

Electroweak Precision Physics at FCC-ee

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FUTURE
CIRCULAR
COLLIDER

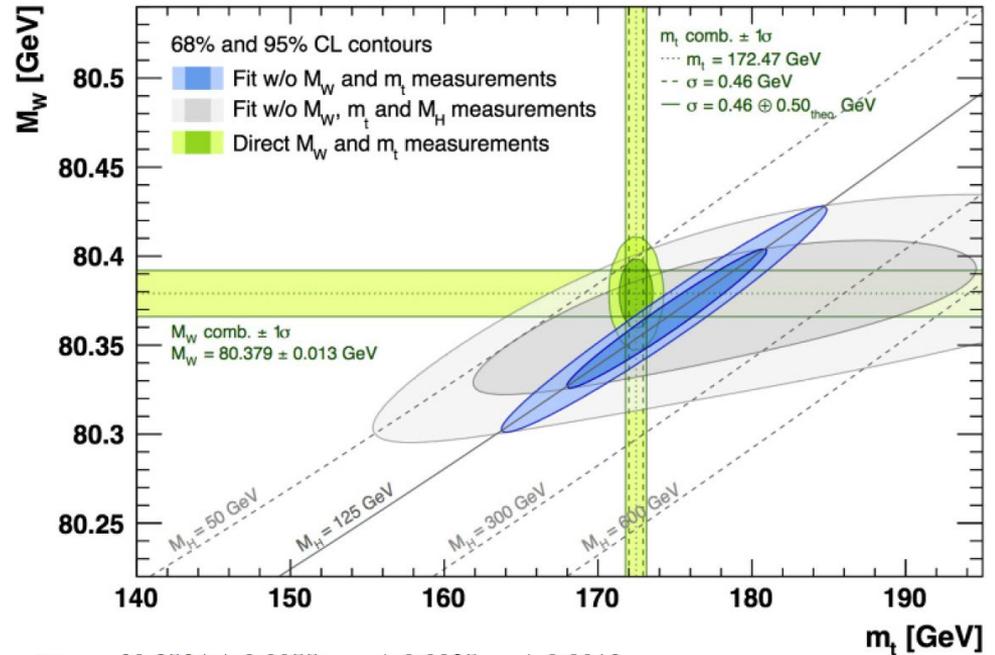
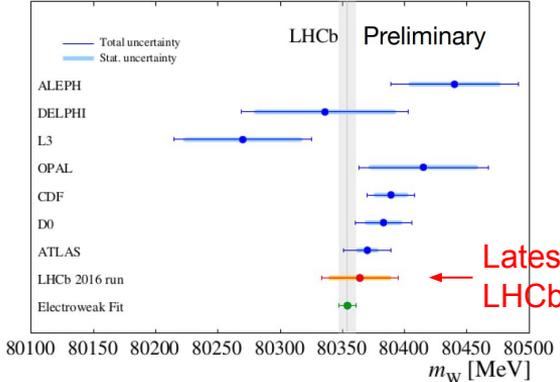


EWK measurements overview

Contour fits of EWK measurements with experimental data available to date

Higher precision on EWK parameters enable further constraints and test SM closure tests:

- Direct sensitive to new physics
- Parameters entangled: m_W , m_{top} , α_S , ...
- Also theory improvements necessary



$$m_W = 80.3584 \pm 0.0055_{m_{top}} \pm 0.0025_{m_Z} \pm 0.0018_{\alpha_{QED}} \pm 0.0020_{\alpha_S} \pm 0.0001_{m_H} \pm 0.0040_{\text{theory}} \text{ GeV}$$

Data PDG: 80.379 ± 0.012 GeV

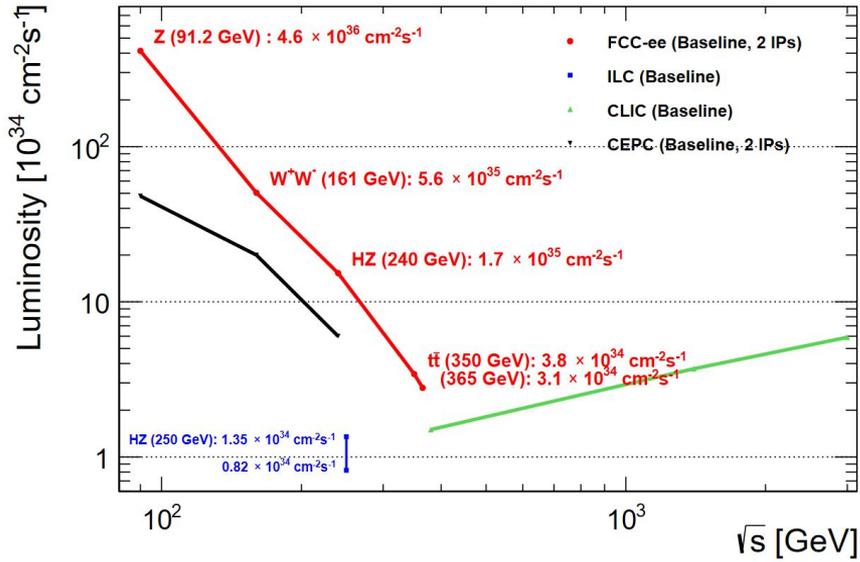
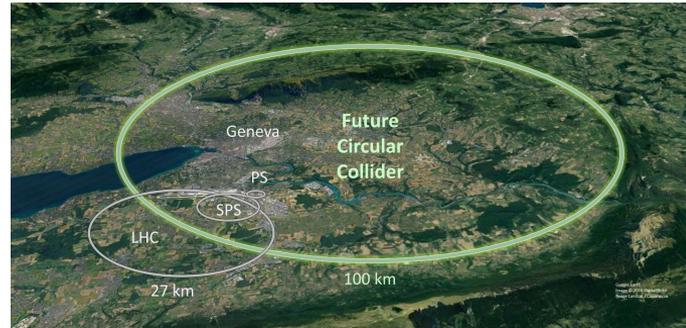
$$\sin^2 \theta_W^{\text{eff}} = 0.231488 \pm 0.000029_{m_{top}} \pm 0.000015_{m_Z} \pm 0.000035_{\alpha_{QED}} \pm 0.000010_{\alpha_S} \pm 0.000001_{m_H} \pm 0.000047_{\text{theory}}$$

