### Impact of quark flavor violating SUSY on h(125) decays

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References:

Phys. Rev. D 91 (2015) 015007 [arXiv:1411.2840 [hep-ph] ] JHEP 1606 (2016) 143 [arXiv:1604.02366 [hep-ph]] IJMP A34 (2019) 1950120 [arXiv:1812.08010 [hep-ph]]

SUSY2021, 26 Aug. 2021, 'Beijing'

# 1. Introduction

- What is the SM-like Higgs boson discovered at LHC?
- It can be the SM Higgs boson.
- It can be a Higgs boson of New Physics.
- This is one of the most important issues in the present particle physics field!
- Here we study a possibility that it is the lightest Higgs boson  $h^{\circ}$  of the Minimal Supersymmetric Standard Model (MSSM), focusing on the decays  $h^{\circ}(125) \rightarrow c \overline{c}$ ,  $b \overline{b}$ ,  $b \overline{s}$ ,  $\gamma \gamma$ , g.

## 2. MSSM with QFV

Key parameters in this study are: \* QFV parameters:  $\tilde{c}_{L/R} - \tilde{t}_{L/R} \& \tilde{s}_{L/R} - \tilde{b}_{L/R}$  mixing parameters \* QFC parameter:  $\tilde{t}_L - \tilde{t}_R \& \tilde{b}_L - \tilde{b}_R$  mixing parameters  $M_{023}^2 = (\tilde{c}_L - \tilde{t}_L \text{ mixing parameter})$  $M_{I/23}^2 = (\tilde{c}_R - \tilde{t}_R \text{ mixing parameter})$  $M_{D23}^2 = (\tilde{s}_R - \tilde{b}_R \text{ mixing parameter})$  $T_{II23} = (\tilde{c}_R - \tilde{t}_L mixing parameter)$  $T_{U32} = (\tilde{c}_L - \tilde{t}_R \text{ mixing parameter})$  $T_{U33} = (\tilde{t}_L - \tilde{t}_R \text{ mixing parameter})$  $T_{D23} = (\tilde{s}_R - \tilde{b}_L \text{ mixing parameter})$  $T_{D32} = (\tilde{s}_L - \tilde{b}_R \text{ mixing parameter})$  $T_{D33} = (\tilde{b}_L - \tilde{b}_R \text{ mixing parameter})$ 

# 3. Constraints on the MSSM

We respect the following experimental and theoretical constraints:

- (1) The recent LHC limits on the masses of squarks, sleptons, gluino, charginos and neutralinos.
- (2) The constraint on  $(m_{A/H^+}, \tan\beta)$  from recent MSSM Higgs boson search at LHC.
- (3) The constraints on the QFV parameters from the B & K meson data.

$$B(b \to s \gamma) \quad \Delta M_{Bs} \quad B(B_s \to \mu^+ \mu^-) \quad B(B_u^+ \to \tau^+ \nu) \text{ etc.}$$

- (4) The constraints from the observed Higgs boson mass and couplings at LHC; e.g.  $121.6 \text{ GeV} < m_h^0 < 128.6 \text{ GeV}$  (allowing for theoretical uncertainty),  $0.71 < \kappa_b < 1.43$  (ATLAS),  $0.56 < \kappa_b < 1.70$  (CMS)
- (5) The experimental limit on SUSY contributions to the electroweak  $\rho$  parameter  $\Delta \rho$  (SUSY) < 0.0012.
- (6) Theoretical constraints from the vacuum stability conditions for the trilinear couplings  $T_{U\alpha\beta}$  and  $T_{D\alpha\beta}$ .

### 4. Parameter scan for $h^0 \rightarrow c \overline{c}, b \overline{b}, b \overline{s}$

- We compute the decay widths  $\Gamma(h^0 \to c \ \overline{c})$ ,  $\Gamma(h^0 \to b \ \overline{b})$ , and  $\Gamma(h^0 \to b \ \overline{s})$  at full 1-loop level in the MSSM with QFV.

- We take parameter scan ranges as follows:

 $1 TeV < M_{SUSY} < 5 TeV$ 

 $\begin{array}{l} 10 < \tan \beta < 80 \\ 2500 < M_3 < 5000 \ GeV \\ 100 < M_2 < 2500 \ GeV \\ 100 < M_1 < 2500 \ GeV \\ 100 < \mu < 2500 \ GeV \\ 1350 < m_A(pole) < 6000 \ GeV \\ etc. \ etc. \end{array}$ 

- In the parameter scan, all of the relevant experimental and theoretical constraints are imposed.

- 377180 parameter points are generated and 3208 points survive the constraints.

### 5. $\underline{h^0} \rightarrow c \overline{c}, b \overline{b}, b \overline{s} \text{ in the MSSM}$

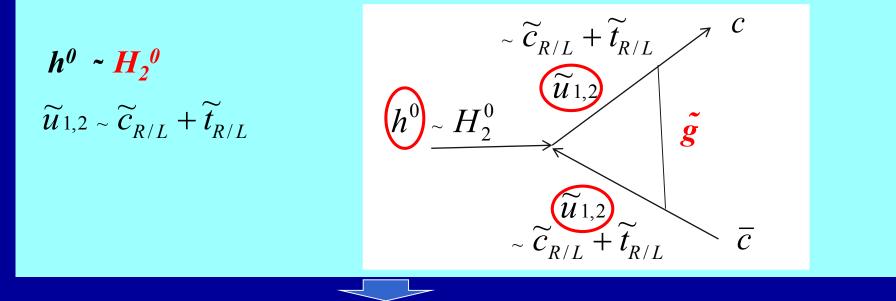
- We compute the decay widths  $\Gamma(h^0 \to c \ \overline{c})$ ,  $\Gamma(h^0 \to b \ \overline{b})$ , and  $\Gamma(h^0 \to b \ \overline{s})$  at full 1-loop level in the DRbar renormalization scheme in the MSSM with QFV.
- Main 1-loop correction to  $h^0 \rightarrow c \ \overline{c}$ :

gluino - su loops [ su =  $(\tilde{t} - \tilde{c} mixture)$ ] can be enhanced by large trilinear couplings  $T_{U23}$ ,  $T_{U32}$ ,  $T_{U33}$ 

- Main 1-loop corrections to  $h^0 \rightarrow b \ \overline{b} \& b \ \overline{s}$ :

gluino – sd loops [ sd = ( $\tilde{b}$  -  $\tilde{s}$  mixture)] can be enhanced by large trilinear couplings  $T_{D23}$ ,  $T_{D32}$ ,  $T_{D33}$ chargino - su loops [ su = ( $\tilde{t}$  -  $\tilde{c}$  mixture)] can be enhanced by large trilinear couplings  $T_{U23}$ ,  $T_{U32}$ ,  $T_{U33}$ 

### In large $\widetilde{c}_{R/L} - \widetilde{t}_{R/L} \& \widetilde{t}_{L} - \widetilde{t}_{R}$ mixing scenario;

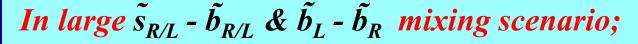


In our scenario, "trilinear couplings" ( $\widetilde{c}_R - \widetilde{t}_L - H_2^0$ ,  $\widetilde{c}_L - \widetilde{t}_R - H_2^0$ ,  $\widetilde{t}_L - \widetilde{t}_R - H_2^0$ couplings) = ( $T_{U23} T_{U32}$ ,  $T_{U33}$ ) are large!



