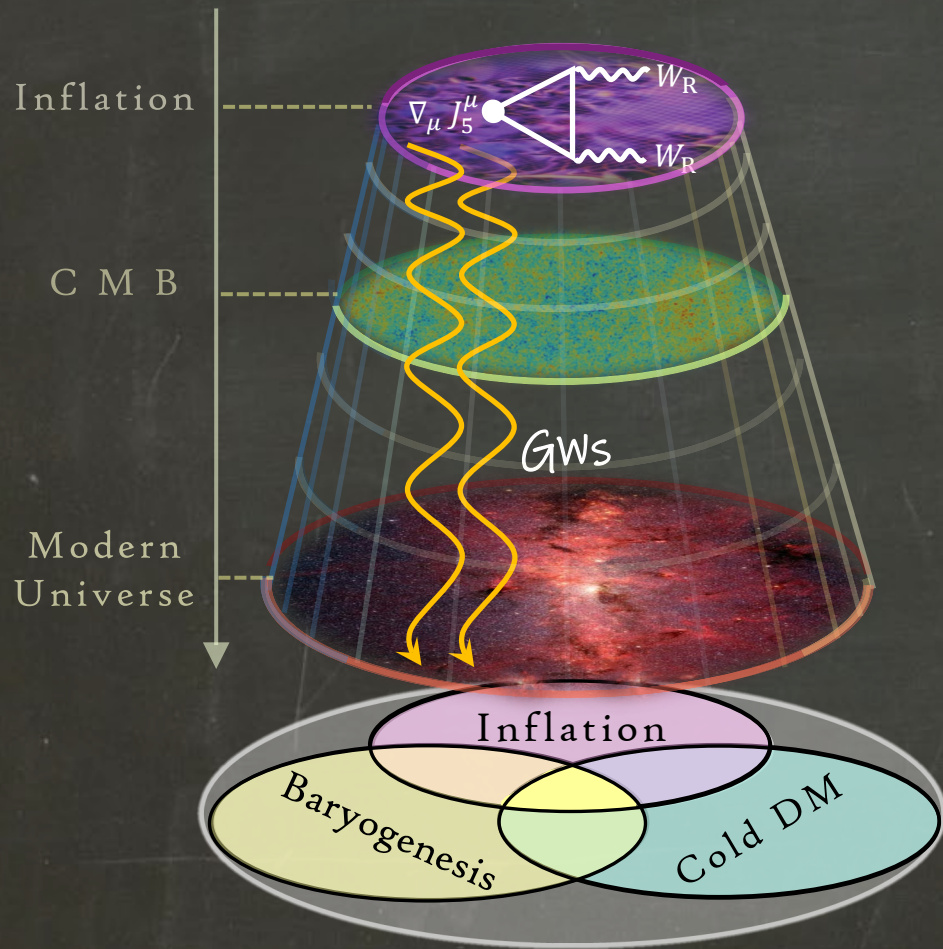


Cosmic Inflation, Origin of Matter & Gravitational waves



Azadeh Malek-Nejad
CERN

- Particle Physics of Inflation
Based on Axion-Inflation with Gauge Fields

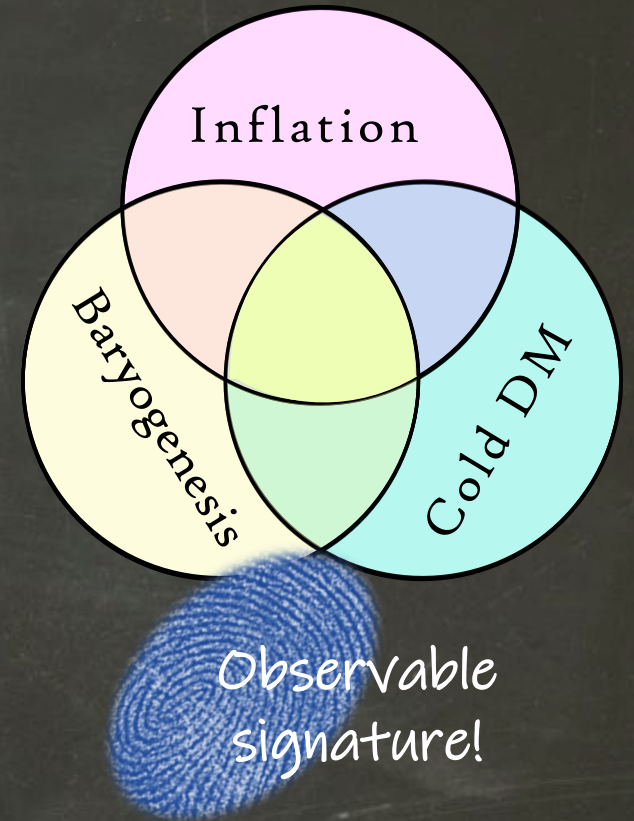
- Fermions & QFT Anomalies

$$\nabla_{\mu} J_5^{\mu} = \frac{g^2}{16\pi^2} W\tilde{W} + \frac{N_L - N_R}{24(16\pi^2)} R\tilde{R}$$

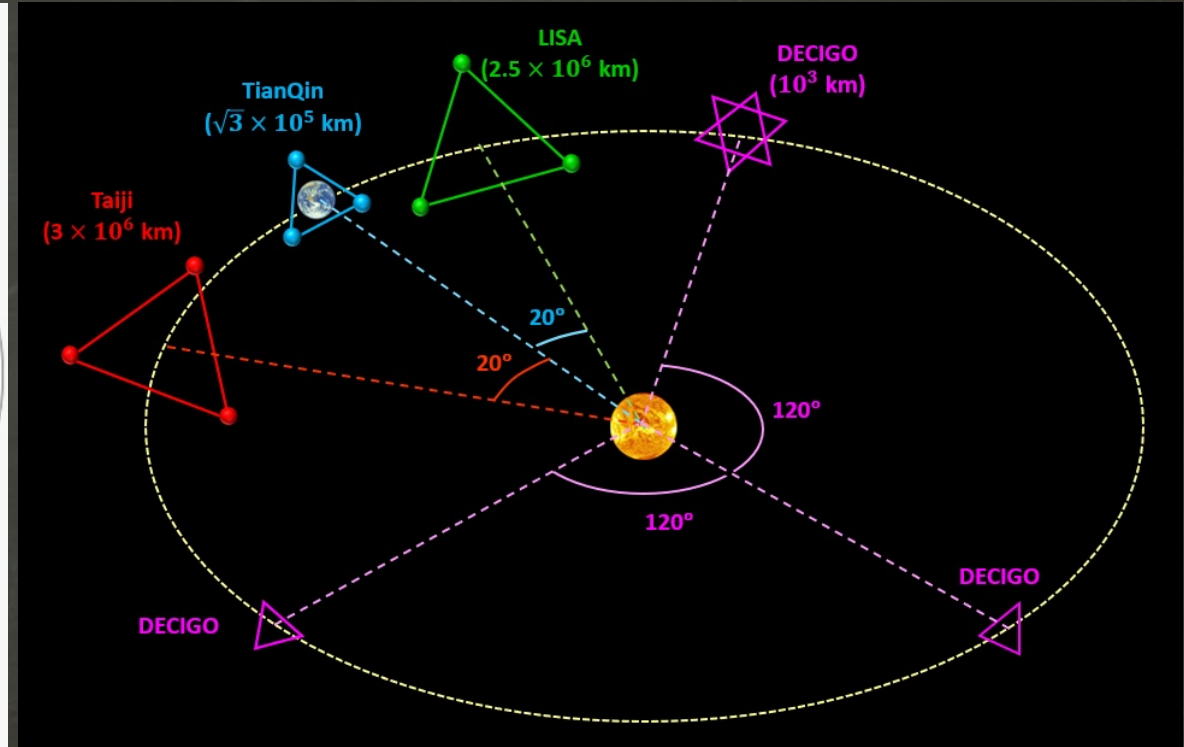
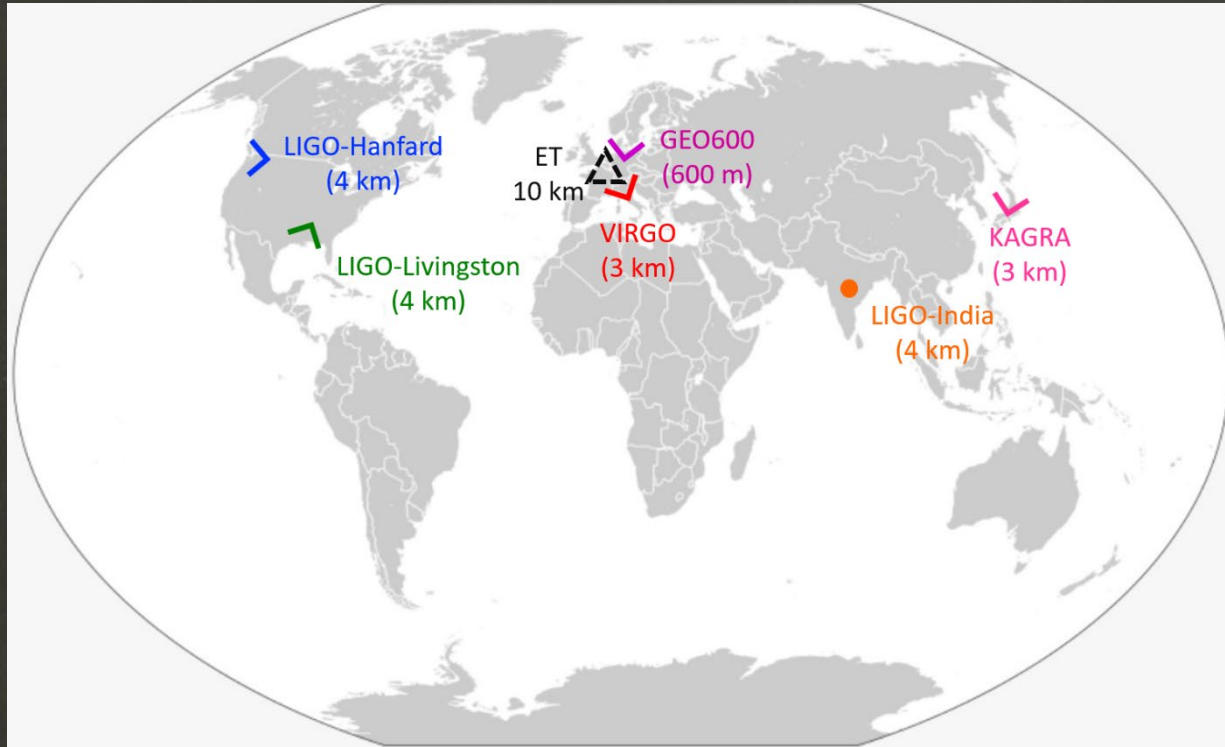
Adler–Bell–Jackiw
anomaly

(Global) Gravitational
anomaly

- Gravitational Waves Signature

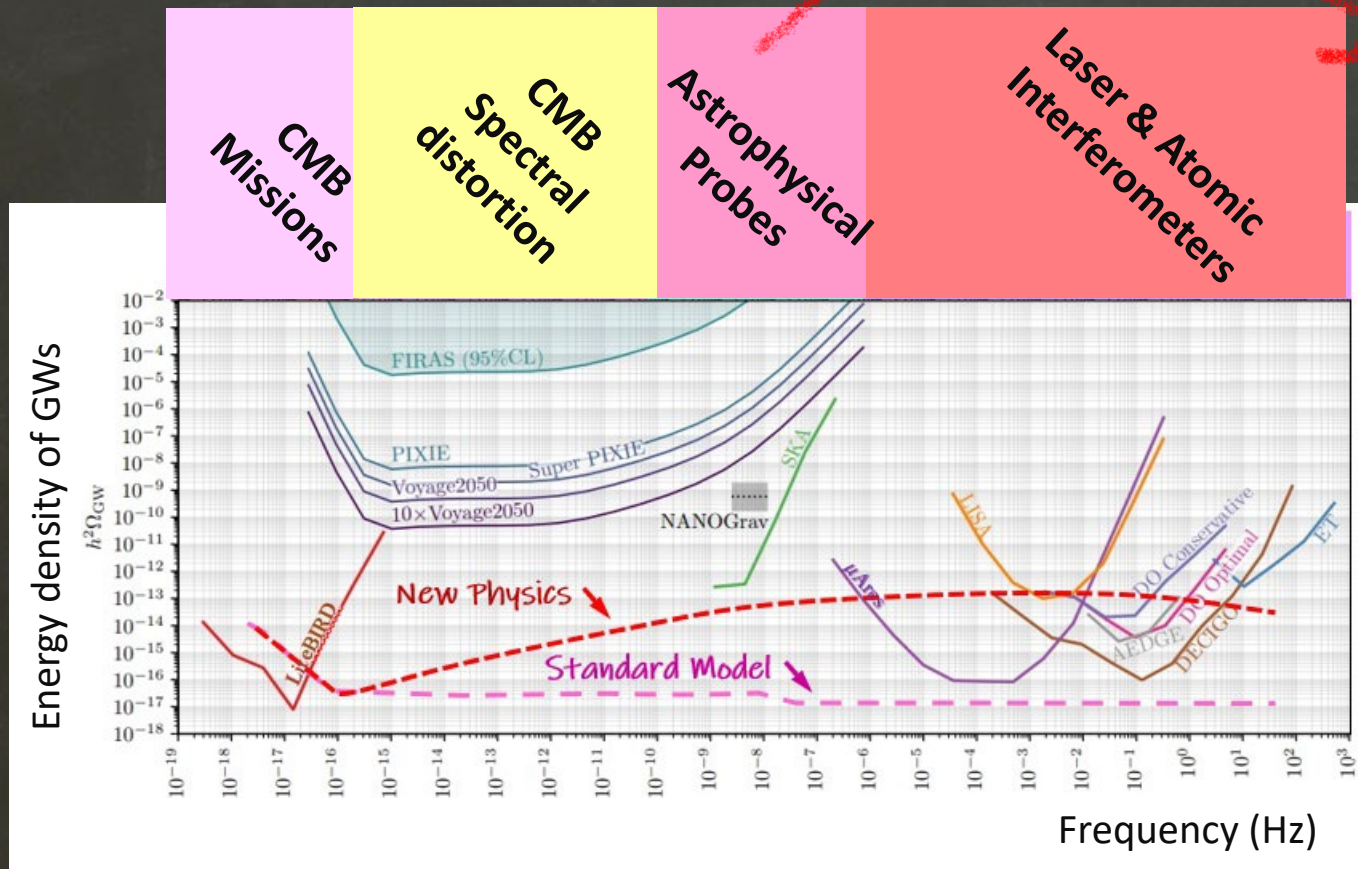


Networks of GWs Detectors

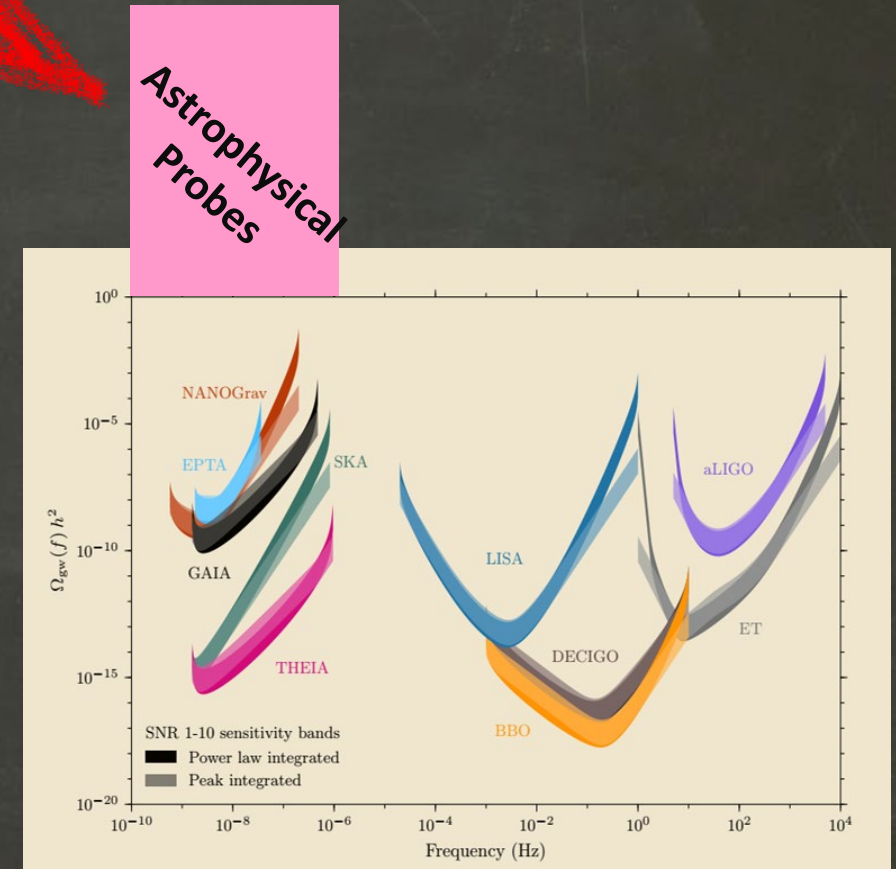


Network of laser interferometer detectors of GWs on Earth (left) & in the sky (right)

Sensitivity curves on energy density of GWs



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2021

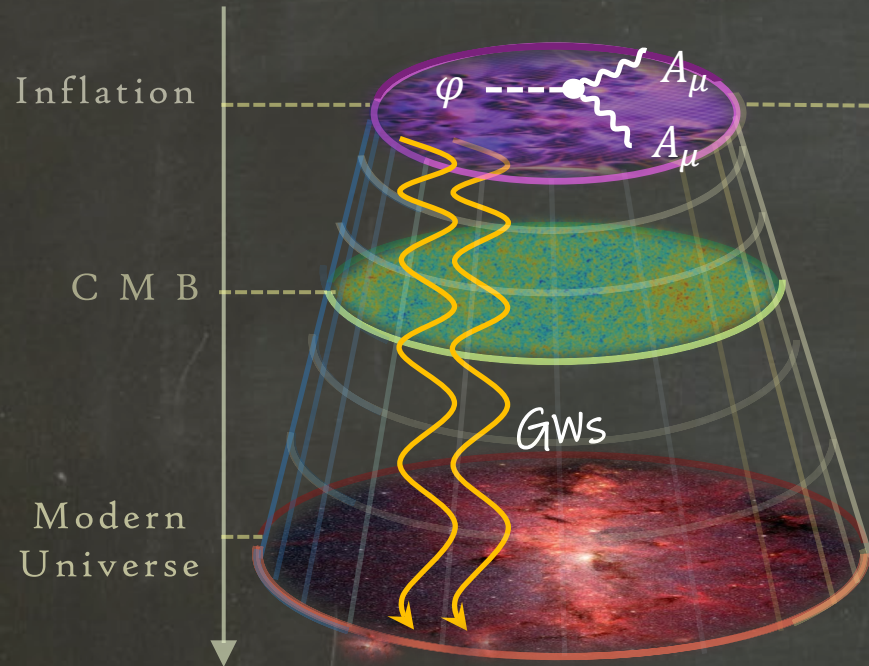


J. Garcia-Bellido, H. Murayama, and G. White 2021

A New Class of Inflation Models

(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011
P. Adshead, M. Wyman, 2012



Axion-inflation and gauge fields (non-Abelian)

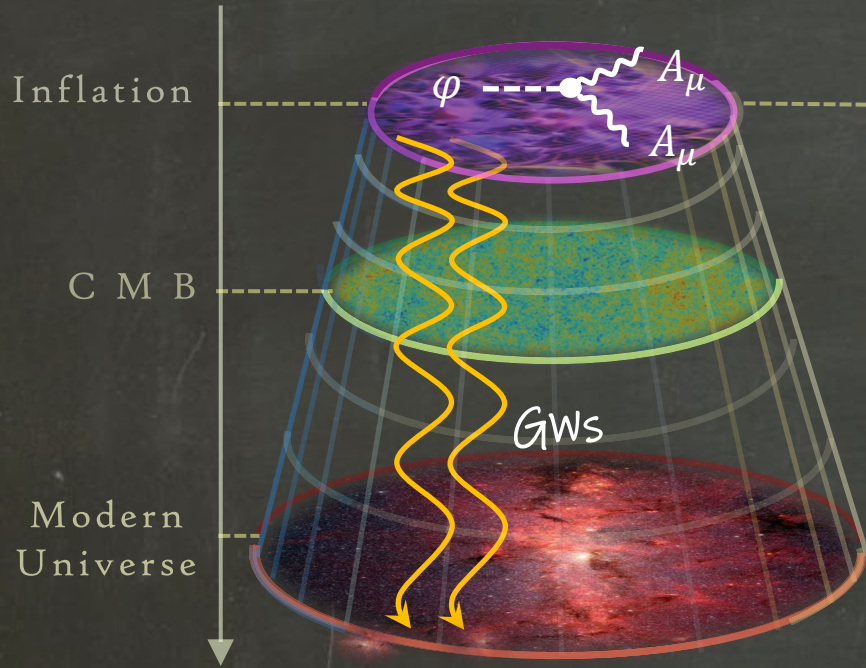
Particle Production
In Axion-Inflation



A New Class of Inflation Models

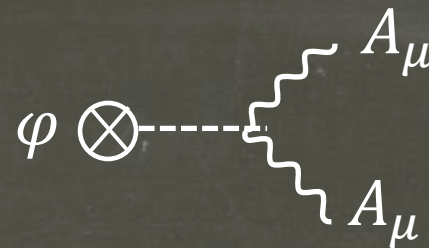
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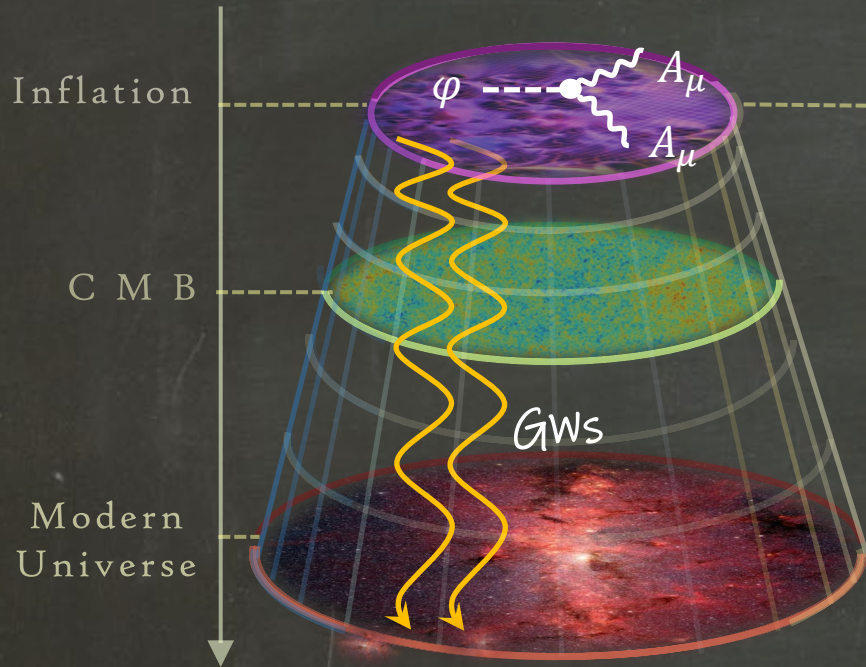
Particle Production
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A New Class of Inflation Models

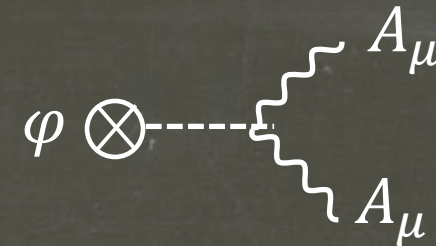
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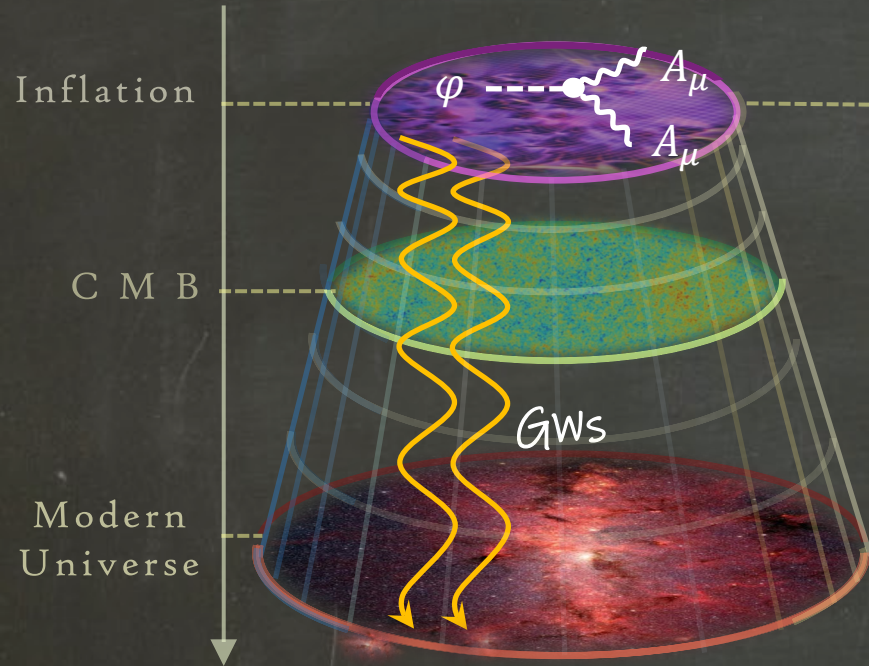
A new mechanism
for Fermion Production in
Inflation!