Data PDG: 0.23121 ± 0.00004



FCCee overview

- Circular e+/e- collider with ~ 100 km in circumference
- Colliding at 2 interaction points (4 IPs under discussion)
- Facility to host hh collider at later stage (cfr. LEP-LHC)
- Foreseen timeline: construction 2030-40, operation 40-55 (15y)



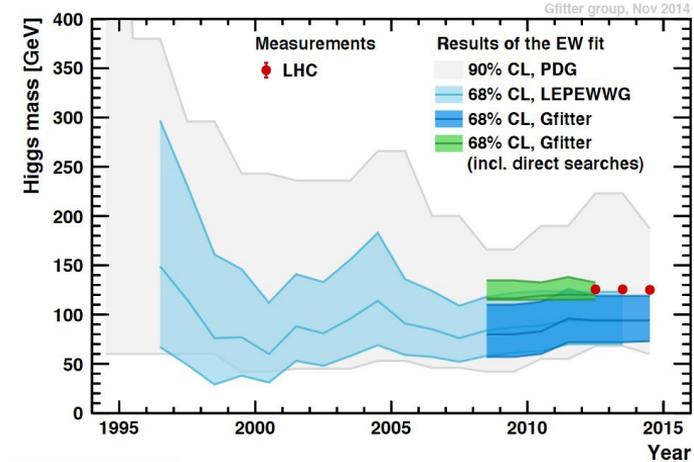
Multiple energy points exploiting large range of physics			
Threshold	Center-of-mass	Luminosity	Events
Z-pole	91 GeV	150	5x10 ⁶ M Z
WW-pole	161 GeV	12	50M WW
H-pole	240 GeV	5	1M ZH
tt-pole	365 GeV	1.5	1M tt

FCCee physics potential

“FCCee = TeraZ or Higgs factory”: true, but also a discovery machine!

Rich physics programme including (EWK) precision measurements:

- Mass, width, cross section of W, Z, top and Higgs
- Strong and electromagnetic coupling constants at various \sqrt{s}
- Neutrino species/Z-invisible
- Flavor physics
- Direct searches for new physics
- ...



Put large constraints on SM EWK parameter space, narrowing down closure tests hence sensitive to new physics

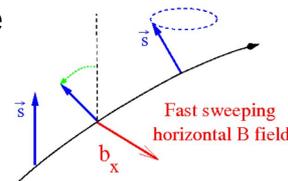
Ref.: [“Future Circular Collider Study, Volume 1: Physics Opportunities, Conceptual Design Report, preprint edited by M. Mangano et al. CERN accelerator reports, CERN-ACC-2018-0056, Geneva, December 2018. Published in Eur. Phys. J. C”](#)

To further increase and optimize the physics potential, a detailed feasibility study is needed:

- Baseline of machine parameters and detector concepts
- Assess impact on systematic uncertainties with direct feedback to machine/detector R&D
- Assess shortcomings on theory

Key elements of FCCee for order-of-magnitude(s) improvement of EWK precision measurements

- 1) **High statistics** (e.g. 10^7 times more Zs than LEP1)
- 2) **Dedicated energy points** for precision measurements and combinations → unique programme
- 3) **In-situ beam energy calibration** ([arXiv:1909.12245](https://arxiv.org/abs/1909.12245)):
 - Center-of-mass uncertainty dominant for many EWK precision (mass) measurements
 - Z/WW: resonant depolarisation measurements on a continuous basis → 10^{-6} relative accuracy achievable
100(300) keV unc. at Z(WW)
 - Higher energies: cannot use RDP, usage of Z- γ radiative return events (~ 2 MeV at 240 GeV)
- 4) **Online luminosity meter**:
 - Precise knowledge of luminosity important for cross-section measurements
 - Using Bhabha-scattering events with dedicated forward detector → $dL/L \sim 10^{-4}$ accuracy achievable
Point-to-point $\sim 10^{-5}$
- 5) Detectors: high granularity, improved impact parameter → **better reconstruction and resolutions**
- 6) **Very clean environment** (cfr. LEP)





Z lineshape – $\alpha_{\text{QED}}(m_Z^2)$

Z → μμ forward/backward asymmetry sensitive to $\alpha_{\text{QED}}(m_Z^2)$ due to Z-γ interference:

