

Roads for Right-handed Neutrino Dark Matter: Fast Expansion, Standard Freeze-out, and Early Matter Domination

GIORGIO ARCARDI¹, JACINTO PAULO NETO², FARINALDO QUEIROZ²³, CLARISSA SIQUEIRA⁴

¹DIPARTIMENTO DI MATEMATICA E FISICA, UNIVERSITA DI ROMA.

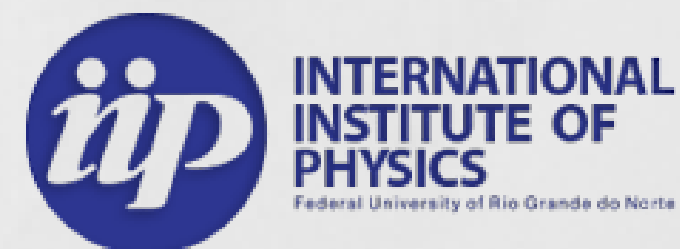
²DEPARTAMENTO DE FÍSICA, UFRN.

³INTERNATIONAL INSTITUTE OF PHYSICS, UFRN.

⁴USP SÃO CARLOS

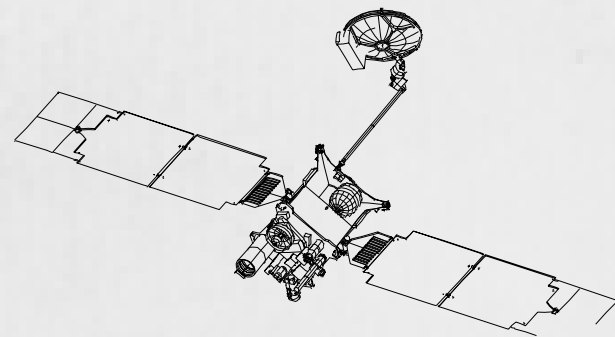
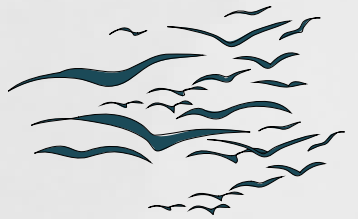
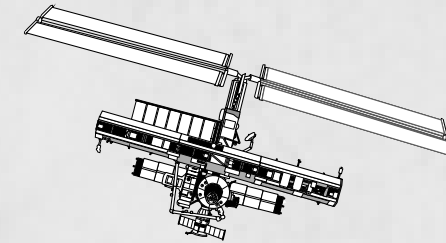
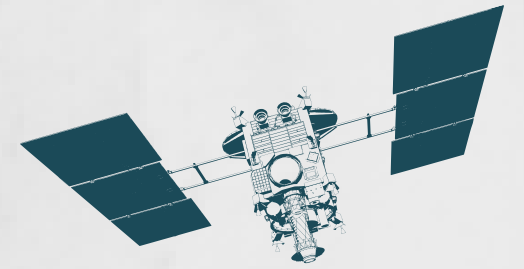
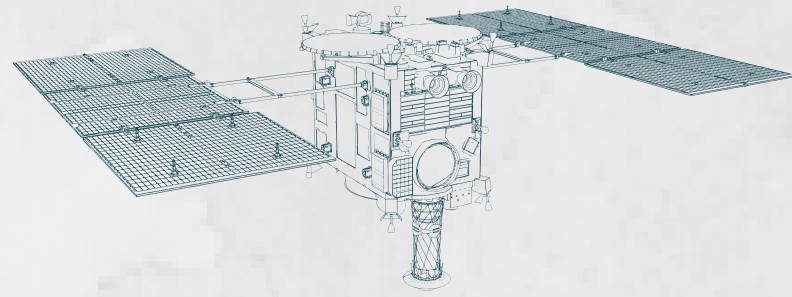
AUGUST 24, 2021.

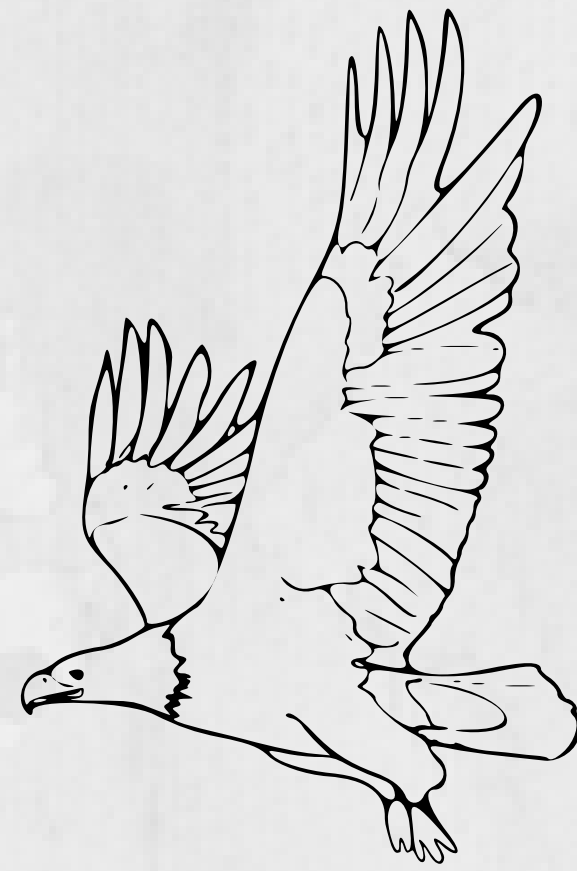
ARXIV
2108.XXXXX



Outline

- BIRD'S EYE VIEW OF THE WORK
- NON-STANDARD COSMOLOGICAL HISTORIES
- RESULTS
- CONCLUSIONS





Bird's Eye View of the Work



Hubble rate **versus** Annihilation Rate

Faster Than Usual
Early Expansion

Quintessence

Cosmology

Early Matter-dominated
freeze-out

Early Radiation-
dominated
freeze-out

Fermions interact only
with the second doublet.

Type-I 2HDM

+ B-L symmetry

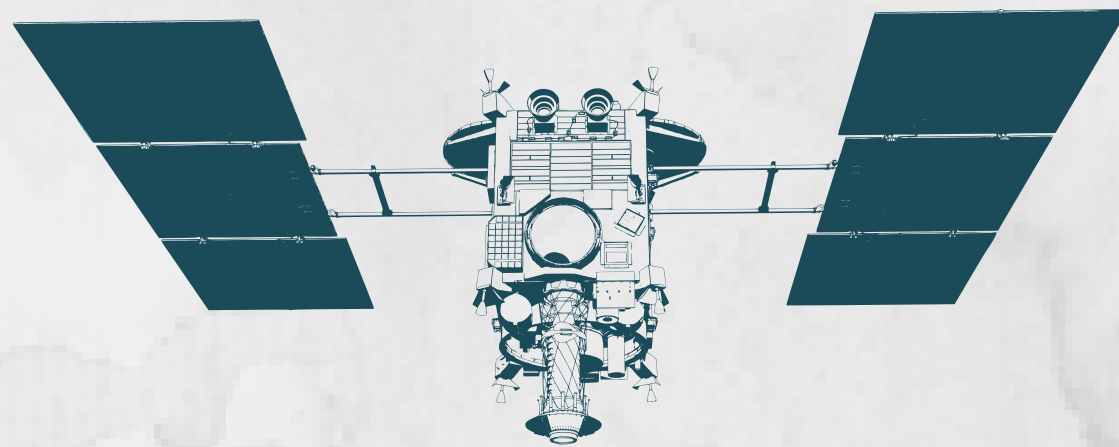
+ 2RH ν + 1RHN

+ Scalar singlet

The scalar singlet
spontaneously breaks the
B-L symmetry.

**Particle
Properties**

The other two neutrinos generate the
active neutrino masses via Type I
Seesaw Mechanism.



Non-standard Cosmologies

Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r} \right)^{n/2}$$

Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r} \right)^{n/2}$$



The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

where

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r} \right)^{n/2}$$

Approximate analytical solutions

$$Y_N(x) \simeq \frac{x_r}{m_N M_{Pl} \langle \sigma v \rangle} \left[\frac{2}{x_f} + \log \left(\frac{x}{x_f} \right) \right]^{-1}, \quad n = 2$$

$$Y_N(x) \simeq \frac{x_r^{n/2}}{2 m_N M_{Pl} \langle \sigma v \rangle} \left[x_f^{n/2-2} + \frac{x^{n/2-1}}{n-1} \right]^{-1}, \quad n > 2.$$

- s-wave annihilation cross-section.
- Apply to the region between $x_f \lesssim x \lesssim x_r$.

The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

where

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r} \right)^{n/2}$$

Approximate analytical solutions

$$Y_N(x) \simeq \frac{x_r}{m_N M_{Pl} \langle \sigma v \rangle} \left[\frac{2}{x_f} + \log \left(\frac{x}{x_f} \right) \right]^{-1}, \quad n = 2$$

$$Y_N(x) \simeq \frac{x_r^{n/2}}{2 m_N M_{Pl} \langle \sigma v \rangle} \left[x_f^{n/2-2} + \frac{x^{n/2-1}}{n-1} \right]^{-1}, \quad n > 2.$$

- s-wave annihilation cross-section.
- Apply to the region between $x_f \lesssim x \lesssim x_r$.

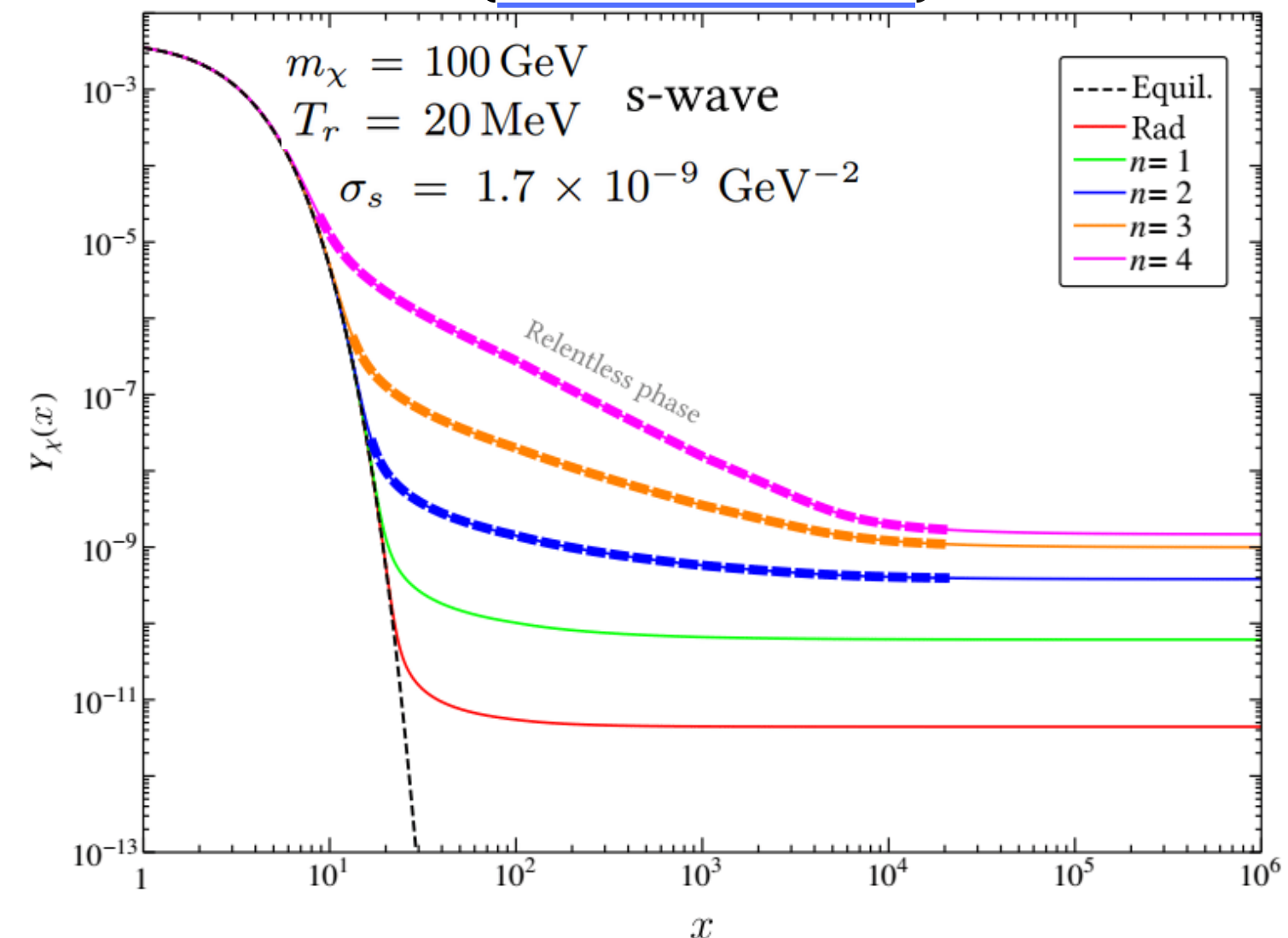
The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

where

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

D'Eramo et al. ([ArXiv: 1703.04793](https://arxiv.org/abs/1703.04793))



Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r} \right)^{n/2}$$

Approximate analytical solutions

$$Y_N(x) \simeq \frac{x_r}{m_N M_{Pl} \langle \sigma v \rangle} \left[\frac{2}{x_f} + \log \left(\frac{x}{x_f} \right) \right]^{-1}, \quad n = 2$$

$$Y_N(x) \simeq \frac{x_r^{n/2}}{2 m_N M_{Pl} \langle \sigma v \rangle} \left[x_f^{n/2-2} + \frac{x^{n/2-1}}{n-1} \right]^{-1}, \quad n > 2.$$

- s-wave annihilation cross-section.
- Apply to the region between $x_f \lesssim x \lesssim x_r$.