A.M., 2019
Mirzagholfi, A.M., Lozanov 2019

A New Class of Inflation Models

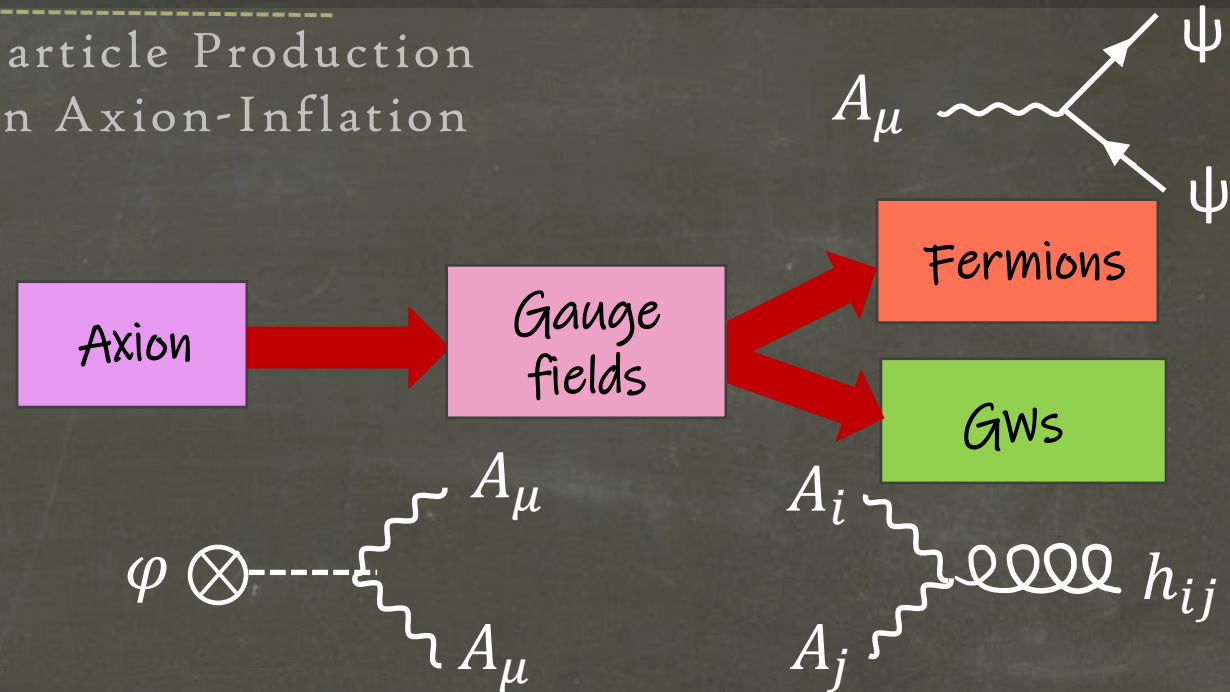
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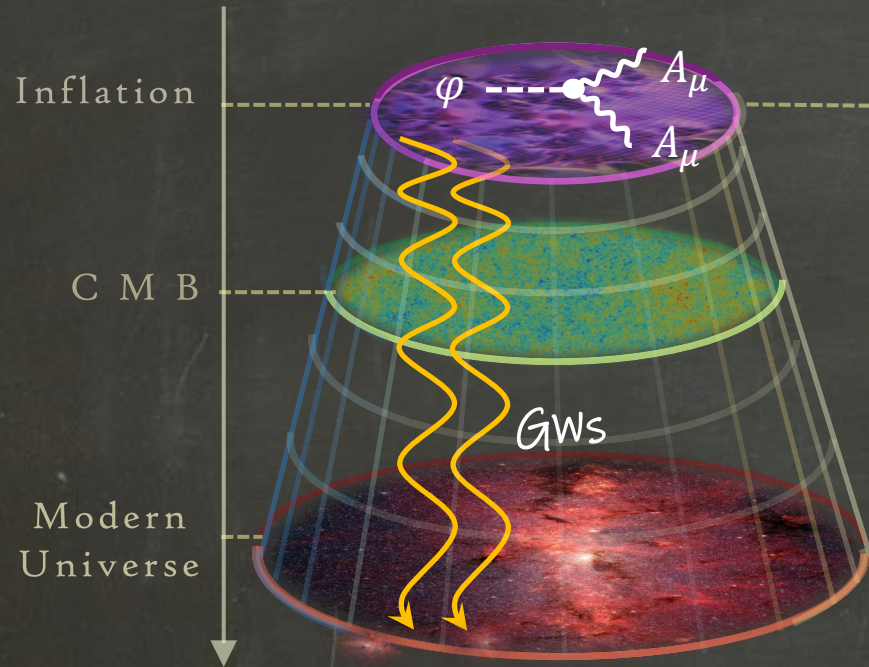
Particle Production
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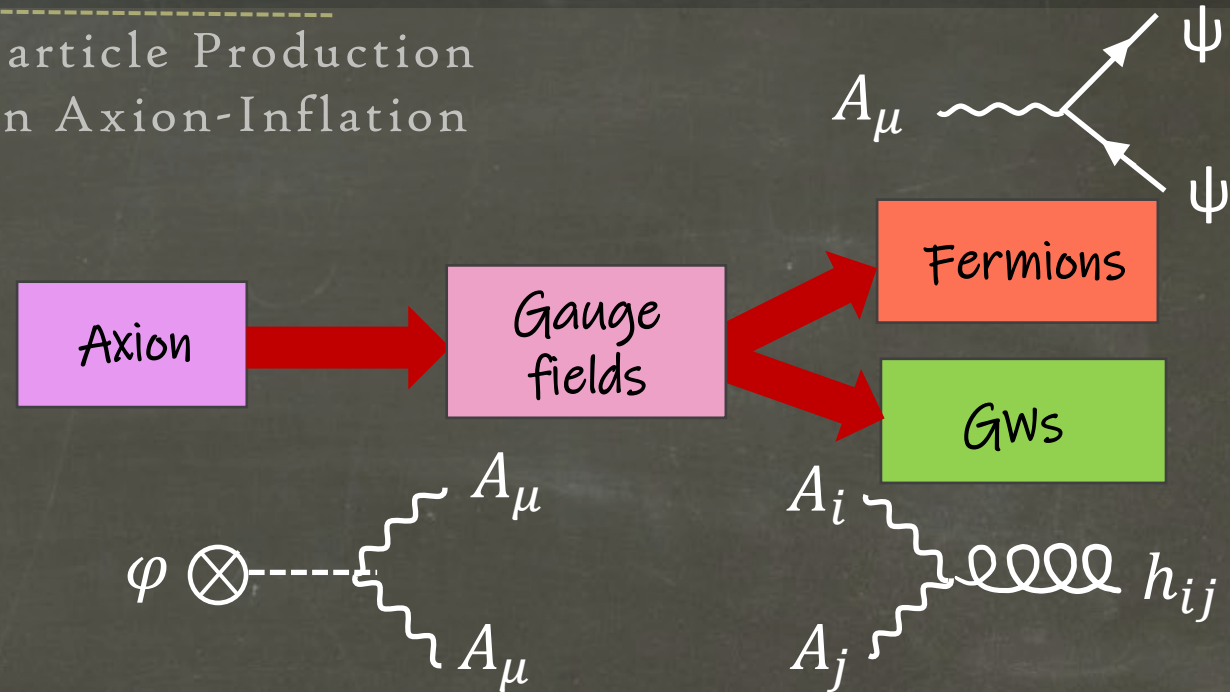
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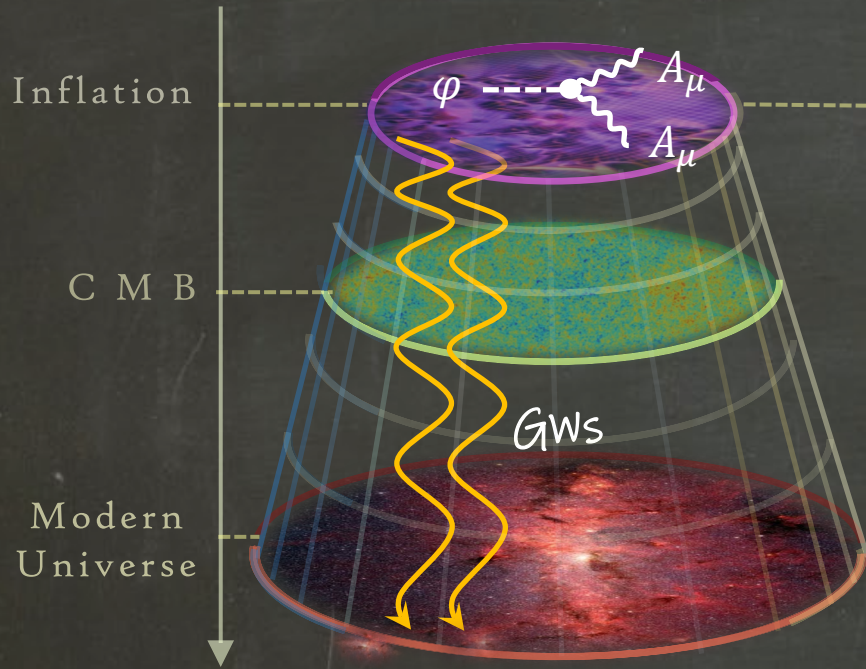
Sourced GWs:
Chiral & non-Gaussian

A. M., 2019
Mirzaghohi, A.M., Lozanov 2019
A. M. et. al, 2011 & 2013
Dimastrogiovanni et. al 2013
P. Adshead et. al, 2013

A New Class of Inflation Models

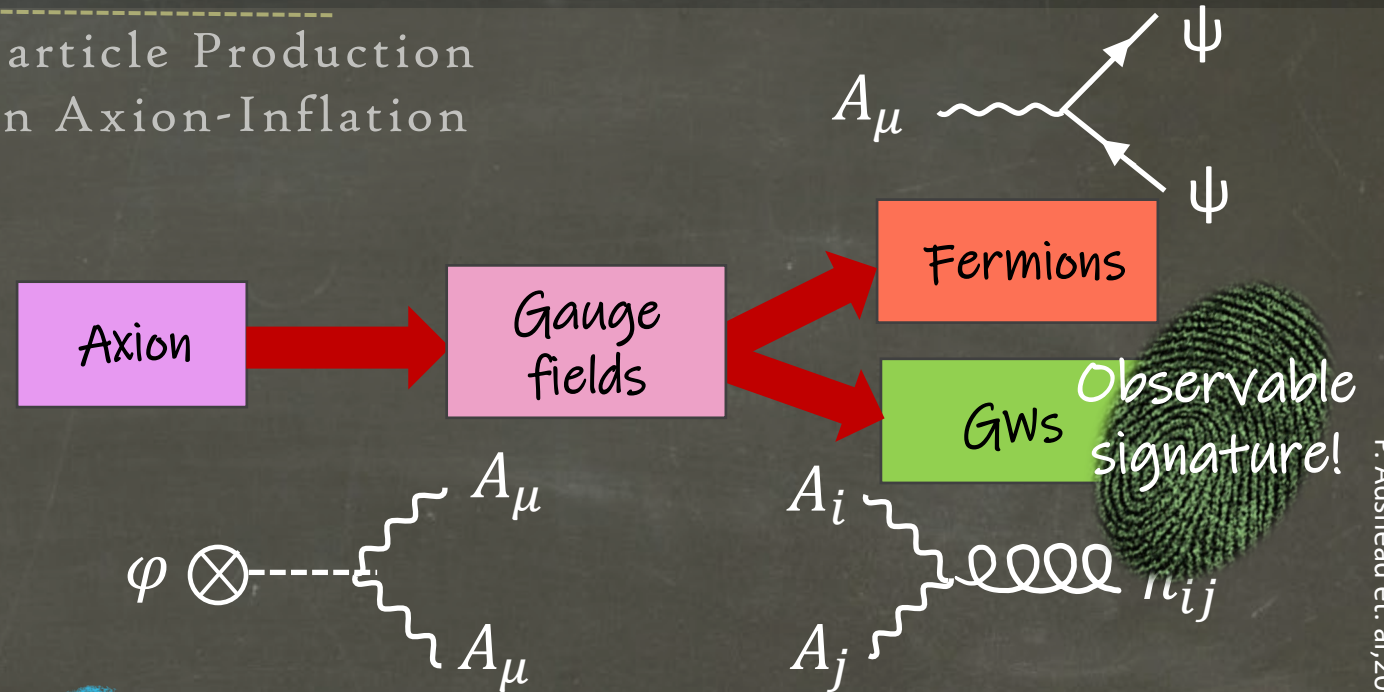
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A. M., & Sheikh-Jabbari, 2011
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Axion-inflation and gauge fields (non-Abelian)

Particle Production
In Axion-Inflation



Vacuum GWS:
Unpolarized & Gaussian

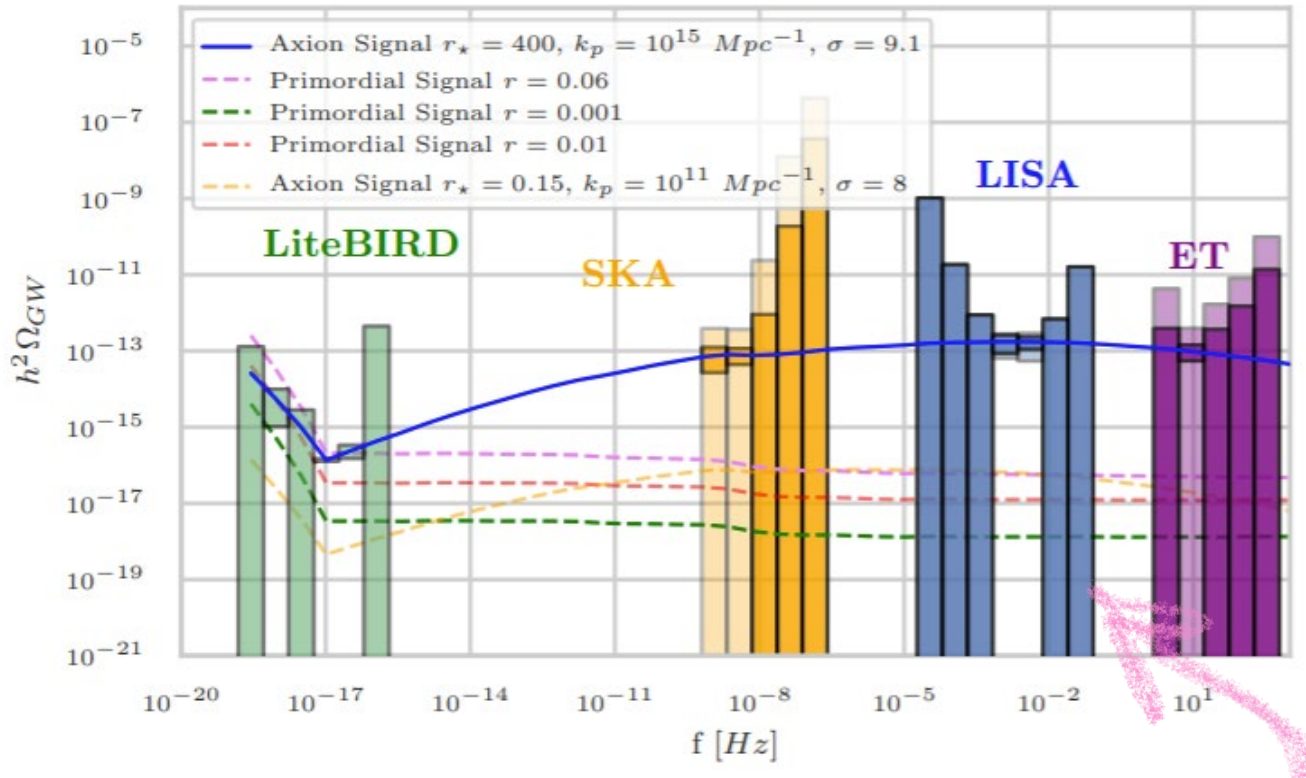
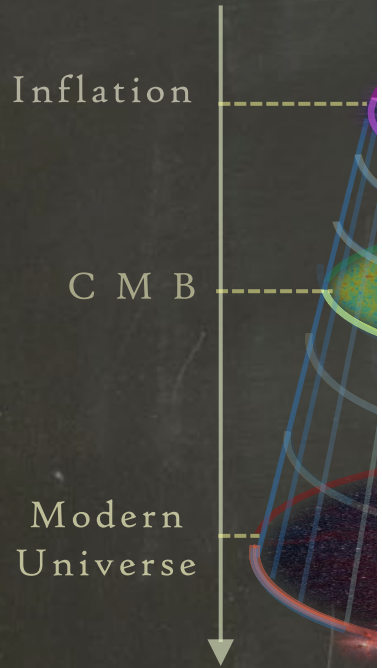


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P. Adshead et. al, 2013

A New Class of Inflation Models

(closer to P)



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

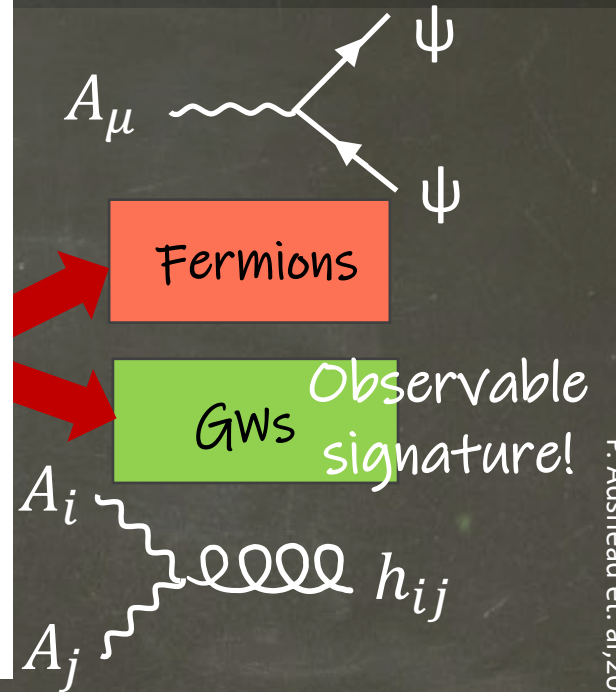
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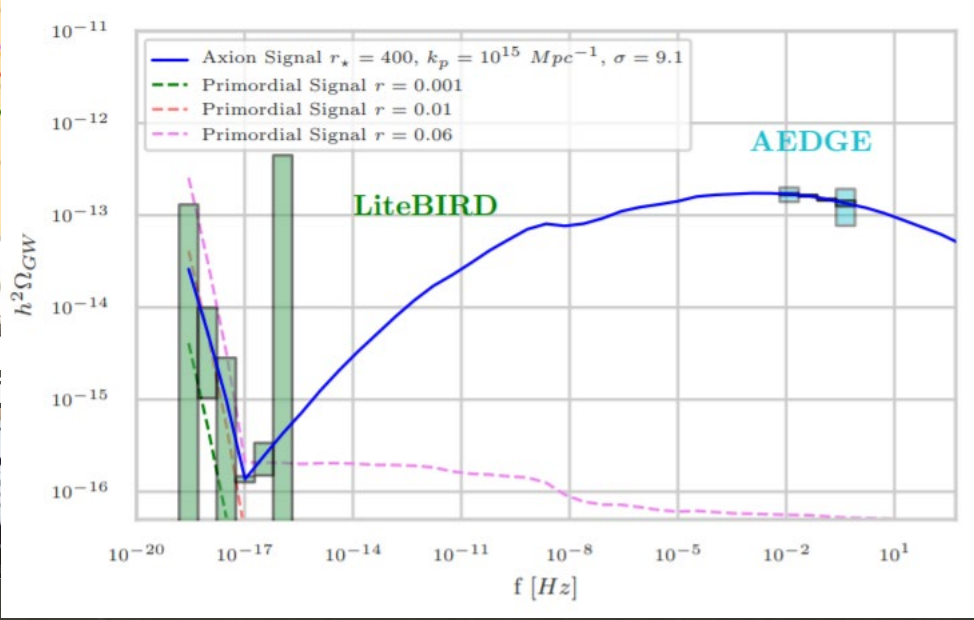
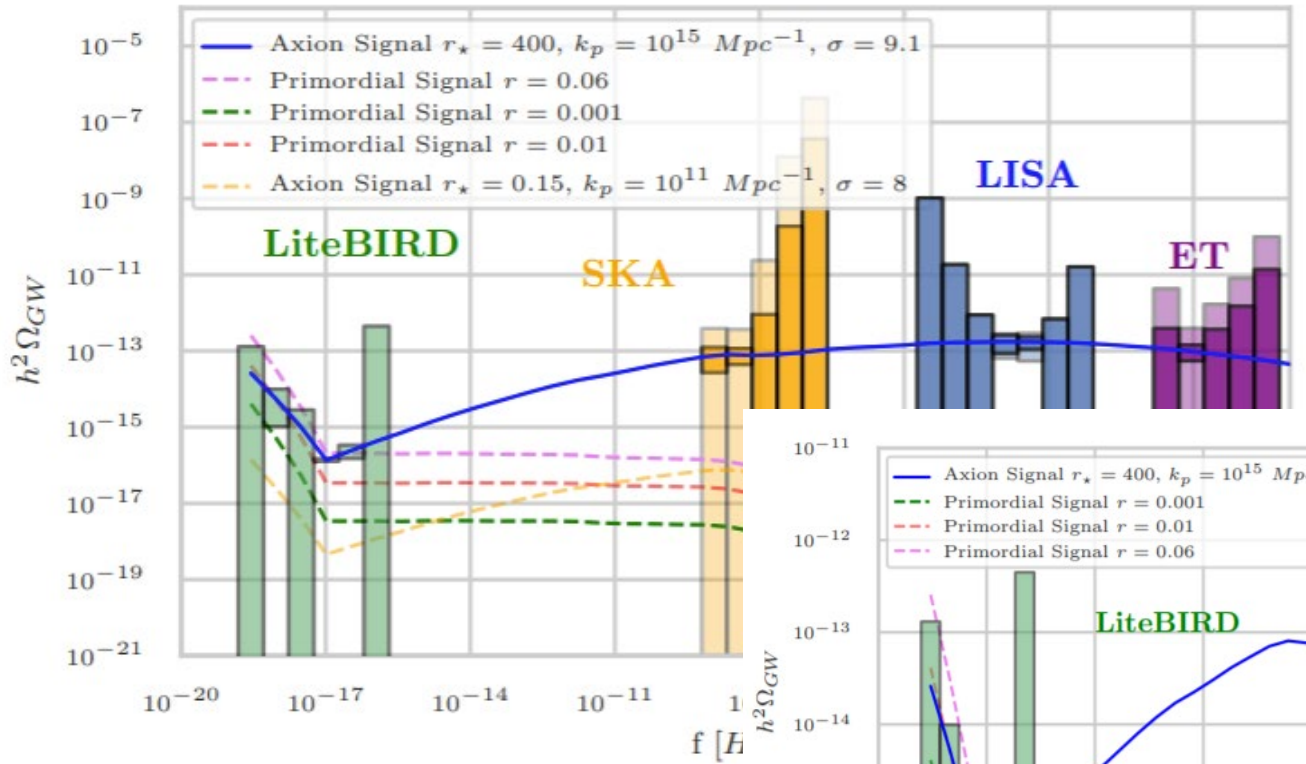
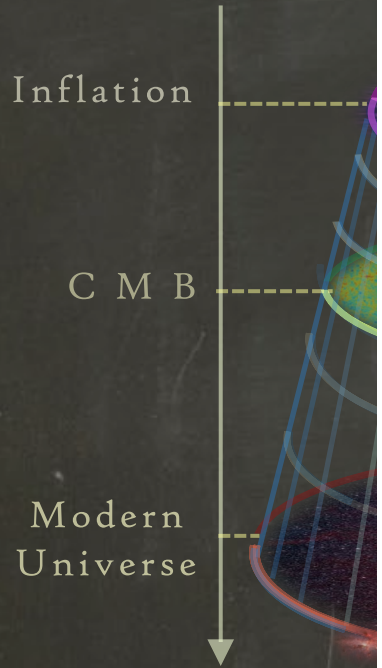
Fields (non-Abelian)



