$$

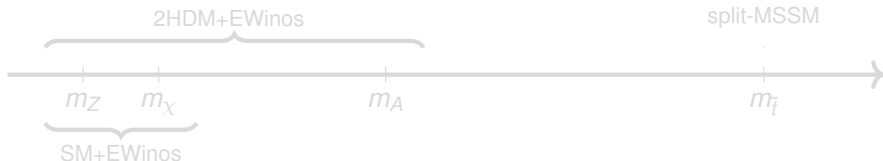
$$m_A \gtrsim 500\text{-}600 \text{ GeV}$$

$$m_{\tilde{t}_1} \gtrsim 1\text{-}2 \text{ TeV}$$

$$m_{\chi_1^\pm} \gtrsim 94 \text{ GeV}$$

$$\tan \beta \gtrsim 1 - 2 \text{ [Bah et. al]}$$

... suggest a hierarchy between scalars and fermions (\rightarrow split SUSY)



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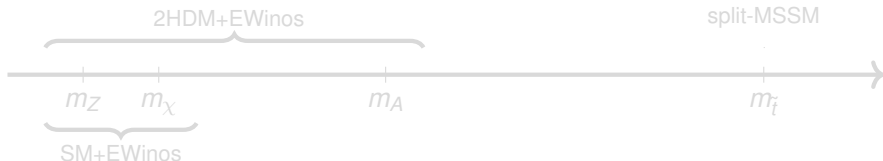
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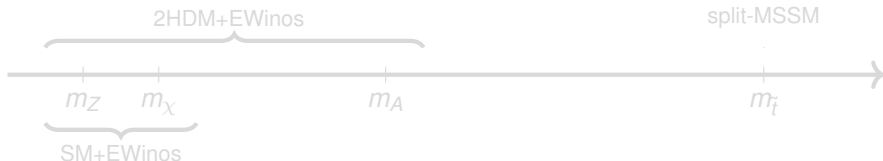
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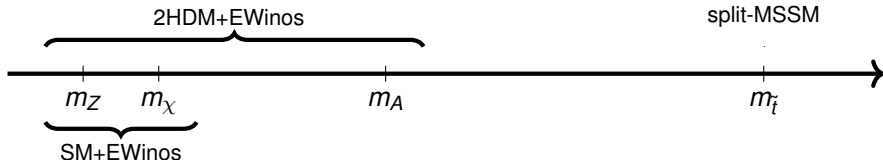
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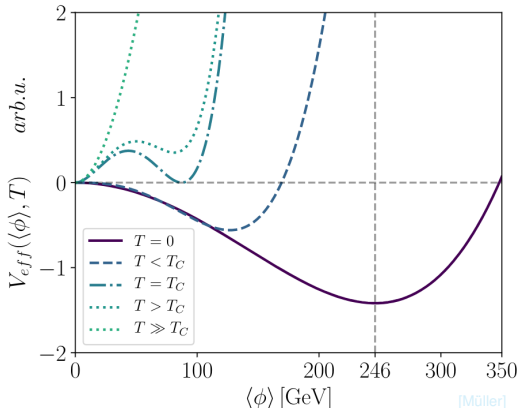
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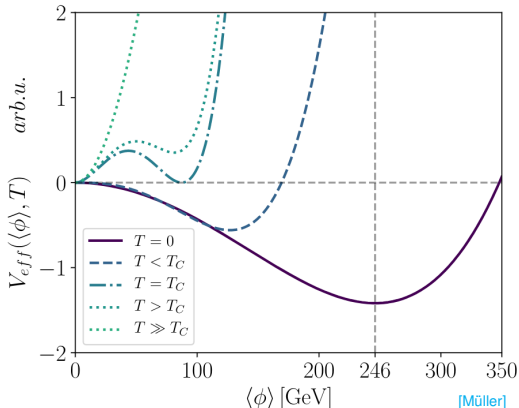
Strong first order EW phase transition (SFOEWPT):