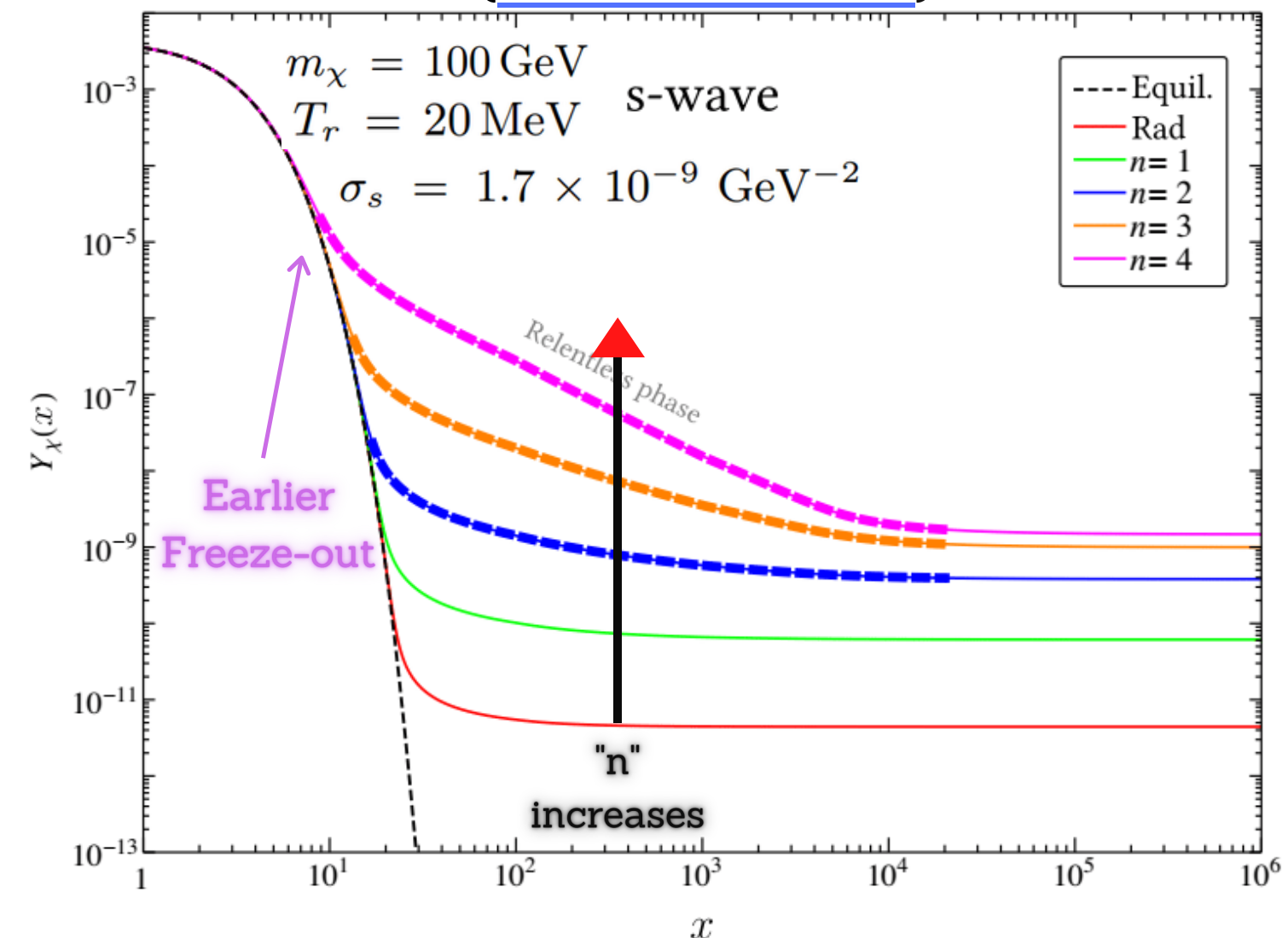
The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

where

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

D'Eramo et al. ([ArXiv: 1703.04793](https://arxiv.org/abs/1703.04793))



Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}$, $n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r}\right)^{n/2}$$

Approximate analytical solutions

$$Y_N(x) \simeq \frac{x_r}{m_N M_{Pl} \langle \sigma v \rangle} \left[\frac{2}{x_f} + \log\left(\frac{x}{x_f}\right) \right]^{-1}, \quad n = 2$$

$$Y_N(x) \simeq \frac{x_r^{n/2}}{2 m_N M_{Pl} \langle \sigma v \rangle} \left[x_f^{n/2-2} + \frac{x^{n/2-1}}{n-1} \right]^{-1}, \quad n > 2.$$

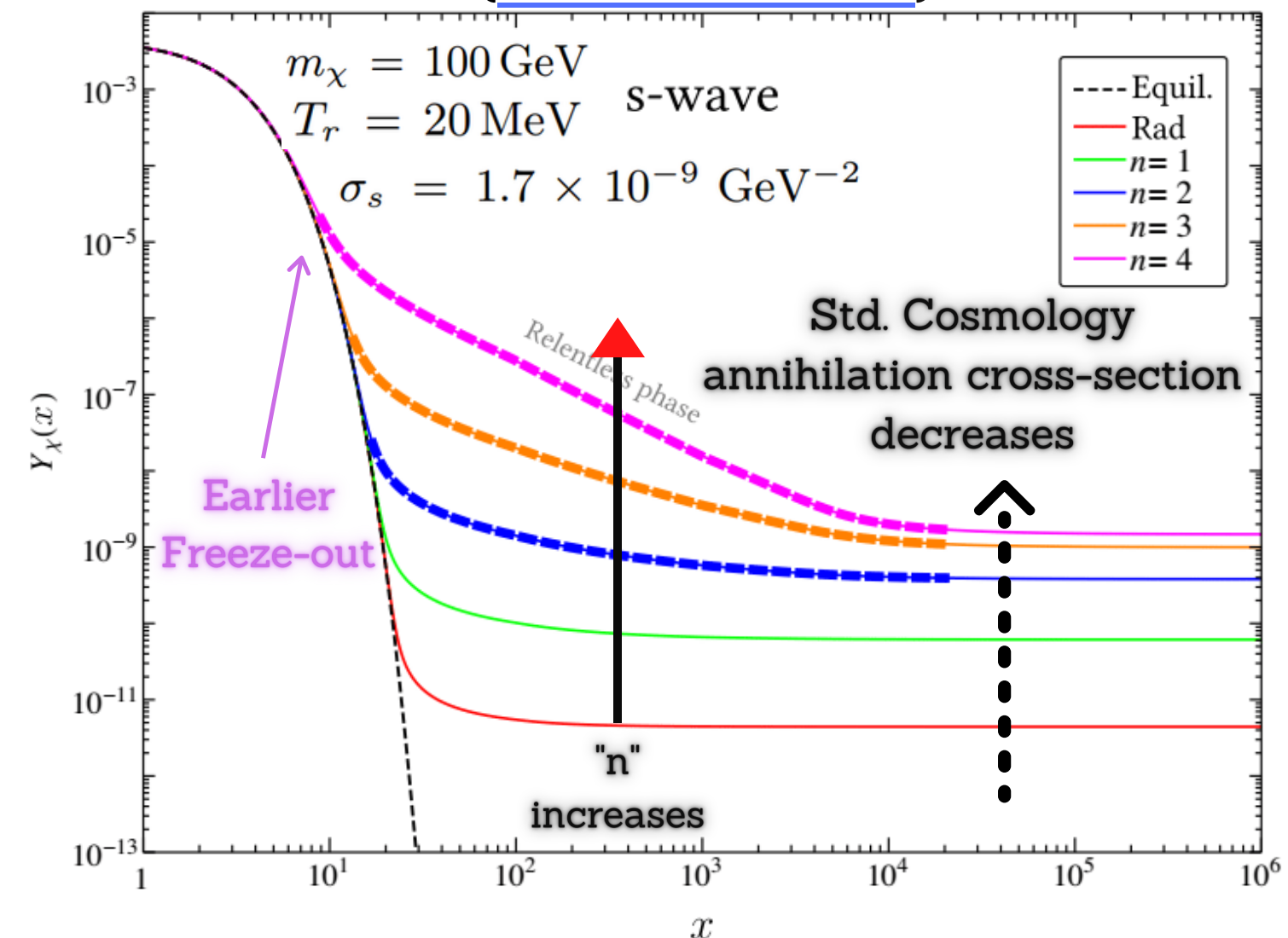
- s-wave annihilation cross-section.
- Apply to the region between $x_f \lesssim x \lesssim x_r$.

The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

D'Eramo et al. ([ArXiv: 1703.04793](https://arxiv.org/abs/1703.04793))



Faster Than Usual Early Expansion

Density energy $\rho_\phi(t) \propto a(t)^{-(4+n)}$, $n > 0$

The Hubble rate

$$H(T) \approx \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{T^2}{M_{Pl}} \left(\frac{T}{T_r}\right)^{n/2}$$

Approximate analytical solutions

$$Y_N(x) \simeq \frac{x_r}{m_N M_{Pl} \langle \sigma v \rangle} \left[\frac{2}{x_f} + \log\left(\frac{x}{x_f}\right) \right]^{-1}, \quad n = 2$$

$$Y_N(x) \simeq \frac{x_r^{n/2}}{2 m_N M_{Pl} \langle \sigma v \rangle} \left[x_f^{n/2-2} + \frac{x^{n/2-1}}{n-1} \right]^{-1}, \quad n > 2.$$

- s-wave annihilation cross-section.
- Apply to the region between $x_f \lesssim x \lesssim x_r$.

The Cosmological Parameters

(n, T_r) with $T_r \gtrsim (15.4)^{1/n}$ MeV

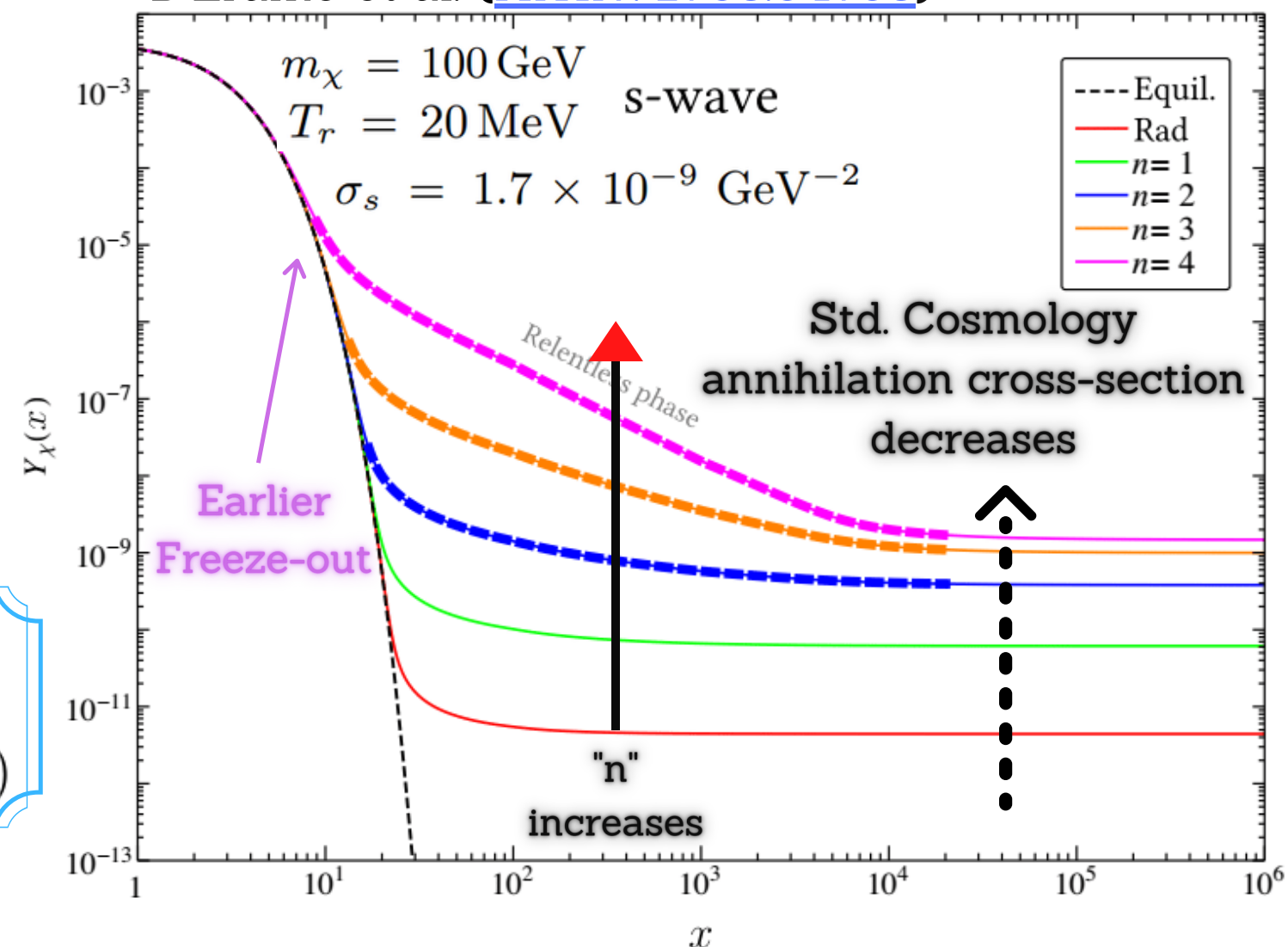
$$\Omega_N h^2 = \frac{s_0}{\rho_0} h^2 m_N Y_N(x \rightarrow \infty) \simeq 2.82 \times 10^8 m_N Y_N(x \rightarrow \infty)$$

The "Faster" Boltzmann Equation

$$\frac{dY_N}{dx} = - \frac{A \langle \sigma v \rangle}{x^{2-n/2} (x^n + x_r^n)^{1/2}} (Y_N^2 - Y_N^{eq2})$$

$$A = \frac{2\sqrt{2}\pi}{3\sqrt{5}} g_\star^{1/2} M_{Pl} m_N$$

D'Eramo et al. ([ArXiv: 1703.04793](https://arxiv.org/abs/1703.04793))



Early Matter-dominated

The Boltzmann Equations

$$\frac{d\rho_\phi}{dt} = -3H\rho_\phi - \Gamma_\phi\rho_\phi,$$

$$\frac{ds}{dt} = -3Hs + \frac{\Gamma_\phi\rho_\phi}{T} + 2\frac{E}{T}\langle\sigma v\rangle(n_N^2 - n_N^{2eq}),$$

$$\frac{dn_N}{dt} = -3Hn_N - \langle\sigma v\rangle(n_N^2 - n_N^{2eq}),$$

$$\omega_\phi = 0$$

Unstable
scalar field

The scalar field decays only into SM radiation. Hence, injecting entropy into SM bath and diluting DM.

