B-physics anomalies and flavor hierarchies: a natural link

Gino Isidori

[University of Zürich]

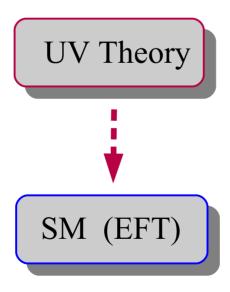
- ▶ Introduction
- ► The anomalies
- ► Effective Field Theory considerations
- From EFT to simplified models
- Speculations on ultraviolet completions
- **▶** Conclusions





Despite all its phenomenological successes, the SM has some deep unsolved problems (<u>hierarchy problem</u>, <u>flavor problem</u>, neutrino masses, dark-matter, dark energy, inflation...)

The Standard Model should be regarded as an <u>Effective Field Theory</u> (*EFT*), i.e. the limit (in the range of energies and effective couplings so far probed) of a more fundamental theory with new degrees of freedom



The most interesting hints toward UV dynamics come from possible <u>un-natural features</u> of the EFT.

UV Theory

Two types of effects in QFT:

$$\mathscr{L}_{\text{SM-EFT}} = \mathscr{L}_{\text{gauge}} + \mathscr{L}_{\text{Higgs}} + \sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} O_i^{d \ge 5}$$

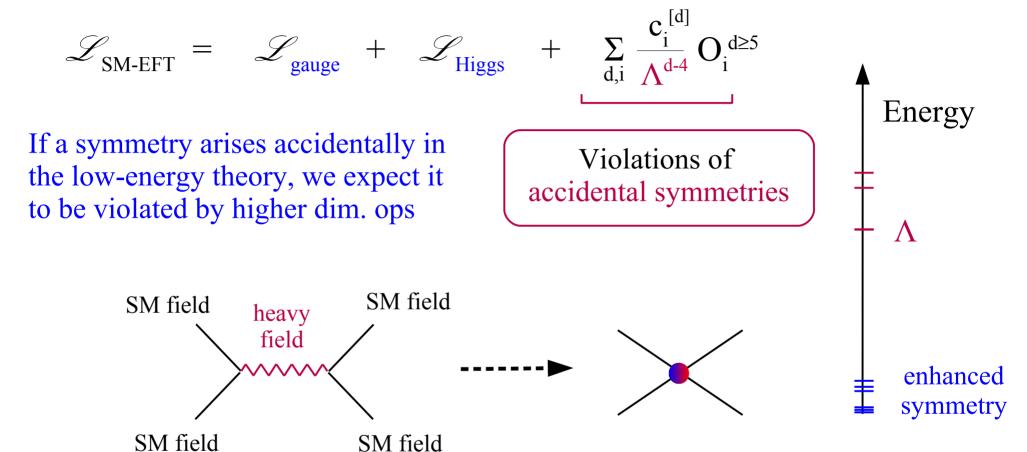
SM (EFT)

Un-natural aspects of low-energy couplings

Violations of accidental symmetries

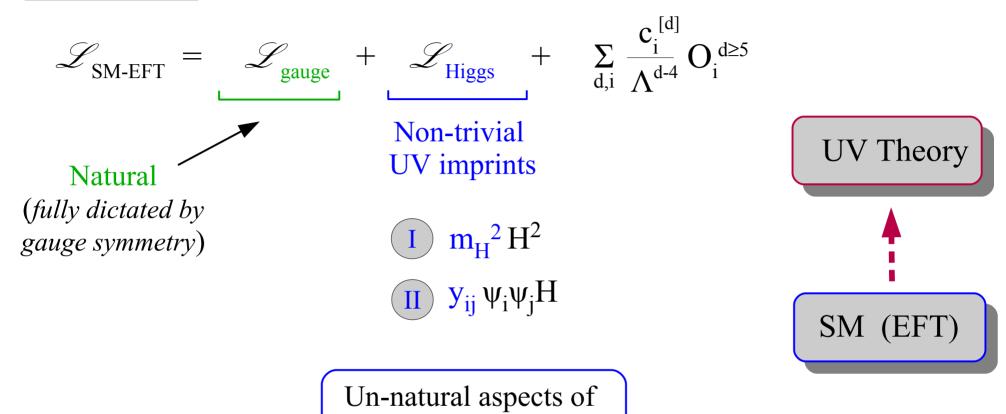
qualitative UV imprint

quantitative
UV imprint

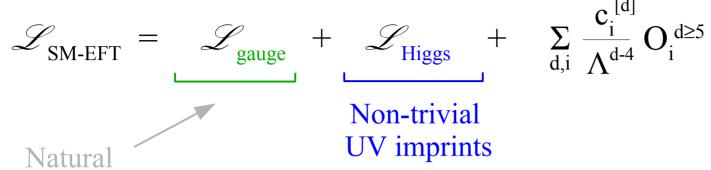


At large distances, not enough "variables" to describe the violation of the symmetry [~ multipole expansion]

The violations of Lepton Flavor Universality recently reported by experiments belong to this category



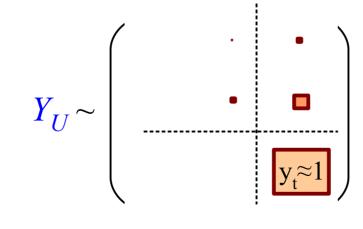
the SM couplings

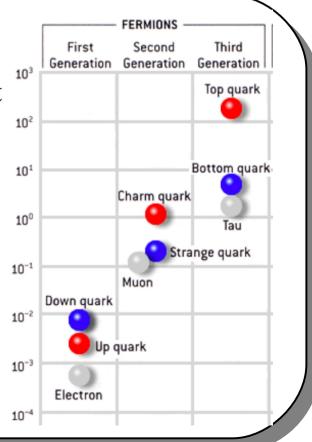


(fully dictated by gauge symmetry)

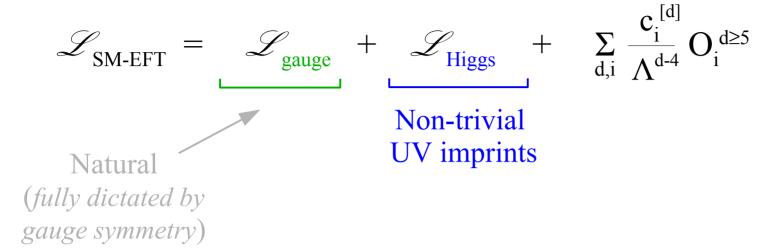
II. Flavor problem

The entries of the Yukawa couplings span <u>5 orders of magnitude</u> & do not appear at all accidental:





<u>Introduction</u>



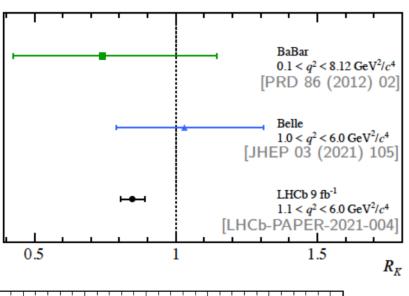
- I. Electroweak hierarchy problem
- Instability of the Higgs mass under quantum corrections
- New Physics in the TeV domain