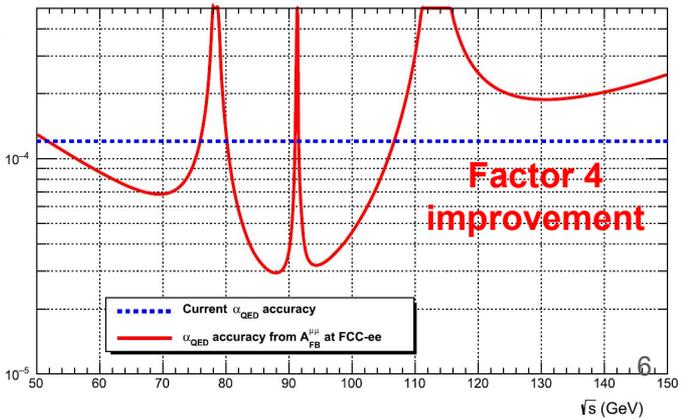
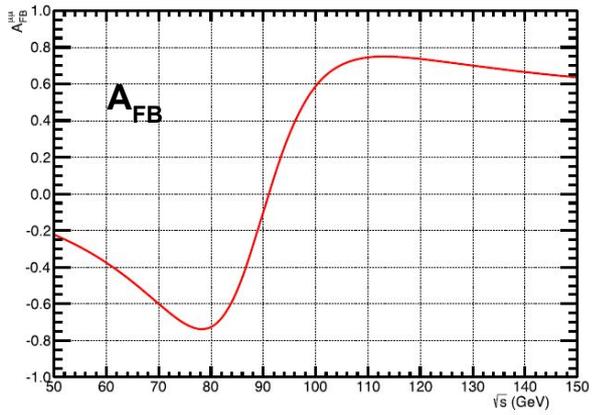
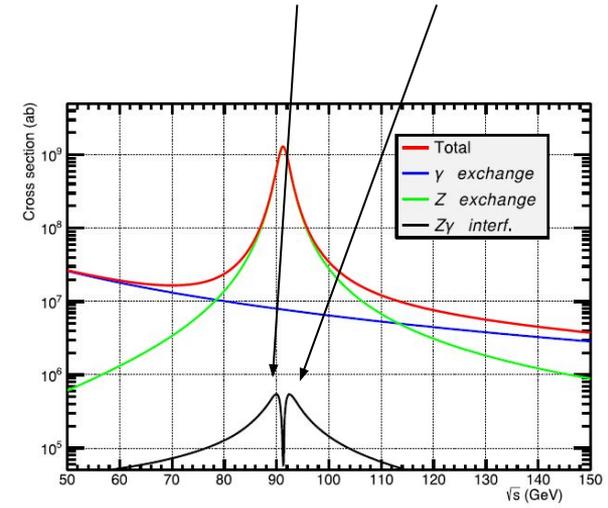
$$A_{\text{FB}}^{\mu\mu}(s) \simeq \frac{3}{4} \mathcal{A}_e \mathcal{A}_\mu \times \left[1 + \frac{8\pi \sqrt{2} \alpha_{\text{QED}}(s)}{m_Z^2 G_F (1 - 4 \sin^2 \theta_W^{\text{eff}})^2} \frac{s - m_Z^2}{2s} \right]$$

→ strongly depends on \sqrt{s}
 → **direct** measurement of $\alpha_{\text{QED}}(s)$ at $\sqrt{s} \neq m_Z$
 → measure $\sin^2 \theta_W$ to high precision (later)

Perform line-scan around Z-pole to maximise Z-γ interference and measure A_{FB} :

- Nominal 91.2 GeV, 80 /ab
- Off-peak: 87.7 and 93.9 GeV, each 40 /ab

→ Measure $\alpha_{\text{QED}}(m_Z^2)$ to 3×10^{-5} rel. precision (currently 1.1×10^{-4})
 → Stat. dominated; syst. uncertainties $< 10^{-5}$ (dominated by \sqrt{s} calib)
 → Theoretical uncertainties $\sim 10^{-4}$, higher order calcs needed



Z peak – $\sin^2\theta_W$

Z → $\mu\mu$ forward/backward asymmetry also used to measure ewk mixing angle $\sin^2\theta_W$ at Z-pole = 91.2 GeV:

$$A_{FB}^{\mu\mu}(s) \simeq \frac{3}{4} \mathcal{A}_e \mathcal{A}_\mu \longrightarrow \mathcal{A}_e = \frac{g_{L,e}^2 - g_{R,e}^2}{g_{L,e}^2 + g_{R,e}^2} = \frac{2v_e/a_e}{1 + (v_e/a_e)^2}, \text{ with } v_e/a_e \equiv 1 - 4 \sin^2 \theta_W^{\text{eff}}$$

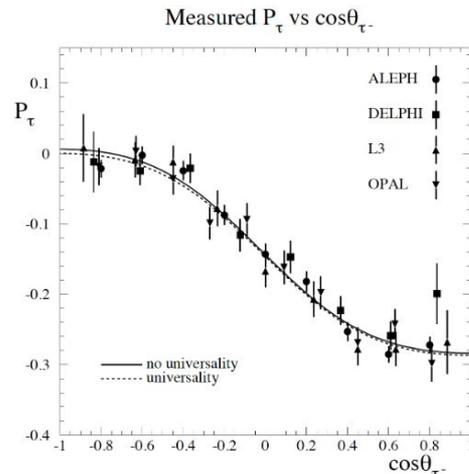
$$\Delta A_{FB}^{\mu\mu}(s) \sim 3 \times 10^{-6} \text{ (stat)} + 4 \times 10^{-6} \text{ (syst)}$$