A. M., 2019
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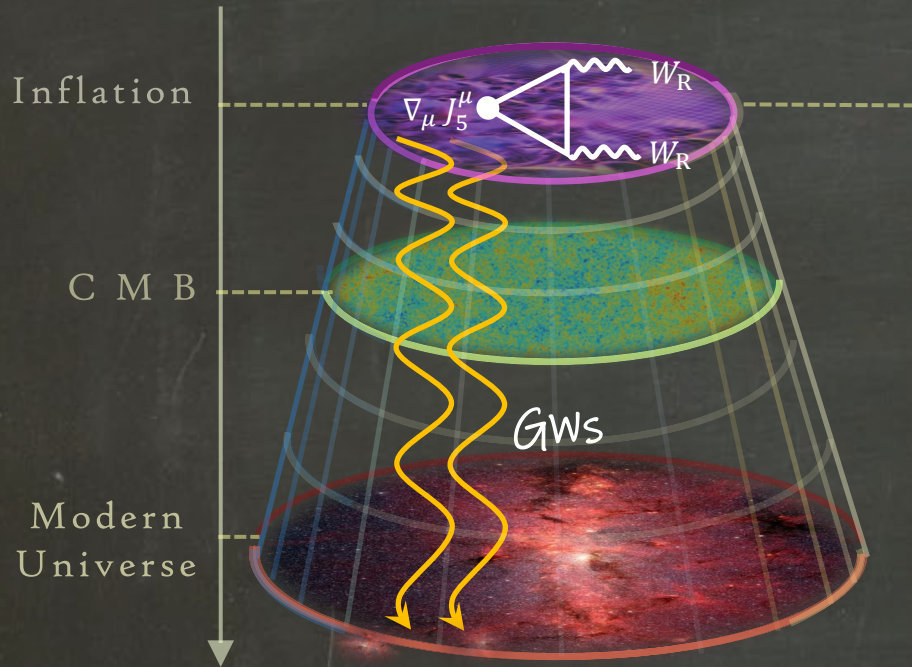
Observable nature!

ij

GWs:
Gaussian

A.M., 2019
 Mirzaghohi, A.M., Lozanov 2019
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 Dimastrogiovanni et. al 2013
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Setup:



I) Axion-inflation and gauge fields (non-Abelian)

A New Class of Inflation Models

II) Embedding Axion-inflation in LR symmetric model

Axion-Inflation



Left-Right Symmetric Model (LRSM)

LRSM: the minimal beyond SM

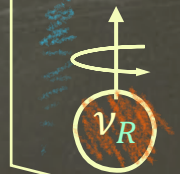
with

$SU(2)_R$ Gauge Symmetry
& Right-handed Neutrinos

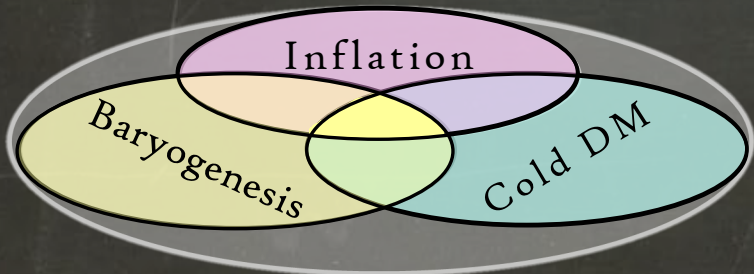
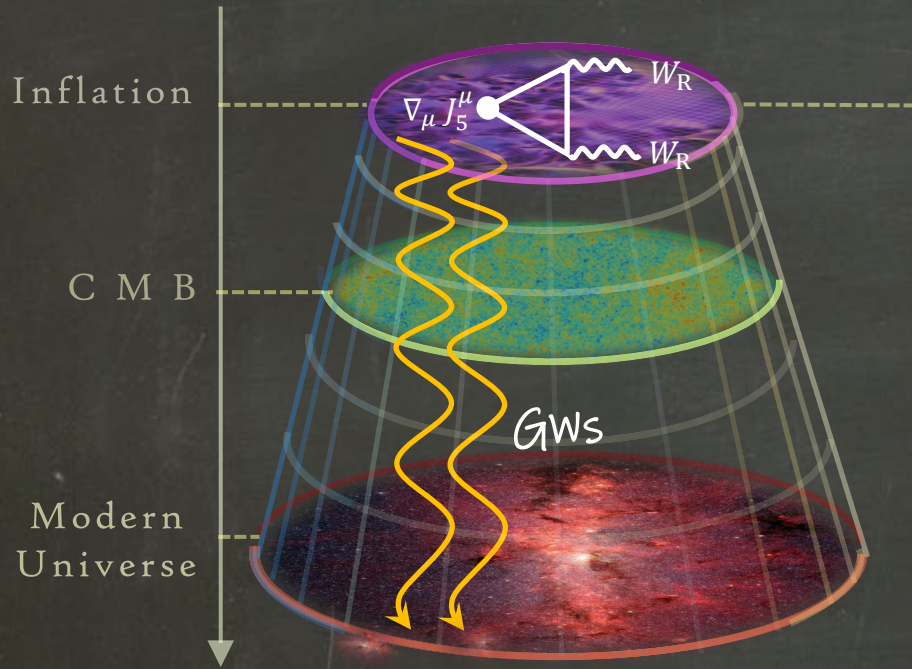
$SU(2)_L$



mirror
 $SU(2)_R$



Setup:



A.M. JHEP 2021, 113 (2021)

A. M. Phys. Rev. D 104, 083518 (2021)

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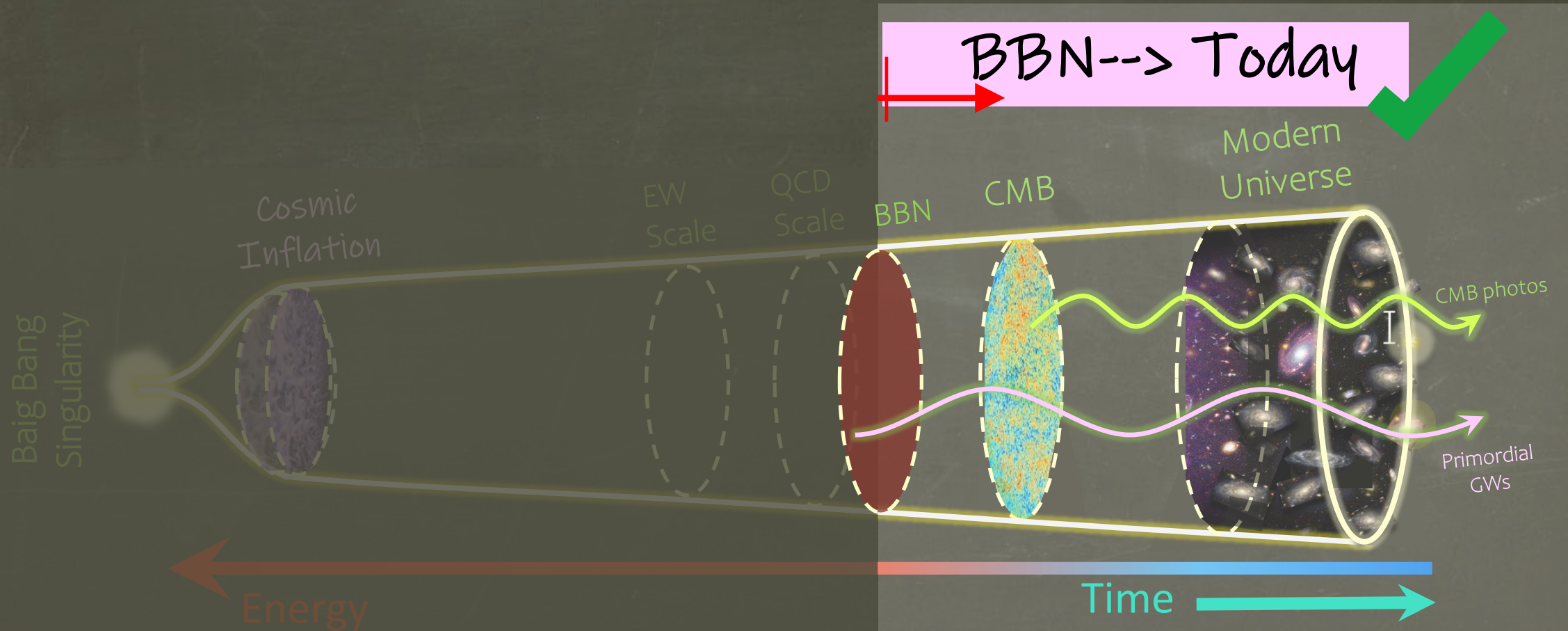
$SU(2)_R$



Early Universe Physics

Modern cosmology remarkably successful from **BBN** until today!

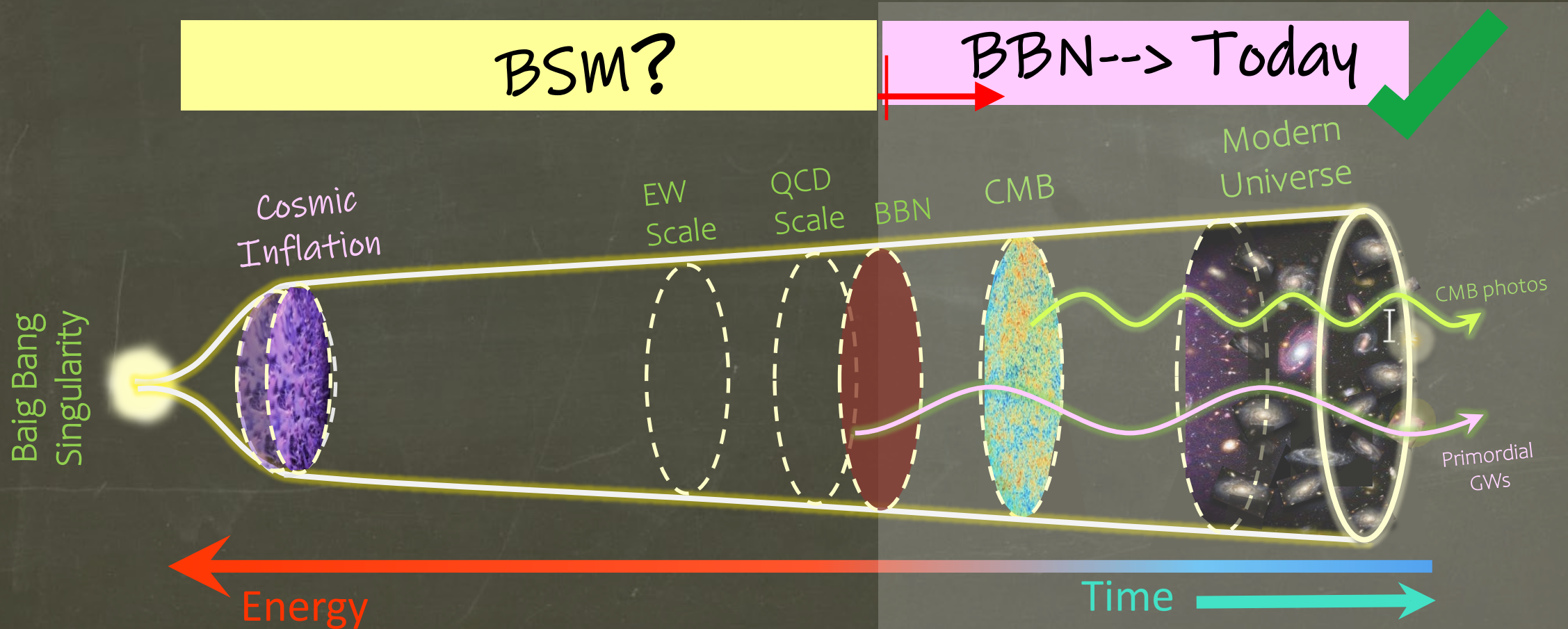
But the physics before BBN is still much less certain!



Early Universe Physics

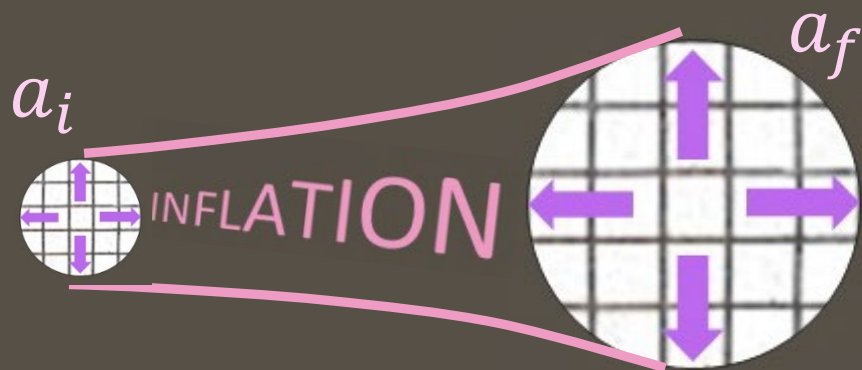
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Cosmic Inflation

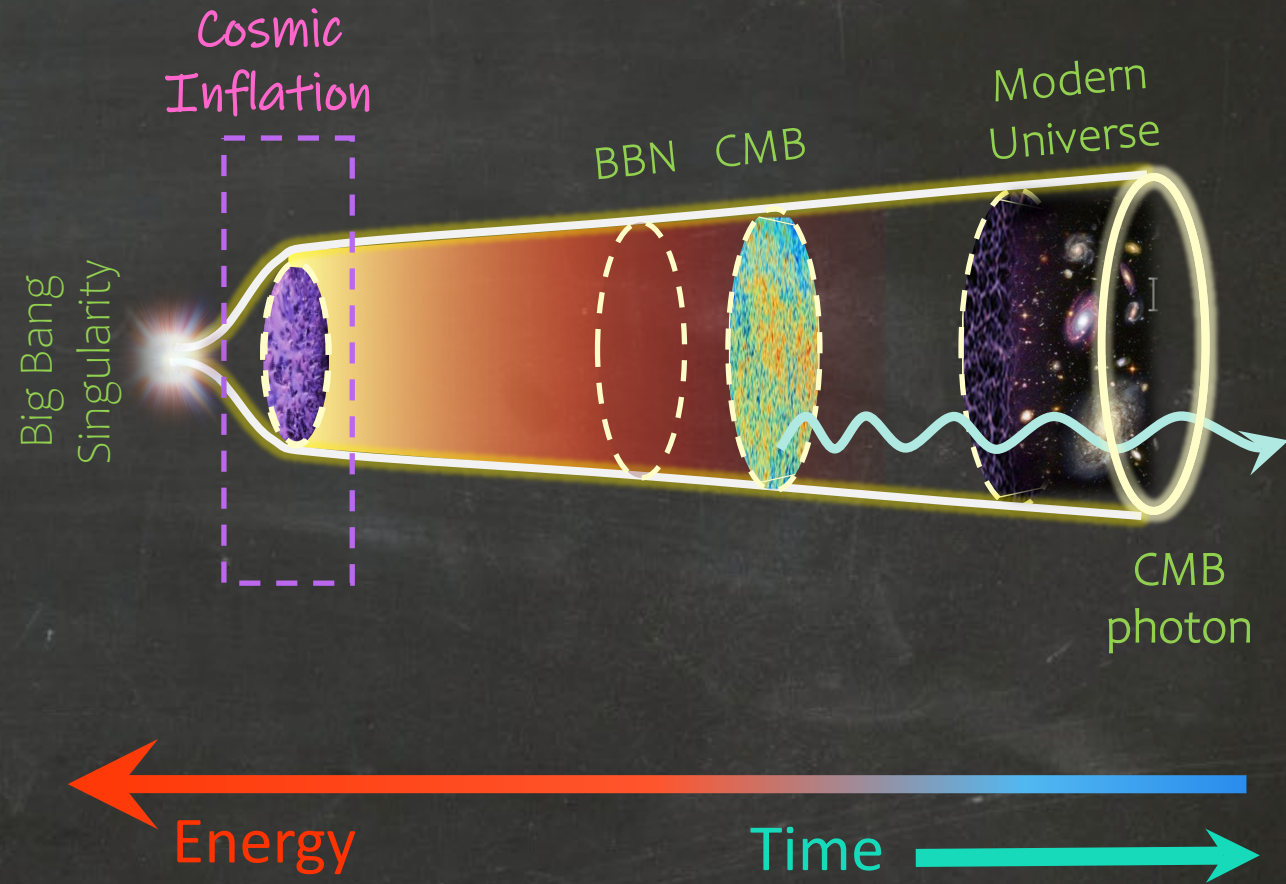
A period of exponential expansion of space shortly after the Big Bang



$$\frac{a_f}{a_i} = e^{60} \approx 10^{26}!$$

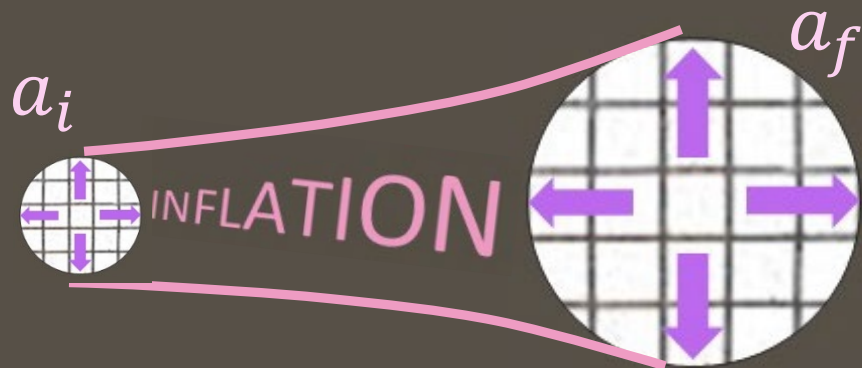
Guth Phys. Rev. D23 (1981)

Linde Phys. Lett. B 108 (1982)