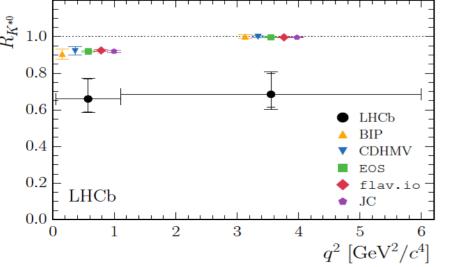
II. Flavor problem

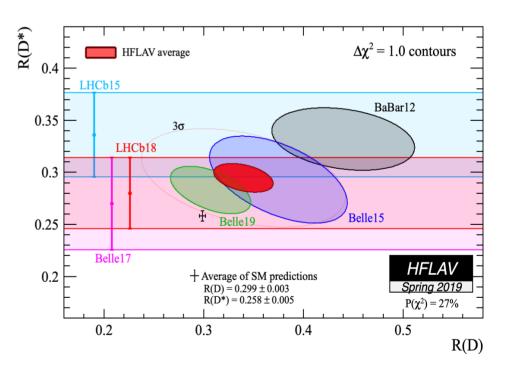
<u>Un-natural</u> hierarchies in the couplings describing fermion masses

flavor non-universal dynamics (at some energy scale)

As I will argue in the rest of this talk, the <u>violations of LFU</u> suggest to "attack" these two problems together, and not one at a time (*as often done in the past*)







Since 2013 results in semi-leptonic B decays started to exhibit tensions with the SM predictions connected to a possible violation of Lepton Flavor Universality

More precisely, we seem to observe a <u>different behavior</u> (beside pure kinematical effects) of different lepton species in the following processes:

```
• b \rightarrow s l^+l^- (neutral currents): \mu vs. e
```

• b \rightarrow c *lv* (charged currents): τ vs. light leptons (μ , e)

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More precisely, we seem to observe a <u>different behavior</u> (beside pure kinematical effects) of different lepton species in the following processes:

- b \rightarrow s l^+l^- (neutral currents): μ vs. e
- b \rightarrow c lv (charged currents): τ vs. light leptons (μ , e)

N.B: LFU is an <u>accidental symmetry</u> of the SM Lagrangian in the limit where we neglect the lepton Yukawa couplings.

LFU is <u>badly broken</u> in the Yukawa sector: $y_e \sim 3 \times 10^{-6}$, $y_\mu \sim 3 \times 10^{-4}$, $y_\tau \sim 10^{-2}$

but all the lepton Yukawa couplings are small compared to SM gauge couplings, giving rise to the (*approximate*) universality of decay amplitudes which differ only by the different lepton species involved

• b \rightarrow s l^+l^- (neutral currents)

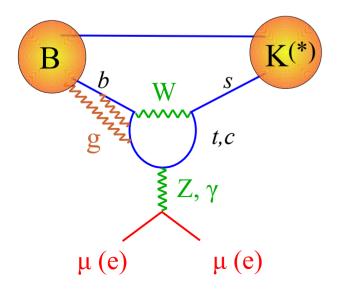
List of the observables exhibiting anomalies (= *deviations from SM*):

- → P'_5 anomaly [B \rightarrow K* $\mu\mu$ angular distribution]
- ► Smallness of all $B \to H_s \mu \mu$ rates $[H_s = K, K^*, \phi \text{ (from } B_s)]$
- ^{*} LFU ratios (μ vs. e) in B → K^{*}ℓℓ & B → K ℓℓ

• th. error <1%

→ Smallness of BR($B_s \rightarrow \mu\mu$)

th. error few %



Some of these observables are affected by irreducible theory errors (form factors + long-distance contrib.)

The recent result
$$R_K \approx \frac{\Gamma(B \to K \, \mu \mu)}{\Gamma(B \to K \, ee)} \approx 0.85 \pm 0.05$$

strengths the consistency of a picture which was already very coherent and points to New Physics of short-distance origin.

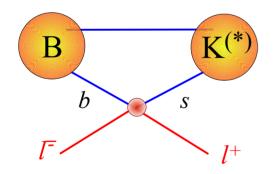
To describe $b \rightarrow sll$ decays we

- build an EFT Lagrangian
- evolve it down to $\mu \sim m_b$
- evaluate hadronic matrix elements

$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb}^* V_{ts} \sum_i C_i \mathcal{O}_i$$

FCNC operators:

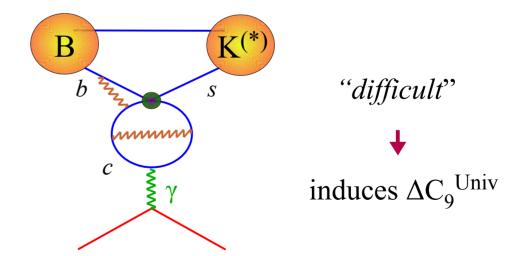
$$\mathcal{O}_{10}^{\ell} = (\bar{s}_L \gamma_{\mu} b_L) (\bar{\ell} \gamma^{\mu} \gamma_5 \ell)$$
$$\mathcal{O}_{9}^{\ell} = (\bar{s}_L \gamma_{\mu} b_L) (\bar{\ell} \gamma^{\mu} \ell)$$



"easy" & "clean"

Four-quark operators:

$$\mathcal{O}_2 = (\bar{s}_L \gamma_\mu b_L)(\bar{c}_L \gamma_\mu c_L)$$
:



N.B.: long-distance effect cannot induce LFU breaking terms (\rightarrow LFU ratios "clean") and cannot induce axial-current contributions (\rightarrow B_s \rightarrow $\mu\mu$ "clean")

The LFU ratios:

$$R_{H} = \frac{\int d\Gamma(B \to H \,\mu\mu)}{\int d\Gamma(B \to H \,ee)} \qquad (H=K, K^{*})$$

SM prediction very robust: $(R_H)=1$

[up tiny QED and lepton mass effects]

Bordone, GI, Pattori '16 GI, Nabeebascus, Zwicky '20

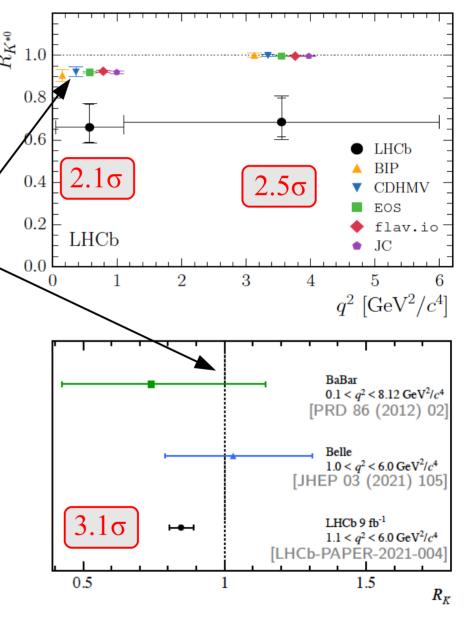
Deviations from the SM predictions ranging from 2.1 σ to 3.1 σ in each of the 3 bins measured by LHCb

$$B_s \rightarrow \mu\mu$$
:

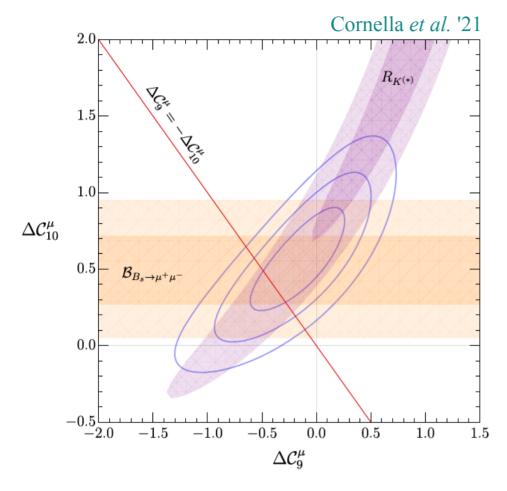
$$BR(B_s \to \mu\mu)_{SM} = (3.66\pm0.14) \times 10^{-9}$$

Beneke *et al.* '19

$$BR(B_s \to \mu\mu)_{exp} = (2.85 \pm 0.32) \times 10^{-9}$$

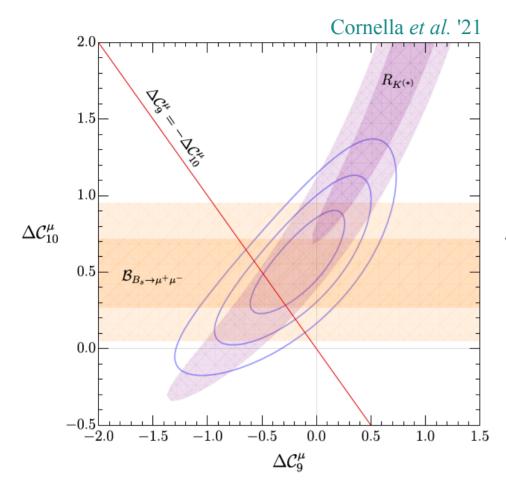


2.3σ



Conservative fit using "clean obs." only [$\Delta C_i^{\mu} = C_i^{\mu} - C_i^{e}$]:

significance of NP hypothesis $\Delta C_9^{\mu} = -\Delta C_{10}^{\mu}$ vs. SM

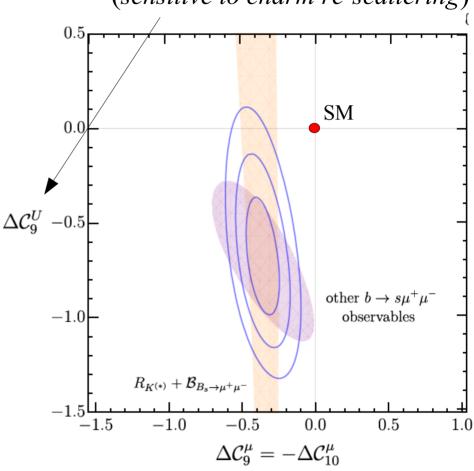


Conservative fit using "clean obs." only [$\Delta C_i^{\mu} = C_i^{\mu} - C_i^{e}$]:

significance of NP hypothesis 4.6σ $\Delta C_0^{\mu} = -\Delta C_{10}^{\mu}$ vs. SM

Lepton-universal shift to C₉

(sensitive to charm re-scattering)

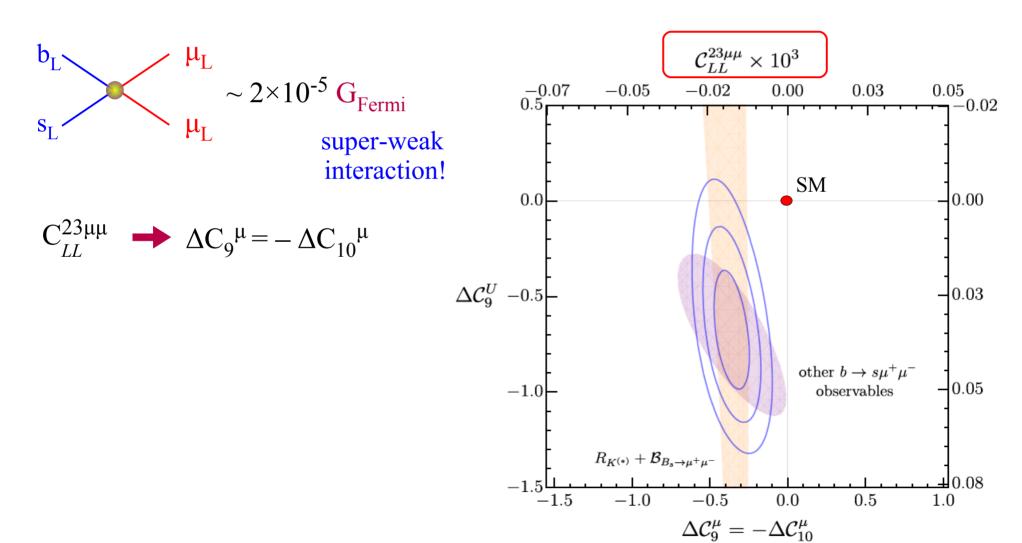


Alguero et al. '19 with current best estimate of charm contrib Ciuchini et al. '20 Li-Sheng Geng et al. '21 Altmanshofer & Stangl '21

4σ *global significance* of NP Lancierini, GI, (very conserv. estimate) Owen, Serra, '21

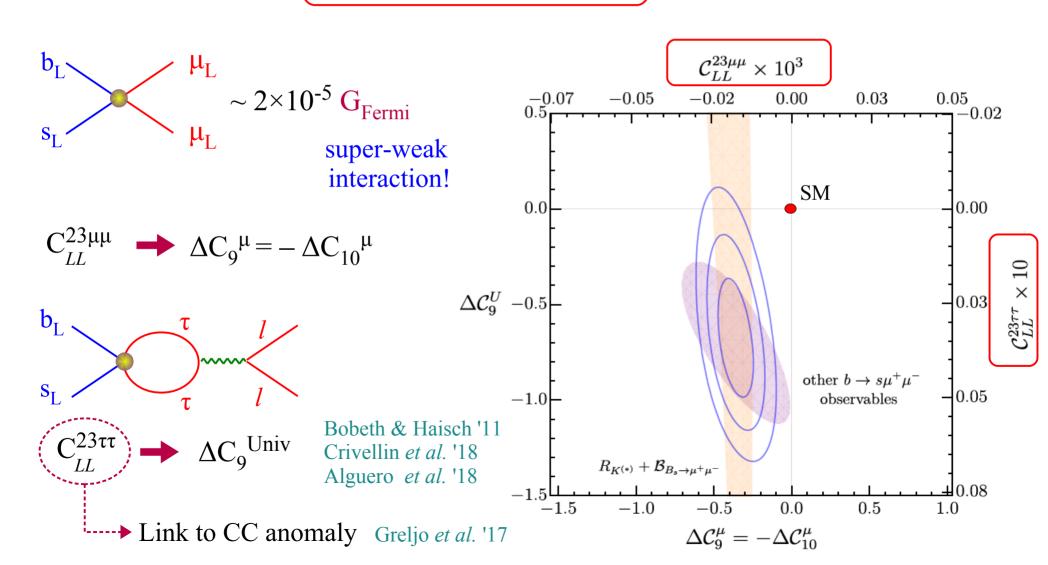
Data point to (short-distance) NP effects in operators of the type

