

*Take-home
messages*

GWs from first-order phase transitions:

A hybrid simulation

& signal enhancement from density perturbations

*Effect of
density pert.*

Ryusuke Jinno (DESY)

SUSY 2021, 8.24.2021 @Shanghai

*Hybrid
simulation*

Intro

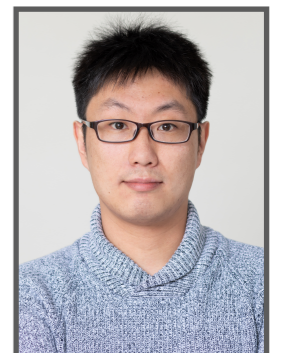
T. Konstandin



J.v.d.Vis



H. Rubira

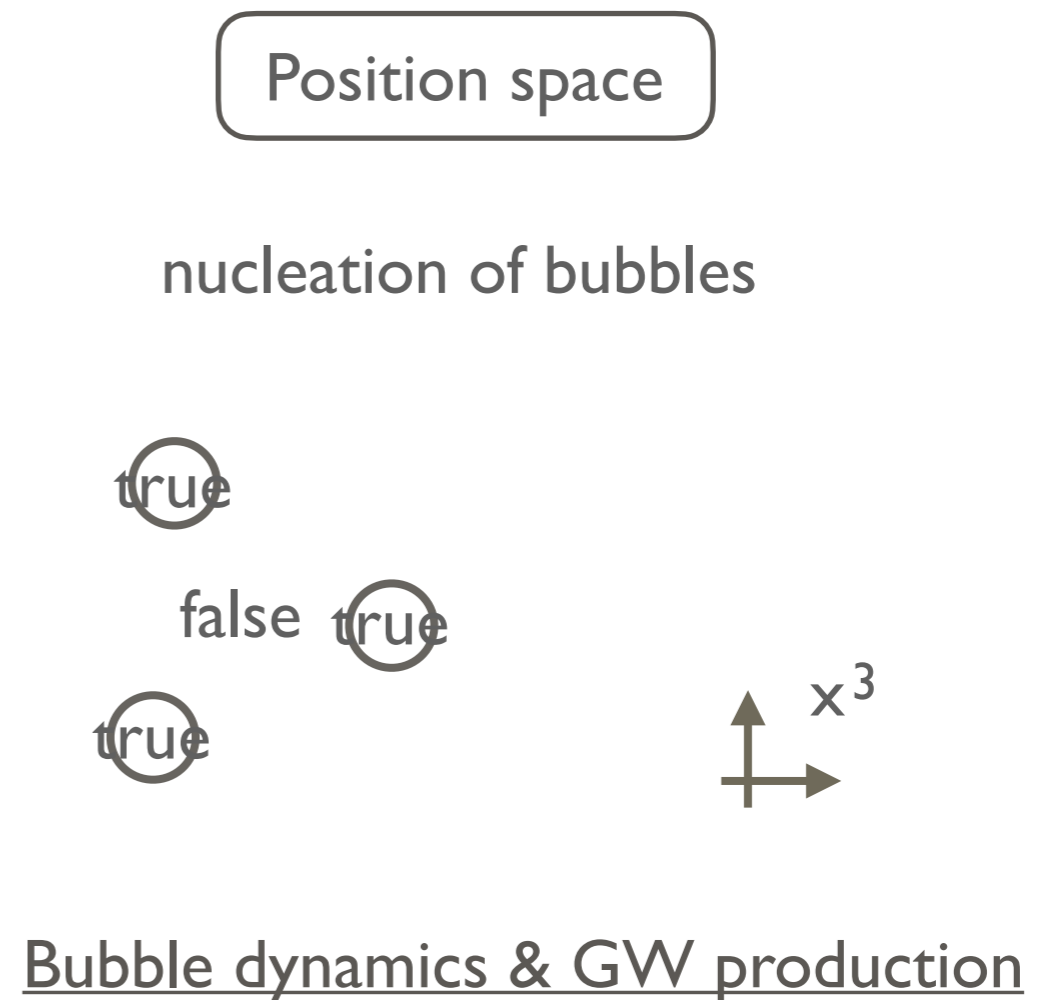
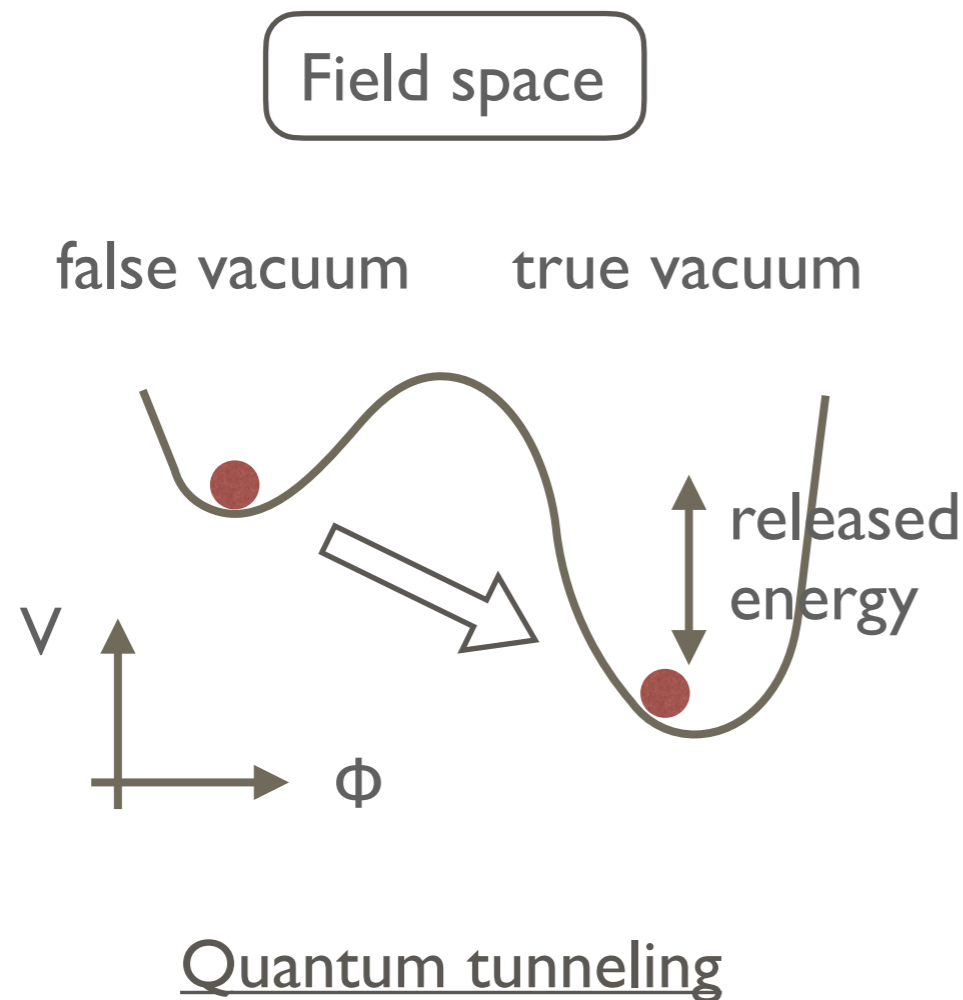


[Jinno, Konstandin, Rubira, v.d.Vis, to appear]

[Jinno, Konstandin, Rubira, JCAP 04 (2021) 014, 2010.00971]

