

Electroweak Precision Physics at FCC-ee

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FUTURE
CIRCULAR
COLLIDER

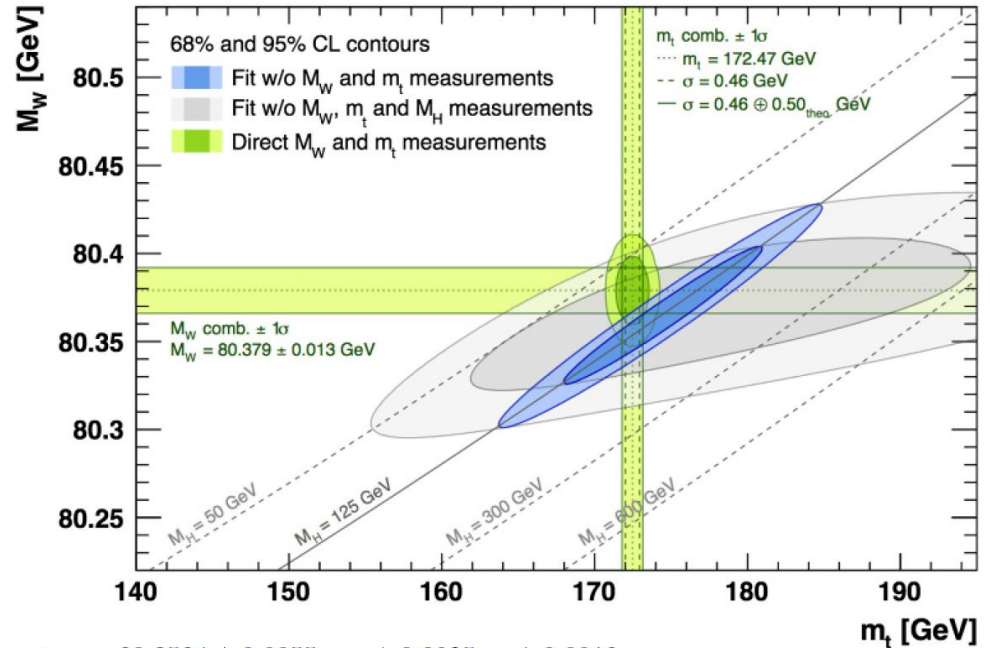
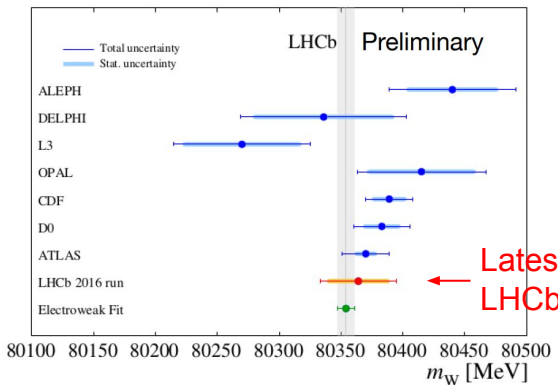


EWK measurements overview

Contour fits of EWK measurements with experimental data available to date

Higher precision on EWK parameters enable further constraints and test SM closure tests:

- Direct sensitive to new physics
- Parameters entangled: m_W , m_{top} , α_S , ...
- Also theory improvements necessary



$$m_W = 80.3584 \pm 0.0055_{m_{top}} \pm 0.0025_{m_Z} \pm 0.0018_{\alpha_{QED}} \pm 0.0020_{\alpha_S} \pm 0.0001_{m_H} \pm 0.0040_{\text{theory}} \text{ GeV}$$

Data PDG 80.379 ± 0.012 GeV

$$= 80.358 \pm 0.008_{\text{total}} \text{ GeV,}$$

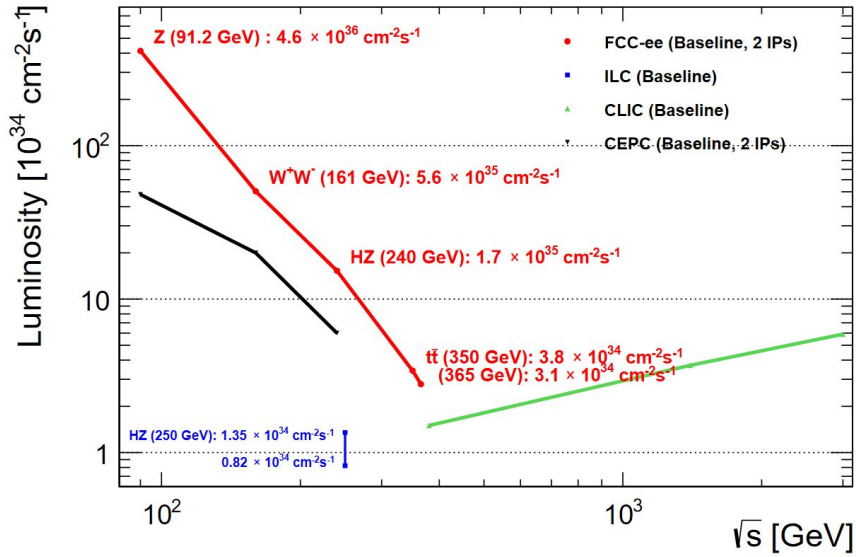
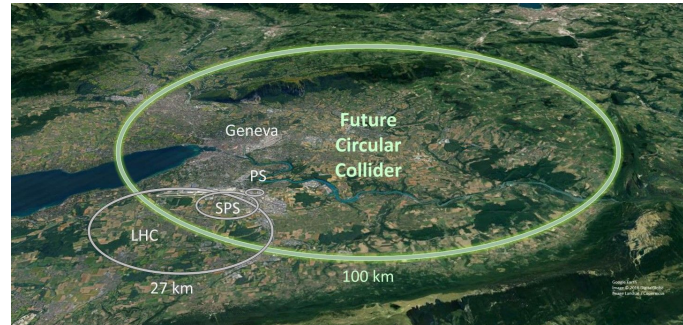
$$\sin^2 \theta_W^{\text{eff}} = 0.231488 \pm 0.000029_{m_{top}} \pm 0.000015_{m_Z} \pm 0.000035_{\alpha_{QED}} \pm 0.000010_{\alpha_S} \pm 0.000001_{m_H} \pm 0.000047_{\text{theory}}$$