Cosmic Inflation

A period of exponential expansion of space shortly after the Big Bang



$$\frac{a_f}{a_i} = e^{60} \approx 10^{26}!$$

Bacterium

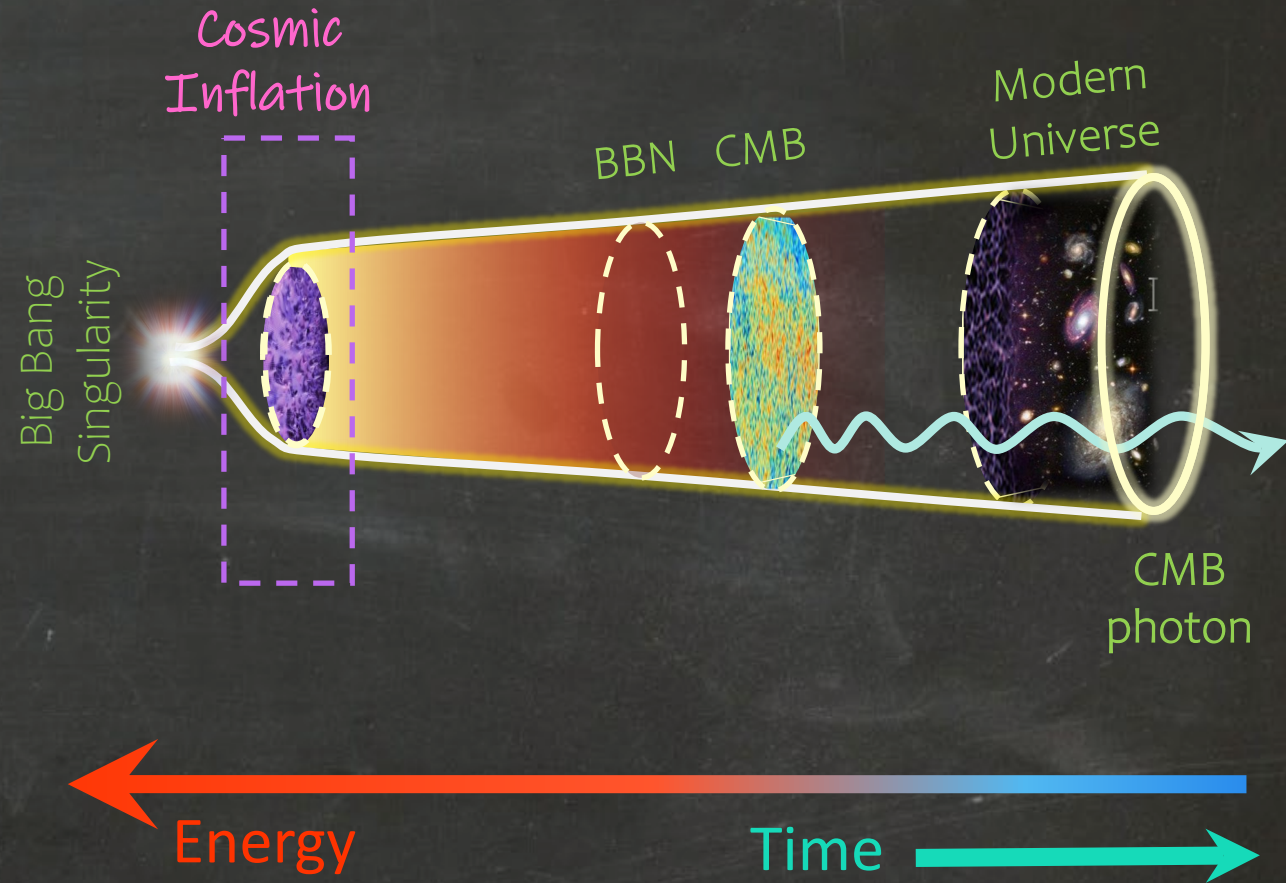
$D \approx 10 \mu\text{m}$



Milky Way

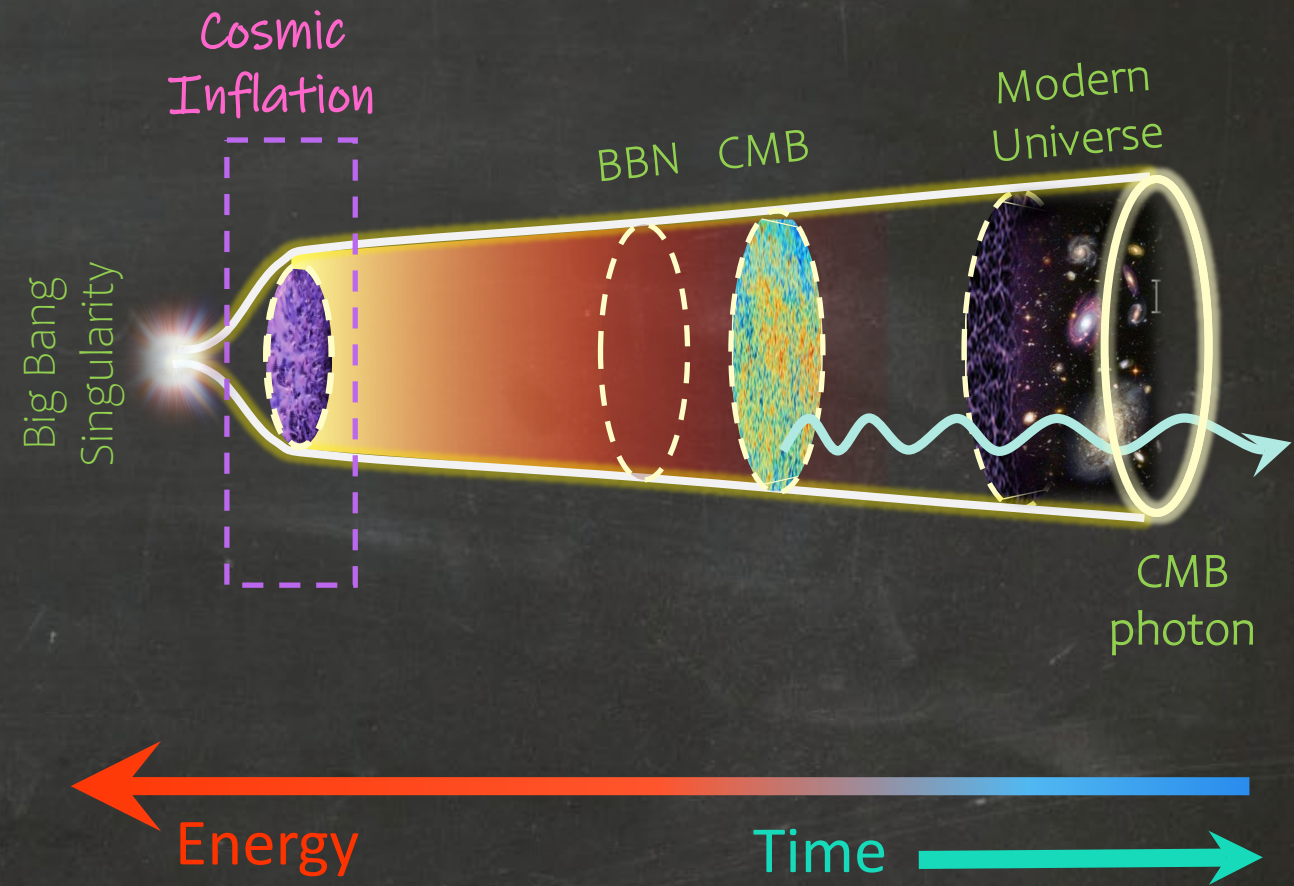
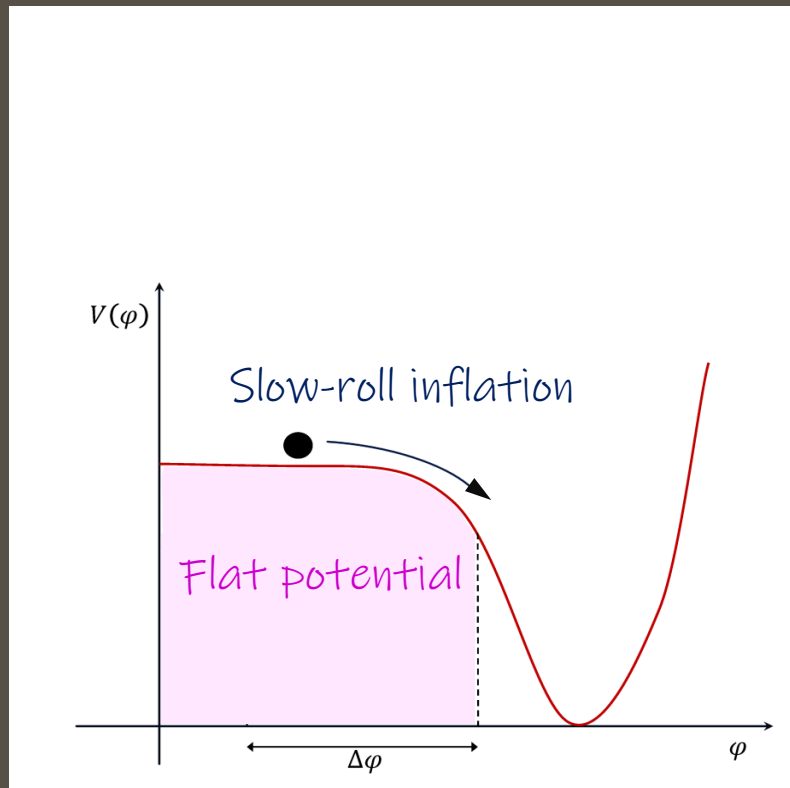
Guth Phys. Rev. D23 (1981)

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What caused inflation?

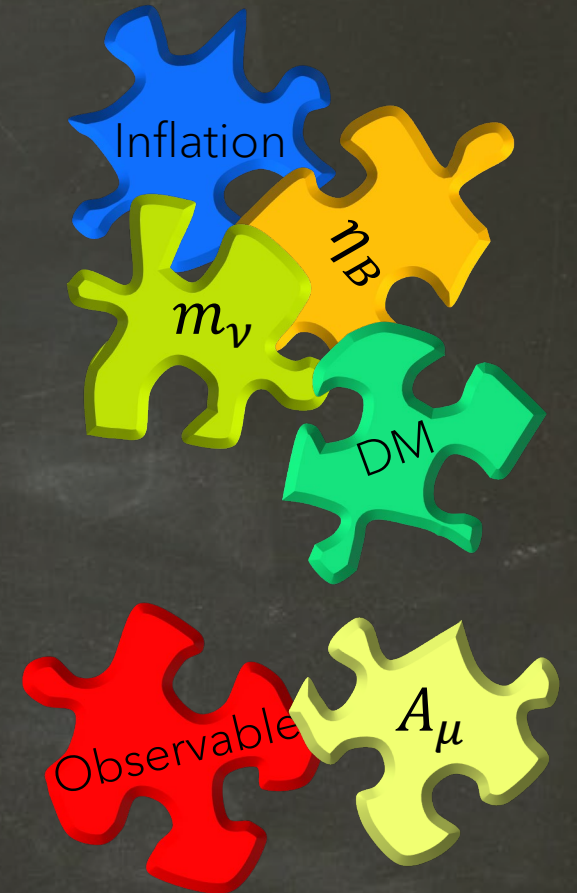
A scalar field "slow-rolling" toward its true vacuum provides a simple model for inflation.



Puzzles of SM & Cosmology

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

Puzzles of
Standard Model of Particle Physics (SM)
& Cosmology which need
Physics Beyond SM



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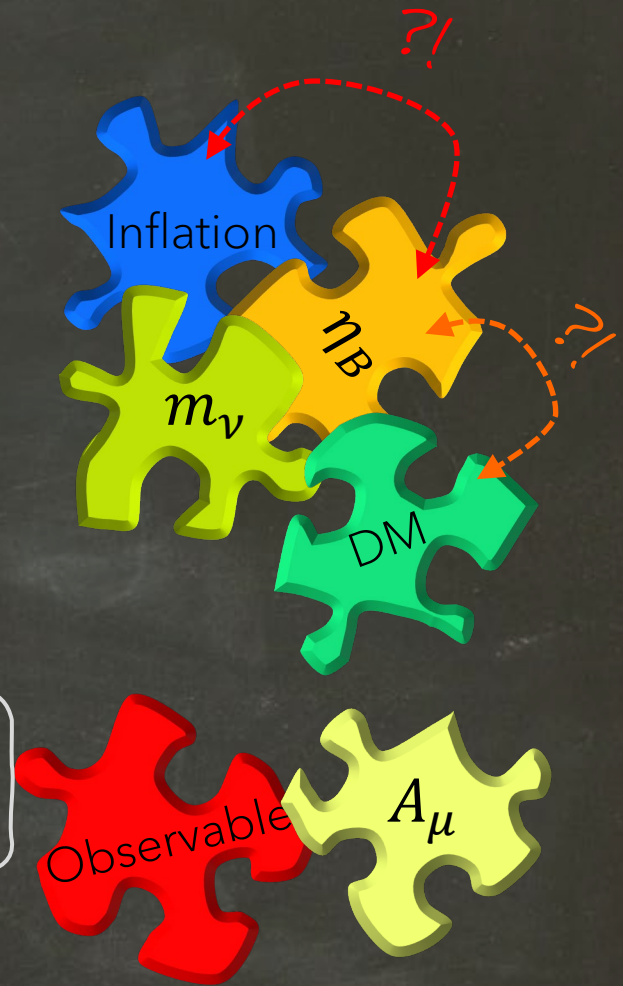
Curious cosmological coincidences $\eta_B \approx 0.3 P_\zeta$ and $\Omega_{DM} \approx 5\Omega_B$!

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 6 \times 10^{-10}$$

Baryon to Photon Ratio
Today

$$P_\zeta = \frac{1}{2\epsilon} \left(\frac{1}{2\pi} \frac{H}{M_{pl}} \right)^2 \approx 2 \times 10^{-9}$$

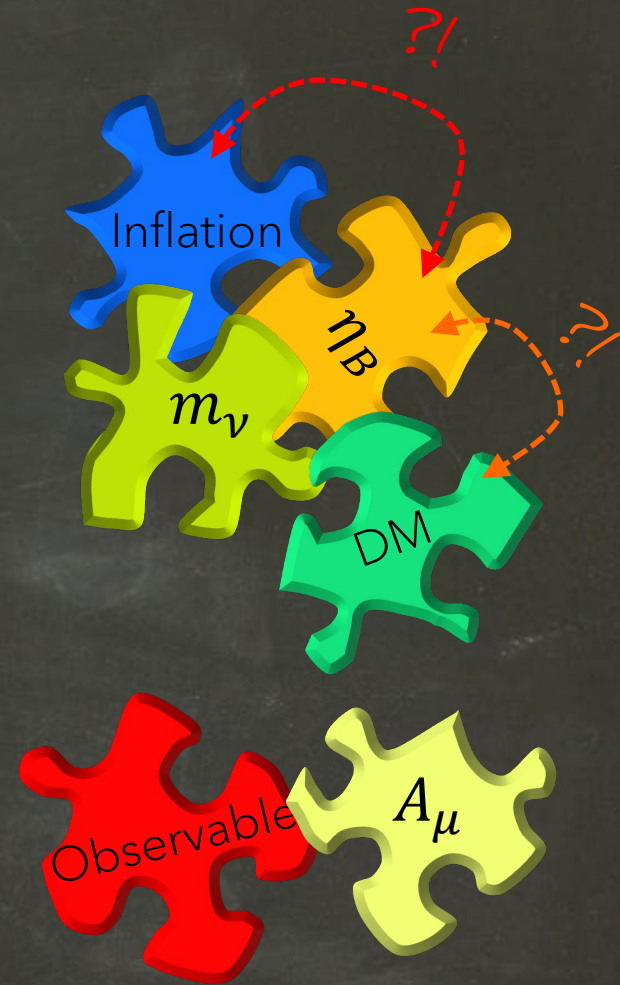
Curvature Power Spectrum in
Inflation



Puzzles of SM & Cosmology

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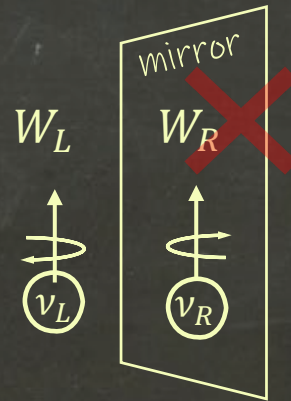
Puzzles of Standard Model of Particle Physics (SM) & Cosmology Which need Physics Beyond SM



Curious cosmological coincidences $\eta_B \simeq 0.3 P_z$ and $\Omega_{DM} \simeq 5\Omega_B!$

- 1. Ad hoc parity violation
- 2. Accidental B-L global symmetry
- 3. Vacuum Stability problem

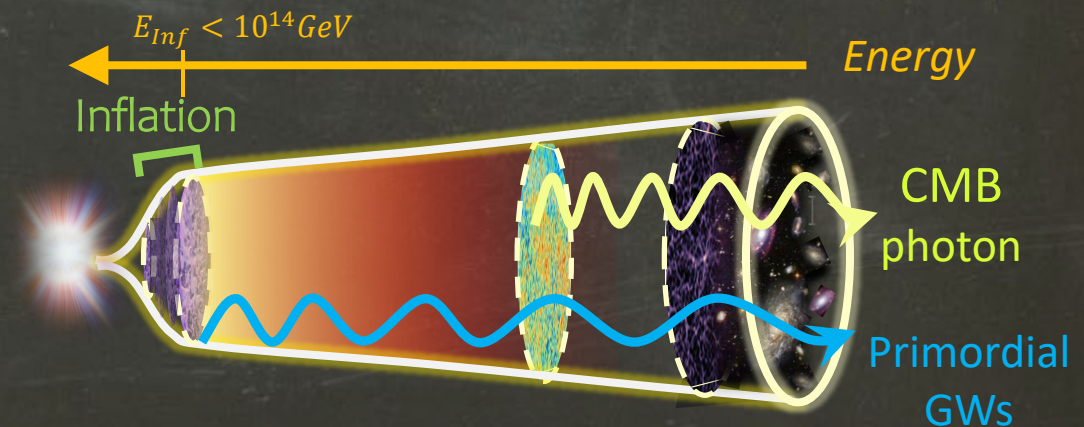
SM as a particle physics model also faces some conceptual issues



As Yet

- Observations are in perfect agreement with Inflation.
- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on Scalars.

Inflation Particle Physics: a scalar field beyond the SM.



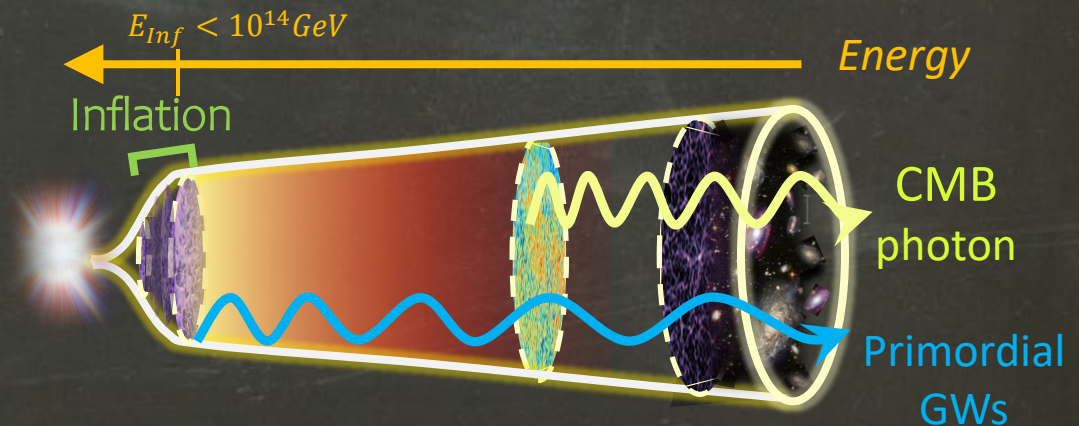
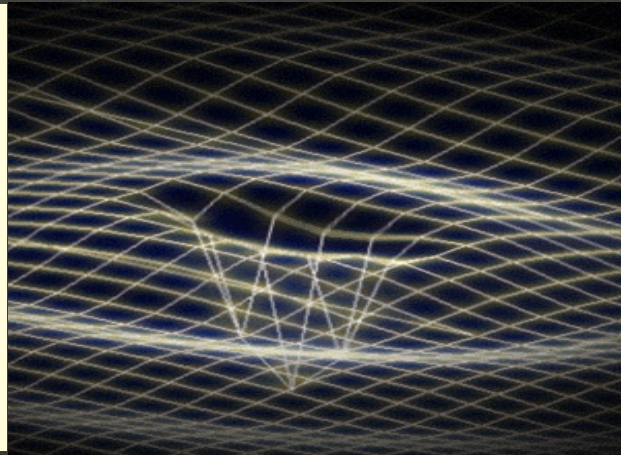
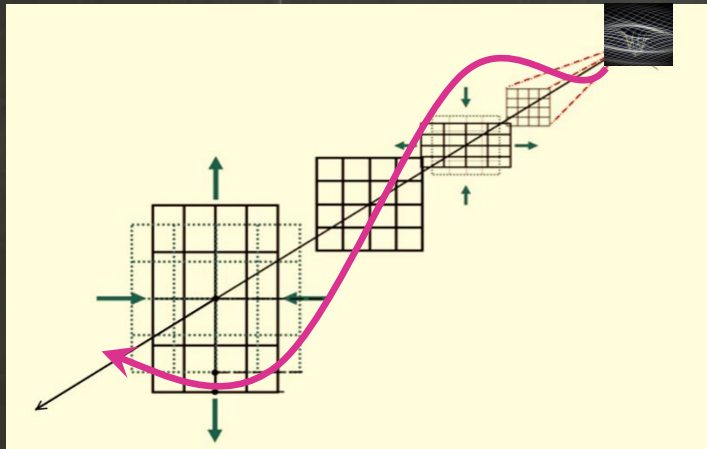
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- Primordial Gravitational Waves (PGW):

Vacuum fluctuations: unpolarized, red-tilted, and nearly Gaussian.



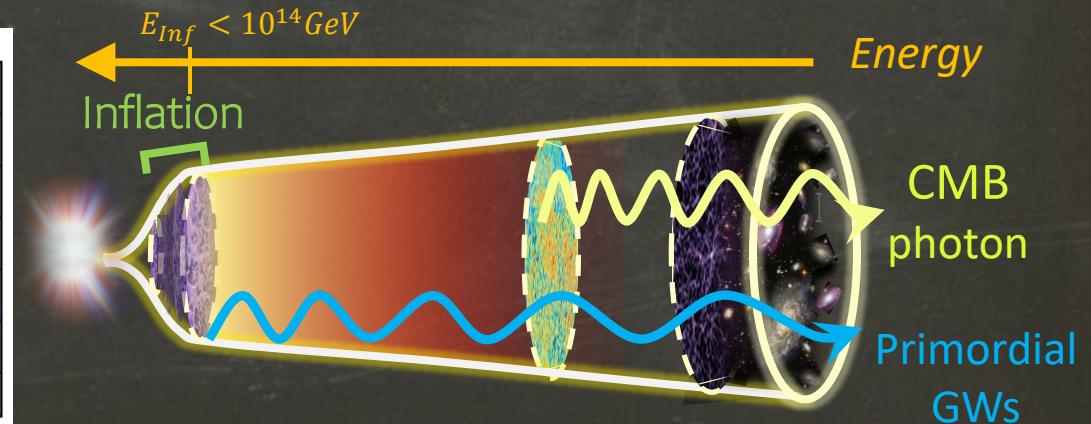
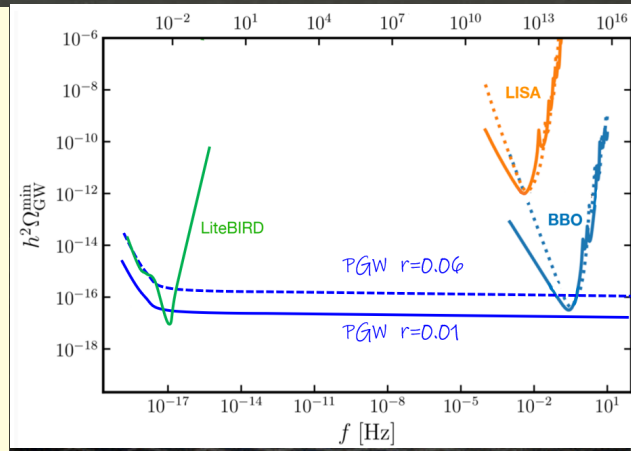
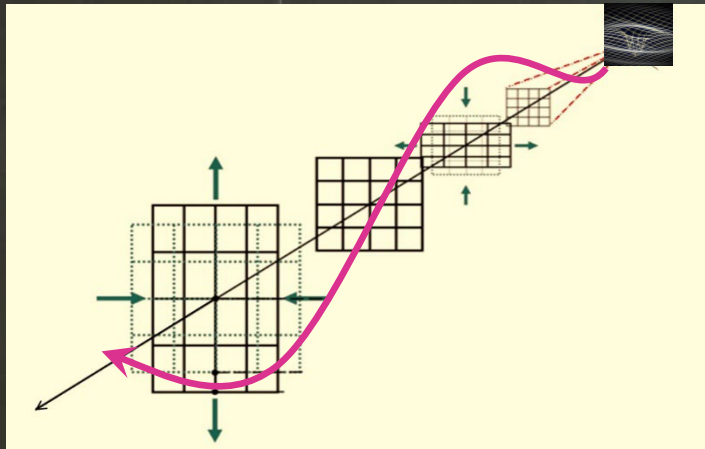
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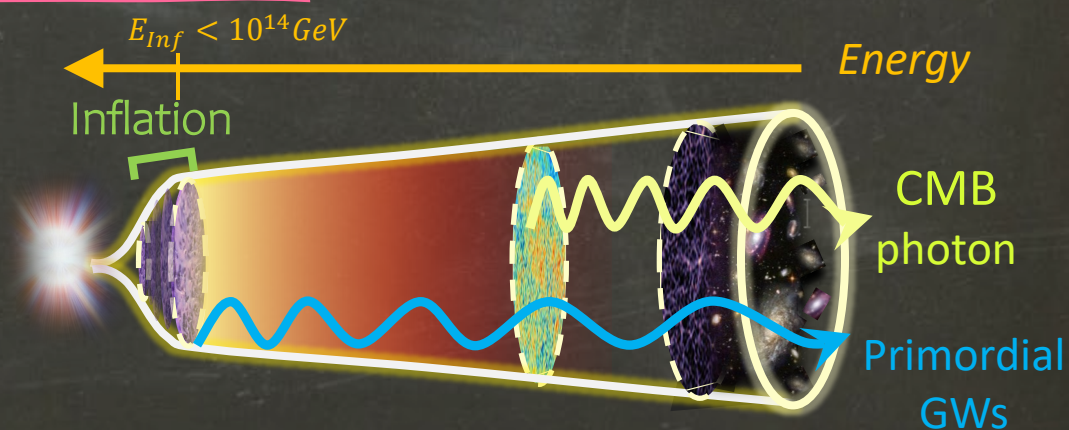


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What about Gauge Fields?!

- Inflation happened at highest energy scales observable!
- They are building blocks of particle physics, SM & beyond.
- What do they do in inflation?!

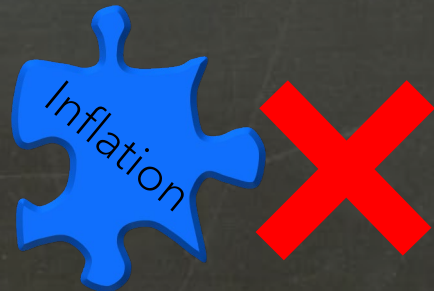


I) Axion-inflation & gauge fields (non-Abelian)

Challenges:

Gauge fields given by Yang-Mills

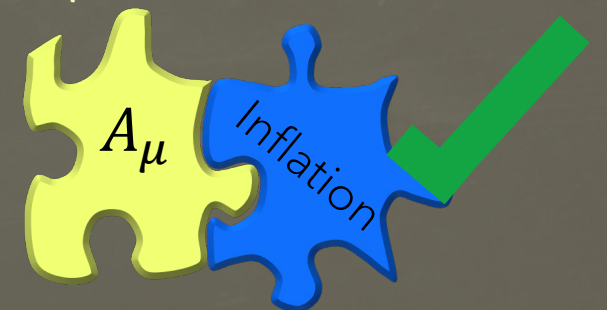
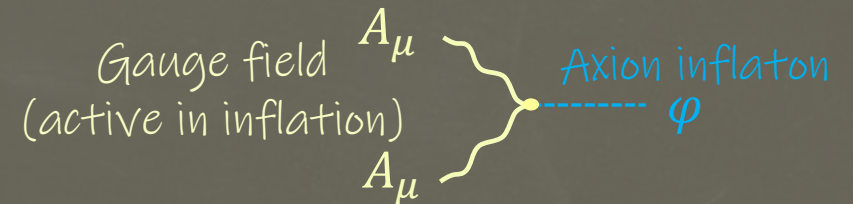
dilutes like radiation $A_\mu \sim 1/a$



Gauge fields coupled to inflaton
are generated in inflation.

$$\frac{\lambda}{8f} F \tilde{F} \varphi \quad \text{Axion}$$

(Axion fields are naturally
coupled to gauge fields.)



Challenges:

Gauge fields given by Yang-Mills

dilutes like radiation $A_\mu \sim 1/a$

Spatial isotropy & homogeneity

U(1) vacuum A_μ

$$A_i = Q(t) \delta_i^3$$



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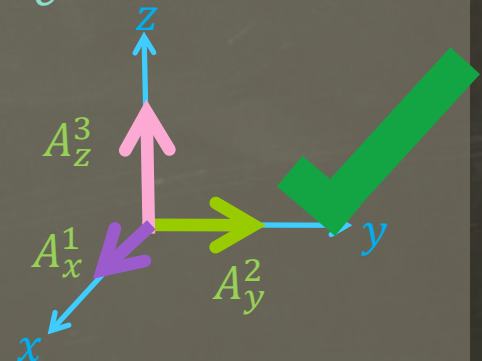
A.M. & Sheikh-Jabbari, 2011

$$\text{SU(2) vacuum } A_\mu = A_\mu^a T_a$$

$$[T_a, T_b] = i \varepsilon^{abc} T_c$$

Spatially isotropic

$$A_i^a = Q(t) \delta_i^a$$



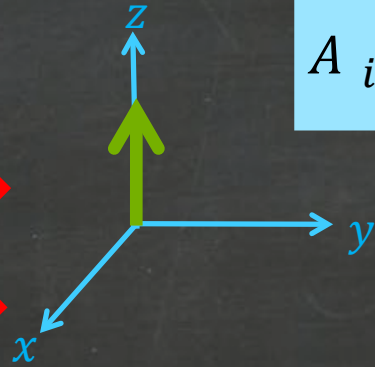
so(3) & su(2) are isomorphic

How SU(2) restores isotropy?

