

# The Standard Model Quiver in de Sitter String Compactifications



Figure credits: Getty Images

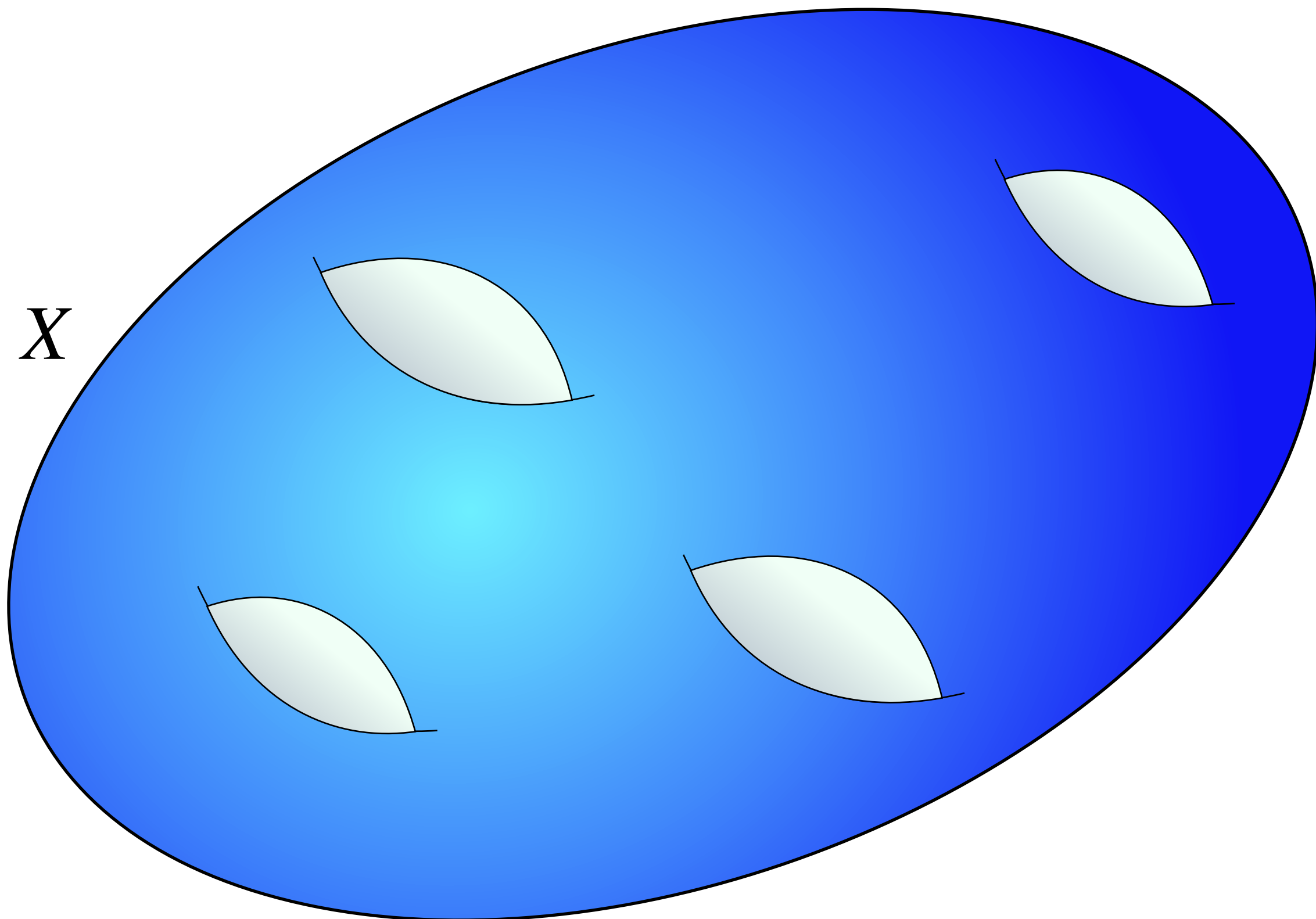


Department of Applied Mathematics  
and Theoretical Physics  
University of Cambridge

in collaboration with M. Cicoli, I. García Etxebarria, F. Quevedo, P. Shukla and R. Valandro

JHEP 08(2021)109 ArXiv: 2106.11964

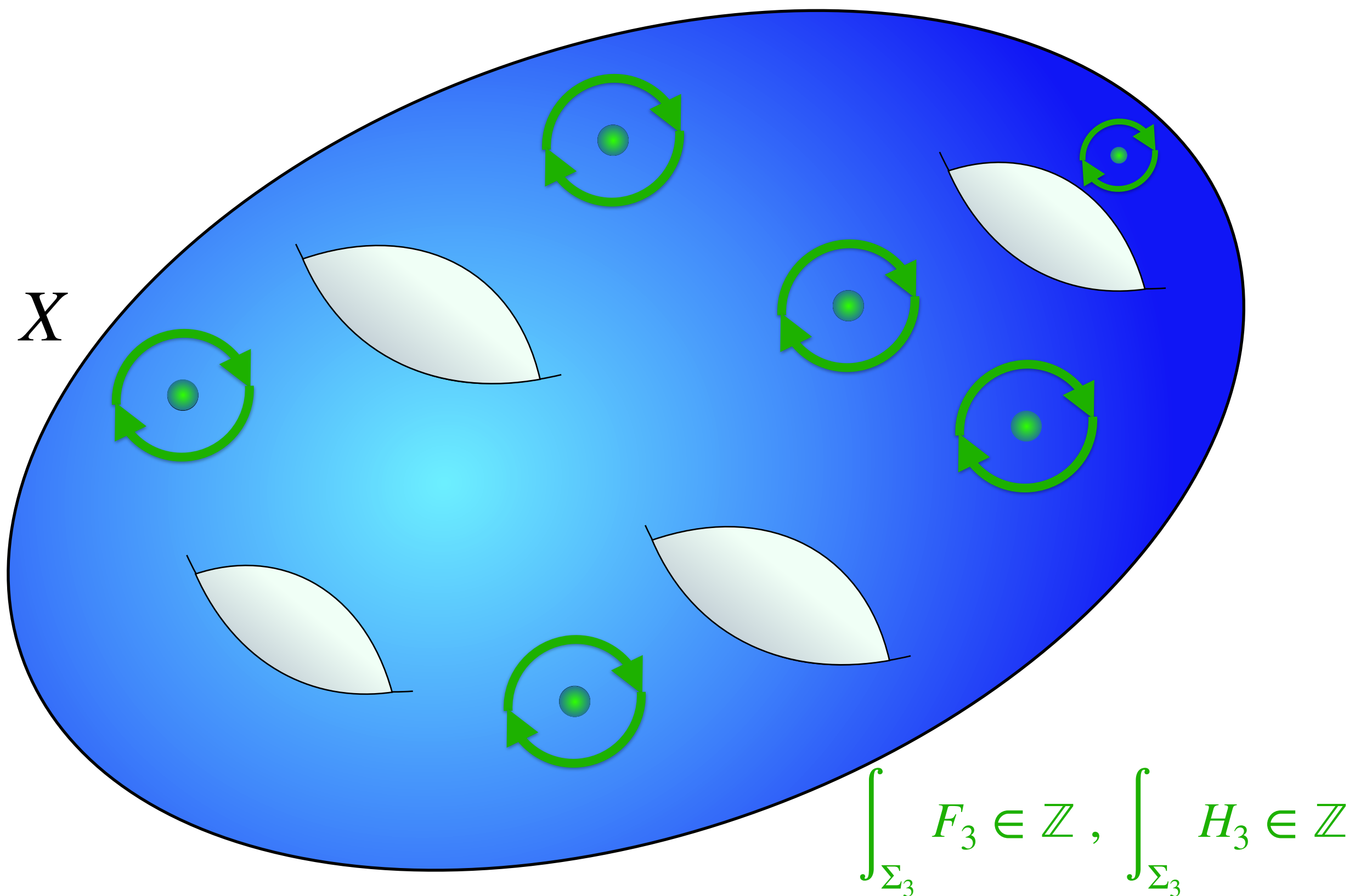
# Aspects of Type IIB Model Building



## Global aspects:

- Compact Calabi-Yau manifold  $X$

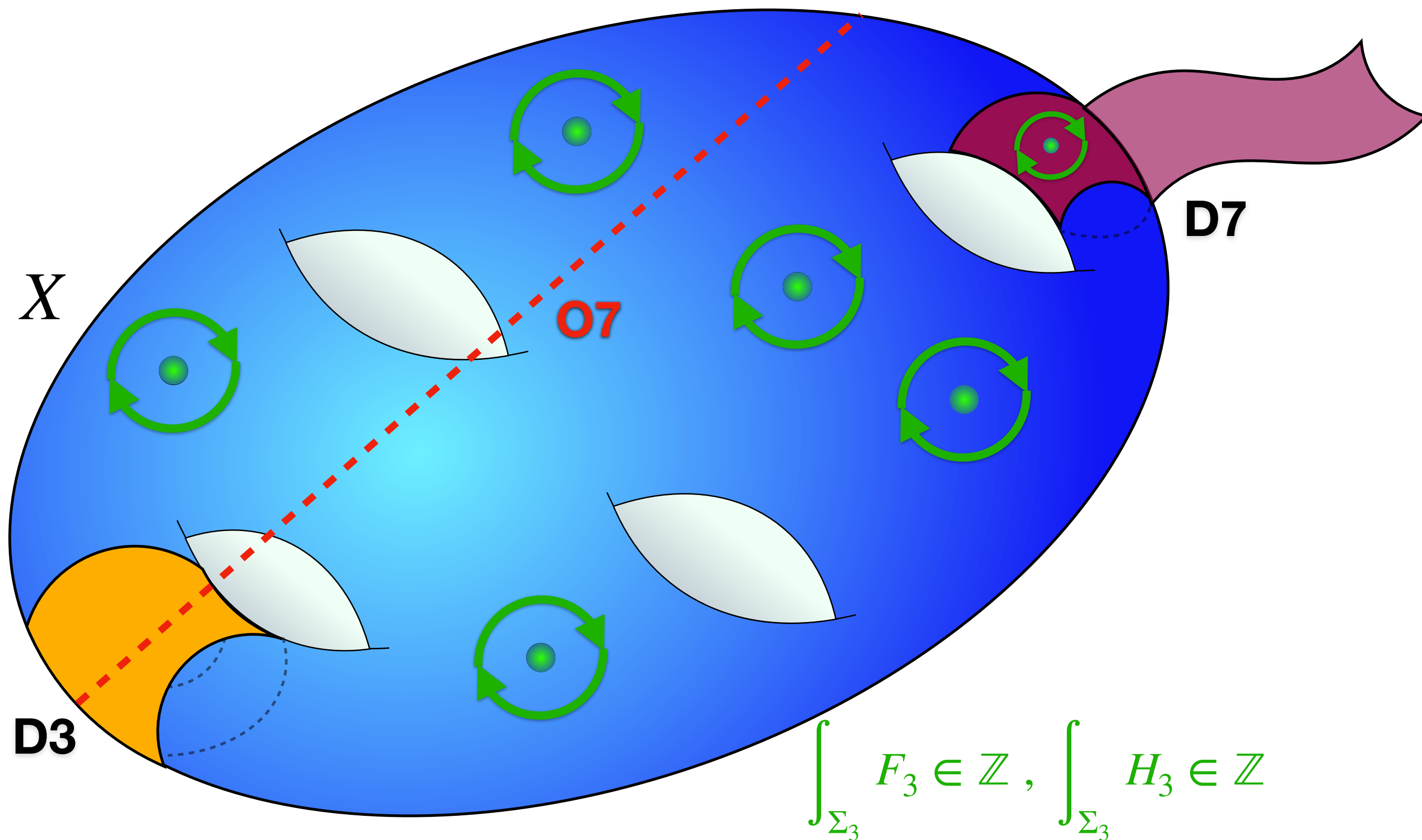
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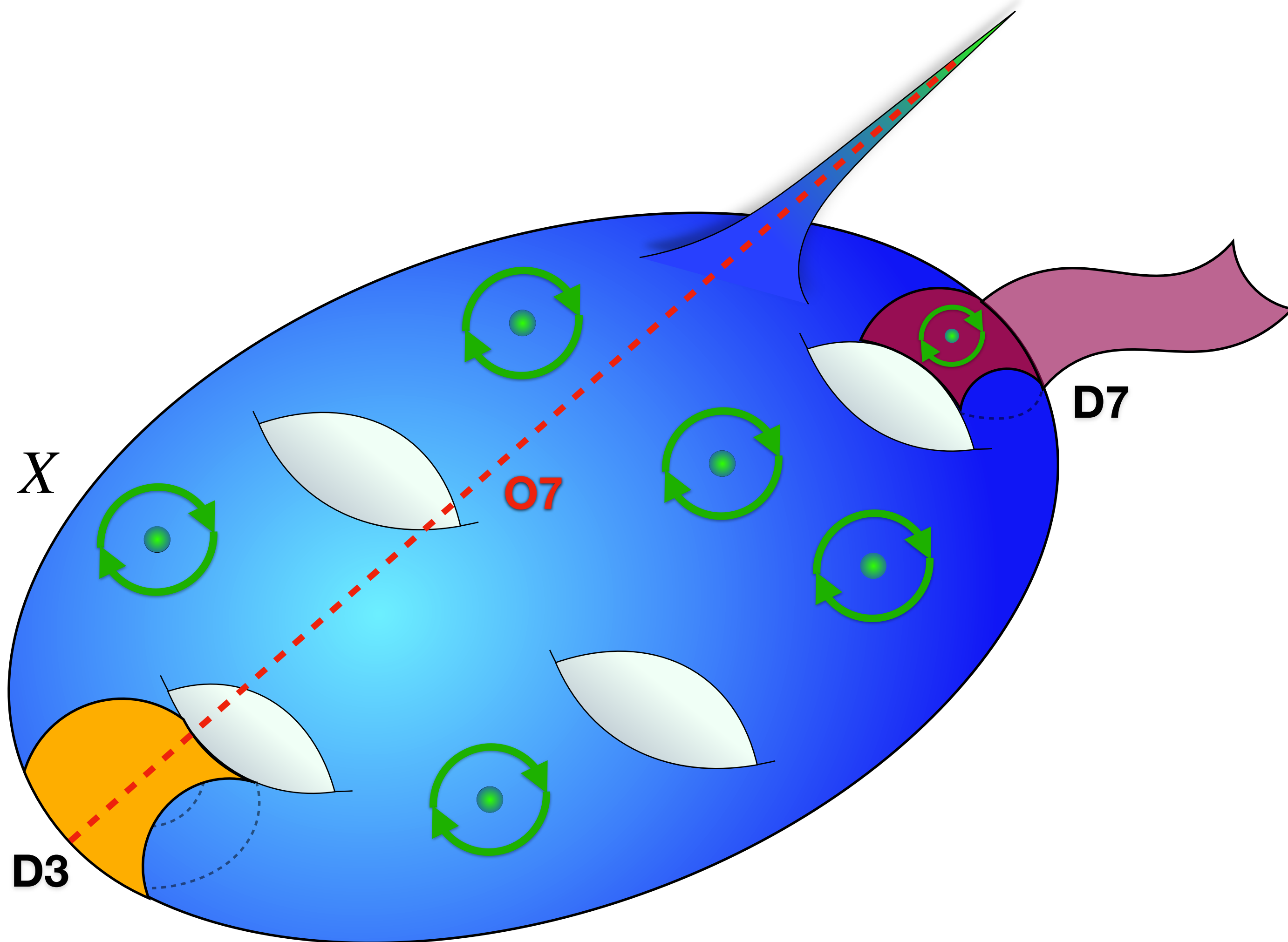
# Aspects of Type IIB Model Building



## Global aspects:

- Compact Calabi-Yau manifold  $X$
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- D-brane and O-plane configuration
- Tadpole cancellation
- Moduli stabilisation in de Sitter minima
- ...