Early Matter-dominated

The Boltzmann Equations

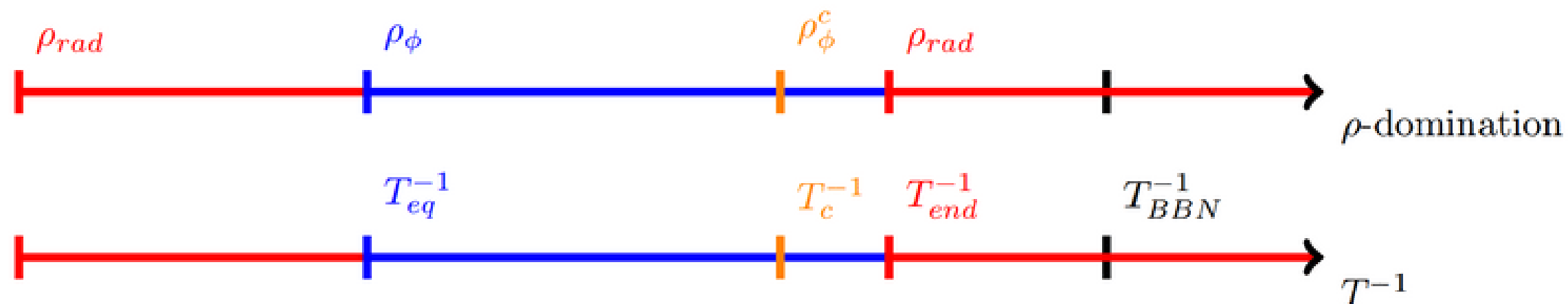
$$\frac{d\rho_\phi}{dt} = -3H\rho_\phi - \Gamma_\phi\rho_\phi,$$

$\omega_\phi = 0$
Unstable
scalar field

$$\frac{ds}{dt} = -3Hs + \frac{\Gamma_\phi\rho_\phi}{T} + 2\frac{E}{T}\langle\sigma v\rangle(n_N^2 - n_N^{2eq}),$$

$$\frac{dn_N}{dt} = -3Hn_N - \langle\sigma v\rangle(n_N^2 - n_N^{2eq}),$$

The scalar field decays only into SM radiation. Hence, injecting entropy into SM bath and diluting DM.



Early Matter-dominated

Early Radiation-dominated Freeze-out $T_{eq} \ll T_f$

The Hubble rate

$$H_R(x) \simeq \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{m_N^2}{M_{Pl}} x^{-2}$$

Early Matter-dominated

Early Radiation-dominated Freeze-out $T_{eq} \ll T_f$

The Hubble rate

$$H_R(x) \simeq \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{m_N^2}{M_{Pl}} x^{-2}$$



The Boltzmann Equation is the standard one

$$\frac{dY_N}{dx} = -\frac{s \langle \sigma v \rangle}{H_R x} (Y_N^2 - Y_N^{eq2})$$



Approx. Solution

$$Y_N^{std}$$

Early Matter-dominated

Early Radiation-dominated Freeze-out $T_{eq} \ll T_f$

The Hubble rate

$$H_R(x) \simeq \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{m_N^2}{M_{Pl}} x^{-2}$$



The Boltzmann Equation is the standard one

$$\frac{dY_N}{dx} = -\frac{s \langle \sigma v \rangle}{H_R x} (Y_N^2 - Y_N^{eq2})$$



Approx. Solution

$$Y_N^{std}$$

The energy conservation and the definition of κ provide the dilution factor

$$D \equiv \frac{s(T_2)}{s(T_1)} = \left(\frac{T_2}{T_1}\right)^3 = \kappa \frac{m_N}{T_{end}}$$

Early Matter-dominated

Early Radiation-dominated Freeze-out $T_{eq} \ll T_f$

The Hubble rate

$$H_R(x) \simeq \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{m_N^2}{M_{Pl}} x^{-2}$$



The Boltzmann Equation is the standard one

$$\frac{dY_N}{dx} = -\frac{s \langle \sigma v \rangle}{H_R x} (Y_N^2 - Y_N^{eq2})$$



Approx. Solution

$$Y_N^{std}$$

The energy conservation and the definition of κ provide the dilution factor

$$D \equiv \frac{s(T_2)}{s(T_1)} = \left(\frac{T_2}{T_1}\right)^3 = \kappa \frac{m_N}{T_{end}}$$

The Cosmological Parameters

$$\kappa = \frac{\rho_\phi}{\rho_R} \Big|_{T=m_N} \quad T_{end} \equiv \left[\frac{90 M_{Pl}^2}{\pi^2 g_\star(T_{end})} \right]^{1/4} \Gamma_\phi^{1/2}$$

$T_{end} \gtrsim 4 \text{ MeV}$

Early Matter-dominated

Early Radiation-dominated Freeze-out $T_{eq} \ll T_f$

The Hubble rate

$$H_R(x) \simeq \frac{\pi}{3} \sqrt{\frac{g_\star}{10}} \frac{m_N^2}{M_{Pl}} x^{-2}$$



The Boltzmann Equation is the standard one

$$\frac{dY_N}{dx} = -\frac{s \langle \sigma v \rangle}{H_R x} (Y_N^2 - Y_N^{eq2})$$



Approx. Solution

$$Y_N^{std}$$

The energy conservation and the definition of κ provide the dilution factor

$$D \equiv \frac{s(T_2)}{s(T_1)} = \left(\frac{T_2}{T_1}\right)^3 = \kappa \frac{m_N}{T_{end}}$$

The Cosmological Parameters

$$\kappa = \frac{\rho_\phi}{\rho_R} \Big|_{T=m_N} \quad T_{end} \equiv \left[\frac{90 M_{Pl}^2}{\pi^2 g_\star(T_{end})} \right]^{1/4} \Gamma_\phi^{1/2}$$

$T_{end} \gtrsim 4 \text{ MeV}$

The approximate standard solution

taking into account the entropy dilution

$$Y_N = \frac{Y_N^{std}}{D} \quad \Omega_N h^2 = \frac{\Omega_N^{std} h^2}{D}$$

Early Matter-dominated

Early Matter-dominated Freeze-out $T_c \ll T_f \ll T_{eq}$

The Hubble rate

$$H \simeq H_\star \left(\frac{g_\star(T)}{g_\star(T_\star)} \right)^{3/8} \left(\frac{T}{T_\star} \right)^{3/2} \left[(1-r) + r \left(\frac{T}{T_\star} \right) \right]^{1/2}$$

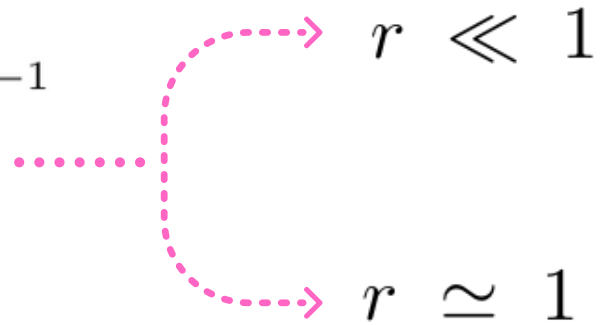
Early Matter-dominated

Early Matter-dominated Freeze-out $T_c \ll T_f \ll T_{eq}$

The Hubble rate

$$H \simeq H_\star \left(\frac{g_\star(T)}{g_\star(T_\star)} \right)^{3/8} \left(\frac{T}{T_\star} \right)^{3/2} \left[(1-r) + r \left(\frac{T}{T_\star} \right) \right]^{1/2}$$

The $r \in [0, 1]$ parameter

$$r \equiv \frac{\rho_R + \rho_N}{\rho_\phi + \rho_R + \rho_N} \Big|_{T=T_\star} = \left[1 + \frac{g_\phi(T_\star)}{g_\star(T_\star) + g_N} \left(\frac{m_\phi}{T_\star} \right)^4 \right]^{-1}$$


$r \ll 1$
 $r \simeq 1$

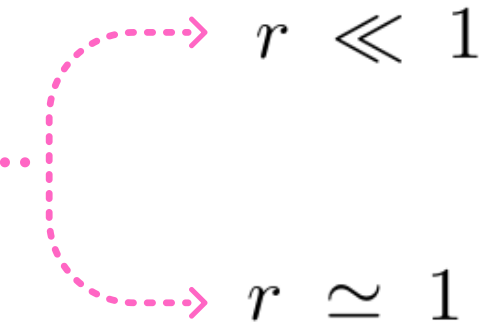
Early Matter-dominated

Early Matter-dominated Freeze-out $T_c \ll T_f \ll T_{eq}$

The Hubble rate

$$H \simeq H_\star \left(\frac{g_\star(T)}{g_\star(T_\star)} \right)^{3/8} \left(\frac{T}{T_\star} \right)^{3/2} \left[(1-r) + r \left(\frac{T}{T_\star} \right) \right]^{1/2}$$

The $r \in [0, 1]$ parameter

$$r \equiv \frac{\rho_R + \rho_N}{\rho_\phi + \rho_R + \rho_N} \Big|_{T=T_\star} = \left[1 + \frac{g_\phi(T_\star)}{g_\star(T_\star) + g_N} \left(\frac{m_\phi}{T_\star} \right)^4 \right]^{-1}$$


$r \ll 1$
 $r \simeq 1$

The approximate solution for BEQ

$$r \ll 1 \longrightarrow Y_N^{MD} = \frac{3}{2} \sqrt{\frac{45}{\pi}} \frac{\sqrt{g_\star}}{g_{\star s}} \frac{x_f^{3/2}}{m_N M_{Pl} \langle \sigma v \rangle x_\star^{1/2}}$$

Early Matter-dominated

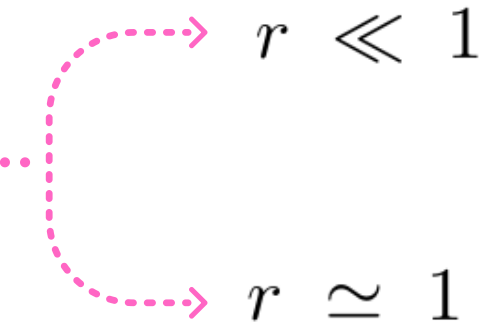
Early Matter-dominated Freeze-out $T_c \ll T_f \ll T_{eq}$

The Hubble rate

$$H \simeq H_\star \left(\frac{g_\star(T)}{g_\star(T_\star)} \right)^{3/8} \left(\frac{T}{T_\star} \right)^{3/2} \left[(1-r) + r \left(\frac{T}{T_\star} \right) \right]^{1/2}$$

The $r \in [0, 1]$ parameter

$$r \equiv \frac{\rho_R + \rho_N}{\rho_\phi + \rho_R + \rho_N} \Big|_{T=T_\star} = \left[1 + \frac{g_\phi(T_\star)}{g_\star(T_\star) + g_N} \left(\frac{m_\phi}{T_\star} \right)^4 \right]^{-1}$$



The approximate solution for BEQ

$$r \ll 1 \quad \longrightarrow \quad Y_N^{MD} = \frac{3}{2} \sqrt{\frac{45}{\pi}} \frac{\sqrt{g_\star}}{g_\star s} \frac{x_f^{3/2}}{m_N M_{Pl} \langle \sigma v \rangle x_\star^{1/2}}$$

The "inverse" dilution factor

$$\zeta = \frac{s(T_1)}{s(T_2)} \simeq (1-r)^{-1} \frac{g_\star(T_c)}{g_\star(T_\star)} \frac{T_{end}}{T_\star}$$

Early Matter-dominated

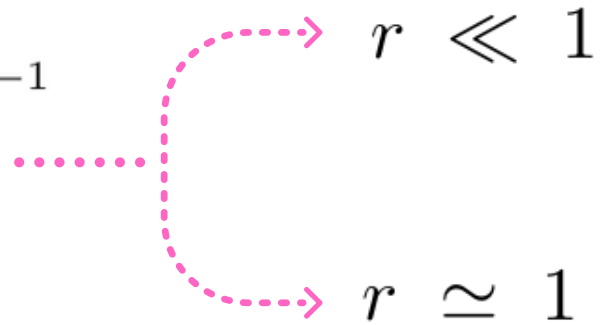
Early Matter-dominated Freeze-out $T_c \ll T_f \ll T_{eq}$

The Hubble rate

$$H \simeq H_\star \left(\frac{g_\star(T)}{g_\star(T_\star)} \right)^{3/8} \left(\frac{T}{T_\star} \right)^{3/2} \left[(1-r) + r \left(\frac{T}{T_\star} \right) \right]^{1/2}$$

The $r \in [0, 1]$ parameter

$$r \equiv \frac{\rho_R + \rho_N}{\rho_\phi + \rho_R + \rho_N} \Big|_{T=T_\star} = \left[1 + \frac{g_\phi(T_\star)}{g_\star(T_\star) + g_N} \left(\frac{m_\phi}{T_\star} \right)^4 \right]^{-1}$$



The approximate solution for BEQ

$$r \ll 1 \longrightarrow Y_N^{MD} = \frac{3}{2} \sqrt{\frac{45}{\pi}} \frac{\sqrt{g_\star}}{g_\star s} \frac{x_f^{3/2}}{m_N M_{Pl} \langle \sigma v \rangle x_\star^{1/2}}$$