- Measure $\sin^2\theta_W$ to 3×10^{-6} abs. precision (currently 1.6×10^{-4})
- Assumes lepton universality: $\mathcal{A}_e = \mathcal{A}_\mu$
- Mainly dominated by energy calibration (point-to-point)

Tau polarization used to constrain the mixing angle to a similar precision

- No assumption on lepton universality (direct separation \mathcal{A}_e and \mathcal{A}_τ)
- \mathcal{A}_τ from P_τ : benefit from high statistics and very robust measurement

$$P_\tau(\cos\theta) = \frac{A_{pol}(1 + \cos^2\theta) + \frac{8}{3} A_{pol}^{FB} \cos\theta}{(1 + \cos^2\theta) + \frac{8}{3} A_{FB} \cos\theta} \implies P_\tau \equiv \frac{\sigma(\tau_R) - \sigma(\tau_L)}{\sigma(\tau_R) + \sigma(\tau_L)} \simeq -2(1 - 4 \sin^2\theta_W)$$





Z lineshape – mass, width and σ_{had}^0

→ **Mass** ± 4 keV (stat) ± 100 keV (syst) [LEP 2.1 MeV]

- Systematics limited due to beam calibration uncertainties (RDP ~ 100 keV)

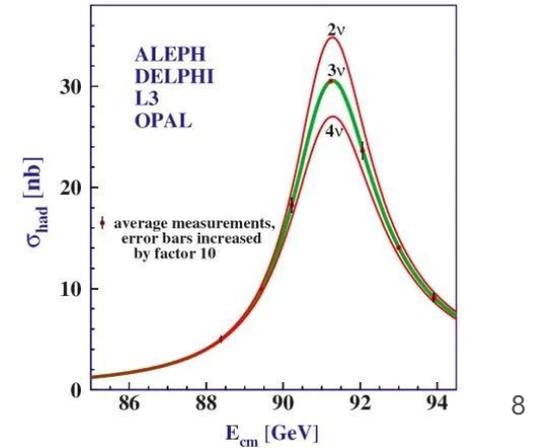
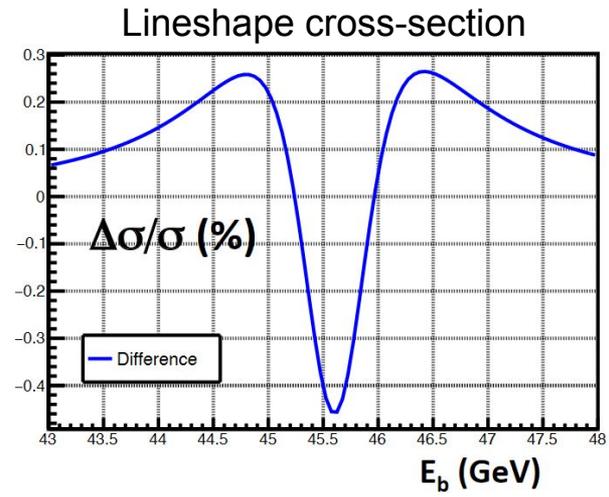
→ **Width** ± 4 keV (stat) ± 25 keV (syst) [LEP 2.3 MeV]

- Systematics dominated by:
 - Relative (point-to-point) uncertainty on the $\sqrt{s} \sim 22$ keV
 - Impact on beam-energy spread uncertainty ~ 10 keV
 - Absolute uncertainty on BES ~ 84 MeV
 - Constrained using $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ events:
 - Constrain BES uncertainty to per-mille level
 - Taking into account asymmetric beam optics (x-angle $\alpha 30$ mrad) and γ -ISR
 - Muon angular resolution ~ 0.1 mrad required

→ **Hadronic cross-section** $\sigma_{\text{had}}^0: \pm 4$ pb [LEP 37 pb]

→ **Number of neutrino families:** 1×10^{-3} (abs) [LEP 7×10^{-3}]

- Dominated by luminosity uncertainty





Z peak – couplings and $\alpha_s(m_Z^2)$

Couplings measured from ratio of hadronic and leptonic partial widths

→ need control on detector acceptances: detector precision $\sim 10 \mu\text{m}$

	Statistical uncertainty	Systematic uncertainty
$R_{\mu} (R_{\ell})$	10^{-6}	5×10^{-5}
R_{τ}	1.5×10^{-6}	10^{-4}
R_e	1.5×10^{-6}	3×10^{-4}
R_b	5×10^{-5}	3×10^{-4}
R_c	1.5×10^{-4}	15×10^{-4}

Relative stat. and syst. unc. (similar)



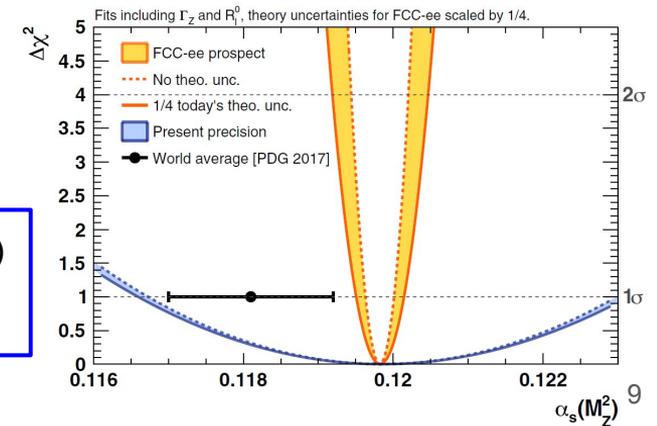
fermion type	g_a	g_v
e	1.5×10^{-4}	2.5×10^{-4}
μ	2.5×10^{-5}	$2. \times 10^{-4}$
τ	0.5×10^{-4}	3.5×10^{-4}
b	1.5×10^{-3}	1×10
c	2×10^{-3}	1×10

