

# IMPROVING THE SENSITIVITY TO LIGHT DARK MATTER WITH THE MIGDAL EFFECT



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based on: G<sup>2</sup>dC, Andrea Messina, Stefano Piacentini, Migdal effect and photon Bremsstrahlung: improving the sensitivity to light dark matter of liquid argon experiments, JHEP 11 (2020) 034, arXiv: 2006.02453

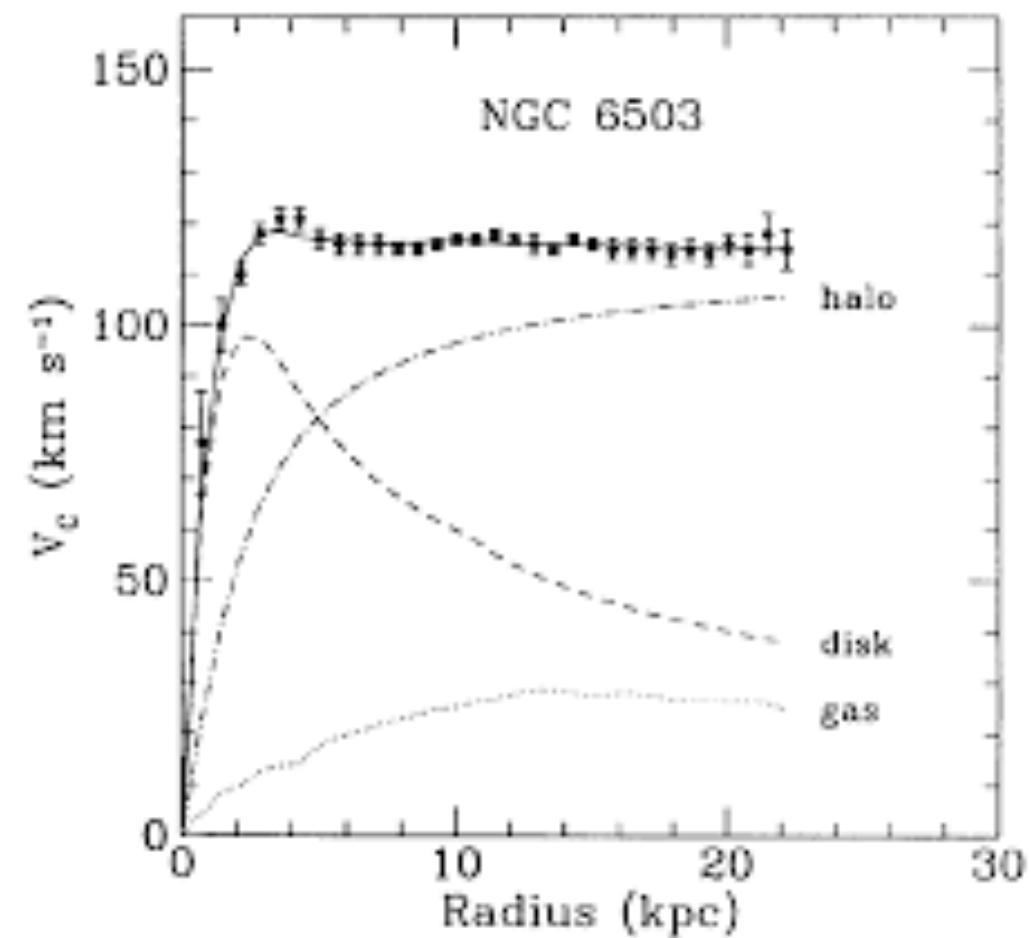
# Outline

- Introduction and motivation
- The Migdal effect
- Impact of the Migdal effect in LAr experiments
- Detecting the Migdal effect in nuclear scattering
- Conclusions

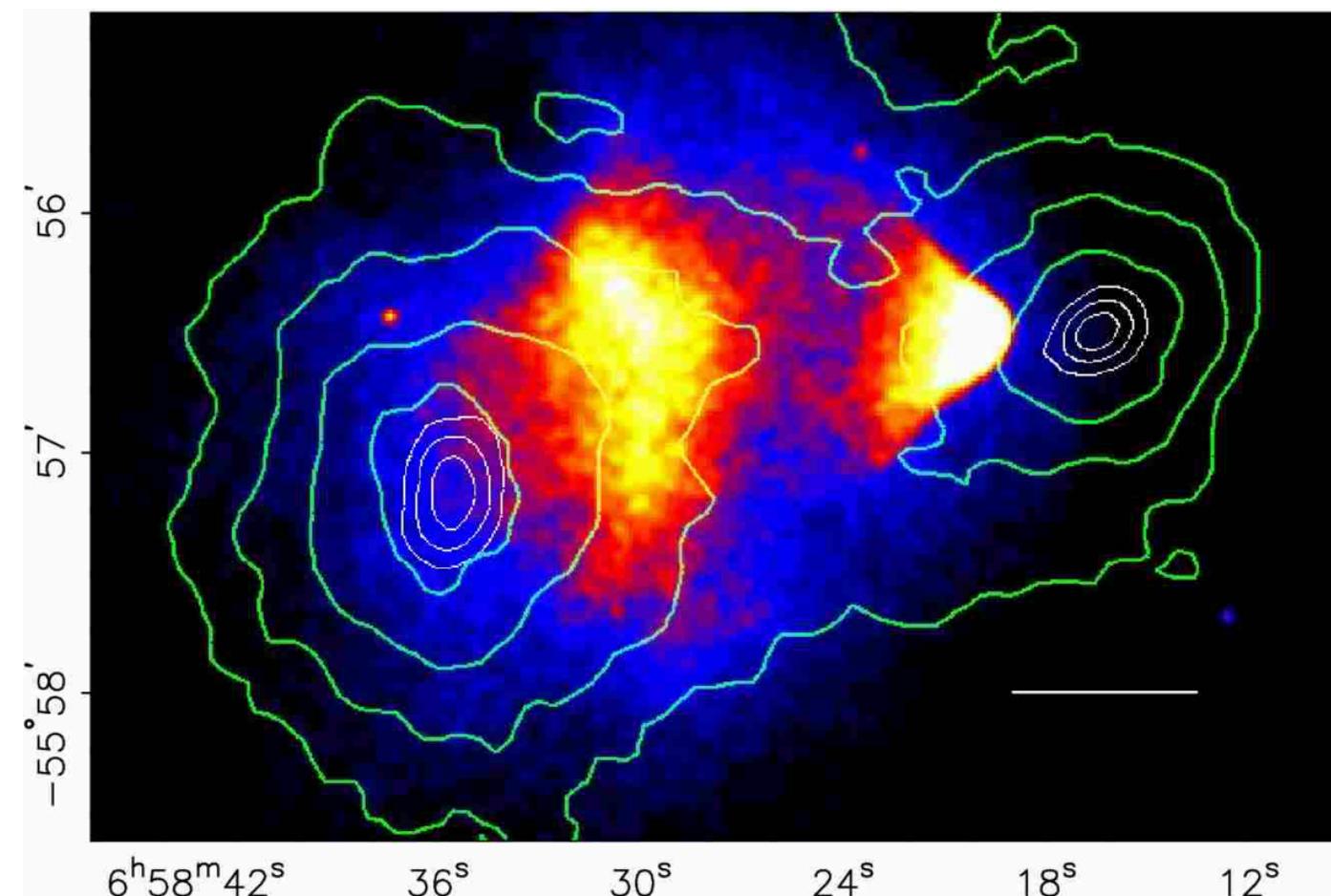
# Introduction

# Introduction and motivation

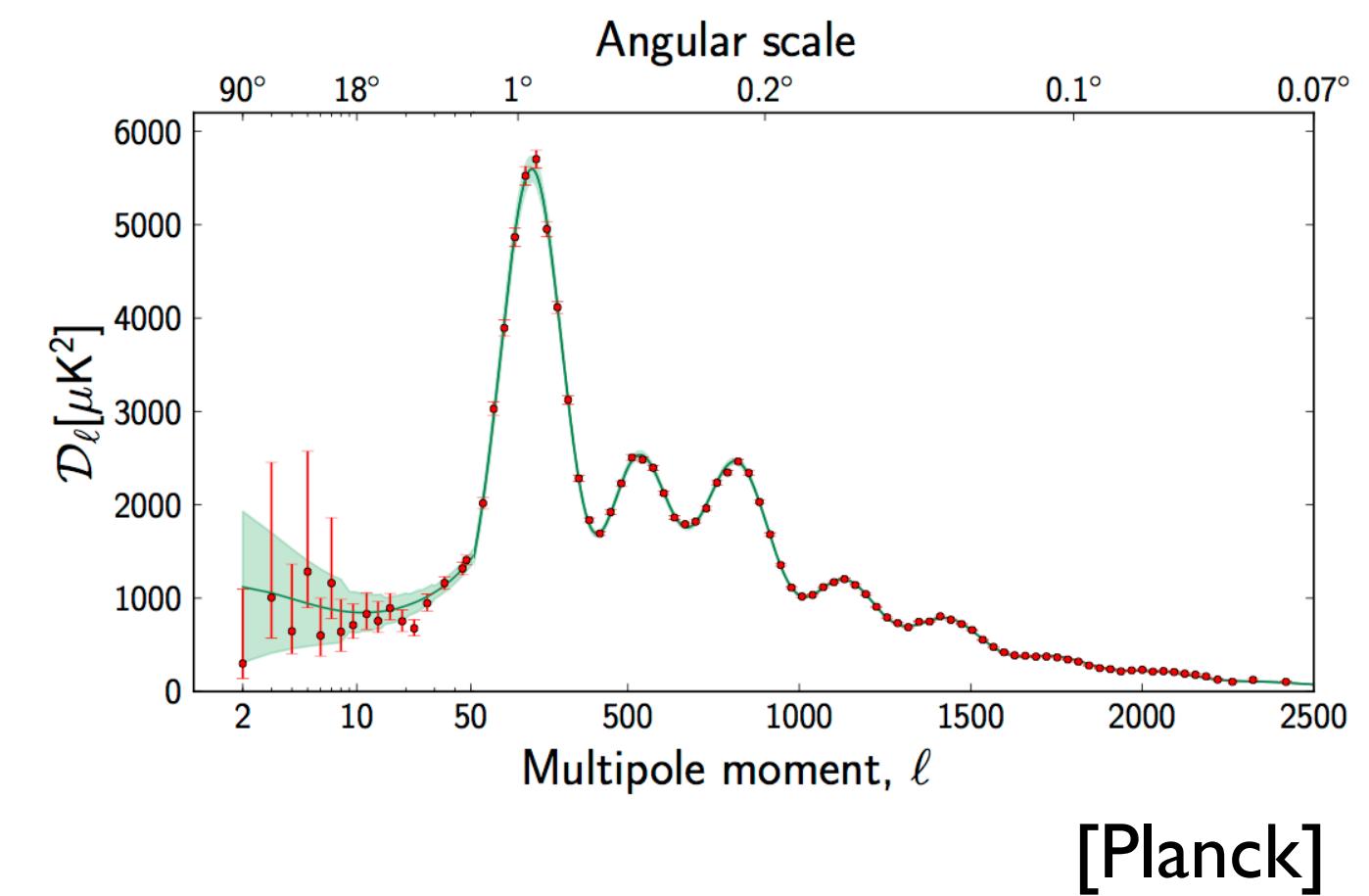
Galaxies



Clusters



Cosmic Microwave Background



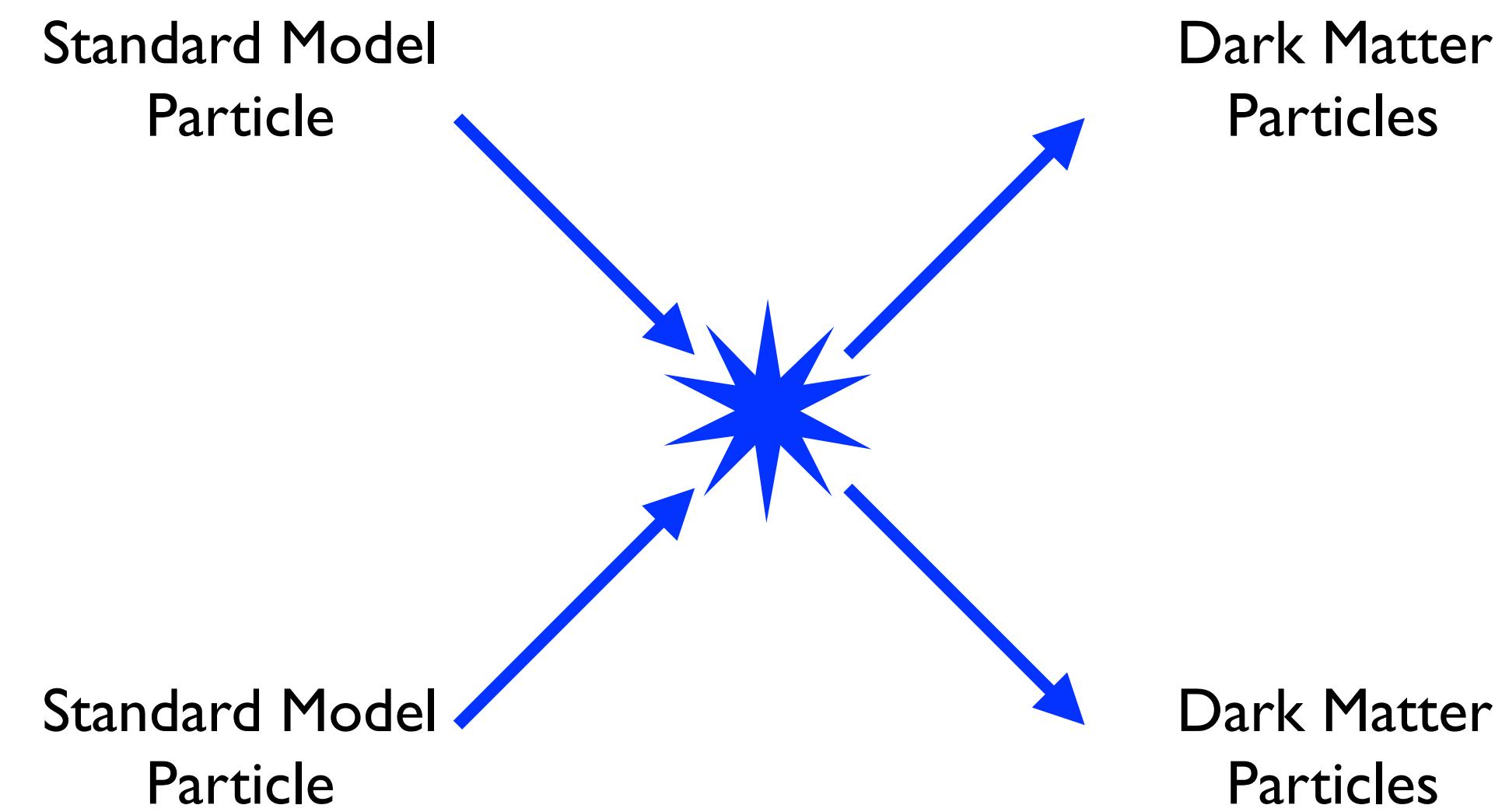
[Clowe et al., APJL 648 (2006) L109-L113]