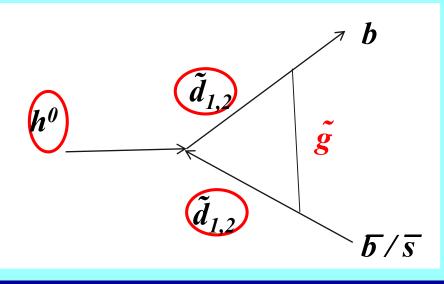
Gluino loop contributions can be large!

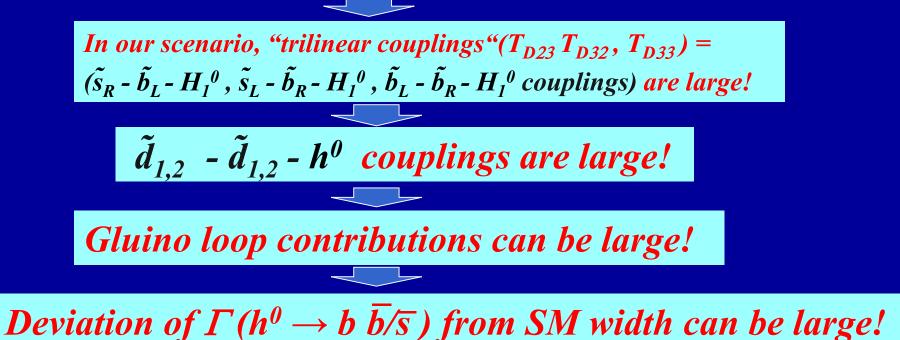
Deviation of  $\Gamma(h^0 \rightarrow c \ \overline{c})$  from SM width can be large!



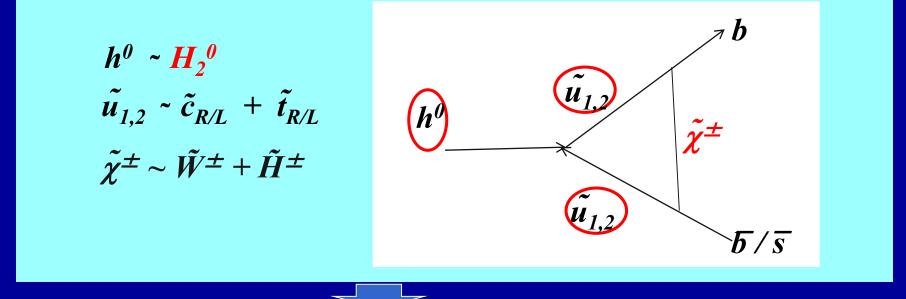








In large  $\tilde{c}_{R/L}$  -  $\tilde{t}_{R/L}$  &  $\tilde{t}_L$  -  $\tilde{t}_R$  mixing scenario;



In our scenario, "trilinear couplings" ( $\widetilde{c}_R - \widetilde{t}_L - H_2^0$ ,  $\widetilde{c}_L - \widetilde{t}_R - H_2^0$ ,  $\widetilde{t}_L - \widetilde{t}_R - H_2^0$ couplings) = ( $T_{U23} T_{U32}$ ,  $T_{U33}$ ) are large!

 $\widetilde{u}_{1,2} - \widetilde{u}_{1,2} - h^0$  couplings are large!

Chargino loop contributions can be large!

Deviation of  $\Gamma(h^0 \rightarrow b \ \overline{b}/\overline{s})$  from SM width can be large!

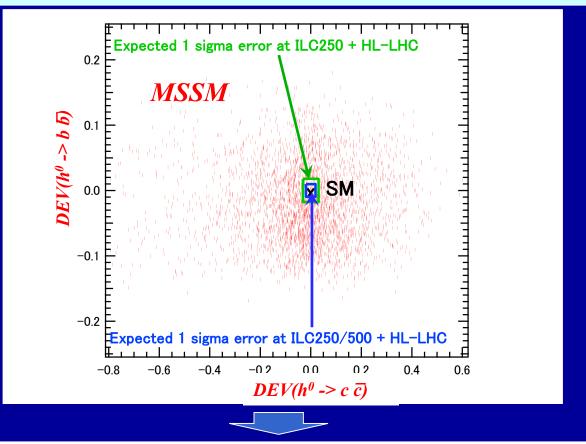
5.1 Deviation of the width from the SM prediction

- The deviation of the width from the SM prediction:

 $\overline{DEV(h^{\theta} \rightarrow X\overline{X})} = \Gamma(h^{\theta} \rightarrow X\overline{X})_{MSSM} / \Gamma(h^{\theta} \rightarrow X\overline{X})_{SM} - 1$ 

X = c, b

#### Scatter plot in $DEV(h^{\theta} \rightarrow c \ \overline{c}) - DEV(h^{\theta} \rightarrow b \ \overline{b})$ plane



DEV(h<sup>0</sup> -> c c̄) and DEV(h<sup>0</sup> -> b b̄) can be very large simultaneously!: DEV(h<sup>0</sup> -> c c̄) can be as large as ~ ±60%. DEV(h<sup>0</sup> -> b b̄) can be as large as ~ ±20%.

- ILC can observe such large deviations from SM at high significance (arXiv:1908.11299)!:
 △ DEV(h<sup>0</sup> -> c c̄) = (3.60%, 2.40%, 1.58%) at (ILC250, ILC500, ILC1000)
 △ DEV(h<sup>0</sup> -> b b̄) = (1.98%, 1.16%, 0.94%) at (ILC250, ILC500, ILC1000)

### 5.2 <u>BR( $h^0 \rightarrow b \ \overline{s} / s \ \overline{b}$ )</u>

 $BR(h^{\theta} \rightarrow b \ \overline{s} / s \ \overline{b}) \cong \theta \ (SM)$ 

### $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b})$ can be as large as ~ 0.17% (MSSM with QFV)! (See also Gomez-Heinemeyer-Rehman, PR D93 (2016) 095021 [arXiv:1511.04342].)