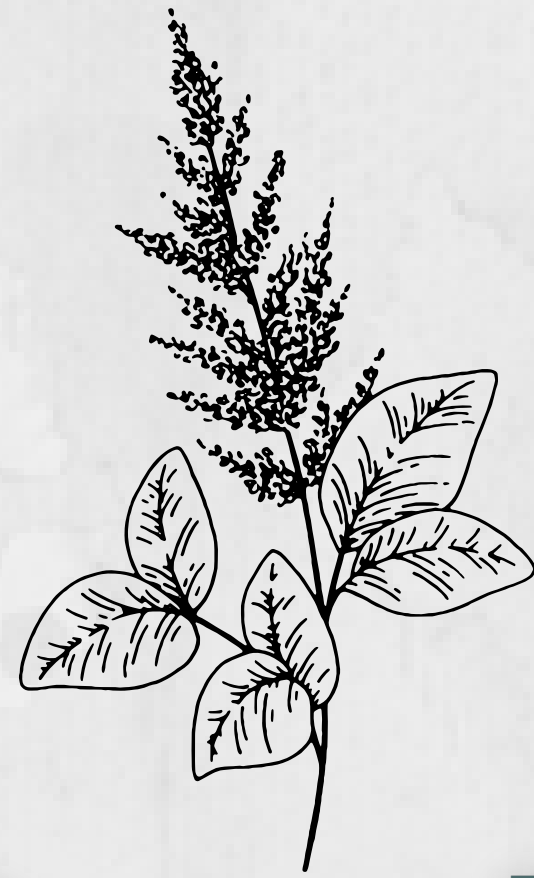
The "inverse" dilution factor

$$\zeta = \frac{s(T_1)}{s(T_2)} \simeq (1-r)^{-1} \frac{g_\star(T_c)}{g_\star(T_\star)} \frac{T_{end}}{T_\star}$$

$$Y_N = \zeta Y_N^{MD} \quad \longrightarrow \quad \Omega_N h^2 = \zeta \Omega_N^{MD} h^2$$

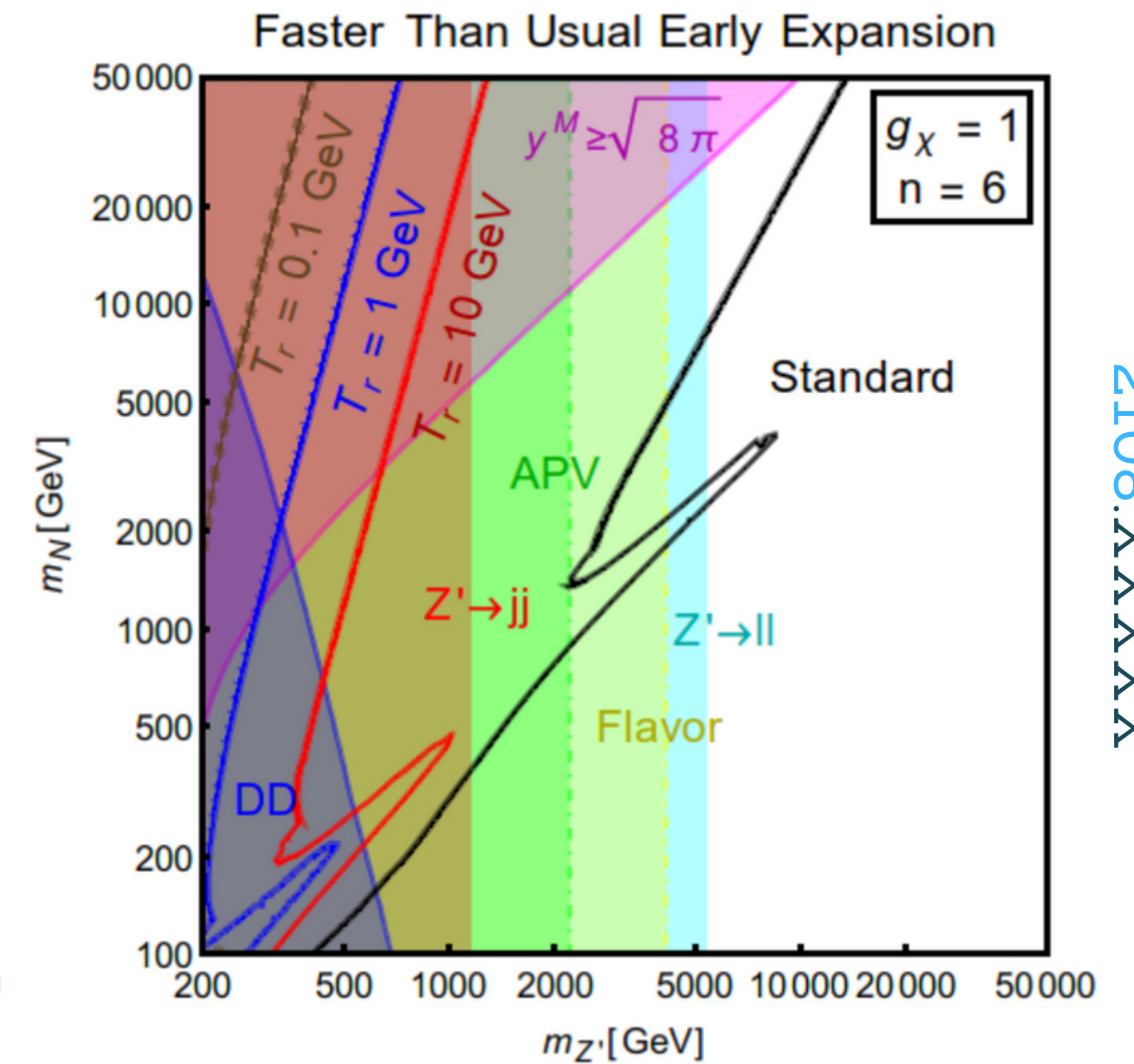
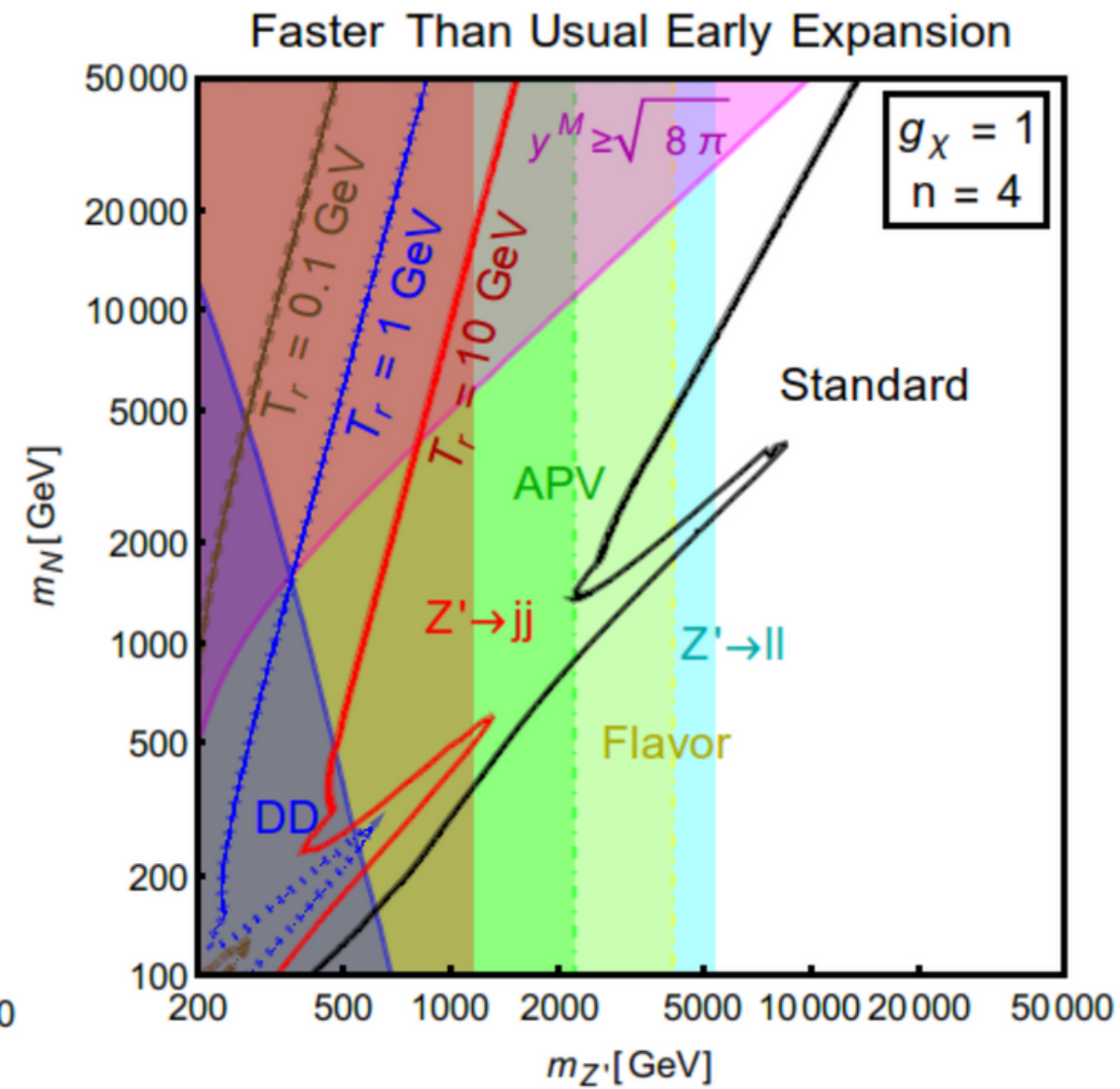
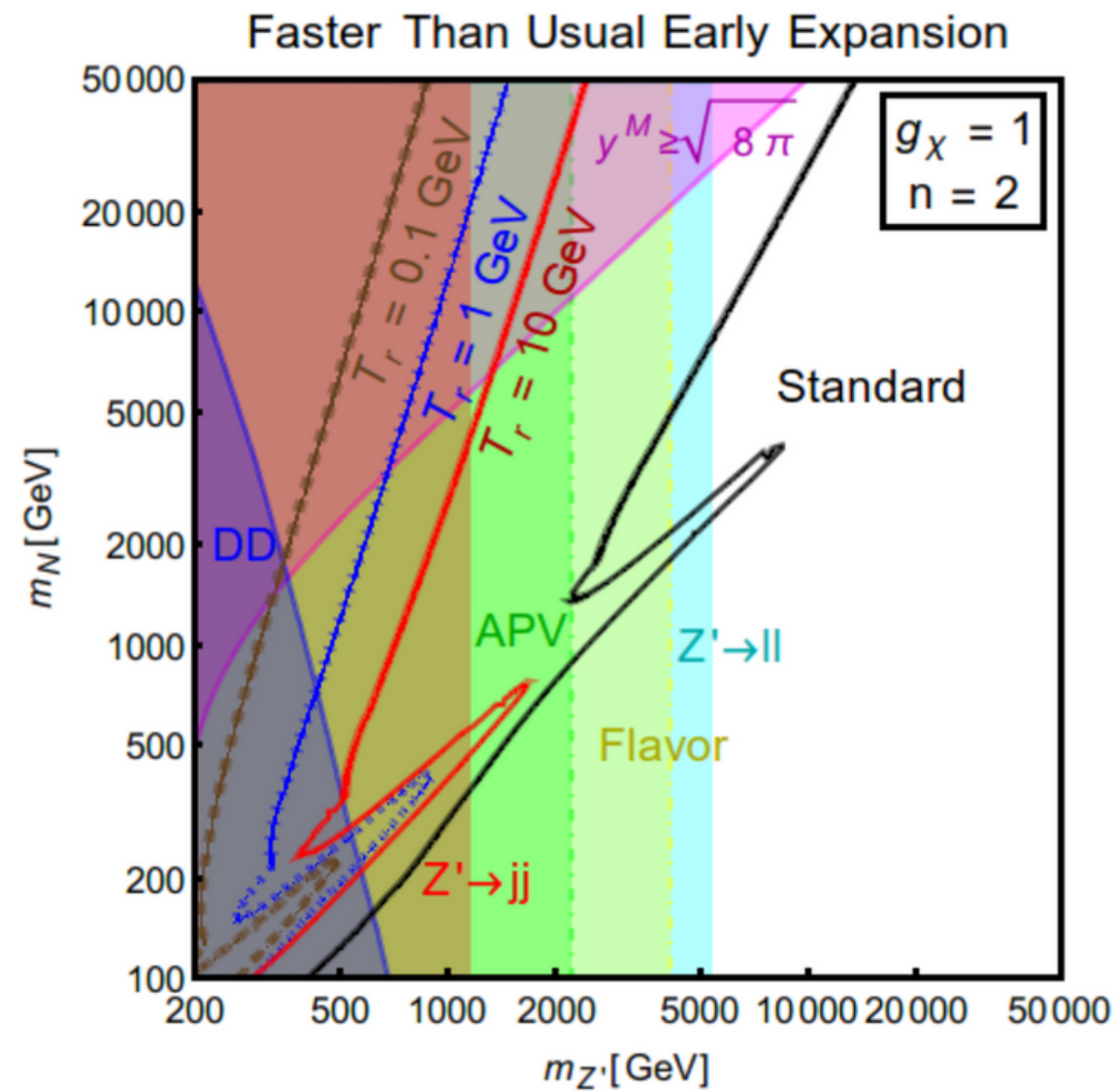
The Cosmological Parameters

