

Machine Learning at LHC

Jernej F. Kamenik



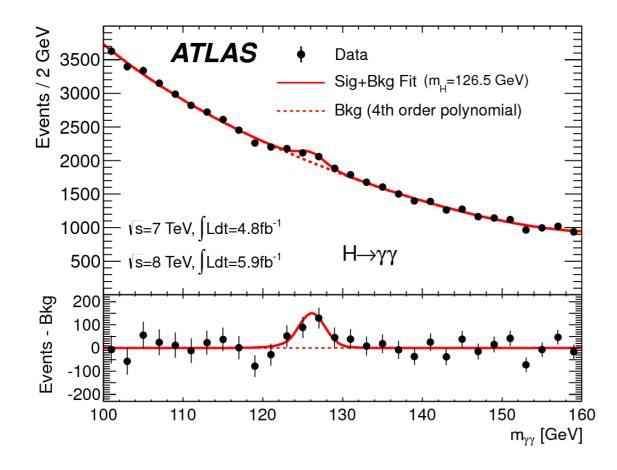




In 2012 last d.o.f predicted

within SM - Higgs boson

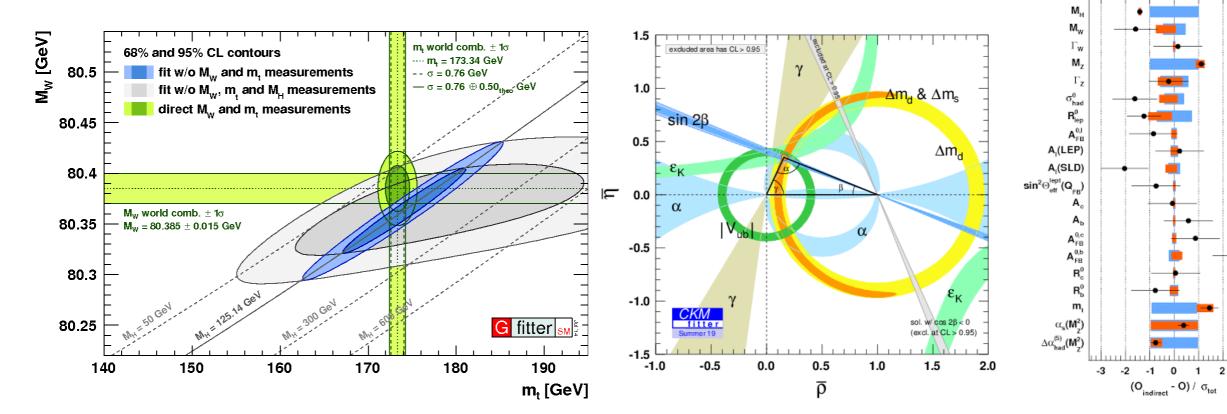
was discovered at LHC.