ILC(250+500+1000) sensitivity could be ~ 0.1% (at 4  $\sigma$  significance)!

Private communication with Junping Tian; See also Barducci et al., JHEP 12 (2017) 105 [arXiv:1710.06657].

# 6. $h^0 \rightarrow \gamma \gamma, g g$ in the MSSM

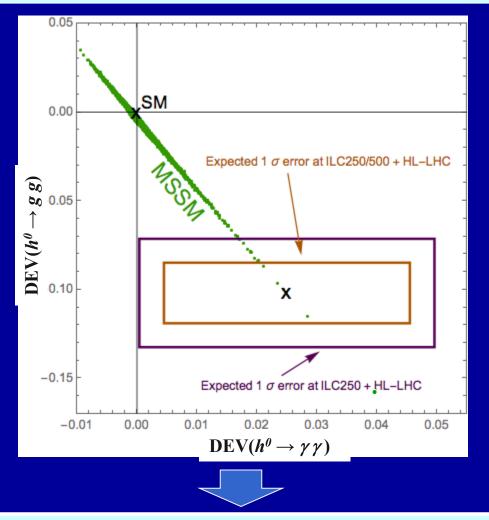
- For the h decays to photon photon and gluon gluon we compute the widths at NLO QCD level. We perform a MSSM parameter scan respecting all the relevant theoretical and experimental constraints.
- From the parameter scan, we find the followings:

(1)  $DEV(h^{\theta} \rightarrow \gamma \gamma)$  and  $DEV(h^{\theta} \rightarrow g g)$  can be sizable simultaneously:  $DEV(h^{\theta} \rightarrow \gamma \gamma)$  can be as large as ~ + 4%,  $DEV(h^{\theta} \rightarrow g g)$  can be as large as ~ -15%.

(2) There is a very strong correlation between  $DEV(h^0 \rightarrow \gamma \gamma)$ and  $DEV(h^0 \rightarrow g g)$ . This correlation is due to the fact that the stop-loop (stop-scharm mixture loop) contributions dominate the two DEVs.

(3) The deviation of the width ratio  $\Gamma(h^0 \to \gamma \gamma) / \Gamma(h^0 \to g g)$  in the MSSM from the SM value can be as large as ~ +20%.

### Scatter plot in DEV( $h^{\theta} \rightarrow \gamma \gamma$ ) - DEV( $h^{\theta} \rightarrow g g$ ) plane



- DEV( $h^0 \rightarrow \gamma \gamma$ ) and DEV( $h^0 \rightarrow g g$ ) can be sizable simultaneously! -There is a strong correlation between DEV( $h^0 \rightarrow \gamma \gamma$ ) and DEV( $h^0 \rightarrow g g$ )!

- ILC can observe such large deviations from SM at high significance (arXiv:1908.11299)!

# 7. Conclusion

- We have studied the decays

 $h^{\theta}$  (125GeV)  $\rightarrow c \overline{c}, b \overline{b}, b \overline{s}, \gamma \gamma, g g in the MSSM with QFV.$ 

- Performing a systematic MSSM parameter scan respecting all of the relevant theoretical and experimental constraints, we have found the followings:
  - \*  $DEV(h^{0} \rightarrow c \ c)$  and  $DEV(h^{0} \rightarrow b \ b)$  can be very large simultaneously! :  $DEV(h^{0} \rightarrow c \ c)$  can be as large as  $\sim \pm 60\%$ ,  $DEV(h^{0} \rightarrow b \ b)$  can be as large as  $\sim \pm 20\%$ .
  - \* The deviation of the width ratio  $\Gamma(h^0 \rightarrow b \overline{b}) / \Gamma(h^0 \rightarrow c \overline{c})$ from the SM value can be as large as ~ +200%.
  - \* BR(h<sup>0</sup> -> b s̄ / s b̄) can be as large as ~ 0.17%!
    <u>ILC(250 + 500 + 1000)</u> sensitivity could be ~ 0.1% at 4 sigma signal significance!

\*  $DEV(h^0 \rightarrow \gamma \gamma)$  and  $DEV(h^0 \rightarrow g g)$  can be sizable simultaneously! :  $DEV(h^0 \rightarrow \gamma \gamma)$  can be as large as ~ +4%,  $DEV(h^0 \rightarrow g g)$  can be as large as ~ -15%.

\* The deviation of the width ratio  $\Gamma(h^0 \rightarrow \gamma \gamma)/\Gamma(h^0 \rightarrow g g)$  from the SM value can be as large as ~ +20%.

\* There is a very strong correlation between  $DEV(h^0 \rightarrow \gamma \gamma)$ and  $DEV(h^0 \rightarrow g g)$ . This correlation is due to the fact that the stop-loop (stop-scharm mixture loop) contributions dominate the two DEVs.

 All of these large deviations in the h<sup>0</sup> (125GeV) decays are due to large c̃ - t̃ mixing & large c̃ / t̃ involved trilinear couplings T<sub>U23</sub>, T<sub>U32</sub>, T<sub>U33</sub> and large s̃ - b̃ mixing & large s̃ / b̃ involved trilinear couplings T<sub>D23</sub>, T<sub>D32</sub>, T<sub>D33</sub>.

- ILC can observe such large deviations from SM at high significance!

- In case the deviation pattern shown here is really observed at ILC, then it would strongly suggest the discovery of QFV SUSY (MSSM with QFV)!

- See next slide also.

- Our analysis suggests the following:

PETRA/TRISTAN e- e+ collider discovered virtual Z<sup>0</sup> effect for the first time. Later, CERN p p collider discovered the Z<sup>0</sup> boson.

Similarly, ILC could discover virtual Sparticle effects for the first time in h<sup>0</sup>(125) decays! Later, FCC-hh p p collider could discover the Sparticles!



