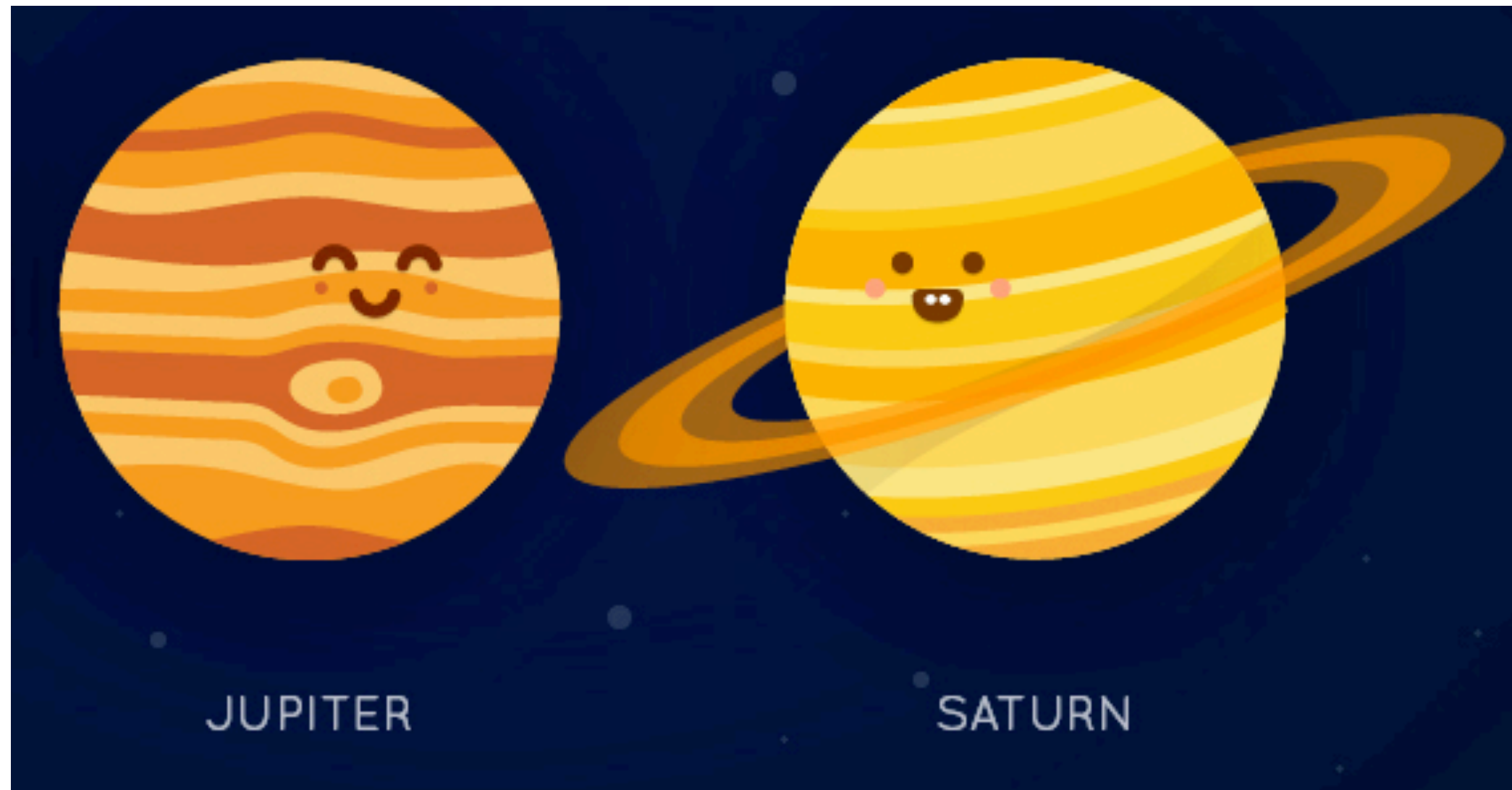


Local Constraints on the Dark Sector

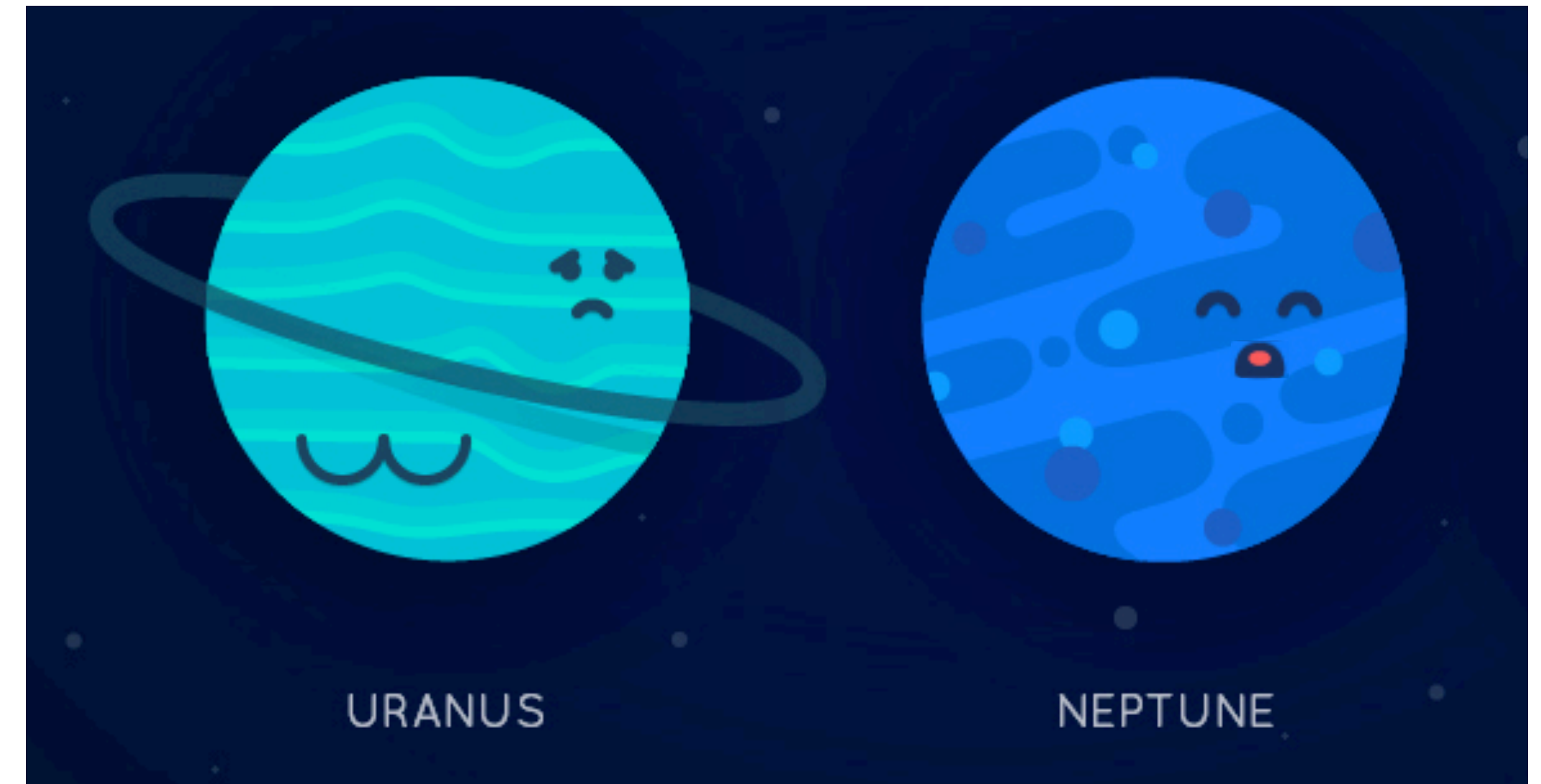
by Future Missions to Uranus and Neptune

Deniz Soyuer, Lorenz Zwick and Prasenjit Saha



Missions that have visited Jupiter and Saturn:

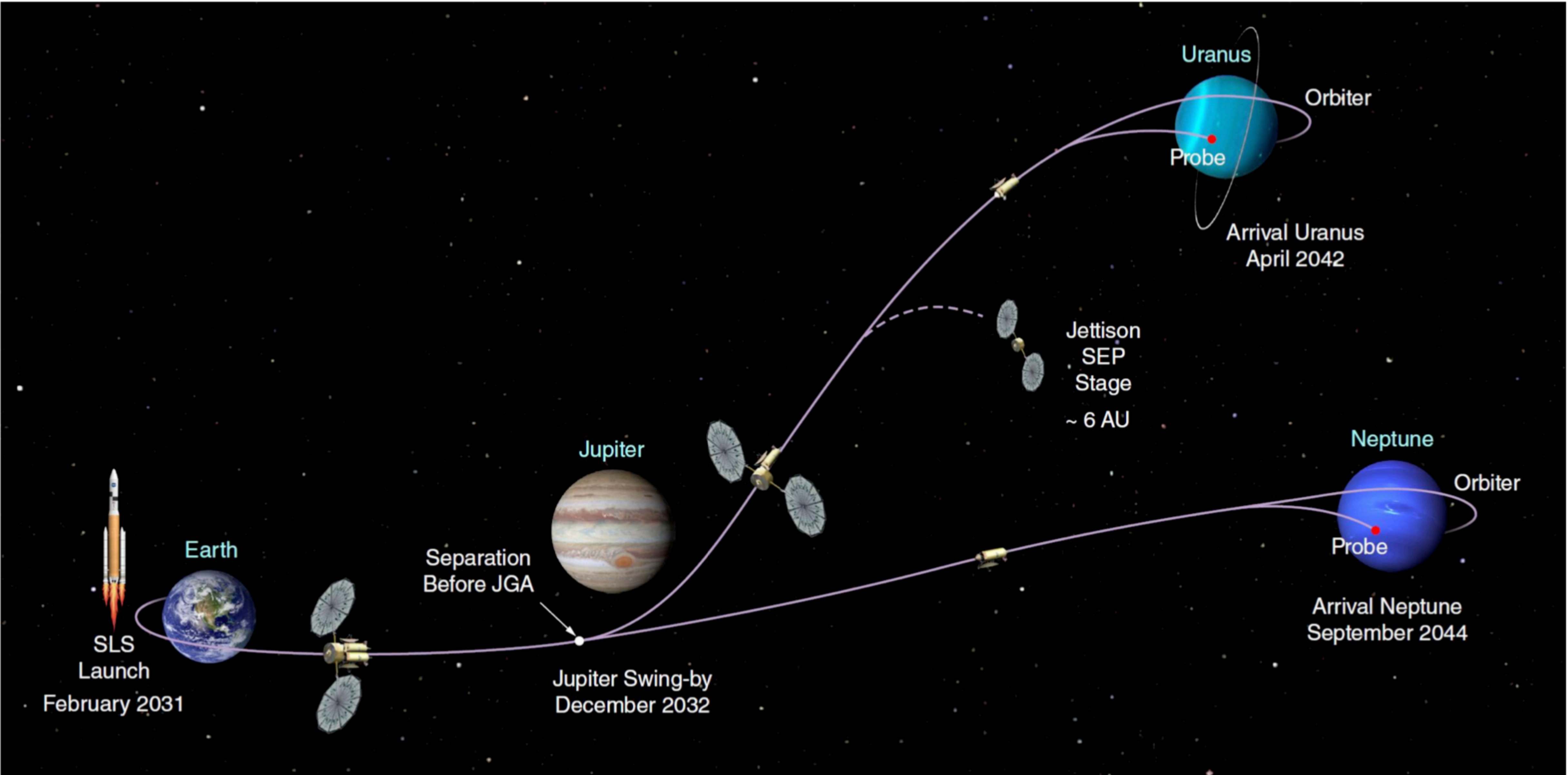
- Pioneer 10
- Pioneer 11
- Voyager 1
- Voyager 2
- Ulysees
- Galileo
- Cassini
- New Horizons
- Juno
- JUICE (2022)



Missions that have visited Uranus and Neptune:

- Voyager 2

Two Planet-Two Spacecraft Mission Concept



Credit: John O. Elliott, *Ice Giant Systems 2020*

Here is how the mission would look like

2031 February:

Space Launch System departure from Earth.

2032 December:

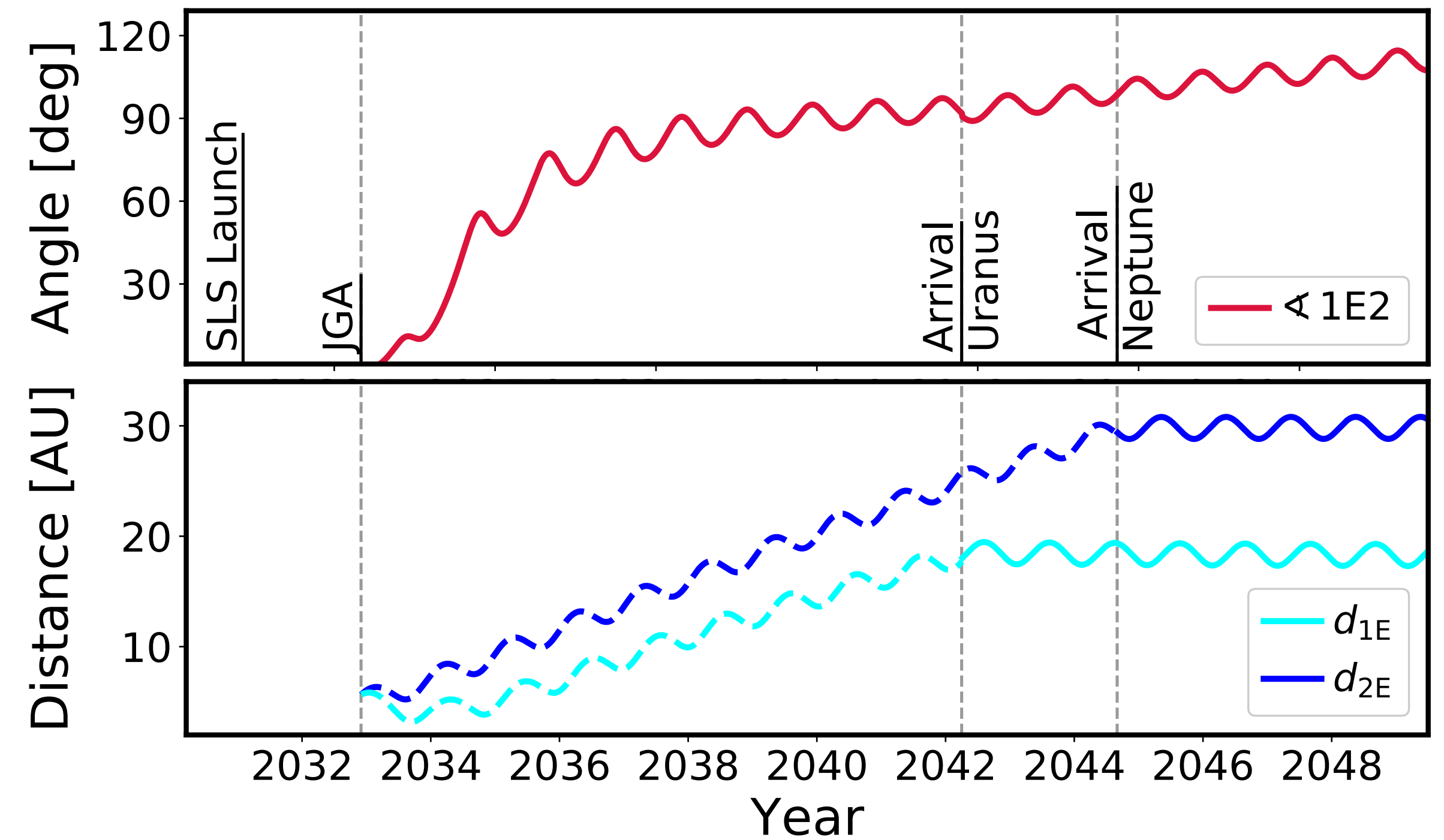
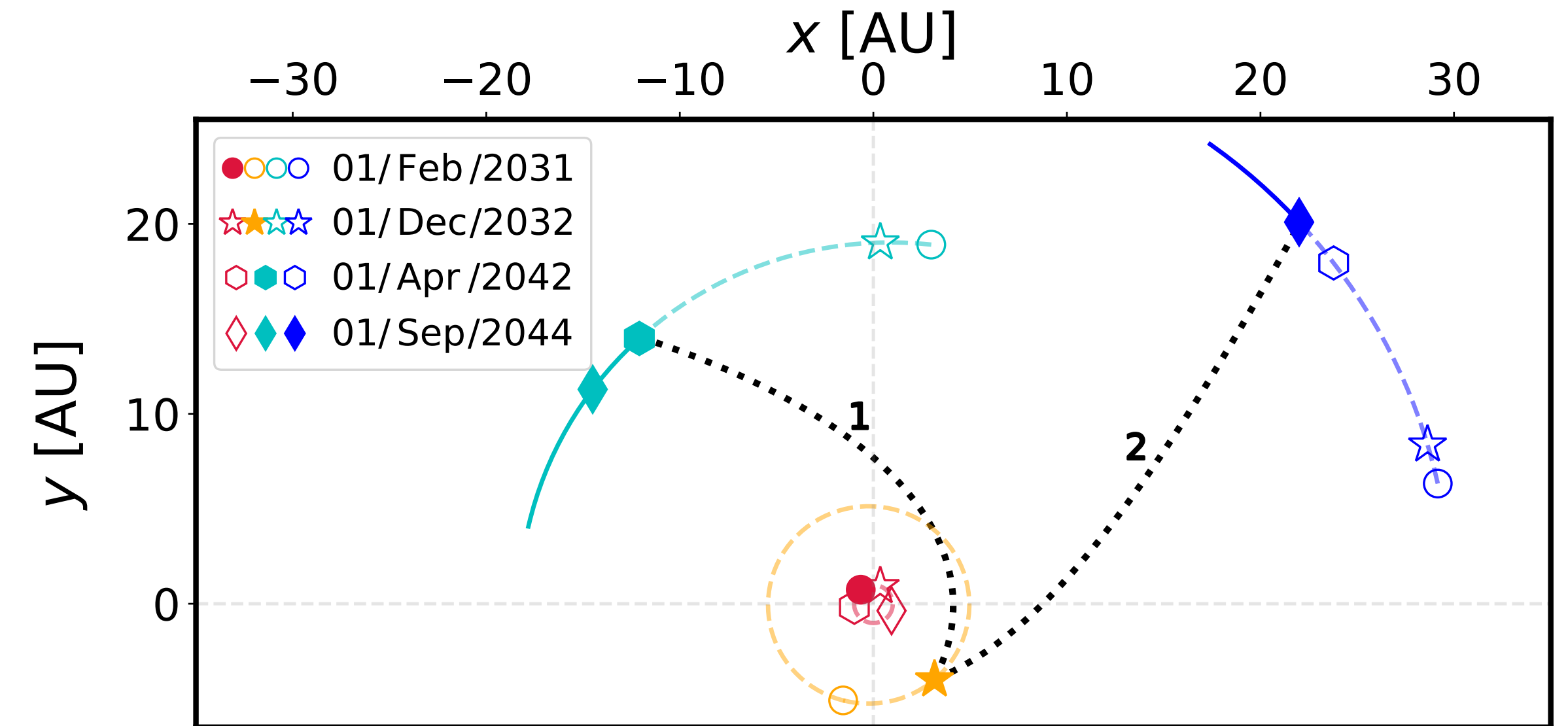
Separation of the spacecraft and subsequent JGA.