# Aspects of Type IIB Model Building



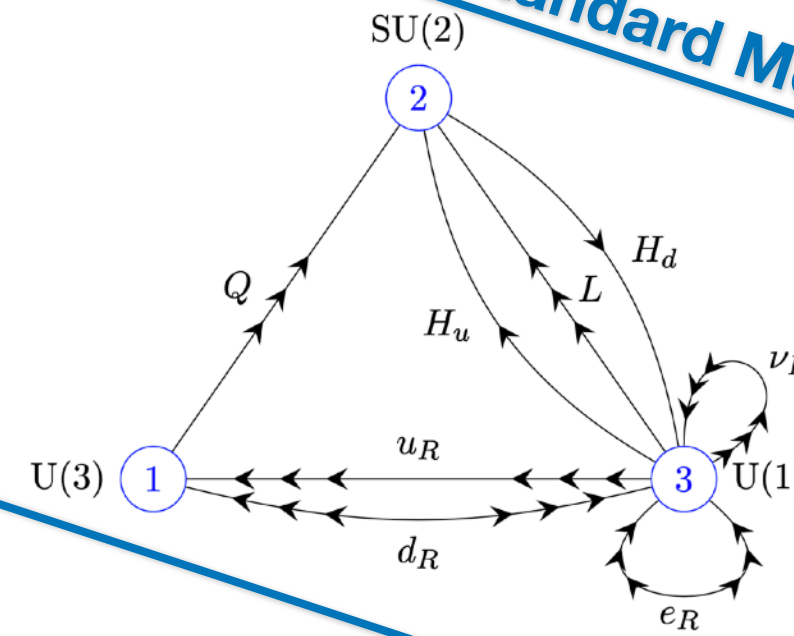
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## Local model building:

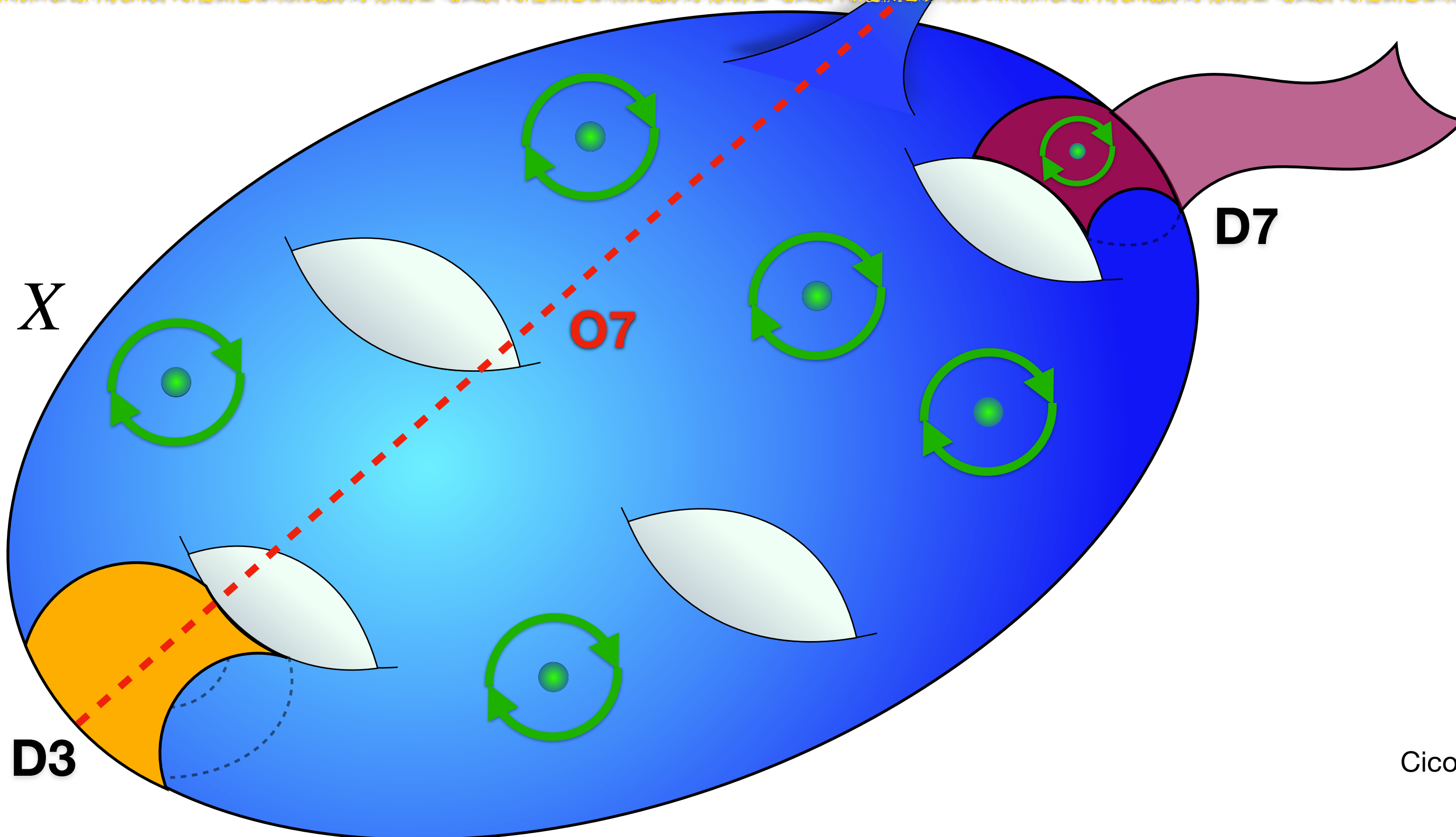
- Choice of singularity
- Standard Model gauge group
- Spectrum of 3 chiral families
- Non-chiral matter
- Global anomalous U(1)'s
- Hierarchies in Yukawas
- ...

## Minimal Quiver Standard Model



Berenstein, Pinansky:  
hep-th/0610104

**D3**



## Global aspects:

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## Previous global constructions:

Dolan, Krippendorf, Maharana, Quevedo: 1002.1790

Dolan, Krippendorf, Quevedo: 1106.6039

Cicoli, Krippendorf, Mayrhofer, Quevedo, Valandro: 1206.5237, 1304.0022, 1304.2771

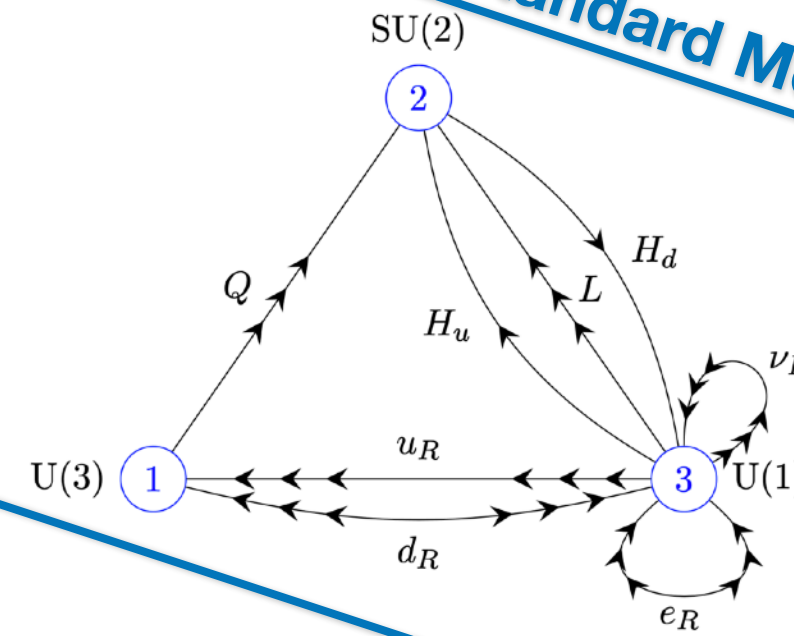
Cicoli, Klevers, Krippendorf, Mayrhofer, Quevedo, Valandro: 1312.0014

Cicoli, García Etxebarria, Mayrhofer, Quevedo, Shukla, Valandro: 1706.06128

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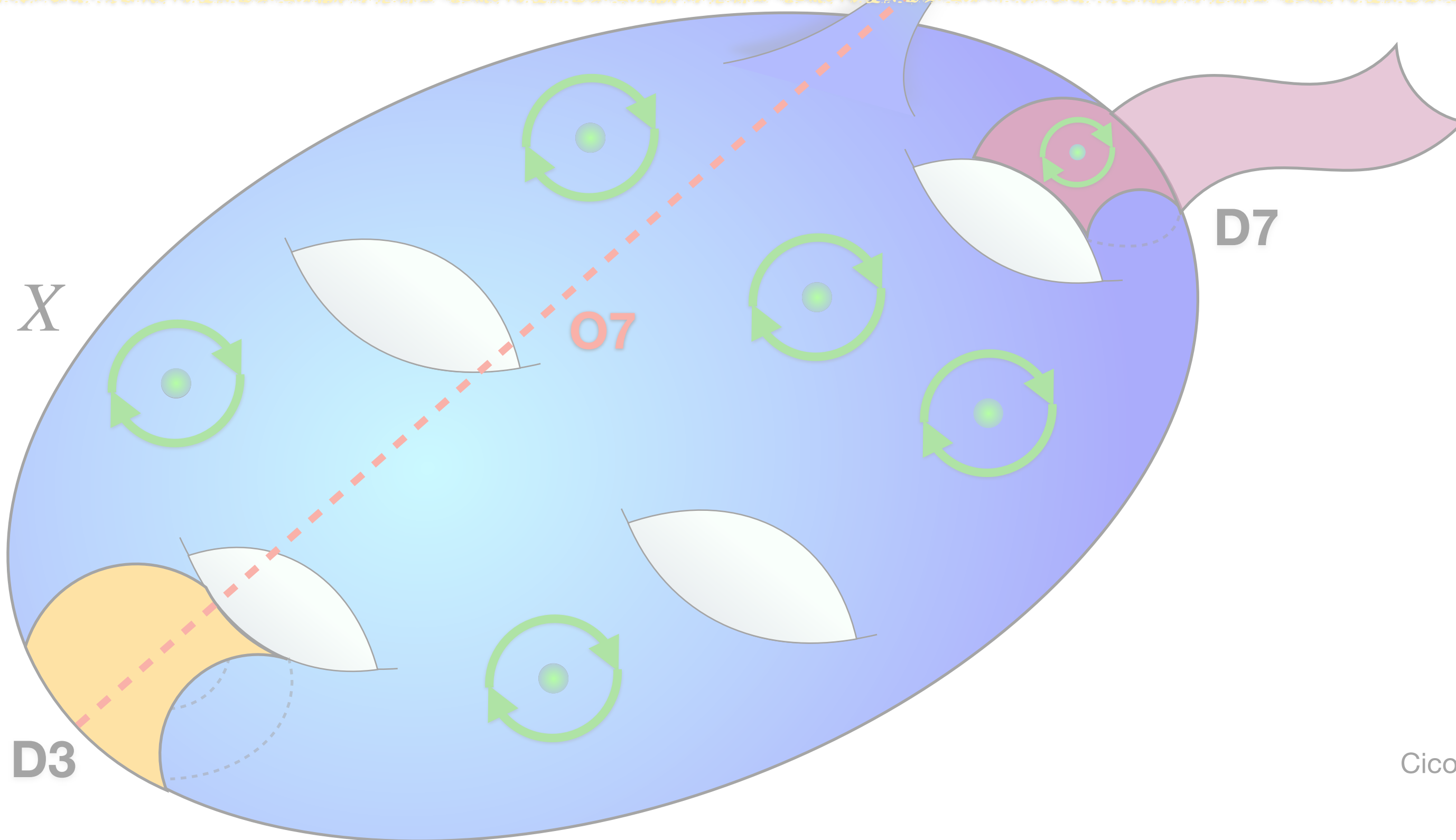
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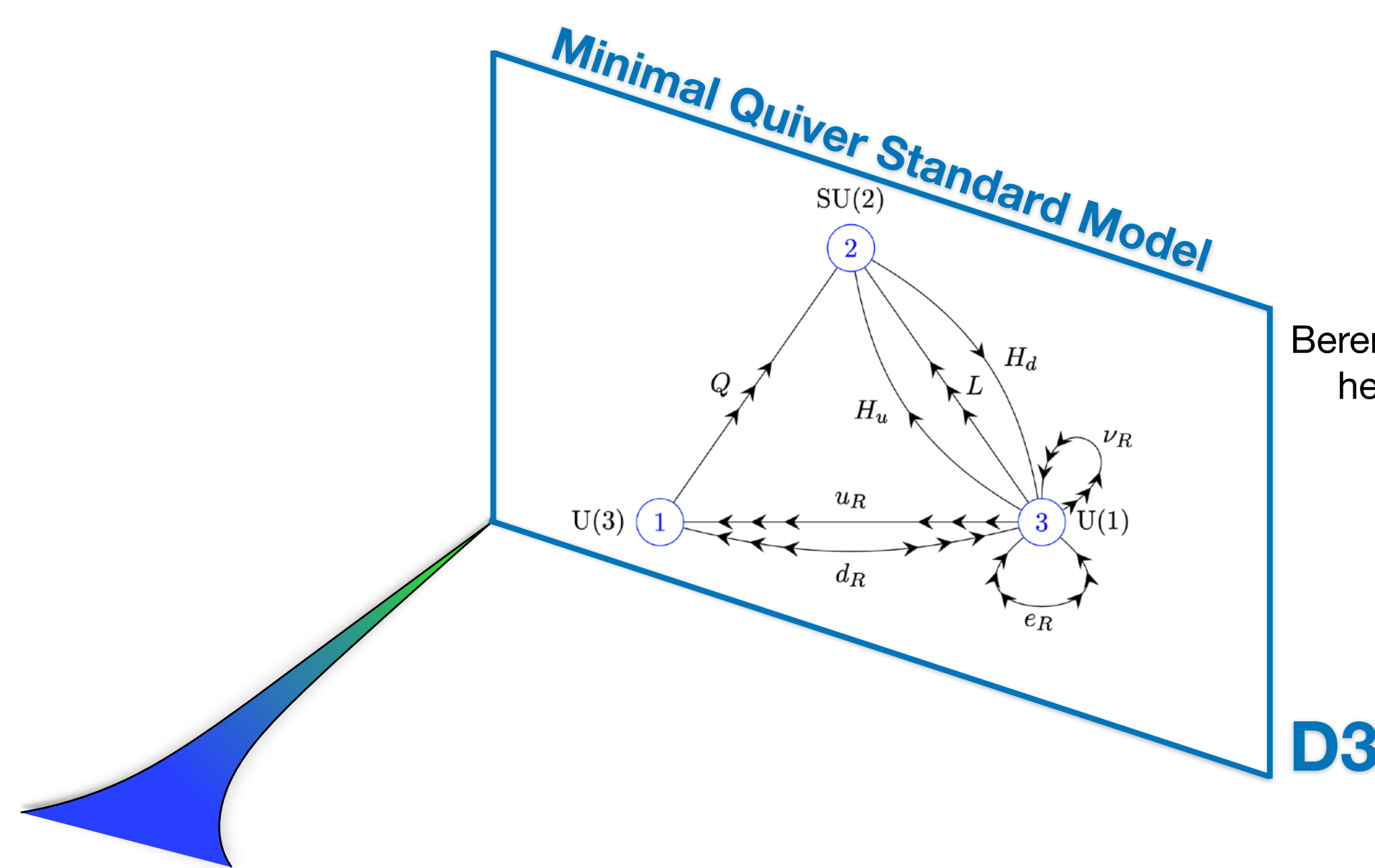
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## What type of singularity?

### del Pezzo surfaces:

Complex 2-dimensional Fano surfaces, i.e., projective algebraic surfaces with ample anti-canonical divisor class  $-K \cdot C > 0$  for every curve  $C$ . We distinguish  $\mathbb{P}^1 \times \mathbb{P}^1$  or  $dP_n$  corresponding to  $\mathbb{P}^2$  blown up at  $n$  points.

### Attractive features of D-branes at $dP_n$ singularities:

- Huge variety of gauge theories from a single D3 brane
- Oriented quiver always comes with 2 anomalous  $U(1)$ 's
- Chiral spectrum from intersections of 2- and 4-cycles

To a point shrinkable 4-cycle must be of del Pezzo type by **Grauter's criterion**

### Today:

$dP_5$  singularity as simplest setup to give rise to exact MSSM locally!

Wijnholt: hep-th/0703047

See e.g. Cordova: 0910.2955  
Malyshev, Verlinde:0711.2451



# Unoriented quivers from D3-branes at $dP_5$ singularities

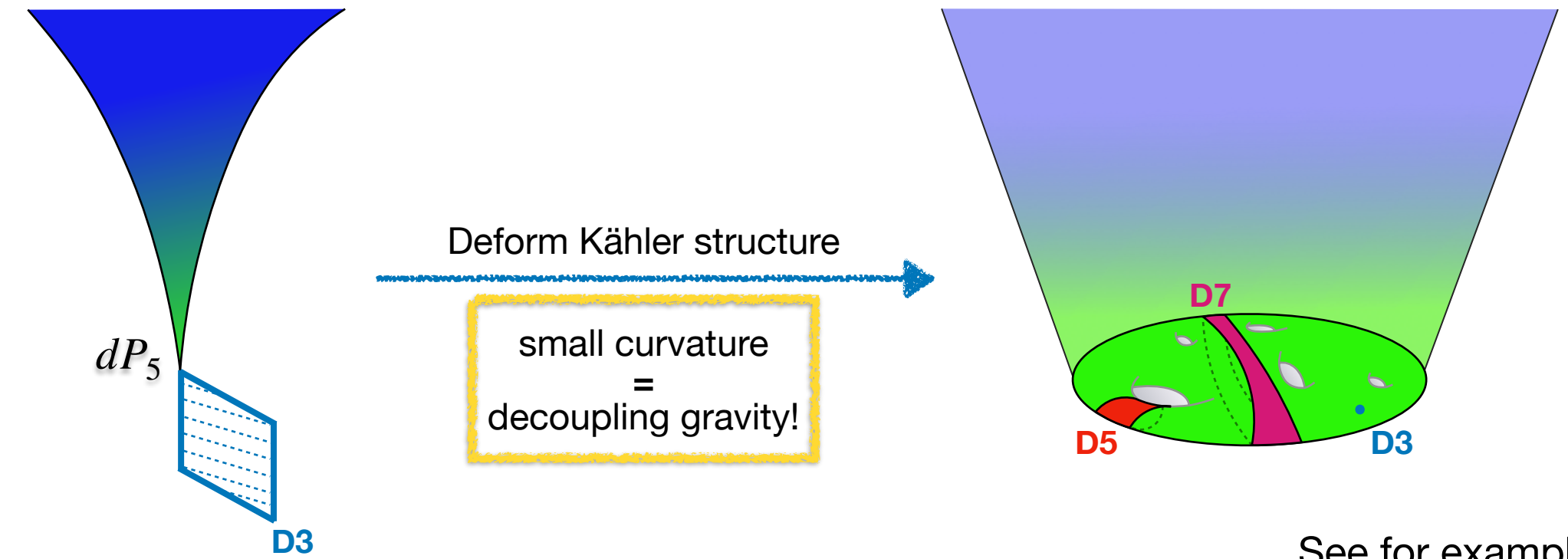
**Fractional branes  $F_i$  :**  
Bound states of several  
D-branes supported on cycles

