

A systematic approach to neutrino masses and their phenomenology

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based on work in collaboration with

Juan Herrero-García 1903.10552 [Eur. Phys. J. C79 (2019) no.11, 938]

+ Tobias Felkl 2102.09898



Majorana neutrino masses

Tree-level. Seesaw models

simple, GUT connection, leptogenesis, but huge scales
 → very hard to test and hierarchy problem

Minkowski; Yanagida; Glashow; Gell-Mann, Ramond, Slansky;
 Mohapatra, Senjanovic; Magg, Wetterich; Lazarides, Shafi, Wetterich; Schechter, Valle; Foot, Lew, He, Joshi

Radiative. In principle more testable, but hundreds of them.

Classified by

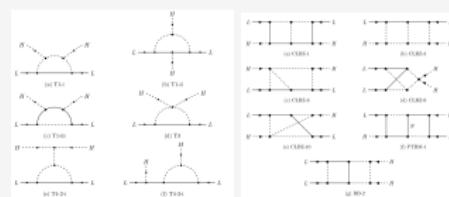
1. Topologies

Bonnet, Hernandez, Ota, Winter 0907.3143; Bonnet, Hirsch, Ota, Winter 1204.5862; Aristizabal Sierra, Degee, Dorame, Hirsch 1411.7038; Cepedello, Fonseca, Hirsch 1807.00629; ...

2. $\Delta L = 2$ EFT operators

Babu, Leung hep-ph/0106054; deGouvea, Jenkins 0708.1344; Angel, Rodd, Volkas 1212.5862; Cai, Clarke, MS, Volkas 1308.0463; Gargalionis, Volkas 2009.13537;

...



$$\begin{aligned} O_1 &= L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl} & O_2 &= L^i L^j L^k \bar{e} H^l \epsilon_{ij} \epsilon_{kl} \\ O_{3a} &= L^i L^j Q^k \bar{d} H^l \epsilon_{ij} \epsilon_{kl} & O_{3b} &= L^i L^j Q^k \bar{d} H^l \epsilon_{ik} \epsilon_{jl} \end{aligned}$$

see review

Cai, Herrero-García, MS, Vicente, Volkas: "From the Trees to the Forest: a review of radiative neutrino mass models" 1706.08524

NEUTRINO MASSES

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SIMPLIFIED MODELS

ooooooo

SINGLY-CHARGED SCALAR SINGLET

ooo

CONCLUSIONS

oo



NEUTRINO MASSES

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SIMPLIFIED MODELS

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SINGLY-CHARGED SCALAR SINGLET

ooo

CONCLUSIONS

oo



Can we do better? → Hybrid approach using simplified models

Main idea

Juan Herrero-García, MS 1903.10552 [Eur.Phys.J. C79 (2019) no.11, 938]

1. m_ν requires at least one **new particle X** (mass M) coupled to SM lepton(s), carrying L (and maybe B).
2. QFT: **L is violated** (by two units) via new operators at scale Λ which encode the (model-dependent) UV physics.
3. Majorana neutrino masses, $m_\nu \propto 1/\Lambda$, are generated.
4. $m_\nu > 0.05\text{eV}$ & $M \leq \Lambda \Rightarrow$ **conservative upper bound on M** .
5. L -conserving pheno mostly determined by renormalizable $\Delta L = 0$ operator

Juan Herrero-García

Bounds apply to all models where X is the lightest particle.



Example at tree level

SM bilinear LH (seesaw type I):

1. **New particle:** fermion singlet N with $Y = 0$ and $L = -1$.
2. L is violated (by two units) via $MNN (+yLHN)$
3. Neutrino masses, $m_\nu = y^2 v^2 / M$, are generated.
4. $m_\nu > 0.05 \text{ eV} \& y \leq 1 \Rightarrow$ conservative upper bound $M \leq 10^{15} \text{ GeV}$

Possible new particles

 $LH \rightarrow N(\text{SSI}), \Sigma(\text{SSIII})$ $LL \rightarrow \Delta(\text{SSII}), h(\text{Zee})$ $\bar{e}e \rightarrow k(\text{Zee-Babu})$ $LH^\dagger \rightarrow \dots$ $\bar{e}H^\dagger \rightarrow \dots$ $\bar{e}\sigma_\mu L^\dagger \rightarrow \dots$ \dots

Particles generating tree level neutrino masses

$$X \sim (SU(3)_c, SU(2)_L, U(1)_Y)_{S/F/V}^{L,3B}$$

$\Delta L = 2$ operators

Seesaw type

	Particle	$\Delta\mathcal{L} = 0$	$ \Delta\mathcal{L} = 2$		BL	ℓ	m_ν	Upper bound
Seesaws	$\bar{N} \sim (1, 1, o)_F^{-1,0}$	$y \bar{N} H L$	$M \bar{N} \bar{N}$	I	\mathcal{O}_1	o	$\frac{y^2 v^2}{M}$	$M \lesssim 10^{15} \text{ GeV}$
	$\Delta \sim (1, 3, 1)_S^{-2,0}$	$y L \Delta L$	$\mu H \Delta^\dagger H$	II	\mathcal{O}_1	o	$\frac{y \mu v^2}{M^2}$	$M \lesssim 10^{15} \text{ GeV}$
	$\bar{\Sigma}_o \sim (1, 3, o)_F^{-1,0}$	$y \bar{\Sigma}_o L H$	$M \bar{\Sigma}_o \bar{\Sigma}_o$	III	\mathcal{O}_1	o	$\frac{y^2 v^2}{M}$	$M \lesssim 10^{15} \text{ GeV}$
	$L_1 \sim (1, 2, -1/2)_F^{1,0}$	$m \bar{L}_1 L$	$\frac{c}{\Lambda} L_1 H L H$		\mathcal{O}_1	o	$\frac{c m}{M} \frac{v^2}{\Lambda} c$	$M \lesssim 10^{15} \text{ GeV}$