# Thank you!



# 2. MSSM with QFV

The basic parameters of the MSSM with **QFV**:

 $\{ \tan\beta, m_A, M_1, M_2, M_3, \mu, M_{Q,\alpha\beta}^2, M_{U,\alpha\beta}^2, M_{D,\alpha\beta}^2, T_{U\alpha\beta}, T_{D\alpha\beta} \}$ (at Q = 1 TeV scale) ( $\alpha, \beta = 1, 2, 3 = u, c, t \text{ or } d, s, b$ )

tan $\beta$ : ratio of VEV of the two Higgs doublets  $\langle H^{\theta}_{2} \rangle / \langle H^{\theta}_{1} \rangle$ 

*m<sub>A</sub>*: *CP* odd Higgs boson mass (pole mass)

 $M_{1,} M_{2}, M_{3}$ : U(1), SU(2), SU(3) gaugino masses  $\mu$ : higgsino mass parameter

 $M^2_{Q,\alpha\beta}$ : left squark soft mass matrix

 $M^2_{U\alpha\beta}$ : right up-type squark soft mass matrix

 $M^2_{D\alpha\beta}$ : right down-type squark soft mass matrix

 $T_{U\alpha\beta}$ : trilinear coupling matrix of up-type squark and Higgs boson

 $T_{D\alpha\beta}$ : trilinear coupling matrix of down-type squark and Higgs boson

# 2. <u>Key parameters of MSSM</u>

Key parameters in this study are:

\* QFV parameters:  $M^2_{023}$ ,  $M^2_{U23}$ ,  $M^2_{D23}$ ,  $T_{U23}$ ,  $T_{U32}$ ,  $T_{D23}$ ,  $T_{D23}$ ,  $T_{D32}$ \* QFC parameter:  $T_{U33}$ ,  $T_{D33}$  $M_{023}^2 = (\tilde{c}_L - \tilde{t}_L \text{ mixing parameter})$  $M^{2}_{II23} = (\tilde{c}_{R} - \tilde{t}_{R} \text{ mixing parameter})$  $M^2_{D23} = (\tilde{s}_R - \tilde{b}_R mixing parameter)$  $T_{U23} = (\tilde{c}_R - \tilde{t}_L \text{ mixing parameter})$  $T_{U32} = (\tilde{c}_L - \tilde{t}_R \text{ mixing parameter})$  $T_{II33} = (\tilde{t}_L - \tilde{t}_R mixing parameter)$  $T_{D23} = (\tilde{s}_R - \tilde{b}_L \text{ mixing parameter})$  $T_{D32} = (\tilde{s}_L - \tilde{b}_R \text{ mixing parameter})$  $T_{D33} = (\tilde{b}_L - \tilde{b}_R \text{ mixing parameter})$ 

## 4. <u>Parameter scan for $h^0 \rightarrow c \overline{c}, b \overline{b}, b \overline{s}$ </u> in the MSSM

- We compute the decay widths  $\Gamma(h^0 \to c \ \overline{c})$ ,  $\Gamma(h^0 \to b \ \overline{b})$ , and  $\Gamma(h^0 \to b \ \overline{s})$  at full 1-loop level in the MSSM with QFV.

- Parameter points are generated by using random numbers in the following ranges (in units of GeV or GeV^2):

 $1 \text{ TeV} < M_{SUSY} < 5 \text{ TeV}$ 

 $10 < tan \beta < 80$   $2500 < M_3 < 5000$   $100 < M_2 < 2500$   $100 < M_1 < 2500$ (without assuming the GUT relation for M\_1, M\_2, M\_3)  $100 < \mu < 2500$  $1350 < m_A(pole) < 6000;$ 

 $MQ2 \ 11 = 4500^{2}$  (fixed)  $2500^2 < MQ2$   $22 < 4000^2$  $2500^2 < MQ2$  33 < 4000<sup>2</sup>  $|MQ2 23| < 1000.^2$ <=== **QFV** param. <u> $MU2 \ 11 = 4500^{2}$  (fixed)</u> *1000.*<sup>2</sup> < *MU2 22* < *4000.*<sup>2</sup> 600.<sup>^</sup>2 < MU2 33 < 3000.<sup>^</sup>2  $|MU2 23| < 2000.^2$ <=== **QFV** para<u>m</u>. <u>MD2</u>  $11 = 4500^{2}$  (fixed)  $2500.^{2} < MD2 \ 22 < 4000.^{2}$ 1000.<sup>^</sup>2 < MD2 33 < 3000.<sup>^</sup>2  $|MD2 \ 23| < 2000.^2$ <u>ML2</u>  $11 = 1500^{2}$  (fixed)  $ML2 \ 22 = 1500^{2} (fixed)$  $ML2 \ 33 = 1500^{2}$  (fixed)  $ML2 \ 23 = 0.$  (fixed)

ME2  $11 = 1500^{2}$  (fixed) ME2  $22 = 1500^{2}$  (fixed) ME2  $33 = 1500^{2}$  (fixed)  $ME2 \ 23 = 0.$  (fixed) |TU 23| < 4000<=== *QFV* param |TU||32| < 4000<=== *QFV* param |TU||33| < 5000<=== QFC param |TD | 23| < 3000<=== *QFV* param |TD||32| < 3000<=== *QFV* param **TD** 33 < 4000 <=== *QFC* param TE 23 = 0. (fixed)  $\overline{TE} \ 32 = 0.$  (fixed) |TE | 33| < 500

- In the parameter scan, all of the relevant experimental and theoretical constraints are imposed.

- 377180 parameter points are generated and 3208 points survive the constraints.

Table 1: Scanned ranges and fixed values of the MSSM parameters (in units of GeV or GeV<sup>2</sup>, except for tan  $\beta$ ). The parameters that are not shown explicitly are taken to be zero.  $M_{1,2,3}$  are the U(1), SU(2), SU(3) gaugino mass parameters.

$\tan\beta$	$M_1$	$M_2$	$M_3$	μ	$m_A(pole)$
10 ÷ 80	$100 \div 2500$	$100 \div 2500$	$2500 \div 5000$	$100 \div 2500$	$1350 \div 6000$
$M_{Q22}^{2}$	$M_{Q33}^{2}$	$ M_{Q23}^2 $	$M_{U22}^{2}$	$M_{U33}^{2}$	$ M_{U23}^2 $
$2500^2 \div 4000^2$	$2500^2 \div 4000^2$	$< 1000^{2}$	$1000^2\div 4000^2$	$600^2 \div 3000^2$	$< 2000^{2}$
$M_{D22}^2$	$M_{D33}^{2}$	$ M_{D23}^2 $	$ T_{U23} $	$ T_{U32} $	$ T_{U33} $
$2500^2 \div 4000^2$	$1000^2 \div 3000^2$	$< 2000^{2}$	< 4000	< 4000	< 5000
$ T_{D23} $	$ T_{D32} $	$ T_{D33} $	$ T_{E33} $		
< 3000	< 3000	< 4000	< 500		

$M_{Q11}^{2}$	$M_{U11}^{2}$	$M_{D11}^2$	$M_{L11}^2$	$M^2_{L22}$	$M^2_{L33}$	$M_{E11}^2$	$M_{E22}^2$	$M_{E33}^2$
4500 <sup>2</sup>	$4500^{2}$	$4500^{2}$	$1500^{2}$	$1500^{2}$	$1500^{2}$	$1500^{2}$	$1500^{2}$	$1500^{2}$

### **Constraints on the MSSM parameters from** <u>K & B meson and h<sup>0</sup> data:</u>

Table 5: Constraints on the MSSM parameters from the K- and B-meson data relevant mainly for the mixing between the second and the third generations of squarks and from the data on the  $h^0$  mass and couplings  $\kappa_b$ ,  $\kappa_g$ ,  $\kappa_\gamma$ . The fourth column shows constraints at 95% CL obtained by combining the experimental error quadratically with the theoretical uncertainty, except for  $B(K_L^0 \to \pi^0 \nu \bar{\nu})$ ,  $m_{h^0}$  and  $\kappa_{b,g,\gamma}$ .