2042 April:

Arrival of the first spacecraft at Uranus.

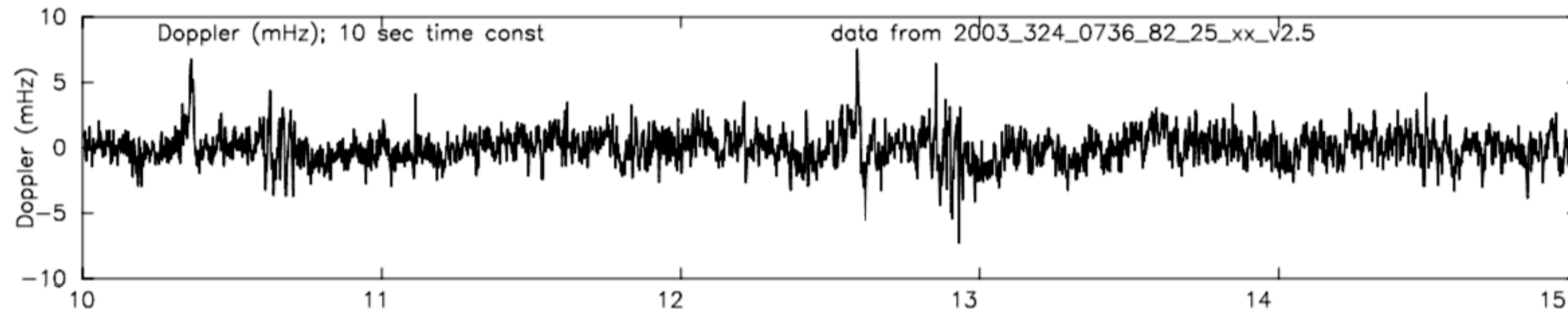
2044 September:

Arrival of the second spacecraft at Neptune.