Relative unc. on couplings

1-2 orders of magnitude Improvement w.r.t. LEP

Extract strong coupling constant $\alpha_s(m_Z^2)$ using leptonic/hadronic width ratio: $R_1 = \Gamma_{\text{had}} / \Gamma_{\text{lep}}$

→ $\Delta\alpha_s(m_Z) \sim 1 \times 10^{-5}$ (stat) + 1.5×10^{-4} (syst) abs. (current value $\Delta\alpha_s$ 30×10^{-4})
 → Systematically dominated (acceptance)





WW threshold

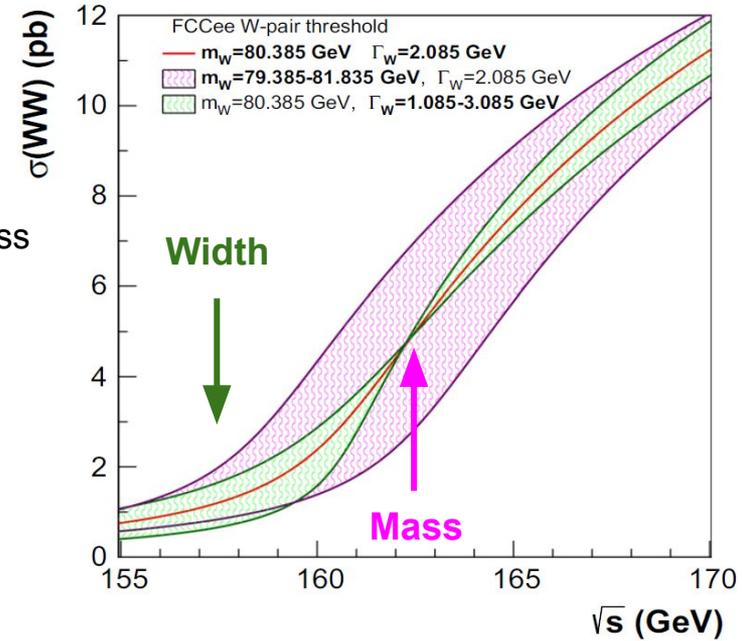
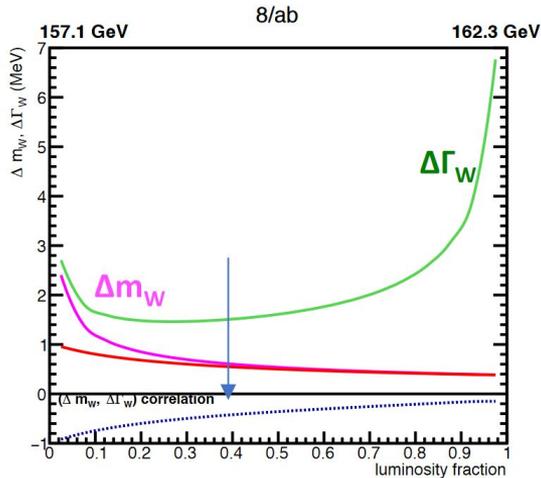
W mass and width extracted from line-scans using WW xsec

2 energy points determined from Δm_W and $\Delta \Gamma_W$ sensitivities on WW xsec:

→ **157.1 GeV width measurement:** maximum sensitivity on width

→ **162.5 GeV mass measurement:** minimal impact on width, max. on mass

Luminosity ($<10^{-4}$) and center-of-mass (< 0.5 MeV) uncertainties to be controlled, but weaker constraints than on Z pole



Combined fit with optimized lumi fraction ($f=0.4$: 5 /ab at 157.1, 7 /ab at 162.5)

→ precision m_W to 0.25 (stat) + 0.3 (syst) MeV (present 15 MeV)

→ precision Γ_W to 1.2 (stat) + 0.3 (syst) MeV (present 42 MeV)



W kinematic reconstruction

Independent analysis on W mass and width using kinematic reconstruction techniques in WW → qq ν events