Spectrum of open strings from **quiver diagrams:**

$U(N_i)$   $\textcircled{i}$   $\longleftrightarrow$   $N_i$  copies of a fractional brane  $F_i$

$U(N_i)$   $\textcircled{i}$   $\longrightarrow$   $\textcircled{j}$   $U(N_j)$   $\longleftrightarrow$  Chiral multiplet in bi-fundamental of  $U(N_i) \times U(N_j)$

Geometric description of local model in the large volume limit:



See for example:  
Wijnholt: hep-th/0212021  
Verlinde, Wijnholt: hep-th/0508089

# Unoriented quivers from D3-branes at $dP_5$ singularities

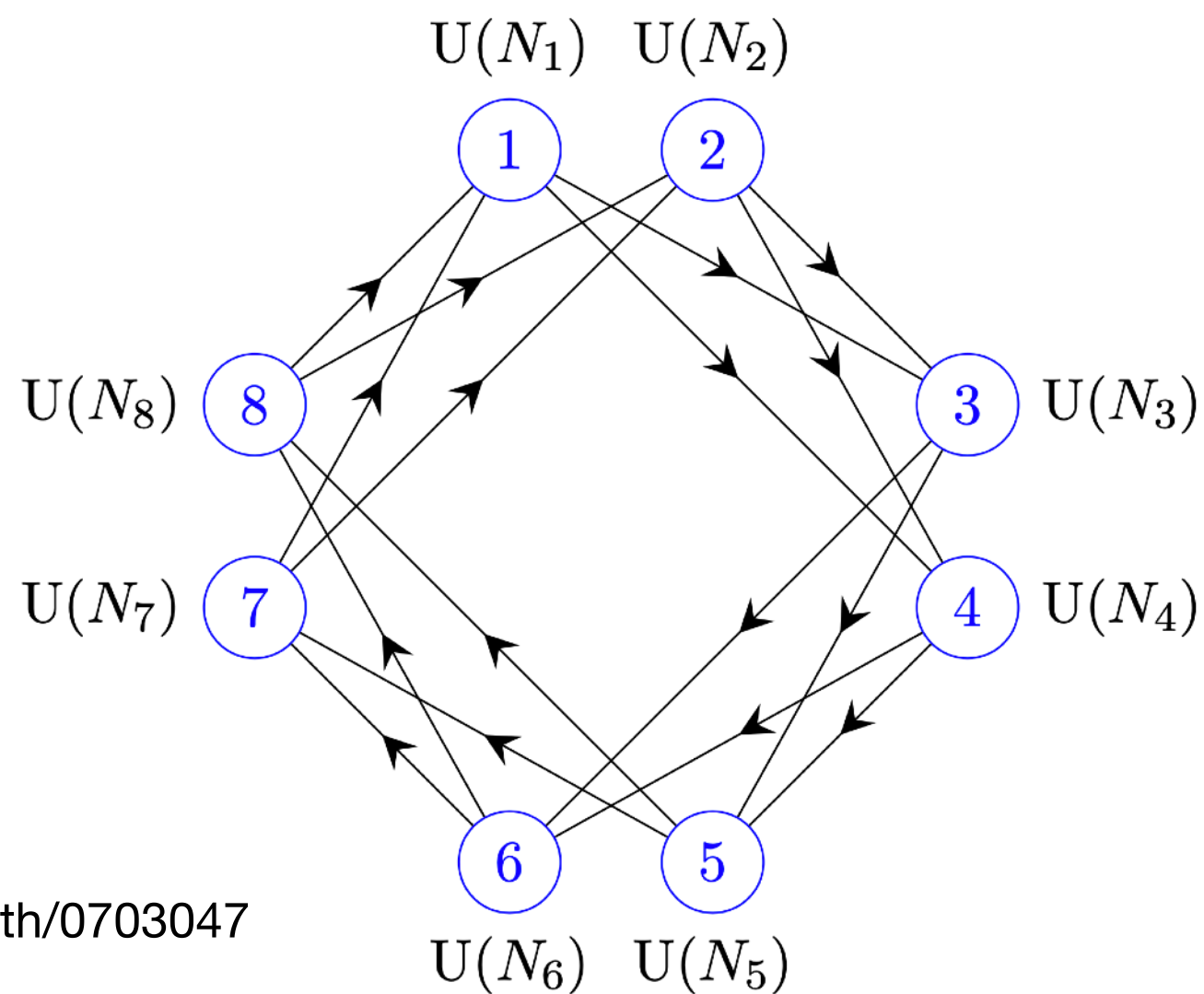
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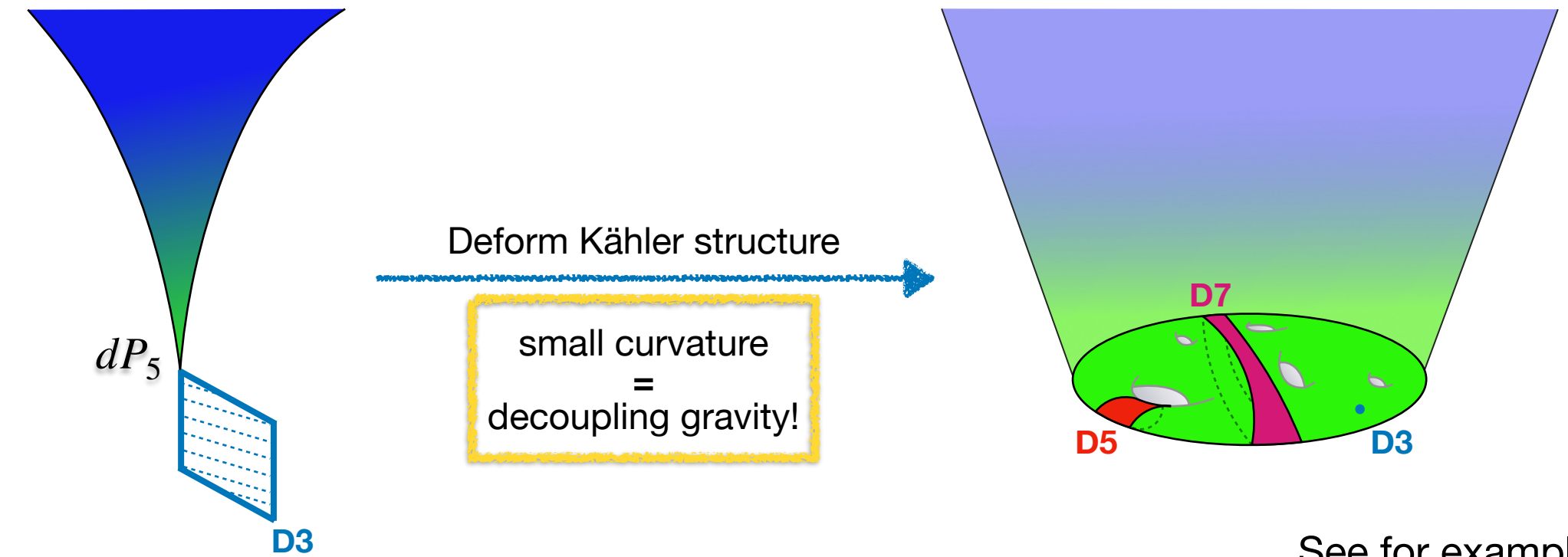
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**$dP_5$  quiver diagram:**



Wijnholt: hep-th/0703047

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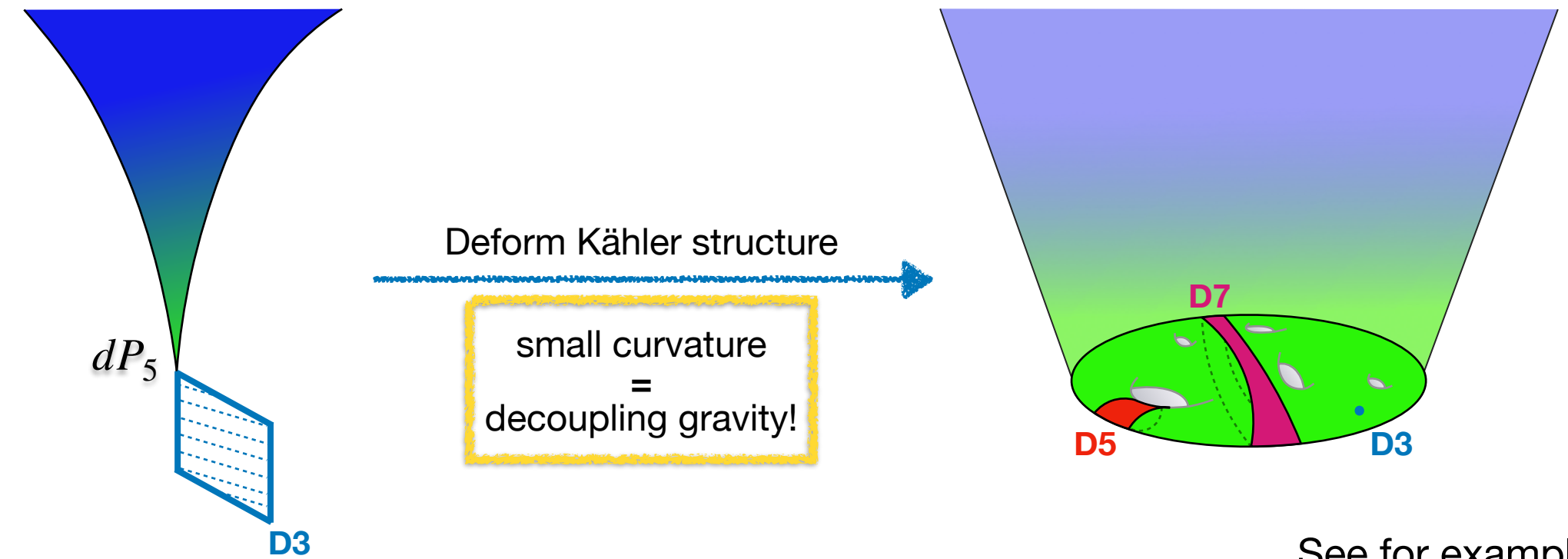
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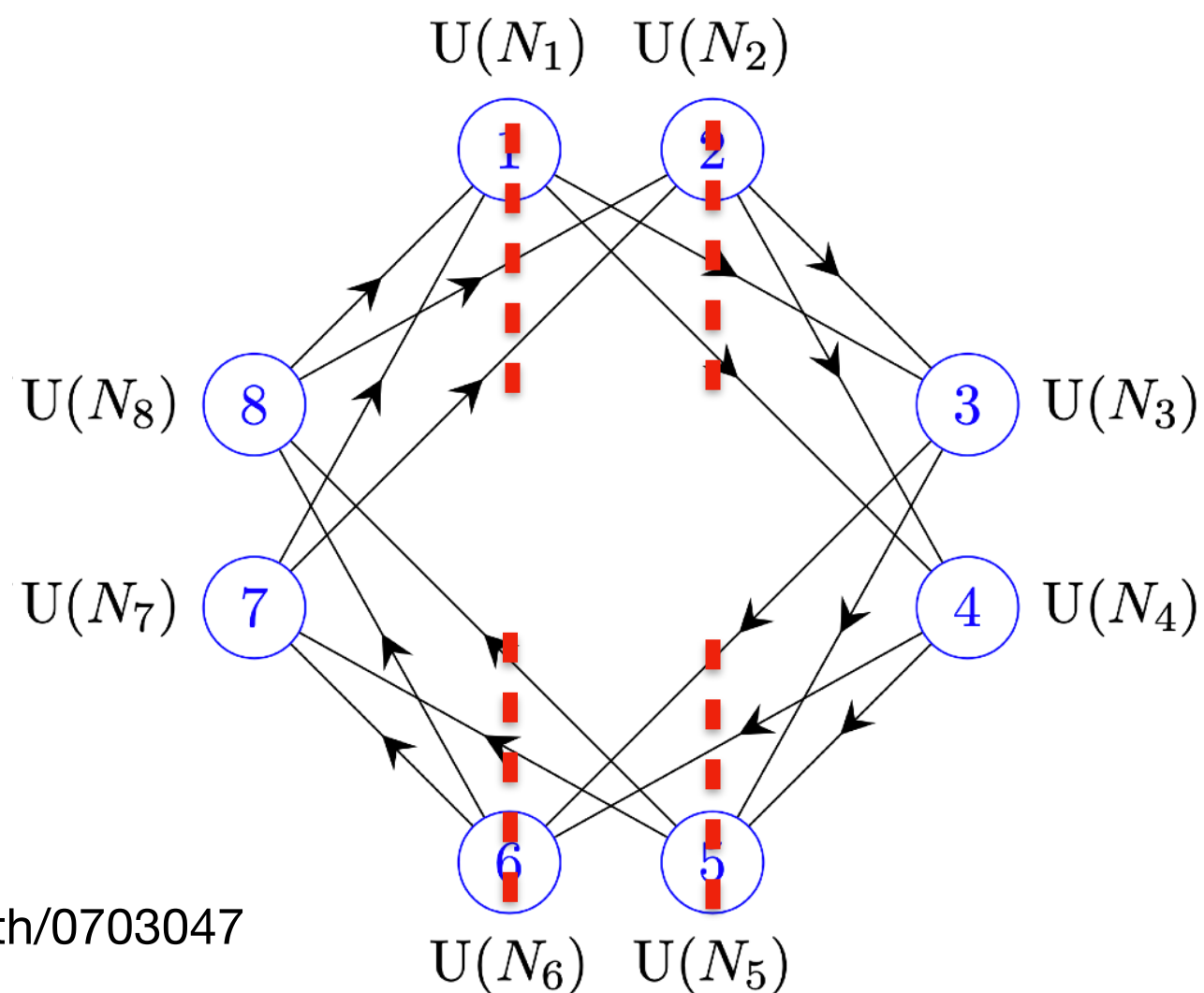
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**Geometric description of local model in the large volume limit:**



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**$dP_5$  quiver diagram:**



Wijnholt: hep-th/0703047

**Orientifold involution:**

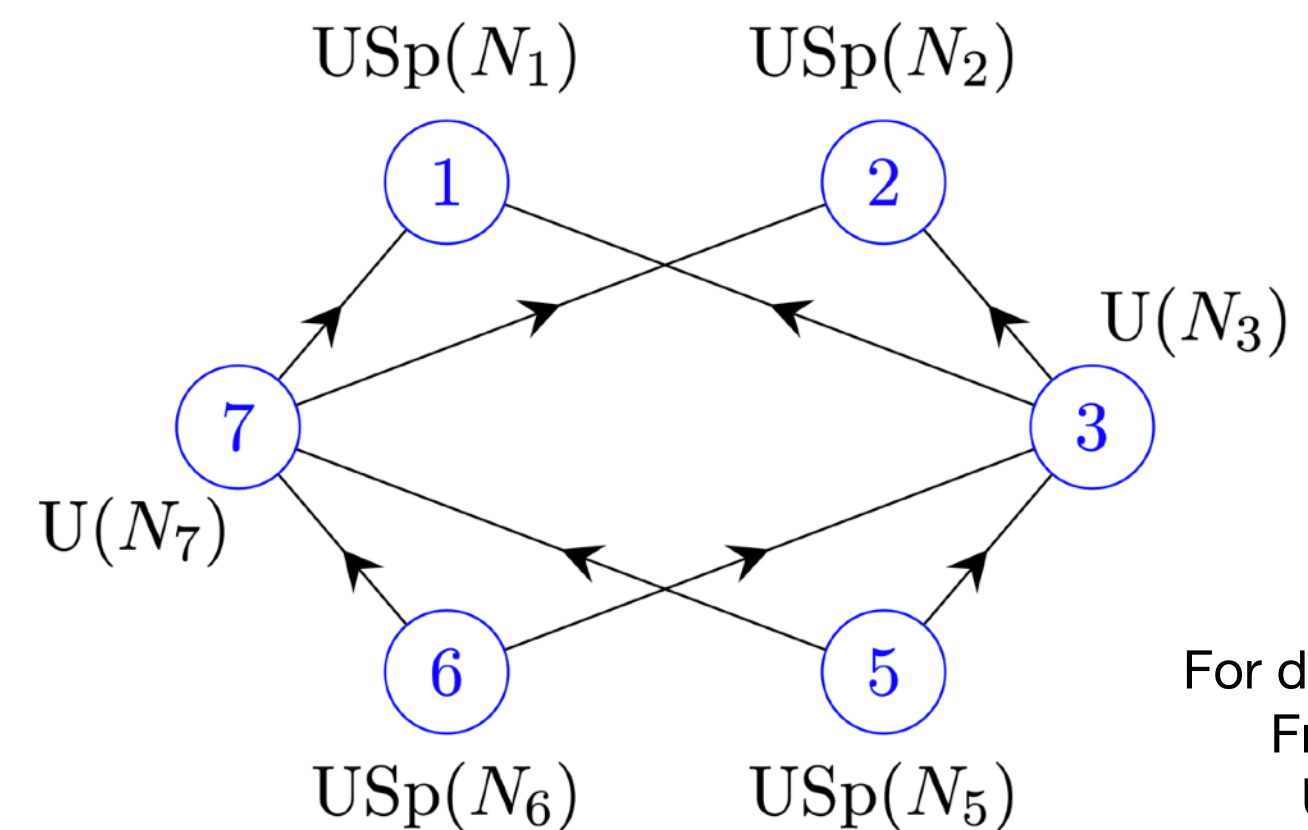
$1 \leftrightarrow 1^*$ ,  $2 \leftrightarrow 2^*$ ,  $3 \leftrightarrow 8^*$