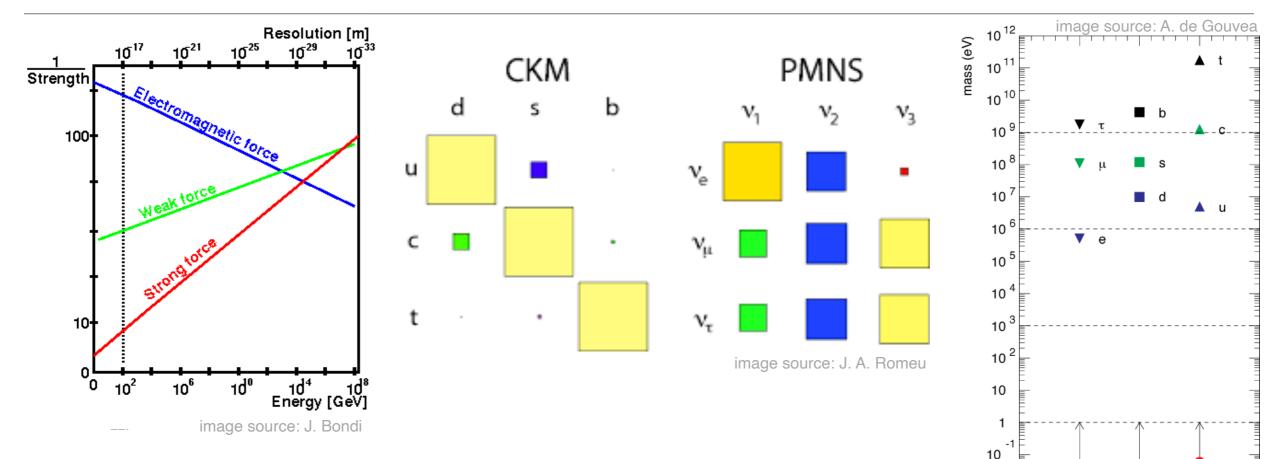
SM immensely successful

- ✓ predictive up to very large energy scales $\Lambda \gg M_{\rm Planck} \simeq 10^{16} \,{\rm TeV}$
- ✓ all key predictions confirmed
- in excellent agreement with precision measurements in particle physics experiments over past 40+ years



3

3



Several outstanding theoretical puzzles

- unification of fundamental forces (with gravity)
- Solution of parameters describing particle flavors
- Solution of the second seco