Data PDG 0.23121 ± 0.00004



FCCee overview

- Circular e+/e- collider with ~ 100 km in circumference
- Colliding at 2 interaction points (4 IPs under discussion)
- Facility to host hh collider at later stage (cfr. LEP-LHC)
- Foreseen timeline: construction 2030-40, operation 40-55 (15y)



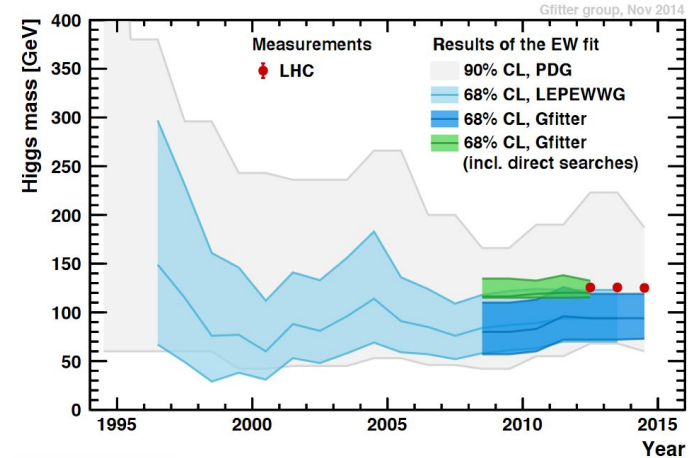
| Multiple energy points exploiting large range of physics | | | |
|--|----------------|------------|---------------------|
| Threshold | Center-of-mass | Luminosity | Events |
| Z-pole | 91 GeV | 150 | 5×10^6 M Z |
| WW-pole | 161 GeV | 12 | 50M WW |
| H-pole | 240 GeV | 5 | 1M ZH |
| tt-pole | 365 GeV | 1.5 | 1M tt |

FCCee physics potential

“FCCee = TeraZ or Higgs factory”: true, but also a discovery machine!

Rich physics programme including (EWK) precision measurements:

- Mass, width, cross section of W, Z, top and Higgs
- Strong and electromagnetic coupling constants at various \sqrt{s}
- Neutrino species/Z-invisible
- Flavor physics
- Direct searches for new physics
- ...



Put large constraints on SM EWK parameter space, narrowing down closure tests hence sensitive to new physics

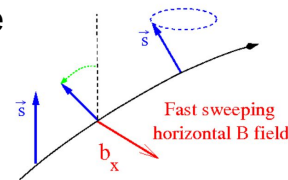
Ref.: [“Future Circular Collider Study, Volume 1: Physics Opportunities, Conceptual Design Report, preprint edited by M. Mangano et al. CERN accelerator reports, CERN-ACC-2018-0056, Geneva, December 2018. Published in Eur. Phys. J. C”](#)

To further increase and optimize the physics potential, a detailed feasibility study is needed:

- Baseline of machine parameters and detector concepts
- Assess impact on systematic uncertainties with direct feedback to machine/detector R&D
- Assess shortcomings on theory

Key elements of FCCee for order-of-magnitude(s) improvement of EWK precision measurements

- 1) **High statistics** (e.g. 10^7 times more Zs than LEP1)
- 2) **Dedicated energy points** for precision measurements and combinations → unique programme
- 3) **In-situ beam energy calibration** ([arXiv:1909.12245](https://arxiv.org/abs/1909.12245)):
 - Center-of-mass uncertainty dominant for many EWK precision (mass) measurements
 - Z/WW: resonant depolarisation measurements on a continuous basis → 10^{-6} relative accuracy achievable
100(300) keV unc. at Z(WW)
 - Higher energies: cannot use RDP, usage of Z- γ radiative return events (~ 2 MeV at 240 GeV)
- 4) **Online luminosity meter**:
 - Precise knowledge of luminosity important for cross-section measurements
 - Using Bhabha-scattering events with dedicated forward detector → $dL/L \sim 10^{-4}$ accuracy achievable
Point-to-point $\sim 10^{-5}$
- 5) Detectors: high granularity, improved impact parameter → **better reconstruction and resolutions**
- 6) **Very clean environment** (cfr. LEP)





Z lineshape – $\alpha_{\text{QED}}(m_Z^2)$

Z $\rightarrow \mu\mu$ forward/backward asymmetry sensitive to $\alpha_{\text{QED}}(m_Z^2)$ due to Z- γ interference:

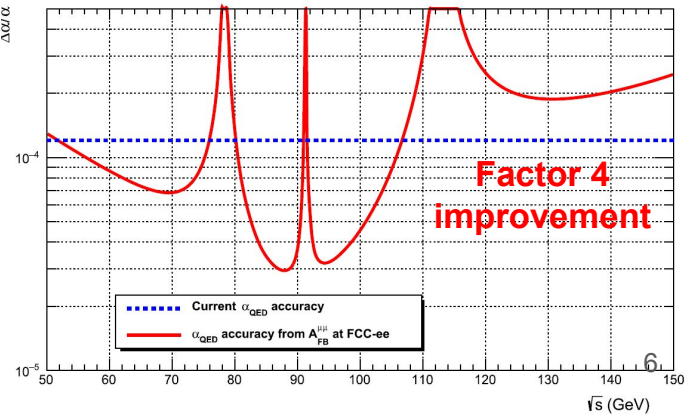
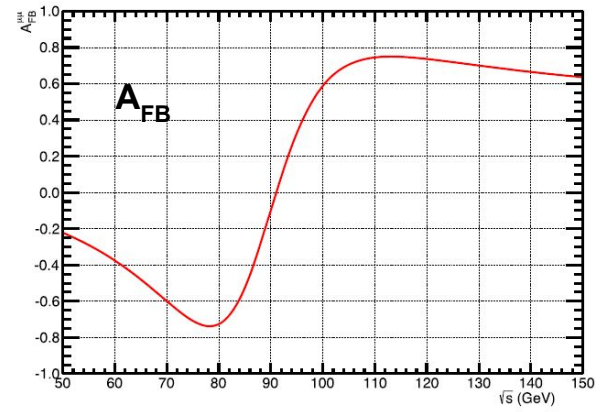
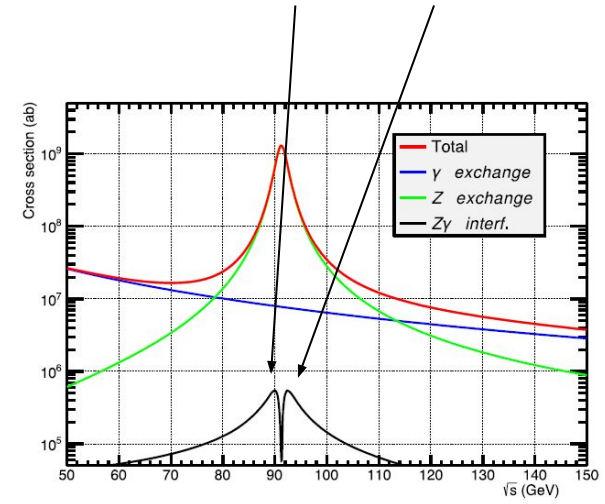
$$A_{\text{FB}}^{\mu\mu}(s) \simeq \frac{3}{4} \mathcal{A}_e \mathcal{A}_\mu \times \left[1 + \frac{8\pi \sqrt{2} \alpha_{\text{QED}}(s)}{m_Z^2 G_F (1 - 4 \sin^2 \theta_W^{\text{eff}})^2} \frac{s - m_Z^2}{2s} \right]$$

\rightarrow strongly depends on \sqrt{s}
 \rightarrow **direct** measurement of $\alpha_{\text{QED}}(s)$ at $\sqrt{s} \neq m_Z$
 \rightarrow measure $\sin^2 \theta_W$ to high precision (later)

Perform line-scan around Z-pole to maximise Z- γ interference and measure $A_{\text{FB}}^{\mu\mu}$:

- Nominal 91.2 GeV, 80 /ab
- Off-peak: 87.7 and 93.9 GeV, each 40 /ab

\rightarrow Measure $\alpha_{\text{QED}}(m_Z^2)$ to 3×10^{-5} rel. precision (currently 1.1×10^{-4})
 \rightarrow Stat. dominated; syst. uncertainties $< 10^{-5}$ (dominated by \sqrt{s} calib)
 \rightarrow Theoretical uncertainties $\sim 10^{-4}$, higher order calcs needed



Z peak – $\sin^2\theta_W$

Z → $\mu\mu$ forward/backward asymmetry also used to measure ewk mixing angle $\sin^2\theta_W$ at Z-pole = 91.2 GeV:

$$A_{FB}^{\mu\mu}(s) \simeq \frac{3}{4} \mathcal{A}_e \mathcal{A}_\mu \longrightarrow \mathcal{A}_e = \frac{g_{L,e}^2 - g_{R,e}^2}{g_{L,e}^2 + g_{R,e}^2} = \frac{2v_e/a_e}{1 + (v_e/a_e)^2}, \text{ with } v_e/a_e \equiv 1 - 4 \sin^2 \theta_W^{\text{eff}}$$

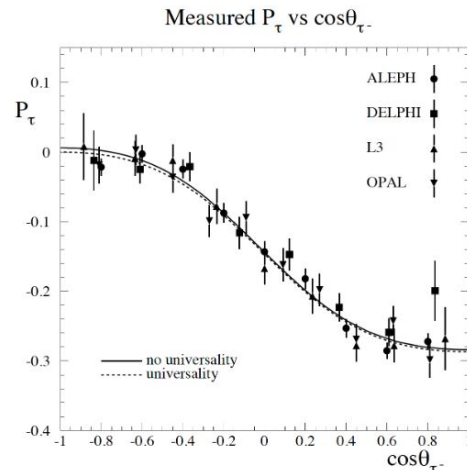
$$\Delta A_{FB}^{\mu\mu}(s) \sim 3 \times 10^{-6} \text{ (stat)} + 4 \times 10^{-6} \text{ (syst)}$$

- Measure $\sin^2\theta_W$ to 3×10^{-6} abs. precision (currently 1.6×10^{-4})
- Assumes lepton universality: $\mathcal{A}_e = \mathcal{A}_\mu$
- Mainly dominated by energy calibration (point-to-point)