Small scales

Large scales

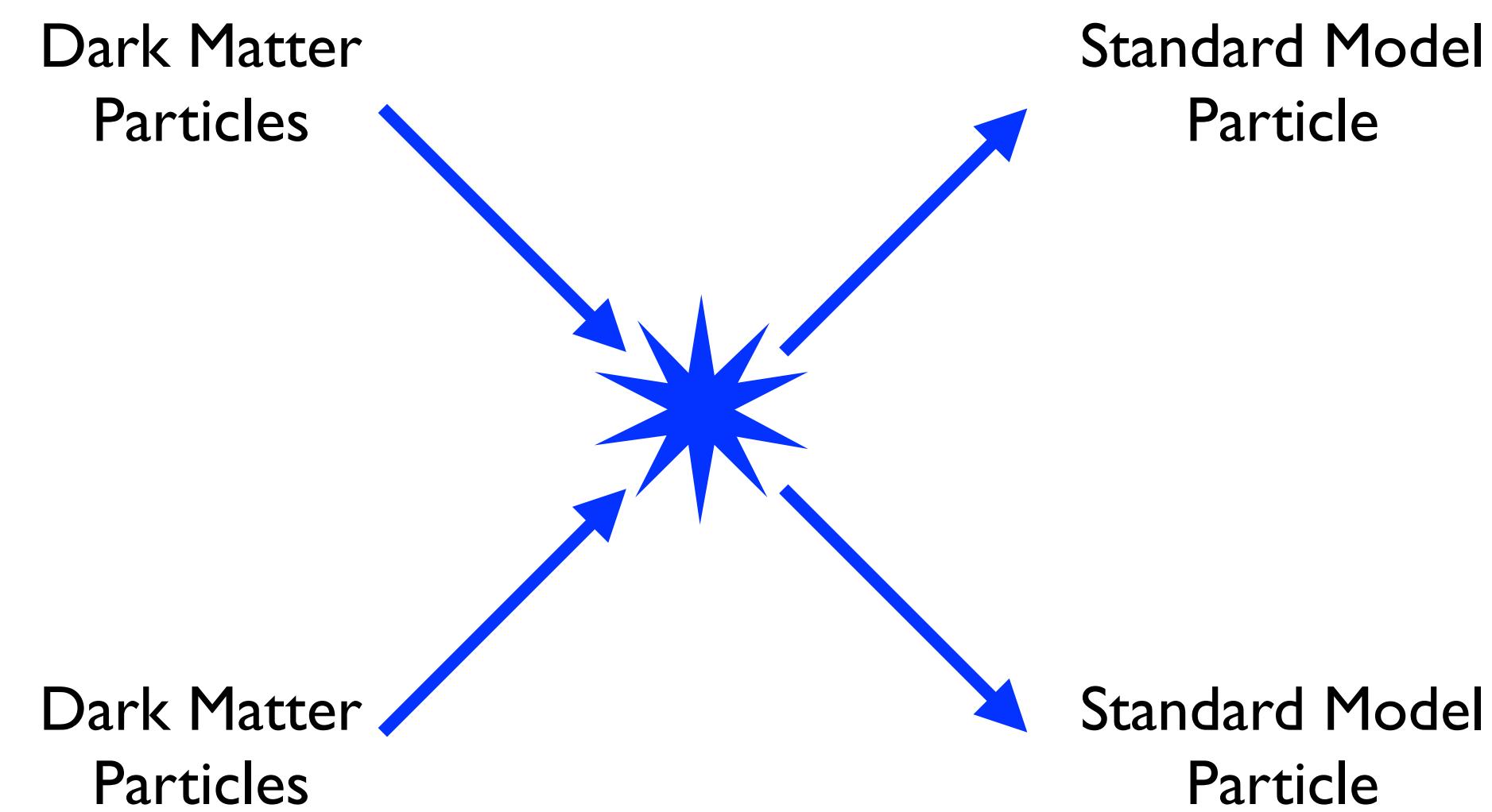
# Introduction and motivation

## Colliders



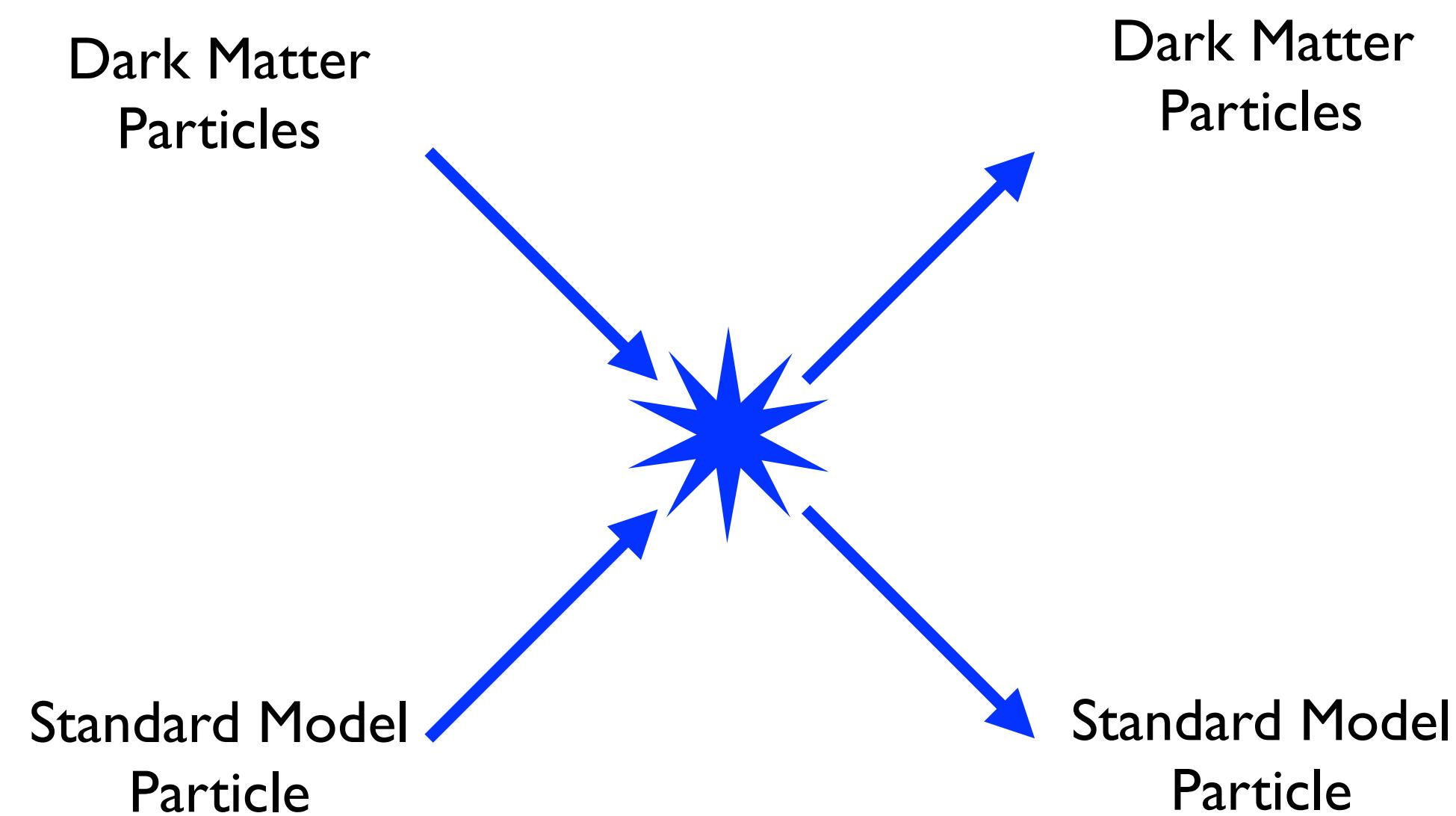
# Introduction and motivation

## Indirect detection

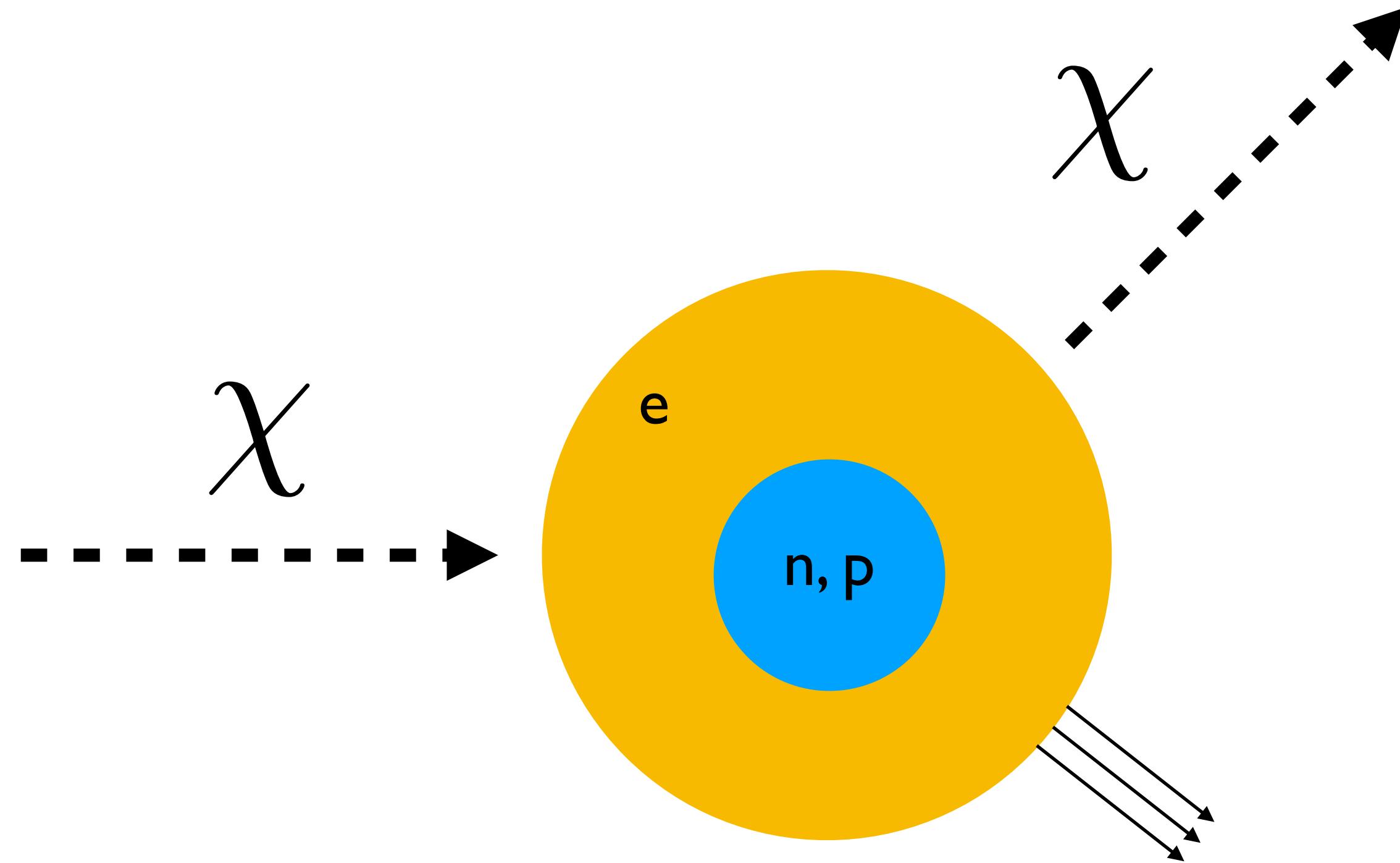


# Introduction and motivation

## Direct detection

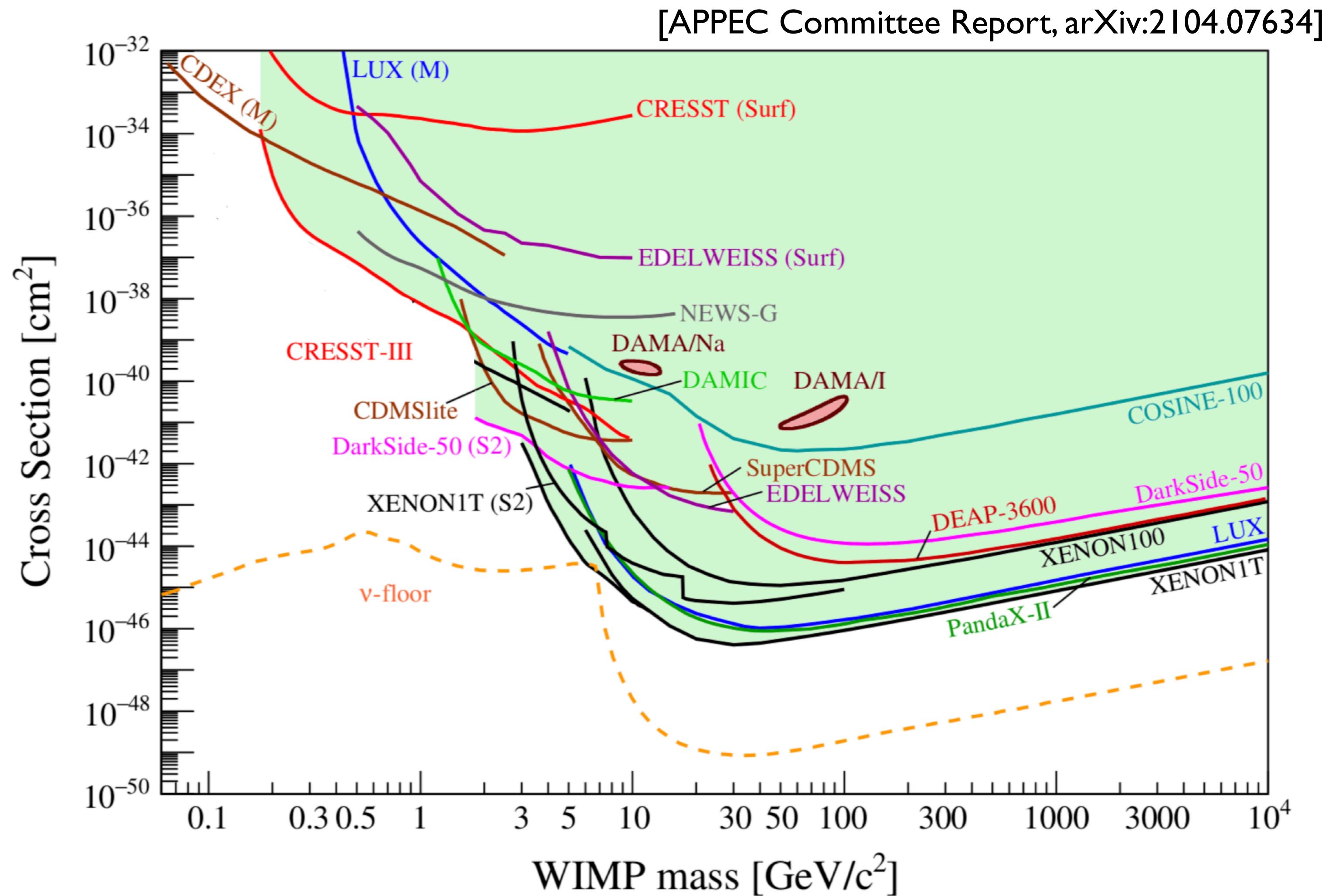