Observable	Exp. data	Theor. uncertainty	Constr. (95%CL)
$ \begin{array}{c} 10^{3} \times  \epsilon_{K}  \\ 10^{15} \times \Delta M_{K} [\text{GeV}] \\ 10^{9} \times \mathcal{B}(K_{L}^{0} \rightarrow \pi^{0} \nu \bar{\nu}) \\ 10^{10} \times \mathcal{B}(K^{+} \rightarrow \pi^{+} \nu \bar{\nu}) \\ \Delta M_{B_{s}} [\text{ps}^{-1}] \\ 10^{4} \times \mathcal{B}(b \rightarrow s \gamma) \\ 10^{6} \times \mathcal{B}(b \rightarrow s \ l^{+} l^{-}) \\ (l = e \text{ or } \mu) \\ 10^{9} \times \mathcal{B}(B_{s} \rightarrow \mu^{+} \mu^{-}) \\ 10^{4} \times \mathcal{B}(B^{+} \rightarrow \tau^{+} \nu) \\ m_{h^{0}} [\text{GeV}] \\ \kappa_{b} \\ \kappa_{g} \\ \kappa_{\gamma} \end{array} $	$\begin{array}{c} \text{Exp. data} \\ \hline 2.228 \pm 0.011 \ (68\% \ \text{CL}) \ [21] \\ 3.484 \pm 0.006 \ (68\% \ \text{CL}) \ [21] \\ < 3.0 \ (90\% \ \text{CL}) \ [21] \\ 1.7 \pm 1.1 \ (68\% \ \text{CL}) \ [21] \\ 17.757 \pm 0.021 \ (68\% \ \text{CL}) \ [21, 41] \\ 3.32 \pm 0.15 \ (68\% \ \text{CL}) \ [21, 41] \\ 1.60 \ ^{+0.48} \ (68\% \ \text{CL}) \ [21, 41] \\ 1.60 \ ^{+0.48} \ (68\% \ \text{CL}) \ [43] \\ \hline 2.69 \ ^{+0.37} \ (68\% \ \text{CL}) \ [43] \\ \hline 2.69 \ ^{+0.37} \ (68\% \ \text{CL}) \ [45] \\ 1.06 \ ^{\pm 0.19} \ (68\% \ \text{CL}) \ [41] \\ 125.09 \ ^{\pm } 0.24 \ (68\% \ \text{CL}) \ [48] \\ 1.06 \ ^{+0.37} \ (95\% \ \text{CL}) \ [50] \\ 1.17 \ ^{+0.53} \ (95\% \ \text{CL}) \ [50] \\ 1.03 \ ^{+0.12} \ (95\% \ \text{CL}) \ [51] \\ 1.00 \ ^{\pm 0.12} \ (95\% \ \text{CL}) \ [50] \\ 1.18 \ ^{+0.27} \ (95\% \ \text{CL}) \ [50] \\ 1.07 \ ^{+0.27} \ (95\% \ \text{CL}) \ [51] \\ \hline \end{array}$	$\begin{array}{c} \pm 0.28 \ (68\% \ {\rm CL}) \ [40] \\ \pm 1.2 \ (68\% \ {\rm CL}) \ [40] \\ \pm 0.002 \ (68\% \ {\rm CL}) \ [21] \\ \pm 0.04 \ (68\% \ {\rm CL}) \ [21] \\ \pm 2.7 \ (68\% \ {\rm CL}) \ [42] \\ \pm 0.23 \ (68\% \ {\rm CL}) \ [42] \\ \pm 0.11 \ (68\% \ {\rm CL}) \ [44] \\ \pm 0.23 \ (68\% \ {\rm CL}) \ [44] \\ \pm 0.23 \ (68\% \ {\rm CL}) \ [46] \\ \pm 0.29 \ (68\% \ {\rm CL}) \ [47] \\ \pm 3 \ [49] \end{array}$	$\begin{array}{c} 2.228 \pm 0.549 \\ 3.484 \pm 2.352 \\ < 3.0 (90\% \text{ CL}) \\ 1.7^{+2.16}_{-1.70} \\ 17.757 \pm 5.29 \\ 3.32 \pm 0.54 \\ 1.60 \stackrel{+0.97}_{-0.91} \\ 2.69 \stackrel{+0.85}_{-0.82} \\ 1.06 \pm 0.69 \\ 125.09 \pm 3.48 \\ 1.06 \stackrel{+0.37}_{-0.53} \text{ (ATLAS)} \\ 1.17 \stackrel{+0.53}_{-0.61} \text{ (CMS)} \\ 1.03 \stackrel{+0.14}_{-0.12} \text{ (ATLAS)} \\ 1.18 \stackrel{+0.31}_{-0.27} \text{ (CMS)} \\ 1.00 \pm 0.12 \text{ (ATLAS)} \\ 1.07 \stackrel{+0.27}_{-0.29} \text{ (CMS)} \end{array}$
	-0.29 (1997) (197		-0.29

#### *Main SUSY one-loop contributions to* $h^0 \rightarrow c \overline{c}$

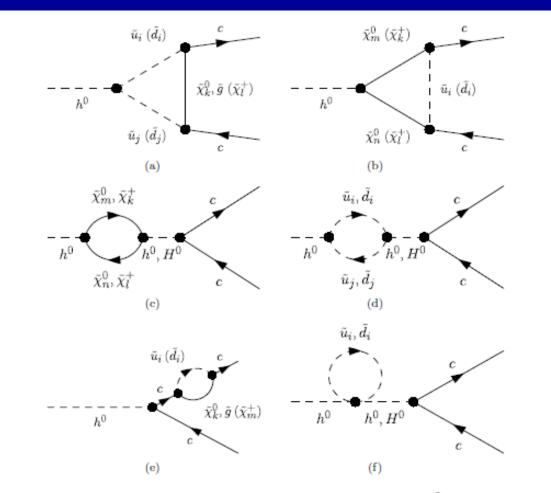
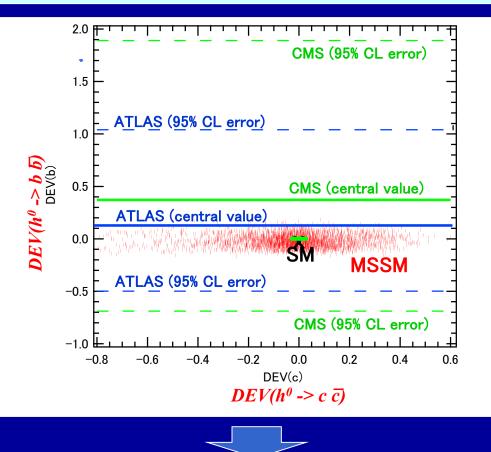


Figure 2: The main one-loop contributions with SUSY particles in  $h^0 \rightarrow c\bar{c}$ . The corresponding diagram to (e) with the self-energy contribution to the other charm quark is not shown explicitly.