Particles generating loop level neutrino masses

Zee-Babu

$$X \sim (SU(3)_c, SU(2)_L, U(1)_Y)_{S/F/V}^{L,3B}$$

Seesaws

Radiative

Loop order

Particle	$\Delta\mathcal{L} = 0$	$ \Delta\mathcal{L} = 2$	BL	ℓ	m_ν	Upper bound
$\bar{N} \sim (1, 1, o)_F^{-1, o}$	$y \bar{N} H L$	$M \bar{N} \bar{N}$	\mathcal{O}_1	o	$\frac{y^2 v^2}{M}$	$M \lesssim 10^{15} \text{ GeV}$
	$y L \Delta L$	$\mu H \Delta^\dagger H$	\mathcal{O}_1	o	$\frac{y_\mu v^2}{M^2}$	$M \lesssim 10^{15} \text{ GeV}$
	$y \bar{\Sigma}_o L H$	$M \bar{\Sigma}_o \bar{\Sigma}_o$	\mathcal{O}_1	o	$\frac{y^2 v^2}{M}$	$M \lesssim 10^{15} \text{ GeV}$
	$m \bar{L}_1 L$	$\frac{c}{\Lambda} L_1 H L H$	\mathcal{O}_1	o	$\frac{c_m}{\Lambda} \frac{v^2}{(4\pi)^4} c$	$M \lesssim 10^{15} \text{ GeV}$
$L_1 \sim (1, 2, -1/2)_F^{1, o}$	$y H^\dagger \bar{e} L_1$	$\frac{c}{\Lambda^2} \bar{L}_1 \bar{u} d^\dagger L^\dagger$	\mathcal{O}_8^\dagger	2	$\frac{c y u y_d y_l}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
$h \sim (1, 1, 1)_S^{-2, o}$	$y L L h$	$\frac{c}{\Lambda} h^\dagger \bar{e} L H$	\mathcal{O}_2	1	$\frac{c y y_l}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{10} \text{ GeV}$
	$y \bar{e}^\dagger \bar{e}^\dagger k$	$\frac{c}{\Lambda^3} k^\dagger L^\dagger L^\dagger L^\dagger L^\dagger$	\mathcal{O}_9^\dagger	2	$\frac{c y y_l^2}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^6 \text{ GeV}$
	$y \bar{E} L H^\dagger$	$\frac{c}{\Lambda^4} L E H Q^\dagger \bar{u}^\dagger H$	\mathcal{O}_6	2	$\frac{c y y_u}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^{10} \text{ GeV}$
	$m \bar{e} E$	$\frac{c}{\Lambda^3} \bar{E} L L L H$	\mathcal{O}_2	1	$\frac{c m}{M} \frac{y_l}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{10} \text{ GeV}$
$\bar{\Sigma}_1 \sim (1, 3, 1)_F^{-1, o}$	$y H^\dagger \bar{\Sigma}_1 L$	$\frac{c}{\Lambda^2} L H H \Sigma_1 H$	$\mathcal{O}_1'^1$	1	$\frac{c y}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{12} \text{ GeV}$
$L_2 \sim (1, 2, -3/2)_F^{1, o}$	$y H \bar{e} L_2$	$\frac{c}{\Lambda^2} \bar{L}_2 L L L$	\mathcal{O}_2	1	$\frac{c y y_l}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{10} \text{ GeV}$
$X_2 \sim (1, 2, 3/2)_V^{-2, o}$	$y \bar{e}^\dagger \bar{\sigma}^\mu L X_{2\mu}$	$\frac{c}{\Lambda} \bar{u}^\dagger \bar{\sigma}^\mu \bar{d} X_{2\mu}^\dagger H$	\mathcal{O}_8	2	$\frac{c y y_u y_d y_e}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$

Particles with B (leptoquarks)

$X \sim (SU(3)_c, SU(2)_L, U(1)_Y)_{S/F/V}^{L, 3B}$ $\Delta L = 2$ operators Loop order