Tau polarization used to constrain the mixing angle to a similar precision

- No assumption on lepton universality (direct separation \mathcal{A}_e and \mathcal{A}_τ)
- \mathcal{A}_τ from P_τ : benefit from high statistics and very robust measurement

$$P_\tau(\cos\theta) = \frac{A_{pol}(1 + \cos^2\theta) + \frac{8}{3} A_{pol}^{FB} \cos\theta}{(1 + \cos^2\theta) + \frac{8}{3} A_{FB} \cos\theta} \implies P_\tau \equiv \frac{\sigma(\tau_R) - \sigma(\tau_L)}{\sigma(\tau_R) + \sigma(\tau_L)} \simeq -2(1 - 4 \sin^2\theta_W)$$





Z lineshape – mass, width and σ_{had}^0

→ **Mass** ± 4 keV (stat) ± 100 keV (syst) [LEP 2.1 MeV]

- Systematics limited due to beam calibration uncertainties (RDP ~ 100 keV)

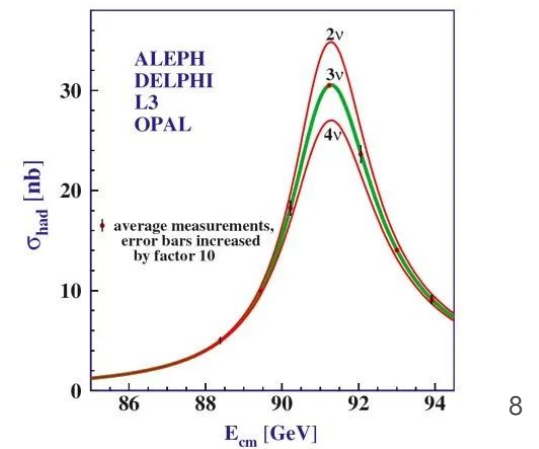
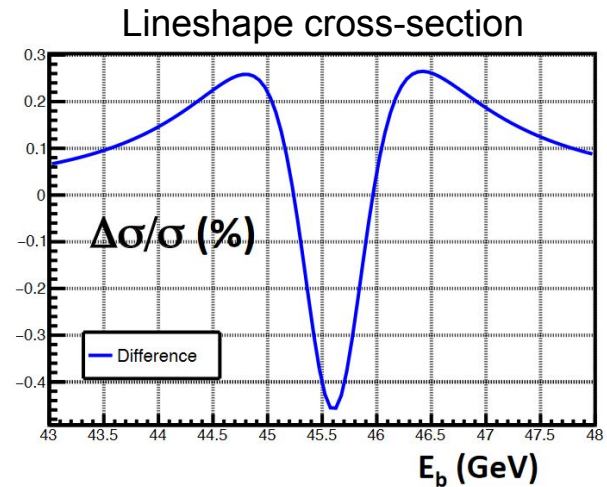
→ **Width** ± 4 keV (stat) ± 25 keV (syst) [LEP 2.3 MeV]

- Systematics dominated by:
 - Relative (point-to-point) uncertainty on the $\sqrt{s} \sim 22$ keV
 - Impact on beam-energy spread uncertainty ~ 10 keV
 - Absolute uncertainty on BES ~ 84 MeV
 - Constrained using $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ events:
 - Constrain BES uncertainty to per-mille level
 - Taking into account asymmetric beam optics (x-angle $\alpha 30$ mrad) and γ -ISR
 - Muon angular resolution ~ 0.1 mrad required

→ **Hadronic cross-section** $\sigma_{\text{had}}^0: \pm 4$ pb [LEP 37 pb]

→ **Number of neutrino families:** 1×10^{-3} (abs) [LEP 7×10^{-3}]

- Dominated by luminosity uncertainty





Z peak – couplings and $\alpha_s(m_Z^2)$

Couplings measured from ratio of hadronic and leptonic partial widths

→ need control on detector acceptances: detector precision $\sim 10 \mu\text{m}$

| | Statistical uncertainty | Systematic uncertainty |
|----------------------|-------------------------|------------------------|
| $R_{\mu} (R_{\ell})$ | 10^{-6} | 5×10^{-5} |
| R_{τ} | 1.5×10^{-6} | 10^{-4} |
| R_e | 1.5×10^{-6} | 3×10^{-4} |
| R_b | 5×10^{-5} | 3×10^{-4} |
| R_c | 1.5×10^{-4} | 15×10^{-4} |

Relative stat. and syst. unc. (similar)



| fermion type | g_a | g_v |
|--------------|----------------------|----------------------|
| e | 1.5×10^{-4} | 2.5×10^{-4} |
| μ | 2.5×10^{-5} | $2. \times 10^{-4}$ |
| τ | 0.5×10^{-4} | 3.5×10^{-4} |
| b | 1.5×10^{-3} | 1×10 |
| c | 2×10^{-3} | 1×10 |

Relative unc. on couplings

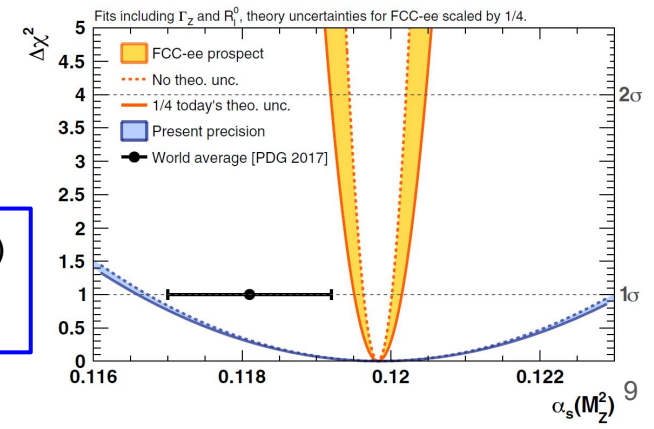
1-2 orders of magnitude Improvement w.r.t. LEP