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha)(\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$



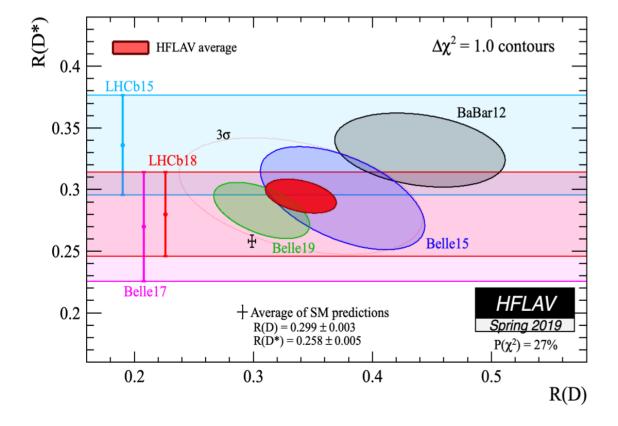
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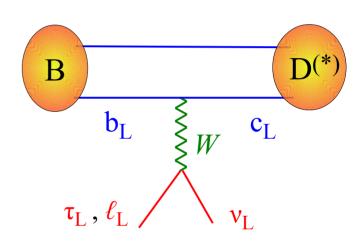
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• b \rightarrow c lv (charged currents): τ vs. light leptons (μ , e)

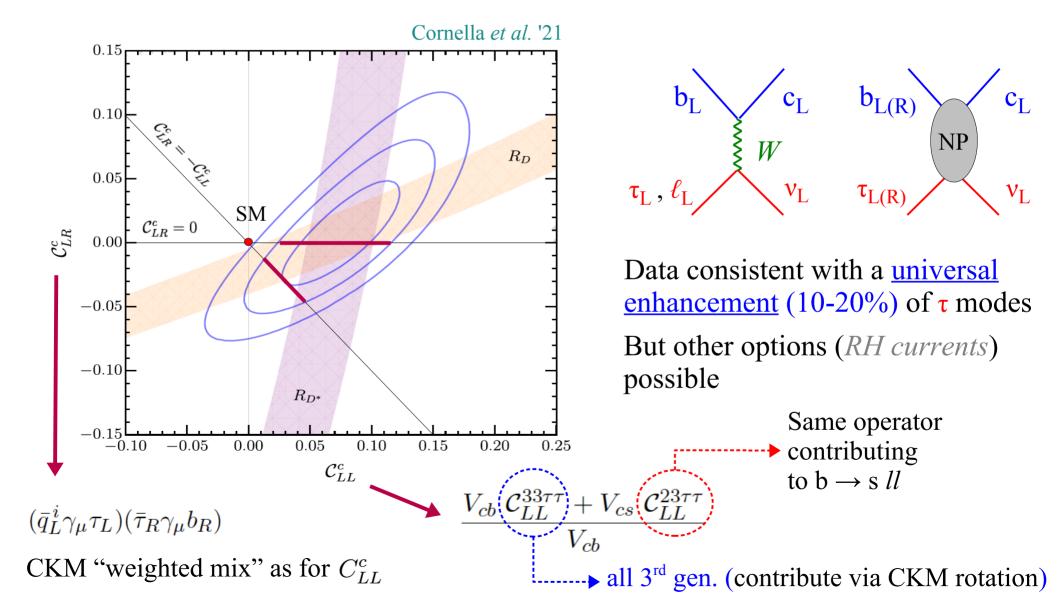
$$R(X) = \frac{\Gamma(B \to X \tau \bar{\nu})}{\Gamma(B \to X \ell \bar{\nu})}$$
 $X = D \text{ or } D^*$



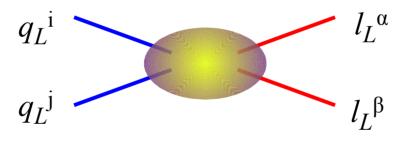


- Consistent results by three different exps. $\sim 3.1\sigma$ excess over SM (*D* and *D** combined)
- SM predictions quite "clean": hadronic uncertainties cancel (to large extent) in the ratios

• b \rightarrow c lv (charged currents): τ vs. light leptons (μ , e)