$4 \leftrightarrow 7^*$ ,  $5 \leftrightarrow 5^*$ ,  $6 \leftrightarrow 6^*$

**The Standard Model quiver itself is unoriented!**

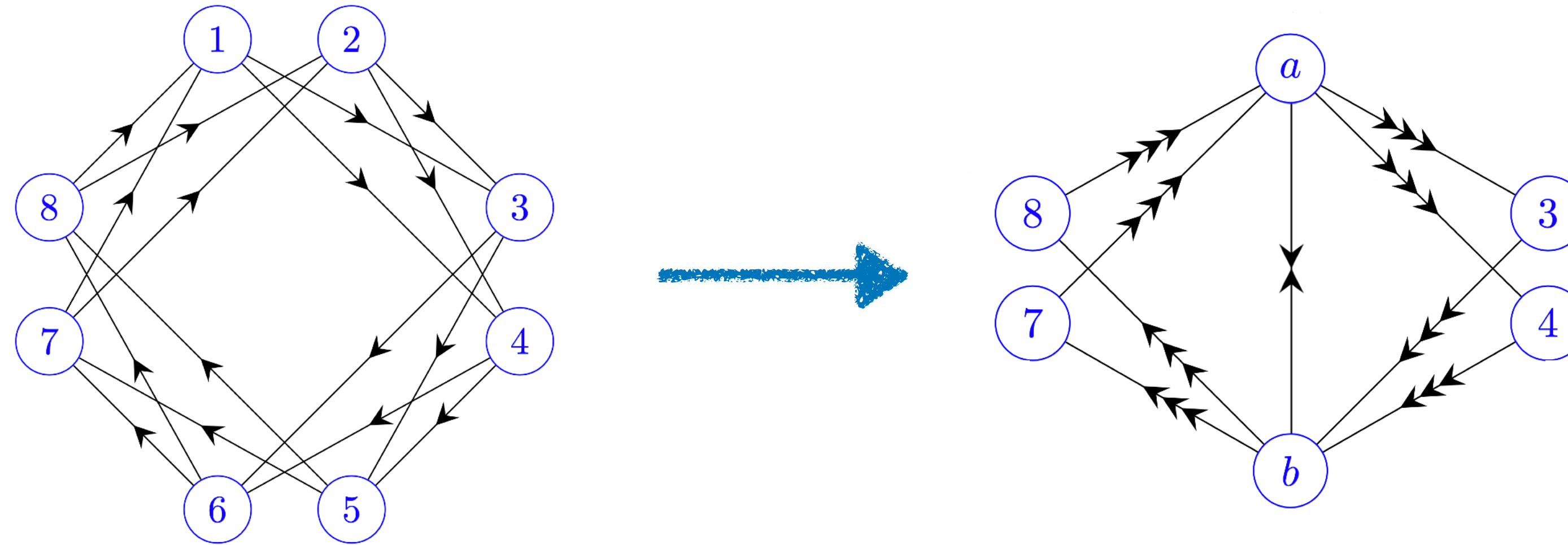
Berenstein, Pinansky: hep-th/0610104

**Orientifolded  $dP_5$  quiver diagram:**



For details on orientifolded quivers:  
Franco, Hanany, Krefl, Park,  
Uranga, Vegh: 0707.0298  
García Etxebarria, Heidenreich,  
Wrase: 1210.7799

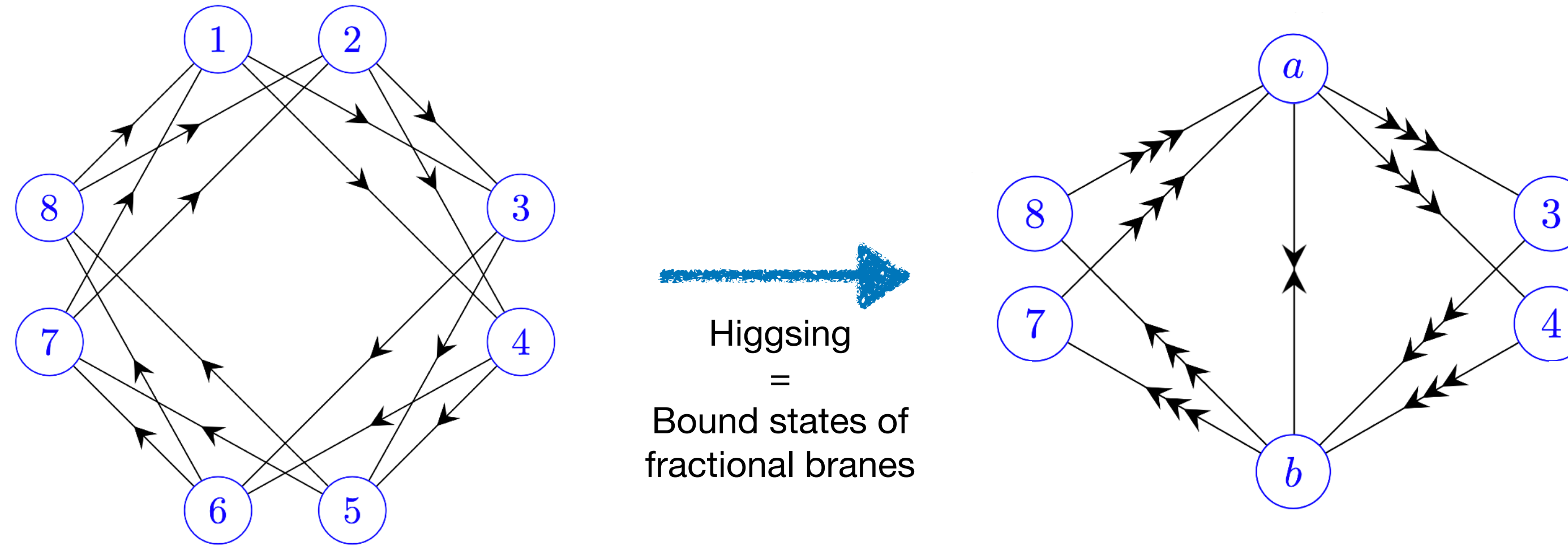
# Higgsing the $dP_5$ quiver gauge theory



## Missing features:

- A. Chiral spectrum with 3 families
- B. Standard Model gauge group
- C. Non-chiral matter

# Higgsing the $dP_5$ quiver gauge theory



## Missing features:

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All of the above is achieved by **turning on VEVs for bi-fundamental fields!**

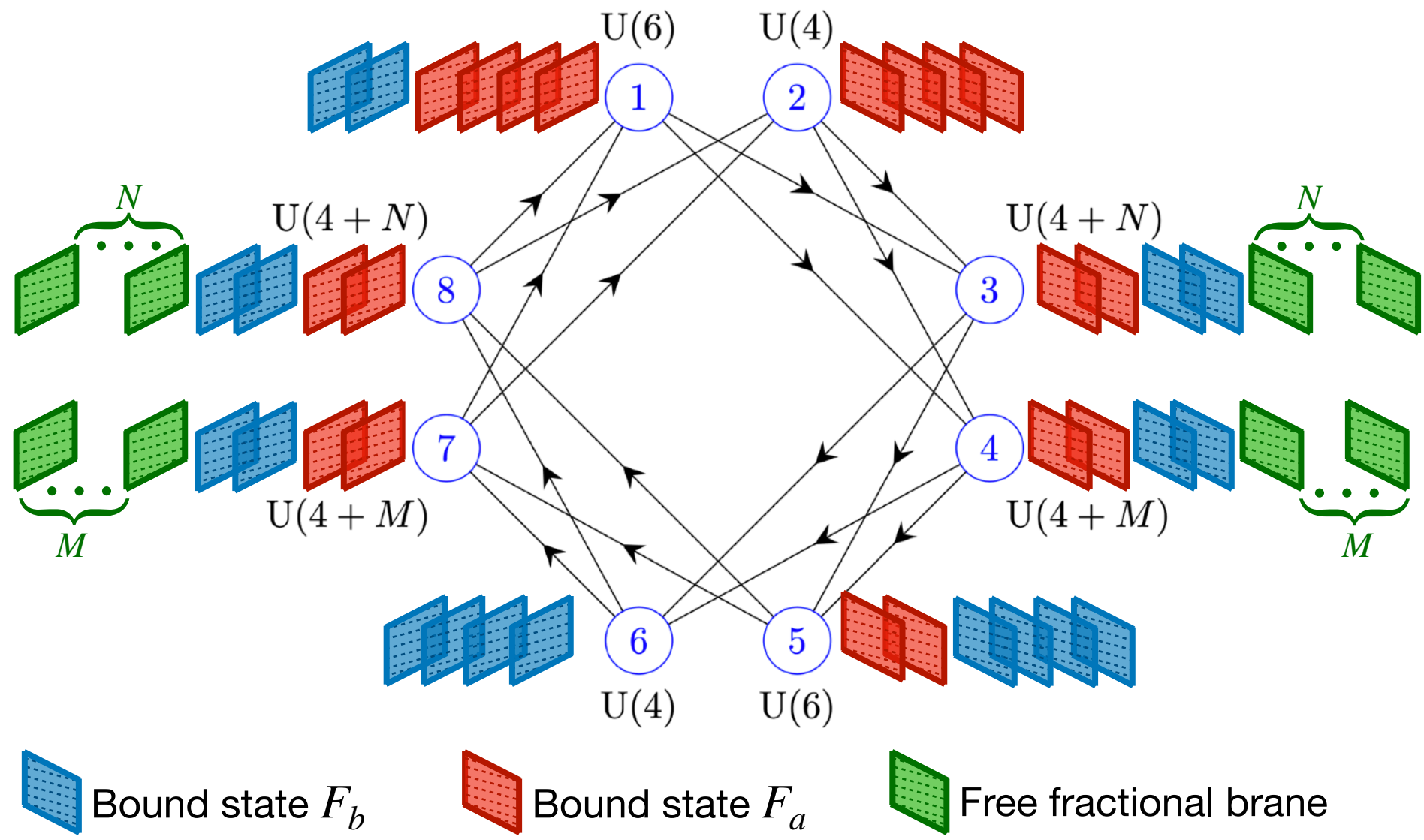
## Interpretation:

- **Fractional brane perspective:** bound states of fractional branes

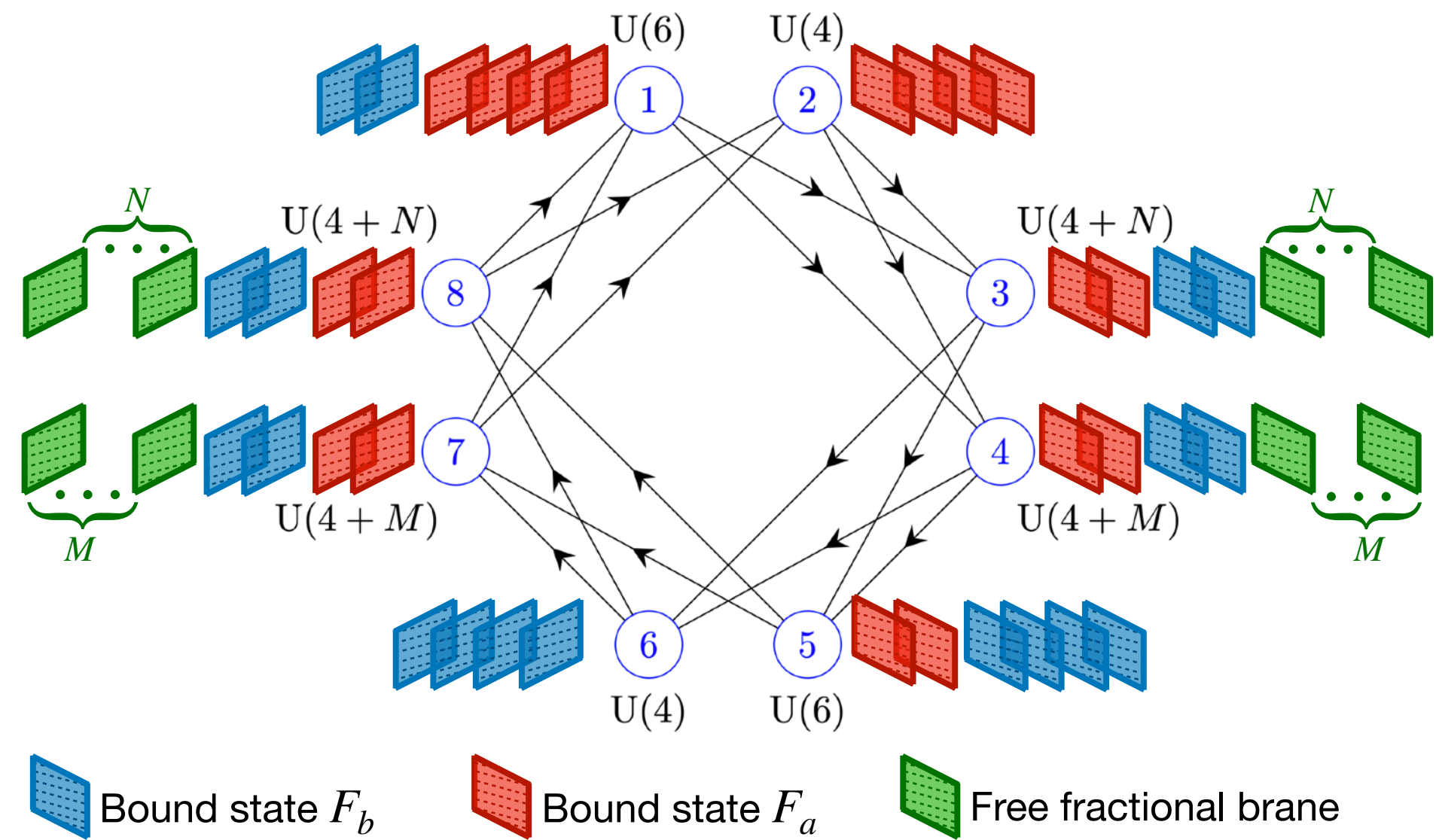
$$\{F_1, \dots, F_8\} \rightarrow \{F_a, F_3, F_4, F_b, F_7, F_8\}$$

- **Geometrically:** partial resolution of singularity

# Original quiver



### Original quiver



### Turn on VEVs:

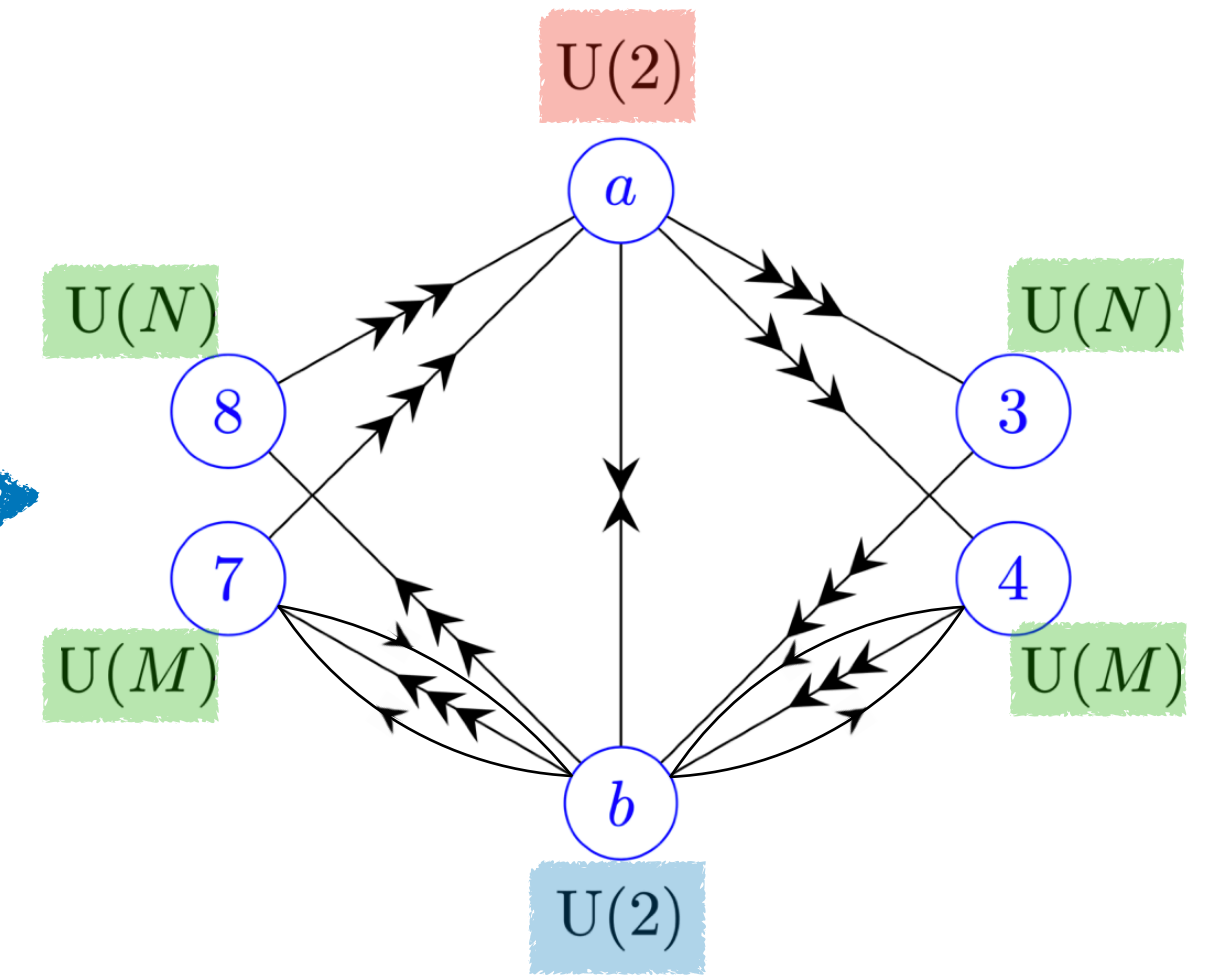
$$\langle X_{13} \rangle = \begin{pmatrix} a_1 & 0 & \dots \\ 0 & a_2 & \dots \\ 0 & a_3 & \dots \end{pmatrix}, \quad \langle X_{14} \rangle = \begin{pmatrix} b_1 & 0 & \dots \\ 0 & b_2 & \dots \\ 0 & b_3 & \dots \end{pmatrix},$$

$$\langle X_{23} \rangle = \begin{pmatrix} 0 & c_1 & \dots \\ 0 & c_2 & \dots \end{pmatrix}, \quad \langle X_{24} \rangle = \begin{pmatrix} 0 & d_1 & \dots \\ 0 & d_2 & \dots \end{pmatrix},$$

$$\langle X_{35}^T \rangle = \begin{pmatrix} x_1 & 0 & \dots \\ x_2 & 0 & \dots \\ 0 & x_3 & \dots \end{pmatrix}, \quad \langle X_{45}^T \rangle = \begin{pmatrix} z_1 & 0 & \dots \\ z_2 & 0 & \dots \\ 0 & z_3 & \dots \end{pmatrix},$$