$$\zeta, T_\star$$



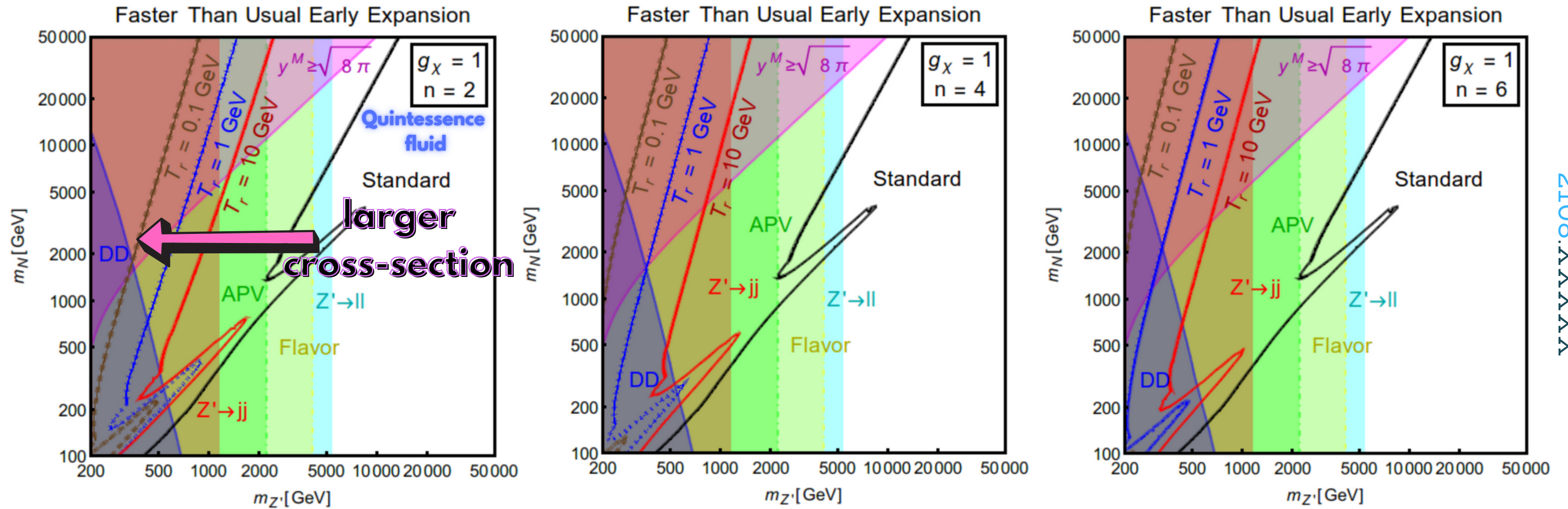
Results

Faster Than Usual Early Expansion



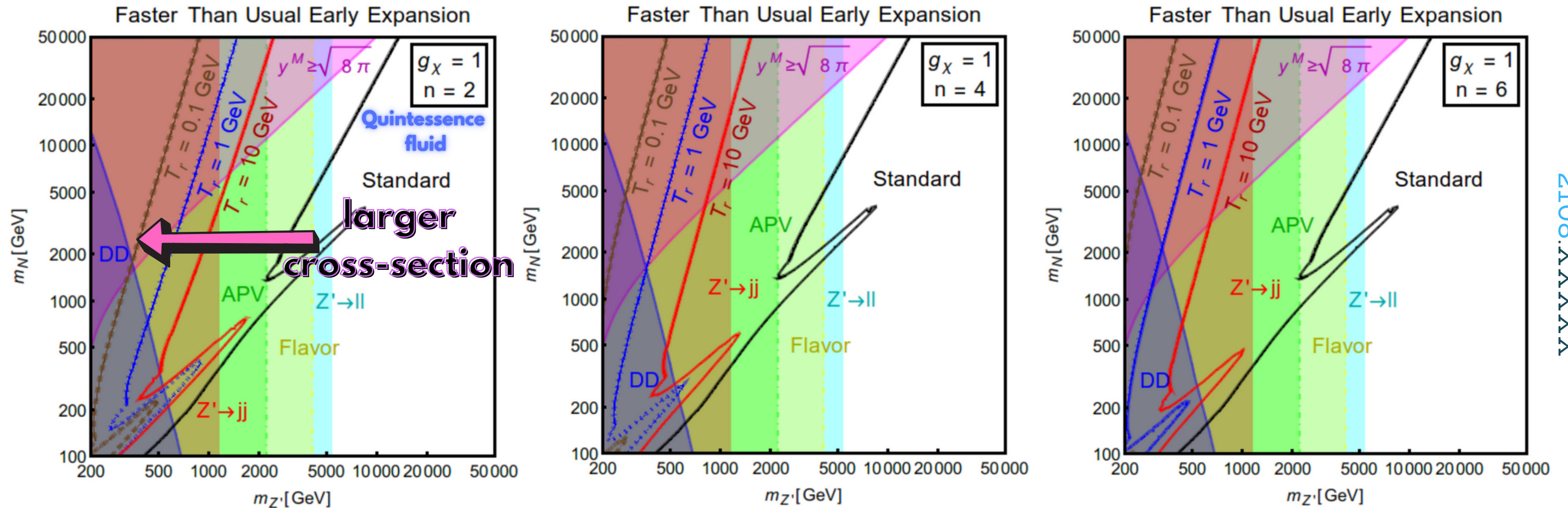
ARXIV
2108.XXXXXX

Faster Than Usual Early Expansion



ARXIV
2108.XXXXXX

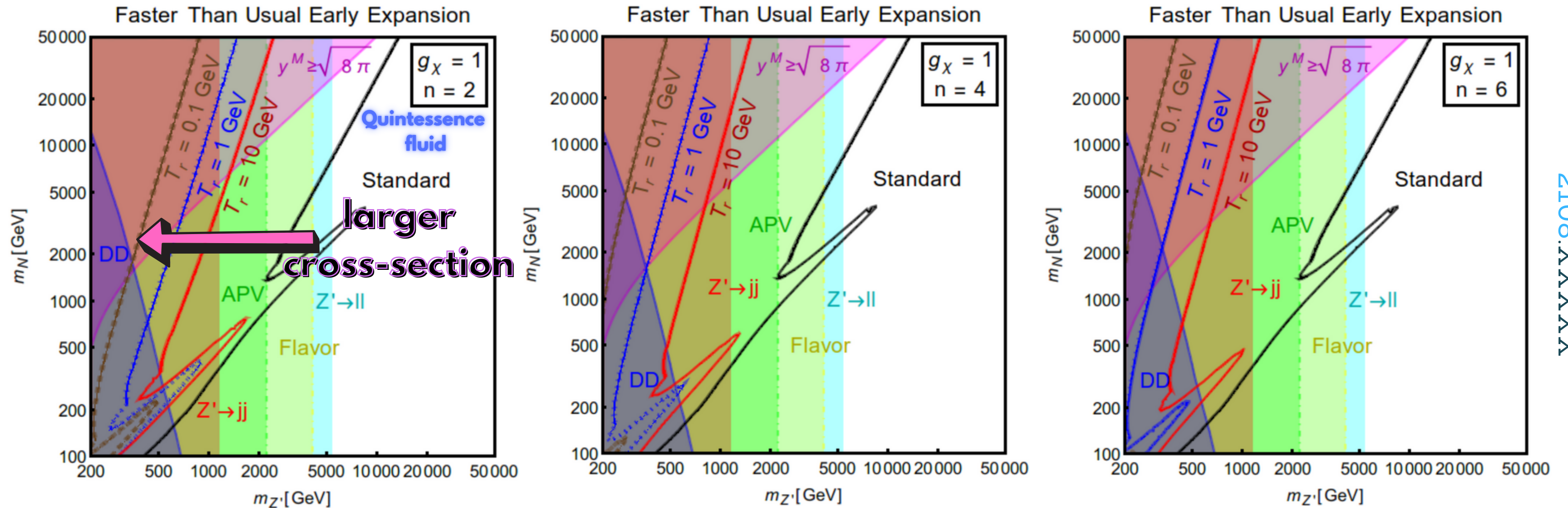
Faster Than Usual Early Expansion



ARXIV
2108.XXXXXX

The contours move toward smaller Z' masses to suppress the enhancement on the DM relic density.

Faster Than Usual Early Expansion



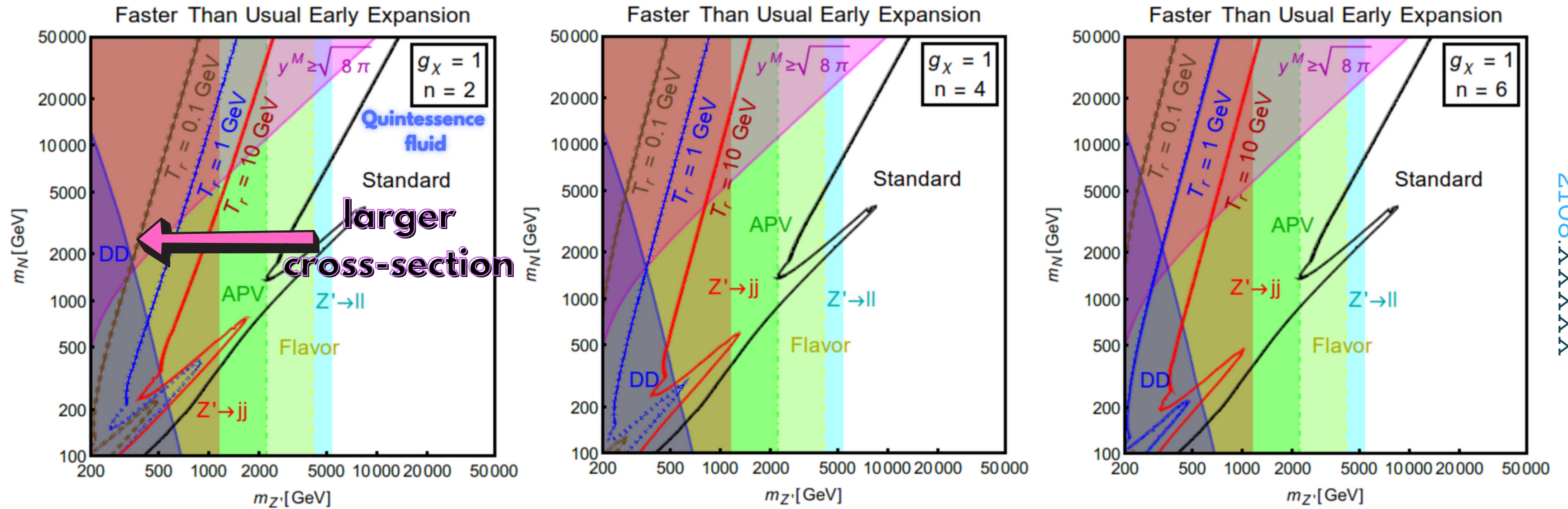
ARXIV
2108.XXXXXX

The contours move toward smaller Z' masses to suppress the enhancement on the DM relic density.

On the other hand,

The heavier the DM mass, the larger the Z' mass

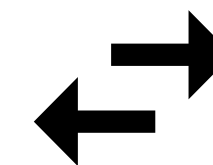
Faster Than Usual Early Expansion



The contours move toward smaller Z' masses to suppress the enhancement on the DM relic density.

On the other hand,

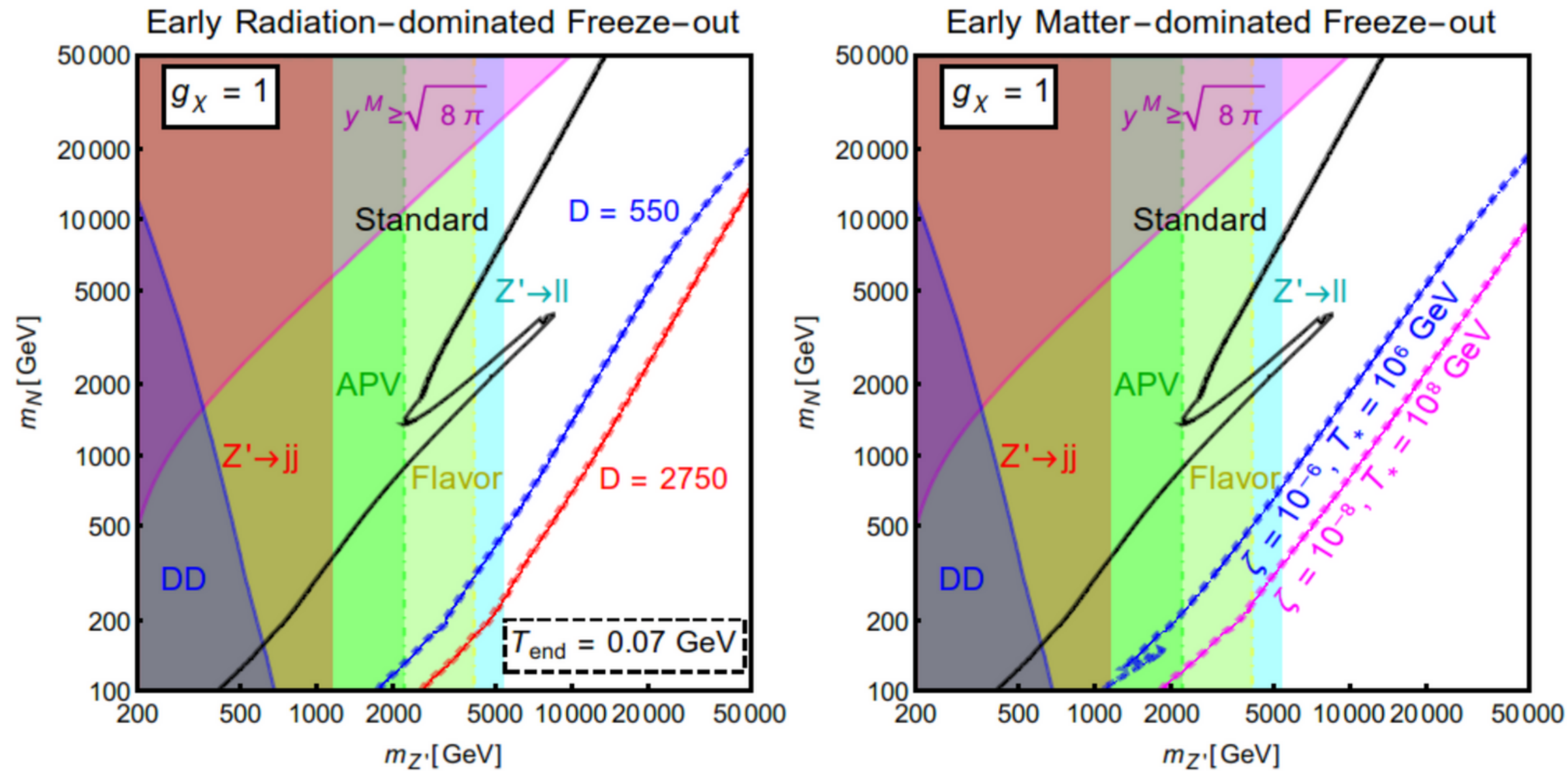
The heavier the DM mass, the larger the Z' mass