Particle	$\Delta \mathcal{L} = 0$	$ \Delta \mathcal{L} = 2$	BL	ℓ	m_ν	Upper bound
$\tilde{R}_2 \sim (3, 2, 1/6)_S^{-1,1}$	$y \bar{d} L \tilde{R}_2$	$\frac{c}{\Lambda} \tilde{R}_2^\dagger Q L H$	\mathcal{O}_{3b}	1	$\frac{c y y_d}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{11} \text{ GeV}$
$R_2 \sim (3, 2, 7/6)_S^{-1,1}$	$y \bar{e}^\dagger Q^\dagger R_2$	$\frac{c}{\Lambda^3} R_2^\dagger L^\dagger L^\dagger L^\dagger \bar{d}^\dagger$	\mathcal{O}_{10}^\dagger	2	$\frac{c y y_d y_l}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
	$y \bar{u} L R_2$	$\frac{c}{\Lambda^3} R_2^\dagger L^\dagger L^\dagger L^\dagger \bar{d}^\dagger$	\mathcal{O}_{15}^\dagger	3	$\frac{c y y_d y_g g^2}{2(4\pi)^6} \frac{v^2}{\Lambda}$	$M \lesssim 10^6 \text{ GeV}$
$S_1 \sim (\bar{3}, 1, 1/3)_S^{-1,-1}$	$y L Q S_1$	$\frac{c}{\Lambda} S_1^\dagger L H \bar{d}$	\mathcal{O}_{3b}	1	$\frac{c y y_d}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{11} \text{ GeV}$
	$y \bar{u}^\dagger \bar{e}^\dagger S_1$	$\frac{c}{\Lambda} S_1^\dagger L H \bar{d}$	\mathcal{O}_8	2	$\frac{c y y_l y_u y_d}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
$S_3 \sim (\bar{3}, 3, 1/3)_S^{-1,-1}$	$y L S_3 Q$	$\frac{c}{\Lambda} \bar{d} L S_3^\dagger H$	\mathcal{O}_{3b}	1	$\frac{c y y_d}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{11} \text{ GeV}$
$\tilde{S}_1 \sim (\bar{3}, 1, 4/3)_S^{-1,-1}$	$y \bar{e}^\dagger \bar{d}^\dagger \tilde{S}_1$	$\frac{c}{\Lambda^3} \tilde{S}_1^\dagger L^\dagger L^\dagger L^\dagger Q^\dagger$	\mathcal{O}_{10}^\dagger	2	$\frac{c y y_d y_l}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
Radiative	$V_2 \sim (\bar{3}, 2, 5/6)_V^{-1,-1}$	$y \bar{d}^\dagger \bar{\sigma}^\mu V_{2\mu} L$	$\frac{c}{\Lambda^5} Q^\dagger \bar{\sigma}^\mu L V_{2\mu}^\dagger H \bar{e} L H$	\mathcal{O}_{23}	$\frac{c y y_d y_l}{(4\pi)^6} \frac{v^2}{\Lambda}$	$M \lesssim 10^4 \text{ GeV}$
		$y Q \sigma^\mu V_{2\mu} \bar{e}^\dagger$	$\frac{c}{\Lambda^5} Q^\dagger \bar{\sigma}^\mu L V_{2\mu}^\dagger H \bar{e} L H$	$\mathcal{O}_{44a,b,d}$	$\frac{c y g^2}{2(4\pi)^6} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
$\tilde{V}_2 \sim (\bar{3}, 2, -1/6)_V^{-1,-1}$	$y \bar{u}^\dagger \bar{\sigma}^\mu \tilde{V}_{2\mu} L$	$\frac{c}{\Lambda} Q^\dagger \bar{\sigma}^\mu L H \tilde{V}_{2\mu}^\dagger$	\mathcal{O}_{4a}	1	$\frac{c y y_u}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{12} \text{ GeV}$
$U_1 \sim (3, 1, 2/3)_V^{-1,1}$	$y Q^\dagger \bar{\sigma}^\mu U_{1\mu} L$	$\frac{c}{\Lambda} \bar{u}^\dagger \bar{\sigma}^\mu L H U_{1\mu}^\dagger$	\mathcal{O}_{4a}	1	$\frac{c y y_u}{(4\pi)^2} \frac{v^2}{\Lambda}$	$M \lesssim 10^{12} \text{ GeV}$
	$y \bar{d} \sigma^\mu U_{1\mu} \bar{e}^\dagger$	$\frac{c}{\Lambda} \bar{u}^\dagger \bar{\sigma}^\mu L H U_{1\mu}^\dagger$	\mathcal{O}_8	2	$\frac{c y y_u y_d y_l}{(4\pi)^4} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$
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$\tilde{U}_1 \sim (3, 1, 5/3)_V^{-1,1}$	$y \bar{u} \sigma^\mu \bar{e}^\dagger \tilde{U}_{1\mu}$	$\frac{c}{\Lambda^5} \bar{u}^\dagger \bar{\sigma}^\mu L H \tilde{U}_{1\mu}^\dagger \bar{e} L H$	\mathcal{O}_{46}	3	$\frac{c y g^2}{2(4\pi)^6} \frac{v^2}{\Lambda}$	$M \lesssim 10^7 \text{ GeV}$

Phenomenology

Juan Herrero-García, MS 1903.10552 [Eur.Phys.J. C79 (2019) no.11, 938]

- Driven by non-renormalizable part:
 1. $\Delta L = 2$ processes, like neutrino-less double beta decay.
 2. Washout of BAU
- Driven by renormalizable interaction:
 1. Violation of lepton flavor, universality, PMNS unitarity.
 2. Direct searches at colliders
 3. B violation, like nucleon decays

B violation (LQ) [Weinberg, Weldon, Nath, Barr, Babu, Arnold, Dorsner, ...]

e.g. tree-level nucleon decays: $S_1 = (\bar{3}, 1, 1/3) : y_1 S_1^\dagger \bar{u} \bar{e} + y_2 S_1 \bar{u} \bar{d}$

$$\Gamma(p \rightarrow \pi^0 e^+) \simeq \frac{|y_1|^2 |y_2|^2}{8\pi} \frac{m_p^5}{M_{S_1}^4} < \frac{1}{10^{33} y} \quad \Rightarrow M_{S_1} \gtrsim 10^{16} \text{GeV}$$

S_1 cannot generate neutrino masses without imposing B conservation.