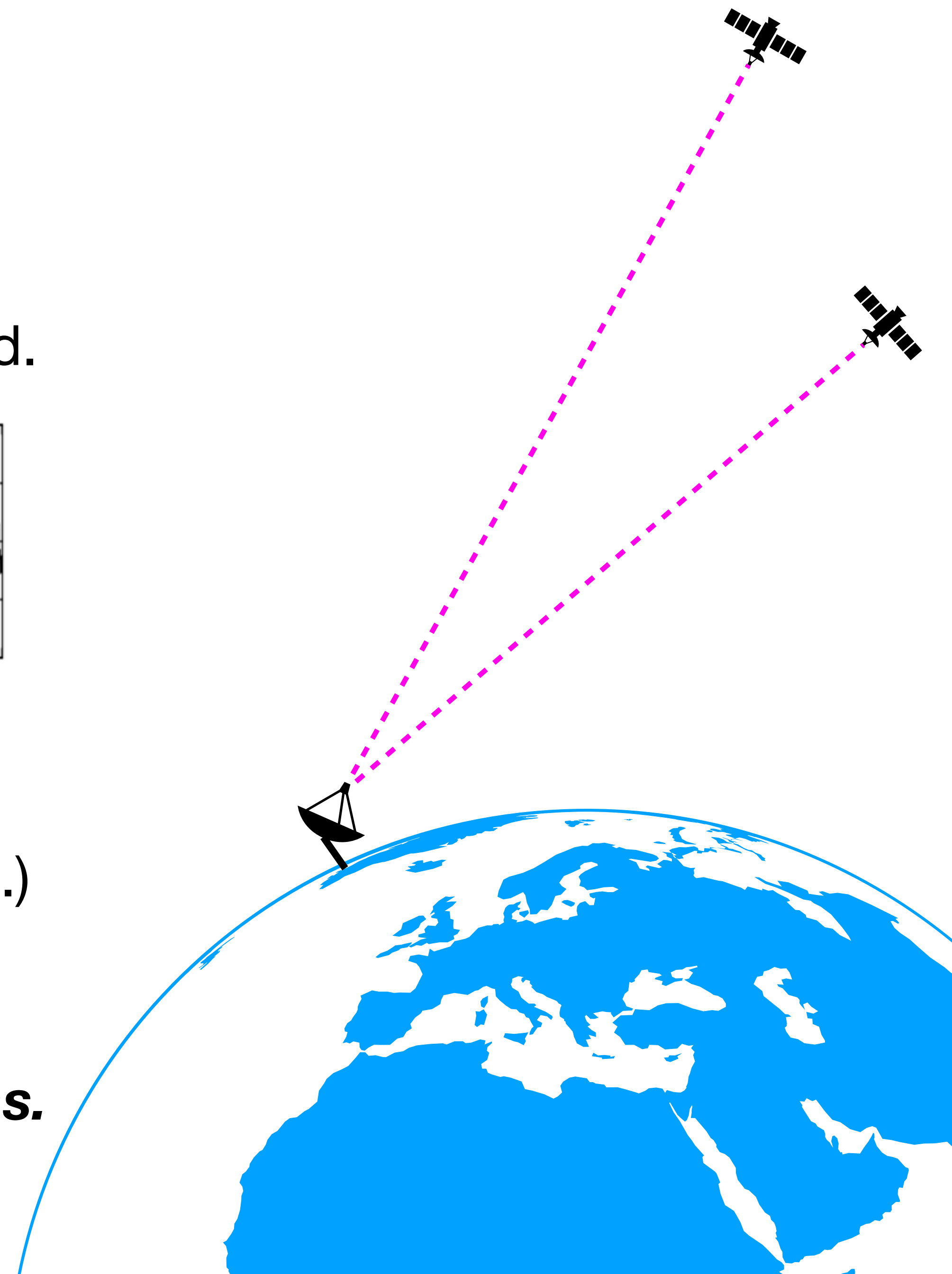


Searching for Gravitational Waves

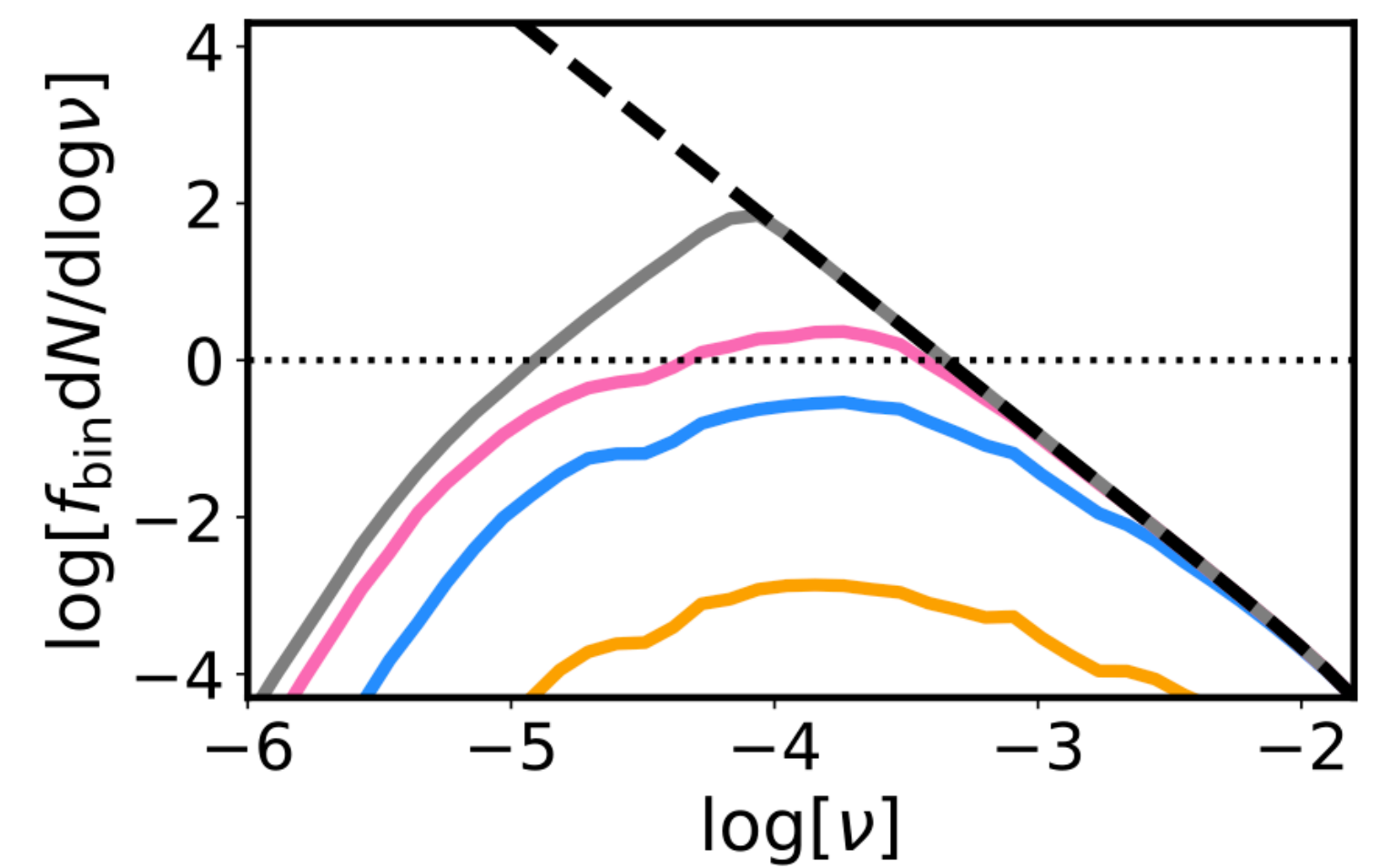
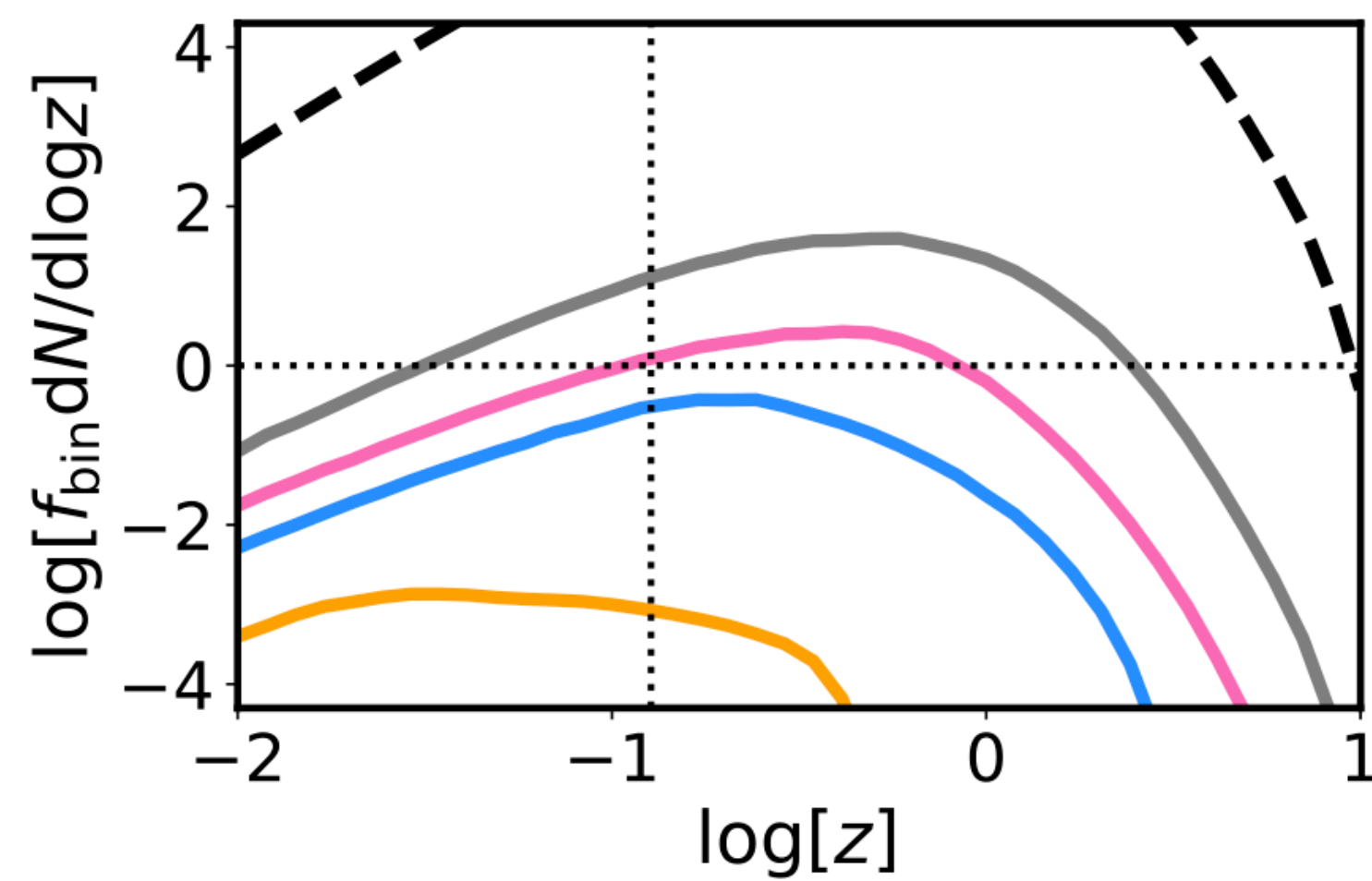
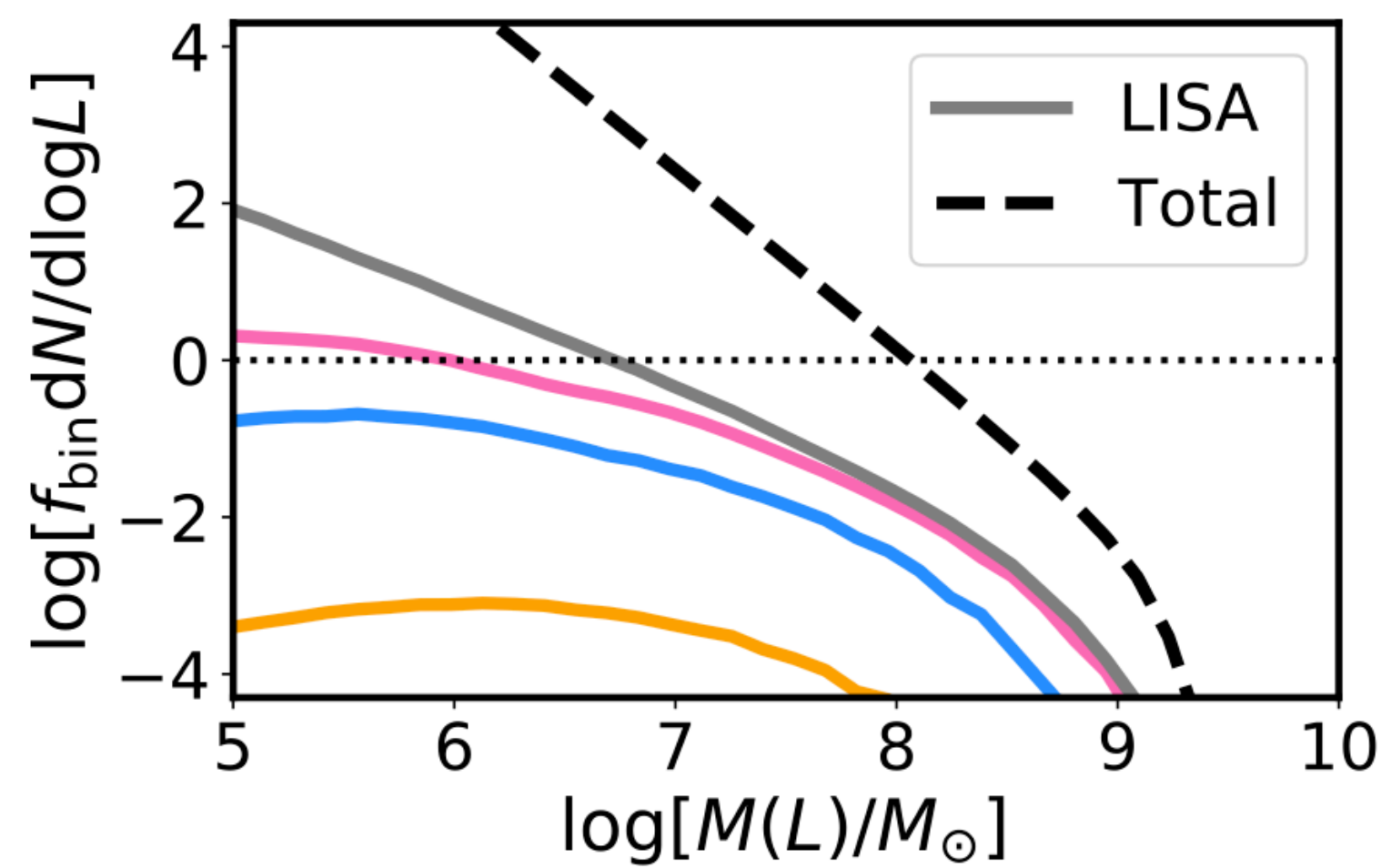