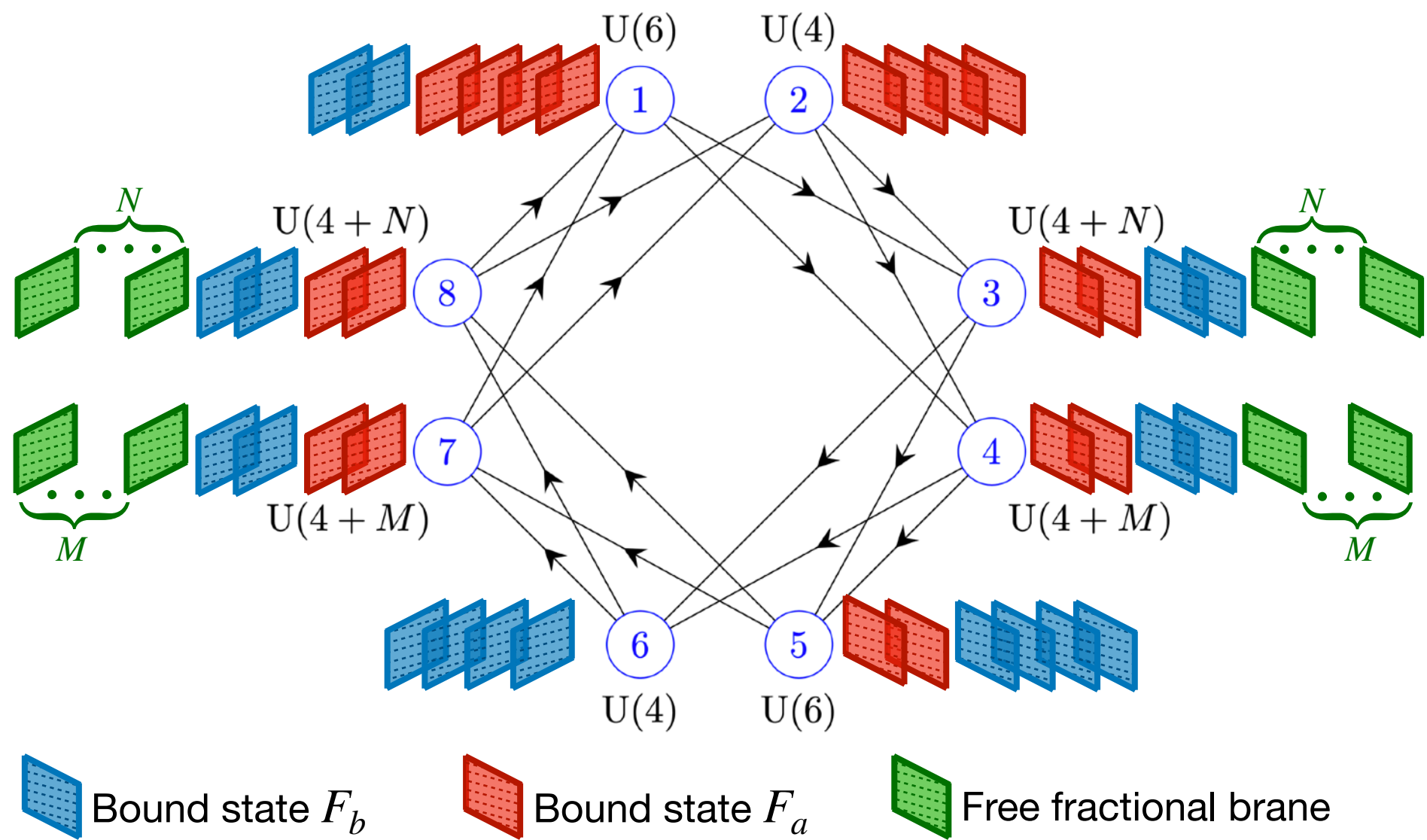
$$\langle X_{36}^T \rangle = \begin{pmatrix} y_1 & 0 & \dots \\ y_2 & 0 & \dots \end{pmatrix}, \quad \langle X_{46}^T \rangle = \begin{pmatrix} w_1 & 0 & \dots \\ w_2 & 0 & \dots \end{pmatrix}$$

### Higgsed quiver



$G = (\text{U}(6) \times \text{U}(4 + N) \times \text{U}(4 + M) \times \text{U}(4))^2 \rightarrow H = (\text{U}(2) \times \text{U}(N) \times \text{U}(M))^2$   
 Breaking pattern confirmed by computing mass matrix for gauge bosons!

### Original quiver



### Turn on VEVs:

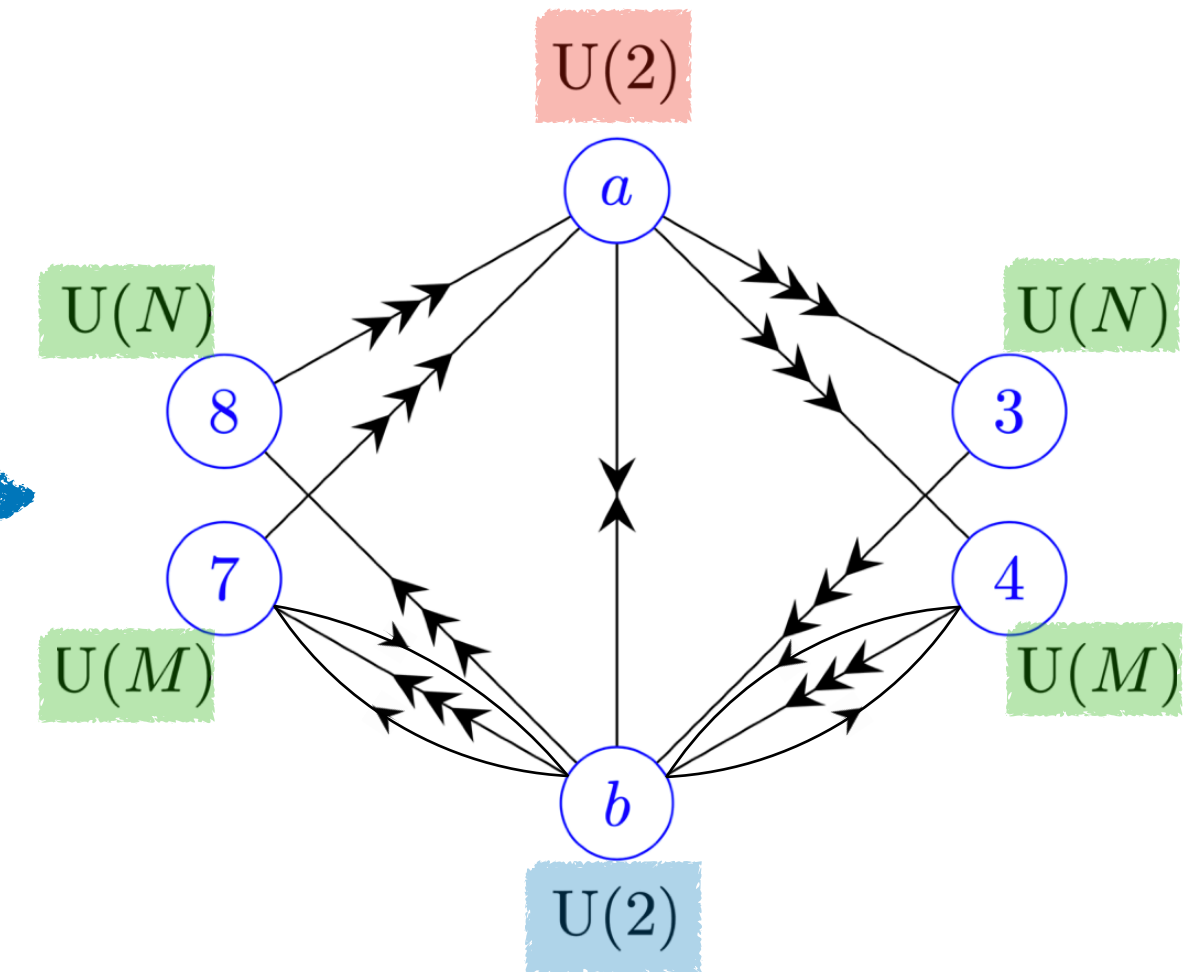
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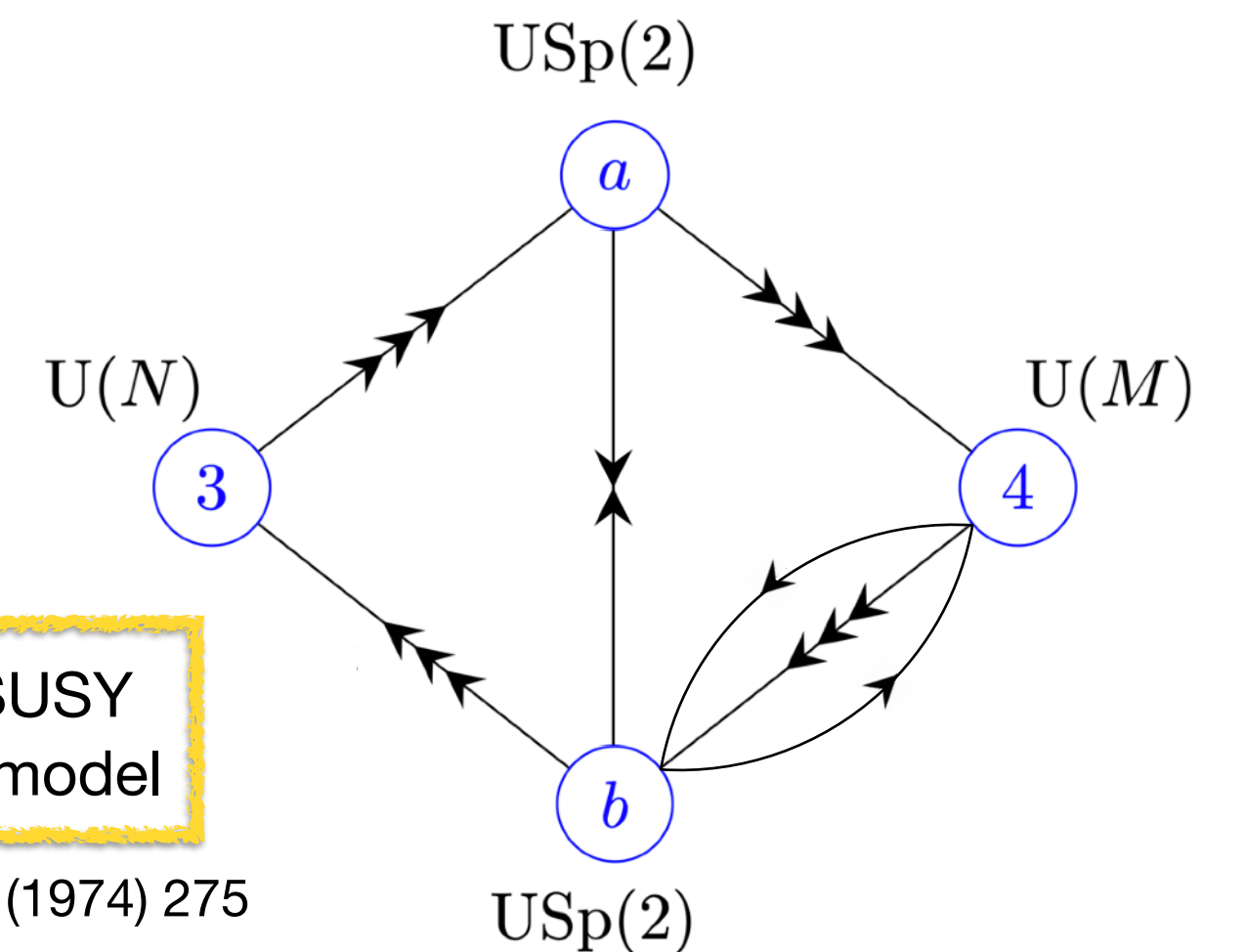
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Breaking pattern confirmed by computing mass matrix for gauge bosons!