**LONGER
RELENTLESS PHASE**

ARXIV
2108.XXXXXXX

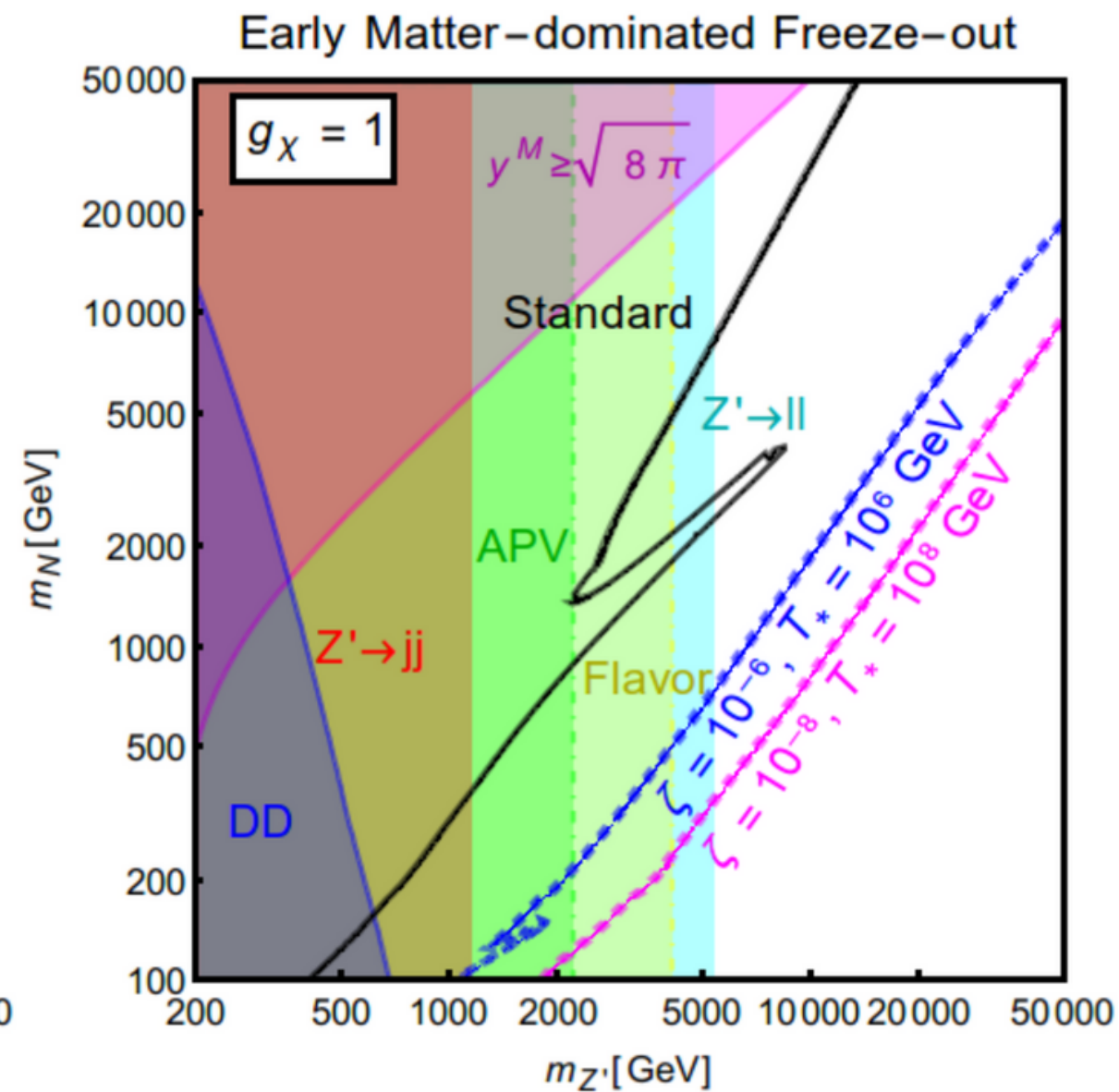
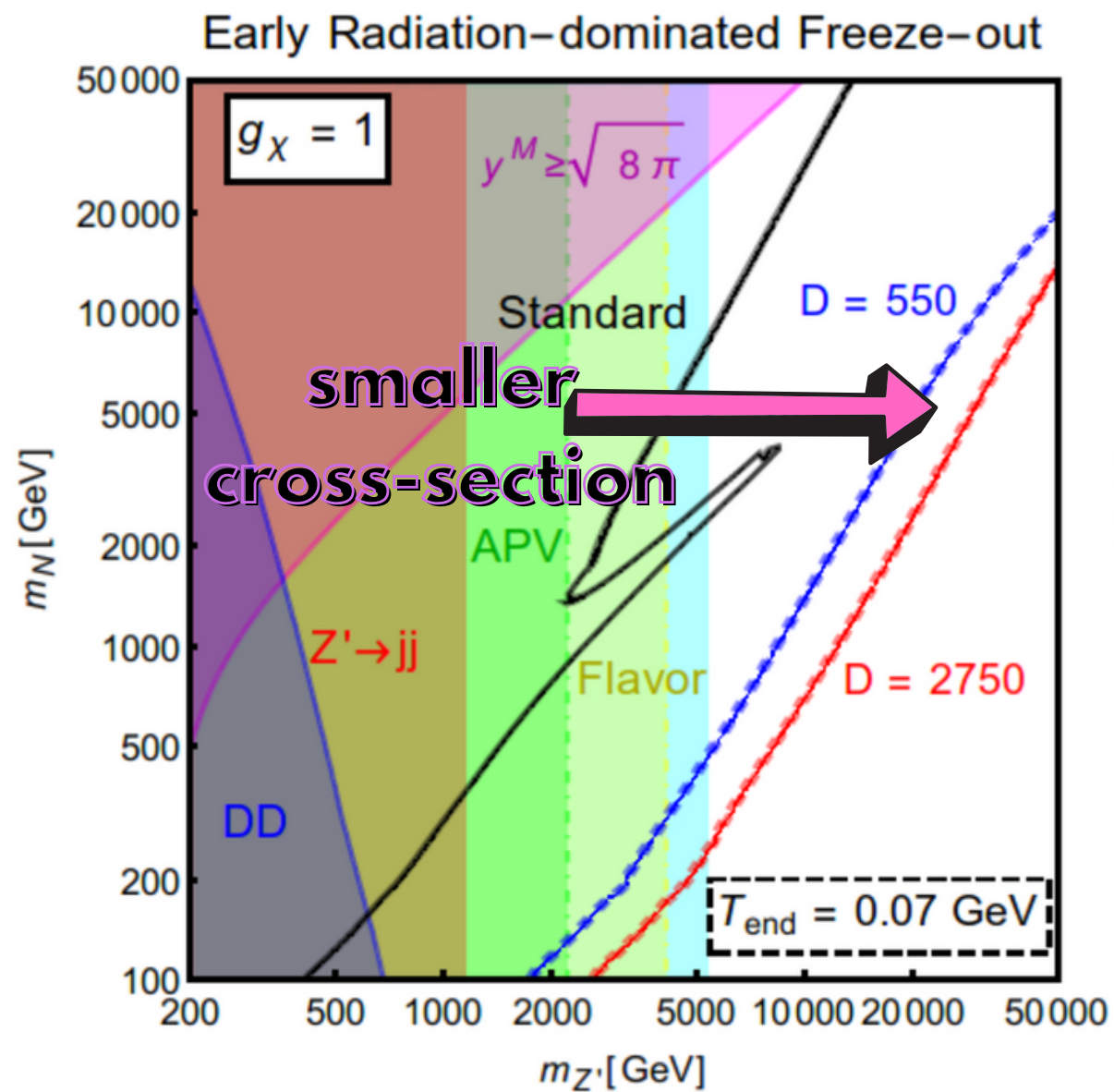
Early Matter-dominated



ARXIV

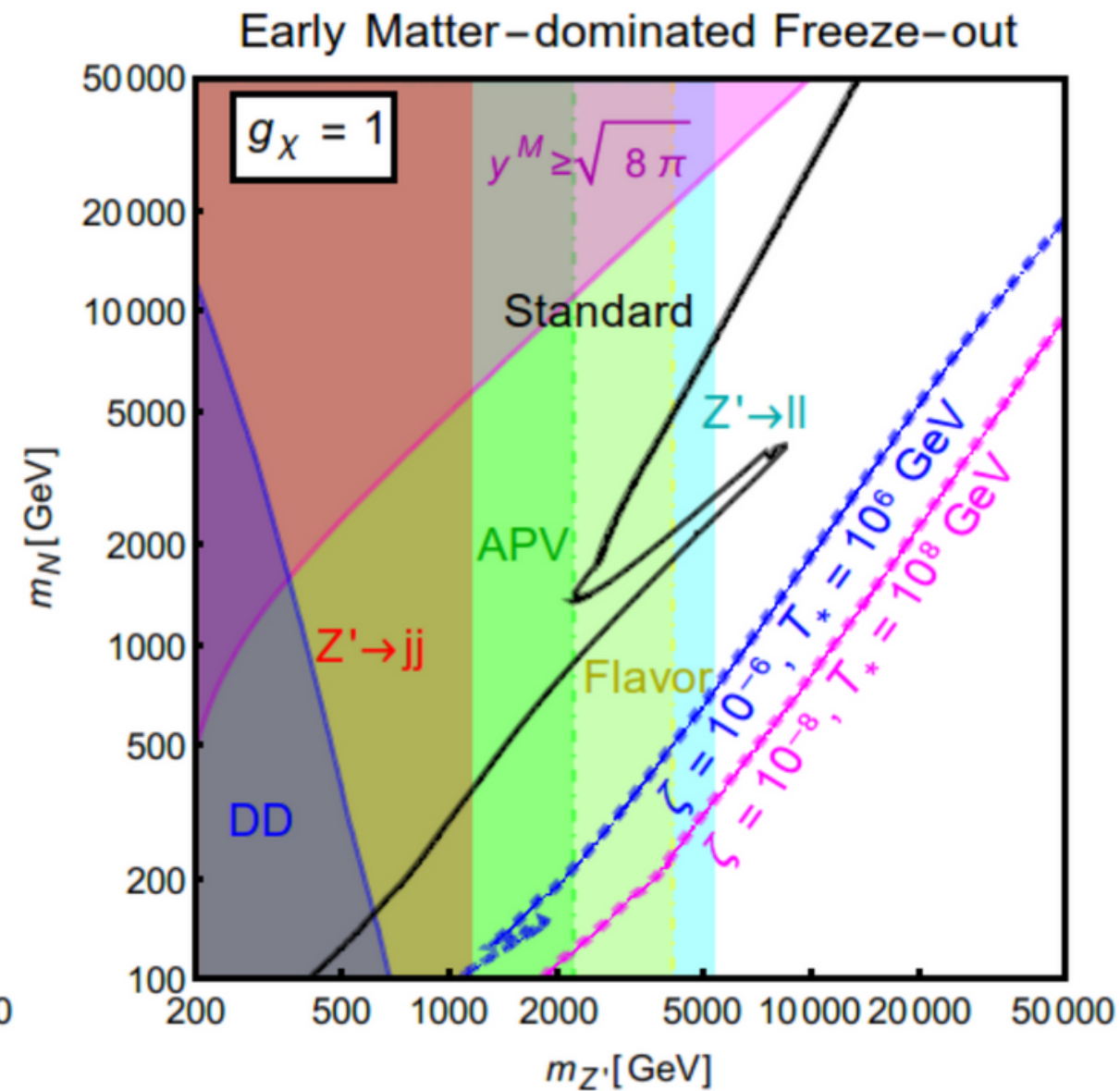
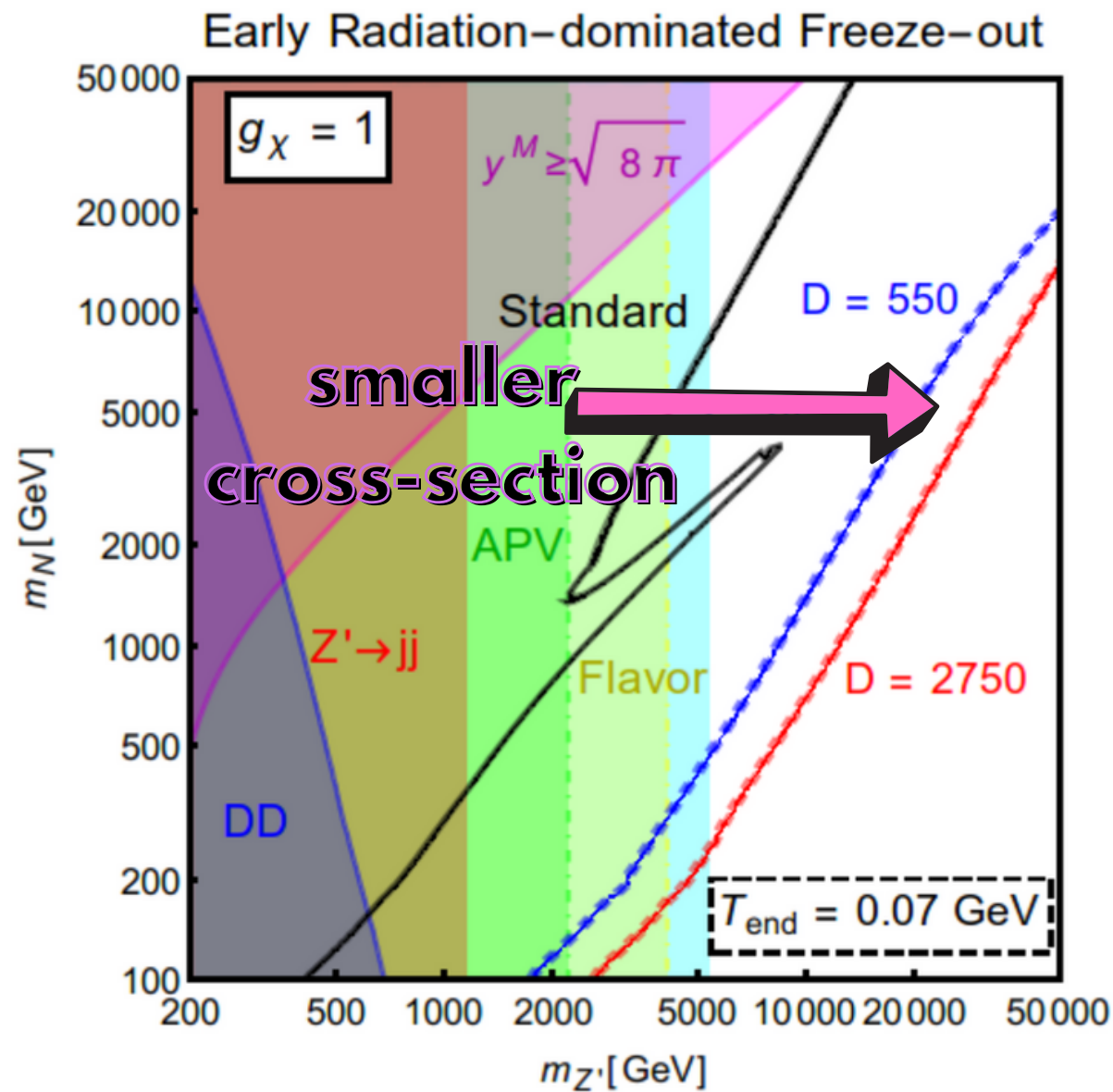
2108.XXXXX