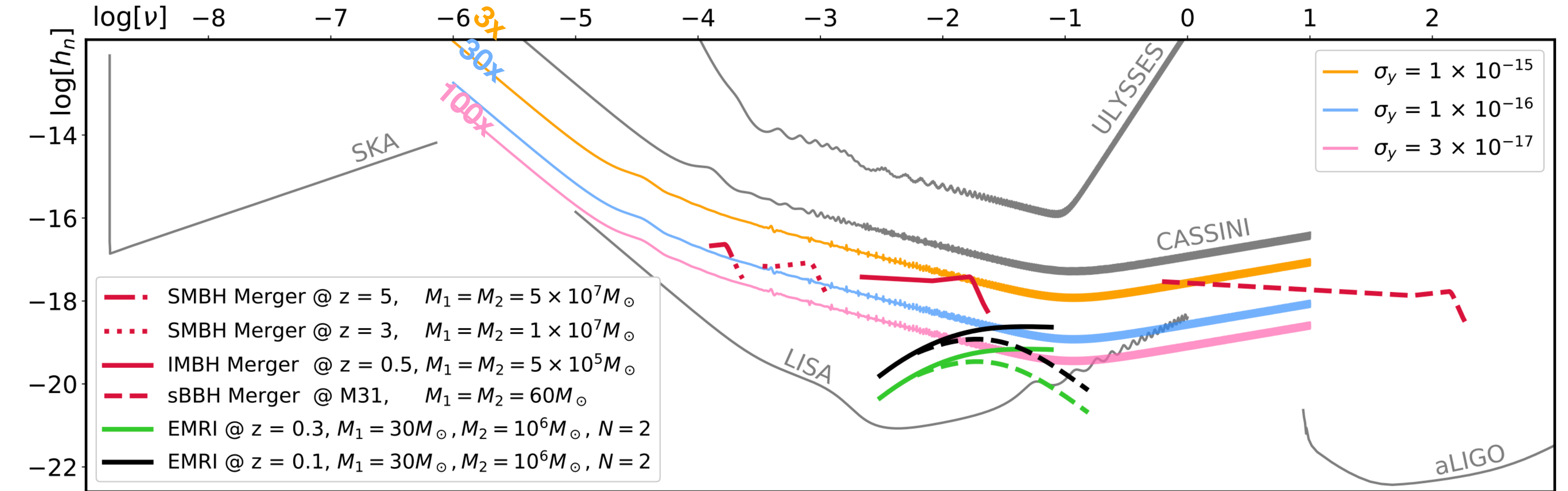
- Cruise time is around **10 years** to the ice giants.
- Constant communication through the **radio link**.
- Fluctuations in the radio carrier frequency are recorded.