Extract strong coupling constant $\alpha_s(m_Z^2)$ using leptonic/hadronic width ratio:

$$R_1 = \Gamma_{\text{had}} / \Gamma_{\text{lep}}$$

→ $\Delta\alpha_s(m_Z) \sim 1 \times 10^{-5}$ (stat) + 1.5×10^{-4} (syst) abs. (current value $\Delta\alpha_s$ 30×10^{-4})

→ Systematically dominated (acceptance)





WW threshold

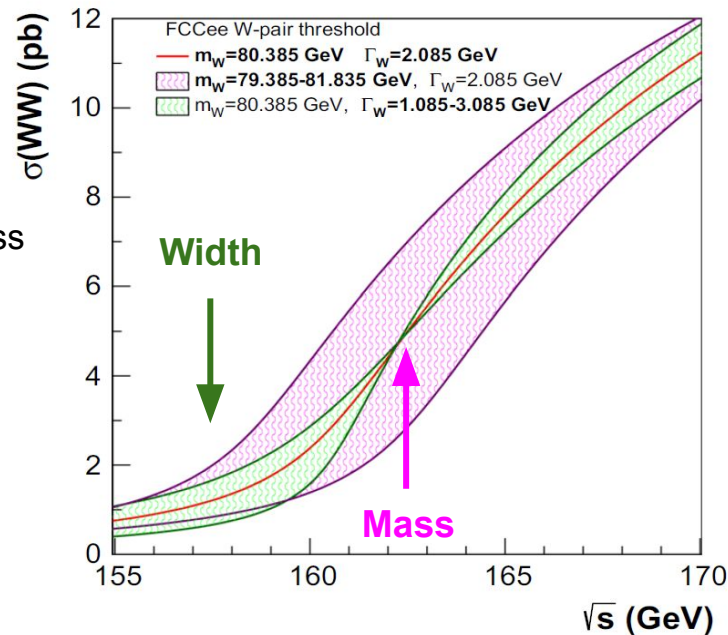
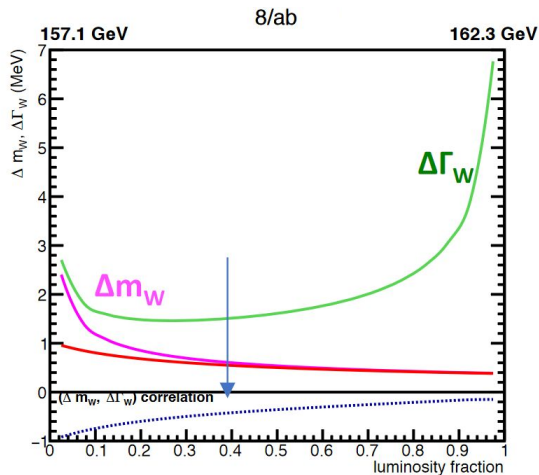
W mass and width extracted from line-scans using WW xsec

2 energy points determined from Δm_W and $\Delta \Gamma_W$ sensitivities on WW xsec:

→ **157.1 GeV width measurement:** maximum sensitivity on width

→ **162.5 GeV mass measurement:** minimal impact on width, max. on mass

Luminosity ($<10^{-4}$) and center-of-mass (< 0.5 MeV) uncertainties to be controlled, but weaker constraints than on Z pole



Combined fit with optimized lumi fraction ($f=0.4$: 5 /ab at 157.1, 7 /ab at 162.5)

→ precision m_W to 0.25 (stat) + 0.3 (syst) MeV (present 15 MeV)

→ precision Γ_W to 1.2 (stat) + 0.3 (syst) MeV (present 42 MeV)



W kinematic reconstruction

Independent analysis on W mass and width using kinematic reconstruction techniques in $WW \rightarrow qq\ell\nu$ events

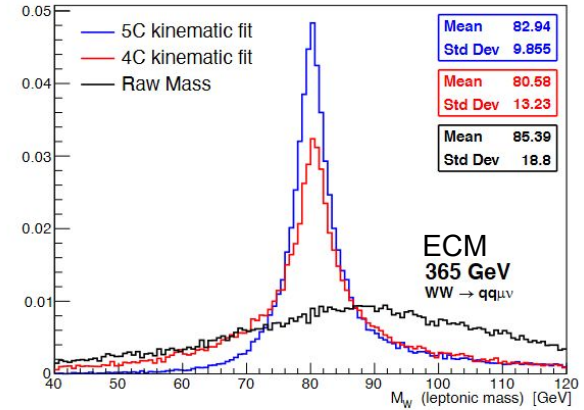
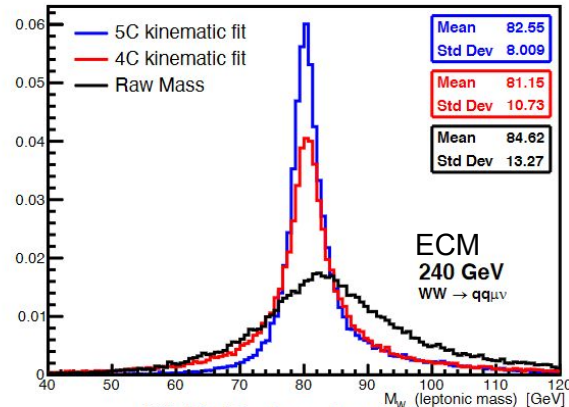
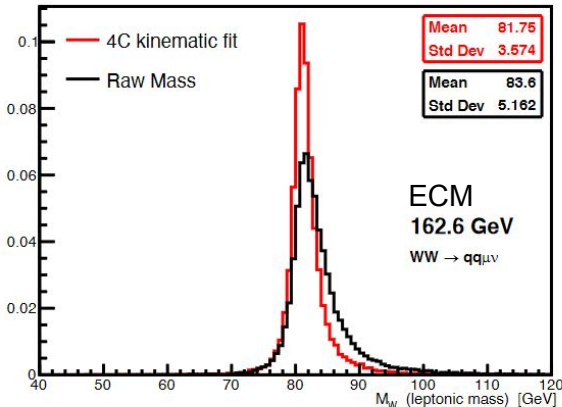
- Profit from precise angle and velocity (β) measurements
- Run at all kinematically accessible energy points (WW, ZH and tt)
- Put conditions on detector requirements