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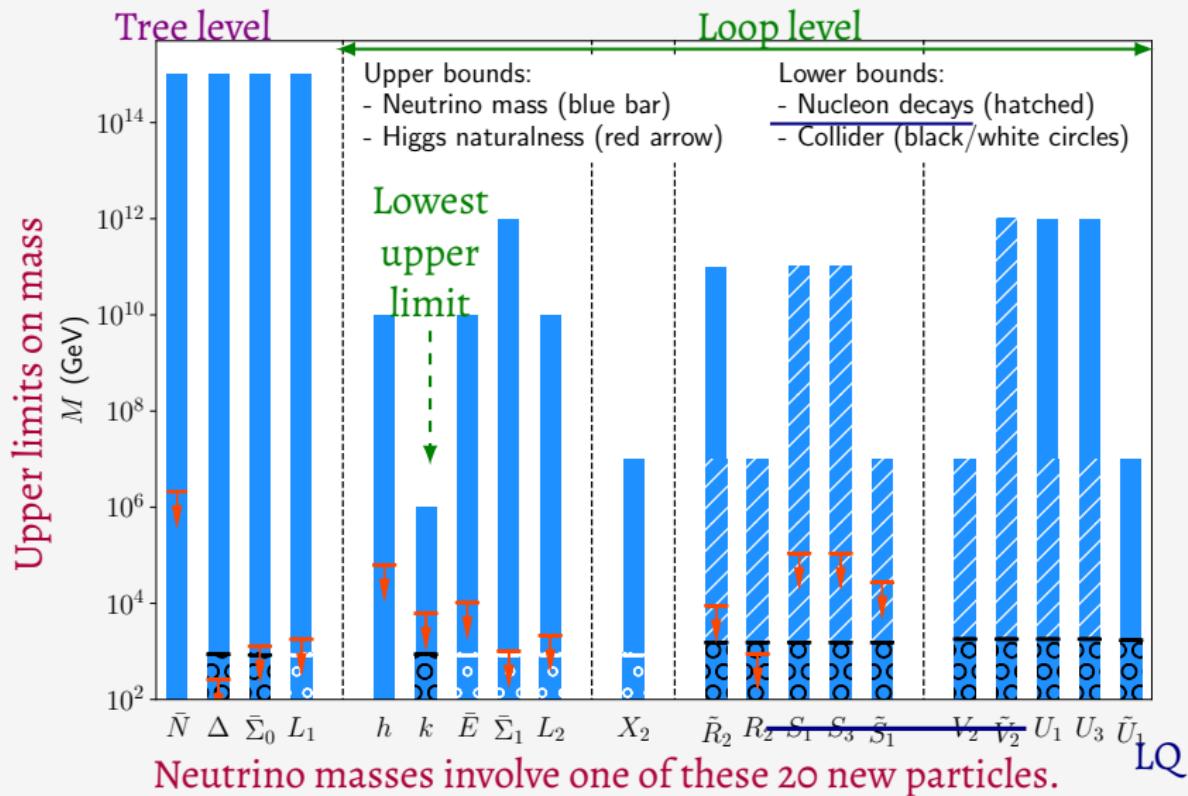
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Summary plot

Juan Herrero-García, MS 1903.10552 [Eur.Phys.J. C79 (2019) no.11, 938]



Singly-charged scalar singlet $h \sim (1, 1, 1)$

- Relevant Yukawa interaction
- y_h is antisymmetric $y_h = -y_h^T$
- non-trivial eigenvector v_h with eigenvalue zero, $y_h v_h = 0$

$$y_h^{ij} L_i L_j h$$

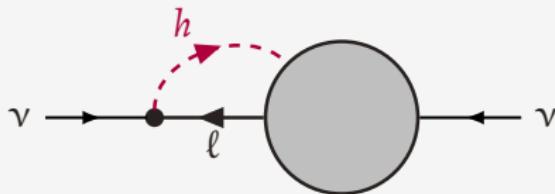


Tobias Felkl



Juan Herrero-García

linear case

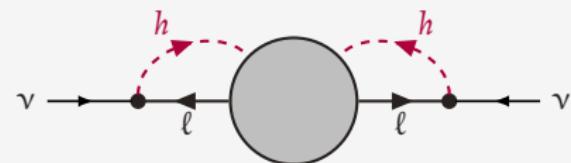


$$M_\nu = X y_h - y_h X^T$$

⇒ 1 complex condition

$$0 = v_h^T M_\nu v_h = v_h^T U^* m_{\text{diag}} U v_h$$

quadratic case



$$M_\nu = y_h S y_h \text{ with } S = S^T$$

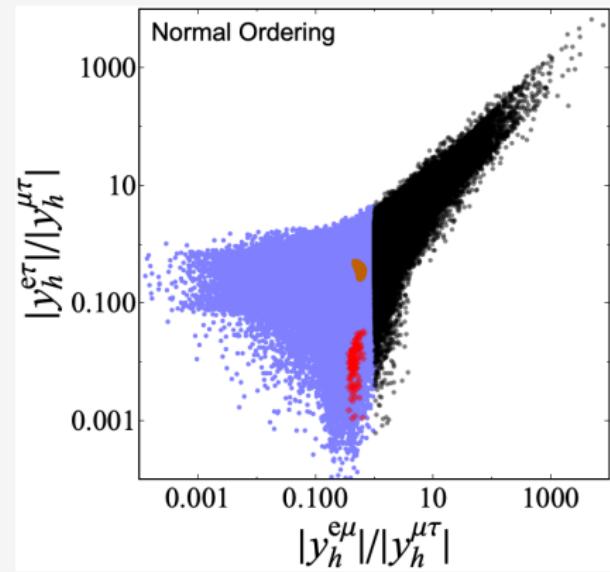
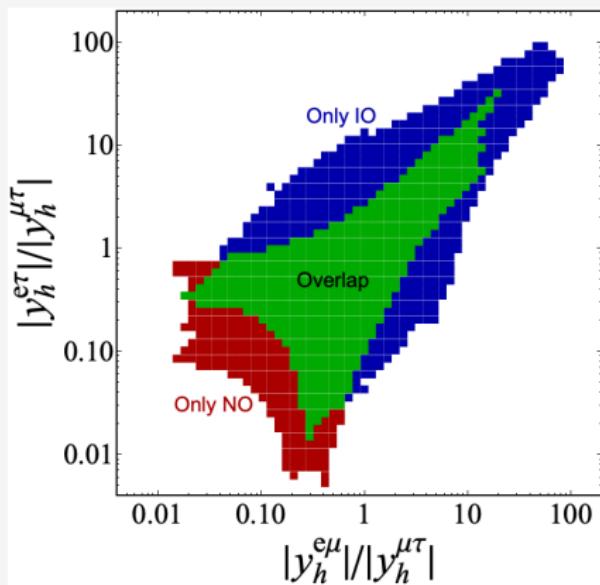
⇒ 2 complex conditions