Let us work in temporal gauge, $A_0 = 0$.

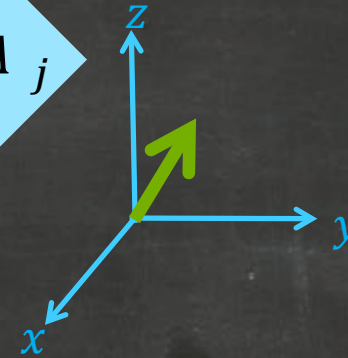
U(1) vacuum A_μ

$$A_i = Q(t)\delta_i^3$$



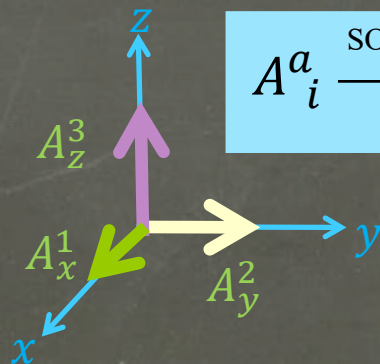
Rotation

$$A_i \xrightarrow{SO(3)} R_{ij} A_j$$



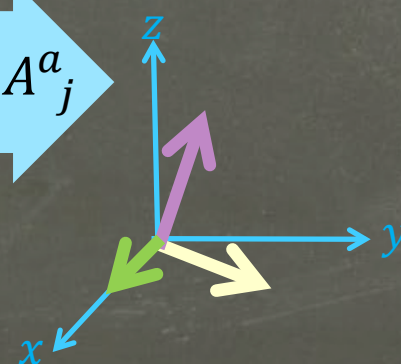
SU(2) VEV, $A_\mu = A_\mu^a T_a$

$$A_i^a = Q(t)\delta_i^a$$



Rotation

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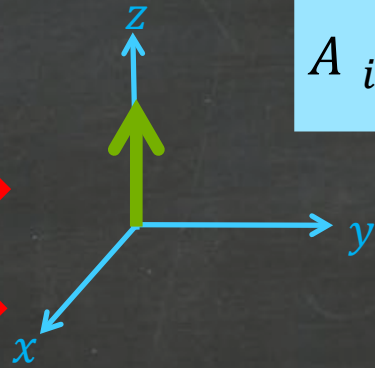


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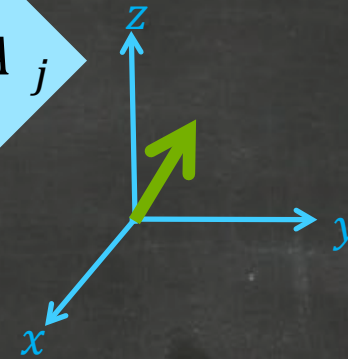
U(1) vacuum A_μ

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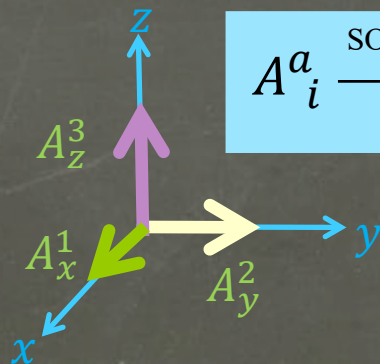
Rotation

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SU(2) VEV, $A_\mu = A_\mu^a T_a$

$$A_i^a = Q(t)\delta_i^a$$

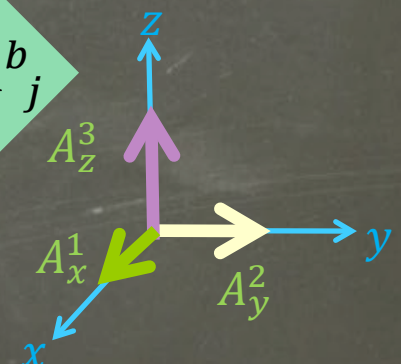
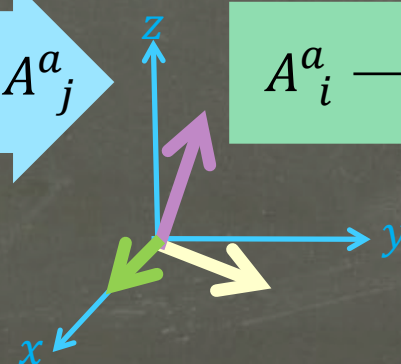


Rotation

$$A_i^a \xrightarrow{SO(3)} R_{ij} A_j^a$$

Gauge Transformation

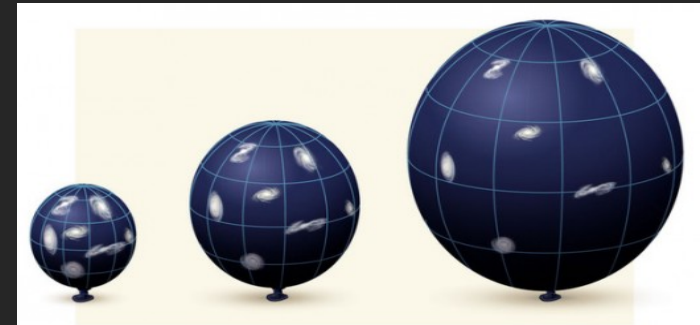
$$A_i^a \rightarrow R_{ab} A_j^b$$



SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$

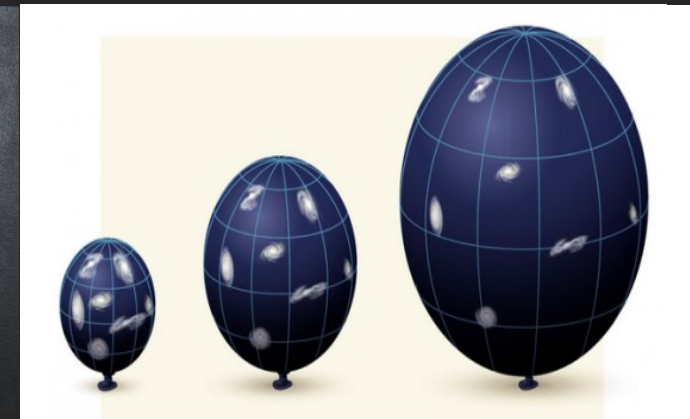
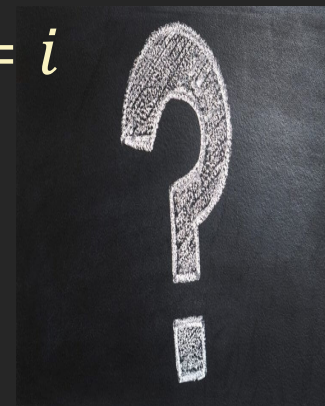


Isotropic
Background

- How stable is the isotropic ansatz against **initial anisotropies**, i.e. Bianchi

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_j^a e^{\lambda_{ij}(t)} & \mu = i \end{cases}$$

Anisotropies in gauge field $Tr[\lambda_{ij}(t)] = 0$

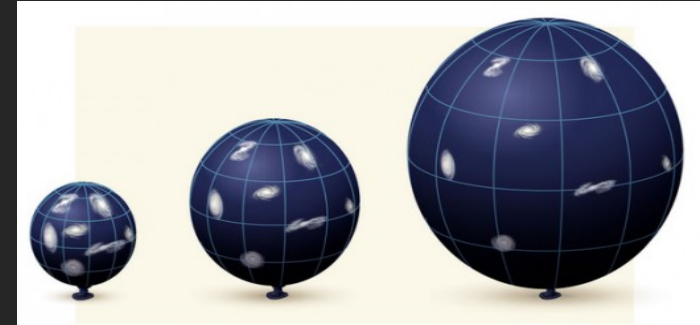


Anisotropic
Background

SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$



- How stable is the isotropic ansatz against **initial anisotropies**, i.e. Bianchi

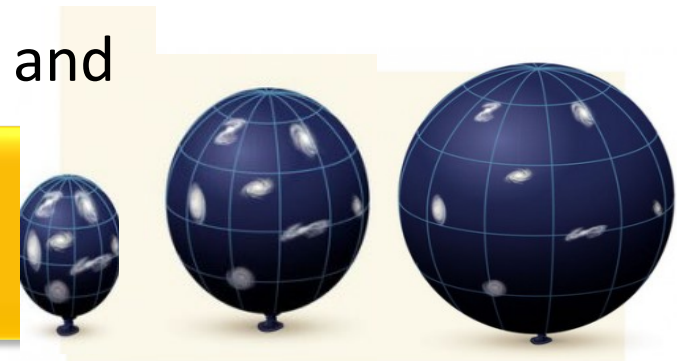
Background
Isotropic

I. Wolfson, A. M., T. Murata, E. Komatsu, T. Kobayashi arXiv:2105.06259

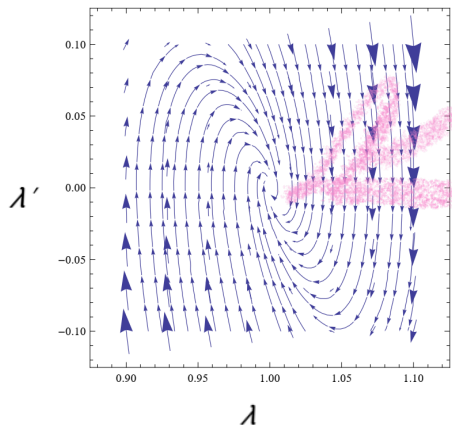
Axion is only coupled to the isotropic part of the gauge field,

Anisotropic part decays like radiation and

**Isotropic Solution is the
Attractor!**



Background
~~Anisotropic~~



A. M. and M.M. Sheikh-Jabbari, J. Soda, 2012
A. M. and E. Erfani, 2013

SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right) \quad \mathcal{S} = -\mathcal{P}$$

- **Chromo-natural** P. Adshead, M. Wyman, 2012

$$S_{cn} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} \left((\partial_\mu \varphi)^2 - \mu^4 \left(1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Natural inflation

Friction

K. Freese, J. A. Frieman and A. V. Olinto 1990

SU(2)-Axion Model Building

- **Gauge-flation**

A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

Ruled-out by the data

R. Namba, E. Dimastrogiovanni, M. Peloso 2013

P. Adshead, E. Martinec, M. Wyman 2013

+ Theoretical issue:
Very large $\lambda \sim 100!$

D. Baumann & L. McAllister 2014

- **Chromo-natural**

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$$S_{cn} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} \left((\partial_\mu \varphi)^2 - \mu^4 \left(1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Inspired by them, several different models with SU(2) fields have been proposed & studied.

An incomplete list of Different Realizations of the SU(2)-Axion Inflation:

1. **A. M.** and M. M. Sheikh-Jabbari, Phys. Rev. D 84:043515, 2011 [[arXiv:1102.1513](#)]
2. P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [[arXiv:1202.2366](#)]
3. **A. M.** JHEP 07 (2016) 104 [[arXiv:1604.03327](#)]
4. C. M. Nieto and Y. Rodriguez Mod. Phys. Lett. A31 (2016) [[arXiv:1602.07197](#)]
5. E. Dimastrogiovanni, M. Fasiello, and T. Fujita JCAP 1701 (2017) [[arXiv:1608.04216](#)]
6. P. Adshead, E. Martinec, E. I. Sfakianakis, and M. Wyman JHEP 12 (2016) 137 [[arXiv:1609.04025](#)]
7. P. Adshead and E. I. Sfakianakis JHEP 08 (2017) 130 [[arXiv:1705.03024](#)]
8. R. R. Caldwell and C. Devulder Phys. Rev. D97 (2018) [[arXiv:1706.03765](#)]
9. E. McDonough, S. Alexander, JCAP11 (2018) 030 [[arXiv:1806.05684](#)]
10. L. Mirzaghali, E. Komatsu, K. D. Lozanov, and Y. Watanabe, [[arXiv:2003.04350](#)]
11. Y. Watanabe, E. Komatsu, [[arXiv:2004.04350](#)]
12. J. Holland, I. Zavala, G. Tasinato, [[arXiv:2009.00653](#)]
13. **A. M.** **SU(2)R –axion inflation** [[arXiv:2012.11516](#)]
14. Oksana Iarygina, Evangelos I. Sfakianakis, [[arXiv:2105.06972](#)]
15. T. Fujita, Nakatsuka, K. Mukaida, & K. Murai [[arXiv:2110.03228](#)]

SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

Ruled-out by the data

R. Namba, E. Dimastrogiovanni, M. Peloso 2013
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SU(2)-Axion inflation has a very rich phenomenology:

- *A new mechanism for generation of Primordial Gravitational Waves*
- *All Sakharov conditions are satisfied in inflation: a new baryogenesis mechanism*
- *Particle Production in inflation by Schwinger effect and chiral anomaly*

P. Adshead et. al 2013

Dimastrogiovanni et. al 2013

A. M. et. al, 2013

A. M. 2014 & A.M. 2016

R. Caldwell et. al 2017

A. M. 2021

K. Lozanov, **A. M.**, E. Komatsu 2017,

L. Mirzagholi, **A. M.**, K. Lozanov 2019,

Domcke et al 2019, **A.M. 2019**

SU(2)-Axion Model Building

- Gauge-flation A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

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- Minimal Scenario of **SU(2)-axion inflation** A. M., 2016 $f < 0.1 M_{\text{pl}}$ & $\lambda < 0.1$

$$S_{AM} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} \left((\partial_\mu \varphi)^2 - V(\varphi) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Axion Monodromy or any mechanism that gives a flat potential

New Tensorial mode in SU(2) Gauge Field

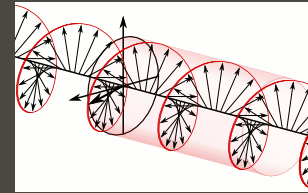
$$\bullet \delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$$

$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

(δ_c and $\frac{m^2}{H^2}$ are given by BG)

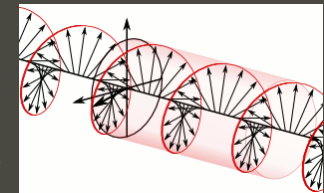
Right-handed

Circular polarizations



B_+

Left-handed



B_-

B_{\pm} is a new tensorial mode in the perturbed SU(2) gauge field!

A.M. & Sheikh-Jabbari, 2011

New Tensorial mode in SU(2) Gauge Field

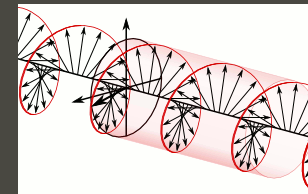
- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

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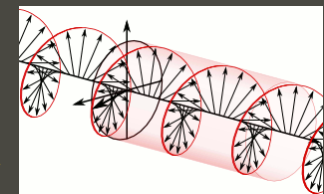
Right-handed

Circular polarizations



B_+

Left-handed



B_-

Vacuum structure

Axion field $\langle \varphi \rangle$

$(\delta_c > 0)$

Slow-roll A

$\langle \delta_a^i A_i^a \rangle$

Slow-roll A_p

Parity

$(\delta_c < 0)$

B_{\pm} is a new tensorial mode in the perturbed SU(2) gauge field!

A.M. & Sheikh-Jabbari, 2011

New Tensorial mode in SU(2) Gauge Field

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

(δ_c and $\frac{m^2}{H^2}$ are given by BG)

For $\delta_c > 0$

Short tachyonic growth of B_+



Chiral Field

$$n_B \sim \frac{H^3}{6\pi^2} \delta_c^3 e^{\frac{(2-\sqrt{2})\pi}{2} \delta_c}$$

Particle Production

A. M. and E. Komatsu, 2018

Vacuum structure

Axion field $\langle \phi \rangle$

($\delta_c > 0$)

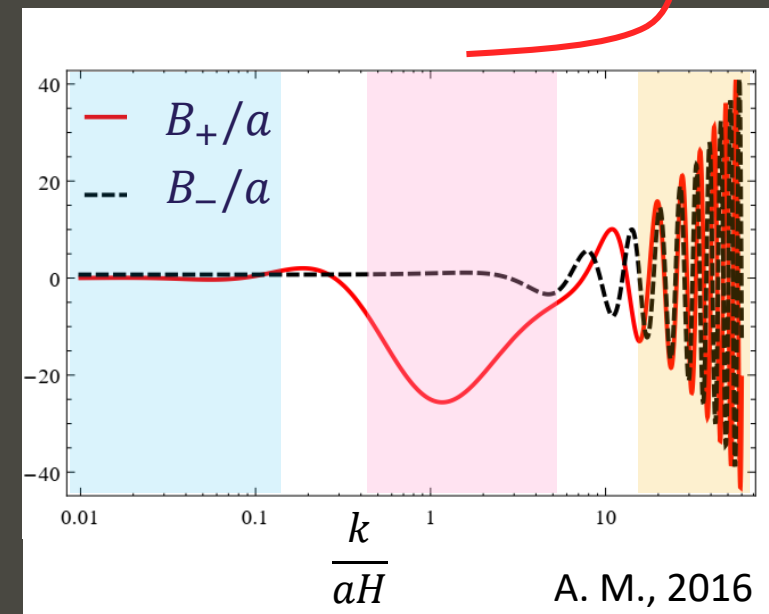
Slow-roll A

$\langle \delta_a^i A_i^a \rangle$

Slow-roll A_p

Parity

($\delta_c < 0$)



A. M., 2016

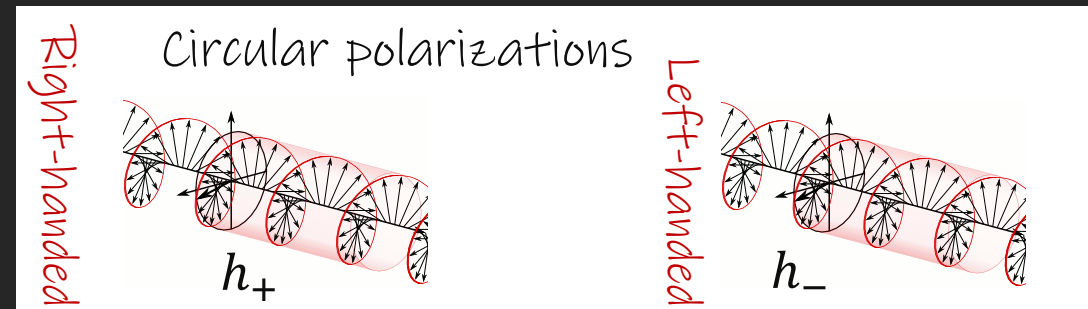
Gauge Field sources Primordial GWs

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$
- The field equation: $B_{\pm}'' + [k^2 \mp \delta_C k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a}] B_{\pm} \approx 0$



- That sourced the GWs

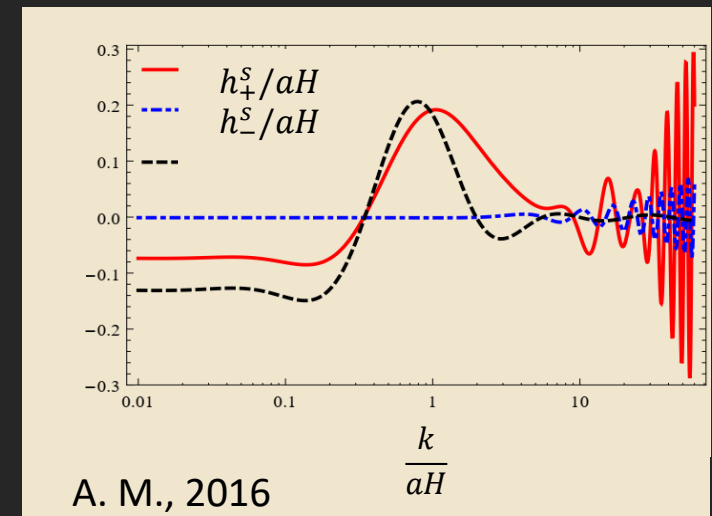
$$h_{\pm}'' + [k^2 - \frac{a''}{a}] h_{\pm} = \mathcal{H}^2 \Pi_{\pm}[B_{\pm}]$$



- Gravitational waves have two uncorrelated terms



$$h_{\pm} = \underbrace{h_{\pm}^{vac}}_{\substack{\text{Vacuum} \\ \text{GWs} \\ \text{unpolarized} \\ h_+^{vac} = h_-^{vac}}} + \underbrace{h_{\pm}^s}_{\substack{\text{Sourced by} \\ B_{\pm} \\ \text{Polarized} \\ h_+^s \neq h_-^s}}$$



Novel Observable Signature: CMB

- The sourced tensor modes is Highly non-Gaussian.