Δm_W (stat) ~ 250 keV \rightarrow similar as xsec measurement

$\Delta \Gamma_W$ (stat) ~ 350 keV \rightarrow reduction factor 2-3

| Source | Δm_W (MeV/ c^2) | | | | $\Delta \Gamma_W$ (MeV) | | | |
|-------------------------------------|----------------------------|-------------------|--------------------|--------------------|-------------------------|-------------------|--------------------|--------------------|
| | $e\nu q\bar{q}$ | $\mu\nu q\bar{q}$ | $\tau\nu q\bar{q}$ | $\ell\nu q\bar{q}$ | $e\nu q\bar{q}$ | $\mu\nu q\bar{q}$ | $\tau\nu q\bar{q}$ | $\ell\nu q\bar{q}$ |
| e+ μ momentum | 3 | 8 | - | 4 | 5 | 4 | - | 4 |
| e+ μ momentum resoln | 7 | 4 | - | 4 | 65 | 55 | - | 50 |
| Jet energy scale/linearity | 5 | 5 | 9 | 6 | 4 | 4 | 16 | 6 |
| Jet energy resoln | 4 | 2 | 8 | 4 | 20 | 18 | 36 | 22 |
| Jet angle | 5 | 5 | 4 | 5 | 2 | 2 | 3 | 2 |
| Jet angle resoln | 3 | 2 | 3 | 3 | 6 | 7 | 8 | 7 |
| Jet boost | 17 | 17 | 20 | 17 | 3 | 3 | 3 | 3 |
| Fragmentation | 10 | 10 | 15 | 11 | 22 | 23 | 37 | 25 |
| Radiative corrections | 3 | 2 | 3 | 3 | 3 | 2 | 2 | 2 |
| LEP energy | 9 | 9 | 10 | 9 | 7 | 7 | 10 | 8 |
| Calibration ($e\nu q\bar{q}$ only) | 10 | - | - | 4 | 20 | - | - | 9 |
| Ref MC Statistics | 3 | 3 | 5 | 2 | 7 | 7 | 10 | 5 |
| Bkgnd contamination | 3 | 1 | 6 | 2 | 5 | 4 | 19 | 7 |

Limited by systematics (beam energy, resolution, fragmentation) \rightarrow constrain



CLD Detector Concept



W decay branching ratios

Precise measurement of W decays

- Precise control of lepton ID to avoid cross contamination in signal channels (e.g. $\tau \rightarrow e, \mu$ vs. e, μ channels)
- Precision of 10^{-4} achievable (rel.)
- Simultaneously probe lepton and q/l universality to high precision ($\sim 10^{-4}$)

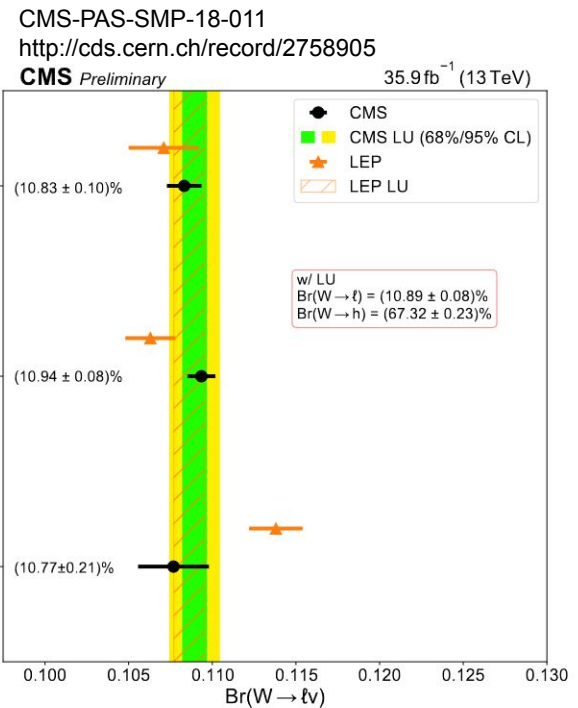
| Decay mode | relative precision | B(W \rightarrow ev) | B(W \rightarrow $\mu\nu$) | B(W \rightarrow $\tau\nu$) | B(W \rightarrow qq) |
|------------|--------------------|-----------------------|------------------------------|-------------------------------|-----------------------|
| LEP2 | | 1.5 % | 1.4 % | 1.8 % | 0.4 % |
| CMS | | 0.9 % | 0.7 % | 2 % | 0.4 % |
| FCCee | | 0.03 % | 0.03 % | 0.04 % | 0.01 % |

Flavor tagging

- Allows precise measurement CKM matrix elements V_{cs}, V_{ub}, V_{cb}
- Extract strong coupling constant at WW-threshold

$$R_W = \frac{B_q}{1 - B_q} = \left(1 + \frac{\alpha_S(m_W^2)}{\pi} \right) \sum_{i=u,c; j=d,s,b} |V_{ij}|^2$$

$\rightarrow \Delta\alpha_S(m_W) \sim 3 \times 10^{-4}$ (abs)
 \rightarrow Statistically dominated