Early Matter-dominated

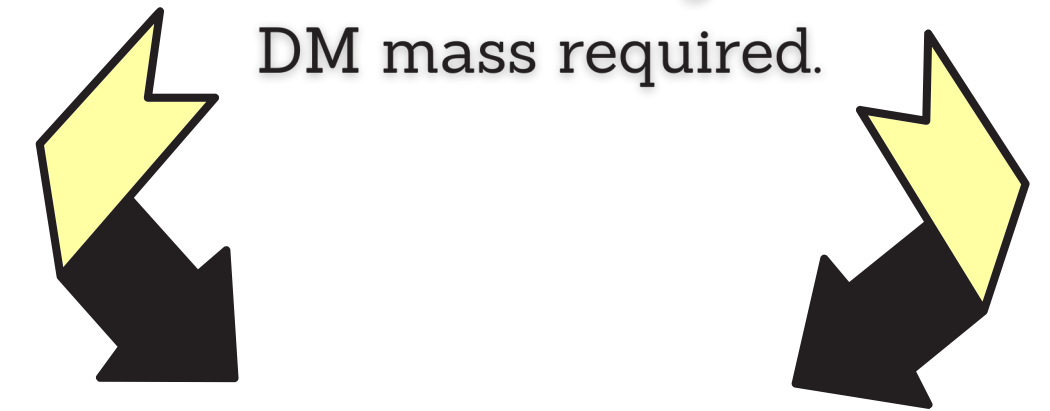


The larger the entropy after the decay of the scalar field, the smaller the cross-sections and the lighter the DM mass required.

Early Matter-dominated



The larger the entropy after the decay of the scalar field, the smaller the cross-sections and the lighter the DM mass required.

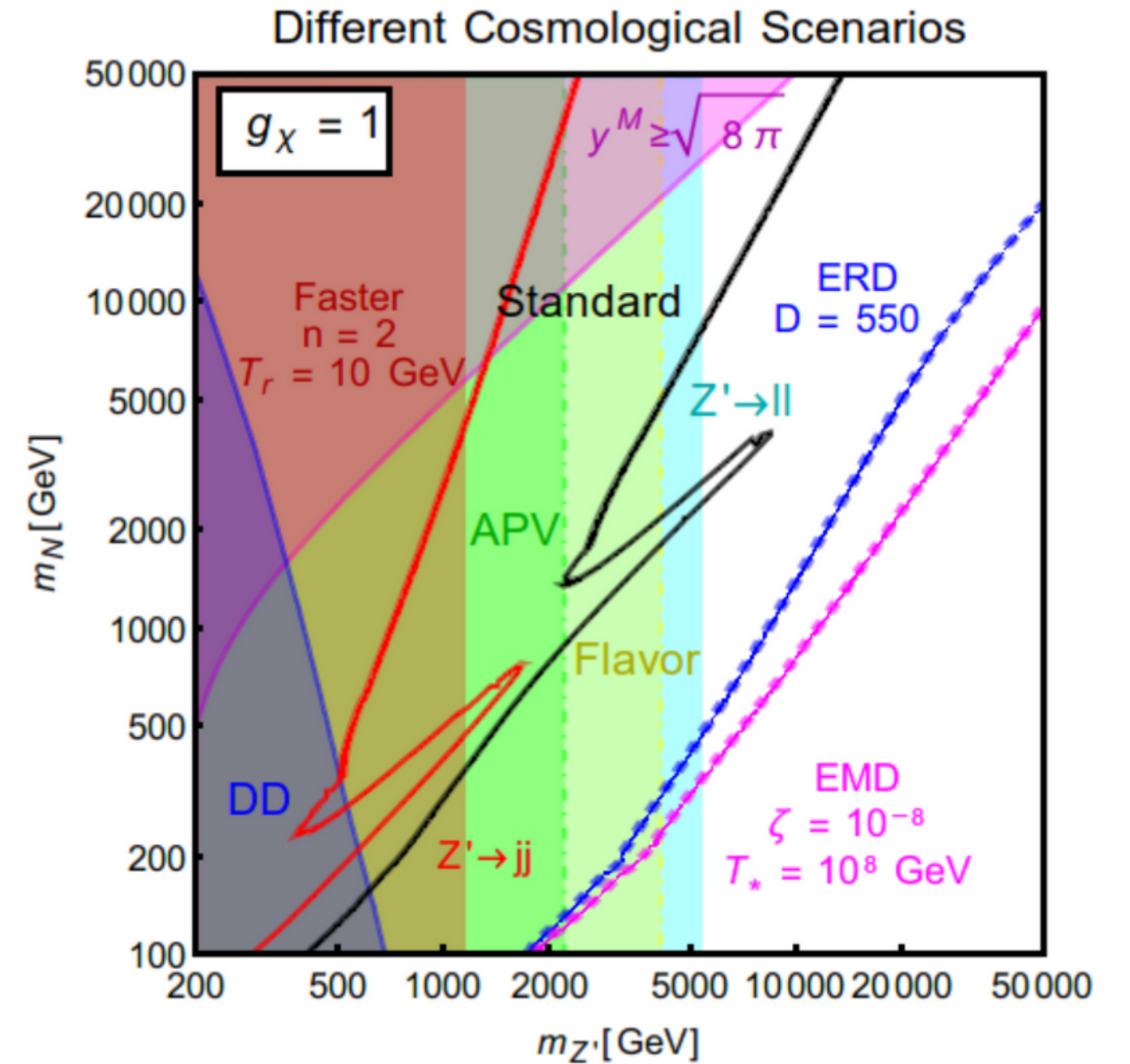


The entropy after the decay must be larger for matter-dominated freeze-out.

ARXIV

2108.XXXXX

The Relentless phase \times Entropy injection

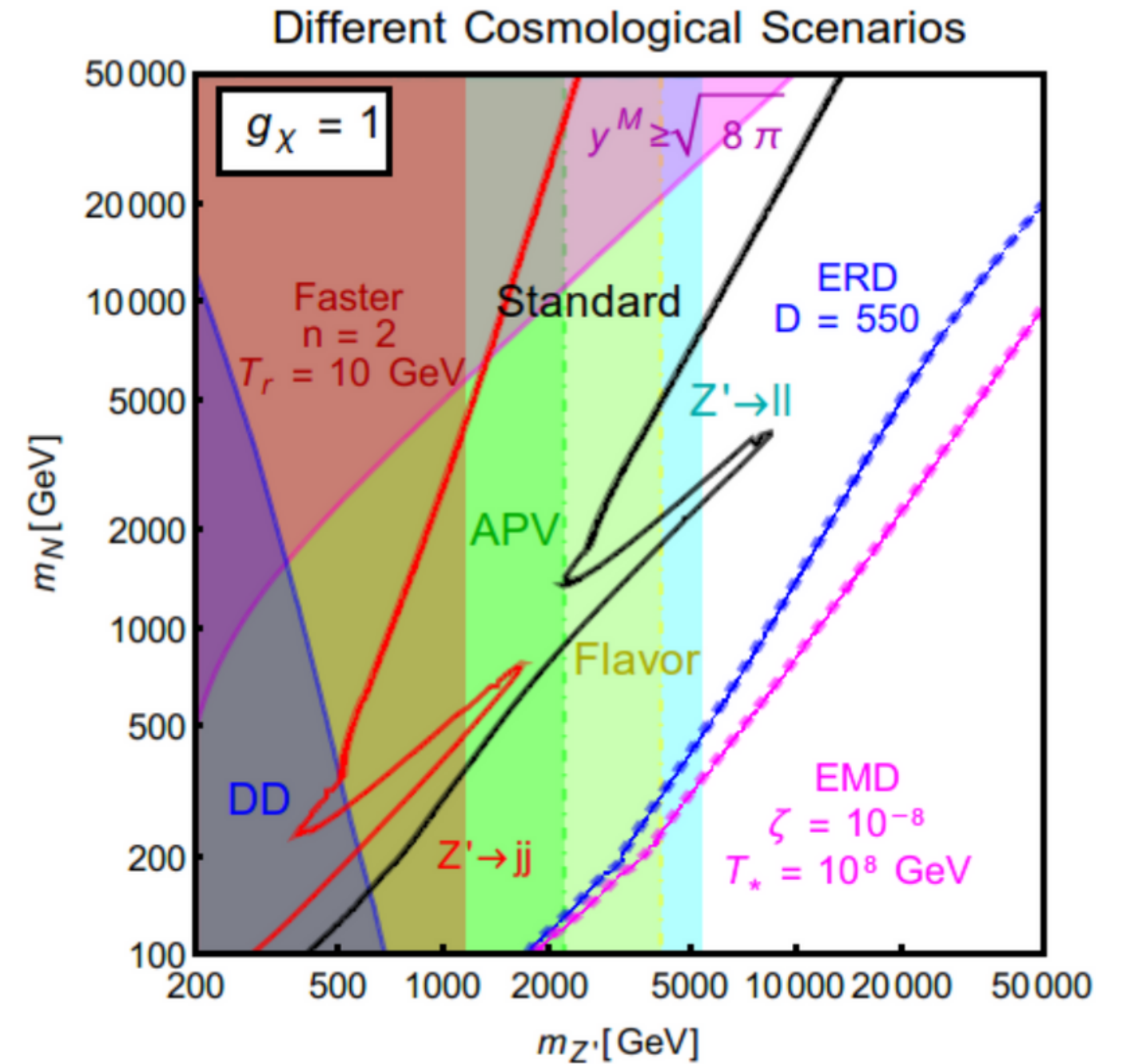


ARXIV

2108.XXXXX

The Relentless phase \times Entropy injection

Freeze-out during larger expansion rates requires larger cross-sections.



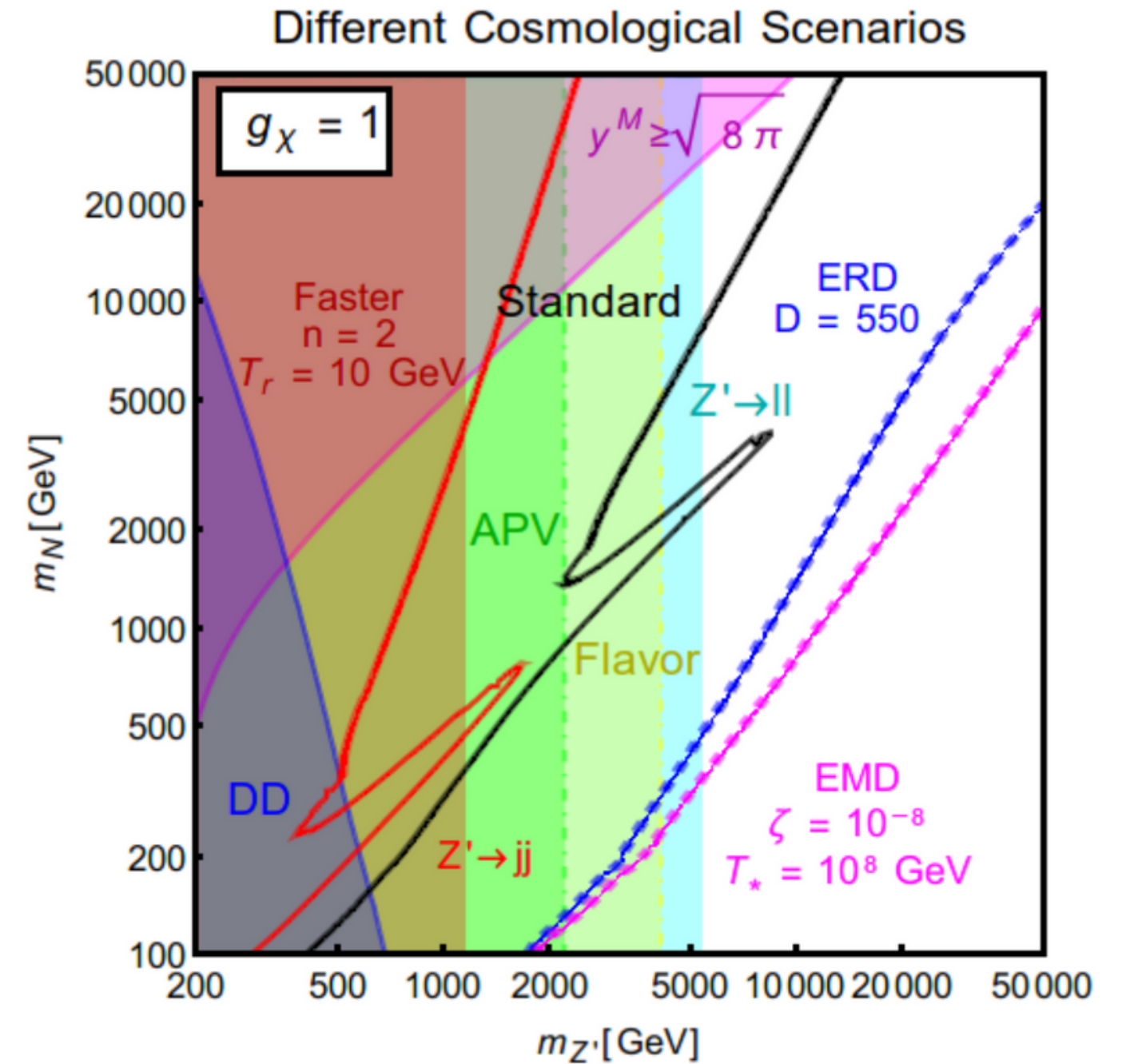
ARXIV

2108.XXXXX

The Relentless phase **x** Entropy injection

Freeze-out during larger expansion rates requires larger cross-sections.