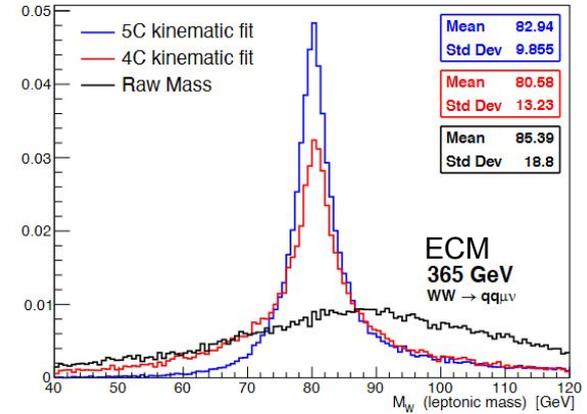
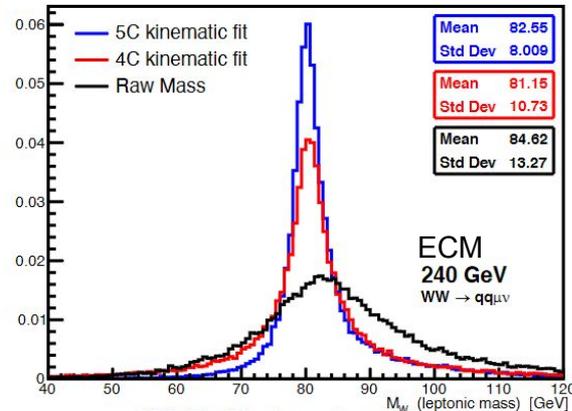
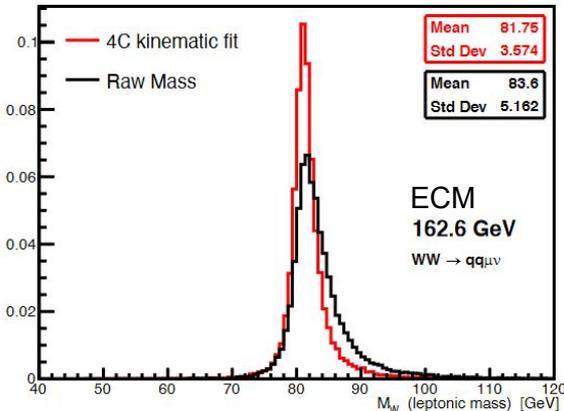
- Profit from precise angle and velocity (β) measurements
- Run at all kinematically accessible energy points (WW, ZH and tt)
- Put conditions on detector requirements

Δm_W (stat) ~ 250 keV → similar as xsec measurement

$\Delta \Gamma_W$ (stat) ~ 350 keV → reduction factor 2-3

Source	Δm_W (MeV/c ²)				$\Delta \Gamma_W$ (MeV)			
	e ν q \bar{q}	$\mu\nu$ q \bar{q}	$\tau\nu$ q \bar{q}	$\ell\nu$ q \bar{q}	e ν q \bar{q}	$\mu\nu$ q \bar{q}	$\tau\nu$ q \bar{q}	$\ell\nu$ q \bar{q}
e+ μ momentum	3	8	-	4	5	4	-	4
e+ μ momentum resoln	7	4	-	4	65	55	-	50
Jet energy scale/linearity	5	5	9	6	4	4	16	6
Jet energy resoln	4	2	8	4	20	18	36	22
Jet angle	5	5	4	5	2	2	3	2
Jet angle resoln	3	2	3	3	6	7	8	7
Jet boost	17	17	20	17	3	3	3	3
Fragmentation	10	10	15	11	22	23	37	25
Radiative corrections	3	2	3	3	3	2	2	2
LEP energy	9	9	10	9	7	7	10	8
Calibration (e ν q \bar{q} only)	10	-	-	4	20	-	-	9
Ref MC Statistics	3	3	5	2	7	7	10	5
Bkgnd contamination	3	1	6	2	5	4	19	7

Limited by systematics (beam energy, resolution, fragmentation) → constrain



CLD Detector Concept



W decay branching ratios

Precise measurement of W decays

- Precise control of lepton ID to avoid cross contamination in signal channels (e.g. $\tau \rightarrow e, \mu$ vs. e, μ channels)
- Precision of 10^{-4} achievable (rel.)
- Simultaneously probe lepton and q/l universality to high precision ($\sim 10^{-4}$)

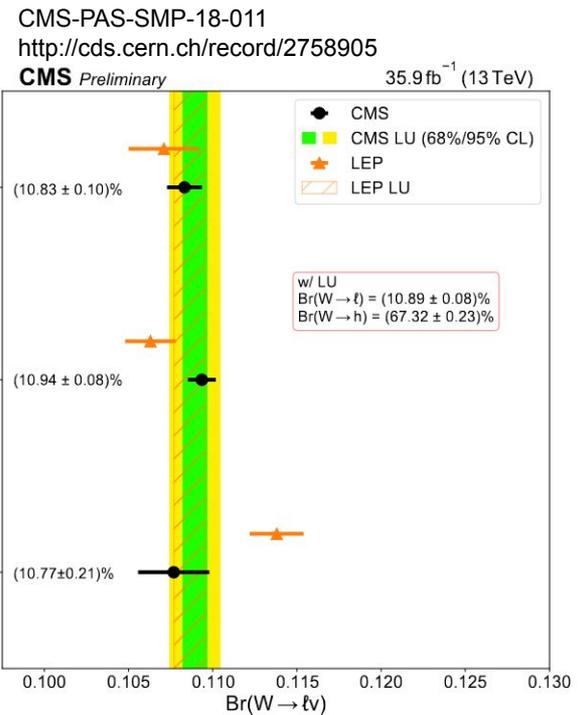
Decay mode	relative precision	B(W \rightarrow ev)	B(W \rightarrow $\mu\nu$)	B(W \rightarrow $\tau\nu$)	B(W \rightarrow qq)
LEP2		1.5 %	1.4 %	1.8 %	0.4 %
CMS		0.9 %	0.7 %	2 %	0.4 %
FCCee		0.03 %	0.03 %	0.04 %	0.01 %

Flavor tagging

- Allows precise measurement CKM matrix elements V_{cs}, V_{ub}, V_{cb}
- Extract strong coupling constant at WW-threshold

$$R_W = \frac{B_q}{1 - B_q} = \left(1 + \frac{\alpha_S(m_W^2)}{\pi} \right) \sum_{i=u,c; j=d,s,b} |V_{ij}|^2$$

$\rightarrow \Delta\alpha_S(m_W) \sim 3 \times 10^{-4}$ (abs)
 \rightarrow Statistically dominated