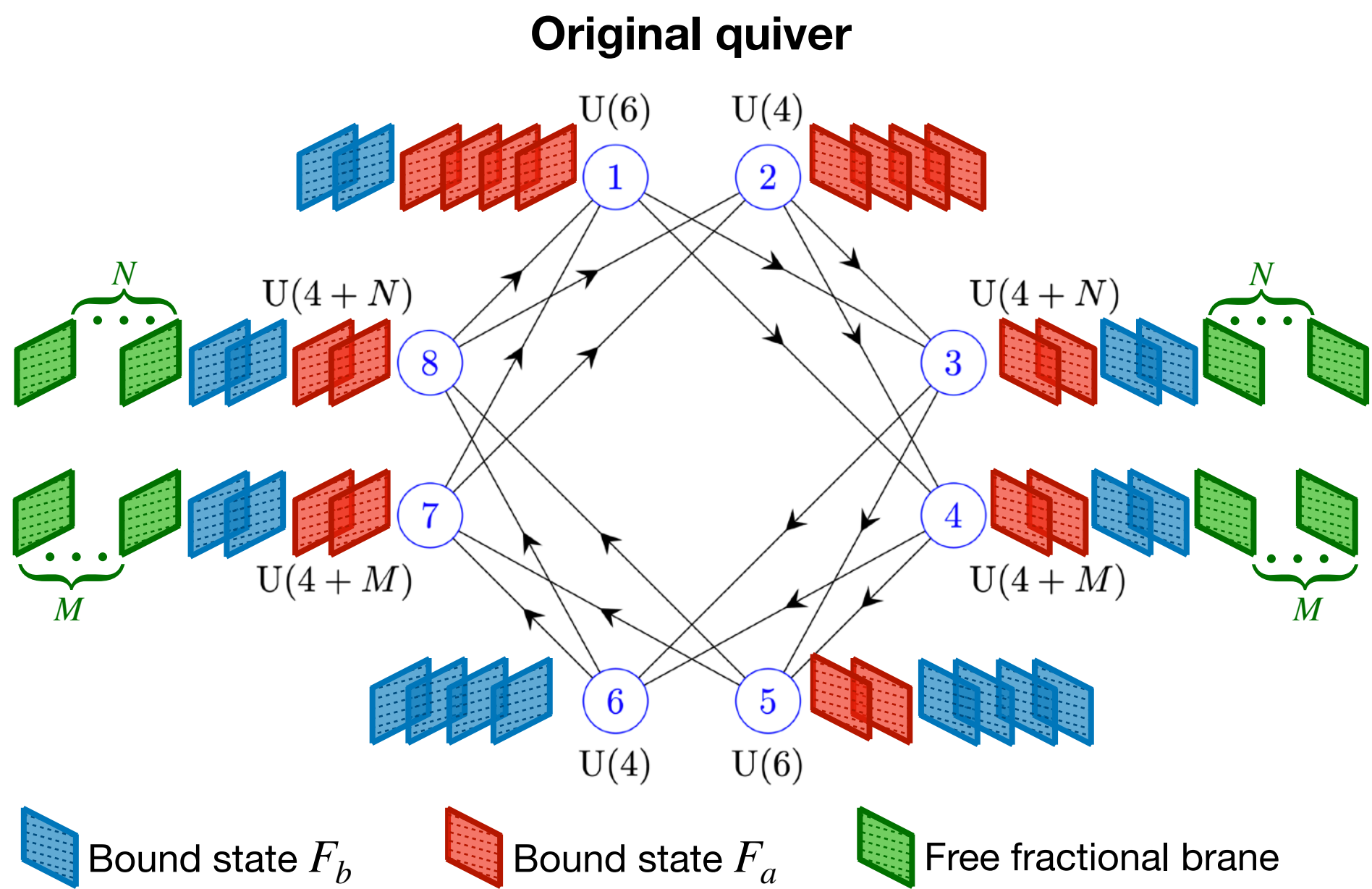
### Higgsed, orientifolded quiver



For  $N = 3, M = 1$ : SUSY  
Left-Right symmetric model

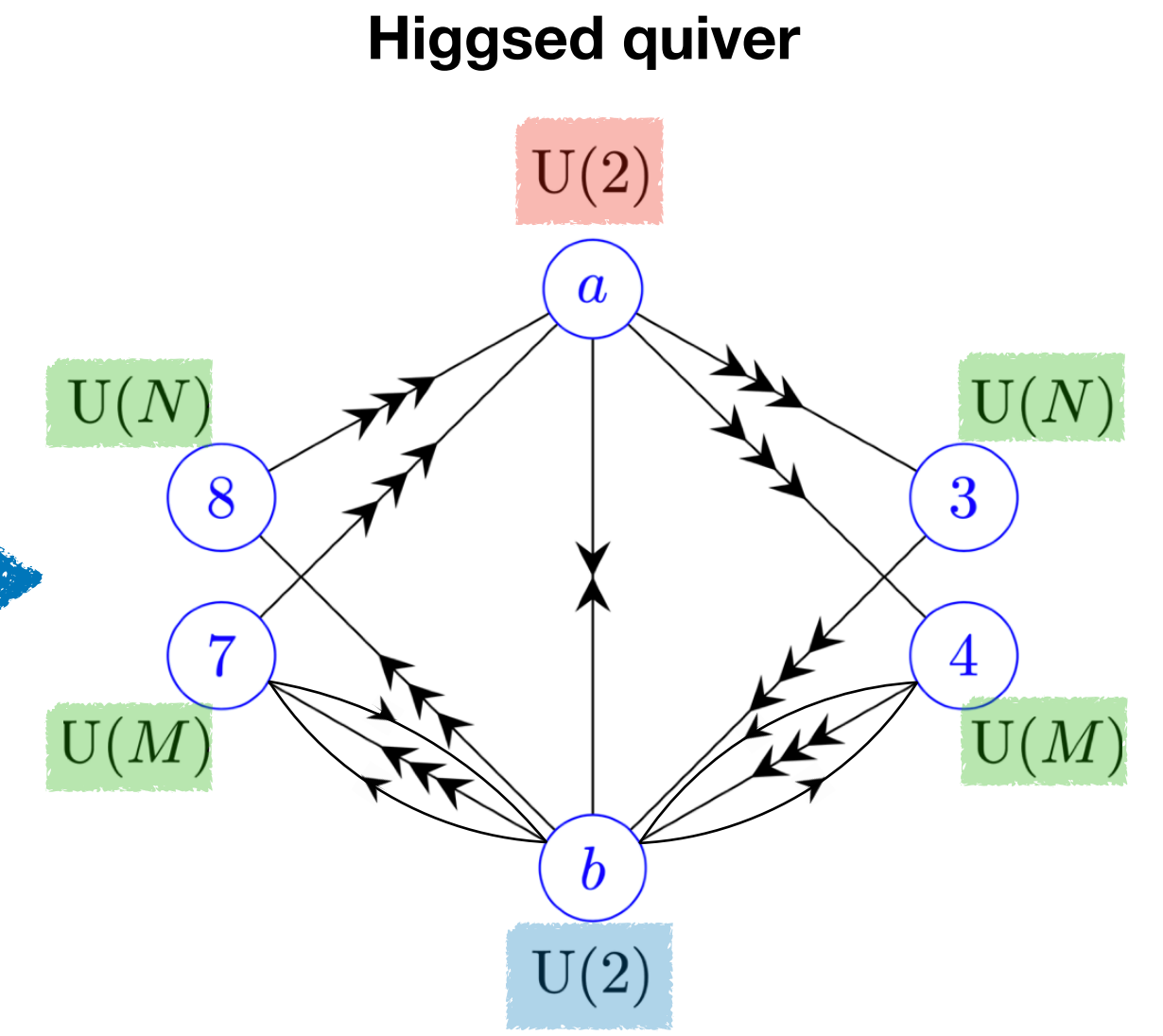
Pati, Salam: Phys. Rev. D10 (1974) 275





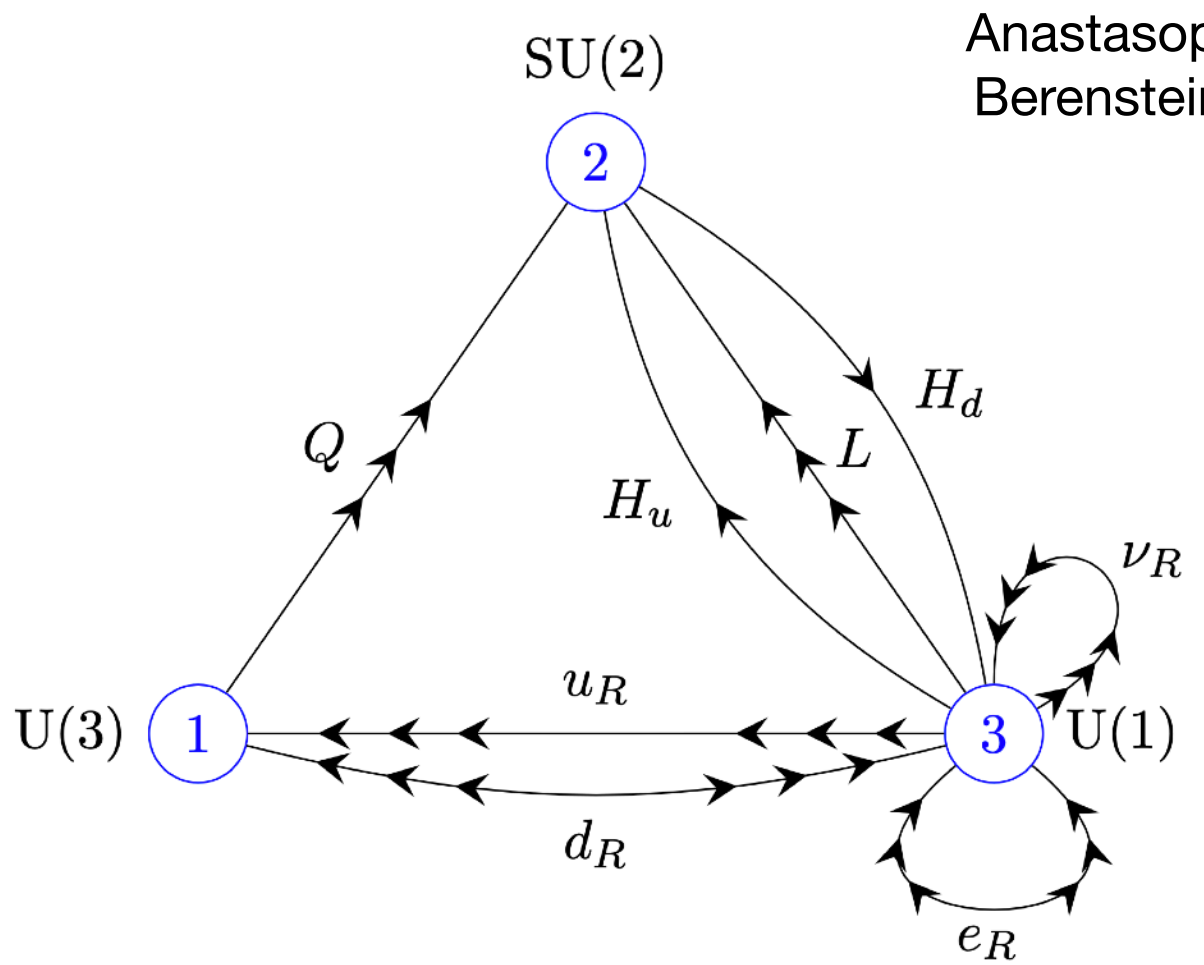
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### Minimal Quiver Standard Model:



Anastasopoulos et al.: hep-th/0605226  
 Berenstein, Pinansky: hep-th/0610104

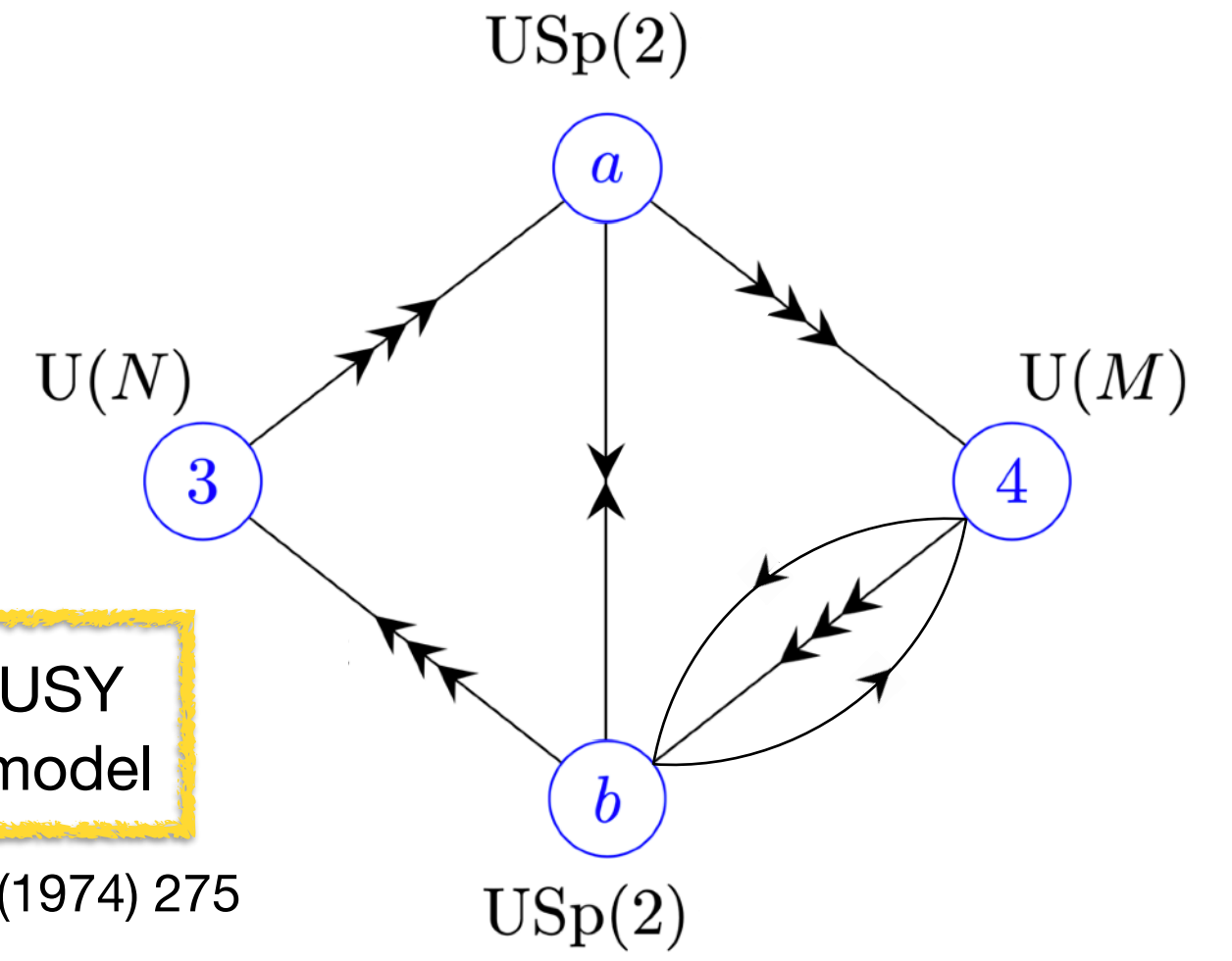
Conventional Higgsing  
 $SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_Y$

See e.g. Heckman, Vafa,  
 Verlinde, Wijnholt: 0711.0387

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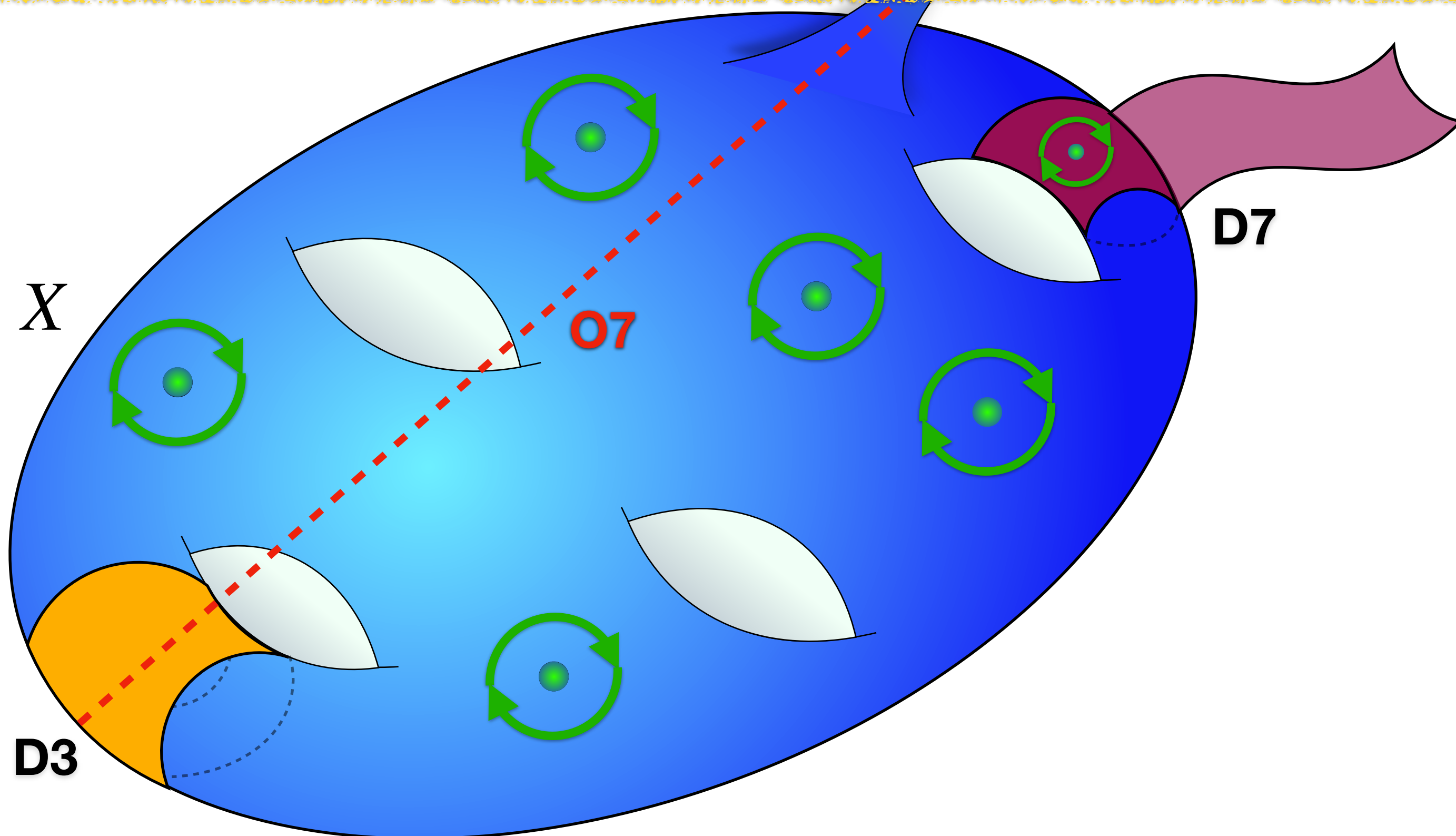
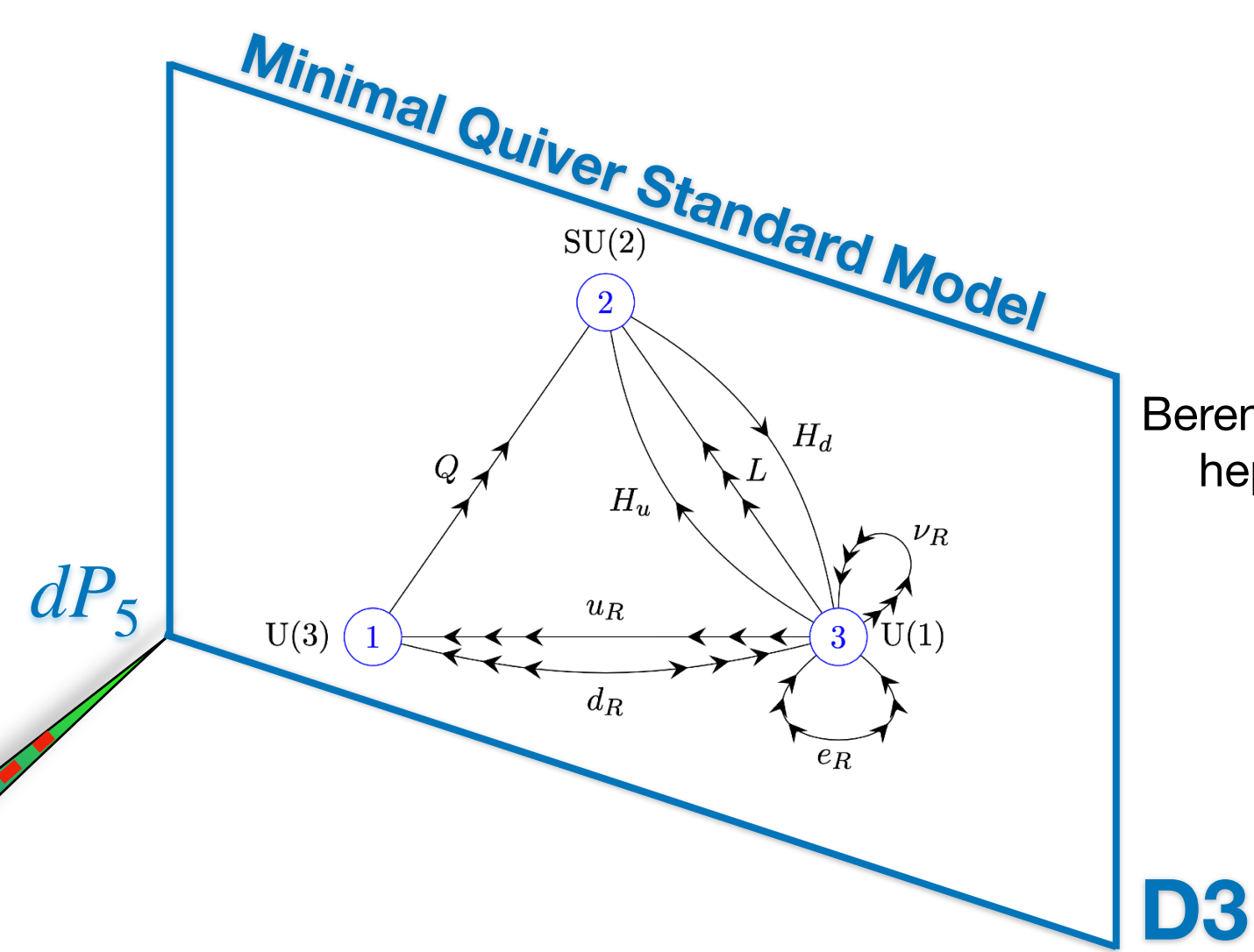
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# The search for a global model in the KS database

For a del Pezzo divisor  $D_s$  of type  $dP_n$

$$\int_{X_3} D_s^3 = k_{sss} = 9 - n, \quad \int_{X_3} D_s^2 D_i \leq 0 \quad \forall i \neq s$$

Diagonality condition for  $dP_5$

$$k_{sss} k_{sij} = k_{ssi} k_{ssj} \quad \forall i, j$$

4-cycle volume becomes complete square

$$\tau_s = \frac{1}{2} k_{sij} t^i t^j = \frac{1}{2 k_{sss}} (k_{ssi} t^i)^2$$

Necessary condition to ensure correct singularity structure!