 v_3

v2

 v_1

10

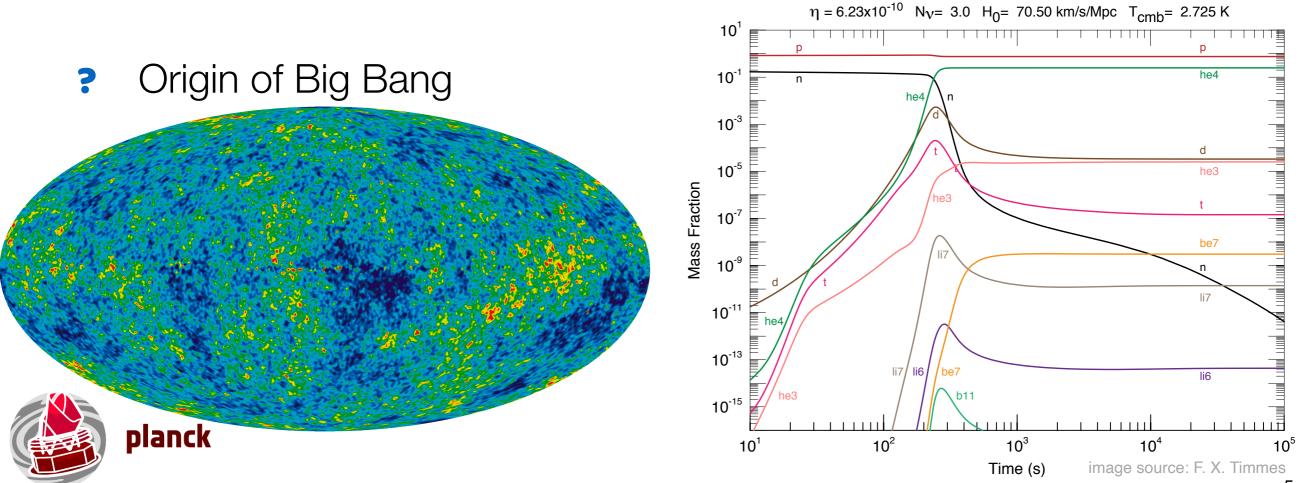
10

10

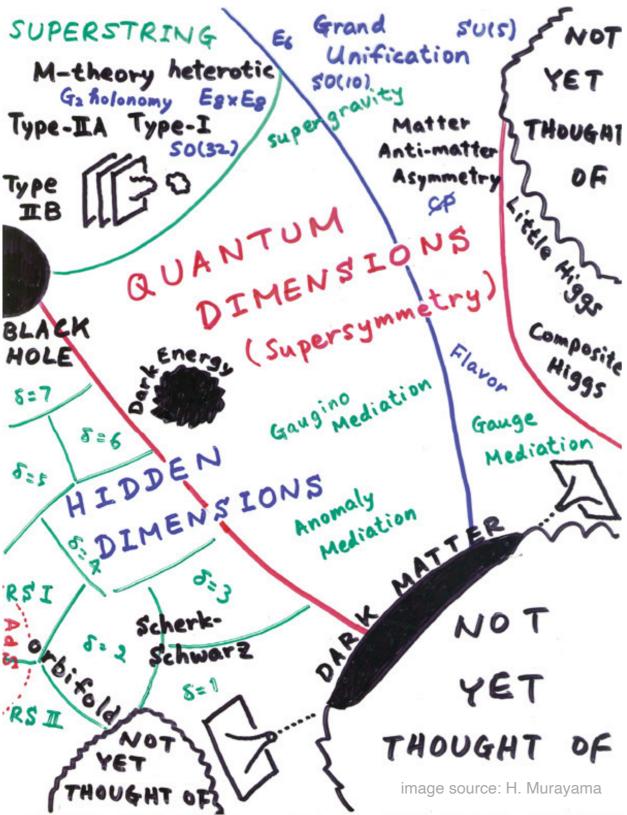
10

Particle physics vs. Cosmology

- ? Origin of most of gravitational mass and energy in Universe
- Origin of matter-antimatter asymmetry in Universe



Searching for unknown physics BSM



Theory

Multitude of theoretical proposals addressing SM shortcomings

Few unambiguous predictions experimentally accessible with current technology

Most prospective directions possibly not yet conceived

Searching for unknown physics BSM

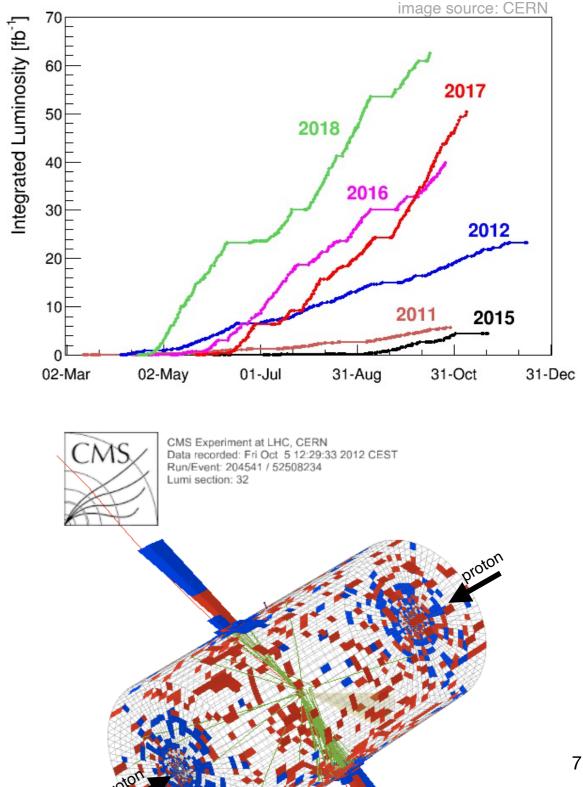
Experiment

LHC produced abundance of data (experiments so far recorded ~200PB of most interesting events)

Expected to increase by order of magnitude in next decade

Challenge to discern interesting events from mundane backgrounds

Which events are interesting?



Searching for unknown physics BSM

Discovering the Higgs boson was like searching for a needle in a haystack...



...at least we knew how the needle looked like.

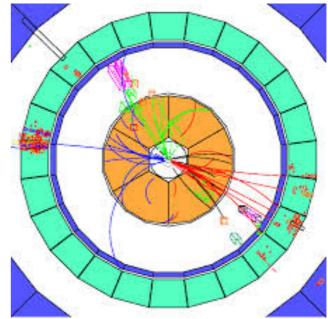
Machine Learning in Particle Physics

ML (subset of AI) uses statistical learning algorithms to build models based on data

ML has been used in HEP, particularly in experimental applications since late 20th century

Track finding with neural networks Carsten Peterson Nuclear Instruments and Methods in Physics Research Section A (1989) 279 (3): 537-5459.

The Use of Neural Networks in High-Energy Physics Bruce Denby Neural Computation (1993) 5 (4): 505–549.