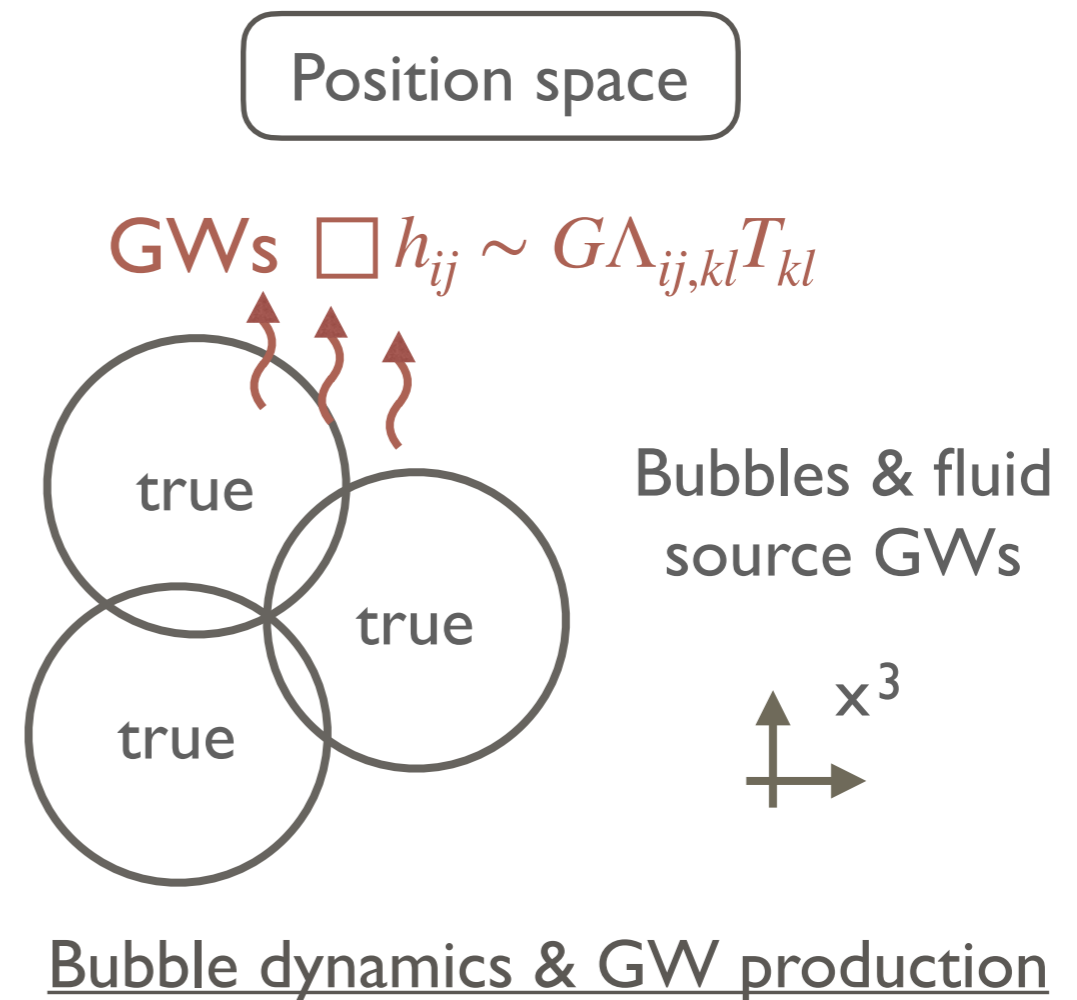
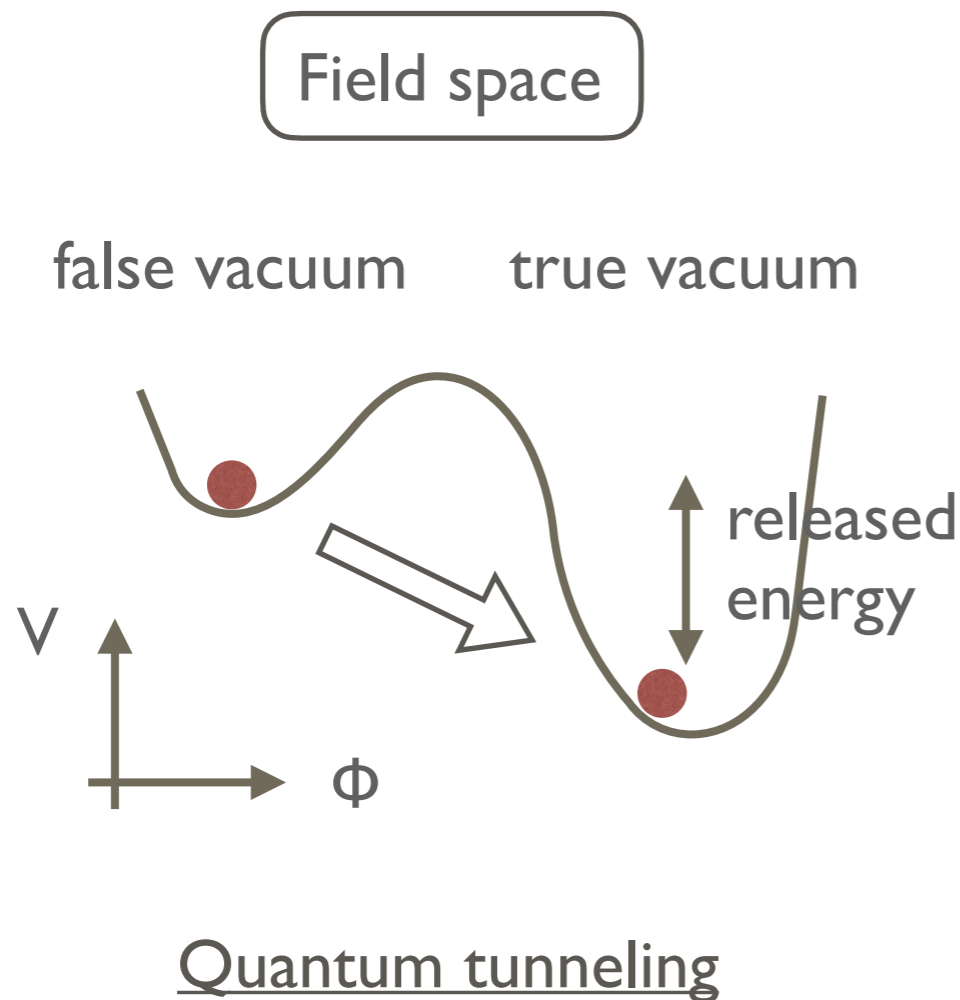
1ST-ORDER PT & GW PRODUCTION: A BRIEF SKETCH

- Bubbles nucleate, expand, collide and disappear



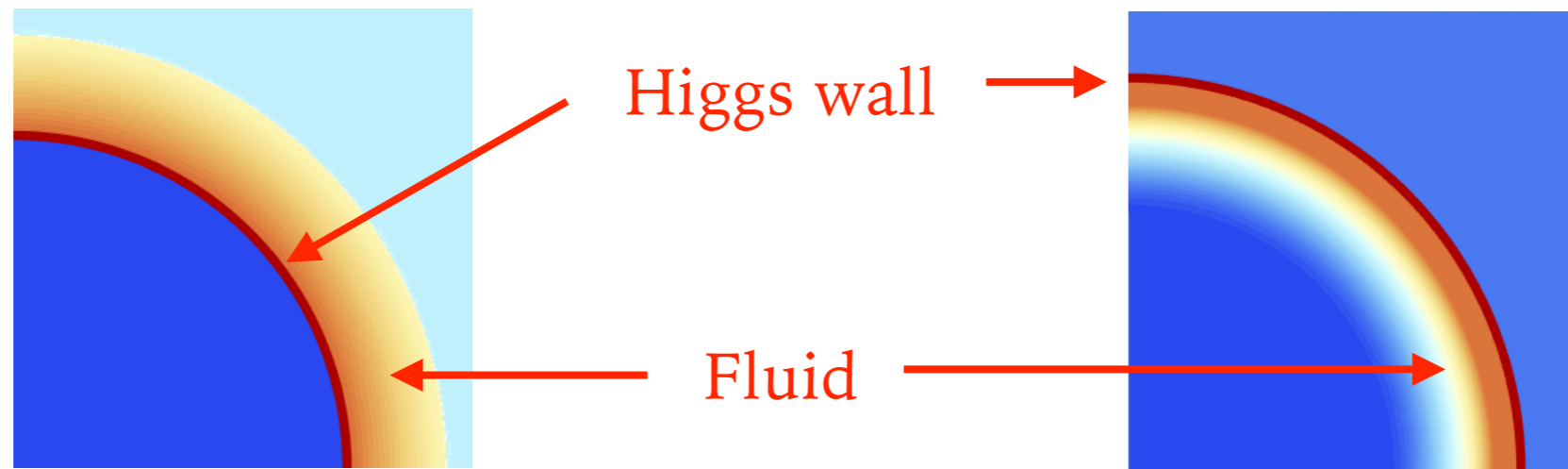
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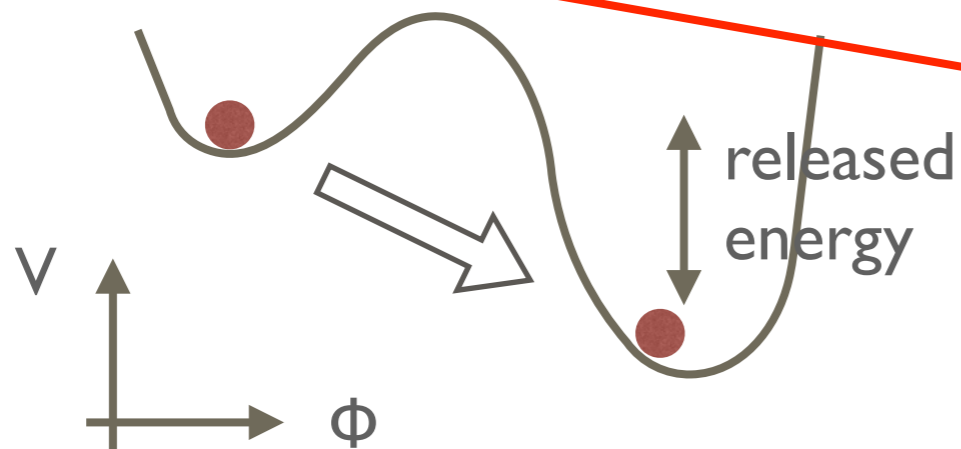


1ST ORDER PT & GW PRODUCTION: A BRIEF SKETCH

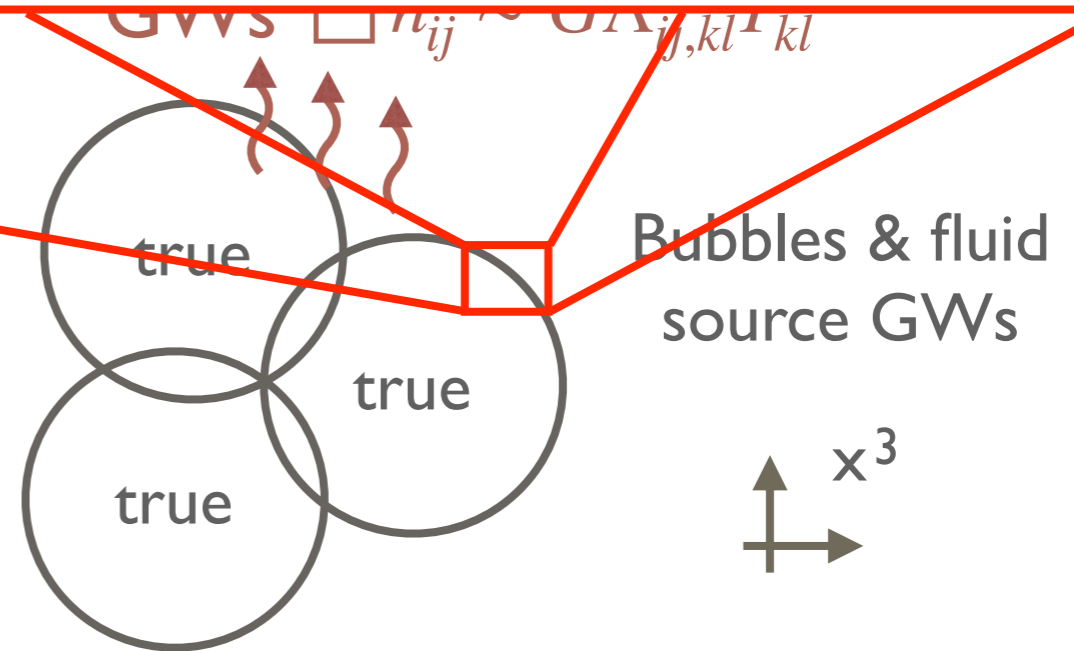
Bubble dynamics is in reality a violent process involving fluid dynamics