# Direct detection

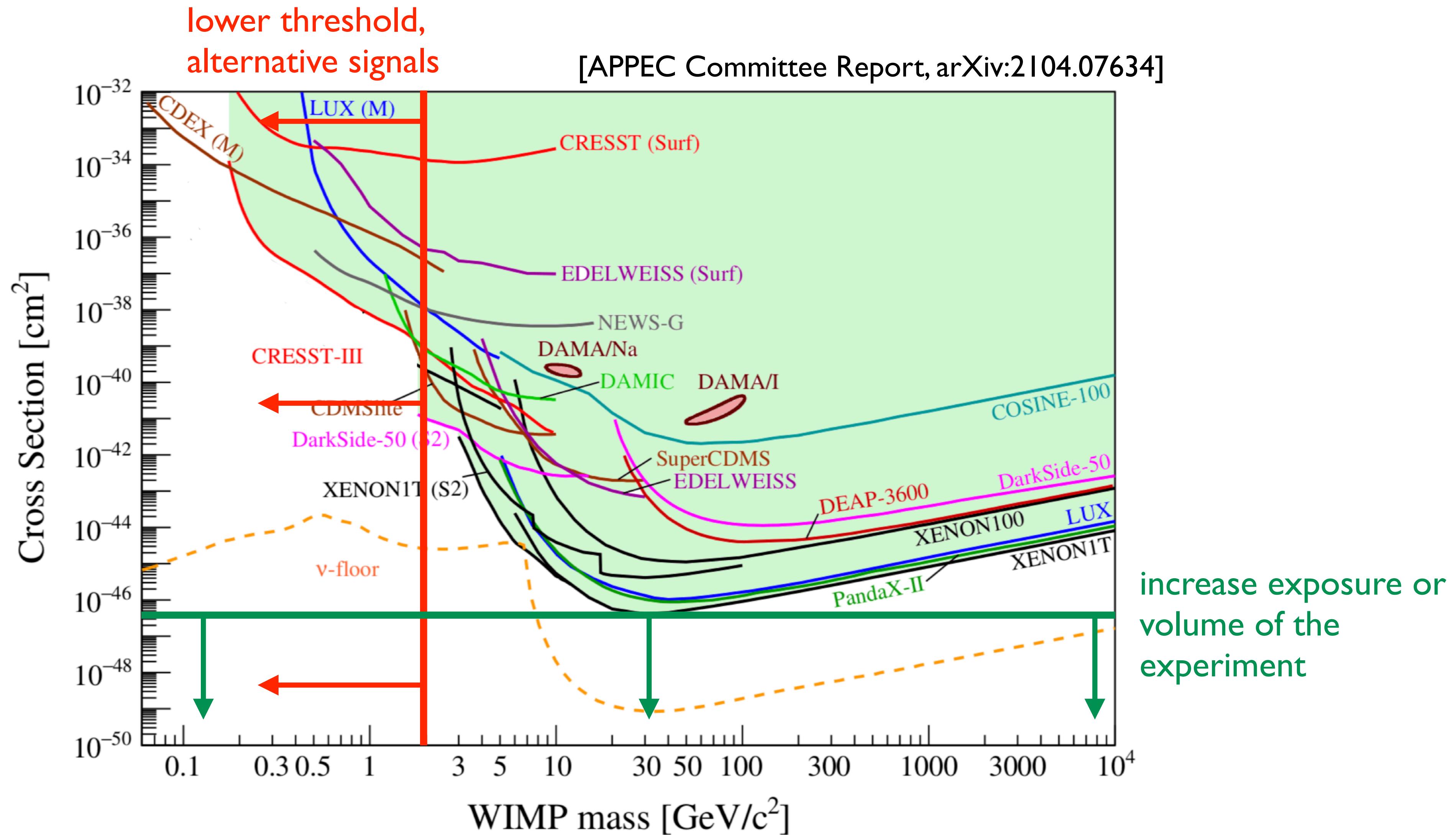


$$\frac{dR}{dE_R} = \frac{\rho_0 M_{\text{det}}}{m_N m_\chi} \int_{v > v_{\min}} v f(v) \frac{d\sigma}{dE_R} dv$$

# Direct detection

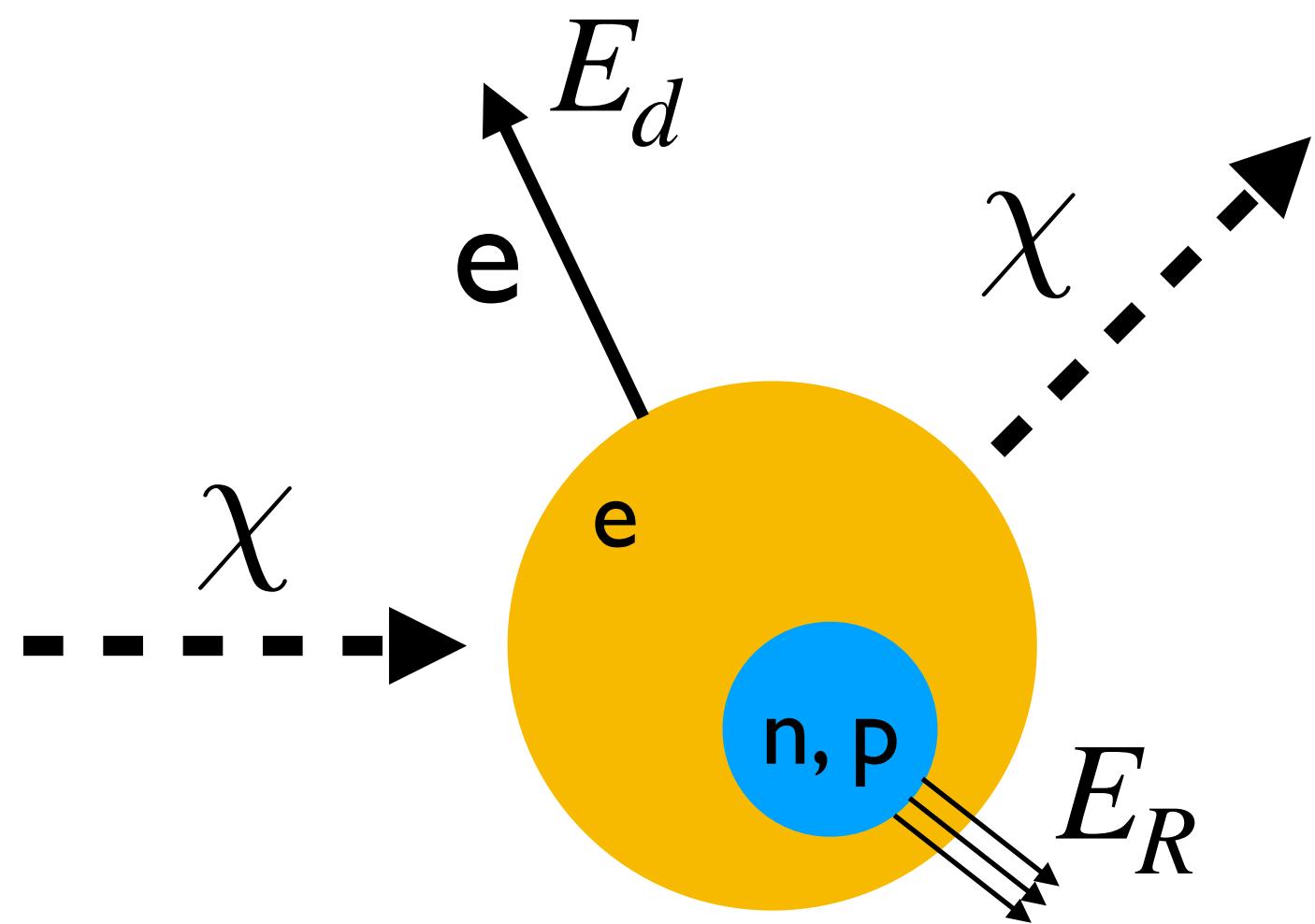


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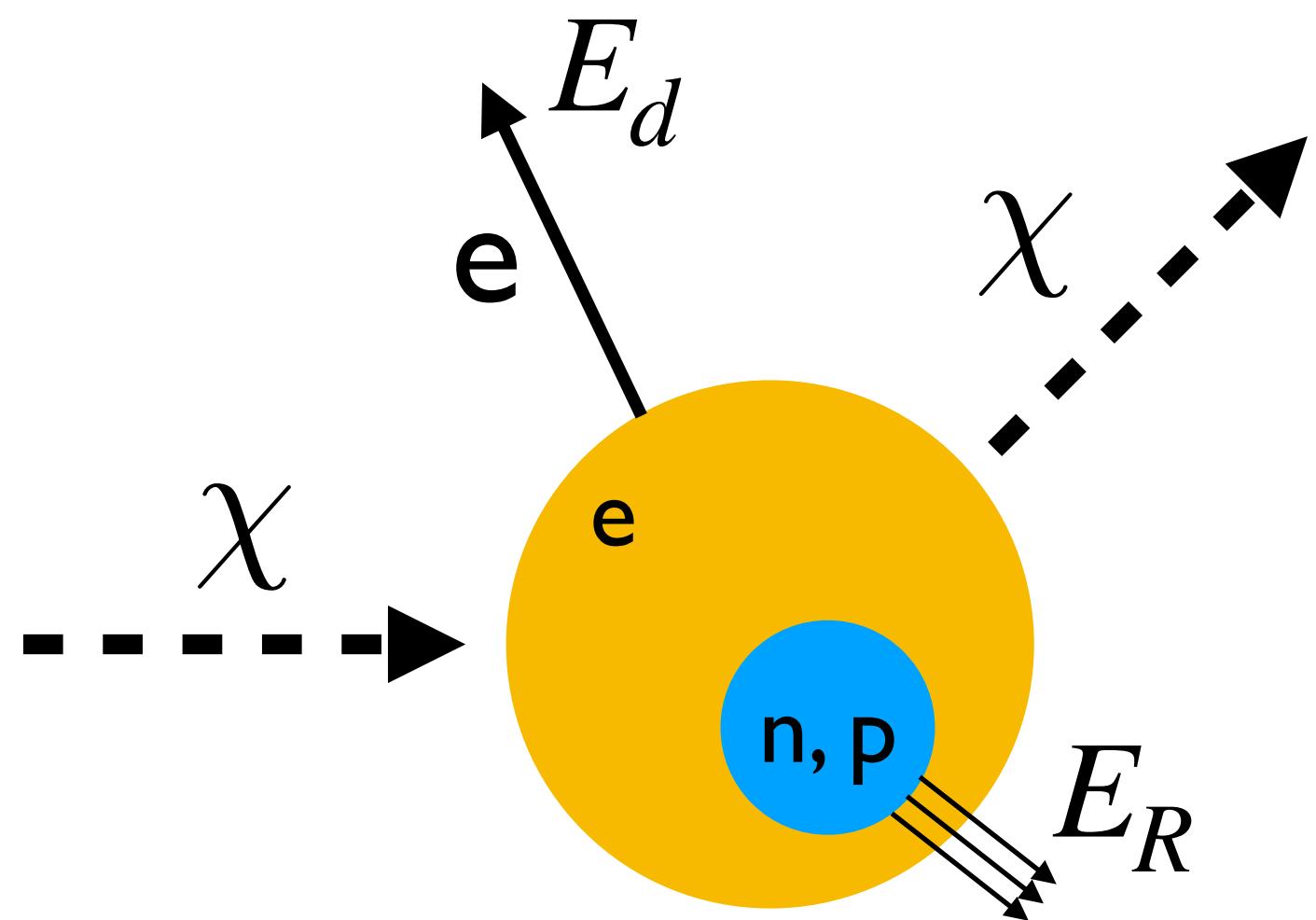