Top mass and width measurement

Top mass and width measurements similar as WW line-shape

Though more energy points needed:

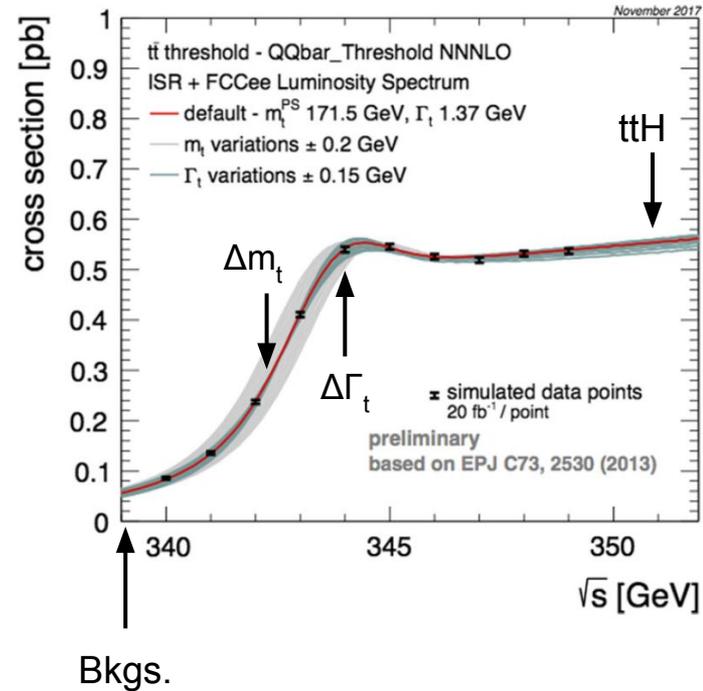
- Relative large uncertainty on top mass (± 0.5 GeV)
- Need to constrain shape in optimal way
- Possible to constrain backgrounds (below) and ttH (above)

→ Multipoint scan in 5 GeV window [340, 345], each ~ 25 /fb

→ Δm_t (stat) ~ 17 MeV (syst negligible)

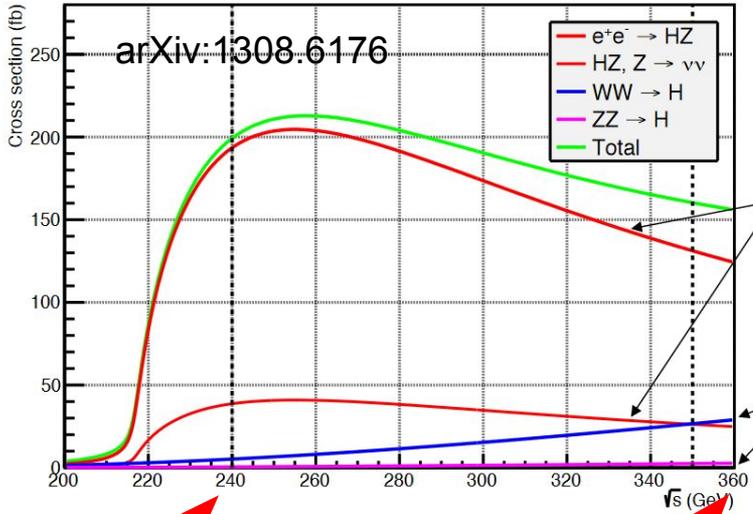
→ $\Delta \Gamma_t$ (stat) ~ 45 MeV (syst negligible)

To date: theoretical QCD errors order of 40 MeV for mass and width





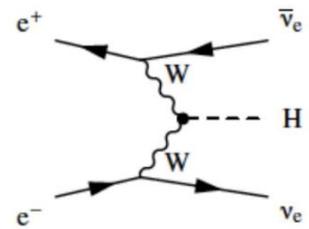
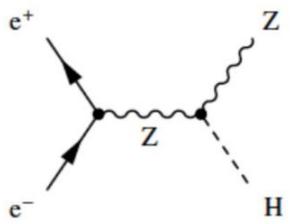
Higgs physics at FCCee



arXiv:1308.6176

240 GeV, 5 /ab
10⁶ ZH events
25k WWH events

365 GeV, 1.5 /ab
200k ZH events
50k WWH events



Higgs-pole at 240 GeV

- Higgs-strahlung dominant: $e^+e^- \rightarrow ZH$
- Precise Higgs **mass measurement** up to ~ 5 MeV
- Measurement of **decay-mode-independent xsec** to % level, sensitive to new physics $H \rightarrow$ invisible
- Higgs width extracted from $H \rightarrow ZZ$ at % level

Top threshold at 365 GeV

- Opens significance for WW fusion: $e^+e^- \rightarrow WW\nu\nu \rightarrow H\nu\nu$
- Significant reduction in couplings and width

Combined performance at both energy points

- Higgs coupling precision $<$ % level
- In particular, exotic Higgs decays constraint to < 1 %
- Probing CP violation using $H \rightarrow \pi\pi$ phase

→ [See dedicated talk Tuesday by S. Braibant](#)