previously discussed in Zee-Babu model 0711.0483

$$0 = m_{\text{diag}} U^\dagger v_h$$

Yukawa couplings

Tobias Felkl, Juan Herrero-García, MS 2102.09898

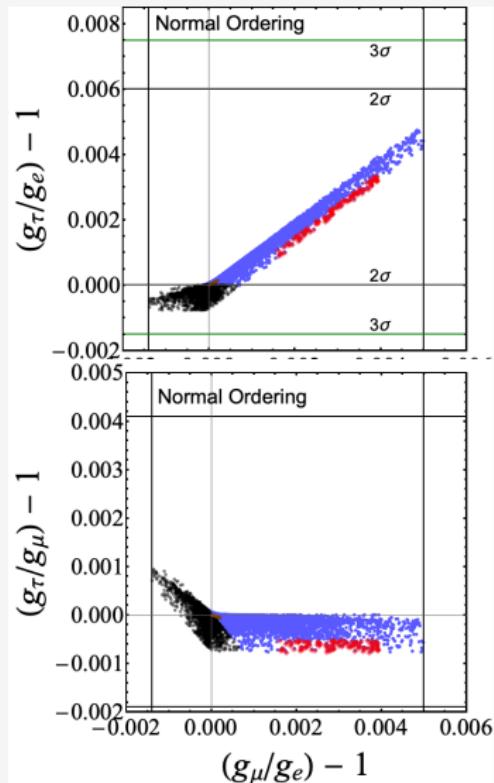


- Linear case: blue (2σ), black (3σ)
- Quadratic case: brown
- Anomalies ($\frac{g_{\mu,\tau}}{g_e}$, Cabibbo angle): red

see 2012.09845

Lepton flavour universality

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$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \epsilon_{ij}^{kl} \left(\nu_i^\dagger \bar{\sigma}^\mu \nu_j \right) \left(\ell_k^\dagger \bar{\sigma}_\mu \ell_l \right)$$

$$\epsilon_{ij}^{kl} = -\frac{1}{\sqrt{2}G_F} \frac{(y_h^{ik})^* y_h^{jl}}{M_h^2}$$

Effective leptonic gauge couplings

$$\frac{g_\mu}{g_e} \simeq 1 + \epsilon_{ee}^{\tau\tau} - \epsilon_{\mu\mu}^{\tau\tau},$$

$$\frac{g_\tau}{g_e} \simeq 1 + \epsilon_{ee}^{\mu\mu} - \epsilon_{\mu\mu}^{\tau\tau},$$

$$\frac{g_\tau}{g_\mu} \simeq 1 + \epsilon_{ee}^{\mu\mu} - \epsilon_{ee}^{\tau\tau}.$$

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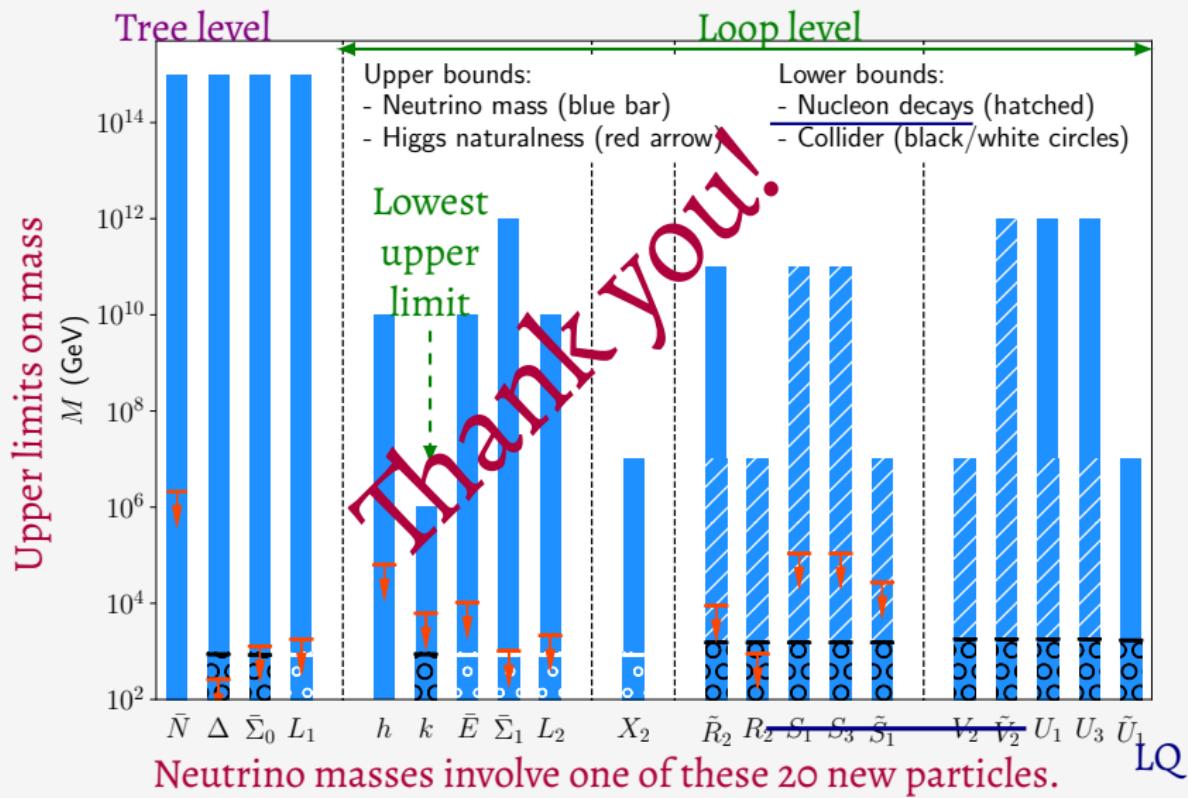
see 2012.09845

Conclusions

- Useful framework to **organize** the plethora of neutrino models and to study their **phenomenology**
 - Robust upper limits on all possible new particles involved in m_ν
 - Nucleon decays rule out some scenarios.
- **Model-independent results** for neutrino masses from singly-charged scalar singlet $h \sim (1, 1, 1)$

Summary plot

Juan Herrero-García, MS 1903.10552 [Eur.Phys.J. C79 (2019) no.11, 938]