### Scatter plot in $DEV(h^{\theta} \rightarrow c \ \overline{c}) - DEV(h^{\theta} \rightarrow b \ \overline{b})$ plane



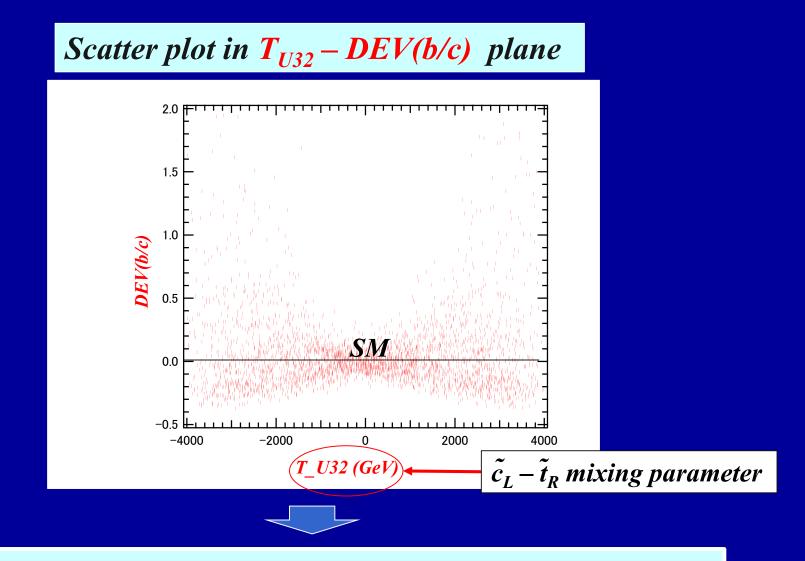
- Recent LHC data:  $DEV(h^0 \rightarrow b \ \overline{b}) = 0.12 + 0.92/-0.62 = [-0.50, 1.04]$  (ATLA S) (arXiv:1909.02845)  $DEV(h^0 \rightarrow b \ \overline{b}) = 0.37 + 1.52/-1.06 = [-0.69, 1.89]$  (CMS) (arXiv:1809.10733)
- Both SM and MSSM are consistent with the recent ATLAS/CMS data! The errors of the recent ATLAS/CMS data are too large!

5.2 Deviation of width ratio from the SM prediction

- The deviation of the width ratio from the SM prediction:

 $DEV(b/c) = [\Gamma(b) / \Gamma(c)]_{MSSM} / [\Gamma(b) / \Gamma(c)]_{SM} - 1$ 

 $\Gamma(X) = \Gamma(h^{\theta} -> XX)$ 



-There is a strong correlation between  $T_{U32}$  – DEV(b/c)! - DEV(b/c) can be as large as ~ +200% for large  $T_{U32}$ !

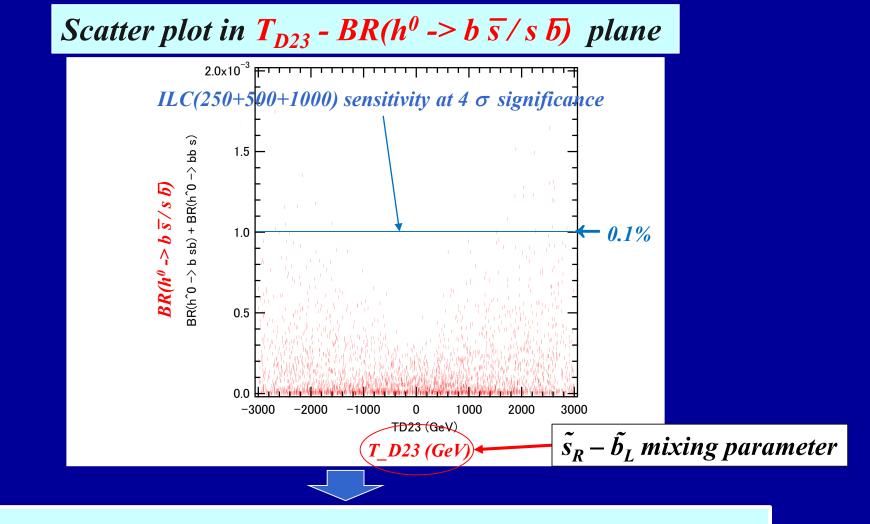
### 5.2 <u>BR( $h^0 \rightarrow b \ \overline{s} / s \ \overline{b}$ )</u>

 $BR(h^{\theta} \rightarrow b \ \overline{s} / s \ \overline{b}) \cong \theta \ (SM)$ 

#### $BR(h^{0} \rightarrow b \overline{s} / s \overline{b})$ can be as large as ~ 0.17% (MSSM with QFV)! (See also Gomez-Heinemeyer-Rehman, PR D93 (2016) 095021 [arXiv:1511.04342].)

ILC(250+500+1000) sensitivity could be ~ 0.1% (at 4  $\sigma$  significance)!

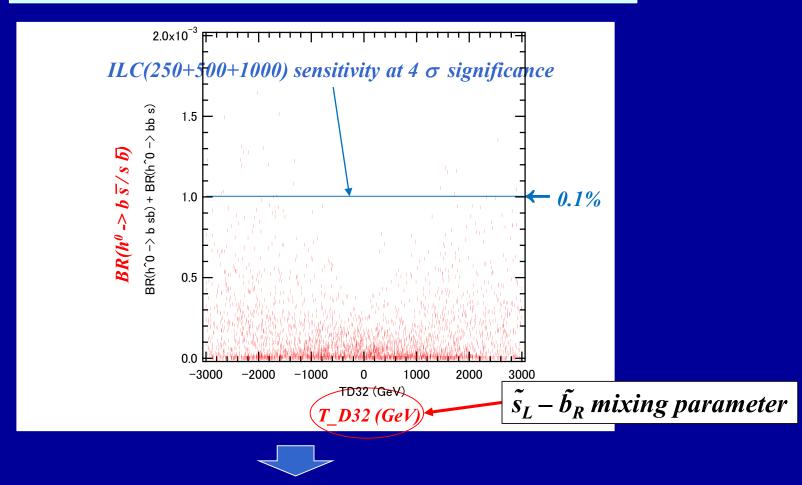
Private communication with Junping Tian; See also Barducci et al., JHEP 12 (2017) 105 [arXiv:1710.06657]



- -There is a strong correlation between  $T_{D23}$   $BR(h^0 \rightarrow b \overline{s} / s \overline{b})!$
- $BR(h^0 \rightarrow b \overline{s} / s \overline{b})$  can be as large as 0.17% for large  $T_{D23}$ !
- ILC(250 + 500 + 1000) sensitivity could be ~ 0.1% at 4 sigma significance! Private communication with Junping Tian; See also Barducci et al., JHEP 12 (2017) 105 [arXiv:1710.06657].