# The Migdal effect

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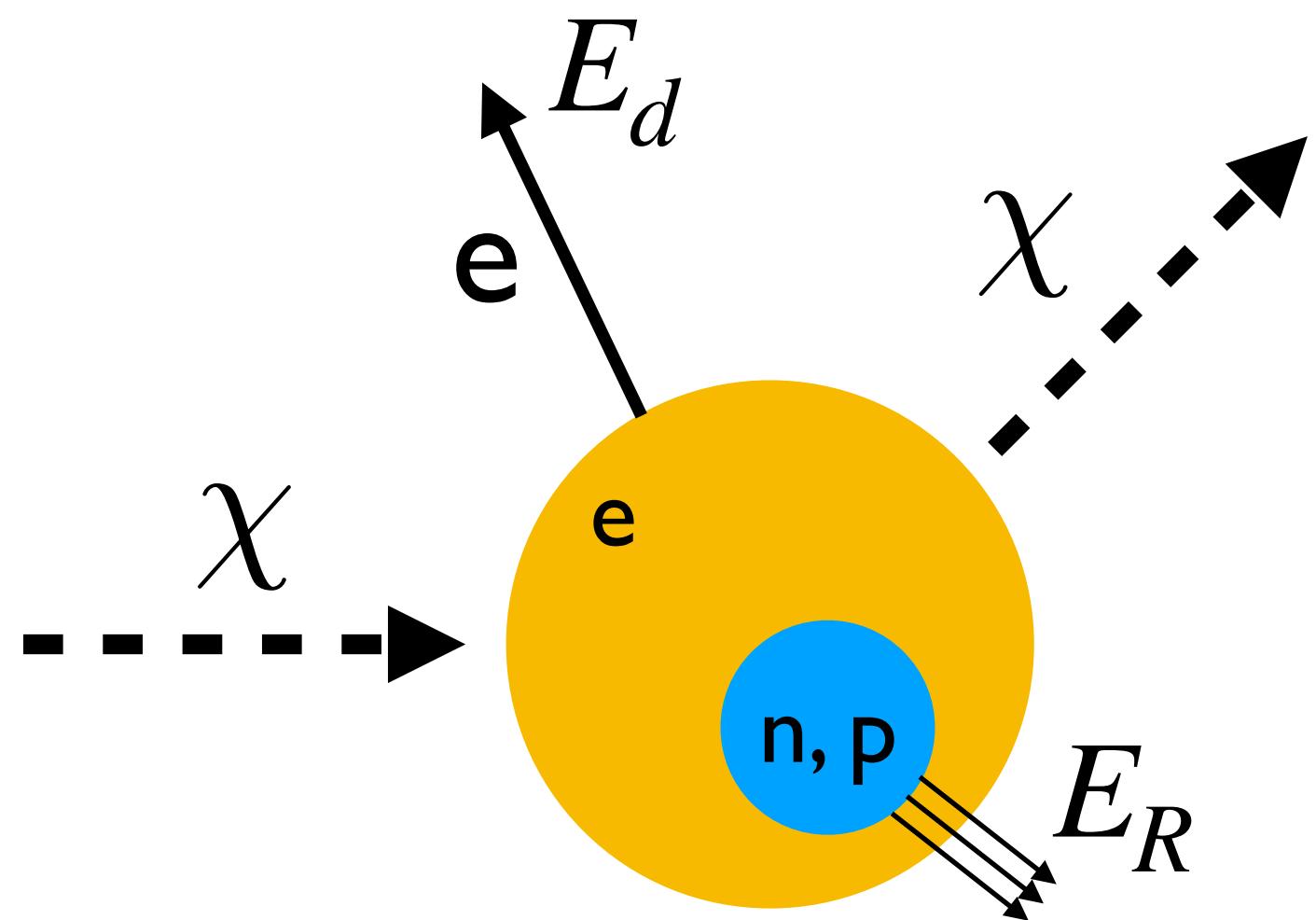
Kinematics

$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu_N^2}} + \frac{E_d}{\sqrt{2m_N E_R}}$$

$$E_R^{\max} = \frac{2\mu_N^2 v_{\max}^2}{m_N}$$

$$E_d^{\max} = \frac{\mu_N v_{\max}^2}{2}$$

# The Migdal effect



## Kinematics

Nuclear recoil energy

$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu_N^2}} + \frac{E_d}{\sqrt{2m_N E_R}}$$

Electron detected energy

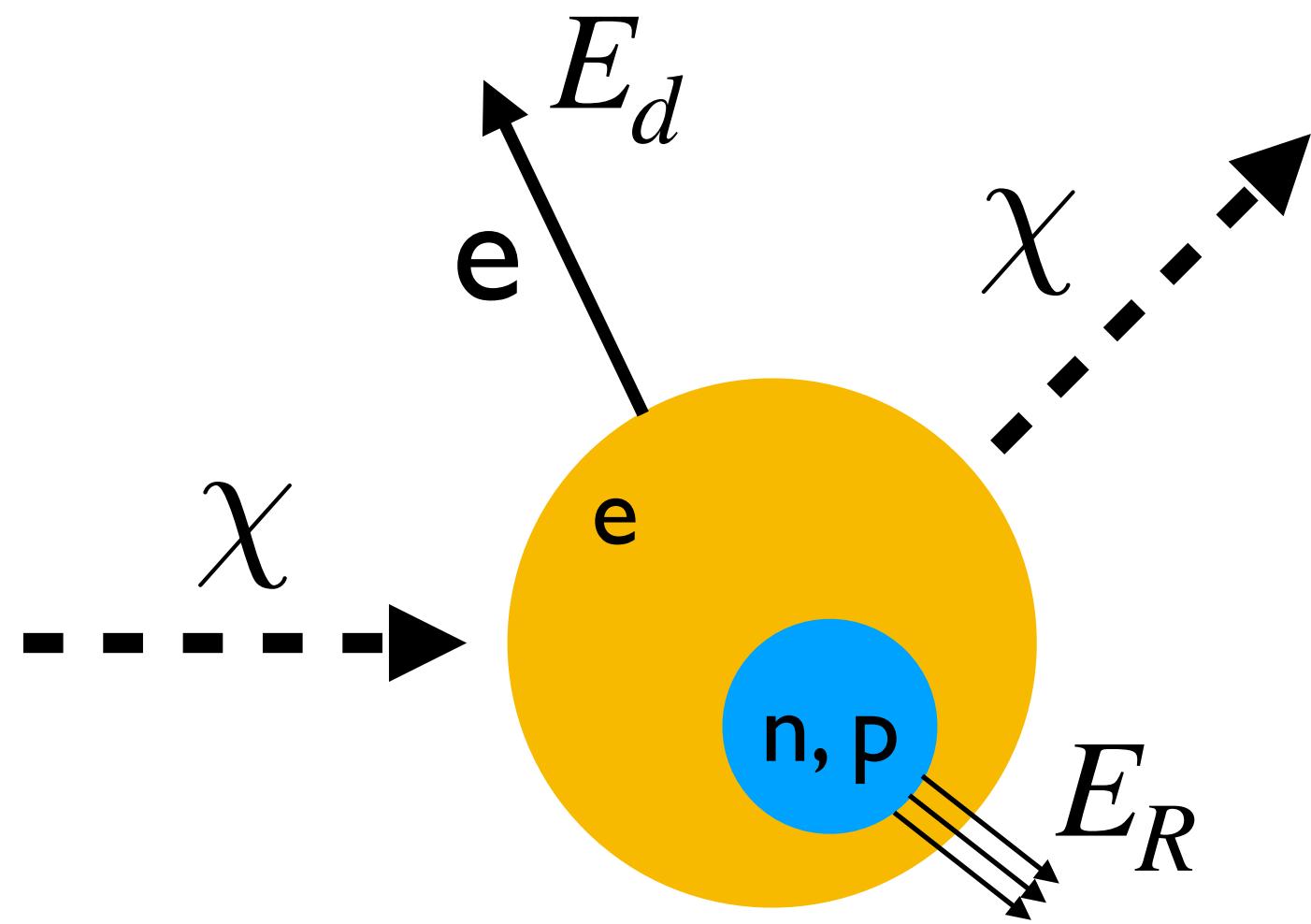
DM-nucleus reduced mass

nucleus mass

$$E_R^{\max} = \frac{2\mu_N^2 v_{\max}^2}{m_N}$$

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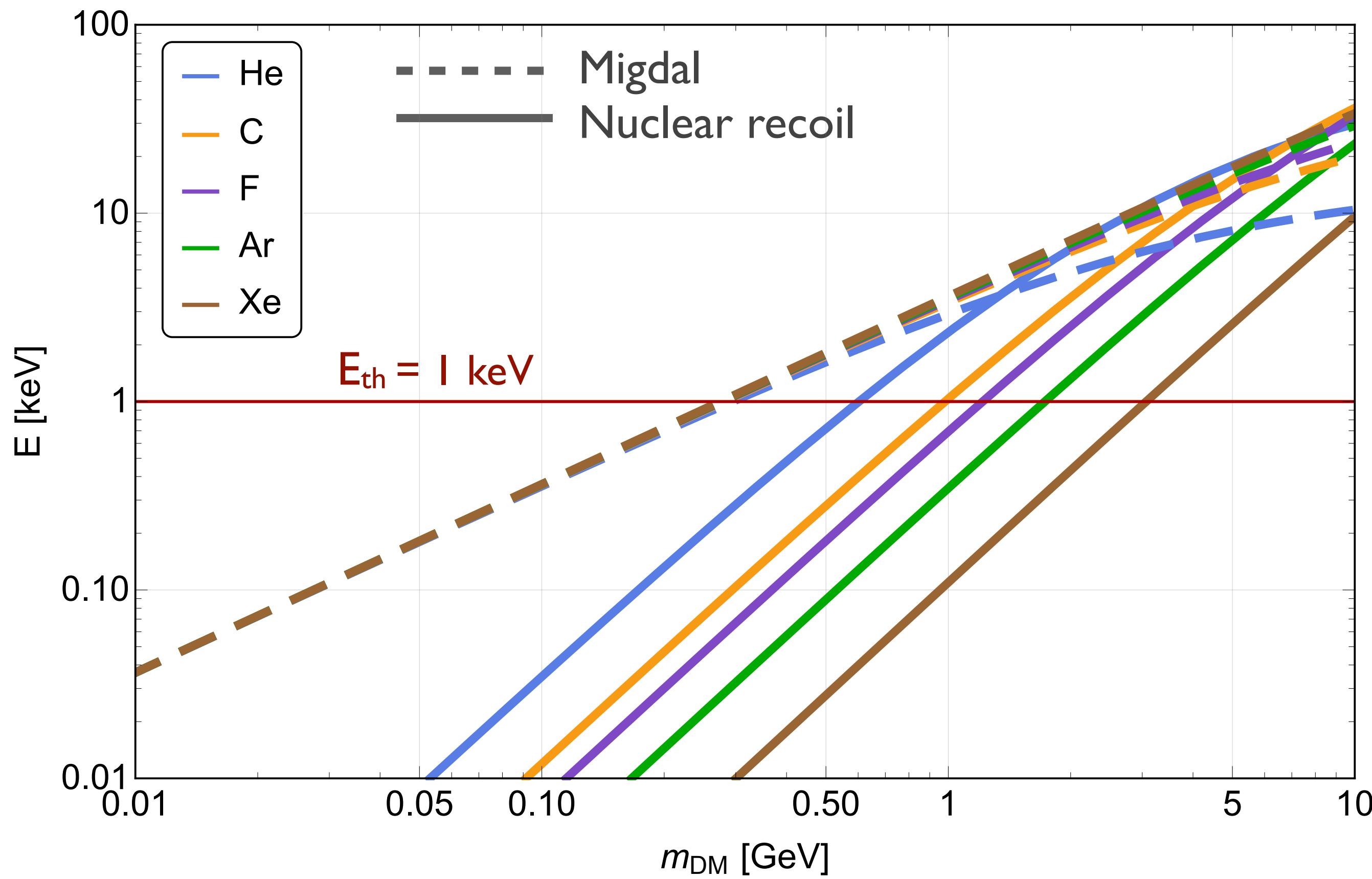


1. Threshold  $E \lesssim 1 \text{ keV}$
2. Sensitivity loss for  $m_{DM} \lesssim 2 \text{ GeV}$
3.  $E_d^{\max} > E_R^{\max}$  for  $m_{DM} \ll m_N$
4. The Migdal effect is sensitive to sub-GeV masses