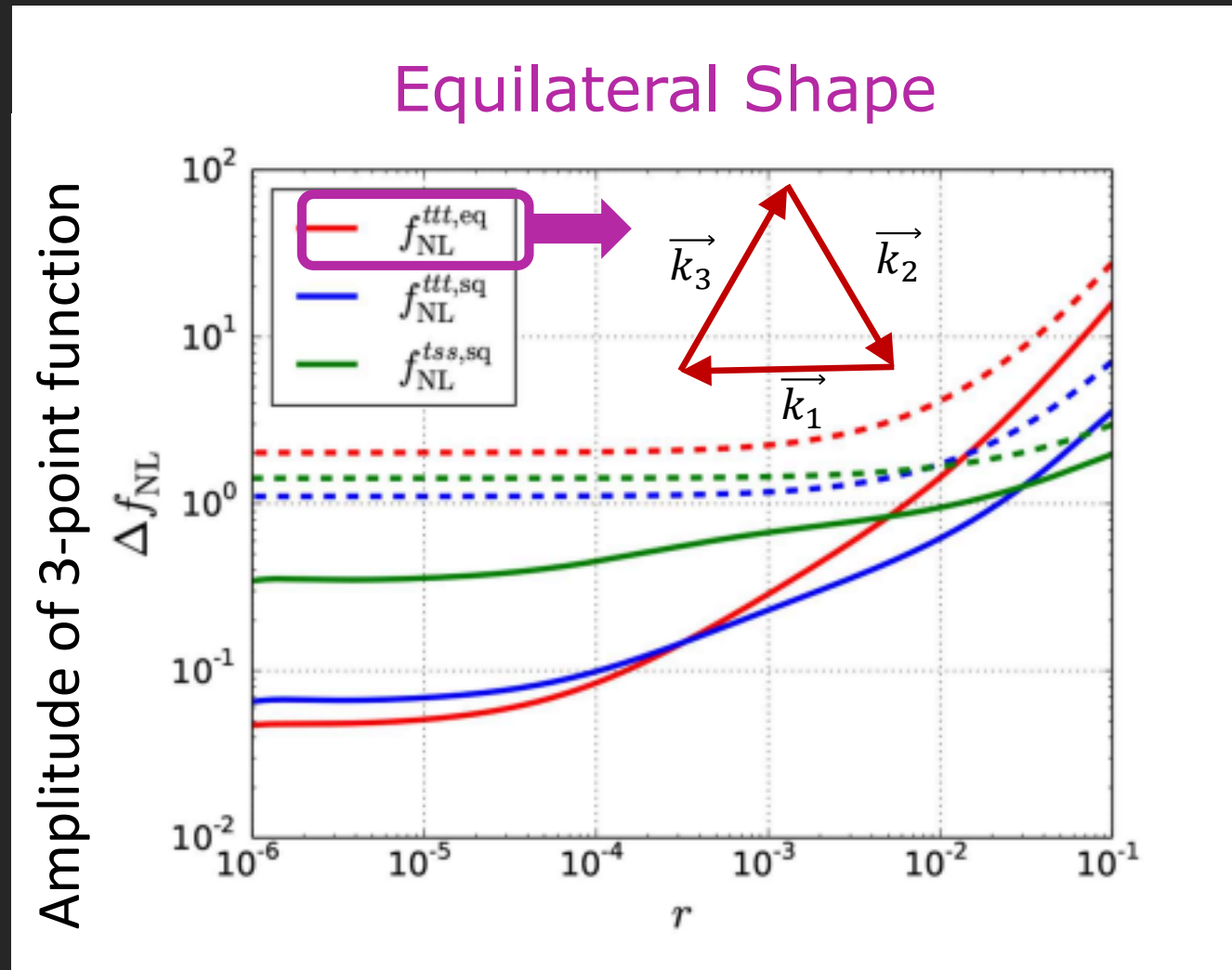
$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - \underbrace{ig [A_\mu, A_\nu]}_{\text{Self-interaction}}$$

Agrawal, Fujita, Komatsu 2018

- That can be probe with future CMB missions., e.g. *Litebird*

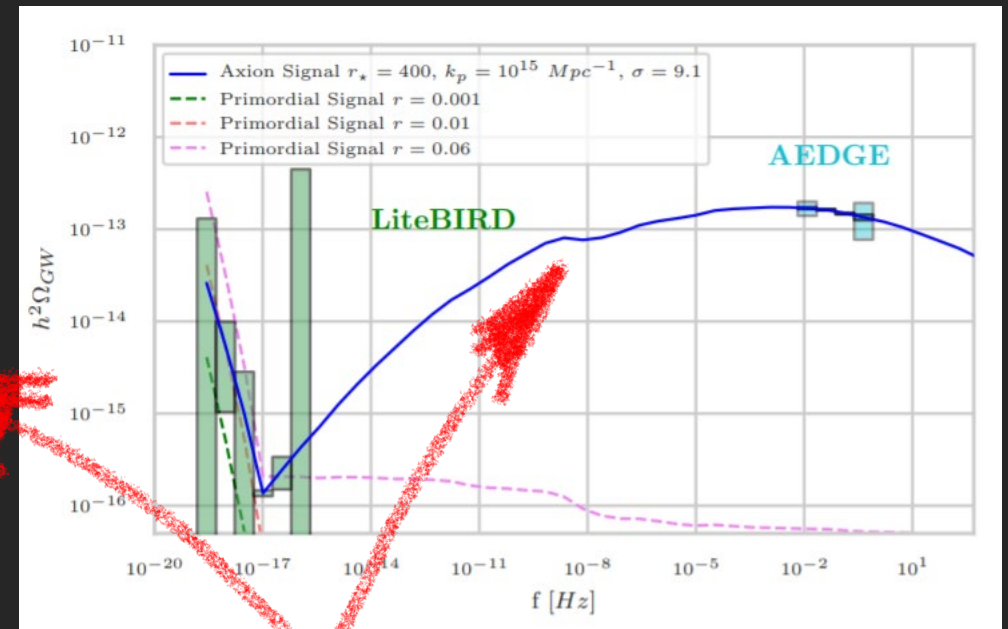
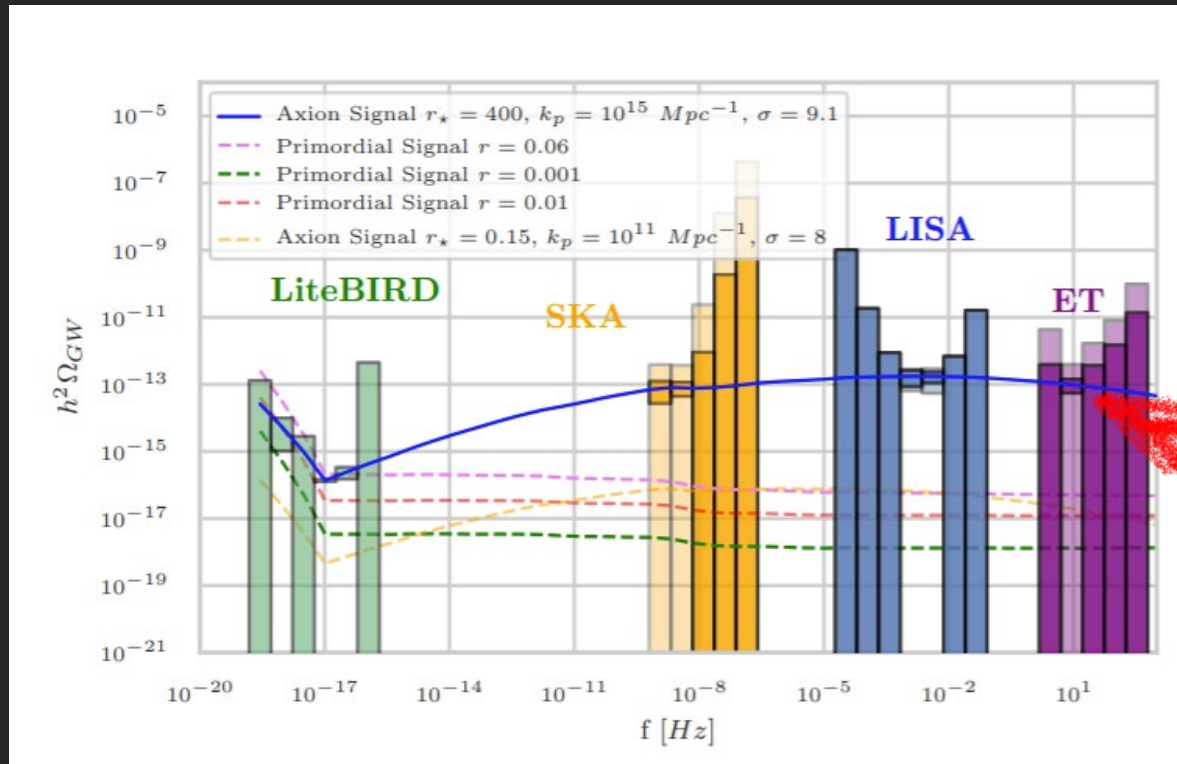


and *CMB-S4*!



Novel Observable Signature: Beyond CMB

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.

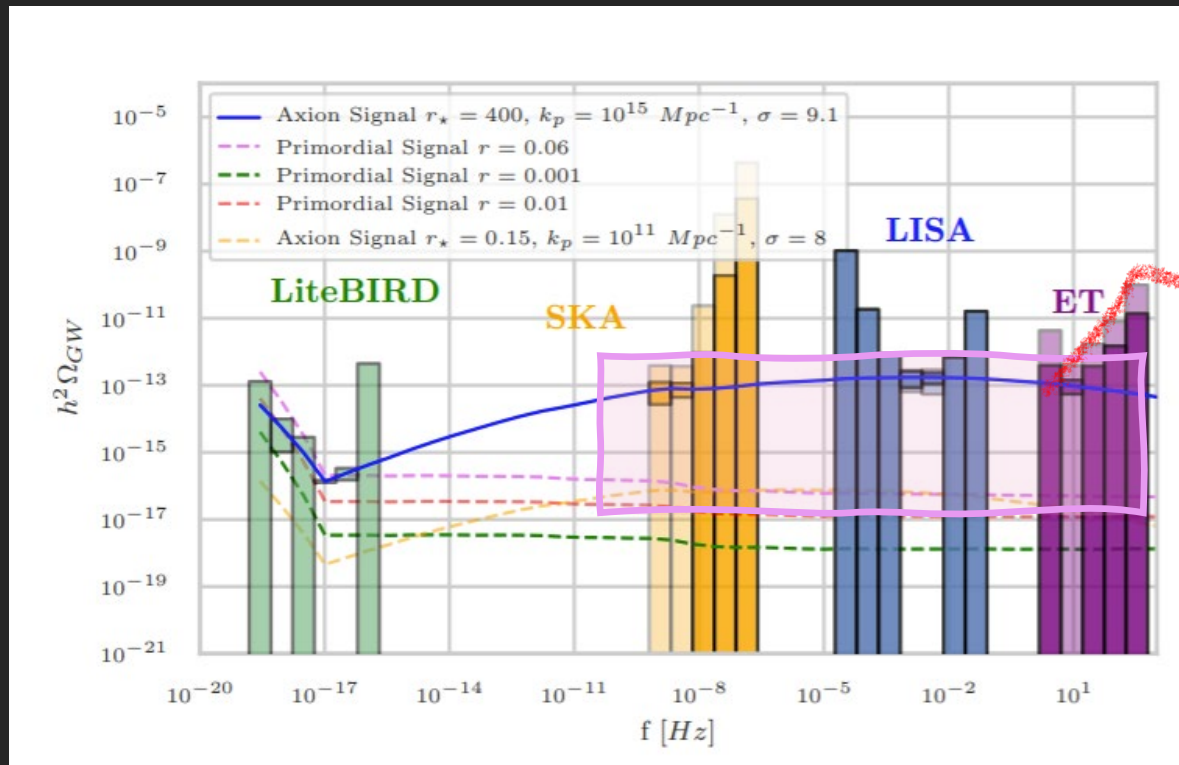


P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

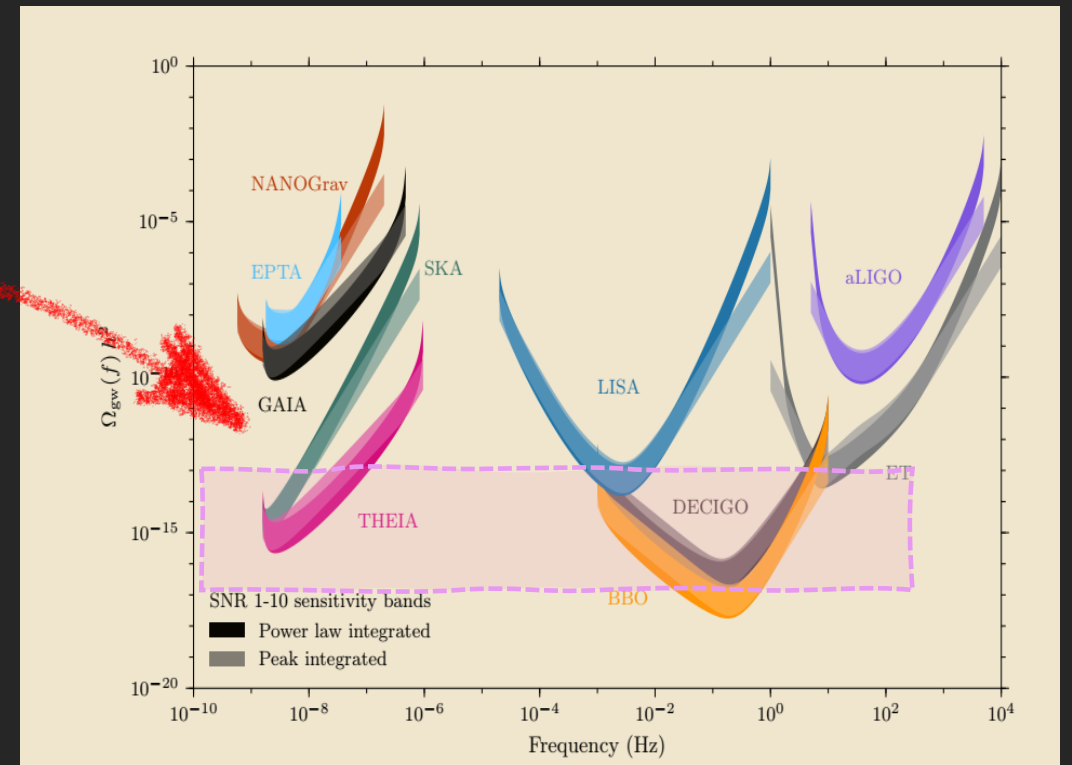
New Physics

Novel Observable Signature: Beyond CMB

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

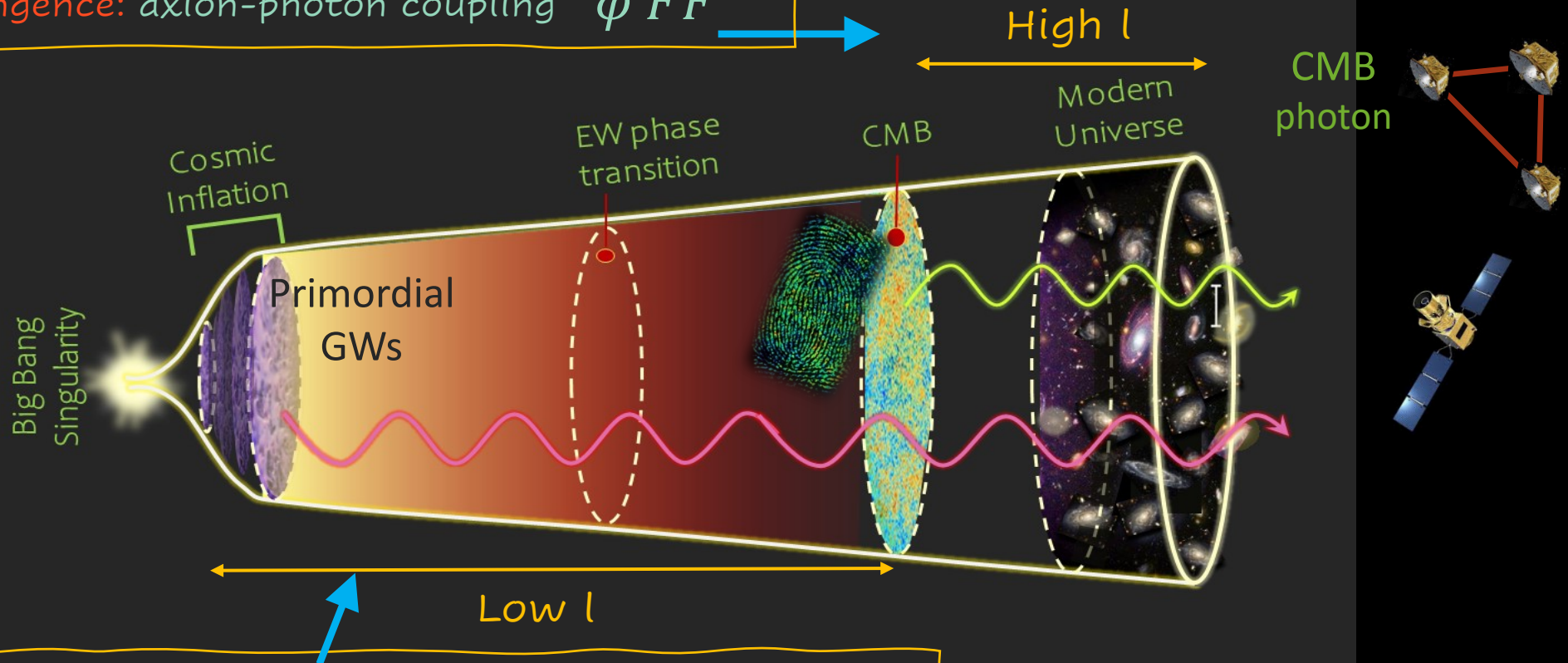


J. Garcia-Bellido, H. Murayama, and G. White 2021

Parity Odd CMB Correlations: TB & EB $\neq 0$

Sources of Parity violation on CMB:

- Cosmic Birefringence: axion-photon coupling $\varphi F\tilde{F}$



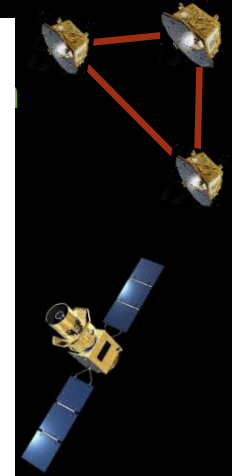
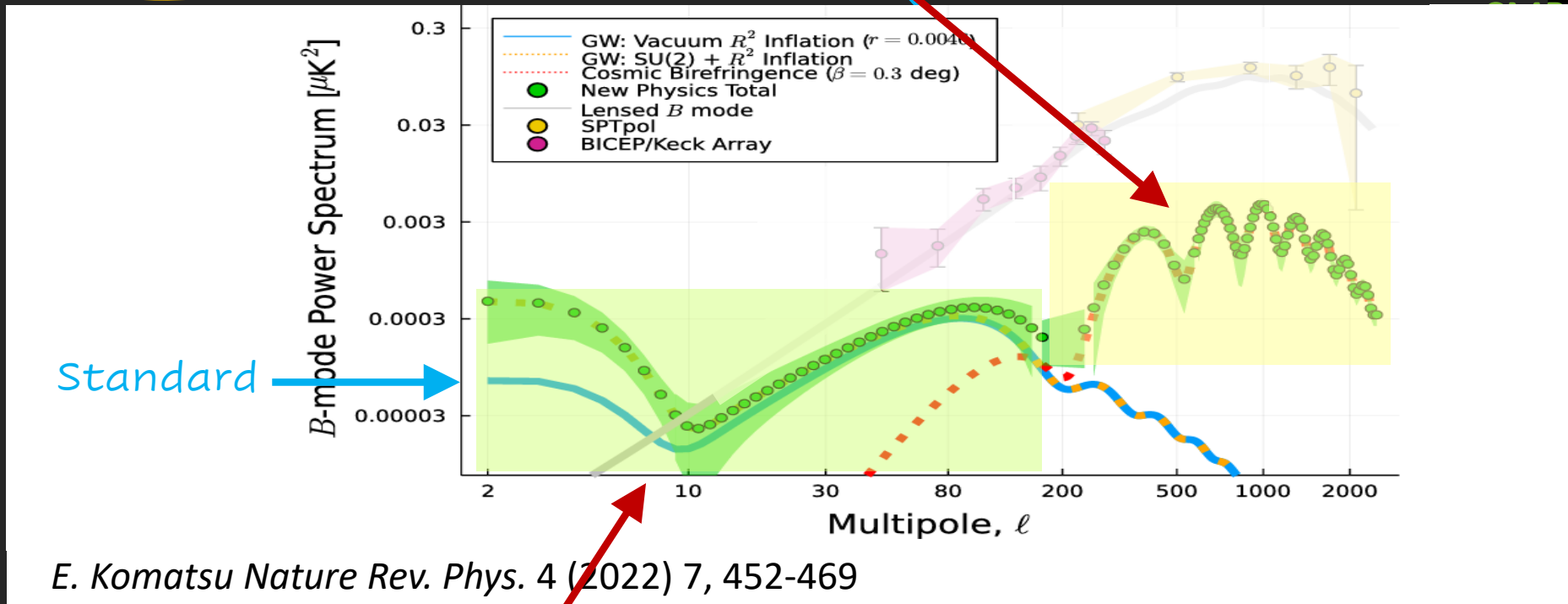
- SU(2)-axion Inflation: SU(2) field-Graviton coupling

- Gravitational Chern-Simons: axion-graviton coupling $\varphi R\tilde{R}$

Parity Odd CMB Correlations: TB & EB $\neq 0$

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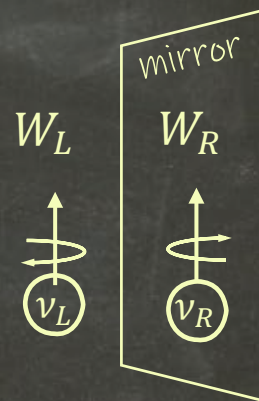


- SU(2)-axion Inflation: SU(2) field-Graviton coupling

- Gravitational Chern-Simons: axion-graviton coupling $\varphi R \tilde{R}$

II) Embedding axion-inflation in Left-Right Symmetric Models

(How to Connect Inflaton to SM?)



How to Connect it to the SM?

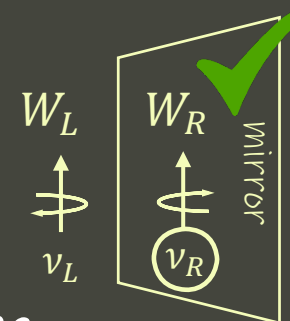
Let us Extend SM Gauge Symmetry by an $SU(2)_R$ and couple it to Axion Inflaton!

- Left-Right Symmetric Model + axion!

$$SU(2)_R \times SU(2)_L \times U(1)_{B-L} \longrightarrow SU(2)_L \times U(1)_Y$$

Left-Right Symmetric

SM Left-handed Weak force



- Minimal Scenario of **SU(2)-axion inflation** A. M., 2016 $f < 0.1 M_{pl}$ & $\lambda < 0.1$

$$S_{AM} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} ((\partial_\mu \varphi)^2 - V(\varphi)) - \frac{\lambda}{8f} \varphi F \tilde{F} \right)$$

Axion Monodromy or any mechanism that gives a flat potential

Gauge field is $SU(2)_R$

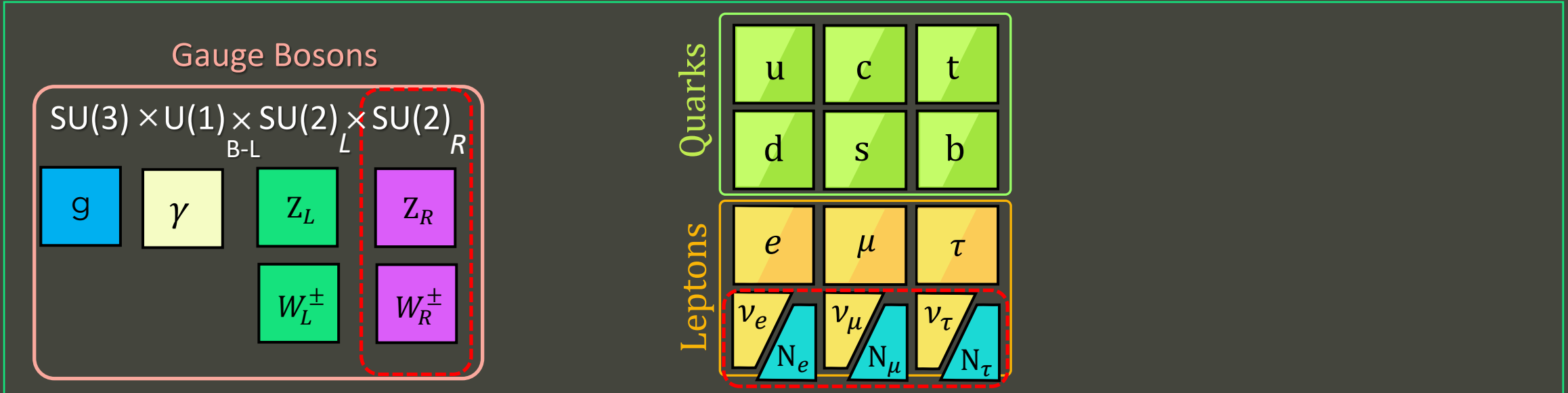
A. M. arXiv: 2012.11516

A.M. arXiv:2103.14611

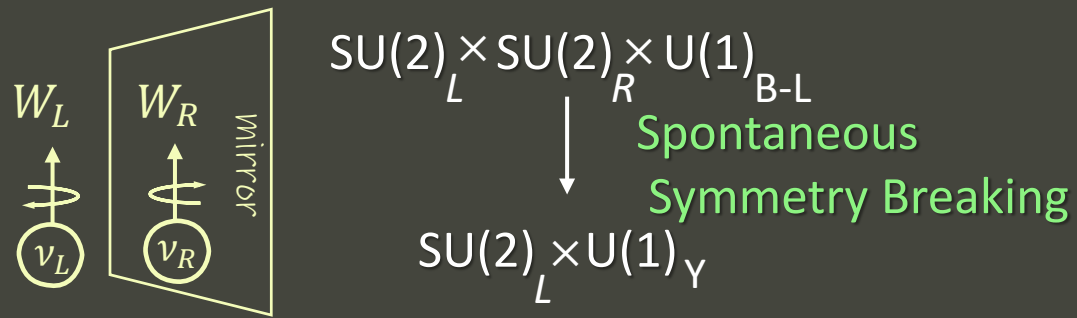
Left-Right Symmetric Model

Minimal Left-Right Symmetric model

- An $SU(2)$ -gauge extension of SM with 3 Right-handed Neutrinos coupled to it.