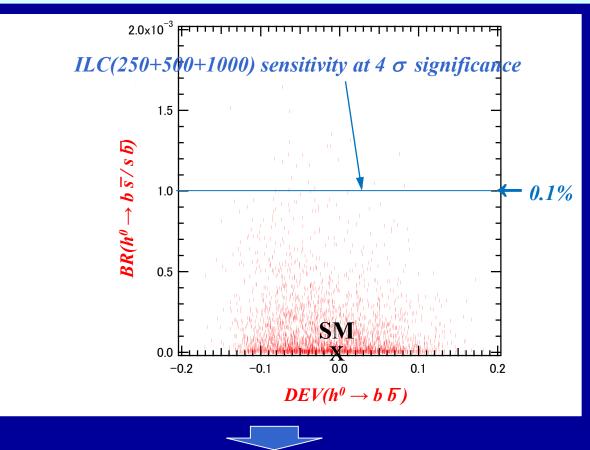
- LHC & HL-LHC sensitivity should not be so good due to huge QCD BG!

### Scatter plot in $T_{D32}$ - $BR(h^{\theta} \rightarrow b \overline{s} / s \overline{b})$ plane



- There is also a strong correlation between  $T_{D32}$  -  $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b})!$ -  $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b})$  can be as large as 0.17% for large  $T_{D32}!$ 

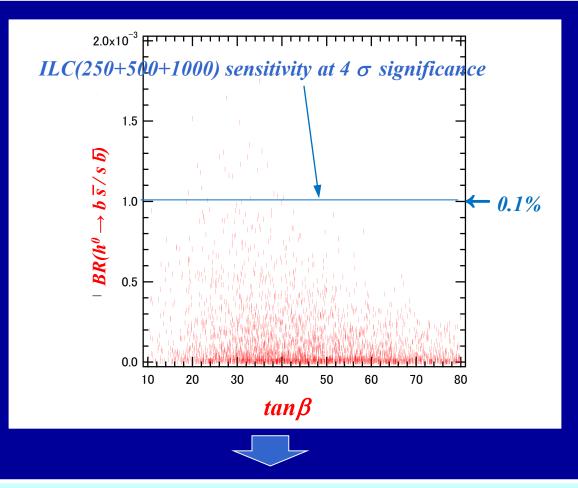
### Scatter plot in $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b}) - DEV(h^0 \rightarrow b \ \overline{b})$ plane



- There is a strong correlation between  $DEV(h^0 \rightarrow b \ \overline{b}) \& BR(h^0 \rightarrow b \ \overline{s}/s \ \overline{b})!$ 

- This is due to the fact that  $DEV(h^0 \rightarrow b \ \overline{b}) \& BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b})$  have a common origin of enhancement effect, i.e. large trilinear couplings  $T_{D23,32,33} \& T_{U23,32,33}$ .

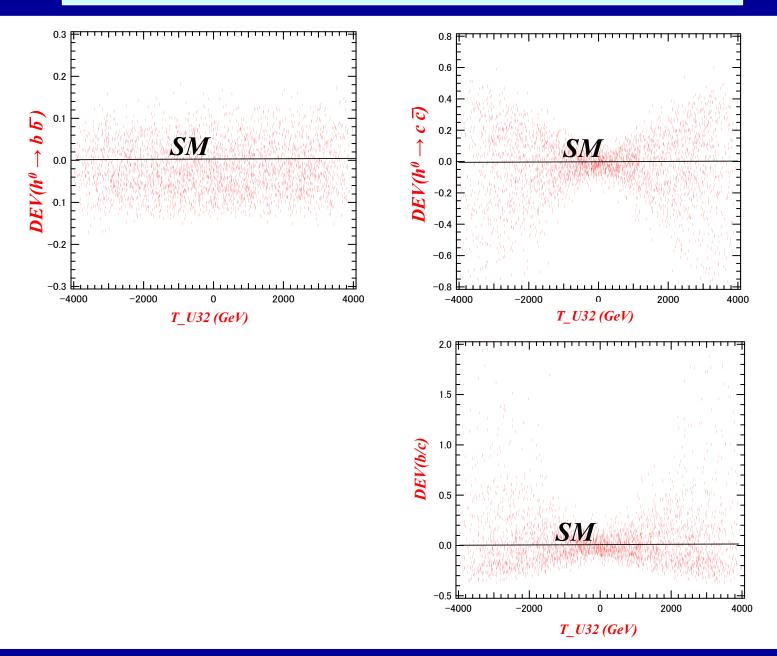
#### Scatter plot in $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b}) - tan\beta$ plane



- There is a strong correlation between  $BR(h^0 \rightarrow b \ \overline{s} / s \ \overline{b}) \& tan \beta!$ 

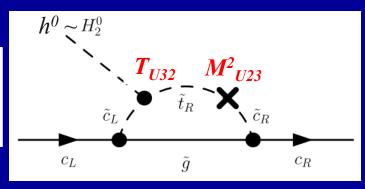
- BR( $h^{0} \rightarrow b \overline{s} / s \overline{b}$ ) can be as large as 0.17% for tan $\beta \sim 30!$ 

### Caveat for very large $DEV(h^{0} \rightarrow c \ \overline{c}) \& DEV(b/c)$



### Caveat for very large $DEV(h^{0} \rightarrow c \ \overline{c}) \& DEV(b/c)$

**Gluino loop** contribution to  $h^0 \rightarrow c \ \overline{c}$  can be very large (positive and negative) for large  $T_{U32} * M^2_{U23}!$ 