- $\xi_c = v_c/T_c \gtrsim 1$
necessary requirement for baryogenesises [Sakharov]
- not possible in the SM ($m_h < 70$ GeV) [Kajantie et. al]
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Implications of Electroweak Phasetransitions

(vanilla) **MSSM**

- scalar potential governed by gauge sector $\lambda_i \propto g_1^2, g_2^2$
- $\xi_c > 1$ requires $m_{\tilde{t}} < 115 \text{ GeV}$
[Carena et. al]

(vanilla) **2HDM**

- $\xi_c > 1$ possible [Bochkarev et. al]
- increasing tension due to constraints on m_A, m_{H^\pm}, m_H
[Black et. al]

→ **Question:**

- Q1: can split-SUSY fermions relax tensions in the 2HDM?
- Q2: can it emerge from non-minimal split-SUSY?

1 Motivation

2 The 2HDM + Electroweakinos

3 Strength of the Electroweak Phase Transition in the 2HDM+EWinos

Type II 2HDM with a soft \mathbb{Z}_2 -breaking term:

$$V_{2\text{HDM}} = \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_2^\dagger \Phi_1|^2 \\ + \left(\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 - m_{12}^2 \Phi_1^\dagger \Phi_2 + h.c. \right) + m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2$$

Spectrum after EWSB:

- 2 CP-even h_{SM} and H
- 1 CP-odd A
- 1 charged Higgs pair H^\pm

Similar to the MSSM, add triplet (\tilde{W}), singlet \tilde{B} and two doublets (\tilde{H}_u, \tilde{H}_d):

$$\begin{aligned}
 V_{inos} = & \frac{1}{\sqrt{2}} H_u^\dagger (g_{2u} \sigma_a \tilde{W}^a + g_{1u} \tilde{B}) \tilde{H}_u - \frac{1}{\sqrt{2}} H_d^\dagger (g_{2d} \sigma_a \tilde{W}^a + g_{1d} \tilde{B}) \tilde{H}_d \\
 & + \frac{M_{\tilde{W}}}{2} \tilde{W}^a \tilde{W}^a + \frac{M_{\tilde{B}}}{2} \tilde{B} \tilde{B} + \mu \tilde{H}_u (i\sigma_2) \tilde{H}_d + h.c.
 \end{aligned}$$

- 4 neutralinos $\chi_{1,\dots,4}^0$
- 2 charginos $\chi_{1,2}^\pm$
- Yukawa couplings g_{ij} and Majorana masses $\mu, M_{\tilde{W}}, M_{\tilde{B}}$ are free input parameters

Isospin rotation:

$$H_u = \Phi_2, \quad H_d = -i\sigma_2 \Phi_1^*$$

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$$V(T) = V_{2\text{HDM}}^{(\text{tree})} + V_{CW}^{(1)} + V_T + V_{CT}$$

- tree-level potential of the 2HDM
- one-loop effective potential $V_{CW}^{(1)}$ including effects of V_{inos}
- temperature corrections V_T (incl. V_{inos})
- Counterterm potential V_{CT}
- extended BSMPT [\[Basler et. al\]](#) to include the EW-ino contributions

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Q1:

Can split-SUSY fermions relax tensions in the 2HDM?

Example Point: 2HDM

Idea: start with 2HDM (without EWinos) and then turn-on fermion contributions.

$$\begin{aligned} m_h &= 125.09 \text{ GeV}, & m_H &= 637.37 \text{ GeV}, \\ m_A &= 811.35 \text{ GeV}, & m_{H^\pm} &= 839.90 \text{ GeV}, \\ \tan \beta &= 6.15, & \alpha &= -0.1605, \end{aligned}$$

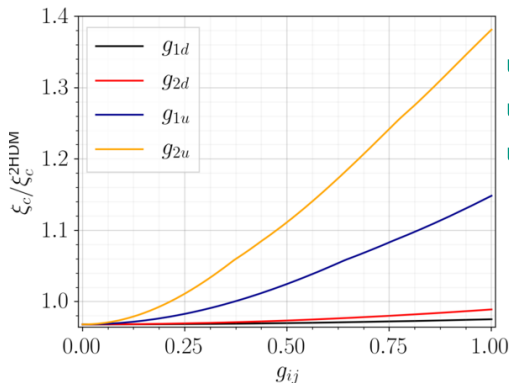
leads to

$$\xi_c^{2\text{HDM}} = 0.82 < 1 \quad \text{⚡}$$

when considering the pure 2HDM type II.