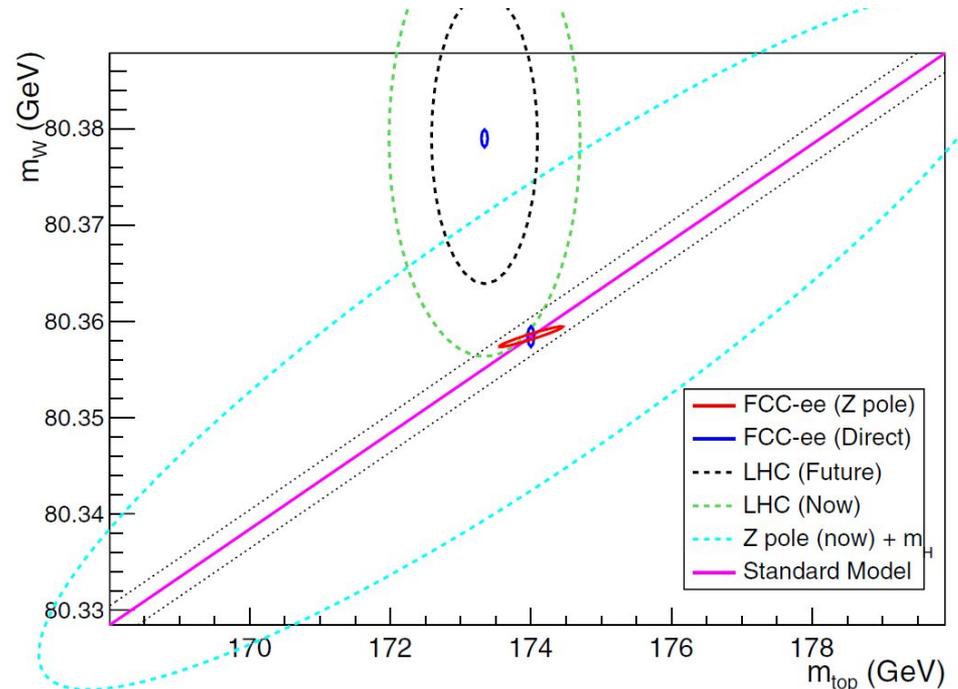
Rich physics programme at Z-threshold and higher energies

- FCC delivers excellent precision on various EWK parameters with improvements of 1-2 orders of magnitude
- Combined results at all energy thresholds provides unique closure tests for SM

→ Ongoing efforts with several analyses to explore and evaluate physics potential

→ Feedback towards detector and machine R&D for systematic uncertainty reduction on key measurements

→ Work on theoretical side needed to cope with experimental level of accuracy



Backup



FCCee Physics Performance overview

[ArXiv 2106.13885](https://arxiv.org/abs/2106.13885)

Observable	present value \pm error	FCC-ee Stat.	FCC-ee Syst.	Comment and leading exp. error
m_Z (keV)	91186700 \pm 2200	4	100	From Z line shape scan Beam energy calibration
Γ_Z (keV)	2495200 \pm 2300	4	25	From Z line shape scan Beam energy calibration
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	231480 \pm 160	2	2.4	from $A_{\text{FB}}^{\mu\mu}$ at Z peak Beam energy calibration
$1/\alpha_{\text{QED}}(m_Z^2) (\times 10^3)$	128952 \pm 14	3	small	from $A_{\text{FB}}^{\mu\mu}$ off peak QED&EW errors dominate
$R_\ell^Z (\times 10^3)$	20767 \pm 25	0.06	0.2-1	ratio of hadrons to leptons acceptance for leptons
$\alpha_s(m_Z^2) (\times 10^4)$	1196 \pm 30	0.1	0.4-1.6	from R_ℓ^Z above
$\sigma_{\text{had}} (\times 10^3)$ (nb)	41541 \pm 37	0.1	4	peak hadronic cross section luminosity measurement
$N_\nu (\times 10^3)$	2996 \pm 7	0.005	1	Z peak cross sections Luminosity measurement
$R_b (\times 10^6)$	216290 \pm 660	0.3	< 60	ratio of bb to hadrons stat. extrapol. from SLD
$A_{\text{FB},0}^b (\times 10^4)$	992 \pm 16	0.02	1-3	b-quark asymmetry at Z pole from jet charge
$A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$	1498 \pm 49	0.15	<2	τ polarization asymmetry τ decay physics
τ lifetime (fs)	290.3 \pm 0.5	0.001	0.04	radial alignment
τ mass (MeV)	1776.86 \pm 0.12	0.004	0.04	momentum scale
τ leptonic ($\mu\nu_\mu\nu_\tau$) B.R. (%)	17.38 \pm 0.04	0.0001	0.003	c/μ /hadron separation
m_W (MeV)	80350 \pm 15	0.25	0.3	From WW threshold scan Beam energy calibration
Γ_W (MeV)	2085 \pm 42	1.2	0.3	From WW threshold scan Beam energy calibration
$\alpha_s(m_W^2) (\times 10^4)$	1170 \pm 420	3	small	from R_ℓ^W
$N_\nu (\times 10^3)$	2920 \pm 50	0.8	small	ratio of invis. to leptonic in radiative Z returns
m_{top} (MeV/c ²)	172740 \pm 500	17	small	From $t\bar{t}$ threshold scan QCD errors dominate
Γ_{top} (MeV/c ²)	1410 \pm 190	45	small	From $t\bar{t}$ threshold scan QCD errors dominate
$\lambda_{\text{top}}/\lambda_{\text{top}}^{\text{SM}}$	1.2 \pm 0.3	0.10	small	From $t\bar{t}$ threshold scan QCD errors dominate
tZ couplings	\pm 30%	0.5 - 1.5%	small	From $\sqrt{s} = 365$ GeV run