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NR de-excitation: negligible

ionization rate

$$|Z(E_R, E_e)|^2 \simeq 1 + |Z_{de}|^2 + |Z_{ion}|^2$$

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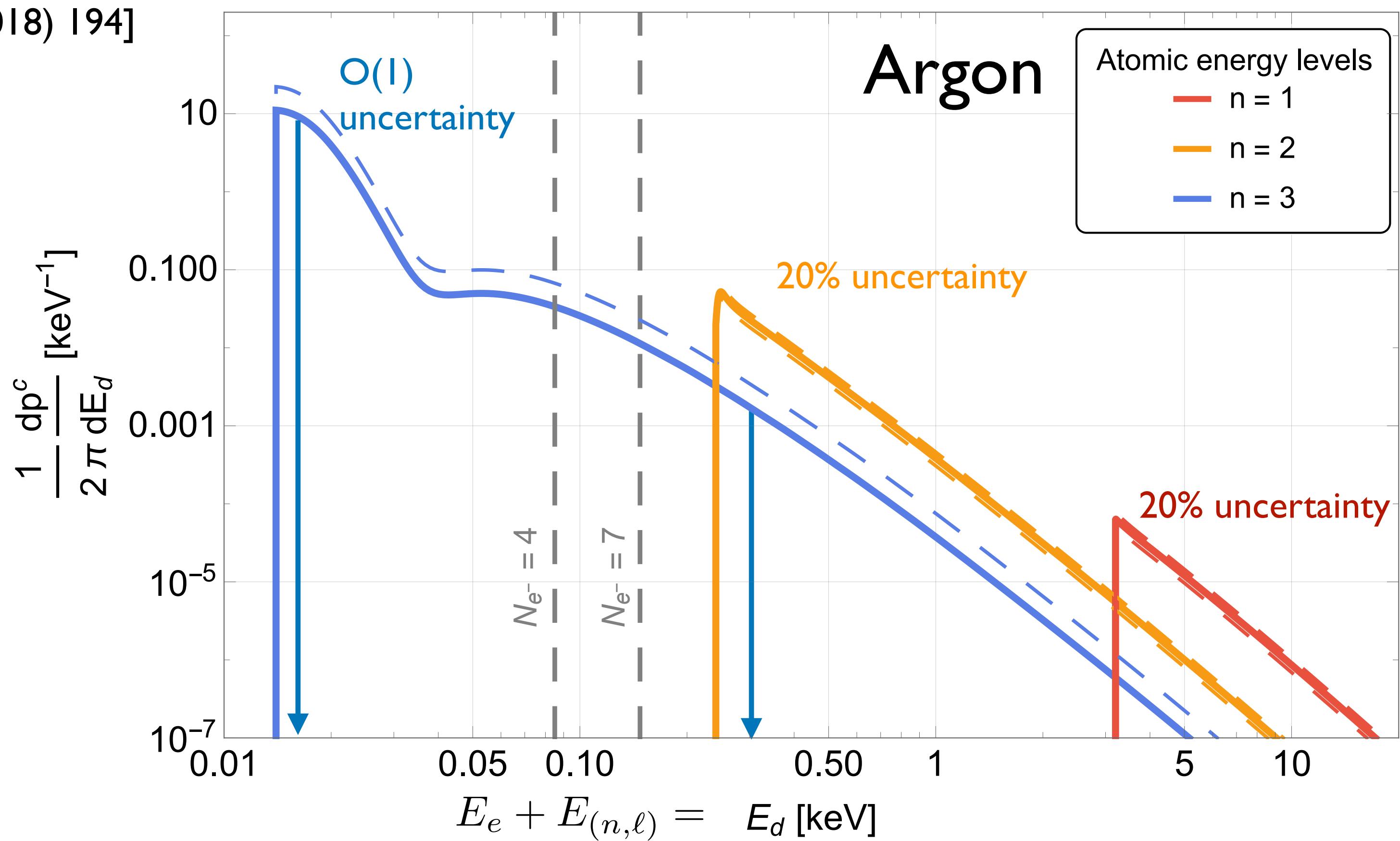
$$|Z_{ion}(E_R, E_e)|^2 = \frac{1}{2\pi} \sum_{n,\ell} \int dE_e \frac{dp_{qe}^c(n\ell \rightarrow E_e)}{dE_e}$$

Migdal

Computed in  
[Ibe et al. JHEP03(2018)194]

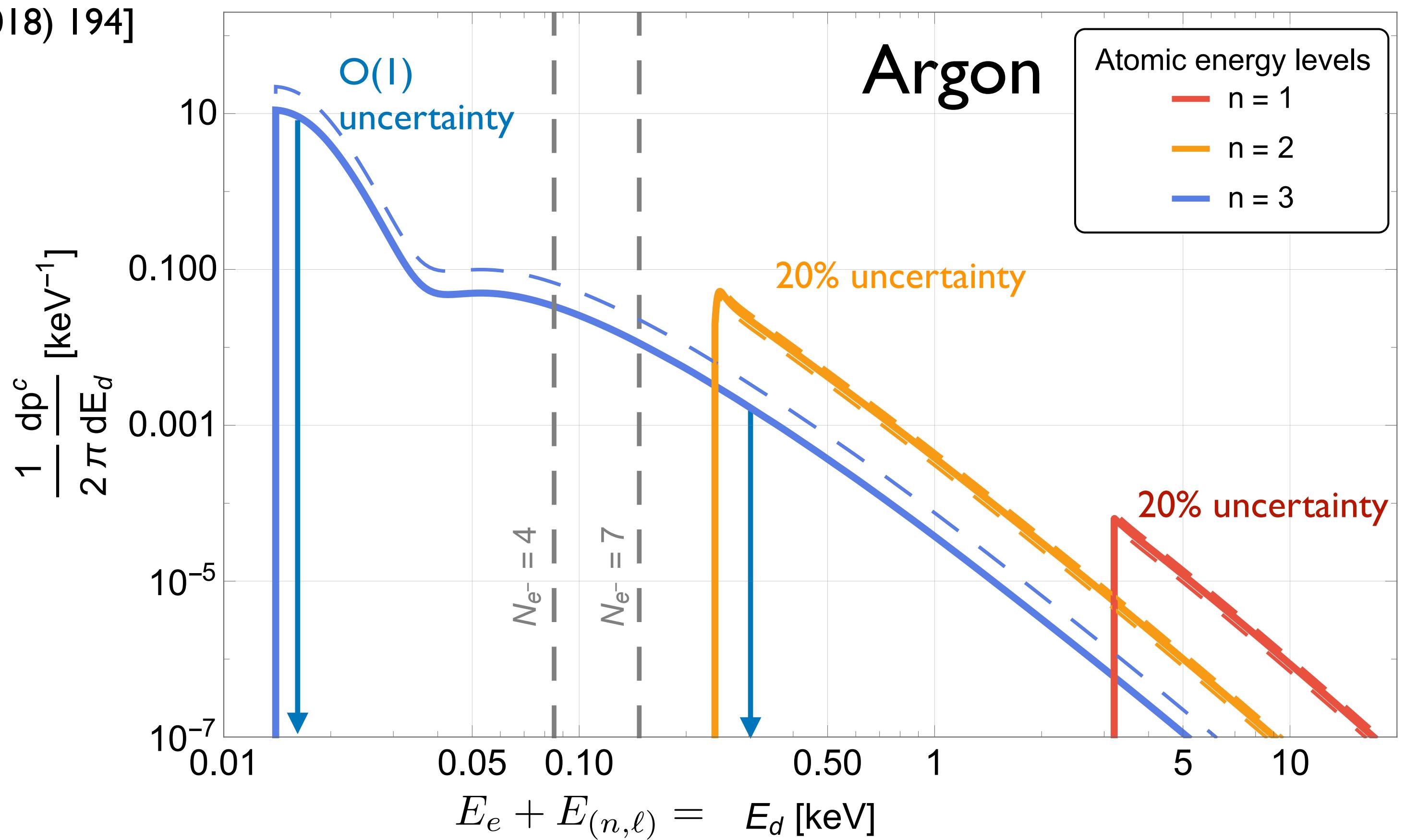
# The Migdal effect

- Computed by [Ibe et al., JHEP 03 (2018) 194] for isolated atoms using the Flexible Atomic Code [Gu, Canadian Journal of Physics 86(2008)675];



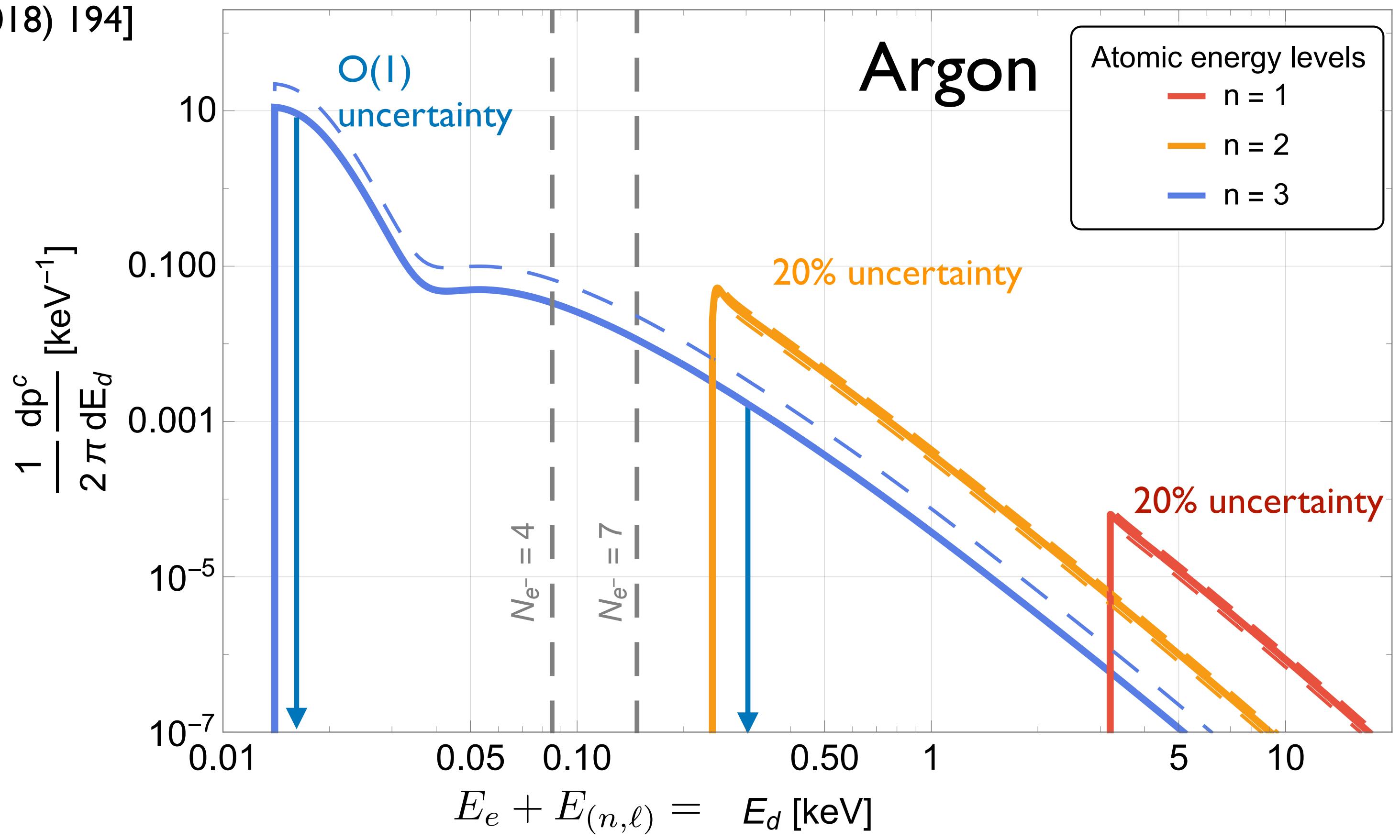
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- The outer shell is potentially affected by large uncertainties;
- The Migdal emission can be rigorously related to photo-absorption, thus relating the probability to experimental input and reducing the theoretical uncertainties [Liu et al., Phys. Rev. D 102 (2020) 121303]



# Migdal effect in LAr

# LAr simulated experiment

Inputs:

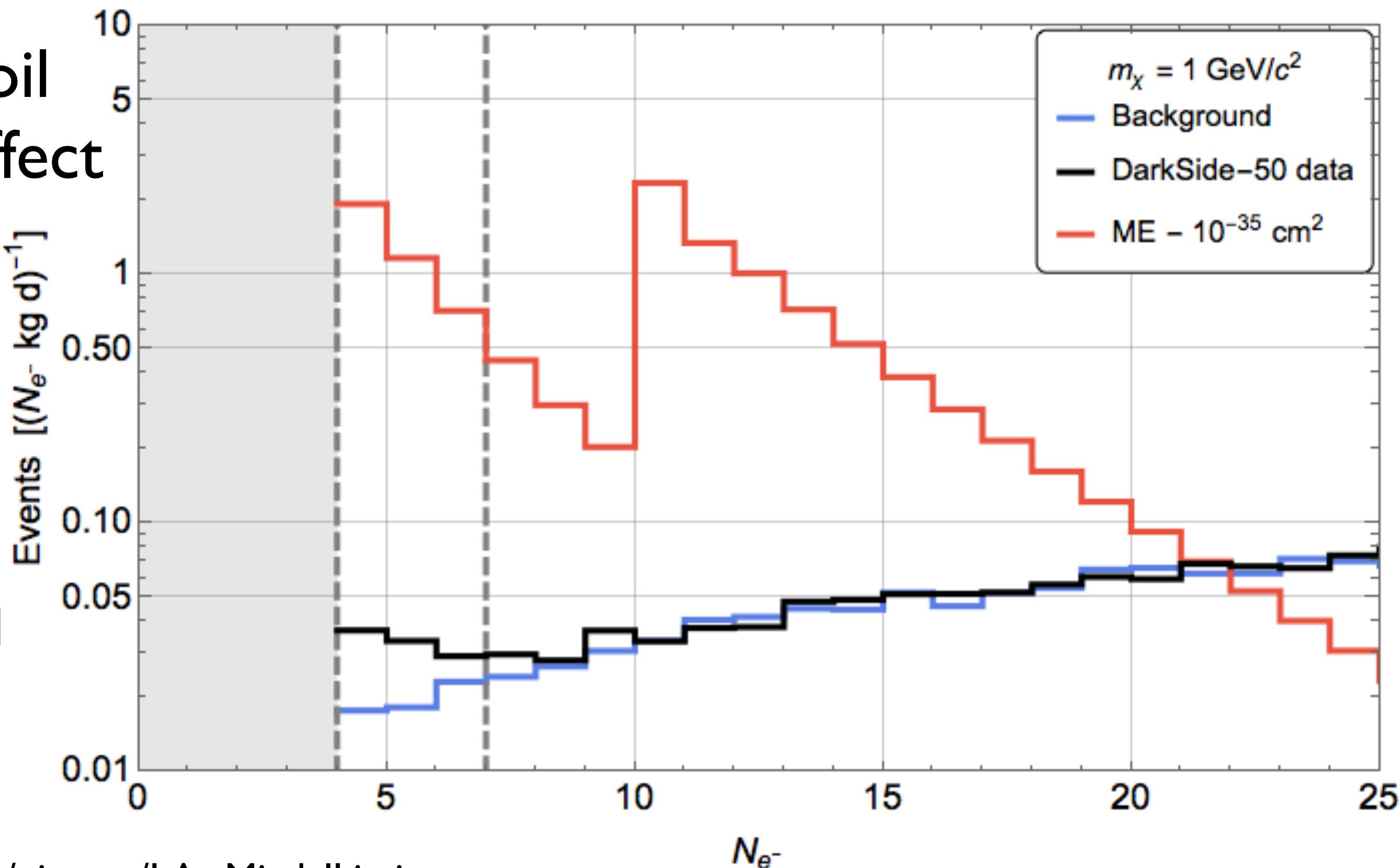
- **Signal templates** (nuclear recoil and Migdal) and systematic effect treatment;

- Realistic LAr spectra and parametrisation of detector effects;

[DarkSide, Phys. Rev. Lett. 121 (2018) no. 8081307]

- Bayesian statistical analysis to extract the sensitivity curves;

Public repository at: <https://github.com/piacent/LAr-MigdalLimits>



# Bayesian analysis

$$\mathcal{L} = \mathcal{L}_C \times \mathcal{L}_B \times \mathcal{L}_S$$

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$$\lambda_i = E[r_S S_i + r_B (B_i + \text{Low} N_{e_i})]$$

# Bayesian analysis

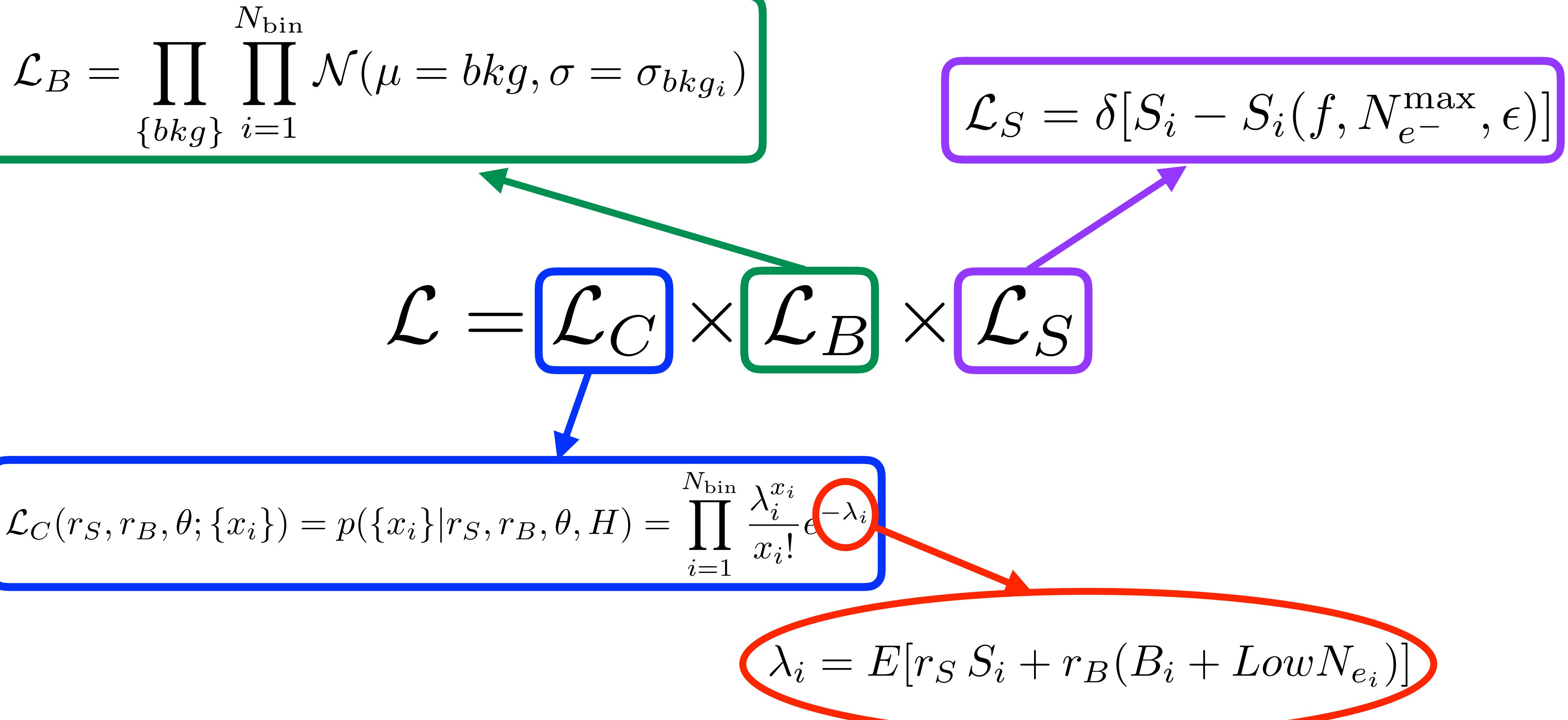
$$\mathcal{L}_B = \prod_{\{bkg\}} \prod_{i=1}^{N_{\text{bin}}} \mathcal{N}(\mu = bkg, \sigma = \sigma_{bkg_i})$$

$$\mathcal{L} = \boxed{\mathcal{L}_C} \times \boxed{\mathcal{L}_B} \times \mathcal{L}_S$$

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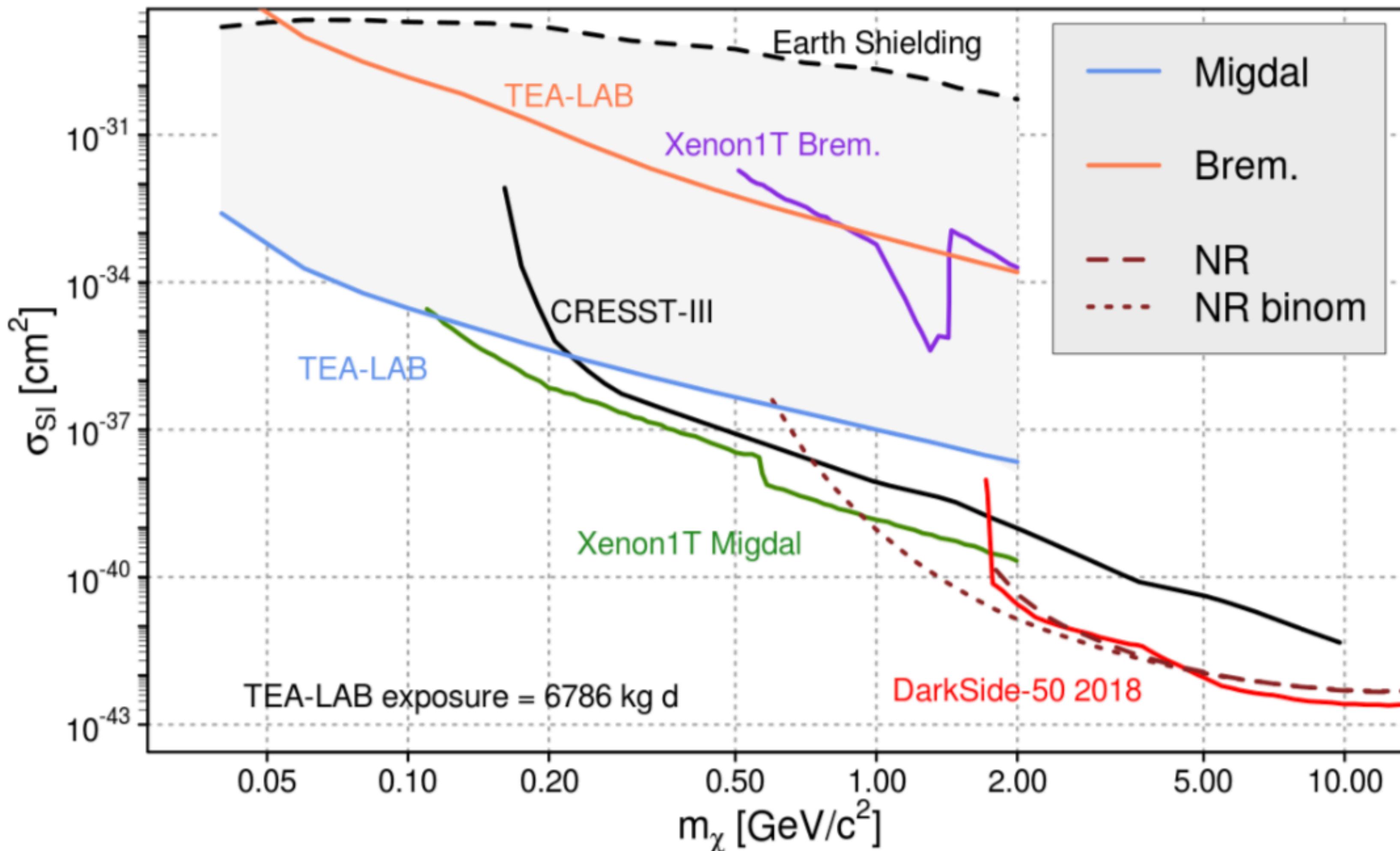
$$\lambda_i = E[r_S S_i + r_B (B_i + \text{Low} N_{e_i})]$$

# Bayesian analysis



# Expected sensitivity

Expected sensitivity: TEA-LAB simulation (bkg + LowNe) with  $N_e^- \geq 4$

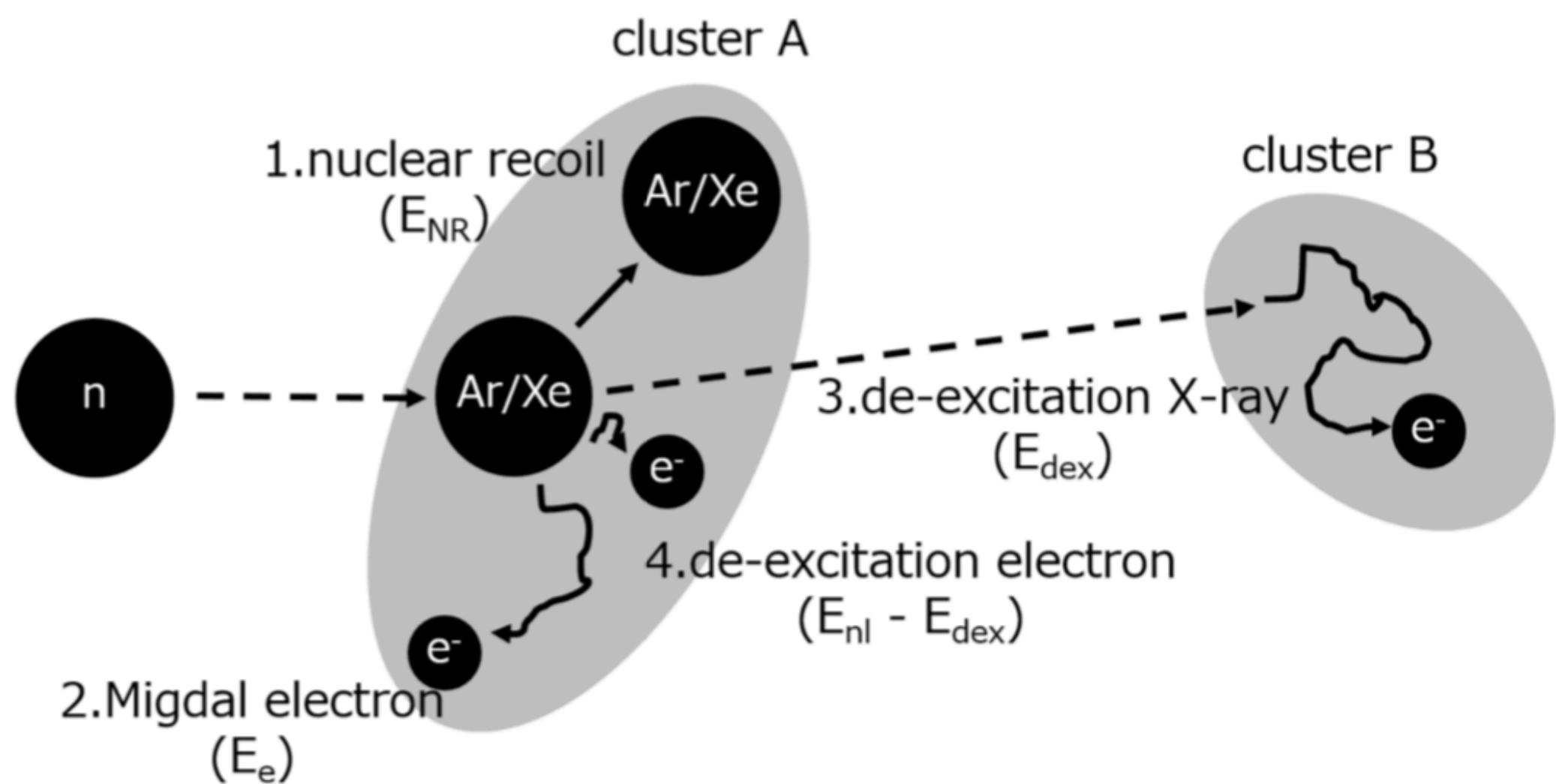


How to measure the Migdal  
effect in nuclear scattering?