Backup slides

Higgs naturalness

See also: SSI: Vissani hep-ph/9709409; SSII(III) 1303.7244

$$\text{Top Diagram: } \Rightarrow M \lesssim \frac{16\pi^2 |\delta m_H^2|_{\max}^{1/2}}{\sqrt{6N_c(3Dg^4 + N_w Y^2 g'^4)}}$$

$$\text{Middle Diagram: } \Rightarrow M \lesssim \frac{2\pi |\delta m_H^2|_{\max}^{1/2}}{|y| \sqrt{2N_c}}$$

$$\text{Bottom Diagram: } \Rightarrow M \lesssim \frac{4\pi^2 |\delta m_H^2|_{\max}^{1/2}}{\sqrt{N_c(3Dg^4 + N_w Y^2 g'^4)}}$$

Naturalness limits much stronger, but less robust

Neutrinoless double β decay

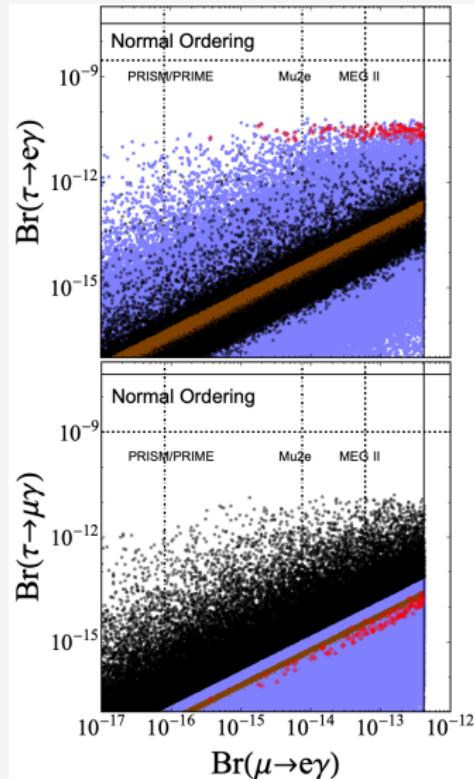
[Ibarra, De Gouvea, Blennow, Rodejohann, Bonnet, ...]

New contributions may be significant for:

1. SSI/III, if new fermion singlets $M_R \sim \mathcal{O}(\text{GeV})$
2. New $D = 7$ operators, if $\Lambda \lesssim \mathcal{O}(100\text{TeV})$
Like $O_8 = \bar{u}^\dagger \bar{e}^\dagger L \bar{d} H$, generated by L_1, X_2, S_1, U_1

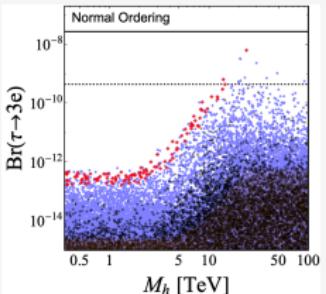
Lepton flavour violation

Tobias Felkl, Juan Herrero-García, MS 2102.09898



$$\frac{\text{Br}(\ell \rightarrow \ell' \gamma)}{\text{Br}(\ell \rightarrow \ell' \nu \bar{\nu})} = \frac{\alpha}{48\pi} \frac{|y_h^{\ell\alpha} y_h^{\ell'\alpha}|^2}{G_F^2 M_h^4}$$

- Photon penguin dominance
- Box diagrams important for $M_h \gtrsim 5$ TeV

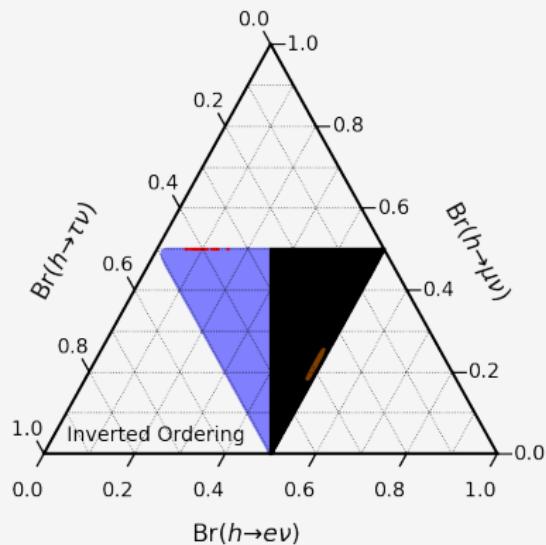
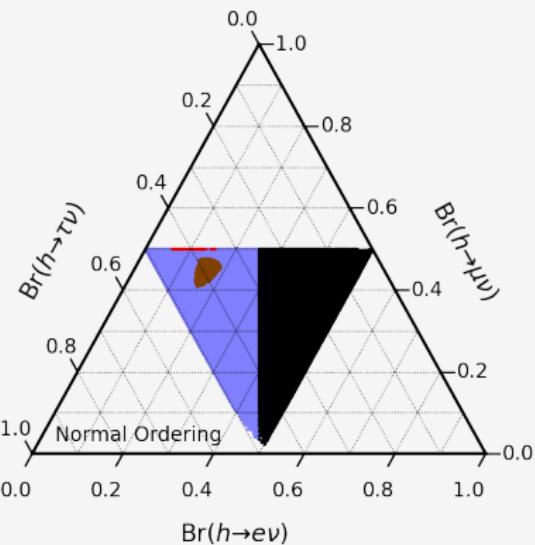