Top mass and width measurement

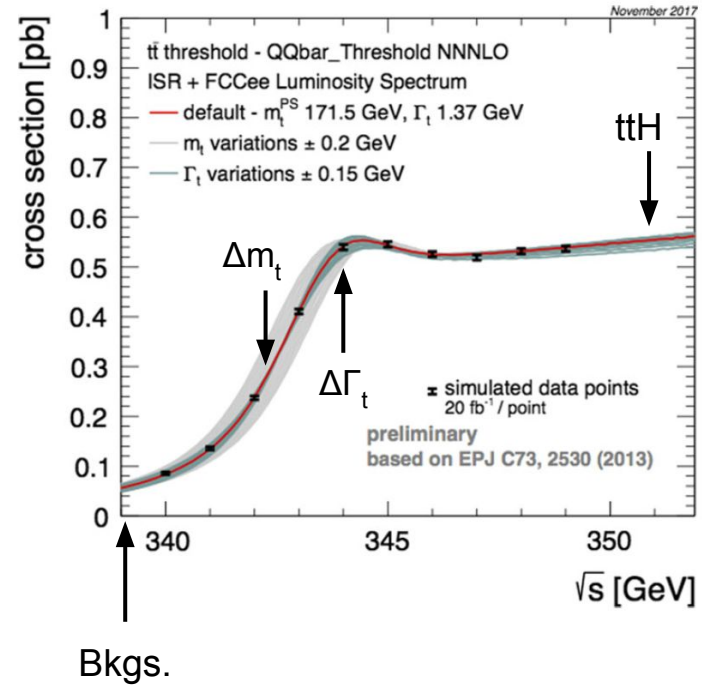
Top mass and width measurements similar as WW line-shape

Though more energy points needed:

- Relative large uncertainty on top mass (+/- 0.5 GeV)
- Need to constrain shape in optimal way
- Possible to constrain backgrounds (below) and ttH (above)

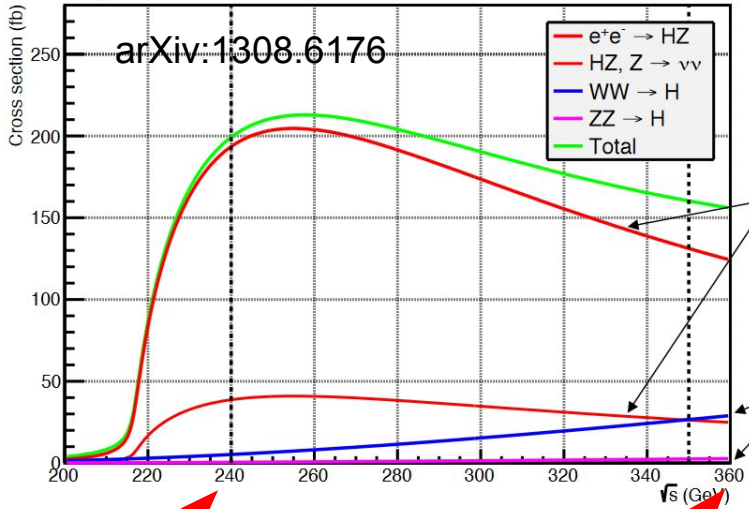
→ Multipoint scan in 5 GeV window [340, 345], each ~ 25 /fb

→ Δm_t (stat) ~ 17 MeV (syst negligible)
 → $\Delta \Gamma_t$ (stat) ~ 45 MeV (syst negligible)
 To date: theoretical QCD errors order of 40 MeV for mass and width





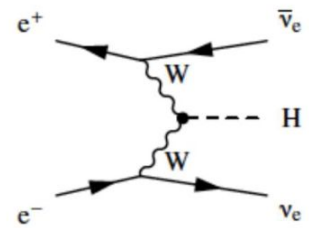
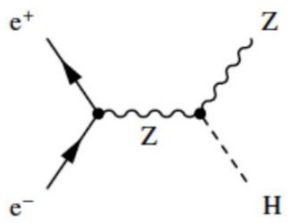
Higgs physics at FCCee



arXiv:1308.6176

240 GeV, 5 /ab
10⁶ ZH events
25k WWH events

365 GeV, 1.5 /ab
200k ZH events
50k WWH events



Higgs-pole at 240 GeV

- Higgs-strahlung dominant: $e^+e^- \rightarrow ZH$
- Precise Higgs **mass measurement** up to ~ 5 MeV
- Measurement of **decay-mode-independent xsec** to % level, sensitive to new physics $H \rightarrow$ invisible
- Higgs width extracted from $H \rightarrow ZZ$ at % level

Top threshold at 365 GeV

- Opens significance for WW fusion: $e^+e^- \rightarrow WW\nu\nu \rightarrow H\nu\nu$
- Significant reduction in couplings and width

Combined performance at both energy points

- Higgs coupling precision $<$ % level
- In particular, exotic Higgs decays constraint to < 1 %
- Probing CP violation using $H \rightarrow \pi\pi$ phase

→ [See dedicated talk Tuesday by S. Braibant](#)