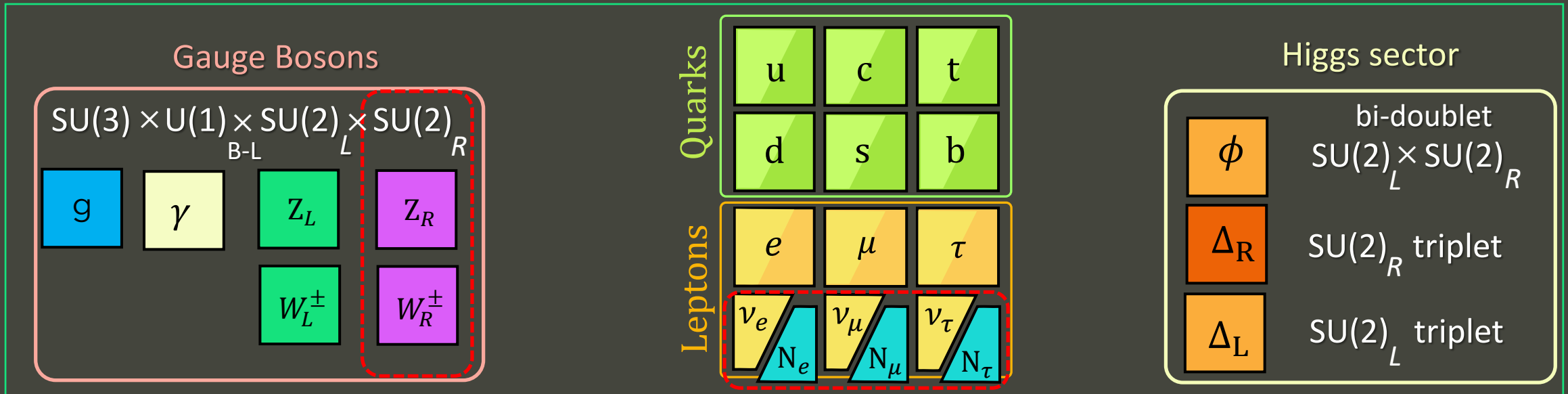
J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)



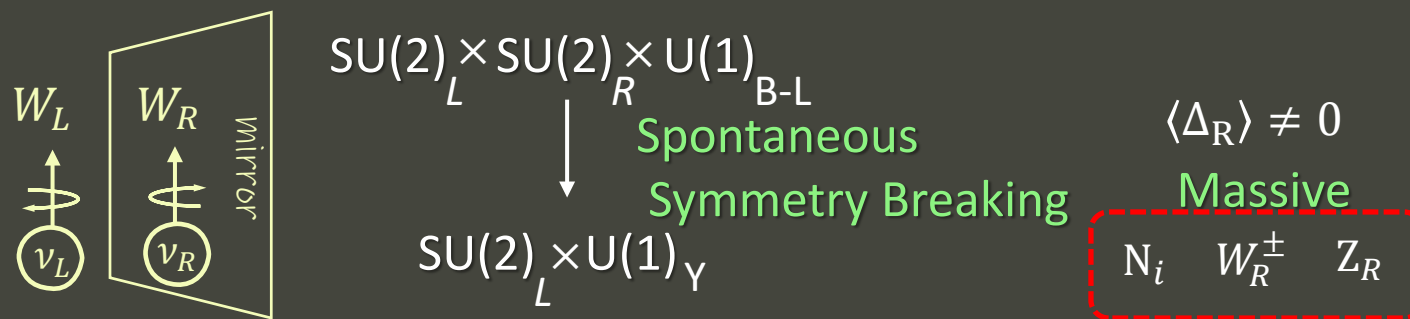
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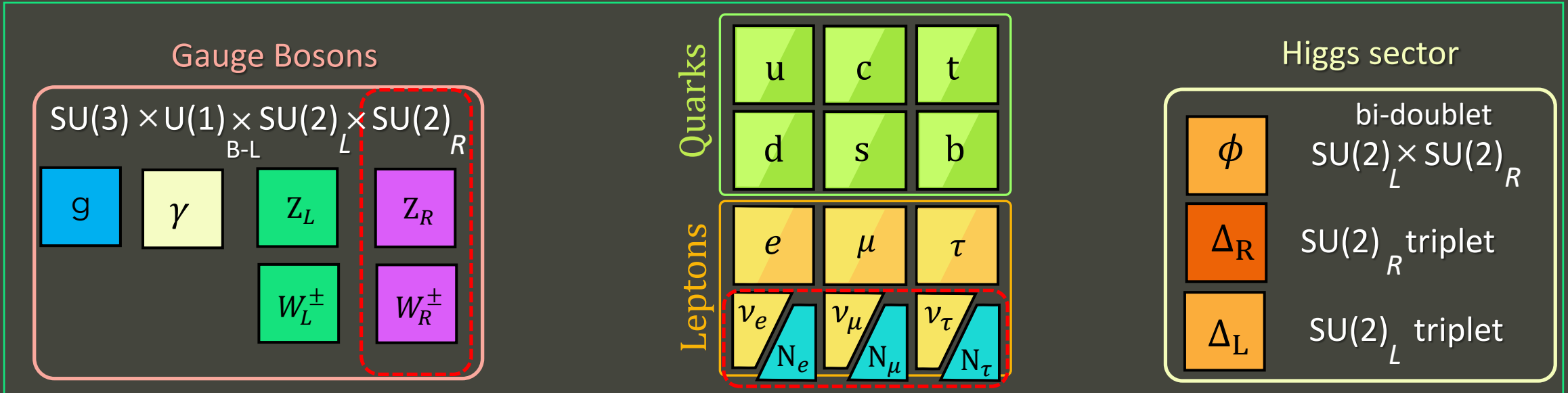
J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)



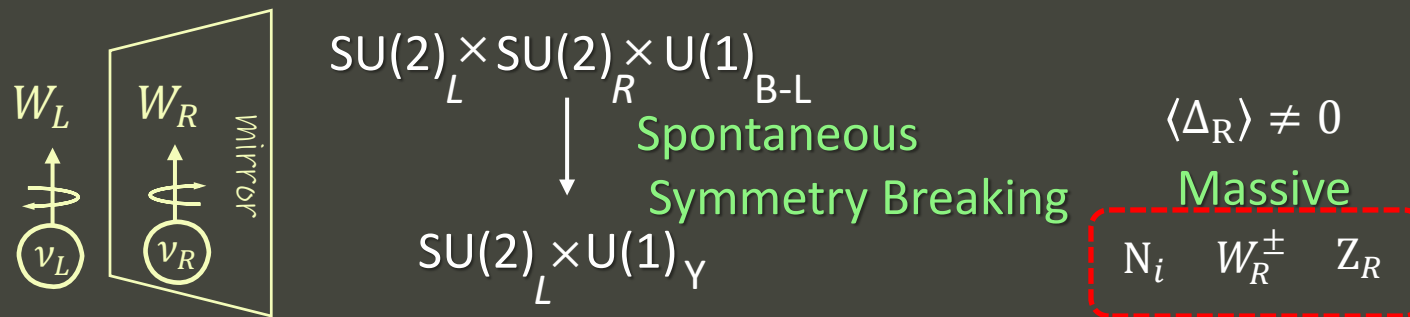
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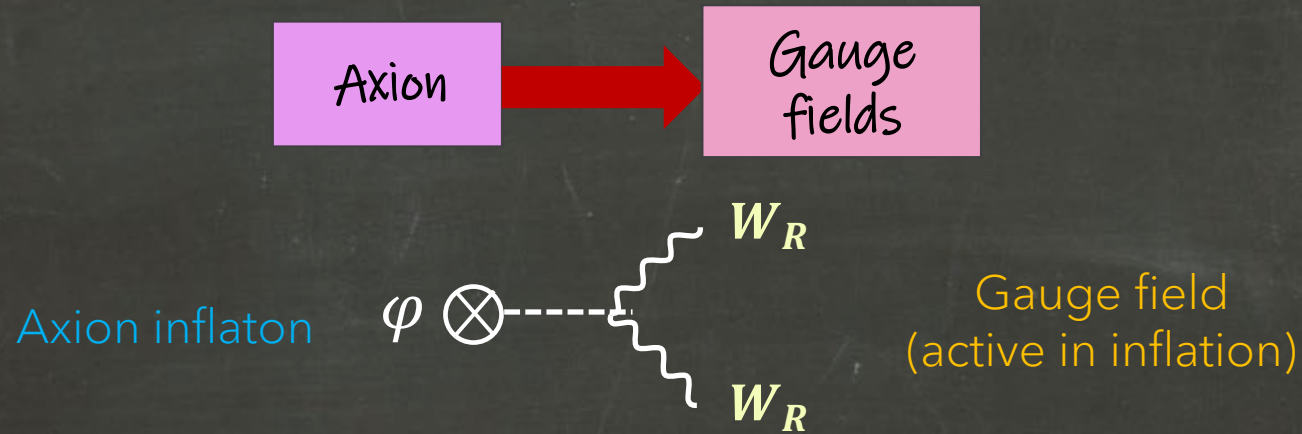
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- Ad hoc parity violation
- Accidental B-L global symmetry
- Vacuum Stability problem

Gauge field Production in Inflation

- SM Gauge fields are diluted by inflation & unimportant, BUT $SU(2)_R$:



SU(2)_R Gauge Field

- $\delta A_i^a = B_+^a(t, k)e_i^+(\vec{k}) + B_-^a(t, k)e_i^-(\vec{k})$

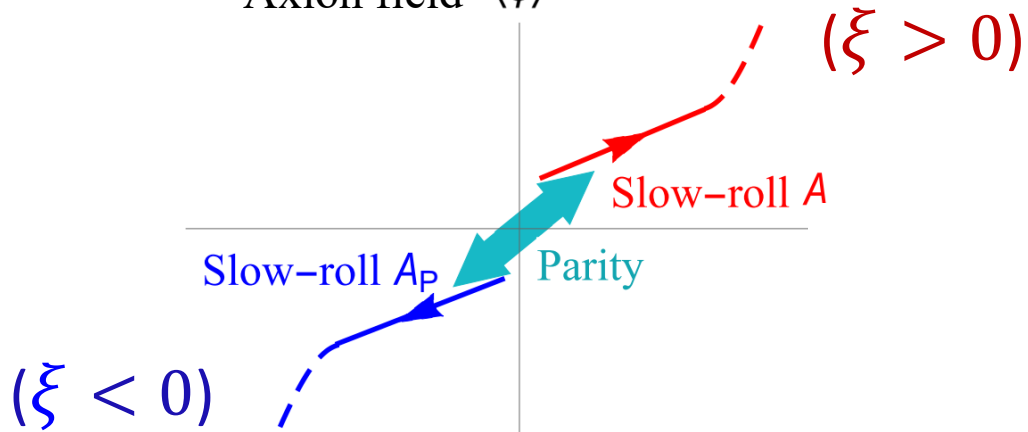
$$B_{\pm}'' + [k^2 \mp \xi k\mathcal{H}] B_{\pm} \approx 0$$

effective frequency

Given by the BG ($\xi = \frac{2\lambda\partial_t\phi}{fH}$)

Vacuum structure

Axion field $\langle\phi\rangle$



For $\xi > 0$

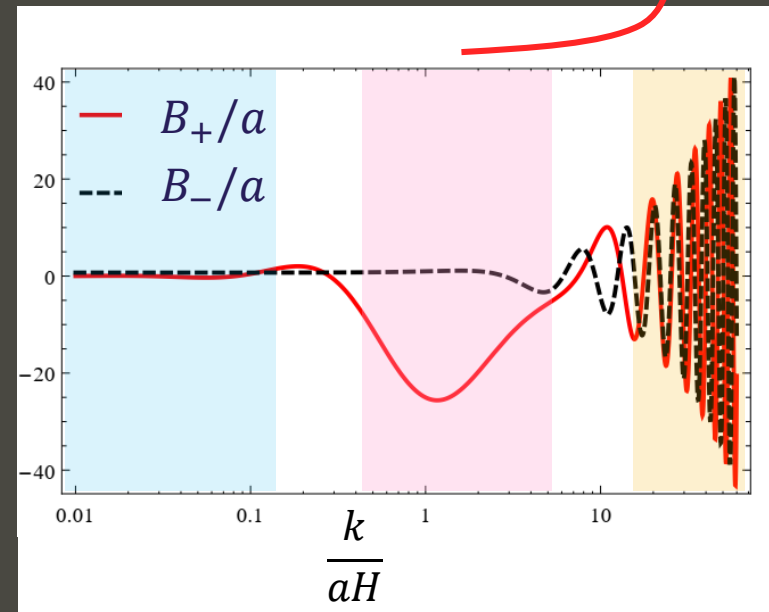
Short tachyonic growth of B_+



Chiral Field

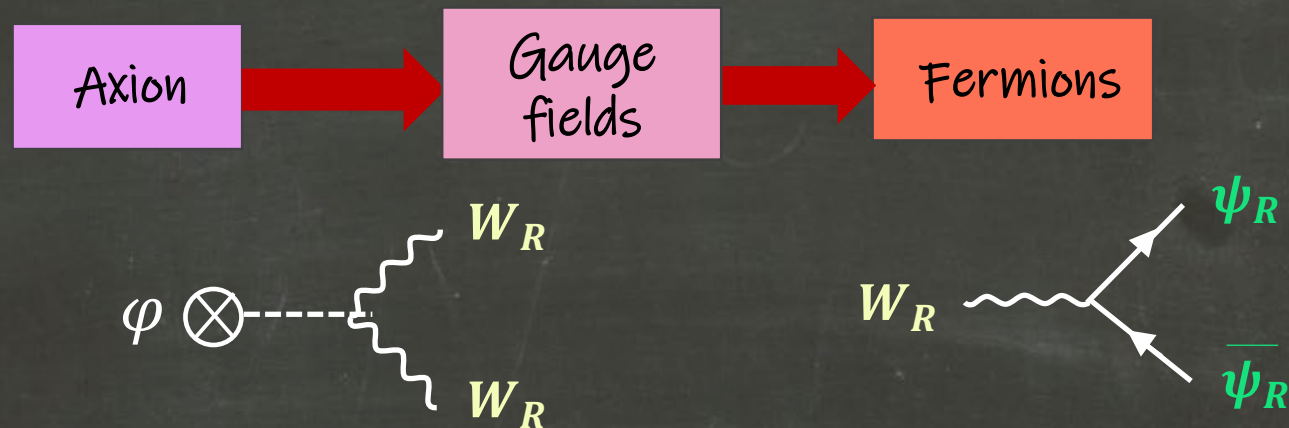
$$n_B \sim \frac{H^3}{6\pi^2} \xi^3 e^{\frac{(2-\sqrt{2})\pi}{2}\xi}$$

Particle Production



Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by $SU(2)_R$ gauge field:

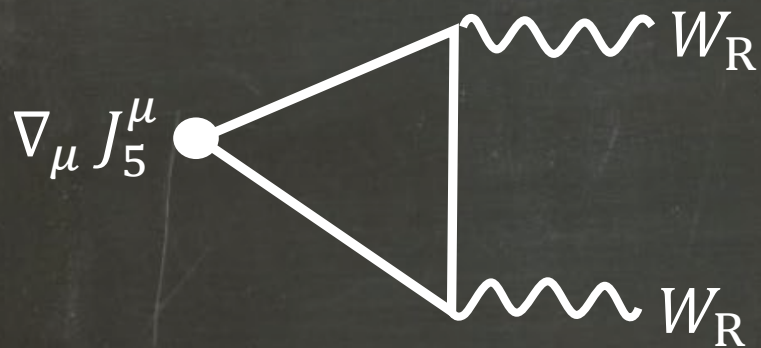


Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by $SU(2)_R$ gauge field:



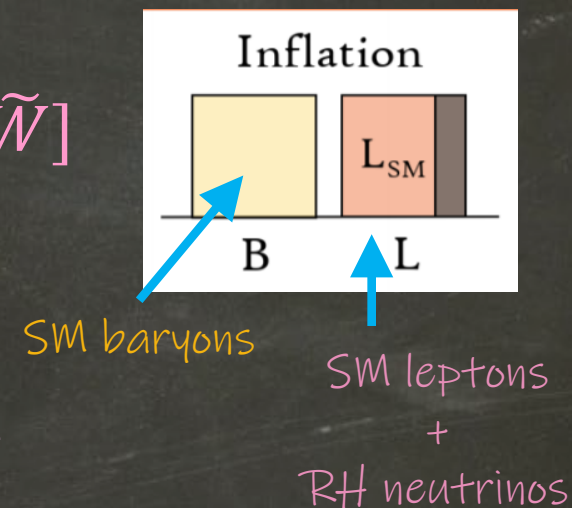
The key ingredient is the Chiral anomaly of $SU(2)_R$ in inflation:



$$\nabla_\mu J_B^\mu = \nabla_\mu J_L^\mu = \frac{g^2}{16\pi^2} \text{tr}[W\tilde{W}]$$

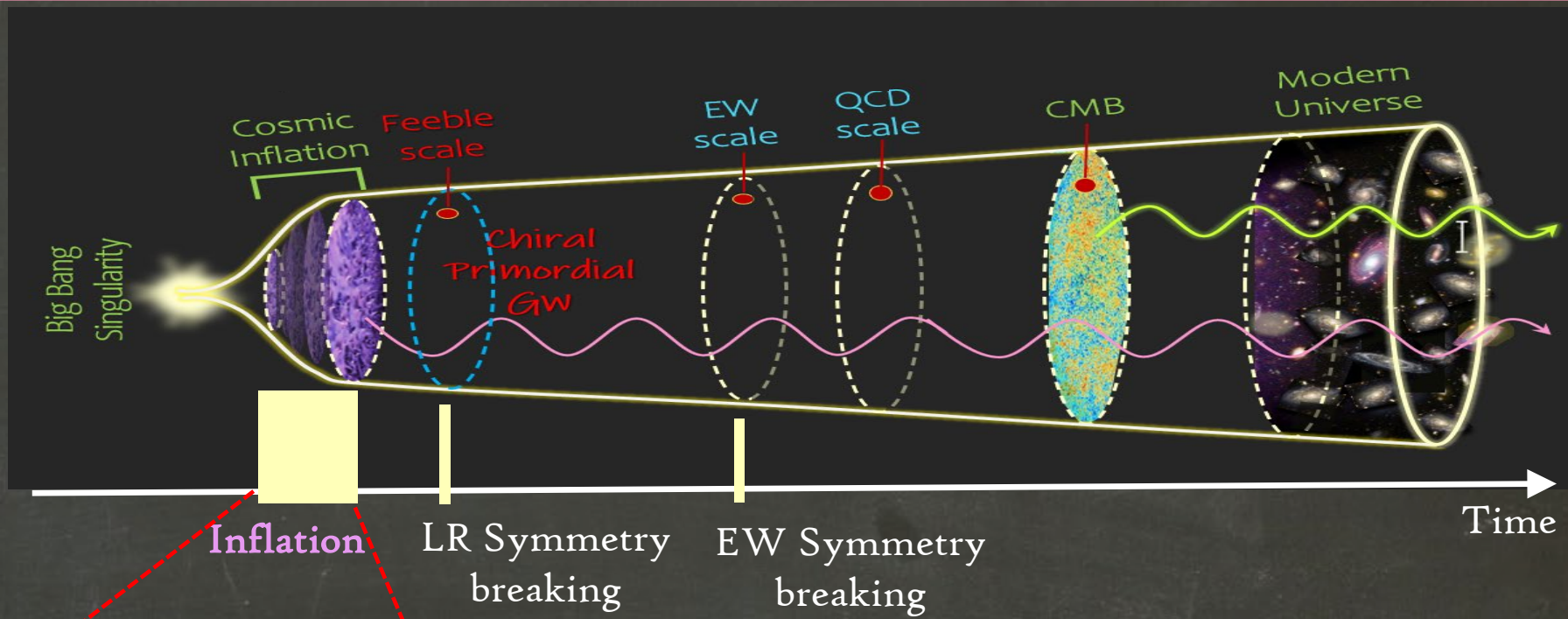
$$n_B = n_L = \alpha_{inf}(\xi) H^3$$

$$\alpha_{inf}(\xi) \sim \frac{g^2}{(2\pi)^4} e^{2\pi\xi}$$

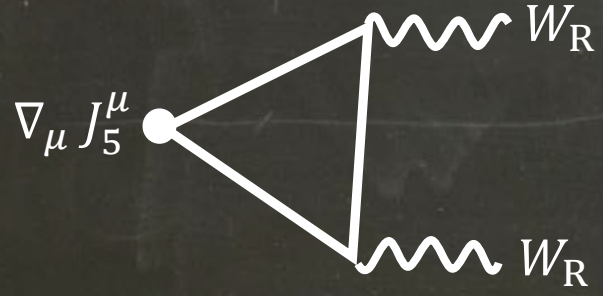


Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	μ	τ
	ν_e	ν_μ	ν_τ
	N_e	N_μ	N_τ



Chiral anomaly of $SU(2)_R$
In inflation



	L _{SM}
B	L

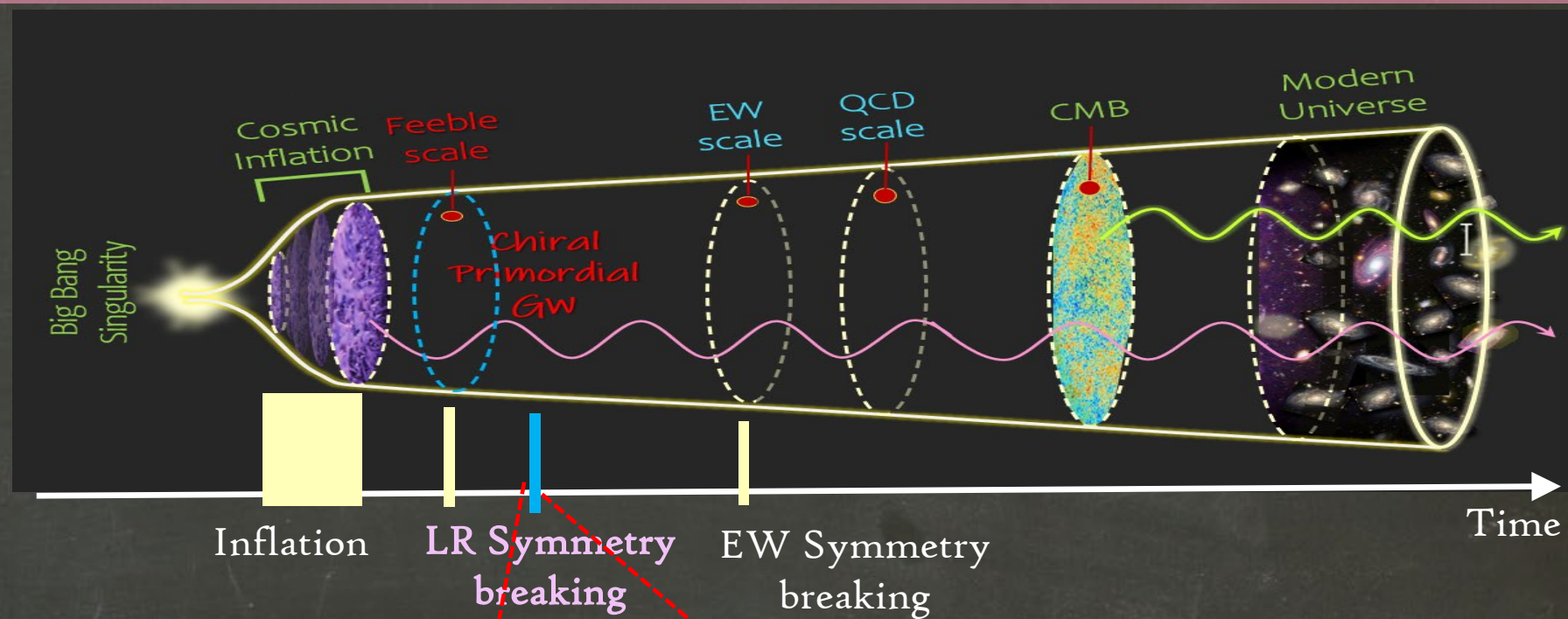
$B = L = 3n_{CS}$
 $B - L_{SM} \neq 0$

B = SM baryons

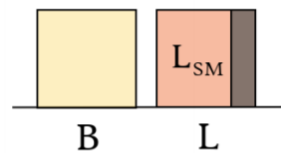
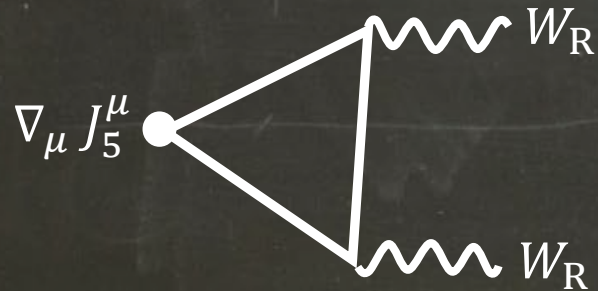
L = SM leptons + RH neutrinos

Summary of the mechanism:

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Leptons	e	μ	τ
	ν_e	ν_μ	ν_τ
	N_e	N_μ	N_τ