false vacuum true vacuum

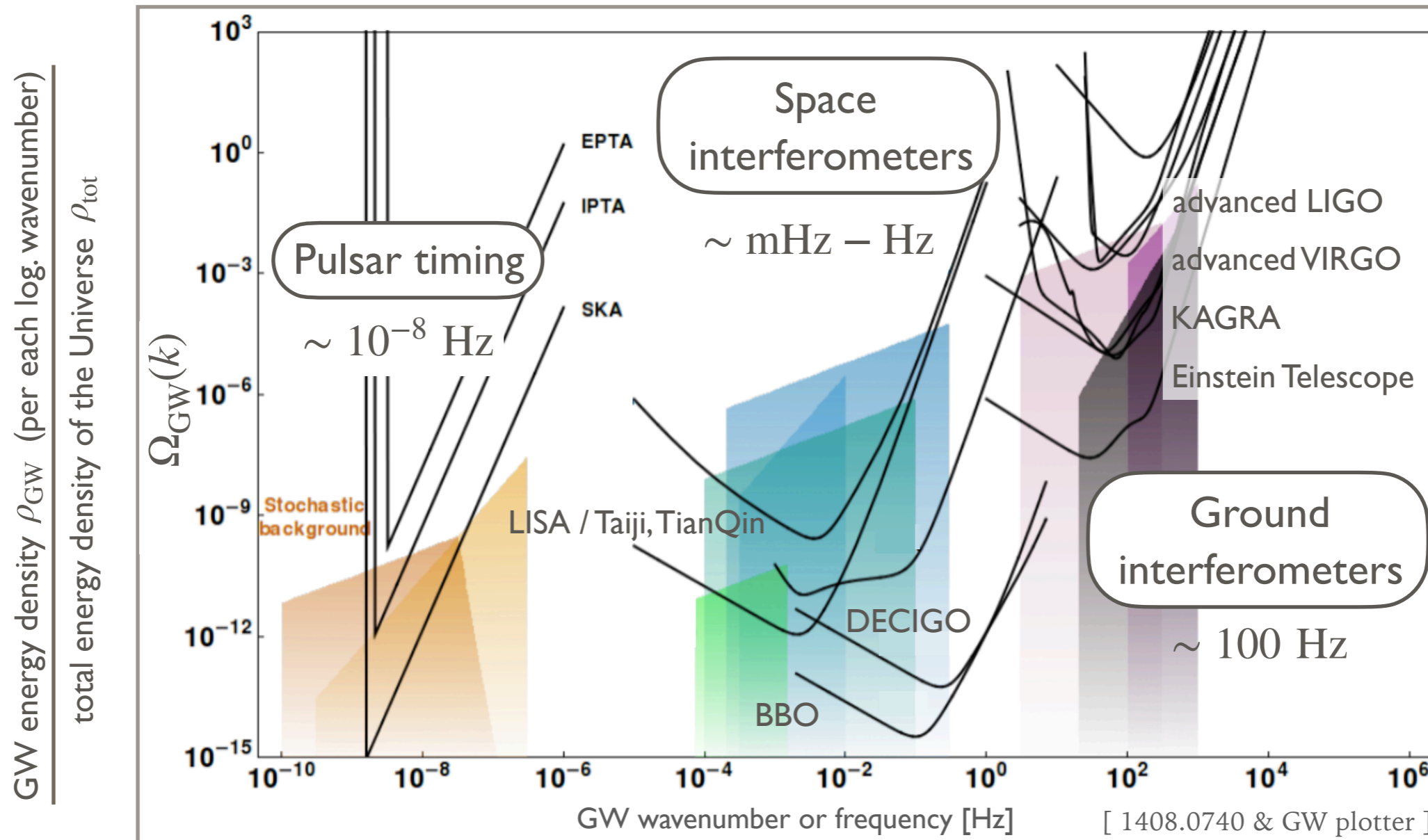


Quantum tunneling



Bubble dynamics & GW production

SUMMARY ON ONGOING/FUTURE GW OBSERVATIONS



- Time to develop robust theoretical predictions



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*Effect of
density pert.*

*Hybrid
simulation*

Intro

ANALYTICAL VS. NUMERICAL METHODS: STATE OF THE ART

from T. Konstandin's talk

(Semi-)analytical

Numerical

e.g. envelope, bulk flow, sound shell, ...

[Kosowsky, Turner, Watkins '92] [Kosowsky, Turner '93]
[Huber, Konstandin '08] [Jinno, Takimoto '17]
[Caprini, Durrer, Servant '08]
[Jinno, Takimoto '19] [Konstandin '17]
[Hindmarsh '18] [Hindmarsh, Hijazi '19]
[Lewicki, Pujolas, Vaskonen '21] [Megevand, Membiela '21] ...

[Hindmarsh, Huber, Rummukainen, Weir '13,'15,'17]
[Cutting, Hindmarsh, Weir '18,'19]
[Cutting, Escartin, Hindmarsh, Weir '20]
[Gould, Sukuvaara, Weir '21] ...

Pros.

Less cost

Better analytical understanding

Less *a priori* assumptions

More robust predictions

Cons.

Modeling = Assumptions

More cost

"Artifact" from Higgs field

(→ next slide)

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Less *a priori* assumptions
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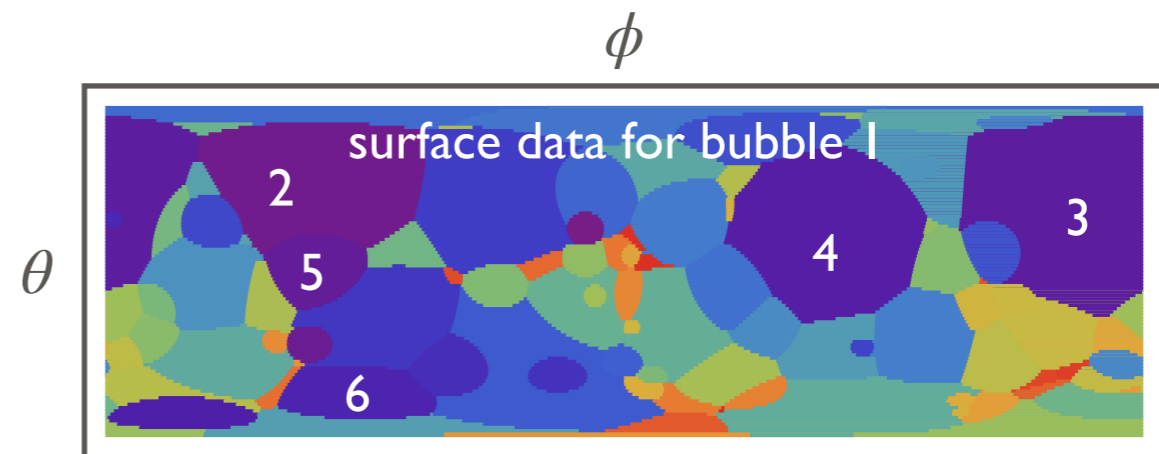
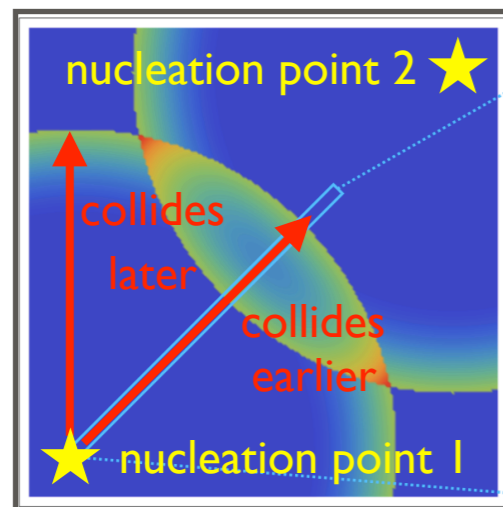
More cost
"Artifact" from Higgs field
(→ next slide)

HYBRID SIMULATION: THE IDEA

- Central idea: To get rid of the Higgs field & simulate only with fluid

Step1: Create surface data for collision time

This is possible without simulation, just from the distribution of the nucleation points (★)



surface data = when, and with which bubble each bubble fragment collides

HYBRID SIMULATION: THE IDEA

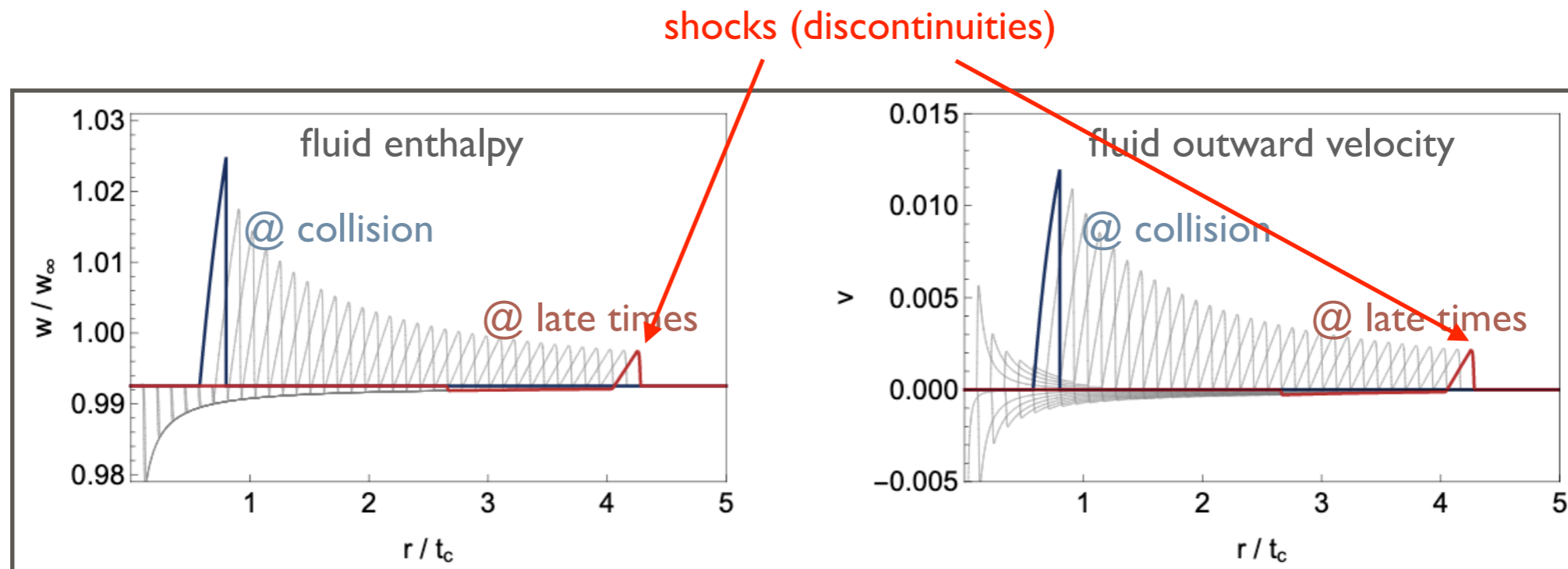
- Central idea: To get rid of the Higgs field & simulate only with fluid

Step2: Simulate radial 1d evolution after collision only with fluid

We do not need to evolve the profile before collision, since it is well known from the literature.