Refer to diagonal  $dP_n$  divisor  $D_s$  as  **$ddP_n$  divisor**

We looked at the divisor structure of CY geometries in the Kreuzer-Skarke (KS) database with  $h^{1,1} \leq 5$  Kreuzer, Skarke: hep-th/0002240

$h^{1,1}$	Poly*	Geom*	dP <sub>0</sub>	dP <sub>1</sub> or F <sub>0</sub>	dP <sub>2</sub>	dP <sub>3</sub>	dP <sub>4</sub>	dP <sub>5</sub>	dP <sub>6</sub>	dP <sub>7</sub>	dP <sub>8</sub>
1	5	5	0	0	0	0	0	0	0	0	0
2	36	39	9	4	0	0	0	0	2	4	5
3	243	305	55	88	4	4	2	9	20	62	64
4	1185	2000	304	767	146	135	52	175	213	566	506
5	4897	13494	2107	6518	1960	2094	880	2005	2011	4358	3837

$h^{1,1}$	Poly*	Geom* (n <sub>CY</sub> )	ddP <sub>0</sub>	dF <sub>0</sub>	ddP <sub>n</sub> (1 ≤ n ≤ 5)	ddP <sub>6</sub>	ddP <sub>7</sub>	ddP <sub>8</sub>	n <sub>LVS</sub> (ddP <sub>n</sub> ≥ 1)
1	5	5	0	0	0	0	0	0	0
2	36	39	9	2	0	2	4	5	22
3	243	305	55	16	0	16	37	34	132
4	1185	2000	304	140	0	97	210	126	750
5	4897	13494	2107	901	0	486	731	374	4104

Distinct favourable polytopes and geometries

## Kreuzer-Skarke $ddP_n$ conjecture:

Calabi-Yau threefolds arising from fine, regular, star triangulations of 4d reflexive polytopes in the Kreuzer-Skarke database do not exhibit diagonal  $dP_n$  divisors with  $1 \leq n \leq 5$

Further checks of ~300.000 distinct geometries at  $6 \leq h^{1,1} \leq 40$  with **CYTools** confirm this trend!

Demirtas, McAllister, Rios-Tascon: 2008.01730

# Global model construction

Let us focus on specific model with  $(h^{2,1}, h^{1,1}) = (52, 4)$

$HY_1$	$HY_2$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	$x_8$	$x_9$
4	4	1	0	0	0	2	2	1	1	1
2	2	0	1	0	0	1	1	0	0	1
2	2	0	0	1	0	1	1	0	1	0
2	2	0	0	0	1	1	1	1	0	0
		NdP <sub>17</sub>	dP <sub>5</sub>	dP <sub>5</sub>	dP <sub>5</sub>	SD1	SD1	SD2	SD2	SD2

Euler characteristic

$$\chi = -96$$

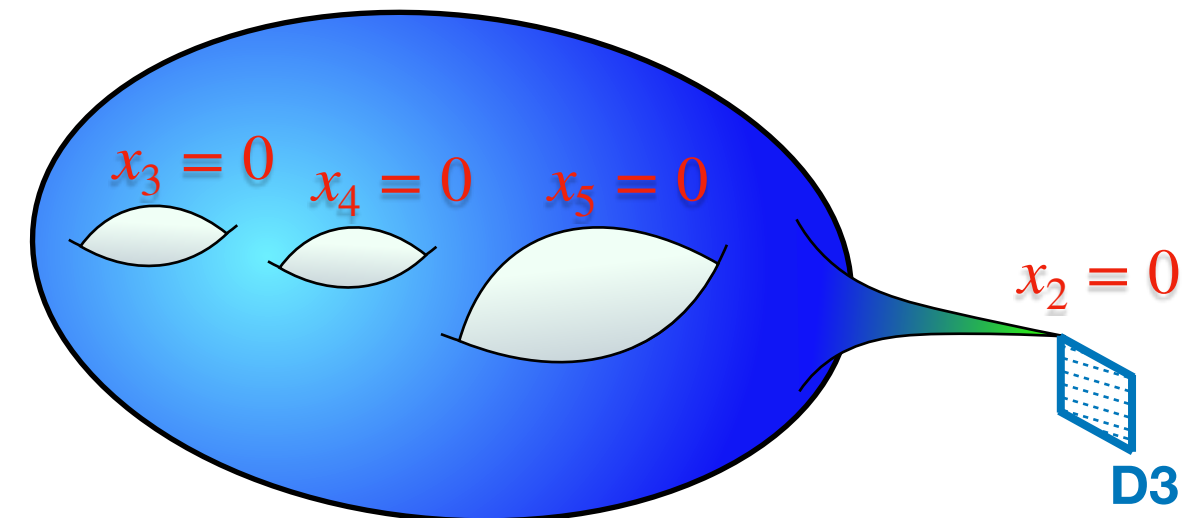
Stanley-Reisner ideal

$$SR = \{x_2x_3, x_2x_4, x_2x_9, x_3x_4, x_4x_7, x_1x_7x_9, x_3x_5x_6x_8, x_1x_5x_6x_7x_8, x_1x_5x_6x_8x_9\}$$

**Construction plan:**

CY threefolds as complete intersections of 2 equations in a 5-dimensional toric space

We take the singular limit  $t_2 \rightarrow 0$  which gives rise to a  $dP_5$  singularity!



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$HY_1$	$HY_2$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	$x_8$	$x_9$
4	4	1	0	0	0	2	2	1	1	1
2	2	0	1	0	0	1	1	0	0	1
2	2	0	0	1	0	1	1	0	1	0
2	2	0	0	0	1	1	1	1	0	0
		NdP <sub>17</sub>	dP <sub>5</sub>	dP <sub>5</sub>	dP <sub>5</sub>	SD1	SD1	SD2	SD2	SD2

Euler characteristic

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**Construction plan:**

CY threefolds as complete intersections of 2 equations in a 5-dimensional toric space

**We take the singular limit  $t_2 \rightarrow 0$  which gives rise to a  $dP_5$  singularity!**

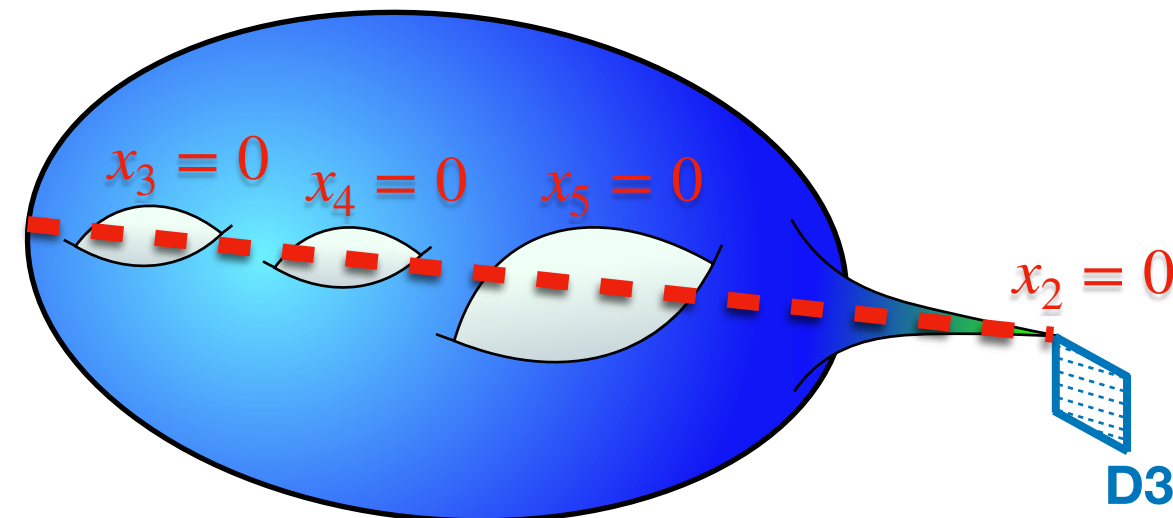
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$$\sigma : x_5 \mapsto -x_5$$

Single O7-plane on

$$D_5 = 2D_b - D_2 - D_3 - D_4$$

**We checked that the local model can indeed be embedded as well as that the **global and local involutions are consistent!****



# Global model construction

Let us focus on specific model with  $(h^{2,1}, h^{1,1}) = (52, 4)$

$HY_1$	$HY_2$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	$x_8$	$x_9$
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2	2	0	1	0	0	1	1	0	0	1
2	2	0	0	1	0	1	1	0	1	0
2	2	0	0	0	1	1	1	1	0	0
		NdP <sub>17</sub>	dP <sub>5</sub>	dP <sub>5</sub>	dP <sub>5</sub>	SD1	SD1	SD2	SD2	SD2

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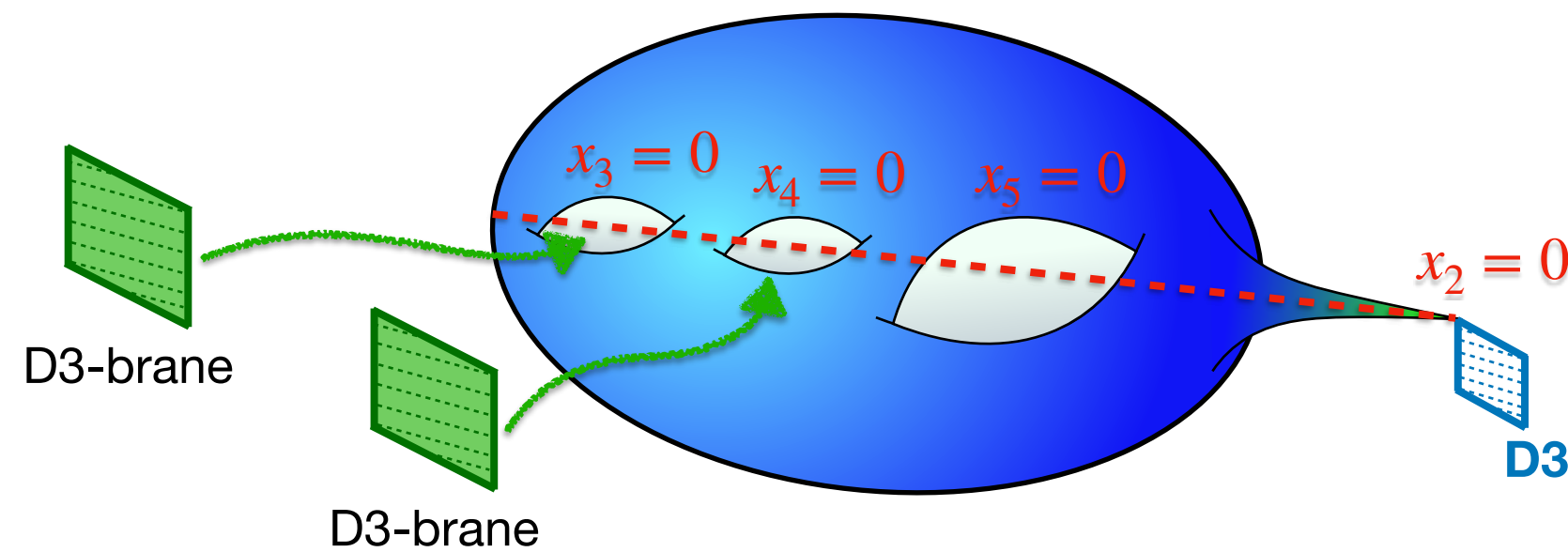
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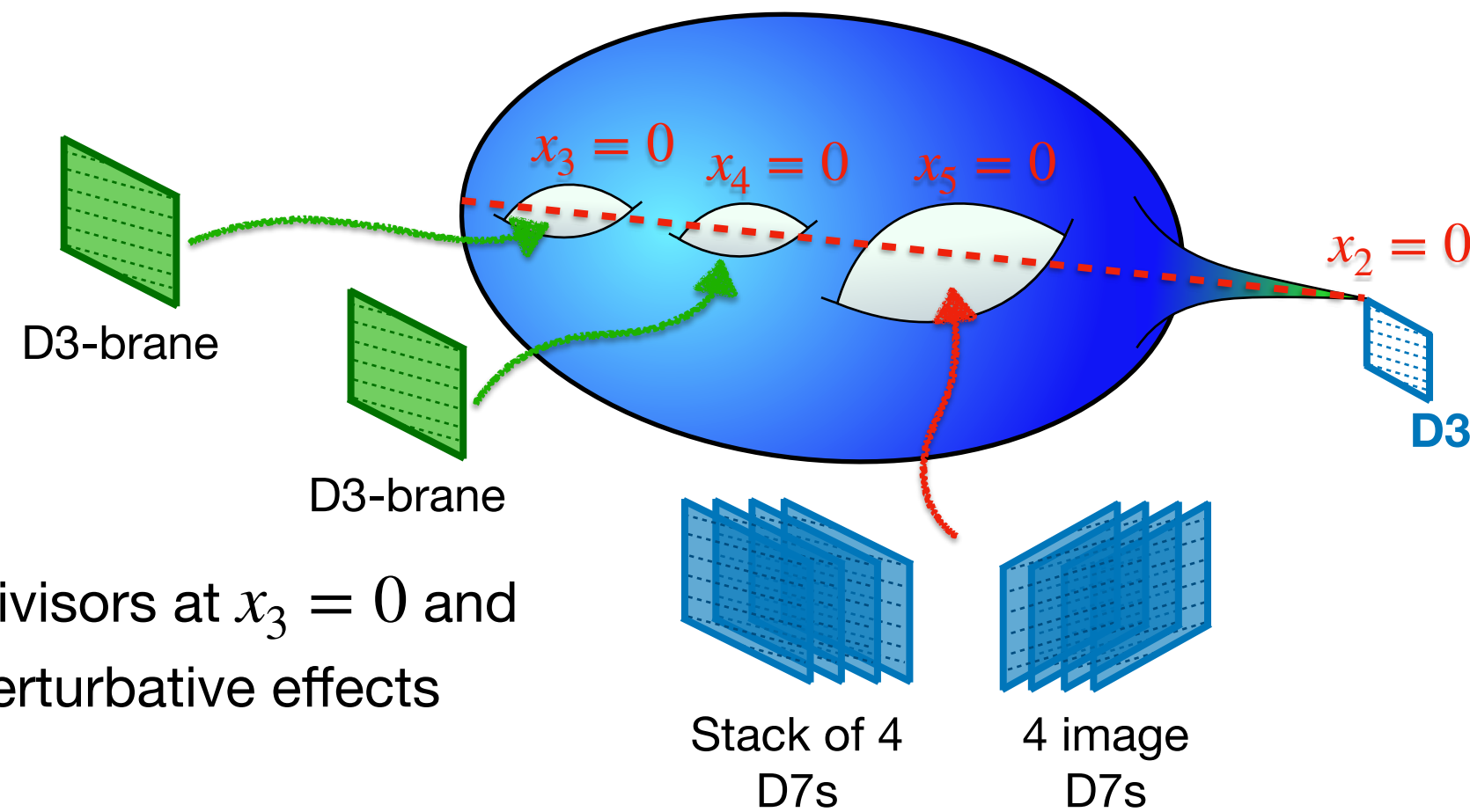
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**Stack of 4 D7-branes** (plus their 4 images) wrapping  $x_5 = 0$  with **SO(8) gauge group** and **flux**

$$\mathcal{F} = F - B = \left(n_b - \frac{1}{2}\right) D_b + \left(n_2 - \frac{1}{2}\right) D_2 \quad n_b, n_2 \in \mathbb{Z}.$$