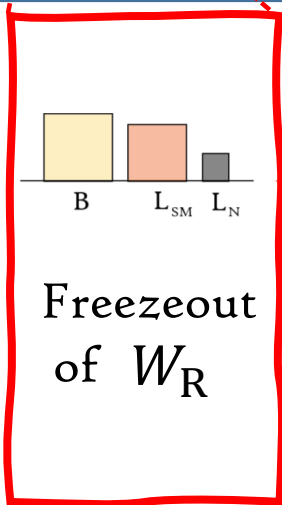
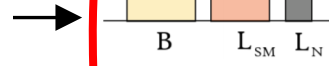


Chiral anomaly of $SU(2)_R$
In inflation



$$B = L = 3n_{CS}$$

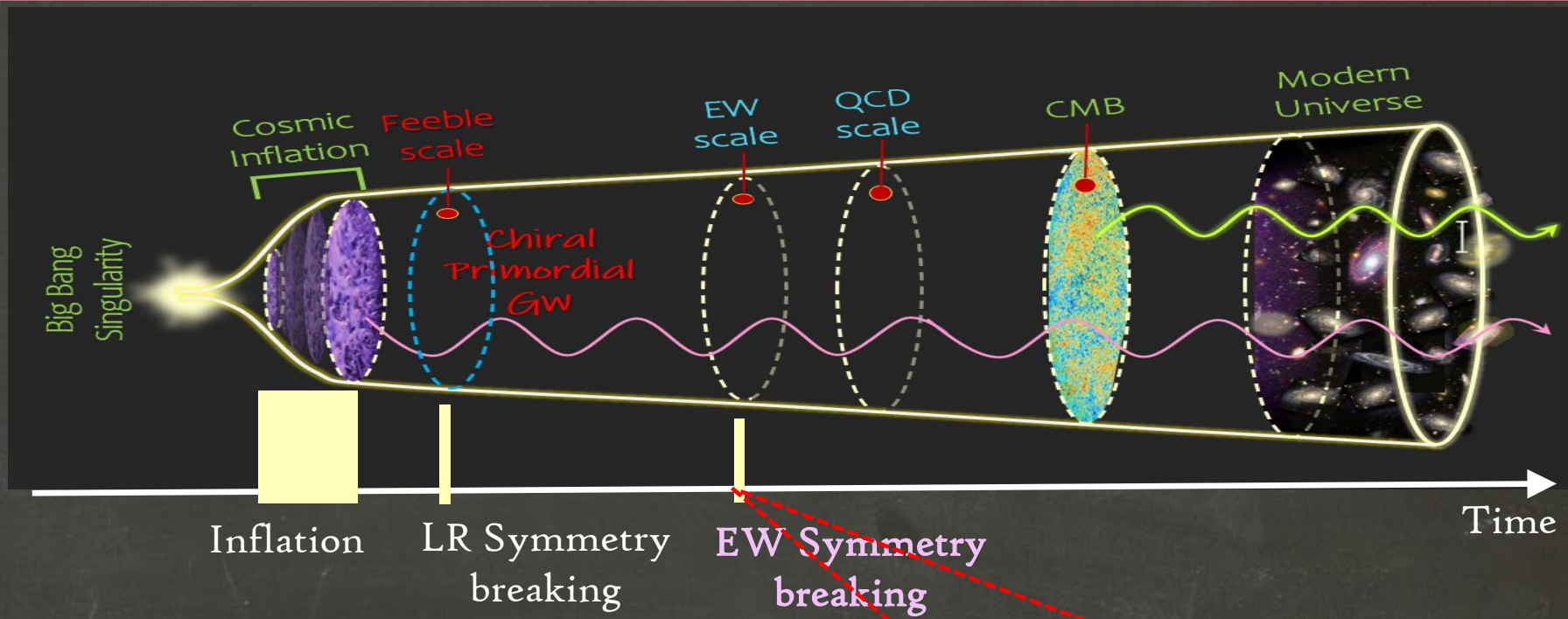
$$B - L_{SM} \neq 0$$



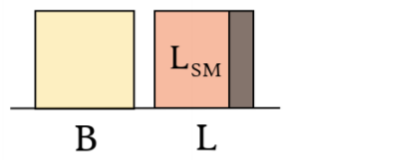
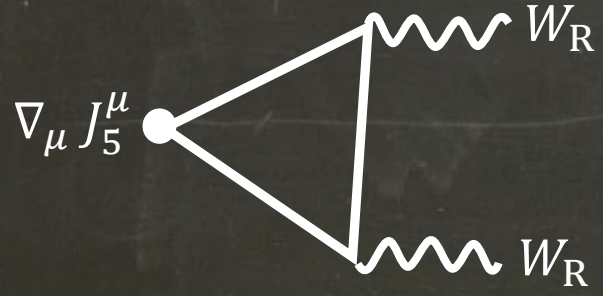
Freezeout
of W_R

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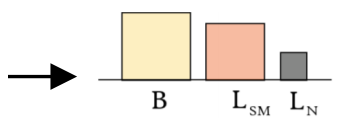


Chiral anomaly of $SU(2)_R$
In inflation

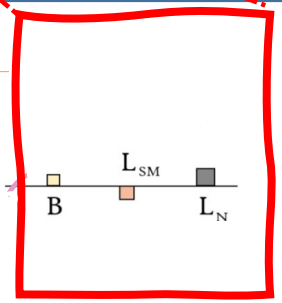


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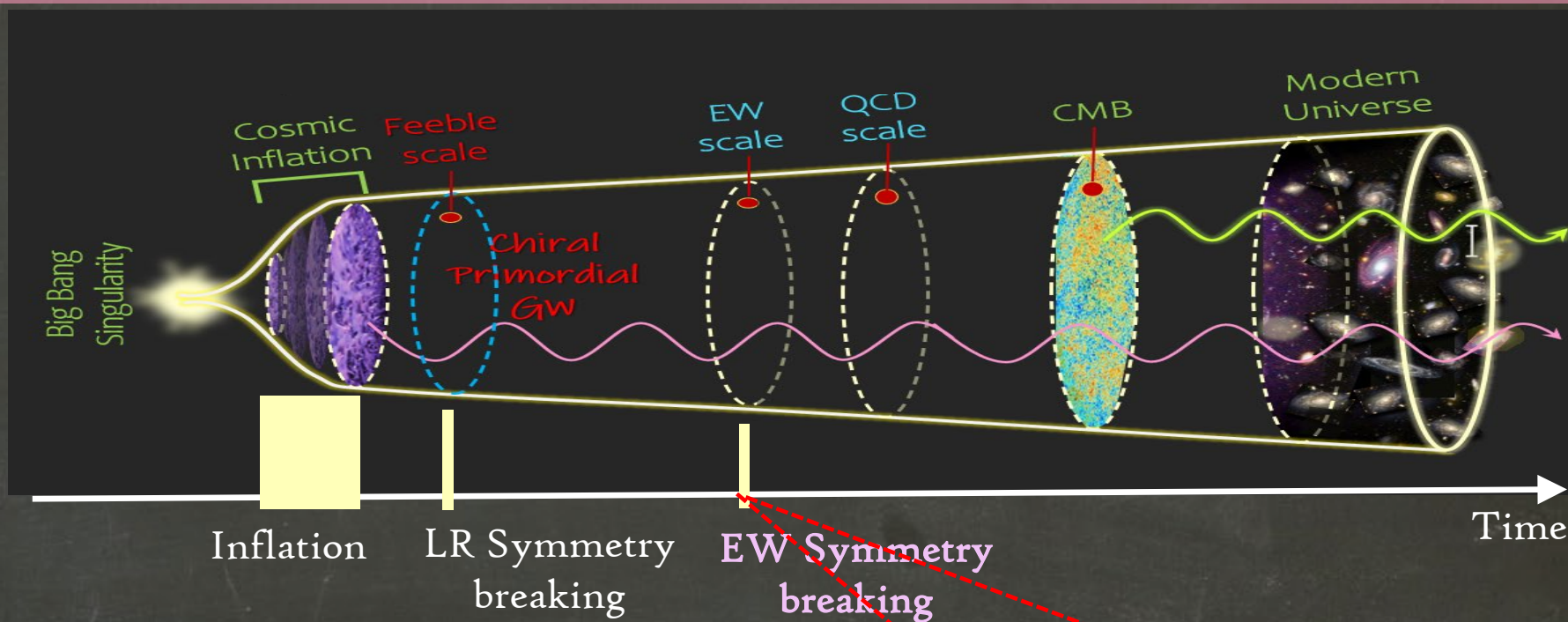
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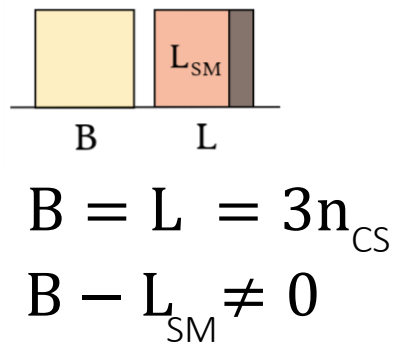
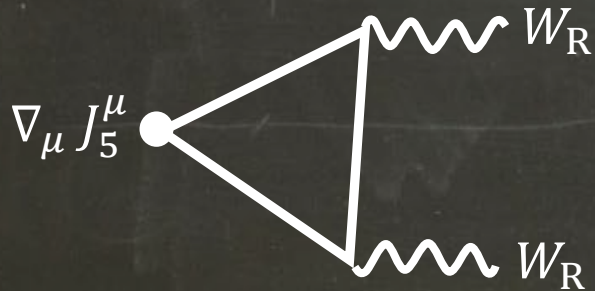
Spectator effects
reshuffle B, L_{SM} & L_N

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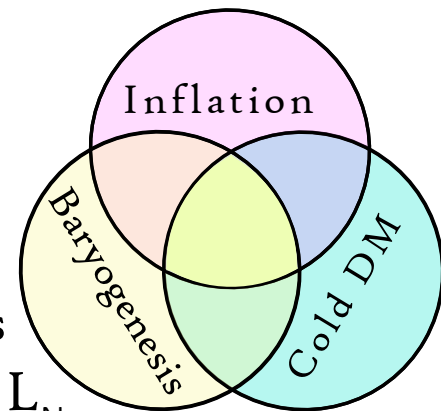


Chiral anomaly of $SU(2)_R$
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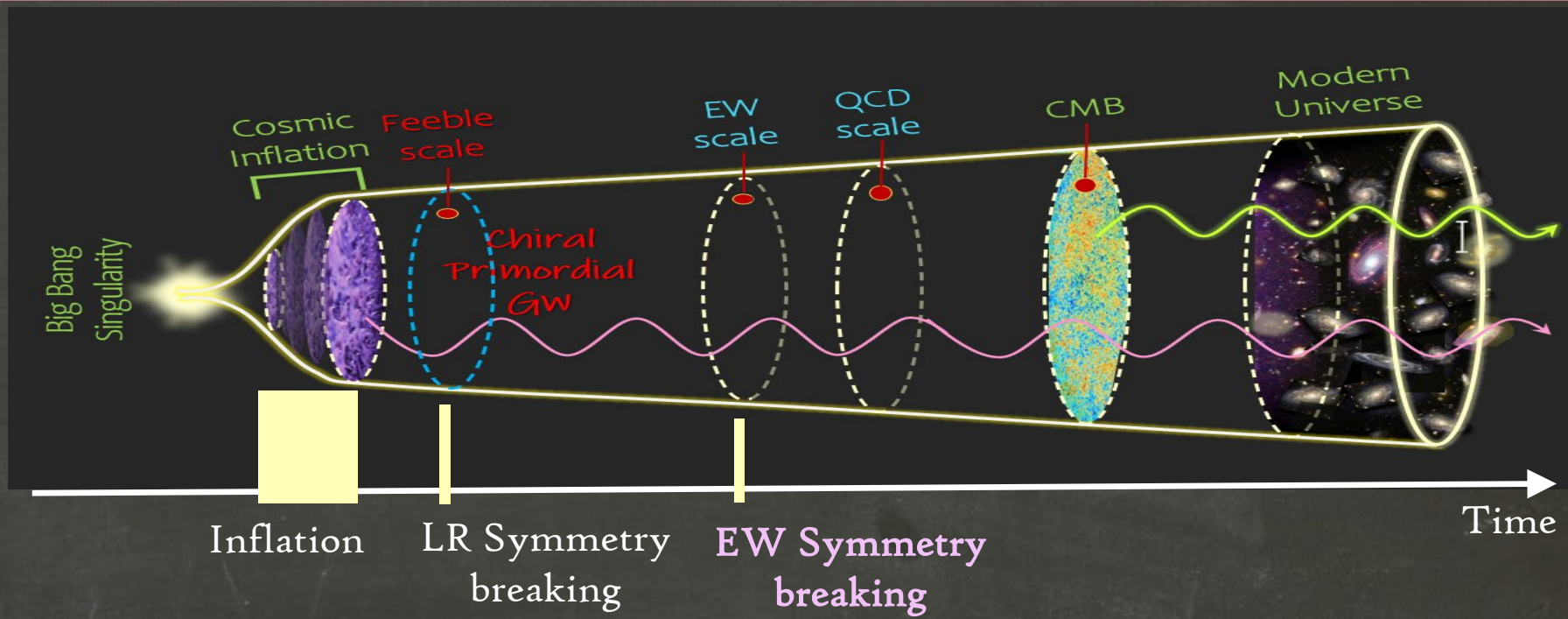
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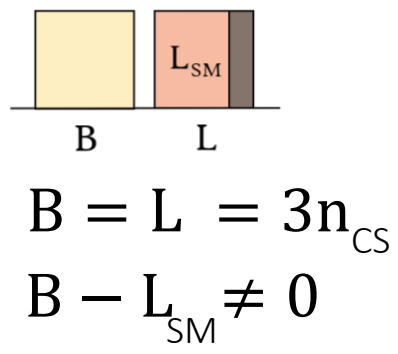
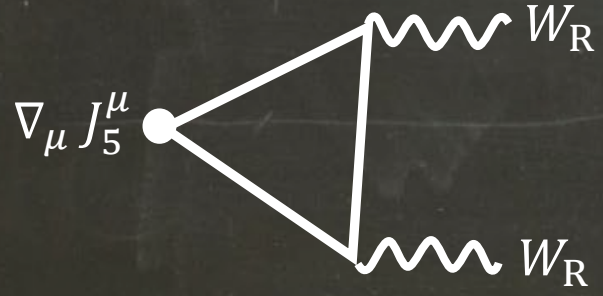


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Chiral anomaly of $SU(2)_R$
In inflation



Freezeout
of W_R

Baryogenesis

$$\eta_B^0 \approx 3 \left(\frac{g_{eff}}{100} \right)^{\frac{3}{4}} \frac{\alpha_{inf}(\xi)}{(\delta_{reh})^{\frac{3}{4}}} \left(\frac{H}{M_{Pl}} \right)^{\frac{3}{2}}$$

DM

$$\Omega_{N_1} \approx 2.8 \frac{m_{N_1}}{m_p} \Omega_B$$

$$m_{N_1} \approx 1.8 m_p = 1.7 \text{ GeV.}$$

Summary & Conclusions

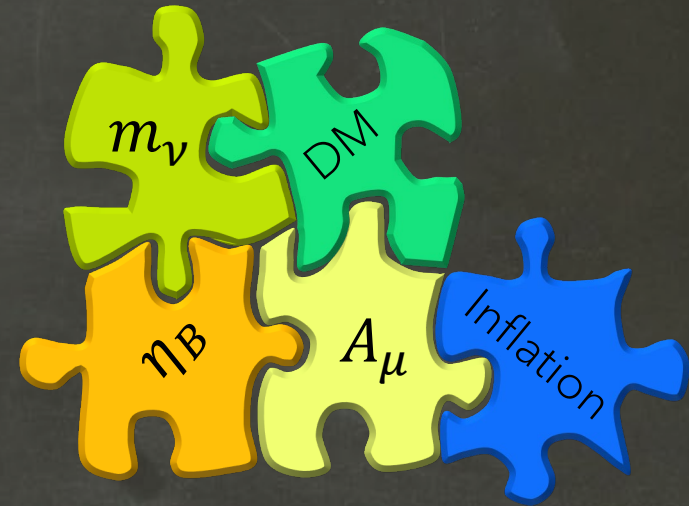


Gauge fields are expected to contribute to physics of axion inflation.

Compelling Consequences:

This Set-up is a **complete BSM** that can solve **I-IV**:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

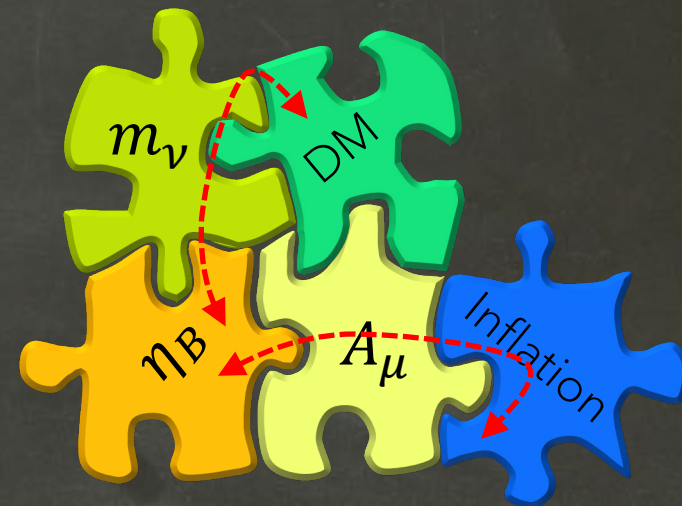


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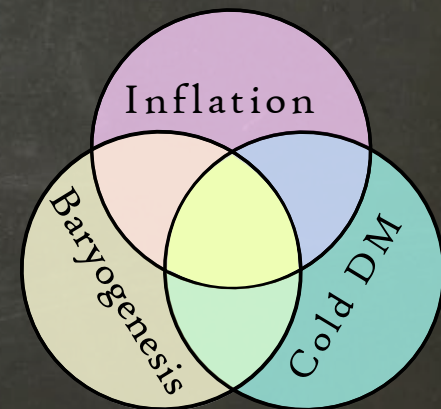
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So naturally explains **cosmological coincidences** $\eta_B \simeq 0.3 P_\zeta$ and $\Omega_{DM} \simeq 5\Omega_B$!

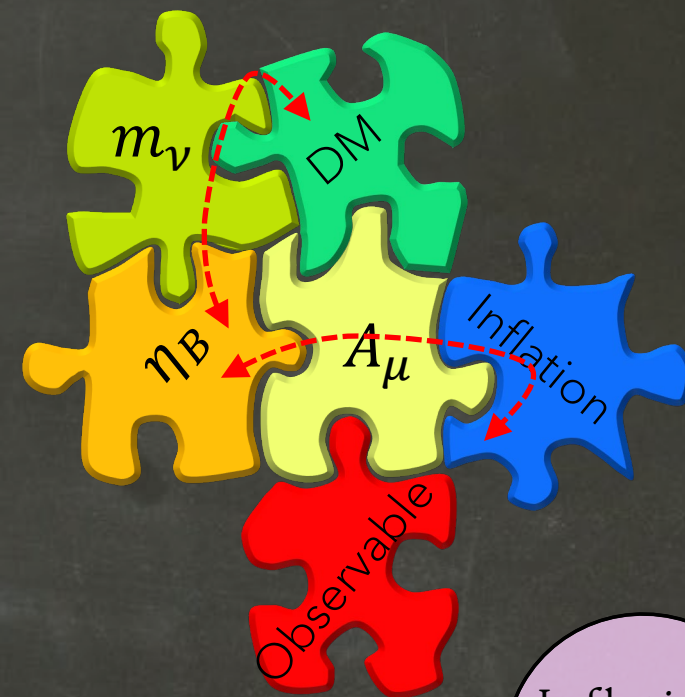


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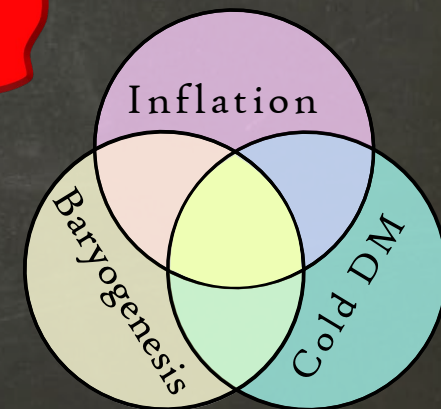
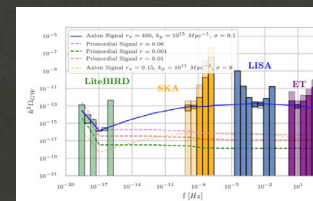
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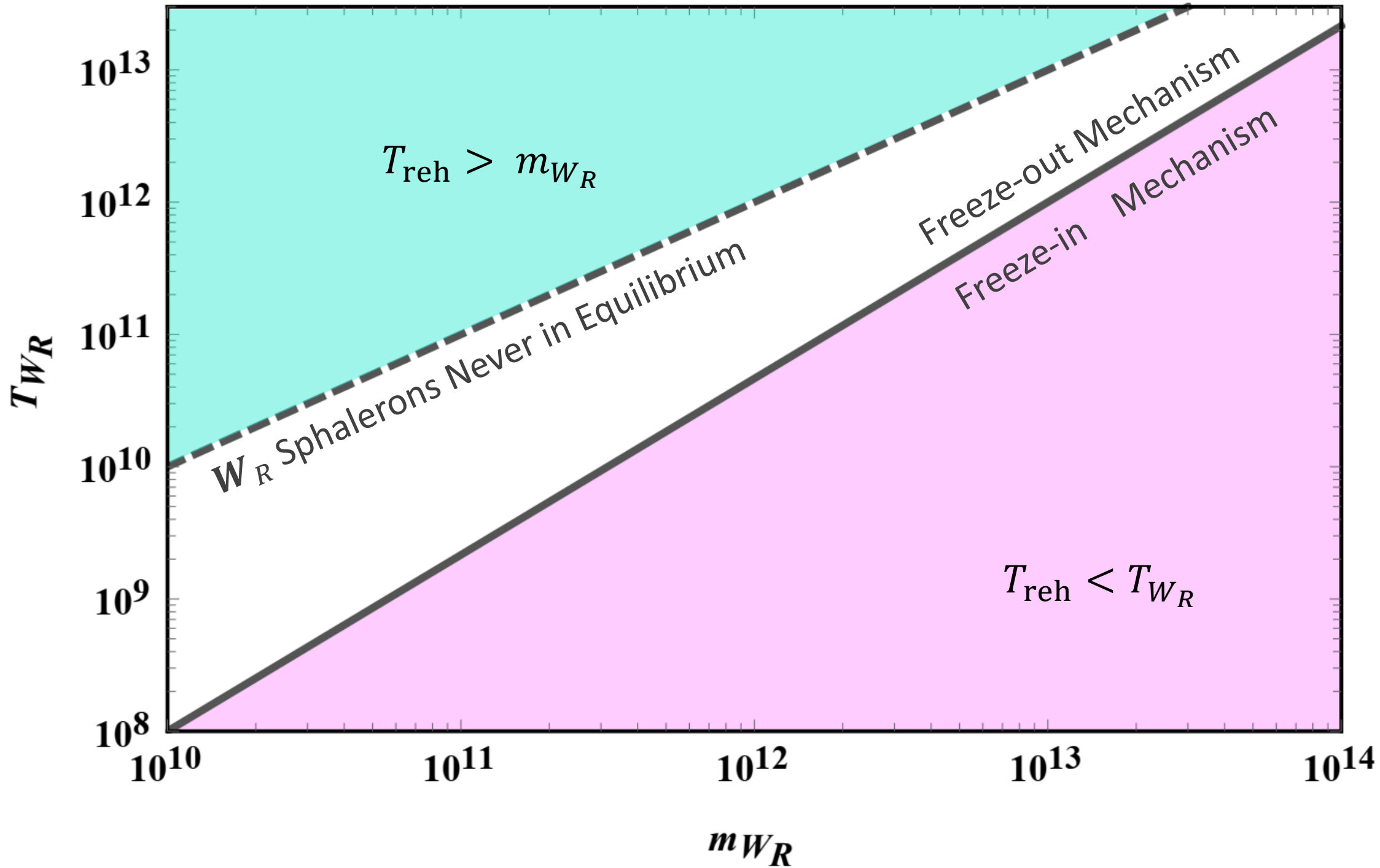
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It comes with a **cosmological smoking gun** on **Primordial GWs**.



Questions?!





This setup prefers Left-Right symmetry breaking scales above $m_{W_R} = 10^{10}$ GeV !
(same as scales suggested by the non-SUSY SO(10) GUT models with intermediate LR symmetry scale.)