# Possible signatures

I. Neutrons can induce energetic NR;

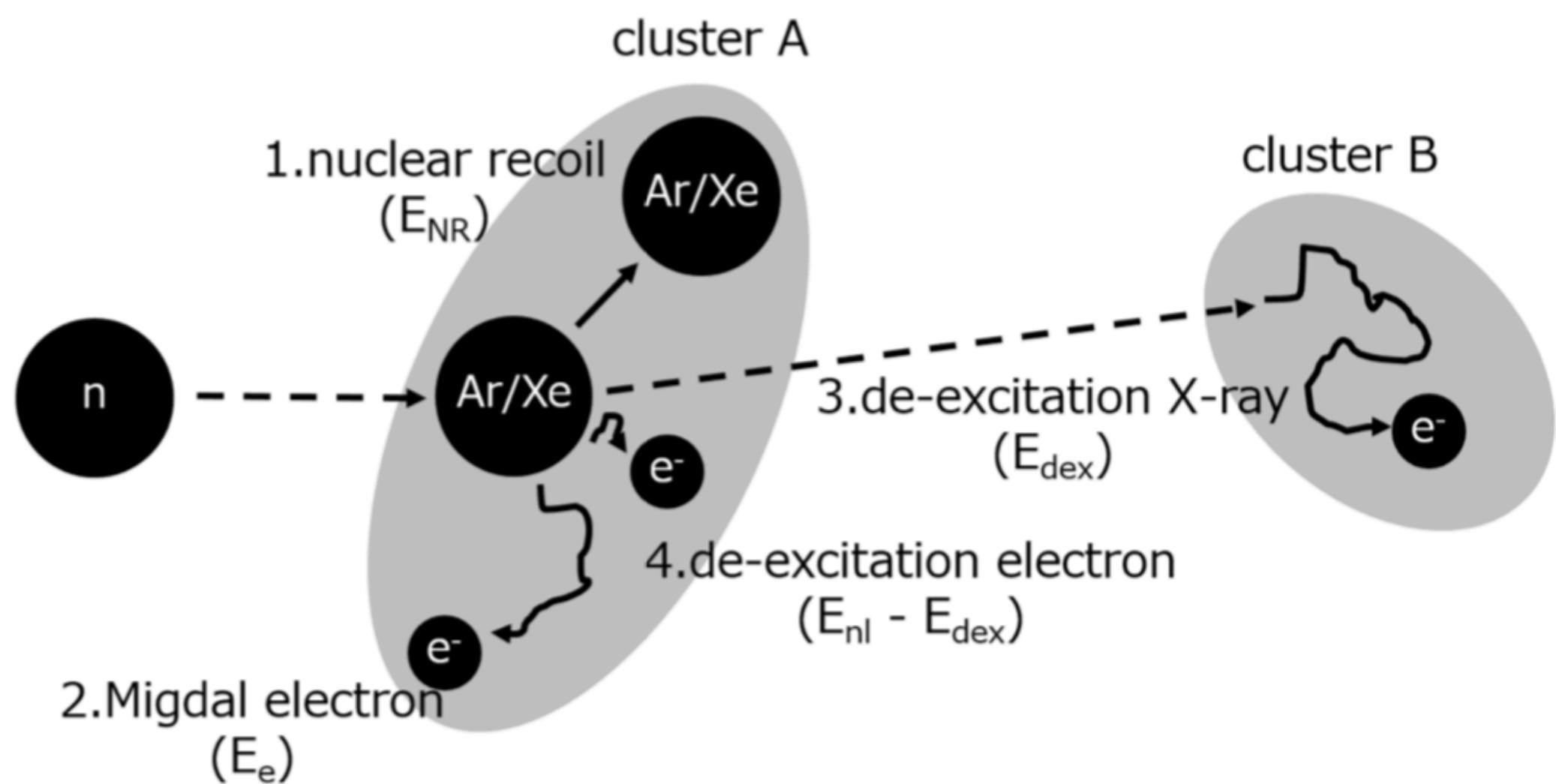
[Nakamura et al., PTEP I (2021) 013C01]



# Possible signatures

1. Neutrons can induce energetic NR;
2. An atom can emit a Migdal electron from the 1s shell with a small probability ( $10^{-5}$ - $10^{-4}$ );

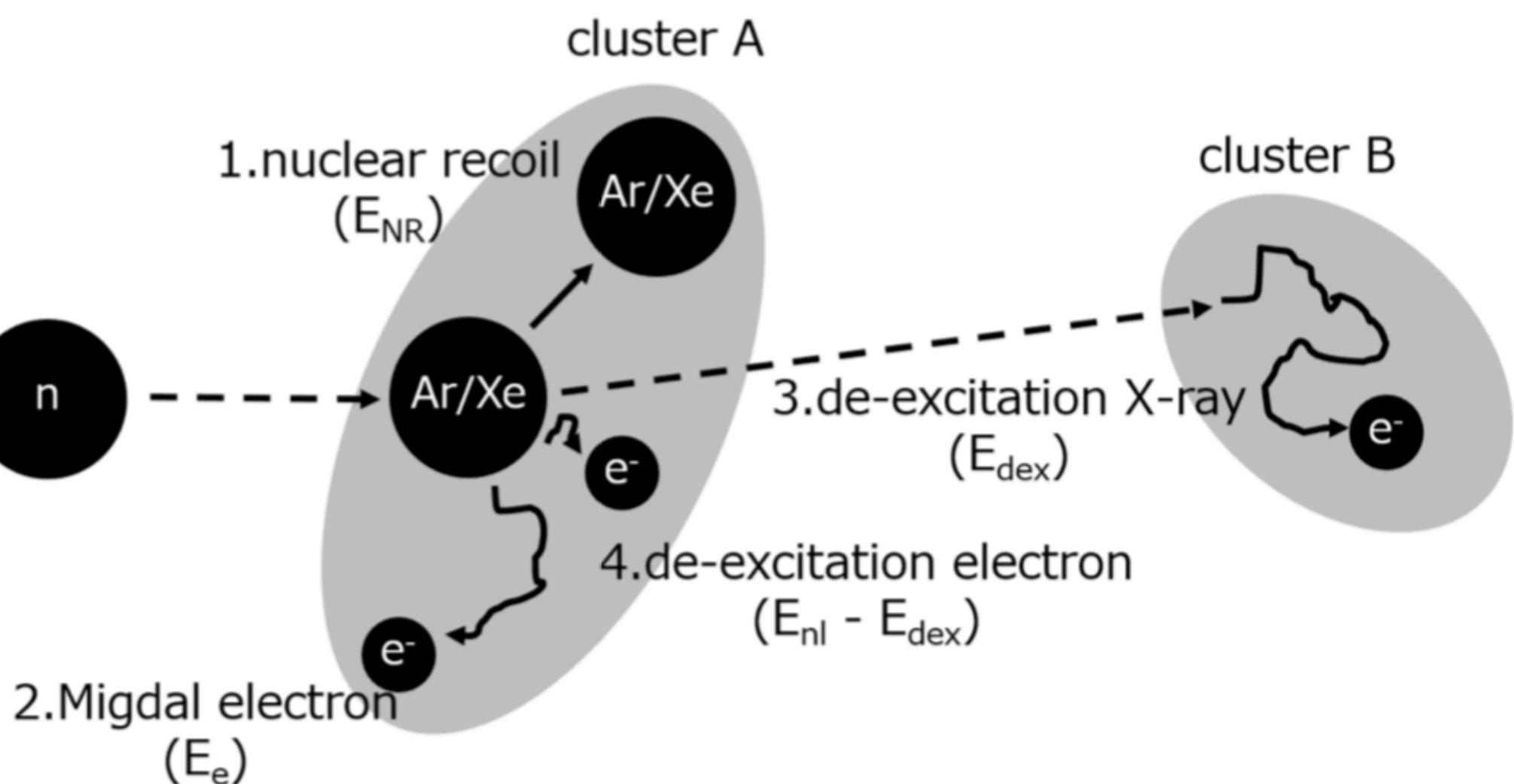
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3. Atoms will fill the hole emitting an X-ray ( $\sim 3$  keV for Ar,  $\sim 30$  keV for Xe);

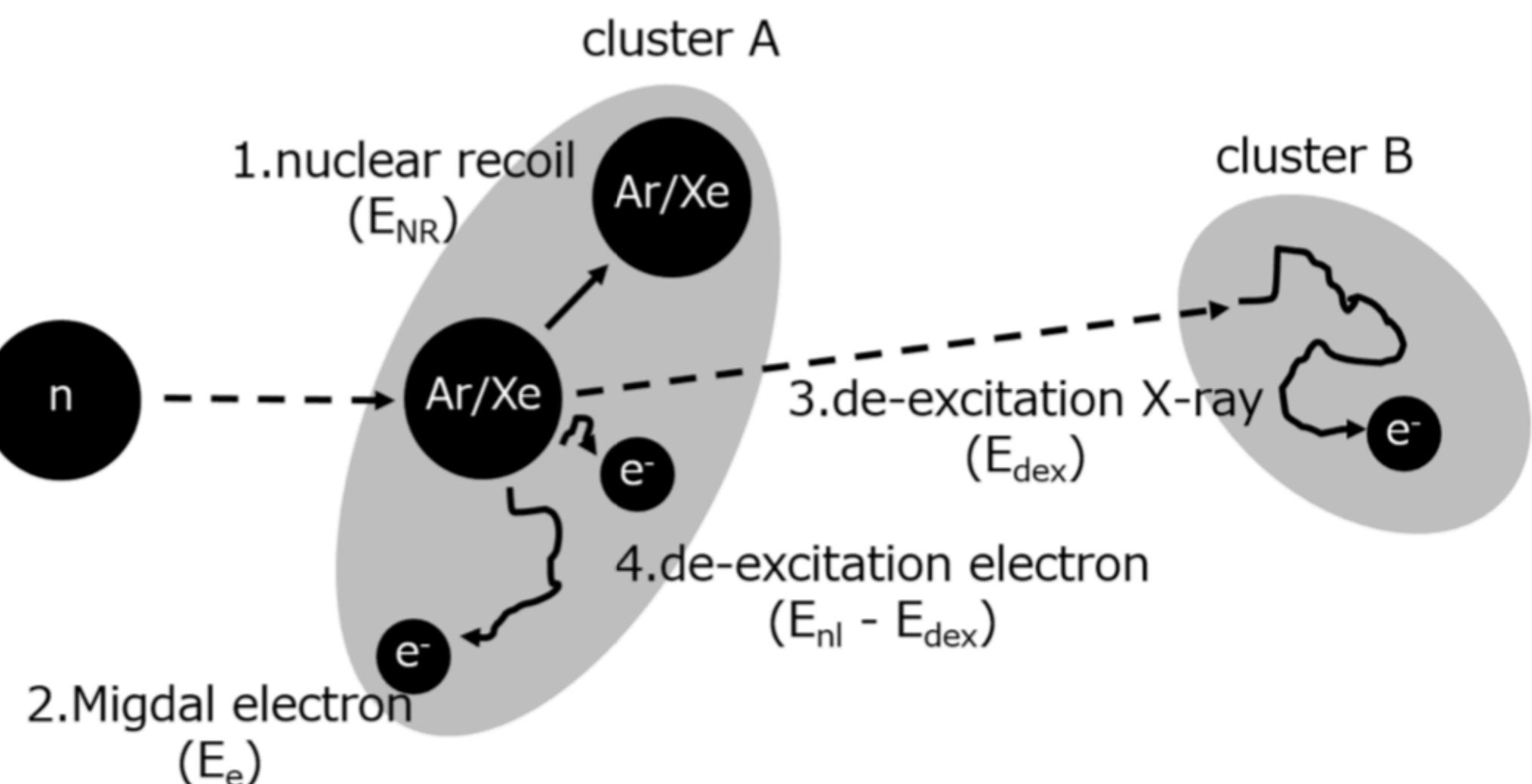
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4. **The signature is a vertex with an energetic NR and a few keV X-ray absorbed after a few cm;**