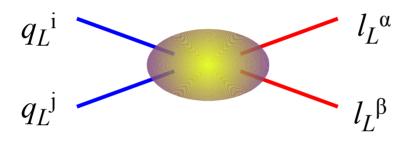


EFT considerations



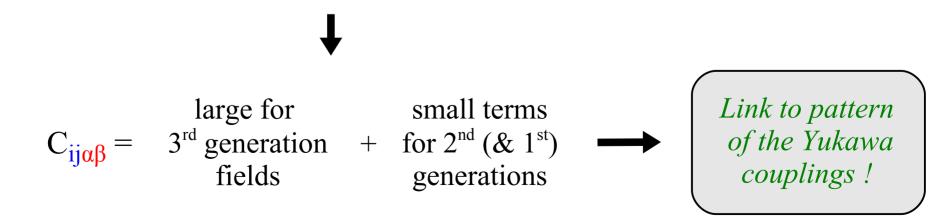
EFT considerations

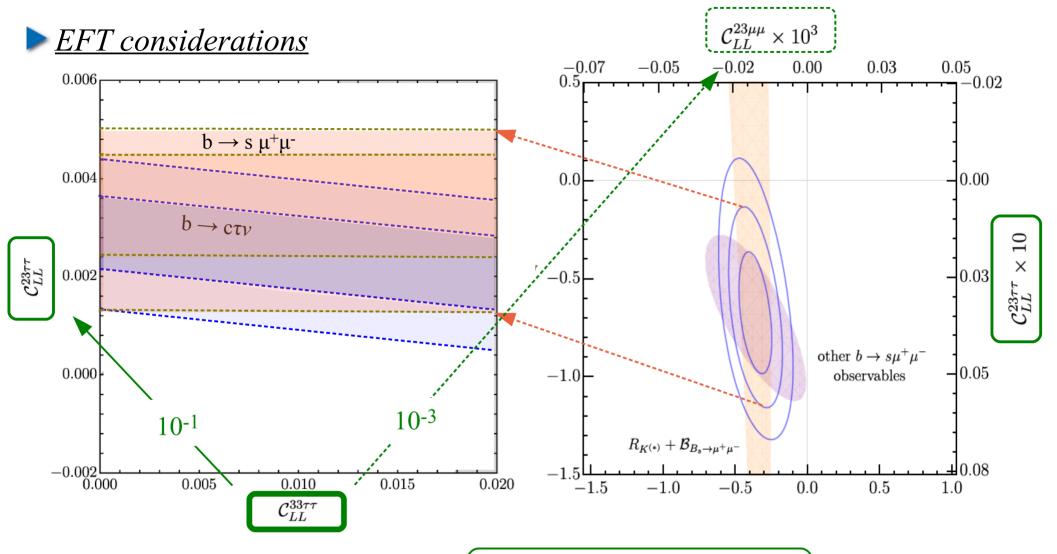
- Anomalies are seen only in semi-leptonic (quark×lepton) operators
- We definitely need non-vanishing <u>left-handed</u> current-current operators although other contributions are also possible



Bhattacharya *et al.* '14 Alonso, Grinstein, Camalich '15 Greljo, GI, Marzocca '15 (+many others...)

- Large coupling [competing with SM tree-level] in $bc \rightarrow l_3 v_3$ [R_D, R_{D*}]
- Small coupling [competing with SM loop-level] in $bs \rightarrow l_2 l_2$ [R_K, R_{K*}, ...]





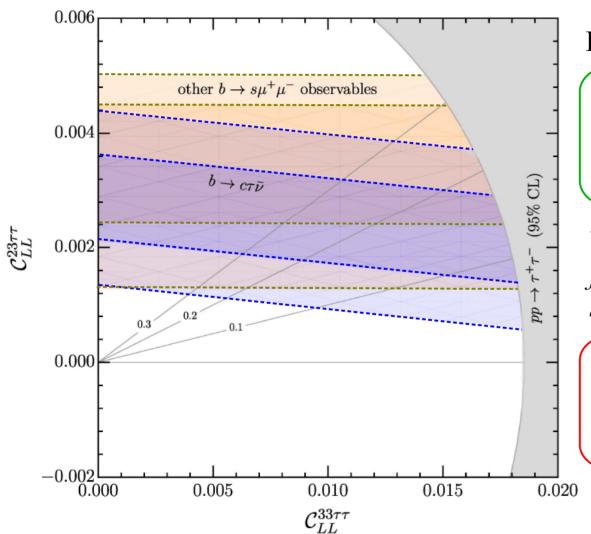
Pattern emerging from data:

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha)(\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$

- **∨** O(10⁻¹) suppress. for each 2nd gen. q_L or l_L [recall $|V_{ts}| \sim 0.4 \times 10^{-1}$]
- ▼ Nice consistency among the 2 sets of anomalies

EFT considerations

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha)(\bar{\ell}_L^\beta \gamma_\mu q_L^j) = \frac{1}{2} \left[\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)} \right]^{ij\alpha\beta}$$



Pattern emerging from data:

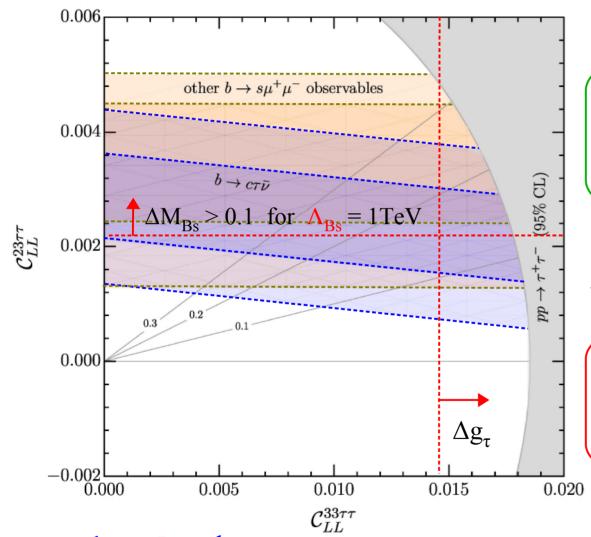
- $ightharpoonup O(10^{-1})$ for each 2^{nd} gen. q_L or l_L
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What we do <u>not</u> see (seem to call for an additional ~ loop suppression):

- * Four-quarks ($\Delta F=2$)
- ***** Four-leptons $(\tau \rightarrow \mu \nu \nu)$
- * Semi-leptonic $O^{(1-3)}$ (b \rightarrow svv)

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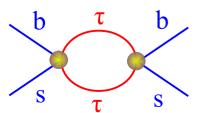


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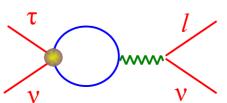
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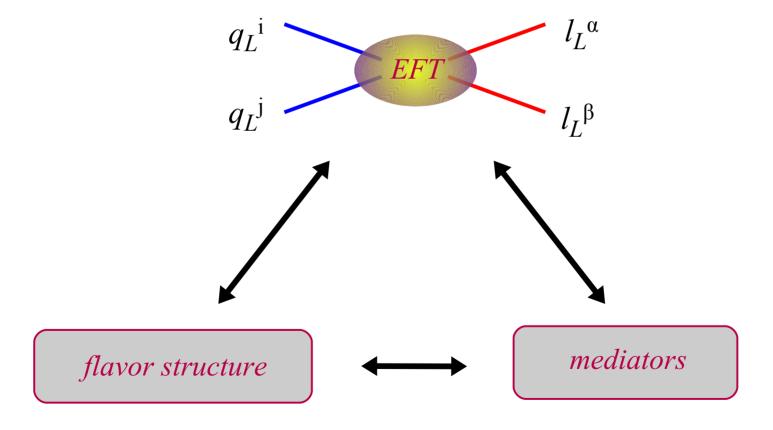


 $\Delta M_{\rm Bs} \sim (C^{23\tau\tau})^2 \Lambda_{\rm Bs}^2$



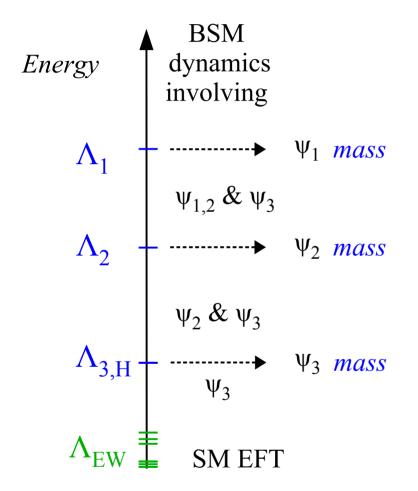
 $\Delta g_{\tau} \sim (C^{33\tau\tau}) \log(\Lambda/m_{t})$