In past 10-15 years, exploration of 'deep learning' approaches in HEP closely follows advances in algorithms & available computing power

Machine Learning in (Particle) Physics

ML plays increasingly important role in HEP including in

- ⇒ Data reconstruction and analysis
 See e.g. Pata et al., 2101.08578
 Kasieczka et al., 1902.09914
 Brehmer et al., 1907.10621
 ...
 (particle flow, object reconstruction & classification)
- ⇒ First-principles theory calculations & detector simulations (MC event generation, Lattice simulations,...) ^{see e.g. Boyda et al., 2202.05838} Butter et al., 2203.07460 Albergo et al., 2101.08176
- ⇒ Detector and Accelerator design and operation (Differentiable detectors, ML triggers, Defect detection)

see e.g. Dorigo, 2203.13818 Govorkova et al.,2108.03986 Akchurin et al., 2203.08969

⇒ Anomaly Detection for BSM physics searches (rest of this talk...)

Anomaly detection in (Particle) Physics

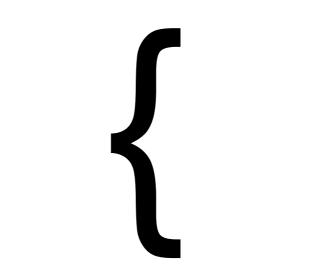
Crucial to understand physics learned by the machine

see e.g. Faucett, Thaler & Whiteson, 2010.11998

⇒ Helps to understand systematics & validate assumptions (i.e. MC, control region dependence)

Challenge of uncovering and characterizing possible unexpected signals in (LHC) data.

⇒ Need to identify signal regions, construct null-hypothesis tests, mitigate potentially large look elsewhere effects...



Supervised ML a.k.a. Universal Function Approximation

Input: representation of model p(x), finite number of examples $\{x_i\}$ sampled/computed/generated from p

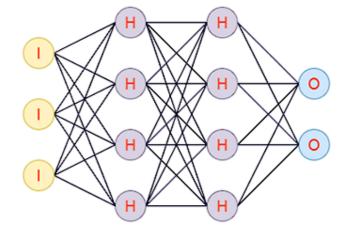
Output: mapping $f(x \rightarrow z)$ minimizing a loss function $\mathcal{L}(f, \{x_i\})$ see e.g. B. Nachman, 1909.03081

Common example: model of two distributions $p_s(x)$, s = 0, 1with loss function $\mathcal{L} = -[s_i \log(z_i) + (1 - s_i) \log(1 - z_i)]$ (cross-entropy)

 $\Rightarrow f \text{ will approximate } f(x) \sim \frac{p_0(x)/p_1(x)}{1+p_0(x)/p_1(x)}$

(likelihood ratio)

Typical implementation in terms of (deep) neural networks



Supervised ML a.k.a. Universal Function Approximation

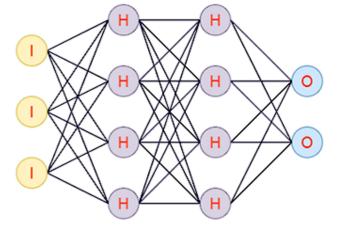
Example: distinguishing boosted massive

S

Input (x): detector readings (particle tracks, calorimeter clusters)

Method: DeepNN trained on artificial (MC) or pre-tagged (labelled) samples $\{x_i\}$