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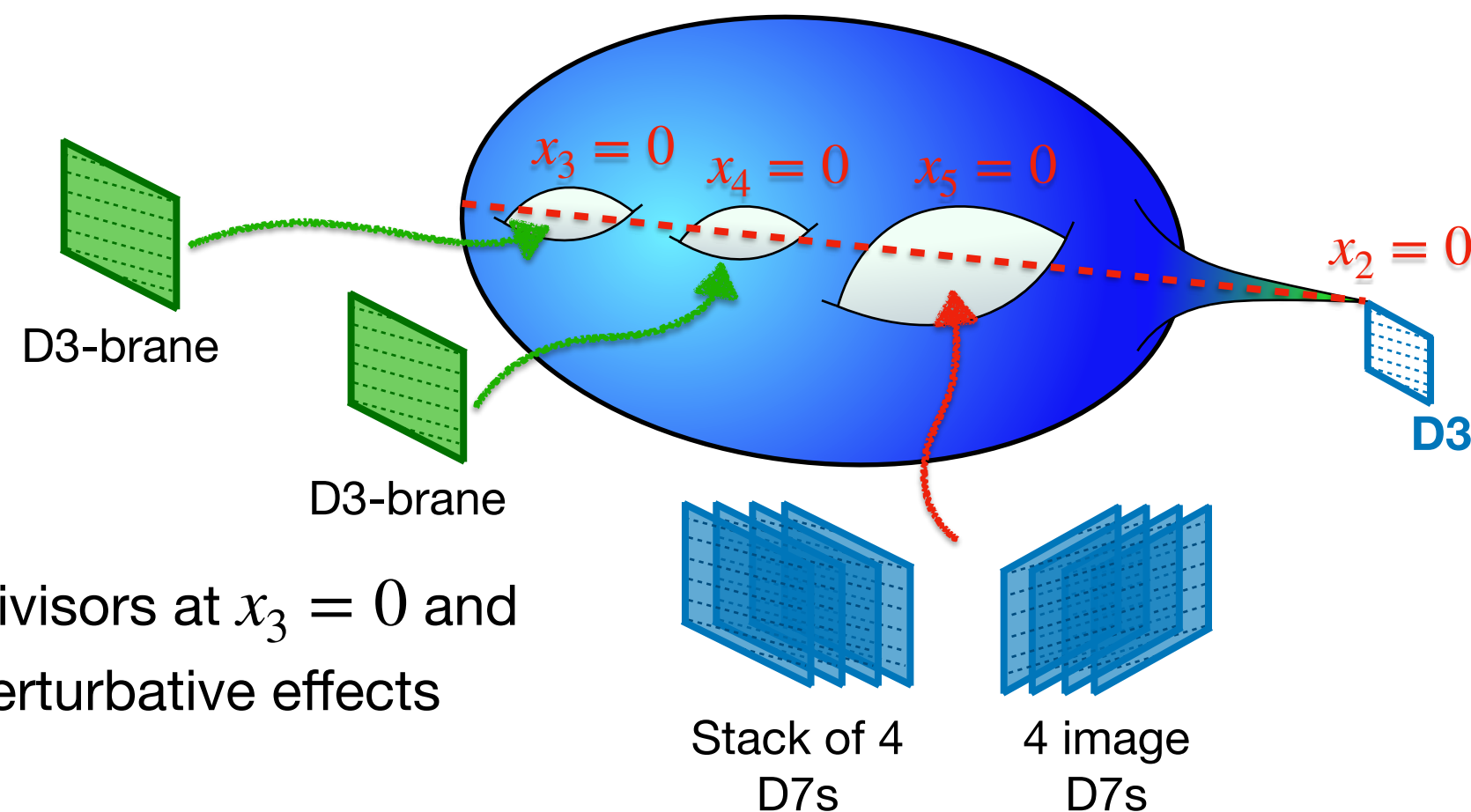
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Flux breaks **SO(8) to U(4)** with **Fayet-Iliopoulos (FI) terms**

$$\xi_{D7} = \frac{1}{4\pi\mathcal{V}} \int_{D7} \mathcal{F} \wedge J \xrightarrow{t_2 \rightarrow 0} \frac{1}{\pi\mathcal{V}} (2n_b - 1)t_b$$

Non-vanishing FI-term implies we have to switch on VEV for adjoint complex scalar  $\Phi$  living on D7 stack  $\rightarrow$  **T-brane background**



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# Moduli stabilisation

$(\alpha')$ <sup>3</sup>-corrected Kähler potential

$$K = \underbrace{-\ln(S + \bar{S}) - \ln\left(-i \int_X \Omega \wedge \bar{\Omega}\right)}_{\text{Complex structure moduli}} \underbrace{- 2 \ln\left(\mathcal{V} + \frac{\zeta}{2}\right)}_{\text{Kähler moduli}} + \underbrace{K_Q}_{\text{Quiver}}$$

$$\mathcal{V} = d_1 \tau_b^{3/2} - d_3 \tau_3^{3/2} - d_4 \tau_4^{3/2}, \quad d_1 = d_3 = d_4 = \frac{1}{3\sqrt{2}}$$

Full **D/F-term scalar potential** for bulk and quiver:

$$V = V_F^{\text{Flux}} + V_F^{\text{quiver}} + V_D^{\text{quiver}} + V_D^{\text{bulk}} + V_F^{\text{LVS}} + V_{\text{soft}}$$

$$\zeta = -\frac{\chi(X) \zeta(3)}{2(2\pi)^3 g_s^{3/2}}$$

**Superpotential** with  $a_3 = 2\pi$

$$W = \underbrace{\int_X G_3 \wedge \Omega}_{\text{Flux}} + \underbrace{A_3 e^{-a_3 T_3}}_{\text{Non-perturbative}} + \underbrace{W_Q(X, U)}_{\text{Quiver}}$$

**Supersymmetric minima** at leading order in the volume  $\mathcal{O}(\mathcal{V}^{-2})$

$$V_F^{\text{Flux}} = V_F^{\text{quiver}} = V_D^{\text{quiver}} = V_D^{\text{bulk}} = 0$$

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Stabilises complex structure and open string moduli

Total scalar potential for Kähler moduli

$$V_{\text{tot}} = \frac{e^{K_{\text{cs}}}}{2 \text{Re}(S)} \left( V_{\text{LVS}} + \frac{\mathcal{F}_{\text{up}} |W_0|^2}{\mathcal{V}^{8/3}} \right), \quad \mathcal{F}_{\text{up}} = \frac{1}{4\pi} \left( \frac{1}{d_1} \right)^{1/3} \approx 0.1822$$

From T-brane background!

Vacuum energy at non-SUSY LVS minima

$$\langle V_{\text{tot}} \rangle \simeq \frac{e^{K_{\text{cs}} |W_0|^2}}{18 \text{Re}(S) \mathcal{V}^3} \left[ \mathcal{F}_{\text{up}} \mathcal{V}^{1/3} - \sum_{i=3}^4 \frac{27 d_i (1 - 4\epsilon_i)}{4 a_i (1 - \epsilon_i)^2} \sqrt{\tau_i} \right]$$

## Conditions for LVS minima

Balasubramanian, Berglund, Conlon, Quevedo: hep-th/0502058

$$\mathcal{V} = \frac{3 d_i \sqrt{\tau_i} (1 - 4\epsilon_i)}{4 a_i (1 - \epsilon_i)} \frac{|W_0|}{|A_i|} e^{a_i \tau_i} \quad \epsilon_i = \frac{1}{4 a_i \tau_i}$$

$$e^{a_3 \tau_3 - a_4 \tau_4} = \frac{a_3 |A_3| d_4}{a_4 |A_4| d_3} \frac{1 - \epsilon_3}{1 - 4\epsilon_3} \frac{1 - 4\epsilon_4}{1 - \epsilon_4} \frac{\sqrt{\tau_4}}{\sqrt{\tau_3}}$$

$$\frac{\zeta}{2} = \sum_{i=3}^4 \frac{d_i (1 - 4\epsilon_i)}{(1 - \epsilon_i)^2} \tau_i^{3/2} - \frac{16 \mathcal{F}_{\text{up}}}{27} \mathcal{V}^{1/3}$$

## Minkowski minima

$$\frac{\zeta}{2} = \sum_{i=3}^4 \frac{d_i (1 - 4\epsilon_i) (1 - 16\epsilon_i)}{(1 - \epsilon_i)^2} \tau_i^{3/2}$$

$$\langle \mathcal{V} \rangle_{\text{Mink.}} = \frac{1}{\mathcal{F}_{\text{up}}^3} \left( \sum_{i=3}^4 \frac{27 d_i (1 - 4\epsilon_i)}{4 a_i (1 - \epsilon_i)^2} \sqrt{\tau_i} \right)^3$$

At the Minkowski minimum, the volume is **not** exponentially large, but grows like  $(h^{1,1} - 2)^2$

# Minkowski minima, mass spectrum and SUSY breaking

Numerical analysis for  $|A_s| = |A_3| = |A_4|$   $\tau_s = \tau_3 = \tau_4$

$g_s$	$ W_0 / A_s $	$\langle \tau_s \rangle$	$\langle \mathcal{V} \rangle$	$ W_0 / A_s $	$\langle \tau_s \rangle$	$\langle \mathcal{V} \rangle$
0.10	$3.57 \cdot 10^{-6}$	3.23	115.6	$2.88 \cdot 10^{-9}$	4.42	188.6
0.05	$2.22 \cdot 10^{-13}$	5.98	301.1	$1.05 \cdot 10^{-19}$	8.35	503.2
0.03	$3.72 \cdot 10^{-23}$	9.63	626.4	$8.38 \cdot 10^{-34}$	13.59	1057.4
0.02	$1.79 \cdot 10^{-35}$	14.21	1131.3	$1.61 \cdot 10^{-51}$	20.15	1919.3
0.01	$1.21 \cdot 10^{-72}$	27.94	3145.2	$6.85 \cdot 10^{-105}$	39.82	5363.7

$$\chi_{eff} = -56$$

$$\chi = -96$$

Minasian, Pugh, Savelli: 1506.06756  $\chi_{eff} = \chi(X) + 2 \int_X D_{O7}^3$

At the Minkowski minimum:

$$\frac{|W_0|}{|A_3|} \simeq \frac{4a_3}{3d_3} \left( \frac{27d_3}{2a_3 \mathcal{F}_{up}} \right)^3 \left( \frac{\zeta}{4d_3} \right)^{2/3} e^{-a_3 [\zeta/(4d_3)]^{2/3}}$$

Tuning in  $W_0$  is model dependent and avoided for gaugino condensation or  $h^{1,1} > 4$

Small  $W_0$  could be achieved via

- A. explicit solutions Demirtas et al.: 1912.10047
- B. stochastic search optimisation Cole, AS, Shiu: 1907.10072

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$$M_{soft} \sim m_{3/2} \sim |W_0| M_p / \mathcal{V}$$

$$m_{3/2} \sim 10^{10} \text{ GeV}$$

$$m_{3/2} \sim 1 \text{ TeV}$$



Soft masses  
below LHC scales

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Field	Name	Mass
dP <sub>5</sub> modulus	$\tau_2, \rho_2$	$\sim M_s$
cx str moduli	$U_\alpha$	$\sim m_{3/2}$
dilaton	$S$	$\sim m_{3/2}$
blow-up cycles	$\tau_3, \tau_4$	$\sim m_{3/2}$
blow-up axions	$\rho_3, \rho_4$	$\sim m_{3/2}$
volume modulus	$\tau_b$	$\sim m_{3/2} / \sqrt{\mathcal{V}}$
volume axion	$\rho_b$	$\sim M_p e^{-\mathcal{V}^{2/3}}$

SUSY broken **spontaneously** through non-vanishing **hidden sector F-terms**:

$$\frac{F^{T_b}}{\tau_b} \sim \frac{F^{T_3}}{\tau_3} \sim \frac{F^{T_4}}{\tau_4} \sim m_{3/2}, \quad F^S \sim F^{U_\alpha} \sim \frac{m_{3/2}}{\mathcal{V}}$$

**Threshold corrections** to the gauge kinetic function for orientifolded singularities amount to

$$\tau_2 \rightarrow \tau_2^{\text{new}} = \tau_2 - \alpha \ln \mathcal{V} \quad F^{T_2} = 0 \rightarrow F^{T_2} \sim \alpha m_{3/2}$$

Conlon, Palti: 0906.1920, 0907.1362  
Conlon, Pedro: 1003.0388

**Breaks sequestering effects** and hence one obtains soft masses  $M_{soft} \sim m_{3/2} \sim |W_0| M_p / \mathcal{V}$

# Conclusions

## Summary:

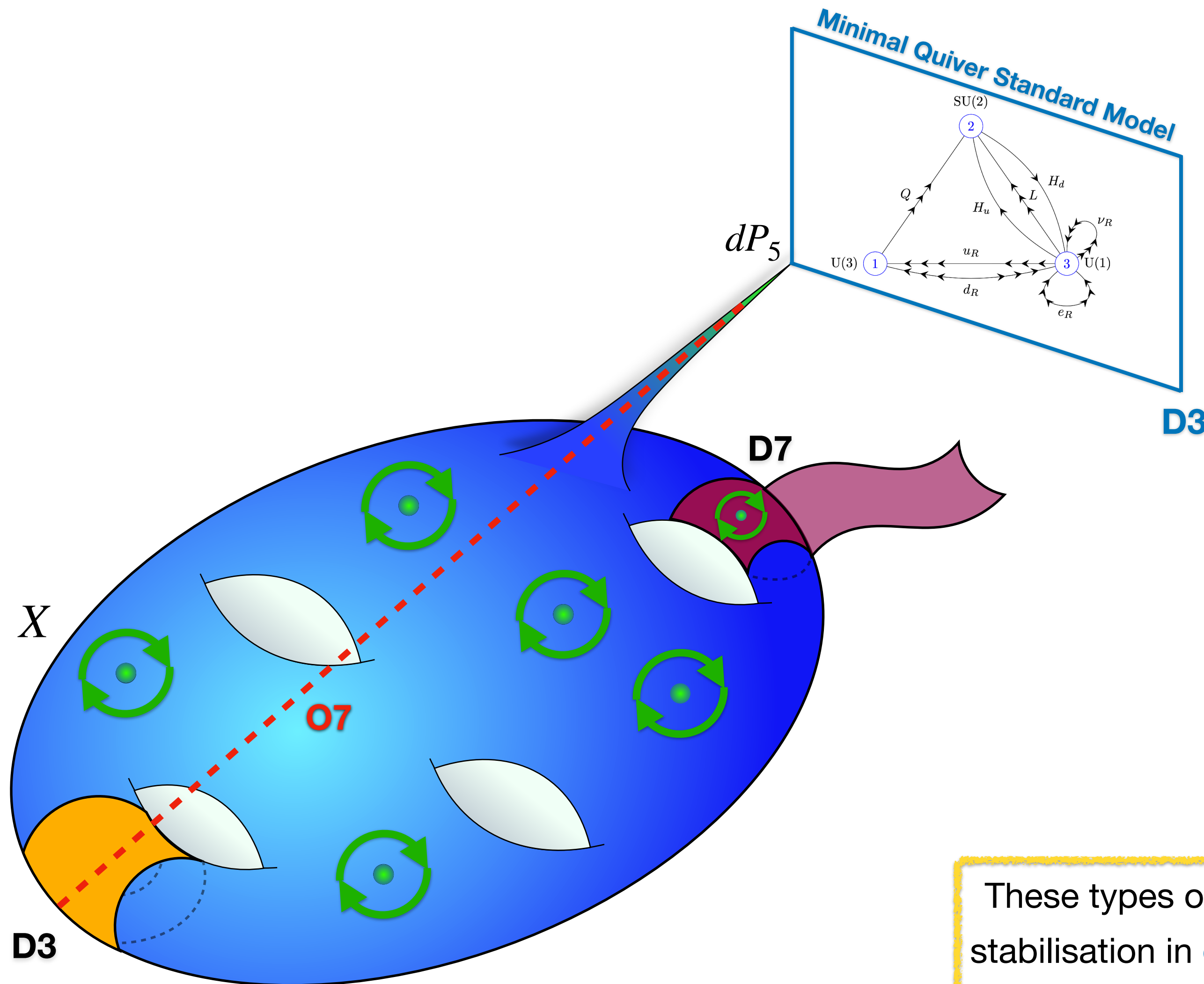
- Standard Model quiver from a single D3-brane at  $dP_5$  singularity
- Explicit construction of compact CY threefolds
- Consistent global embedding with tadpole cancellation etc.
- Moduli stabilisation in de Sitter minimum from T-brane uplift

## Future directions:

- Systematic study of models with  $dP_{n \geq 5}$
- Local orientifold action on exceptional collections
- Models with many Kähler moduli  $h^{1,1} > 4$
- Combine with model for inflation
- Gaugino condensation and additional uplifting sources

## Concluding remark

These types of constructions are the **most explicit** models with moduli stabilisation in **de Sitter** minima and a realisation of the **Standard Model** (and **inflationary cosmology**) in **string theory compactifications!**



**Thank you!**