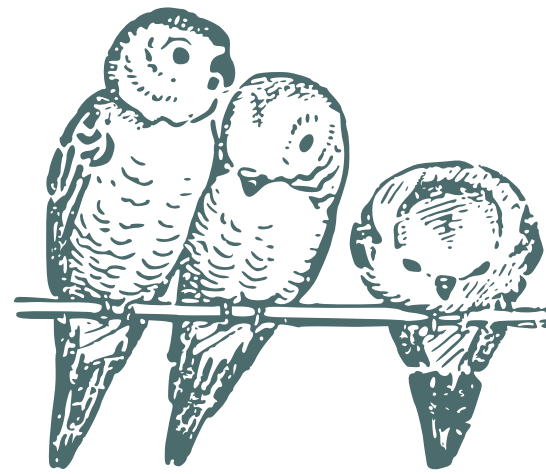
Post-freeze-out in which the DM number density is suppressed by unstable matter field gives lower cross-sections.



Conclusions



Conclusions



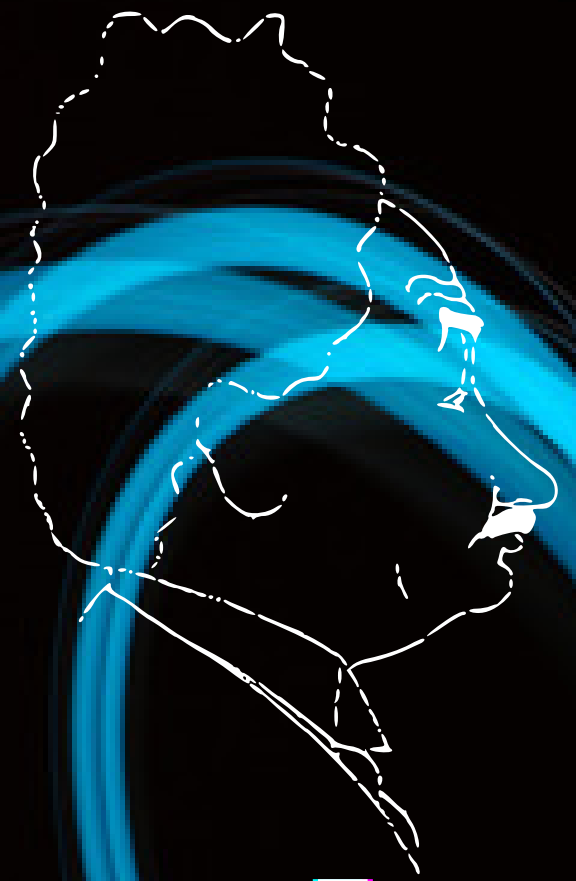
- We explored the impact of different non-standard cosmologies on the right-handed neutrino in a 2HDM augmented by B-L gauge symmetry.
 1. Relentless freeze-out (faster than usual early expansion);
 2. Radiation-dominated freeze-out; and
 3. Matter-dominated freeze-out.
- For faster expanding, it is very bounded due to large cross-sections.
- For early radiation-dominated freeze-out, the model can be completely unconstrained for DM mass around $\simeq 200$ GeV.
- For early matter-dominated freeze-out, a completely unconstrained DM mass arises from nearly 400 GeV up so.



Thank you!

The Dark Side of the Slides

Backup



The Particle Physics Model

Particle Content

STANDARD QUARK SECTOR

$$Q_{aL} = \begin{pmatrix} u_{aL} \\ d_{aL} \end{pmatrix} \sim (\mathbf{3}, \mathbf{2}, 1/6, 1/3),$$

$$u_{aR} \sim (\mathbf{3}, \mathbf{1}, 2/3, 1/3) \text{ and } d_{aR} \sim (\mathbf{3}, \mathbf{1}, -1/3, 1/3).$$

STANDARD LEPTONIC SECTOR + 3RHN

$$L_{aL} = \begin{pmatrix} e_{aL} \\ \nu_{aL} \end{pmatrix} \sim (\mathbf{1}, \mathbf{2}, -1/2, -1),$$

$$e_{aR} \sim (\mathbf{1}, \mathbf{1}, -1, -1) \text{ and } N_{aR} \sim (\mathbf{1}, \mathbf{1}, 0, -1),$$

GAUGE SECTOR

$$A, W^\pm, Z, Z' \text{ and } g_i \text{ (gluons)}$$

Type I 2HDM augmented by B-L gauge symmetry

SCALAR SECTOR

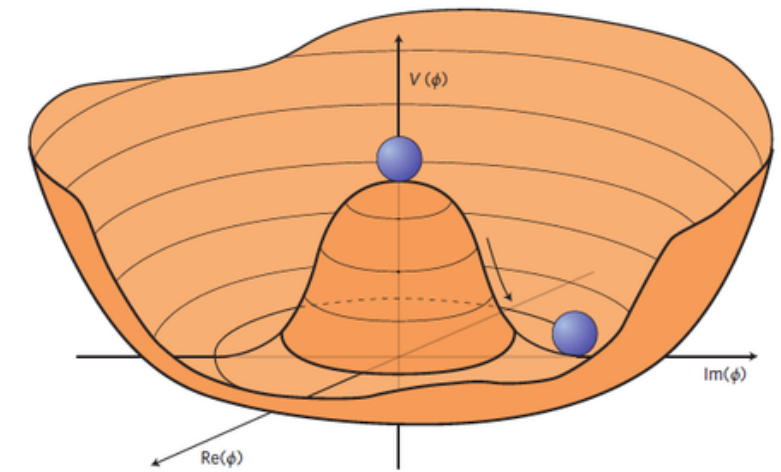
$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \phi_1^0 \end{pmatrix} \sim (\mathbf{1}, \mathbf{2}, 1/2, 2),$$

$$\Phi_2 = \begin{pmatrix} \phi_2^+ \\ \phi_2^0 \end{pmatrix} \sim (\mathbf{1}, \mathbf{2}, 1/2, 0),$$

$$\Phi_s \sim (\mathbf{1}, \mathbf{1}, 0, 2).$$



Yukawa Lagrangian



John Ellis et al. ([ArXiv: 1504.07217](https://arxiv.org/abs/1504.07217))

$$-\mathcal{L}_{Y_1} = y_{ab}^d \bar{Q}_a \Phi_2 d_{bR} + y_{ab}^u \bar{Q}_a \tilde{\Phi}_2 u_{bR} + y_{ab}^e \bar{L}_a \Phi_2 e_{bR} + h.c.,$$

Fermions interact only with the second doublet.

$$-\mathcal{L}_{Y_2} \supset y_{ab} \bar{L}_a \tilde{\Phi}_2 N_{bR} + y_{ab}^M \overline{(N_{aR})^c} \Phi_s N_{bR} + h.c.,$$

The scalar singlet spontaneously breaks the B-L symmetry.

@ Dirac mass

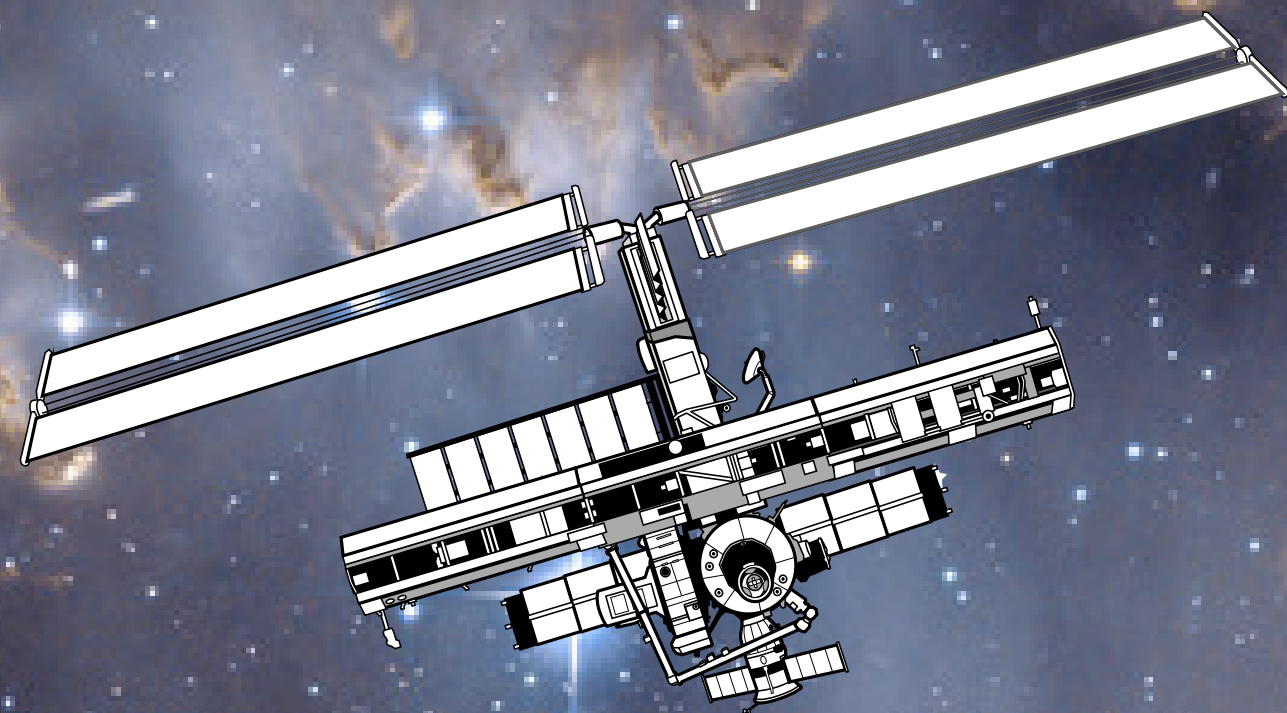
@ Majorana mass

The DM candidate is odd under a Z_2 symmetry to ensure stability.

The other two neutrinos generate the active neutrino masses via Type I Seesaw Mechanism.



$$(\nu \ N) \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu \\ N \end{pmatrix}$$



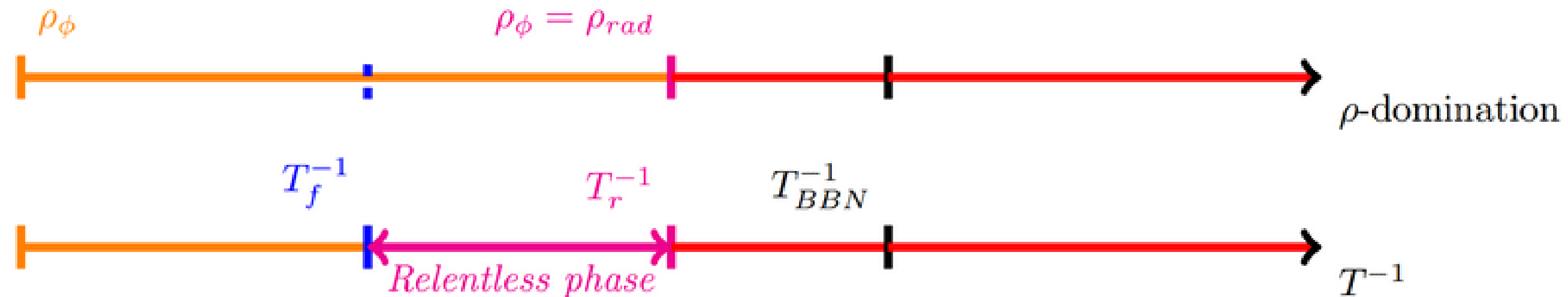
Non-standard Cosmologies

Faster Than Usual Early Expansion

Brief Thermal History

$$\rho_\phi(t) \propto a(t)^{-(4+n)}, \quad n > 0$$

$$\rho_\phi(T) = \rho_\phi(T_r) \left(\frac{g_{\star s}(T)}{g_{\star s}(T_r)} \right)^{(4+n)/3} \left(\frac{T}{T_r} \right)^{4+n}$$



$$\rho(T) = \rho_R(T) + \rho_\phi(T)$$

$$= \rho_R(T) \left[1 + \frac{g_\star(T_r)}{g_\star(T)} \left(\frac{g_{\star s}(T)}{g_{\star s}(T_r)} \right)^{(4+n)/3} \left(\frac{T}{T_r} \right)^n \right]$$

The Cosmological Parameters

$$(n, T_r)$$

$$T_r \gtrsim (15.4)^{1/n} \text{ MeV}$$

Faster Than Usual Early Expansion

The Relentless Phase

For s-wave annihilation cross-section and $n \geq 2$.

$H \propto T^{2+n/2}$ and after freeze-out $\Gamma \propto T^3$, starting the relentless phase in which DM tries unsuccessfully get back to thermal equilibrium.

Just when T_r , the Hubble rate wins and the relentless phase takes over.