- **GWs** passing through the system cause fluctuations.
- Has been tried before (*Pioneer 11*, *Ulysses*, *Cassini* etc.)
- Until now: Low SNR → No detection
- *Revisit the topic 24 years after Cassini for IG missions.*

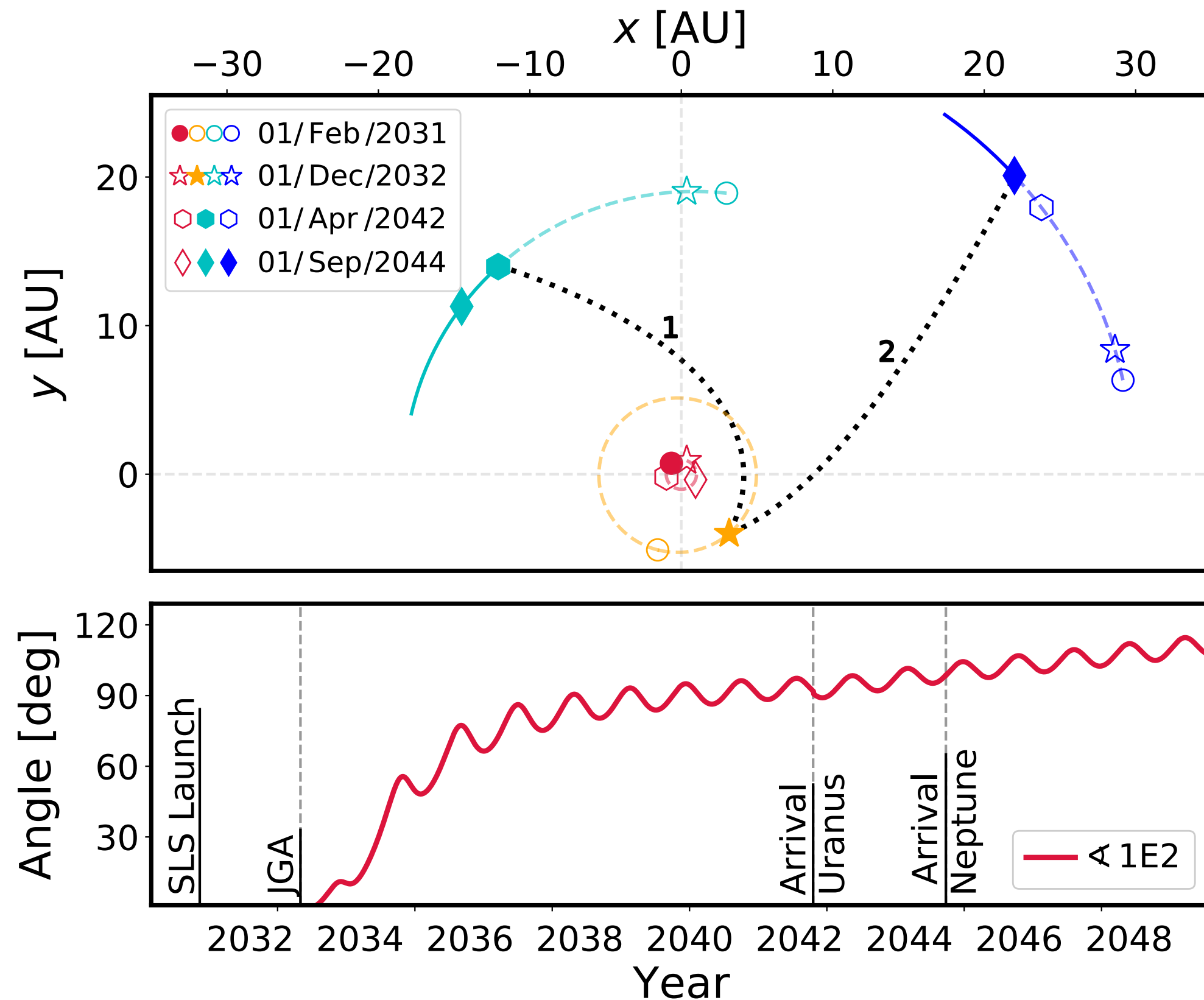


Sensitivity Curve of an Ice Giant mission to Gravitational Waves

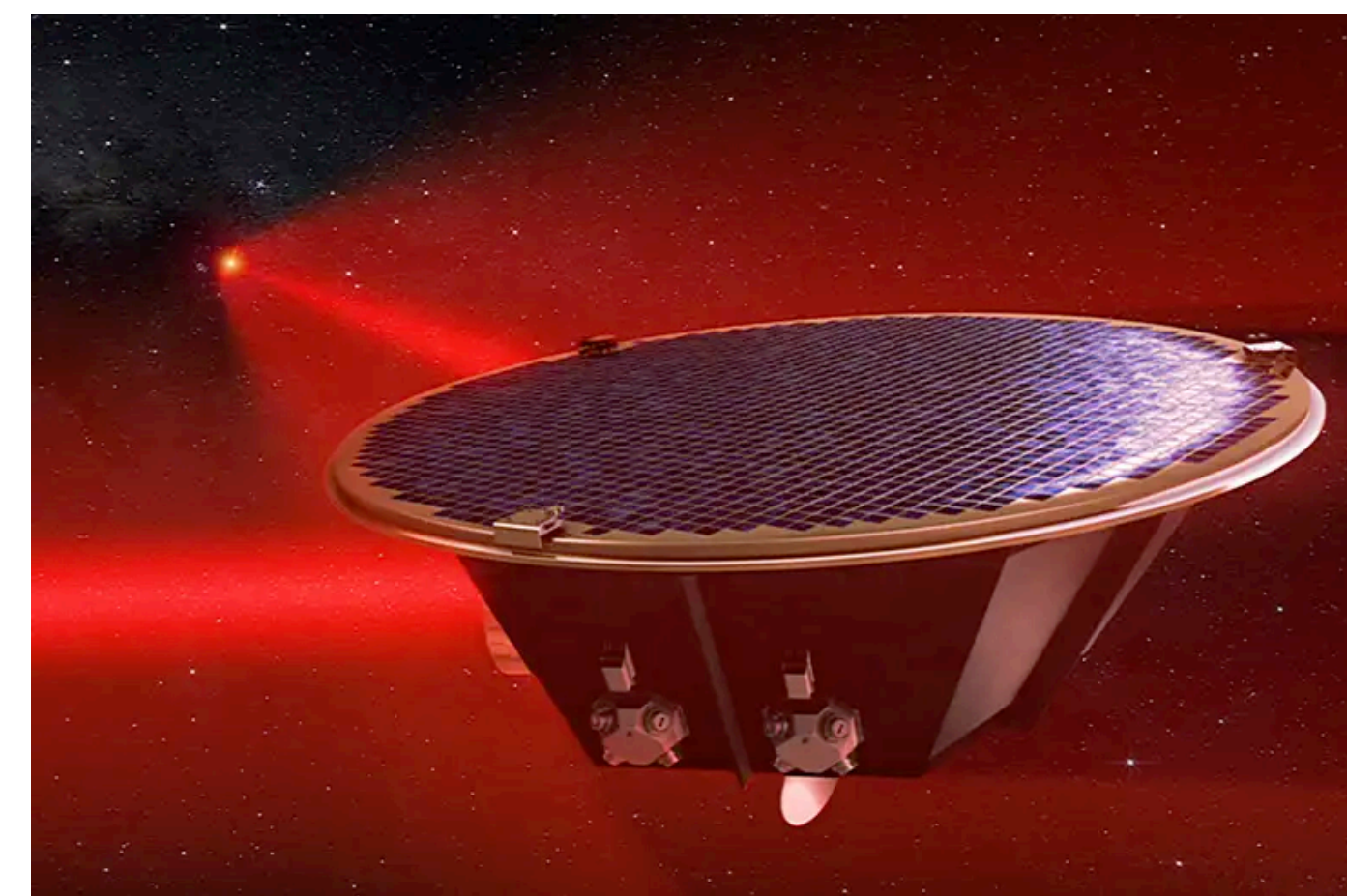


Ice Giants + LISA

- Remember that the IG missions and LISA form a $\sim 90^\circ$ triangle.
- Improved sky localization would enable optical follow-up with wide-field telescopes.



- $2 \times 10^6 M_\odot$ SBHB at $z = 1$:
 - **LISA alone:** $\sim 10 \text{ deg}^2$
 - **LISA with some Doppler help:** $\sim 1 \text{ deg}^2$