[Espinosa, Konstandin, No, Servant '10]

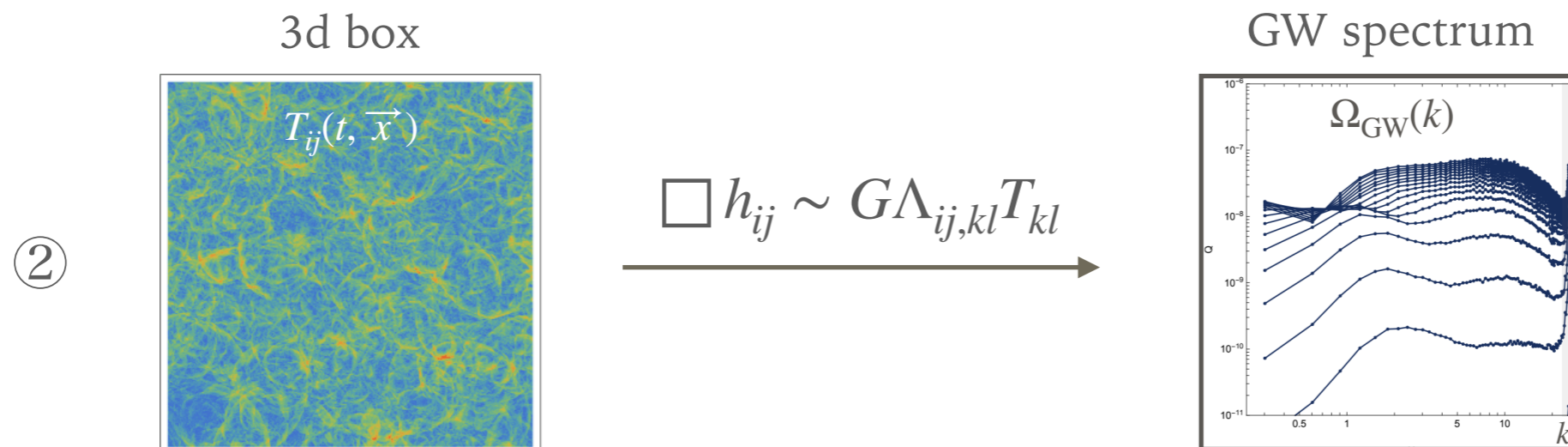
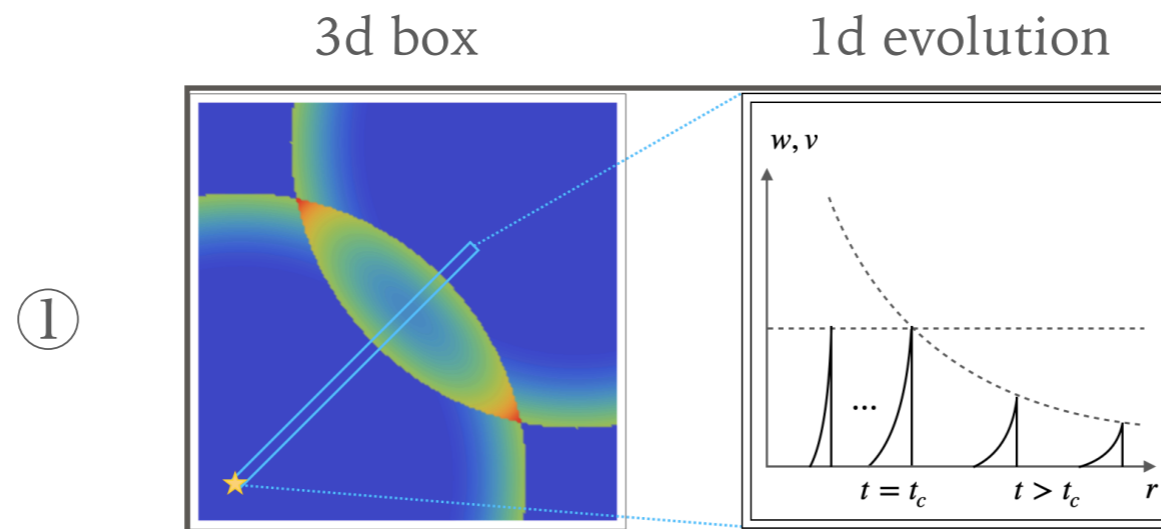
We solve the radial evolution using a shock-conserving scheme (Kurganov-Tadmor).



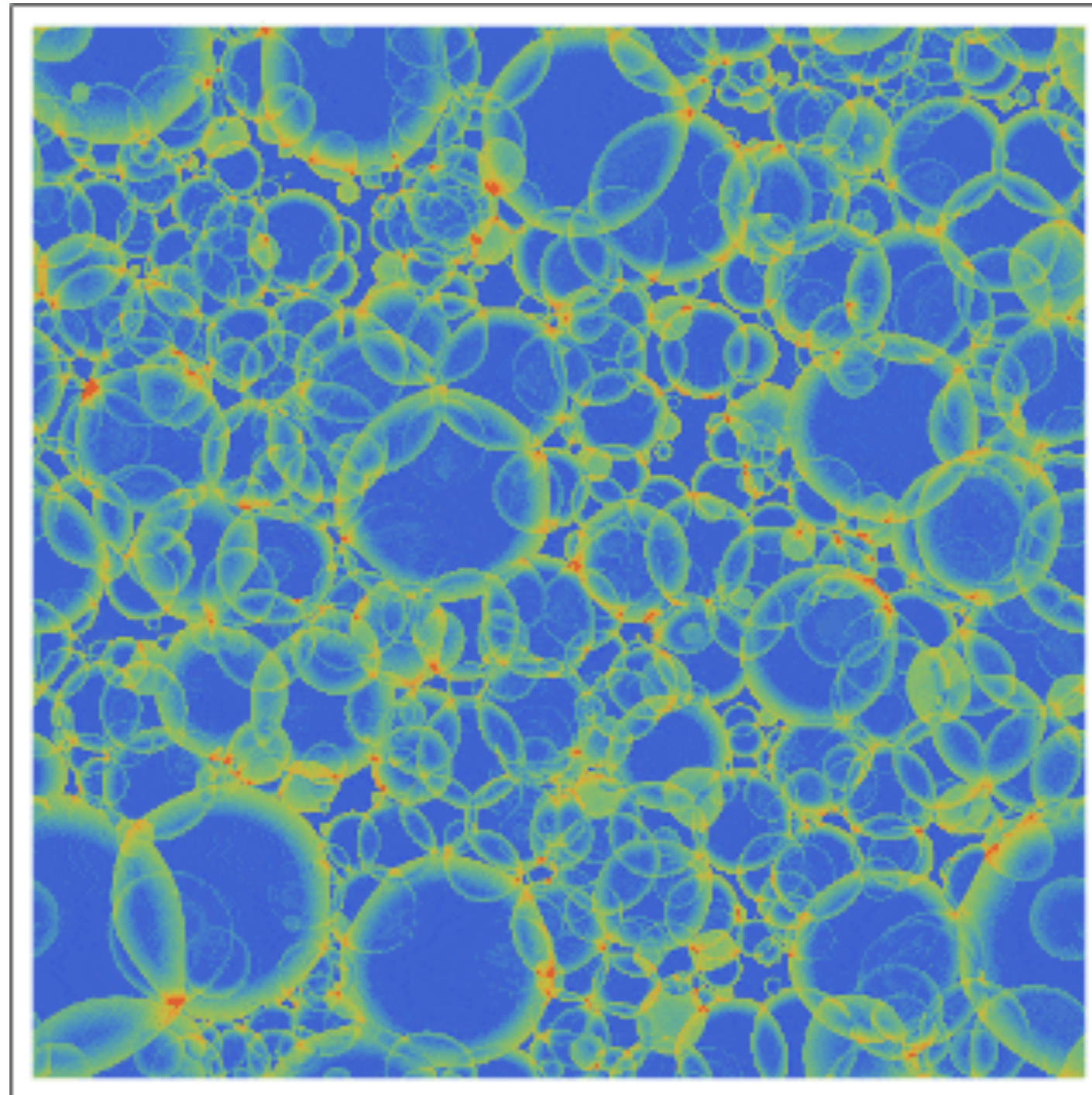
HYBRID SIMULATION: THE IDEA

- Central idea: To get rid of the Higgs field & simulate only with fluid

Step3: embed 1d back into 3d (①) and calculate GWs (②)