Example Point: 2HDM+EWinos

$$M_{\tilde{W}} = M_{\tilde{B}} = \mu = 250 \text{ GeV}$$

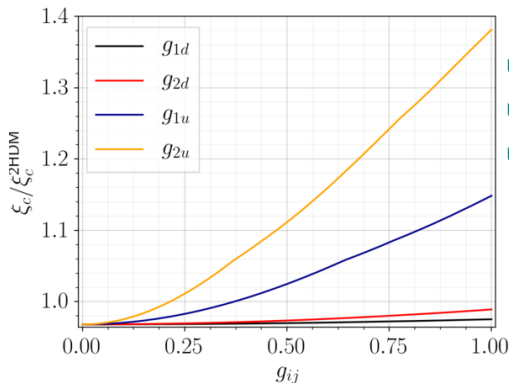


- up to 40% w.r.t. vanilla 2HDM
- up-type Yukawas dominant
- $SU(2)$ Yukawas dominant (more d.o.f)

Backup-slides → general feature of EWinos!

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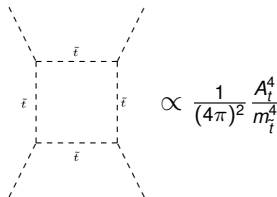
Matching the 2HDM+EWinos to the MSSM

■ MSSM:

- $\lambda_{1,2,3,4} = \mathcal{O}(g_1^2, g_2^2) + \frac{1}{(4\pi)^2} \mathcal{O}\left(\frac{A_t}{m_t}\right)$
- $\lambda_{5,6,7} = 0 + \frac{1}{(4\pi)^2} \mathcal{O}\left(\frac{A_t}{m_t}\right)$
- A_t is a low-scale parameter

■ our scan requires:

$$\lambda_5 > 0.1 \text{ to reach } \xi_c > 1 \quad \zeta$$


$$\propto \frac{1}{(4\pi)^2} \frac{A_t^4}{m_t^4}$$

alternatives:

- add light singlet (split-NMSSM) [\[Demidov et. al\]](#) [\[Athron et. al\]](#)
→ singlet couplings enable SFOEWPT
- integrate out heavy singlet
NMSSM → MSSM → 2HDM+EWinos

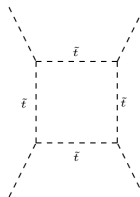
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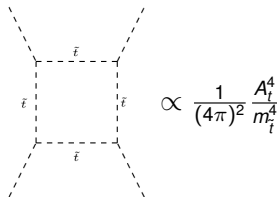
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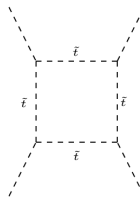
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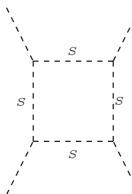
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Summary:

- studied impact on EWPT of additional fermions in a 2HDM
- $SU(2)$ doublets/triplets beneficial *i.e.* strengthen the EWPT
- re-opens parameter space which is forbidden in the default 2HDM
- not possible to be embedded in minimal split-MSSM
→ requires at least an NMSSM with heavy singlet

Outlook:

- study impact in non-minimal SUSY
- impact on collider/flavour phenomenology

Backup

Global View: reopen parameter space with large masses

- random parameter scan using **Scanners** [Coimbra et al.]
- scan with default 2HDM allowing for all ξ_C
- re-evaluate using
2HDM+EWinos:
 - $g_{1u} = g_{1d} = g_1^{\text{SM}}$
 - $g_{2u} = g_{2d} = g_2^{\text{SM}}$
 - $M_B = M_W = \mu = 200 \text{ GeV}$
- compare ξ_C with $\xi_C^{2\text{HDM}}$