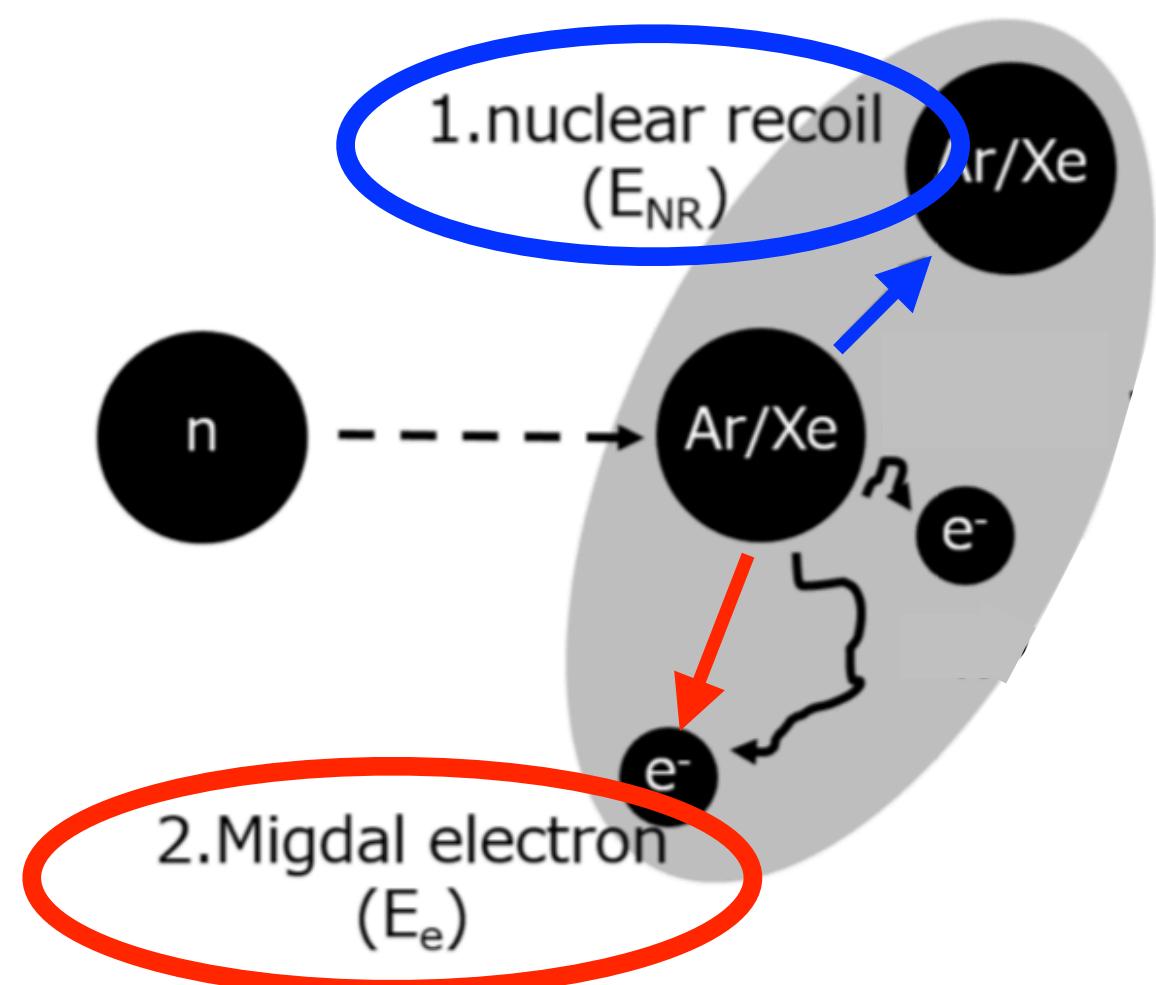
[Nakamura et al., PTEP 1 (2021) 013C01]



# Possible signatures

Or just detect the Migdal electron exploiting all the atomic shells: it needs to be able to reconstruct a **nuclear recoil track** and an **electron recoil track** starting from the same vertex.

Used also to discriminate between signal and background events.



# Experimental opportunity

for Cygno details see A. Messina talk tomorrow

[Baracchini et al., Measur.Sci.Tech. 32 (2021) 2, 025902]

- **Cygno Phase 0 TPC (LIME):** 50 litres of He/CF<sub>4</sub> or Ar/CF<sub>4</sub> with **very good 3-d tracking capability and resolution both for NR and ER;**
- Possibility to exploit available **neutron sources at 2.5 MeV and 14 MeV;**

# Experimental opportunity

X-ray signature

$$N_{\text{events}} = N_T \Phi \sigma_{Ar} f_{Ar} q_e^2 \text{BR}_{\text{Mig}}$$

# Experimental opportunity

## X-ray signature

$7.5 \times 10^{23}$

$3.2 \times 10^{-24} \text{ cm}^2$

$10^{-4} - 10^{-5}$

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Flux for a 2.5 MeV neutron source

$113 \text{ s}^{-1} \text{cm}^{-2}$

0.14

Fluorescence yield

$$\frac{2 m_e^2 E_R}{m_N}$$

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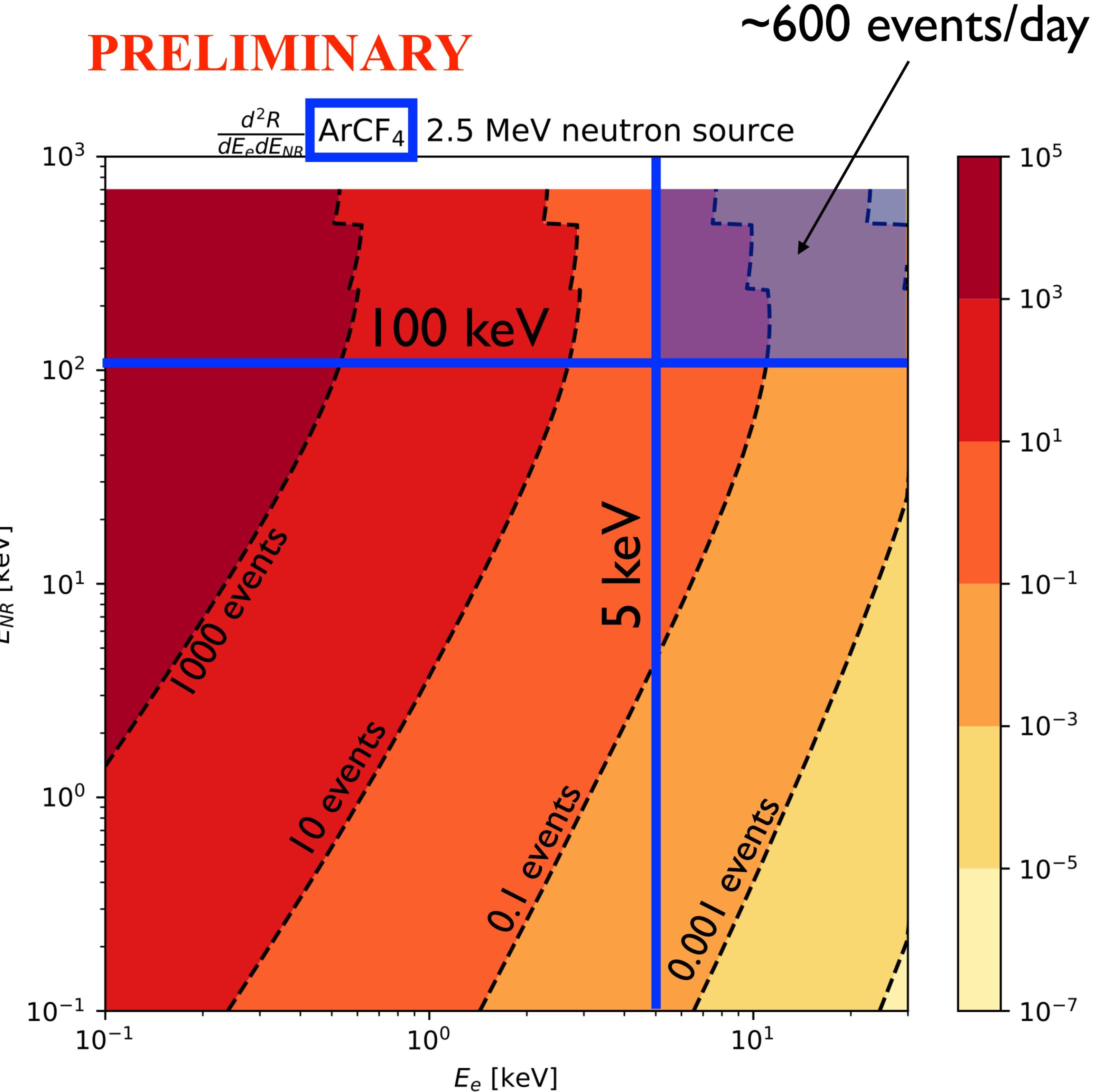
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Expected absorption length for the X-ray:  $\sim 3$  cm

# Experimental opportunity

## Migdal electron signature

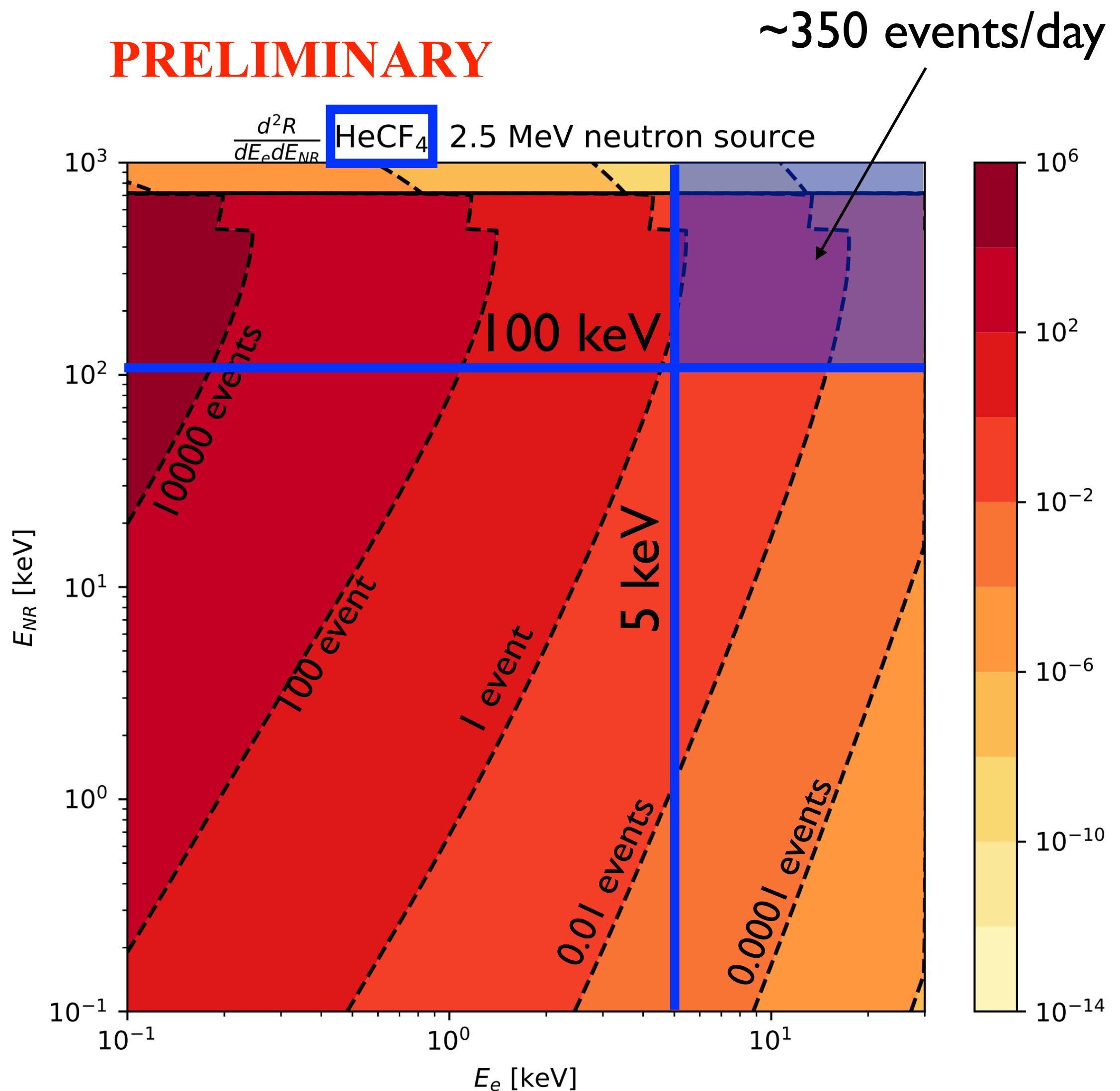
- For large  $E_{NR}$  good tracking capability down to  $E_e \sim 5$  keV.
- Potentially  $\mathcal{O}(100)$  events per day for a realistic  $E_e$  energy threshold of 5 keV (integrating over  $E_{NR} > 100$  keV), for a mixture 60:40 of ArCF<sub>4</sub>;



# Experimental opportunity

## Migdal electron signature

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- Potentially  $\mathcal{O}(100)$  events per day for a realistic  $E_e$  energy threshold of 5 keV (integrating over  $E_{NR} > 100$  keV), for a mixture 60:40 of HeCF<sub>4</sub>;



# Experimental opportunity

Working on signal and background simulations in order to define the optimal detector configuration (gas mix, shielding, neutron source) for a dedicated run to detect Migdal events exploiting (hopefully) both signatures.

# Conclusions

# Conclusions

- The Migdal effect has a great potential to improve the current sensitivity to light dark matter exploiting liquid argon detectors;
- It is important to observe the Migdal effect in nuclear scattering in order to confirm its relevance for dark matter experiments;
- There are promising signatures to be exploited and interesting experimental opportunities using fast neutrons and TPCs: simulations are currently ongoing.

Thank you!