Output: parametric classifier (f) with some (ROC) performance curve



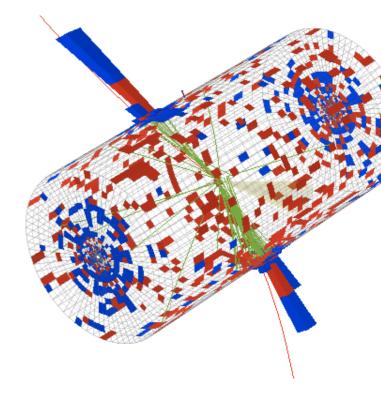
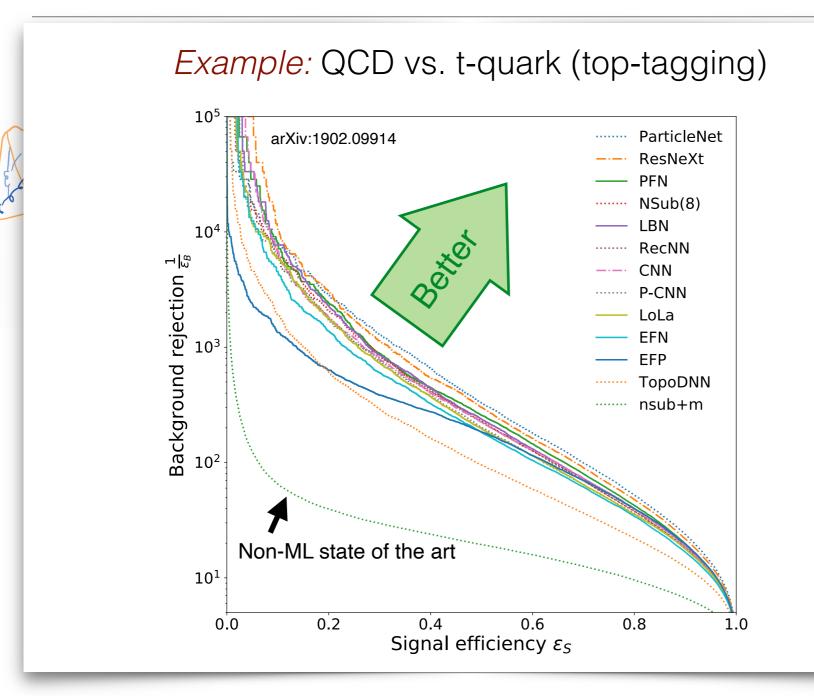
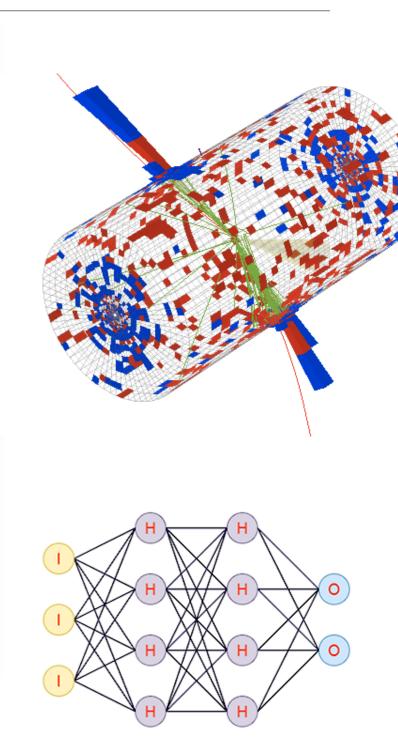


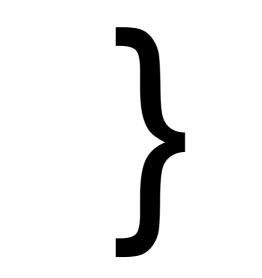
figure by J. Collins

Supervised ML a.k.a. Universal Function Approximation





Output: parametric classifier (f) with some (ROC) performance curve



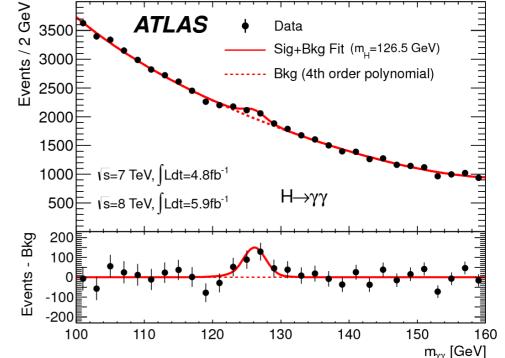
Challenges of ML Applications to BSM

Signal model $p_S(x)$ may not be known, unknown number of unlabelled examples $\{x_i\}$ sampled from $p_S may$ be present somewhere in data.

Background model $p_B(x)$ (SM) known imperfectly, cannot be relied upon to subtract from data.

However, often reasonable to assume signal is quasi-localized (unevenly distributed) in given dataset (e.g. resonant).