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see 2012.09845

Branching ratios

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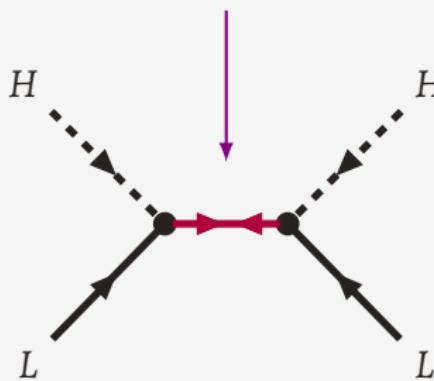
$$Br(h \rightarrow \ell_a \nu) = \frac{\sum_{b \neq a} |y_h^{ab}|^2}{2(|y_h^{e\mu}|^2 + |y_h^{e\tau}|^2 + |y_h^{\mu\tau}|^2)}$$

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Tree level: seesaws

$$\text{SS I: } \bar{N} \sim (1, 1, 0)$$

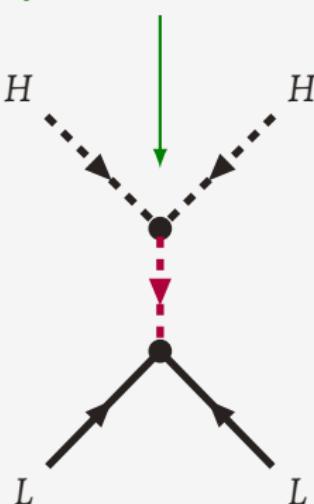
$$yLH\bar{N} + m\bar{N}\bar{N}$$



Minkowski; Yanagida; Glashow;
Gell-Mann, Ramond, Slansky;
Mohapatra, Senjanovic.

$$\text{SS II: } \Delta \sim (1, 2, 1)$$

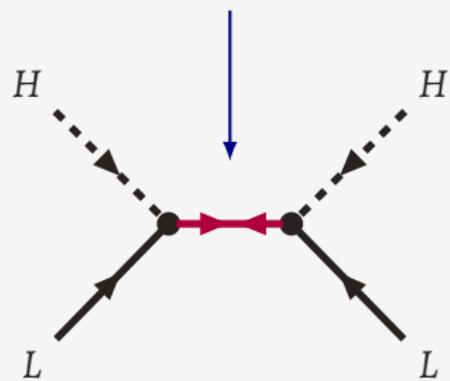
$$yL\Delta L + \mu H\Delta^\dagger H$$



Mohapatra, Senjanovic;
Magg, Wetterich;
Lazarides, Shafi, Wetterich;
Schechter, Valle.

$$\text{SS III: } \bar{\Sigma} \sim (1, 3, 0)$$

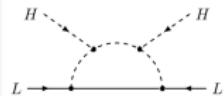
$$yLH\bar{\Sigma} + m\bar{\Sigma}\bar{\Sigma}$$



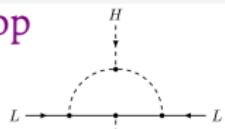
Foot, Lew, He, Joshi.

Loop level models

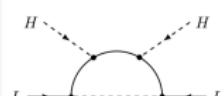
1 loop



(a) T1-i



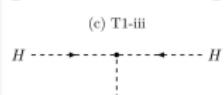
(b) T1-ii



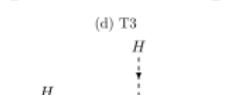
(c) T1-iii



(d) T3

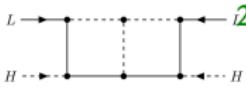


(e) T4-2-i

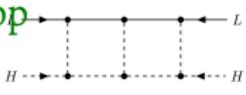


(f) T4-3-i

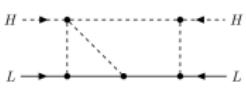
2 loop



(a) CLBZ-1



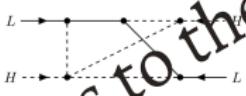
(b) CLBZ-3



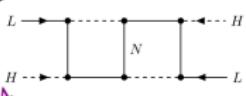
(c) CLBZ-8



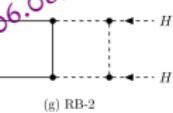
(d) CLBZ-9



(e) CLBZ-10



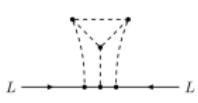
(f) PTBM-1



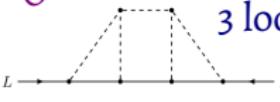
(g) RB-2



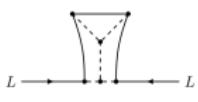
(a) KNT models.



(b) Cocktail models.



(c) AKS models. Cross diagrams may exist.



(d) Fermionic Cocktail models.

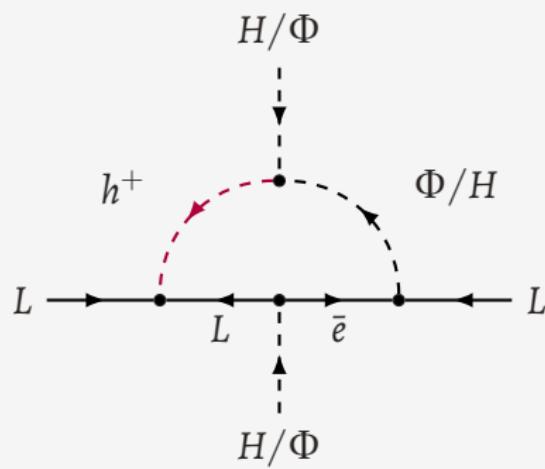
Loop level models: Examples

[Zee, Cheng, Li, Babu]

Singly-charged scalar: $fLLh^+$

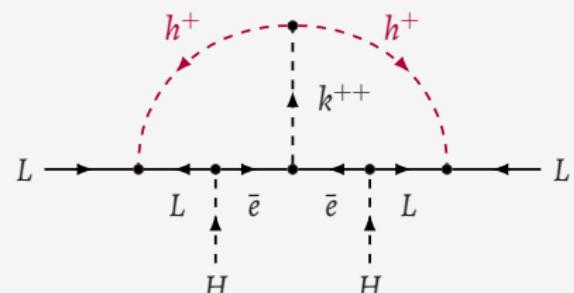
Zee model

$$y\bar{e}\phi^\dagger L + \mu h^{+*} H \phi$$



Zee-Babu model

$$g\bar{e}^\dagger \bar{e}^\dagger k^{++} + \mu h^+ h^+ k^{++*}$$



$\Delta L = 2$ EFT operators [Babu, Leung, De Gouvea, Jenkins]