HYBRID SIMULATION: EXAMPLE ANIMATION



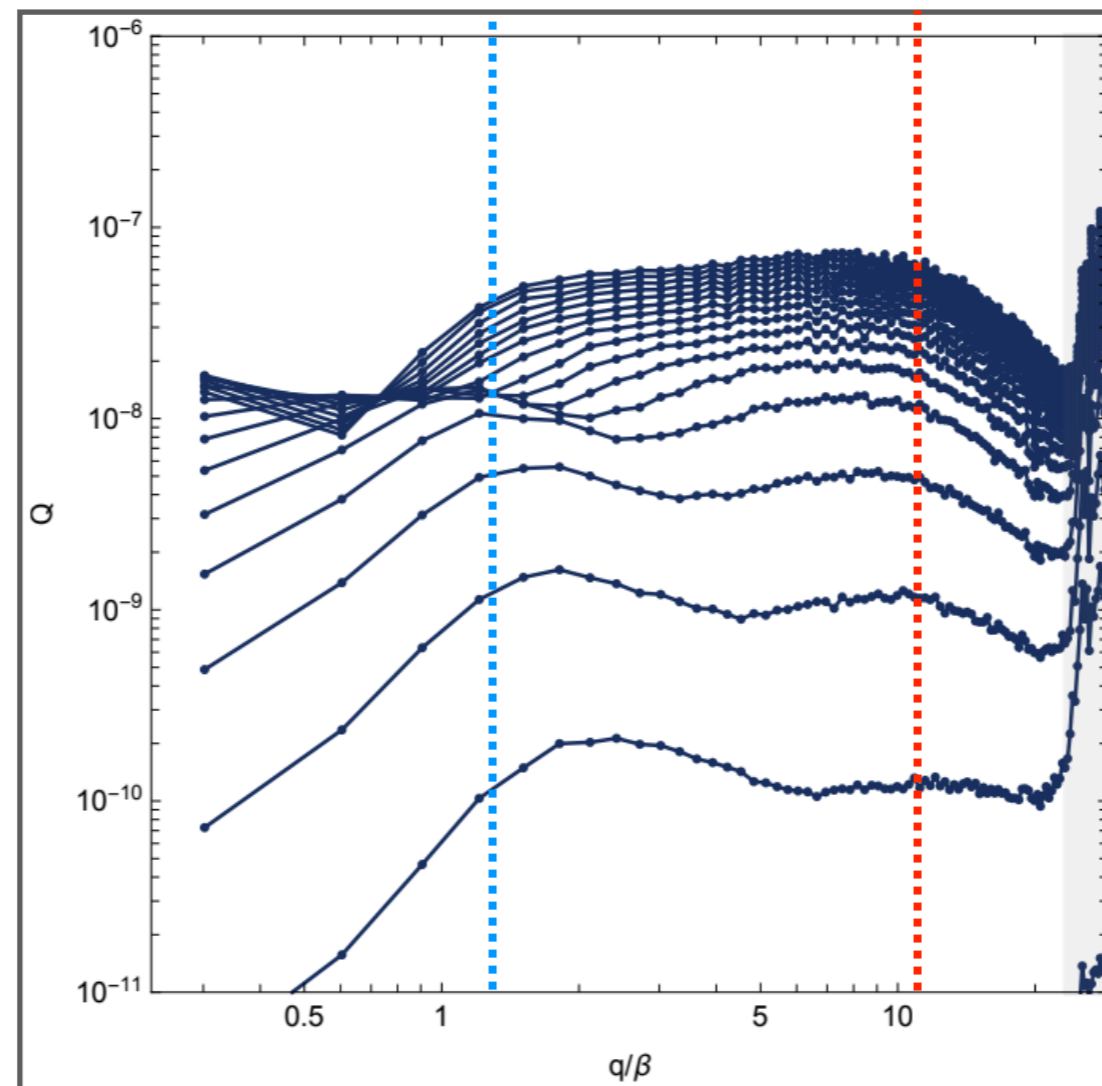
↑↓ (typical fluid shell)
↑↓ (typical bubble size)
 β^{-1}

HYBRID SIMULATION: RESULTS

$$\alpha = 0.0046, v_{\text{wall}} = 0.52$$

(typical bubble size)⁻¹ (typical fluid shell)⁻¹

GW spectrum



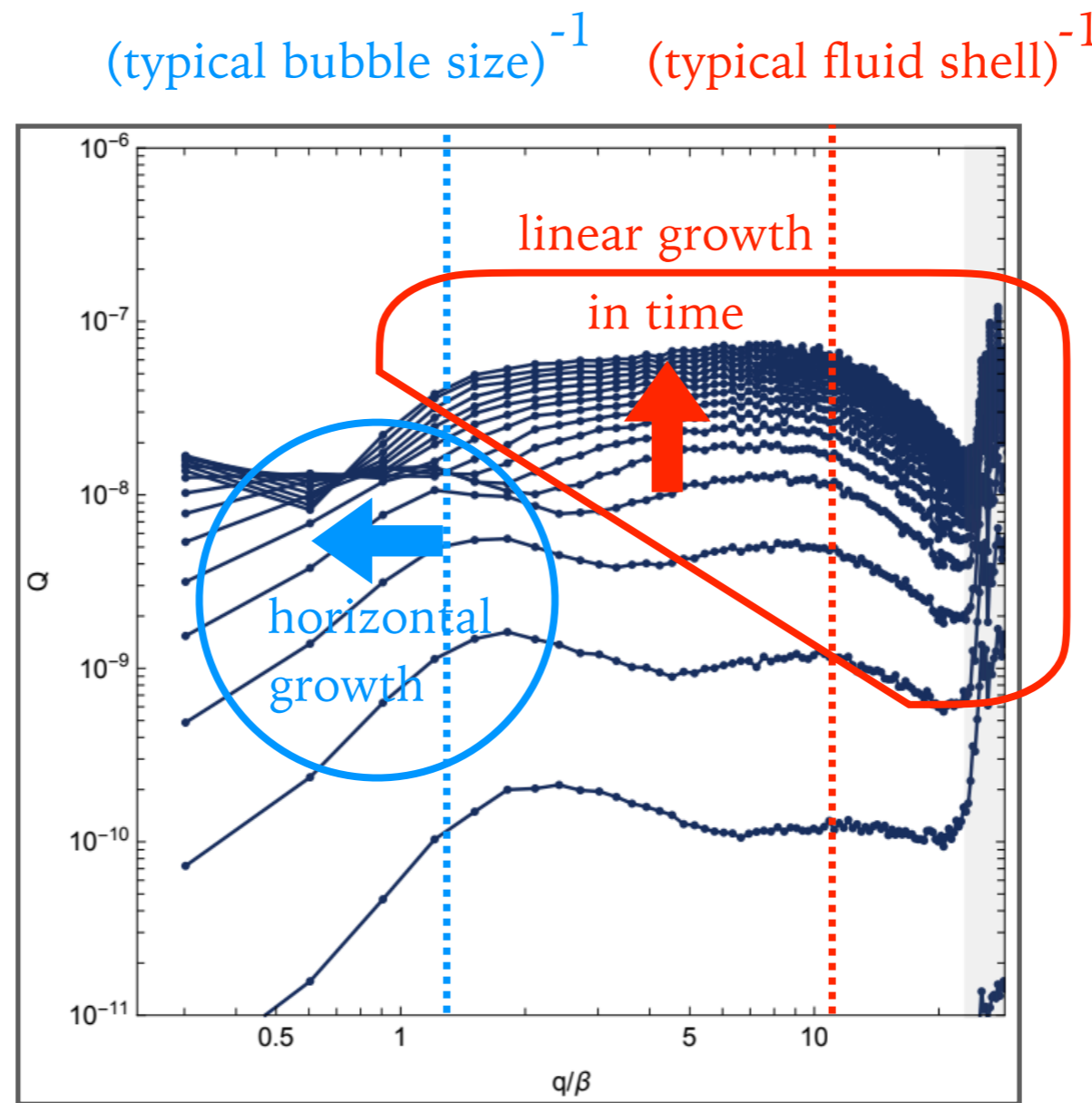
GW spectrum at
different time slices

wavenumber

HYBRID SIMULATION: RESULTS

$$\alpha = 0.0046, v_{\text{wall}} = 0.52$$

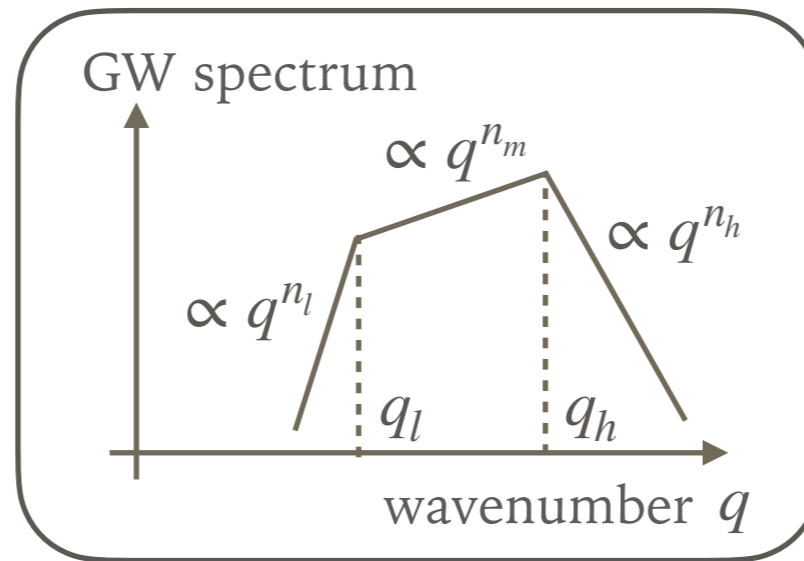
GW spectrum



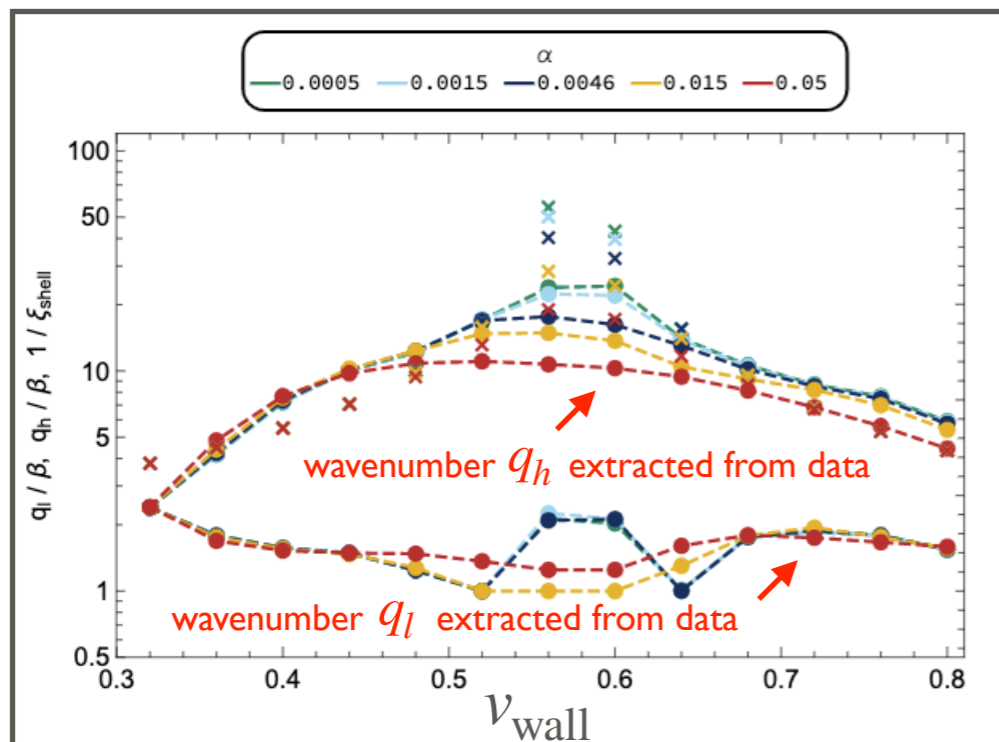
We extract this component
(\rightarrow next slide)