From EFT to simplified models



From EFT to simplified models [the flavor structure]

Multi-scale picture @ origin of flavor:



Barbieri '21
Allwicher, GI, Thomsen '20
:
Bordone *et al.* '17
Panico & Pomarol '16
:
Dvali & Shifman '00

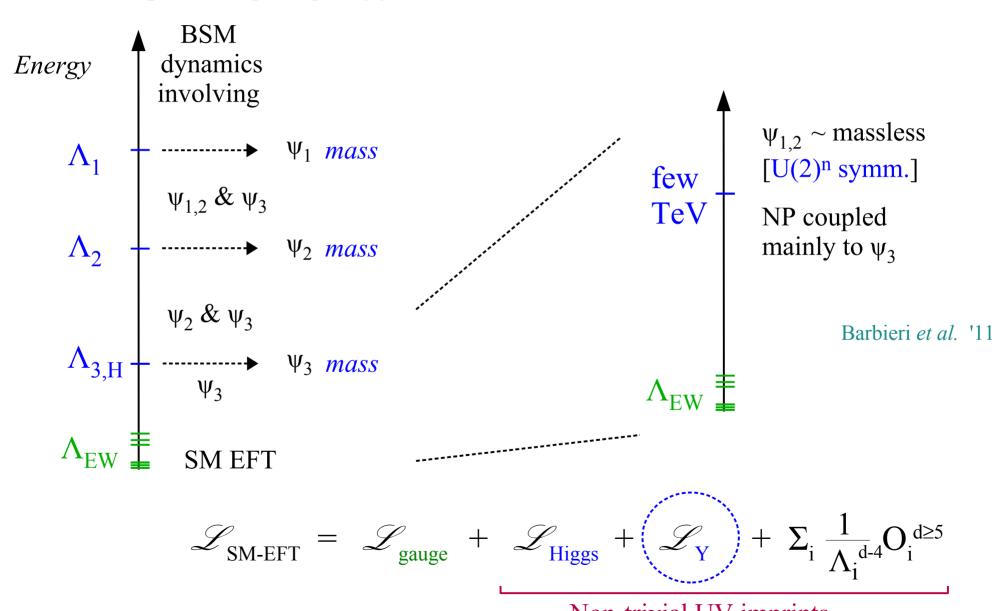
Main idea:

- Flavor non-universal interactions already at the TeV scale:
- 1st & 2nd gen. have small masses because they are coupled to NP at heavier scales

3 gen. = "identical copies" up to high energies

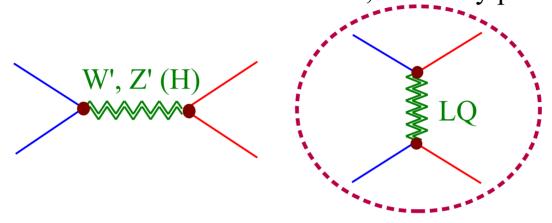
From EFT to simplified models [the flavor structure]

Multi-scale picture @ origin of flavor:

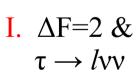


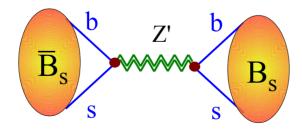
Non-trivial UV imprints

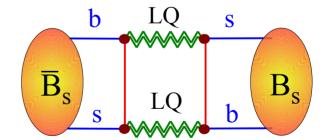
Which mediators can generate the effective operators required for by the EFT fit? If we restrict the attention to tree-level mediators, not many possibilities...



LQ (both scalar and vectors) have two general <u>strong advantages</u> with respect to the other mediators:





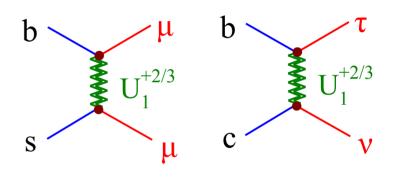


II. Direct searches:

 3^{rd} gen. LQ are also in better shape as far as direct searches are concerned (*contrary to Z'...*).

Which LQ explains which anomaly?

	Model	$R_{K^{(*)}}$	$R_{D(*)}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
Vector Scalars	$S_1 = (3, 1)_{-1/3}$	X	✓	X
	$R_2 = (3, 2)_{7/6}$	X	✓	×
	$\widetilde{R}_2=(3,2)_{1/6}$	X	×	×
	$S_3 = (3, 3)_{-1/3}$	✓	×	×
	$U_1=({f 3},{f 1})_{2/3}$	✓	✓	✓
	$\sigma U_3 = (3,3)_{2/3}$	✓	X	×



Angelescu, Becirevic, DAF, Sumensari [1808.08179]

Barbieri, GI, Pattori, Senia '15

- → mediator: U₁
- flavor structure: U(2)ⁿ

approx. flavor symmetry ensuring a CKM-like mixing 3rd → 1st, 2nd gen.

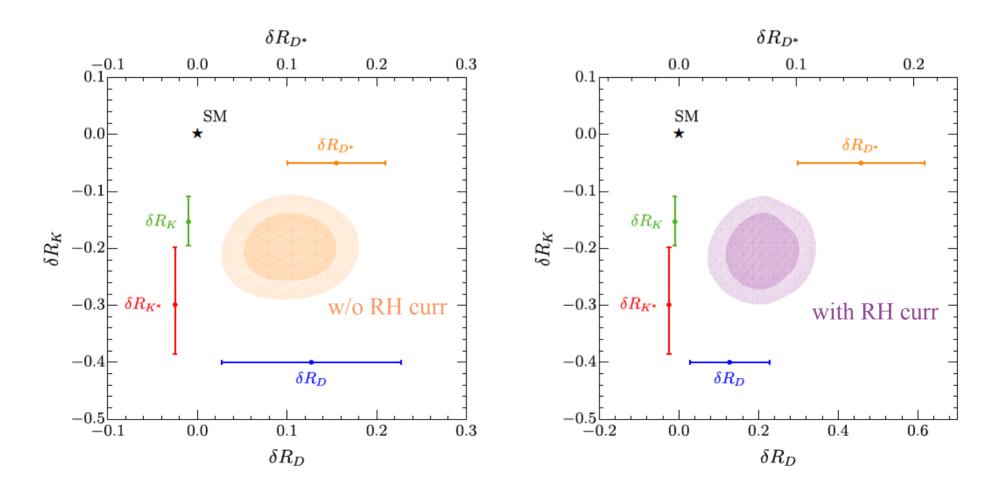
LQ of the Pati-Salam gauge group:

$$SU(4) \times SU(2)_L \times SU(2)_R$$

Considering the U₁ only

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^{\mu} \left[\beta_{i\alpha}^L (\bar{q}_L^i \gamma_{\mu} \mathcal{E}_L^{\alpha}) - \beta_{i\alpha}^R (\bar{d}_R^i \gamma_{\mu} e_R^{\alpha}) \right] + \text{h.c.}$$