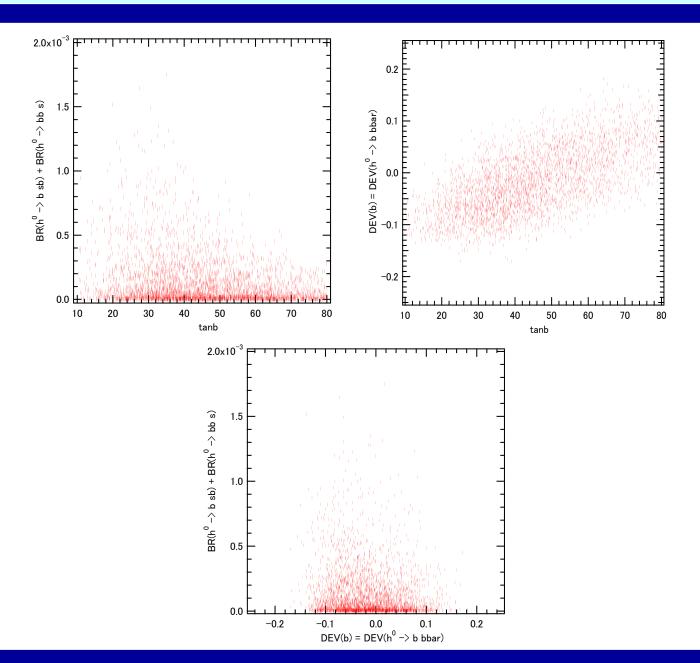
The interference term between the tree diagram and the gluino one-loop diagram can be very large (positive and negative) for large  $T_{U32} * M^2_{U23}$ , which can lead to even NEGATIVE width  $\Gamma(h^0 \rightarrow c \ \overline{c})$  at one-loop level !

In this case perturbation theory breaks down!

A large deviation of  $\Gamma(h^0 \to c \ \overline{c})$  from the SM value is in principle possible due to large values of the product  $T_{U32} * M^2_{U23}$ .

Since there exists no physical constraint on this product, the deviation  $DEV(h^0 \rightarrow c \ \overline{c})$  can be unnaturally large. So, we show only the results with a deviation from the SM up to ~ +/-60%.

### Correlations among $DEV(h^{\theta} \rightarrow b \overline{b})$ , $BR(h^{\theta} \rightarrow b \overline{s} / s \overline{b})$ , $tan\beta$

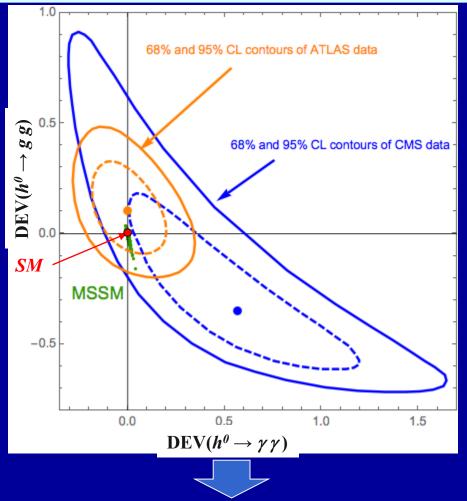


#### Effect of Resummation of the bottom Yukawa coupling at large $tan\beta$

As for  $\Gamma(h^0 \rightarrow b \,\overline{b}) \& \Gamma(h^0 \rightarrow b \,\overline{s}/s \,\overline{b})$ , we have considered the large tan $\beta$ enhancement and the resummation of the bottom Yukawa coupling [1]. It turns out, however, that in our case with large  $m_A$  close to the decoupling Higgs limit, the resummation effect ( $\Delta_b$  effect) is very small (< 0.1%).

[1] M. Carena et al., Nucl. Phys. B 577 (2000) 88 [hep-ph/9912516].

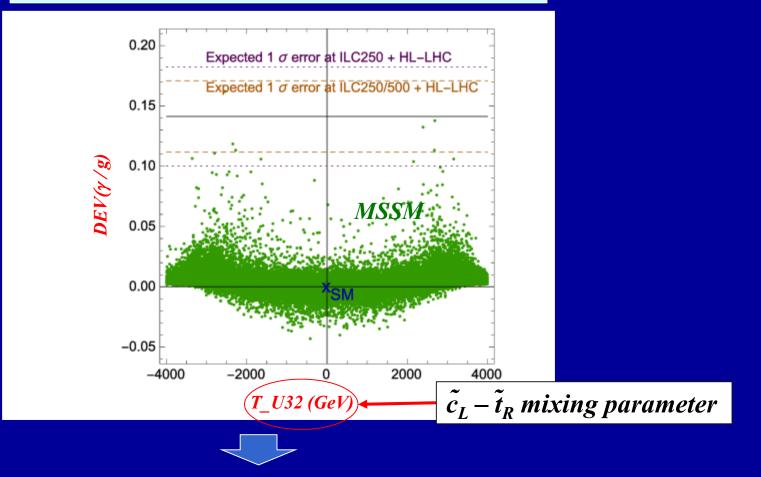
### Scatter plot in DEV( $h^{\theta} \rightarrow \gamma \gamma$ ) - DEV( $h^{\theta} \rightarrow g g$ ) plane



- Both SM and MSSM are consistent with the recent ATLAS/CMS data!: ATLAS: arXiv:1909.02845 (Phys.Rev.D 101 (2020) 012002) CMS: arXiv:1804.02716 (JHEP 11 (2018) 185)

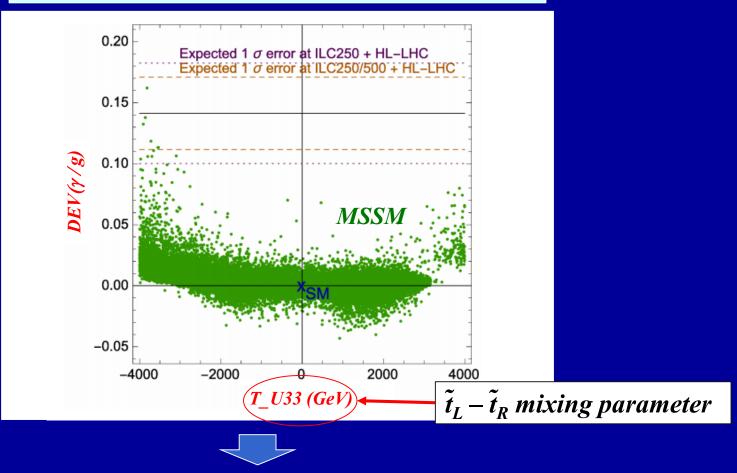
- The errors of the recent ATLAS/CMS data are too large!

### Scatter plot in $T_{U32} - DEV(\gamma/g)$ plane



-There is a strong correlation between  $T_{U32} - DEV(\gamma/g)$  ! -  $DEV(\gamma/g)$  can be as large as ~ +15% for large  $T_{U32}$  !

### Scatter plot in $T_{U33} - DEV(\gamma/g)$ plane



-There is a strong correlation between  $T_{U33} - DEV(\gamma/g)$  ! -  $DEV(\gamma/g)$  can be as large as ~ +16% for large  $T_{U33}$  !