HYBRID SIMULATION: RESULTS

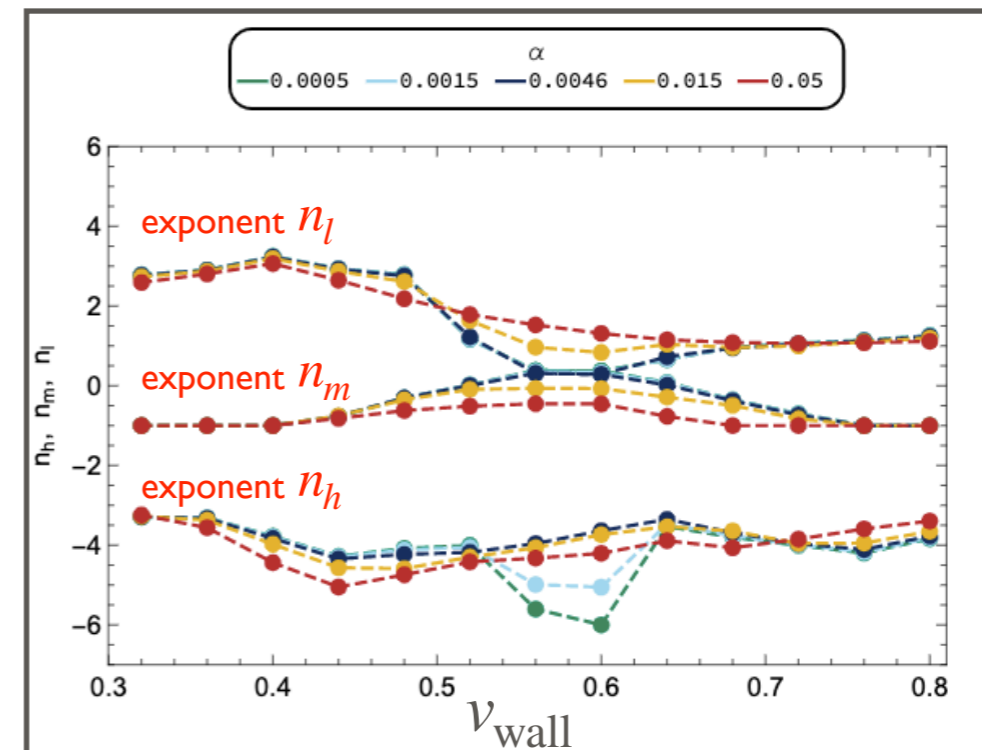
Parametrization of the GW spectrum



Characteristic wavenumber q_l, q_h



Exponents n_l, n_m, n_h





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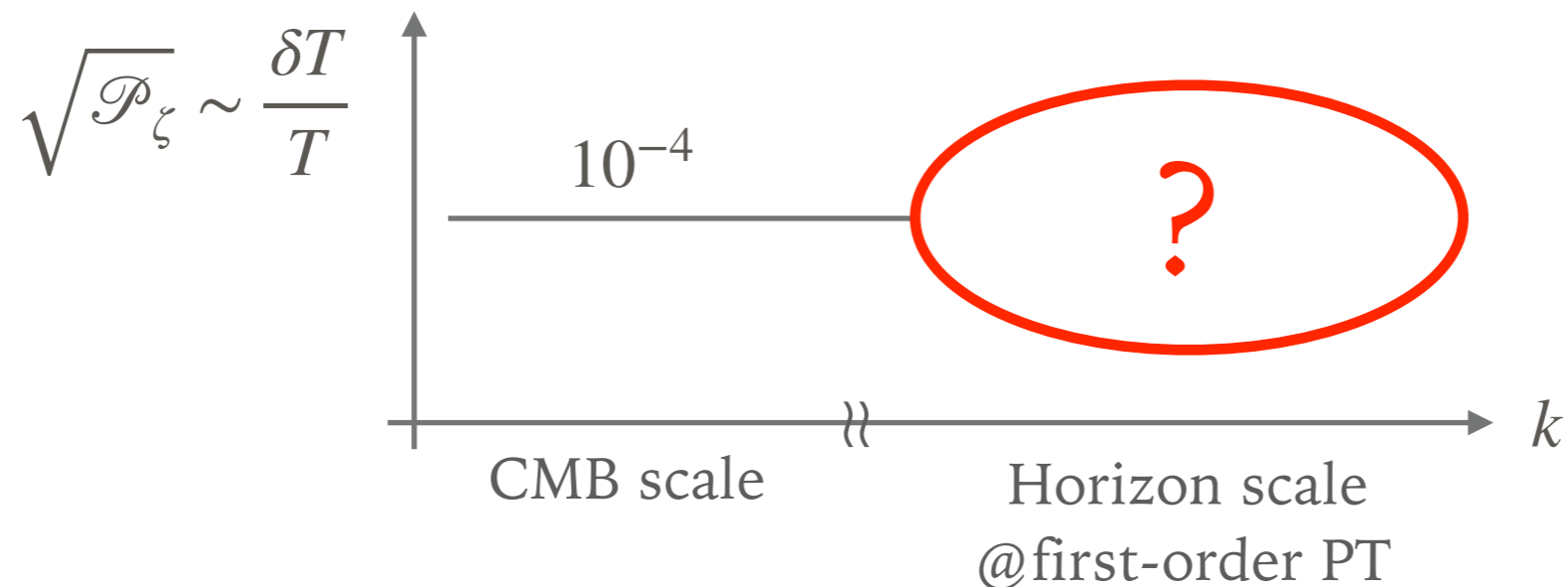
*Hybrid
simulation*

Intro

EFFECT OF DENSITY PERTURBATIONS

► Density (i.e. curvature) perturbations

- Constrained to $\zeta \sim \frac{\delta T}{T} \sim 10^{-4}$ at CMB scales
- Basically unconstrained at smaller scales (large k)



► Our interest: biased nucleation time & position from density perturbations

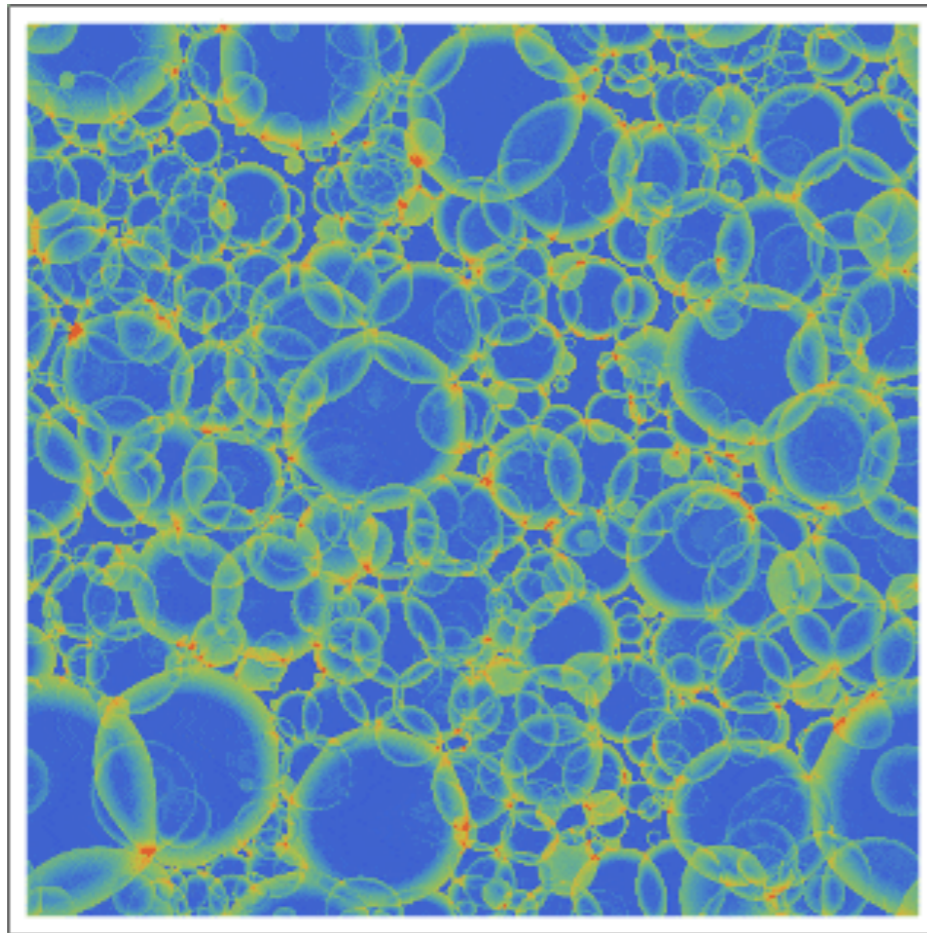
- Density perturbations work as "effective big bubbles"

Summary:

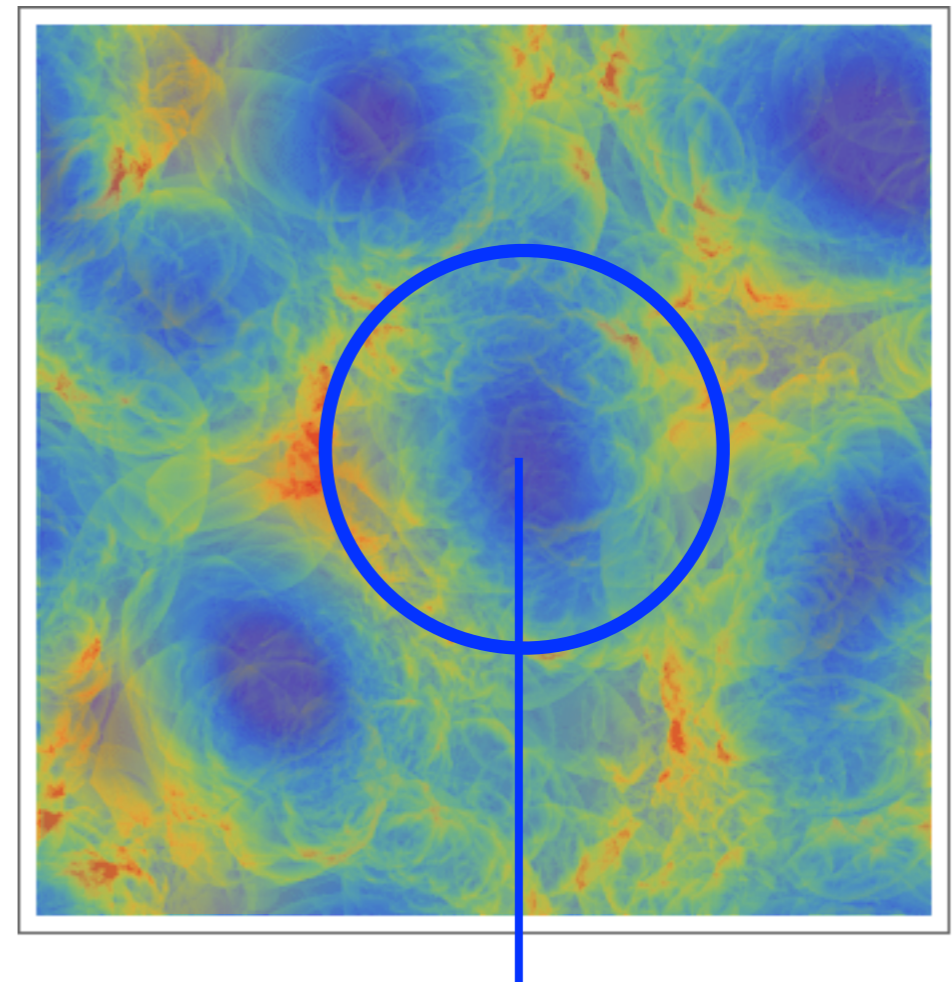
- To have interesting effects, their amplitude only needs to be $\frac{\delta T}{T} \sim \frac{H_*}{\beta} \ll 1$

CENTRAL IDEA

Without density perturbations



With density perturbations



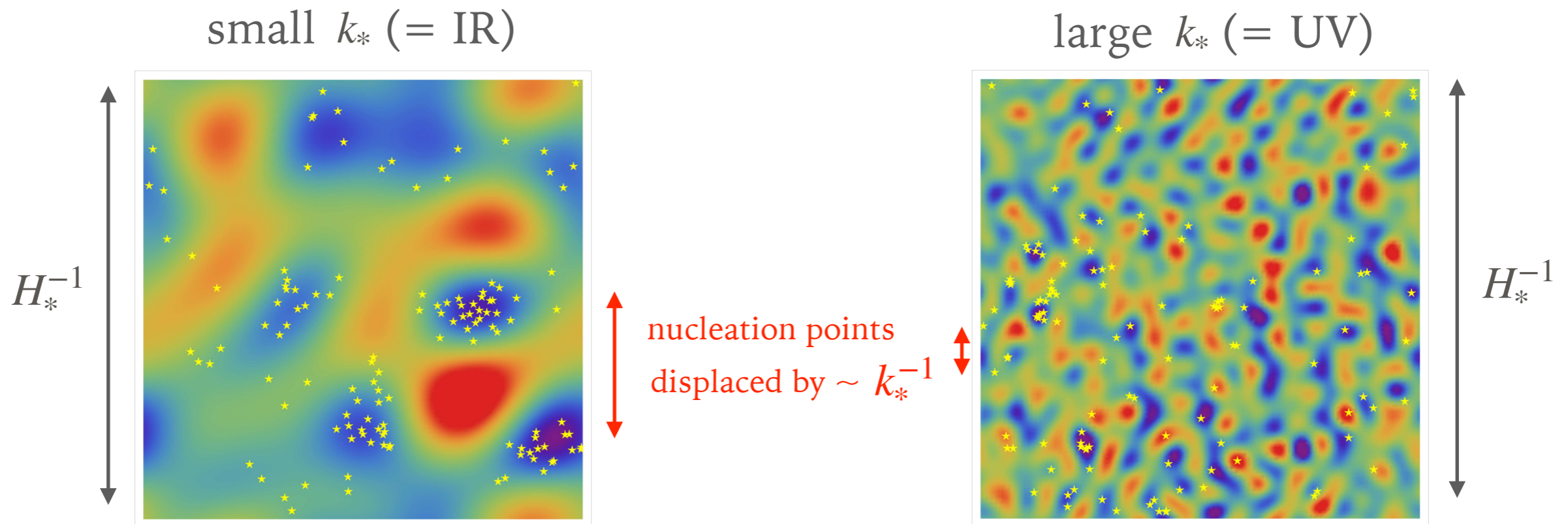
formation of "effective big bubbles"
around the cold spots

EFFECT OF DENSITY PERTURBATIONS

- Density perturbations are parameterized by two quantities

$$\left\{ \begin{array}{l} \text{typical wavenumber } k_* \rightarrow \text{see below} \\ \text{typical normalized amplitude } \sigma \sim \frac{\delta T}{T} / \frac{H_*}{\beta} \rightarrow \text{effects set in once } > 1 \end{array} \right.$$