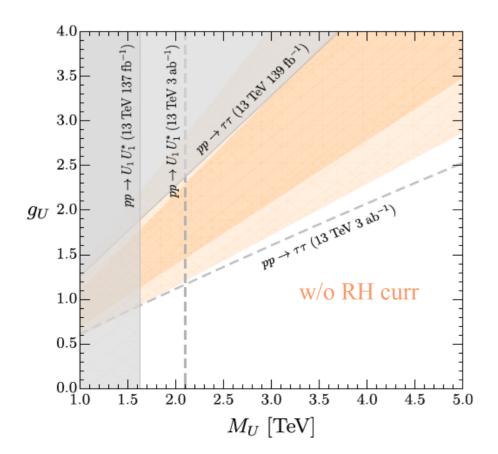
and fitting all low-energy data leads to an excellent description of present data:

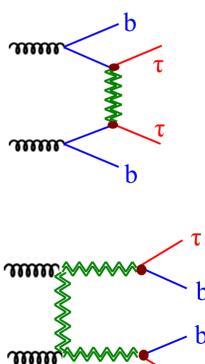


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and fitting <u>all low-energy data</u> leads to an excellent description of present data which is fully <u>consistent with high-pT searches</u> [within the reach of HL-LHC]:

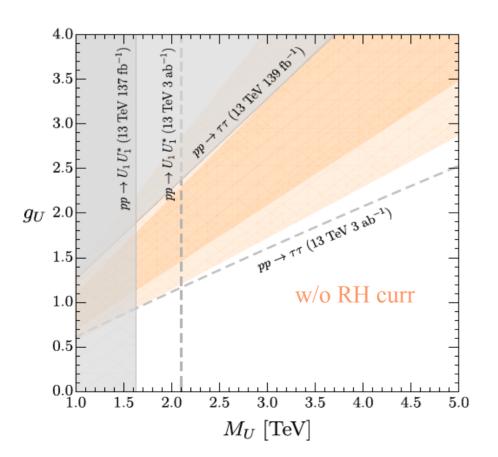




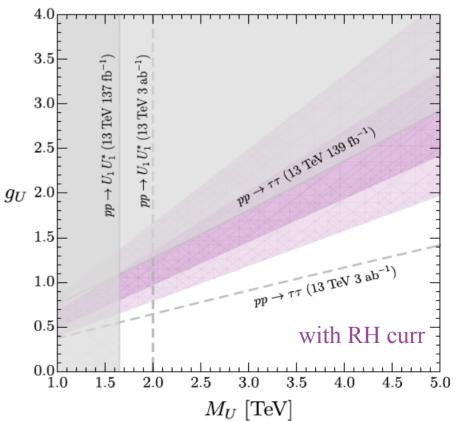
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Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21

and fitting <u>all low-energy data</u> leads to an excellent description of present data which is fully <u>consistent with high-pT searches</u>, and has interesting implications for future low-energy searches:

 10^{-6} Excluded at 95% CL Excluded at 95% CL 10^{-3} 10^{-7} 10^{-8} Belle II (50 ab^{-1}) Belle II (50 ab^{-1}) 10^{-9} 10^{-11} 10^{-6} with RH curr 10^{-12} W/o RH curr 0.10 0.15 10^{-4} 0.00 0.05 0.20 δR_{D^*} $\mathcal{B}(B_s \to \tau^- \mu^+)$



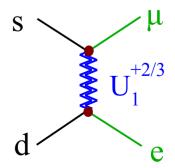
First observation: the Pati & Salam group, proposed in the 70's to unify quarks & leptons predicts the <u>only massive LQ</u> that is a good mediator for <u>both</u> anomalies:

Pati-Salam group: $SU(4)\times SU(2)_L\times SU(2)_R$

The problem of the "original PS model" are the strong bounds on the LQ couplings to 1st & 2nd generations [e.g. M > 200 TeV from $K_L \rightarrow \mu e$]

Attempts to solve this problem simply adding
extra fermions or scalars

Calibbi, Crivellin, Li, '17;
Fornal, Gadam, Grinstein, '18
Heeck, Teresi, '18



Second observation: we can "protect" the light families charging under SU(4) only the 3rd gen. or, more generally, "separating" the universal SU(3) component

PS group:
$$SU(4) \times SU(2)_L \times SU(2)_R \qquad \bullet \text{ flavor universality}$$

$$4321 \text{ models:} \qquad SU(4) \times SU(3) \times G_{EW} = \begin{bmatrix} SU(2)_L \times SU(2)_R \\ SU(2)_L \times U(1)_Y \end{bmatrix}$$

$$SU(4) \times SU(3) \times G_{EW} = \begin{bmatrix} SU(2)_L \times SU(2)_R \\ SU(2)_L \times U(1)_Y \end{bmatrix}$$

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Second observation: we can "protect" the light families charging under SU(4) only the 3rd gen. or, more generally, "separating" the universal SU(3) component

PS group:
$$SU(4) \times SU(2)_{L} \times SU(2)_{R} \qquad \bullet \text{ flavor universality}$$

$$4321 \text{ models:} \qquad SU(4) \times SU(3) \times G_{EW} = \begin{cases} SU(2)_{L} \times SU(2)_{R} \\ SU(2)_{L} \times U(1)_{Y} \end{cases}$$

• Non-universality via mixing

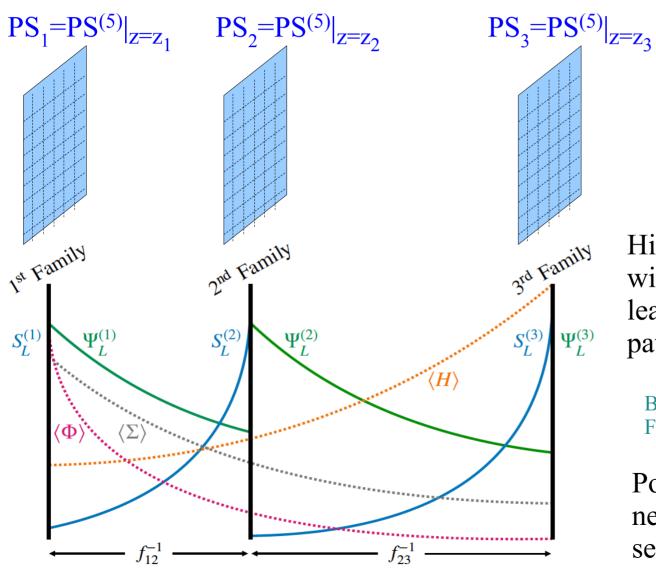
$$SU(4)\times SU(3)$$

$$SU(4)_3 \times SU(3)_{1,2}$$

• Accidental U(2)⁵ flavor symm. in the gauge sect.

Fuentes-Martin *et al.* '20 + work in prog.