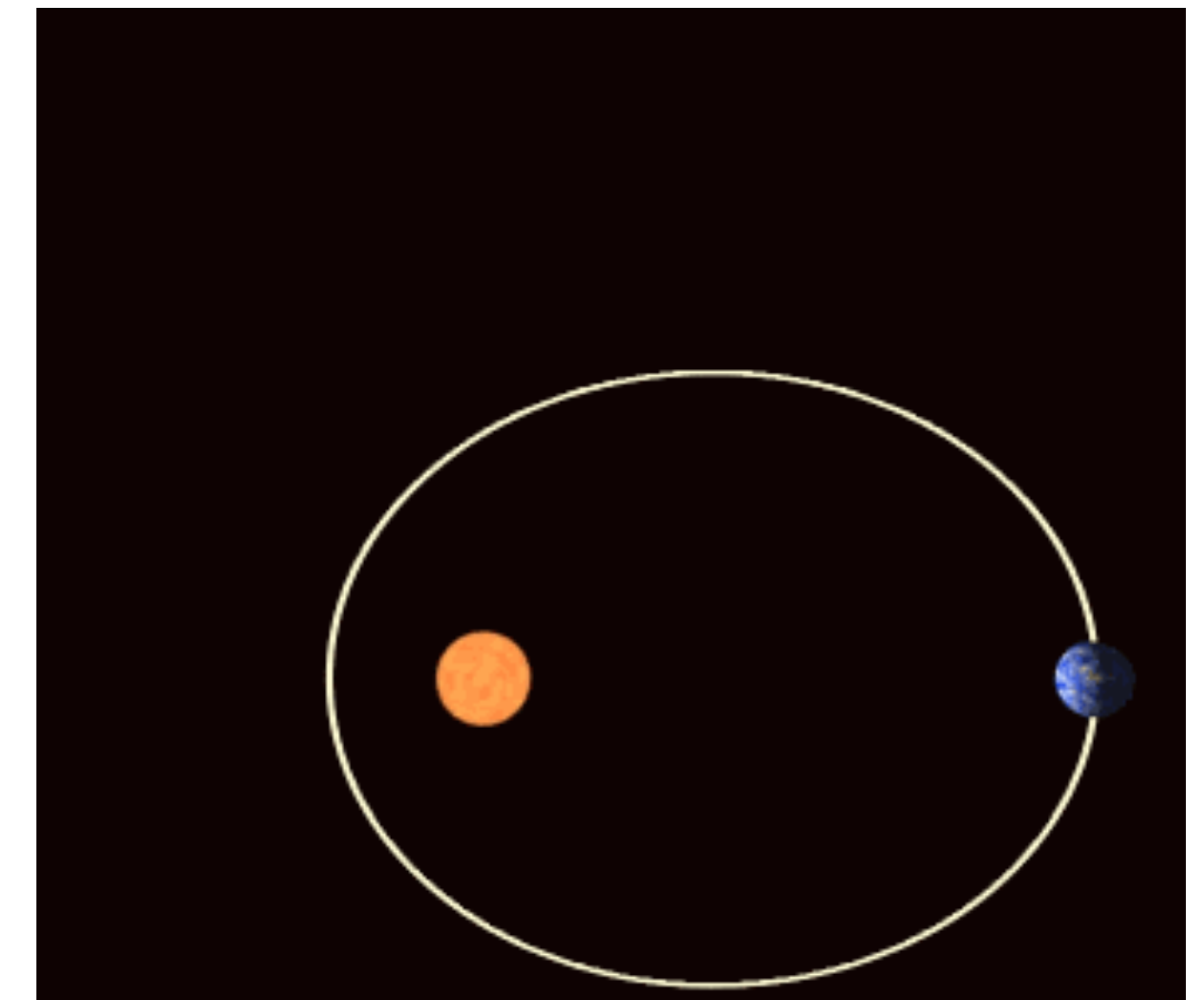
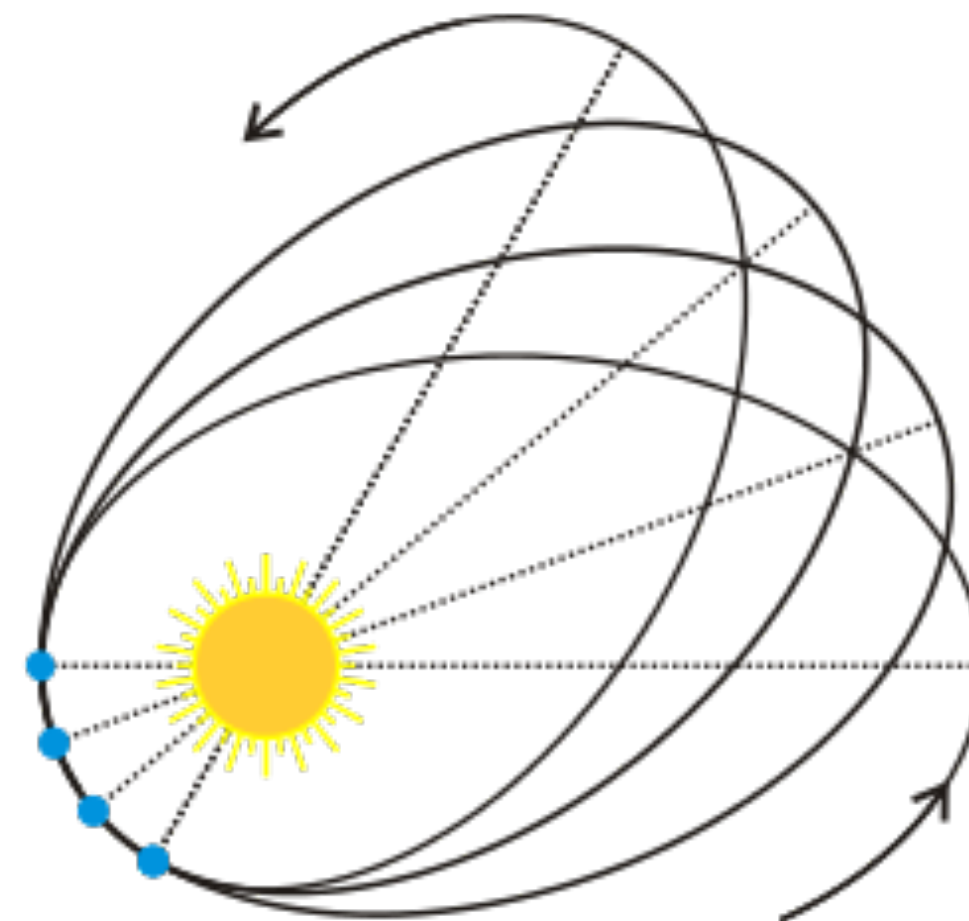


Perihelion Precession of Planets

- The elliptical orbits of planets rotate depending on the **distance to the Sun** and the **enclosed mass**.
- **Radial perturbations** δA_R to the central potential changes this precession rate.
- Compare **expected** precession to **observation** to infer the nature of perturbations.

$$\langle \dot{\omega}_p \rangle = \frac{\sqrt{1 - e^2}}{na} \delta A_R$$

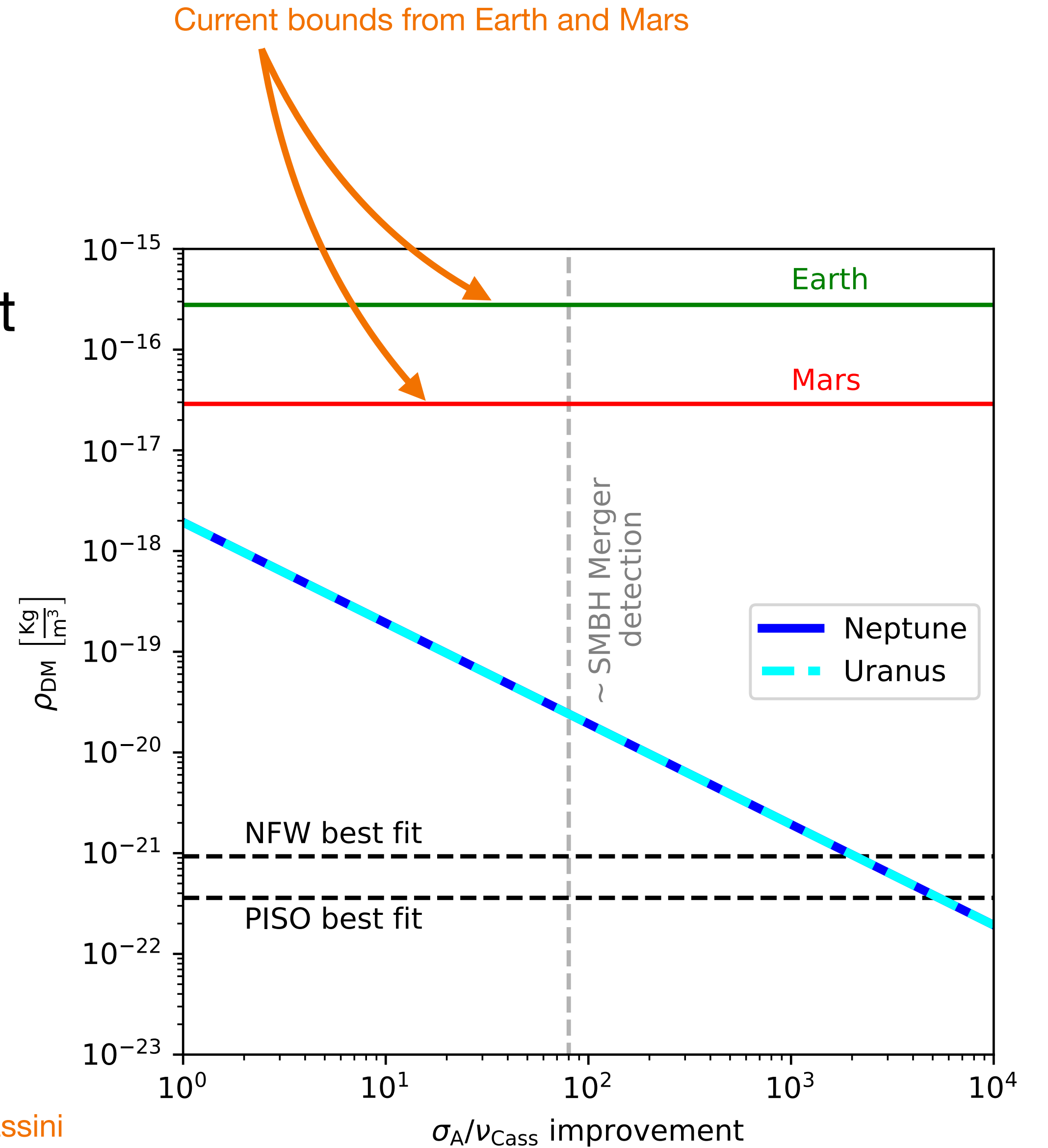
$$n = \sqrt{GM/a^3}$$



Dark Matter

- Modifications to the precession due to constant density local dark matter would look like:

$$\langle \dot{\omega}_p \rangle = - \frac{\sqrt{1 - e^2}}{n} 2\pi G \rho_{\text{DM}}$$