- Dependence of the nucleation points (★) on k_*

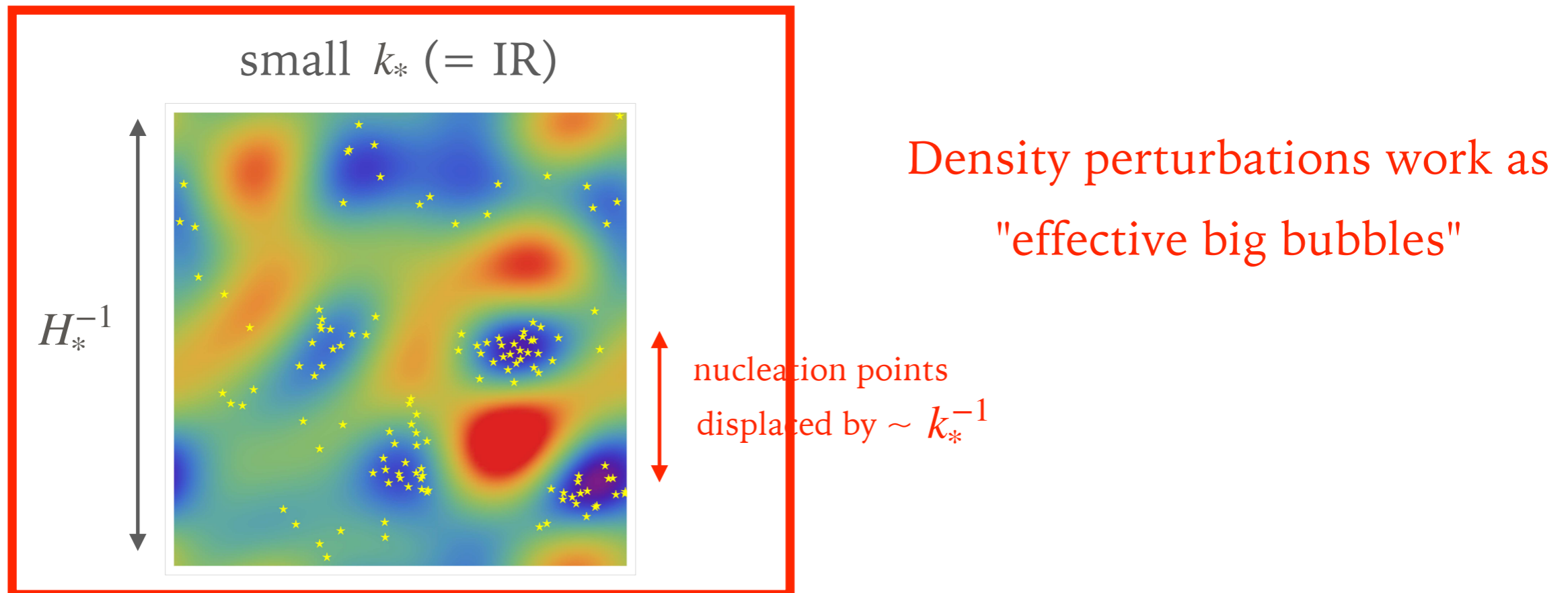


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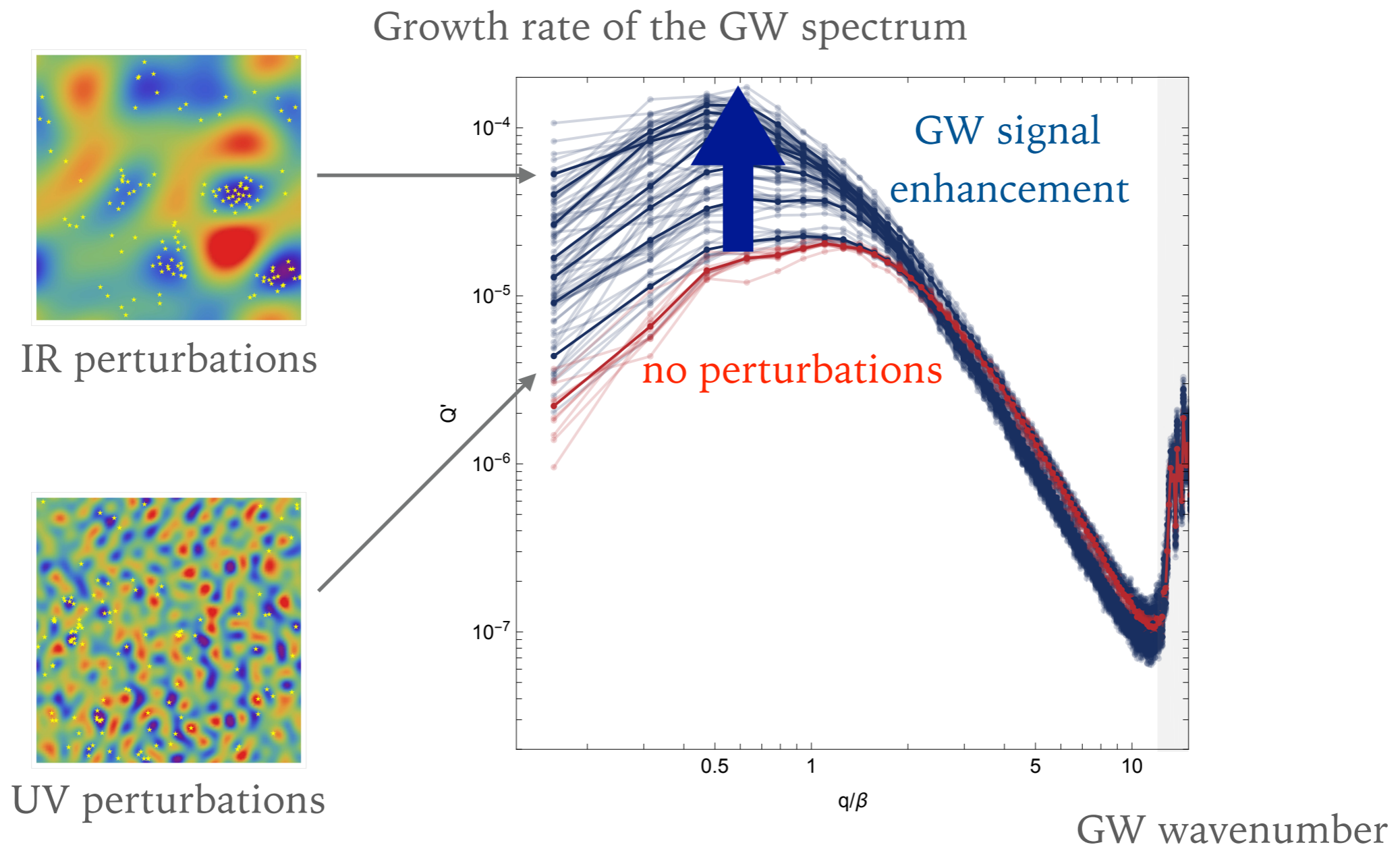
$$\left\{ \begin{array}{l} \text{typical wavenumber } k_* \rightarrow \text{see below} \\ \text{typical normalized amplitude } \sigma \sim \frac{\delta T}{T} / \frac{H_*}{\beta} \rightarrow \text{effects set in once } > 1 \end{array} \right.$$

- Dependence of the nucleation points (★) on k_*



GW ENHANCEMENT FROM DENSITY PERTURBATIONS

- Density perturbations with $H_* < k_* < \beta$ enhance the GW signal





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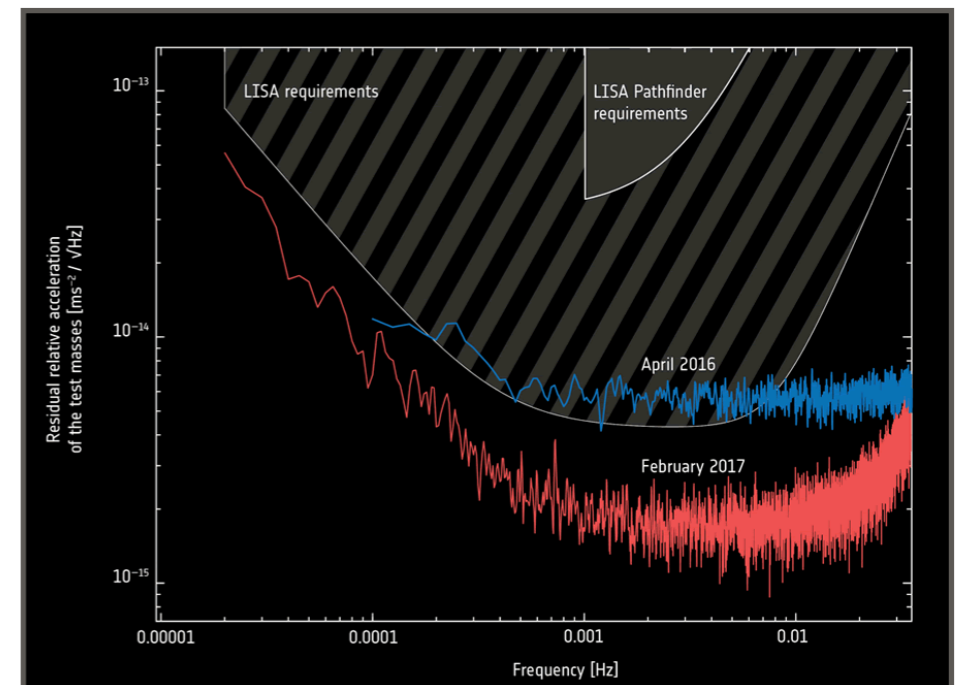
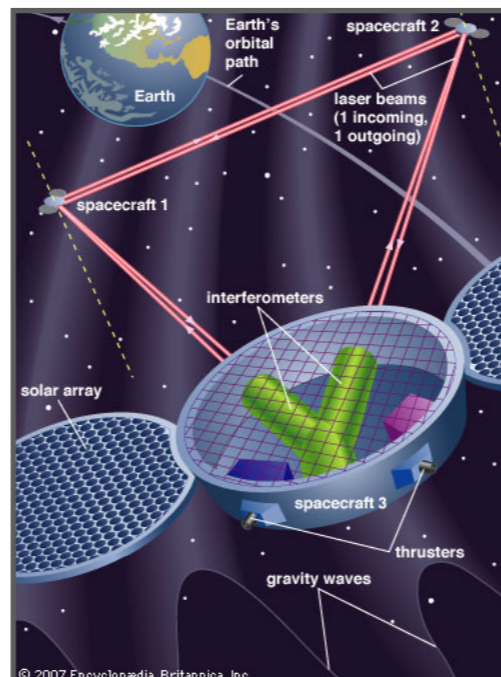
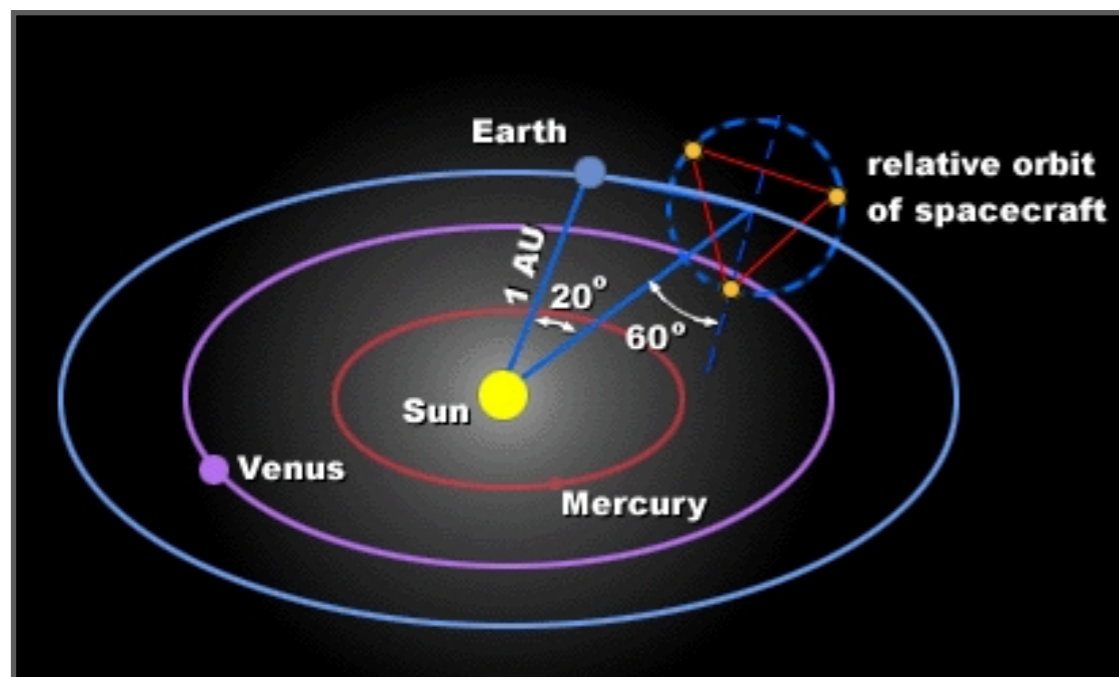
- It's time to develop analytical & numerical methods for GW predictions in first-order phase transitions
- We propose a "hybrid simulation" to get rid of the artifact from the scalar field
- We point out GW signal enhancement from density perturbations:
 - occurs for typical wavenumber $H_* < k_* < \beta$
 - amplitude $\frac{\delta T}{T} \sim \frac{H_*}{\beta} \ll 1$ is enough to have this effect

Backup

PRESENT & FUTURE OBSERVATIONS

LISA (Laser Interferometer Space Antenna)

- Space interferometer project led by ESA & NASA
- Selected as third-large class mission(L3) in 2017. Operation from 2034.
- 3 spacecrafts orbitting around the Sun. Distance btwn spacecrafts = 2.5×10^6 km.
- Tested necessary technologies with LISA pathfinder since 2015.



GW ENHANCEMENT FROM DENSITY PERTURBATIONS