⇒ "Weakly- & Unsupervised" ML





Metodiev, Nachman & Thaler, 1708.02949

see also Nachman & Shih, 2001.04990

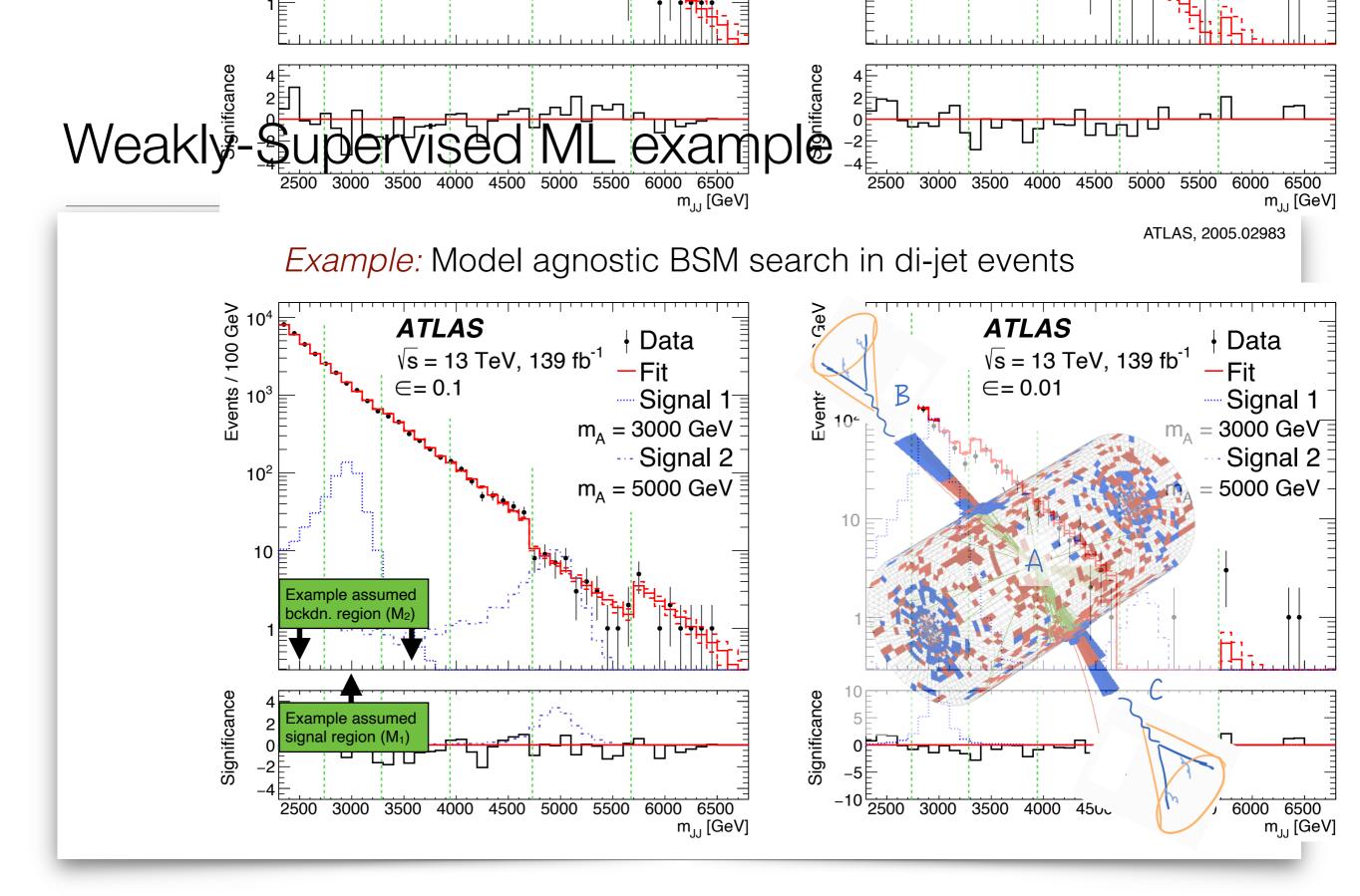
Classification from mixed samples: pure (signal, background) samples not available in real data $p_{M_1}(\vec{x}) = f_1 p_S(\vec{x}) + (1 - f_1) p_B(\vec{x}),$ $p_{M_2}(\vec{x}) = f_2 p_S(\vec{x}) + (1 - f_2) p_B(\vec{x}),$