Zee model Zee-Babu model

$$\begin{array}{lll}
 O_2 = L^i L^j L^k \bar{e} H^l \epsilon_{ij} \epsilon_{kl} & O_{3a} = L^i L^j Q^k \bar{d} H^l \epsilon_{ij} \epsilon_{kl} & O_{3a} = L^i L^j Q^k \bar{d} H^l \epsilon_{ik} \epsilon_{jl} \\
 \downarrow & \cancel{\quad} & \cancel{\quad} \\
 O_{4a} = L^i L^j Q_i^\dagger \bar{u}^\dagger H^k \epsilon_{jk} & O_{4b} = L^i L^j Q_k^\dagger \bar{u}^\dagger H^k \epsilon_{ij} & O_8 = L^i \bar{d} \bar{e}^\dagger \bar{u}^\dagger H^j \epsilon_{ij} \\
 \downarrow & \cancel{\quad} & \cancel{\quad} \\
 O_9 = L^i L^j L^k \bar{e} L^l \bar{e} \epsilon_{ij} \epsilon_{kl} & O_{10} = L^i L^j L^k \bar{e} Q^l \bar{d} \epsilon_{ij} \epsilon_{kl} & \\
 O_{11a} = L^i L^j Q^k \bar{d} Q^l \bar{d} \epsilon_{ij} \epsilon_{kl} & O_{11b} = L^i L^j Q^k \bar{d} Q^l \bar{d} \epsilon_{ik} \epsilon_{jl} & \\
 O_{12a} = L^i L^j Q_i^\dagger \bar{u}^\dagger Q_j^\dagger \bar{u}^\dagger & O_{12b} = L^i L^j Q_k^\dagger \bar{u}^\dagger Q_l^\dagger \bar{u}^\dagger \epsilon_{ij} \epsilon^{kl} & \\
 \dots & & \\
 O_{59} = L^i Q^j \bar{d} \bar{d} \bar{e}^\dagger \bar{u}^\dagger H^k H_i^\dagger \epsilon_{jk} & O_{60} = L^i \bar{d} Q_j^\dagger \bar{u}^\dagger \bar{e}^\dagger \bar{u}^\dagger H^j H_i^\dagger &
 \end{array}$$

operators up to dimension 11 classified

Neutrino masses

Classification in terms of effective $\Delta L = 2$ operators

Babu, Leung hep-ph/0106054; deGouvea, Jenkins 0708.1344 Bonnet, Hernandez, Ota, Winter 0907.3143

$$m_\nu \simeq \frac{c_R v^2}{(16\pi^2)^l \Lambda}, \text{ with } c_R \simeq \prod_i g_i \times \epsilon \times \left(\frac{v^2}{\Lambda^2}\right)^n$$

Loop factor μ/Λ $LLHH(H^\dagger H)^n$

$$m_\nu \gtrsim 0.05 \text{ eV} \Rightarrow \begin{cases} l=1 \rightarrow \Lambda < 10^{12} \text{ GeV} \\ l=2 \rightarrow \Lambda < 10^{10} \text{ GeV} \\ l=3 \rightarrow \Lambda < 10^8 \text{ GeV} \end{cases}$$

→ no information on $\Delta L = 0$ processes

Systematic construction of models

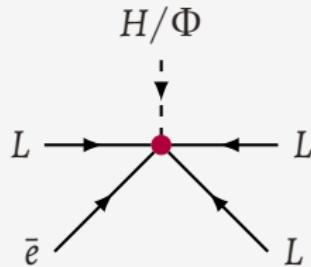
Angel, Rodd, Volkas 1212.5862; Cai, Clarke, MS, Volkas 1308.0463; Gargalionis, Volkas 2009.13537

Bonnet, Hirsch, Ota, Winter 1204.5862; Aristizabal Sierra, Degee, Dorame, Hirsch 1411.7038; Cepedello, Fonseca, Hirsch 1807.00629

Gargalionis, Volkas 2009.13537: "exploding! $\Delta L = 2$ operators" ... "1000s of models"

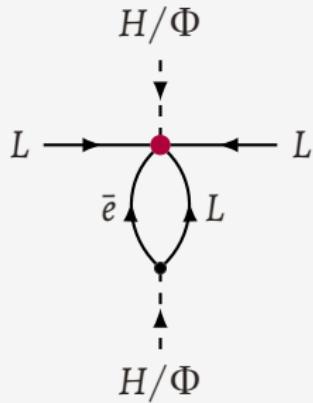
→ a large number of models!

EFT estimate for \mathcal{O}_2



Operator

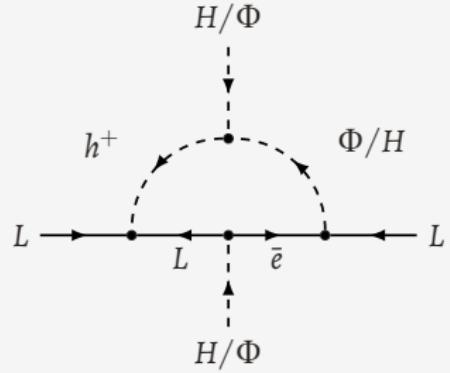
$$\mathcal{O}_2 = LLL\bar{e}H$$



Estimate

$$m_\nu \simeq \frac{1}{16\pi^2} \frac{\text{chirality flip } y_\tau}{y_\tau} \frac{c_2 v^2}{\Lambda}$$

loop factor $\frac{1}{16\pi^2}$



UV model: Zee

$$m_\nu \simeq \frac{fm_\tau^2 \mu}{16\pi^2 m_{h^+}^2}$$