- large-mass points
which were forbidden
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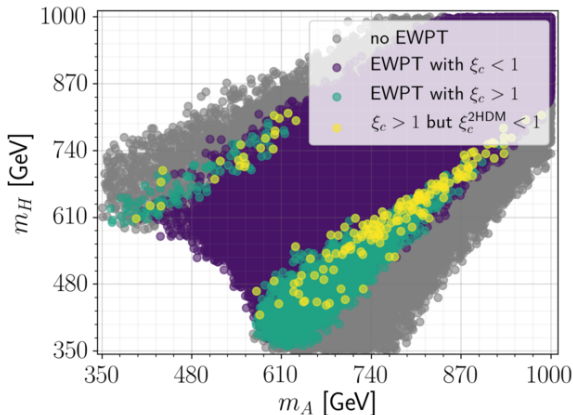
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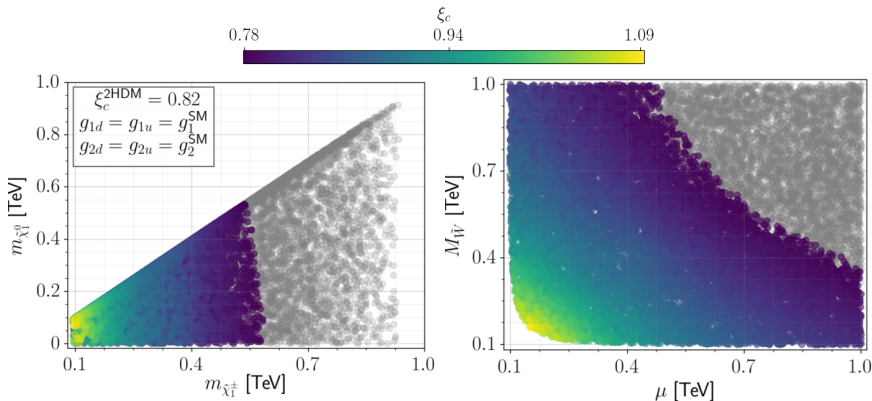
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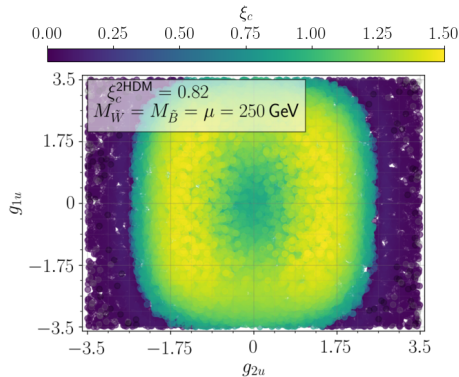
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 $\mu, m_{\tilde{B}}, m_{\tilde{W}}$ varied independently



$\mu, m_{\tilde{B}}, m_{\tilde{W}}$ fix
 g_{ij} varied independently

$$V(T) = V_{2\text{HDM}}^{(\text{tree})} + V_{\text{CW}}^{(1)} + V_T + V_{\text{CT}}$$

- extended to incorporate corrections from fermions in arbitrary model
 - $V_{\text{CW}}^{(1)}|_{\text{inos}}$
 - $V_T|_{\text{inos}} = -\frac{T^4}{\pi^2} \text{Tr} \left[J_+ \left(\mathbf{m}_{\tilde{\chi}_i^0}^2 / T^2 \right) + 2J_+ \left(\mathbf{m}_{\tilde{\chi}_i^-}^2 / T^2 \right) \right] + V_{\text{Debye}}|_{\text{inos}}$
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- calculates all ingredients for $V(T)$
- V_{CT} : achieves equal scalar tree-level and one-loop masses/mixings
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