Noise improvement relative to Cassini

Yukawa-like Potential

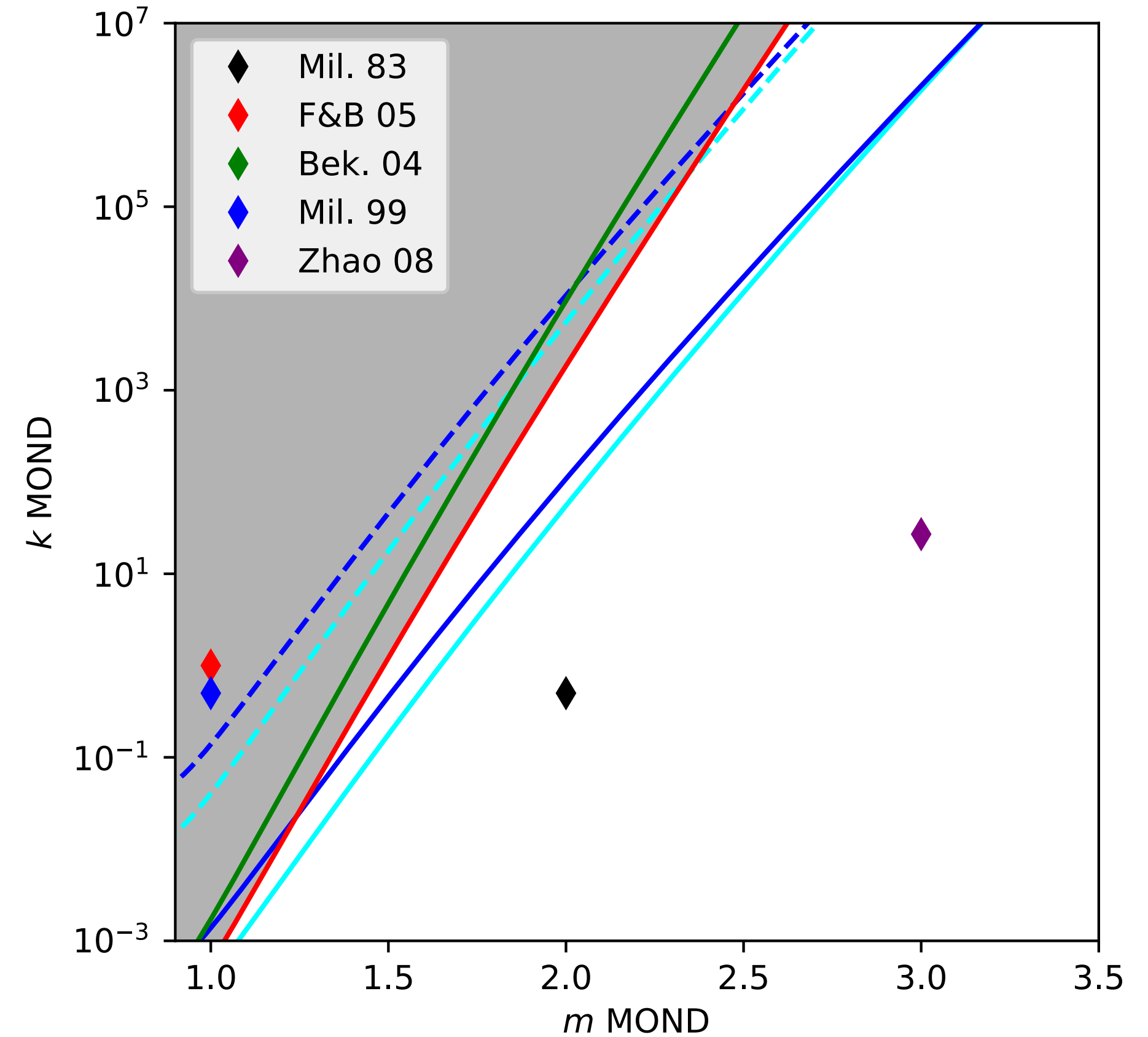
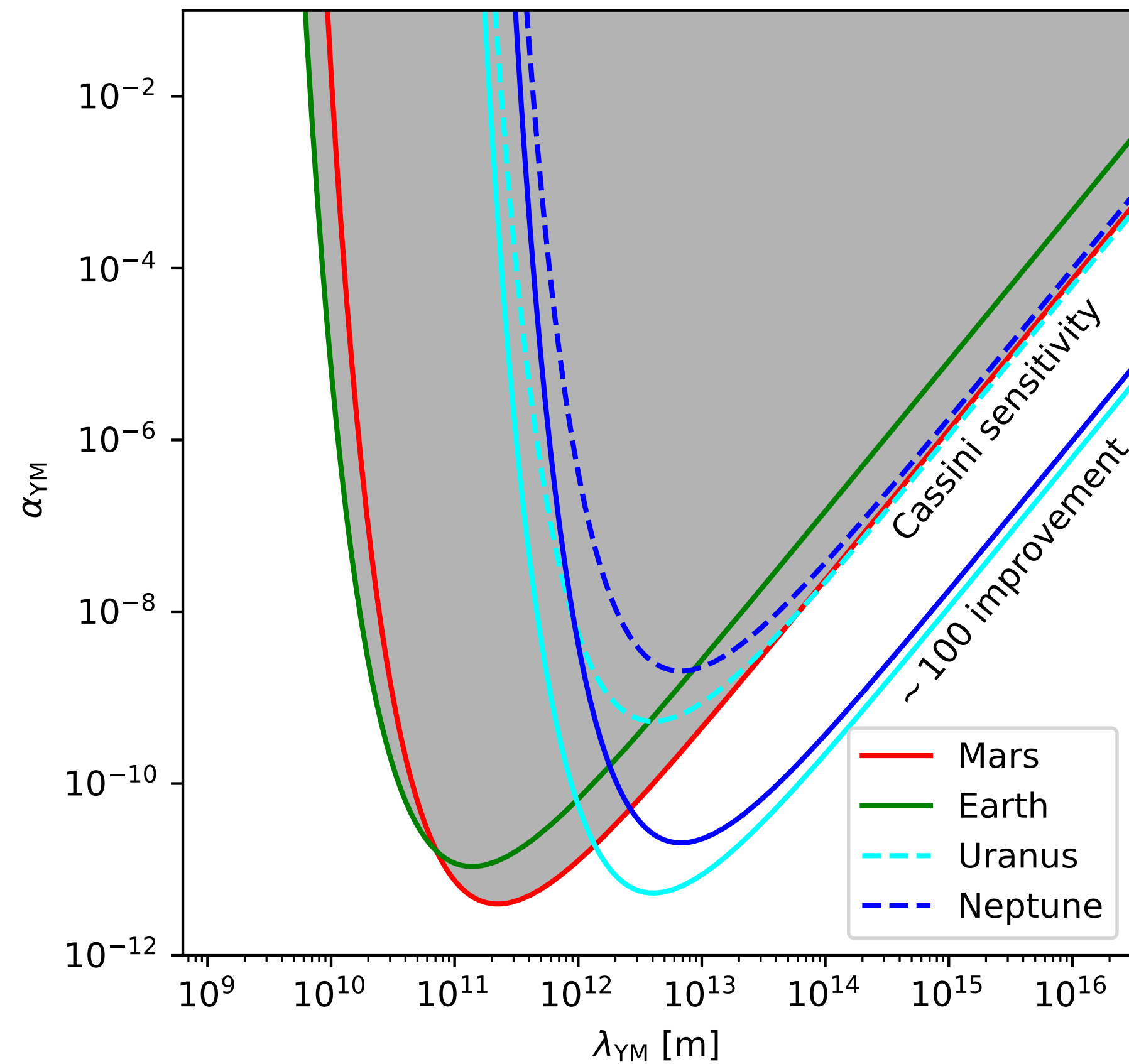
$$\phi = -\frac{G_\infty M}{r} \left[1 + \alpha_Y \exp \left\{ -\frac{r}{\lambda_Y} \right\} \right]$$

$$\langle \dot{\omega}_p \rangle = \alpha_Y \left(\frac{a}{\lambda_Y} \right)^2 \exp \left\{ -\frac{a}{\lambda_Y} \right\} \frac{n}{2} \times \left\{ 1 - \frac{1}{8} \left[4 - \left(\frac{a}{\lambda} \right)^2 \right] e^2 + \mathcal{O}(e^4) \right\}$$

Modified Gravity Models

$$\mathbf{g} \simeq \mathbf{g}_N \left[1 + k_0 \left(a_0 / |\mathbf{g}_N| \right)^m \right]$$

$$\langle \dot{\omega}_p \rangle = -k_0 n \left(\frac{a}{r_M} \right)^{2m} m \left\{ 1 + e^2 [1 - m(5 - 2m)] / 4 + \mathcal{O}(e^4) \right\}$$



Conclusions and Summary

- Doppler tracking experiments are a *cheap* and *easy* way to search for **GWs** from **SBHBs**.
 - Chance of detecting a SBHB merger for the price of LISA's windshield washer fluid.
- Doppler tracking experiments are a *cheap* and *easy* way to complement **LISA** science.
 - ~10x better source localization compared to LISA alone.
- Doppler tracking experiments are a *cheap* and *easy* way to **constrain** the local dark sector.