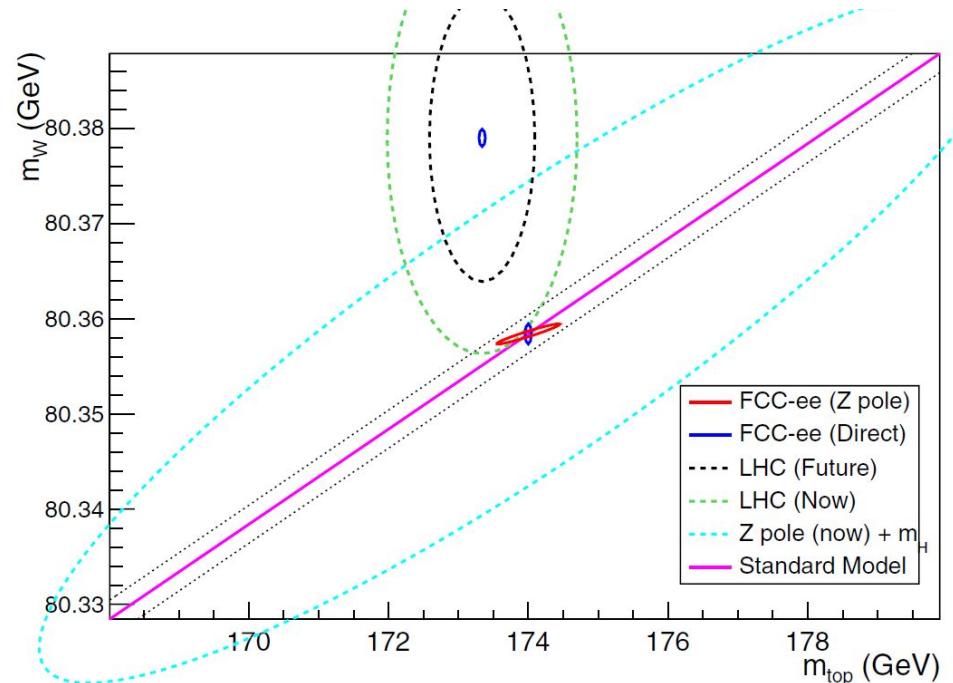
Rich physics programme at Z-threshold and higher energies

- FCC delivers excellent precision on various EWK parameters with improvements of 1-2 orders of magnitude
- Combined results at all energy thresholds provides unique closure tests for SM

→ Ongoing efforts with several analyses to explore and evaluate physics potential

→ Feedback towards detector and machine R&D for systematic uncertainty reduction on key measurements

→ Work on theoretical side needed to cope with experimental level of accuracy



Backup



FCCee Physics Performance overview

[ArXiv 2106.13885](https://arxiv.org/abs/2106.13885)

| Observable | present value \pm error | FCC-ee Stat. | FCC-ee Syst. | Comment and leading exp. error |
|---|---------------------------|--------------|--------------|--|
| m_Z (keV) | 91186700 \pm 2200 | 4 | 100 | From Z line shape scan Beam energy calibration |
| Γ_Z (keV) | 2495200 \pm 2300 | 4 | 25 | From Z line shape scan Beam energy calibration |
| $\sin^2 \theta_W^{\text{eff}} (\times 10^6)$ | 231480 \pm 160 | 2 | 2.4 | from $A_{\text{FB}}^{\mu\mu}$ at Z peak Beam energy calibration |
| $1/\alpha_{\text{QED}}(m_Z^2) (\times 10^3)$ | 128952 \pm 14 | 3 | small | from $A_{\text{FB}}^{\mu\mu}$ off peak QED&EW errors dominate |
| $R_\ell^Z (\times 10^3)$ | 20767 \pm 25 | 0.06 | 0.2-1 | ratio of hadrons to leptons acceptance for leptons |
| $\alpha_s(m_Z^2) (\times 10^4)$ | 1196 \pm 30 | 0.1 | 0.4-1.6 | from R_ℓ^Z above |
| $\sigma_{\text{had}} (\times 10^3)$ (nb) | 41541 \pm 37 | 0.1 | 4 | peak hadronic cross section luminosity measurement |
| $N_\nu (\times 10^3)$ | 2996 \pm 7 | 0.005 | 1 | Z peak cross sections Luminosity measurement |
| $R_b (\times 10^6)$ | 216290 \pm 660 | 0.3 | < 60 | ratio of bb to hadrons stat. extrapol. from SLD |
| $A_{\text{FB},0}^b (\times 10^4)$ | 992 \pm 16 | 0.02 | 1-3 | b-quark asymmetry at Z pole from jet charge |
| $A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$ | 1498 \pm 49 | 0.15 | <2 | τ polarization asymmetry τ decay physics |
| τ lifetime (fs) | 290.3 \pm 0.5 | 0.001 | 0.04 | radial alignment |
| τ mass (MeV) | 1776.86 \pm 0.12 | 0.004 | 0.04 | momentum scale |
| τ leptonic ($\mu\nu_\mu\nu_\tau$) B.R. (%) | 17.38 \pm 0.04 | 0.0001 | 0.003 | c/μ /hadron separation |
| m_W (MeV) | 80350 \pm 15 | 0.25 | 0.3 | From WW threshold scan Beam energy calibration |
| Γ_W (MeV) | 2085 \pm 42 | 1.2 | 0.3 | From WW threshold scan Beam energy calibration |
| $\alpha_s(m_W^2) (\times 10^4)$ | 1170 \pm 420 | 3 | small | from R_ℓ^W |
| $N_\nu (\times 10^3)$ | 2920 \pm 50 | 0.8 | small | ratio of invis. to leptonic in radiative Z returns |
| m_{top} (MeV/c ²) | 172740 \pm 500 | 17 | small | From $t\bar{t}$ threshold scan QCD errors dominate |
| Γ_{top} (MeV/c ²) | 1410 \pm 190 | 45 | small | From $t\bar{t}$ threshold scan QCD errors dominate |
| $\lambda_{\text{top}}/\lambda_{\text{top}}^{\text{SM}}$ | 1.2 \pm 0.3 | 0.10 | small | From $t\bar{t}$ threshold scan QCD errors dominate |
| tZ couplings | \pm 30% | 0.5 - 1.5% | small | From $\sqrt{s} = 365$ GeV run |