An ambitious attempt to construct a *full theory of flavor* has been obtained embedding the Pati-Salam gauge group into an extra-dimensional construction:



Flavor ↔ special position (topological defect) in an extra (compact) space-like dimension

Dvali & Shifman, '00

Higgs and SU(4)-breaking fields with oppositely-peaked profiles, leading to the desired flavor pattern for masses & anomalies

Bordone, Cornella, Fuentes-Martin, GI '17 Fuentes-Martin, GI, Pages, Stefanek '20

Possible to implement anarchic neutrino masses via an inverse see-saw mechanism

In most *PS-extended models* collider and low-energy pheno are controlled by the effective 4321 gauge group that rules TeV-scale dynamics Di Luzio, Greljo,

ider $SU(4)_3 \times SU(3)_{1+2} \times [SU(2)_L \times U(1)']$ $V_3 \qquad V_{1,2}$ $V_{1,2} \qquad Di Luzio, Greljo, Nardecchia, '17 <math>V_1$ the $V_2 \times U(1)'$

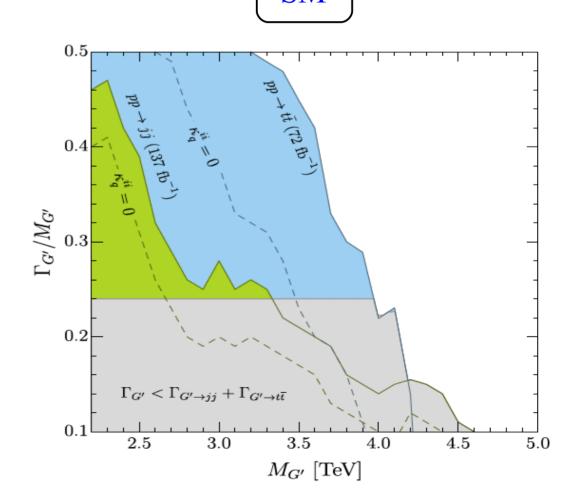
Despite the apparent complexity, the construction is highly constrained

- Positive features the EFT reproduced
- Precise predictions for high-pT data

consistent with present data!

New striking collider signature: G' ("coloron" = heavy color octet)

 \rightarrow strongest constraint on the scale of the model from pp $\rightarrow t \bar{t}$



Conclusions

- The statistical significance of the LFU anomalies is growing: in the $b \rightarrow sll$ system the chance this is a pure statistical fluctuation is marginal...
- <u>If combined</u>, the two sets of anomalies point to non-trivial flavor dynamics around the TeV scale, involving mainly the 3rd family → connection to the origin of flavor [multi-scale picture at the origin of flavor hierarchies]
- <u>No contradiction</u> with existing low- & high-energy data, <u>but new non-standard effects should emerge soon</u> in both these areas

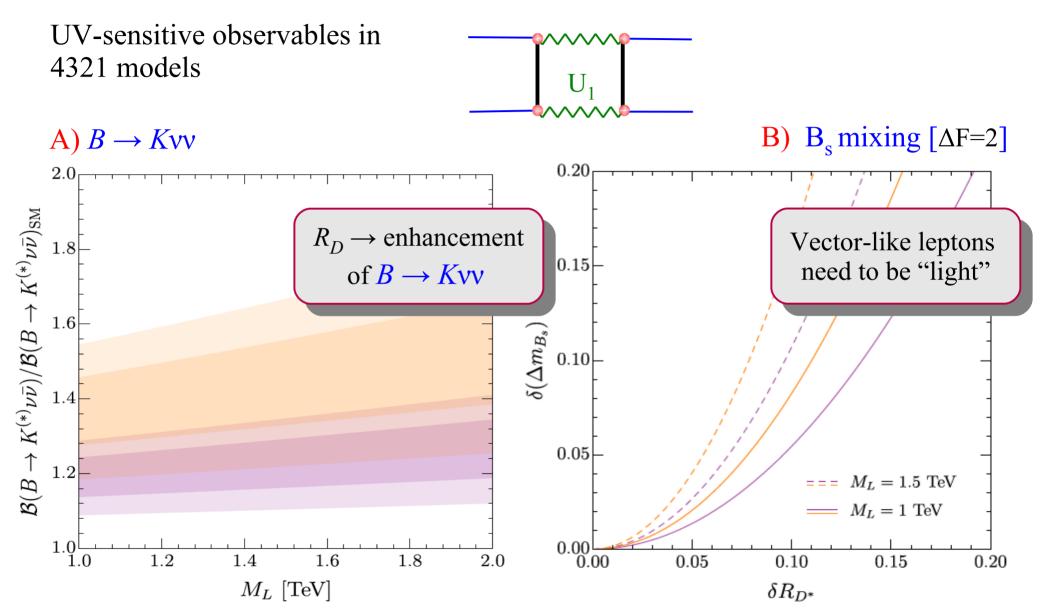


Very interesting (near-by!) future...

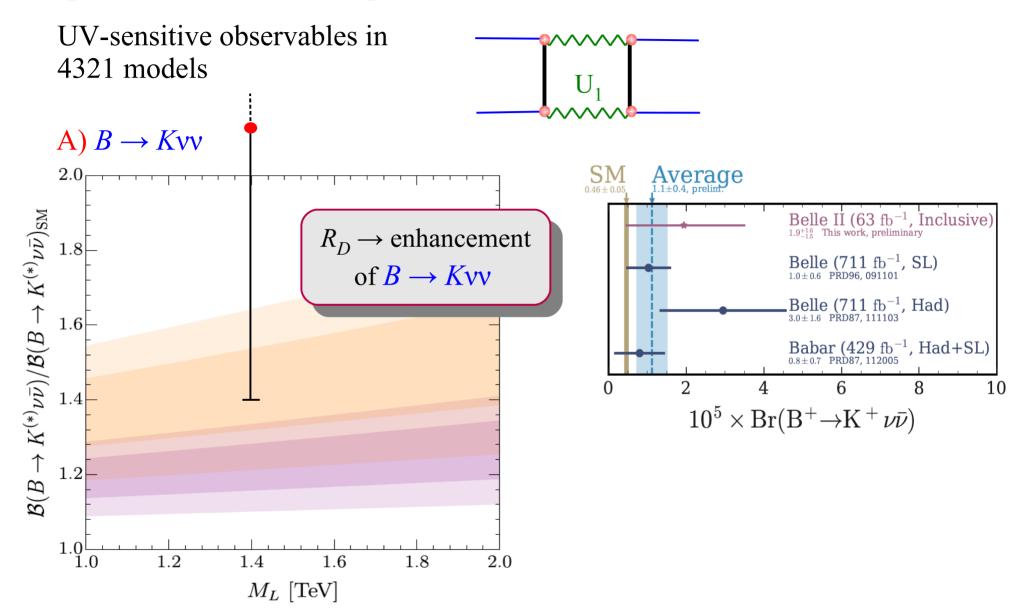
(both on the exp., the pheno,

and the model-building point of view)





Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21 Fuentes-Martin, GI, Konig, Selimovic, '20



Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21 Fuentes-Martin, GI, Konig, Selimovic, '20