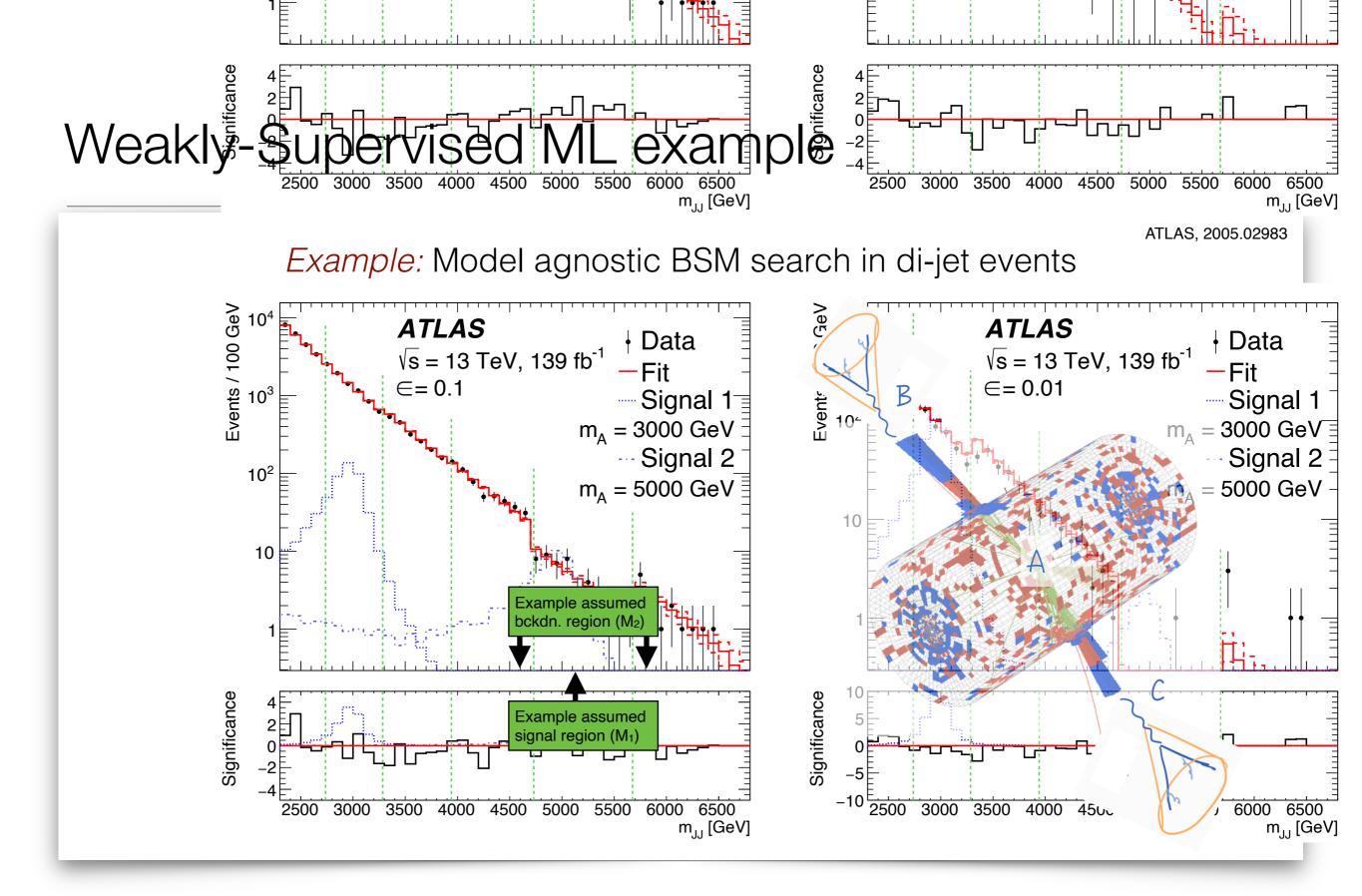
1.) Assume f_1 , f_2 known (e.g. from MC), then simply

 $h_{\text{optimal}}^{M_1/M_2}(\vec{x}) = p_{M_1}(\vec{x})/p_{M_2}(\vec{x})$

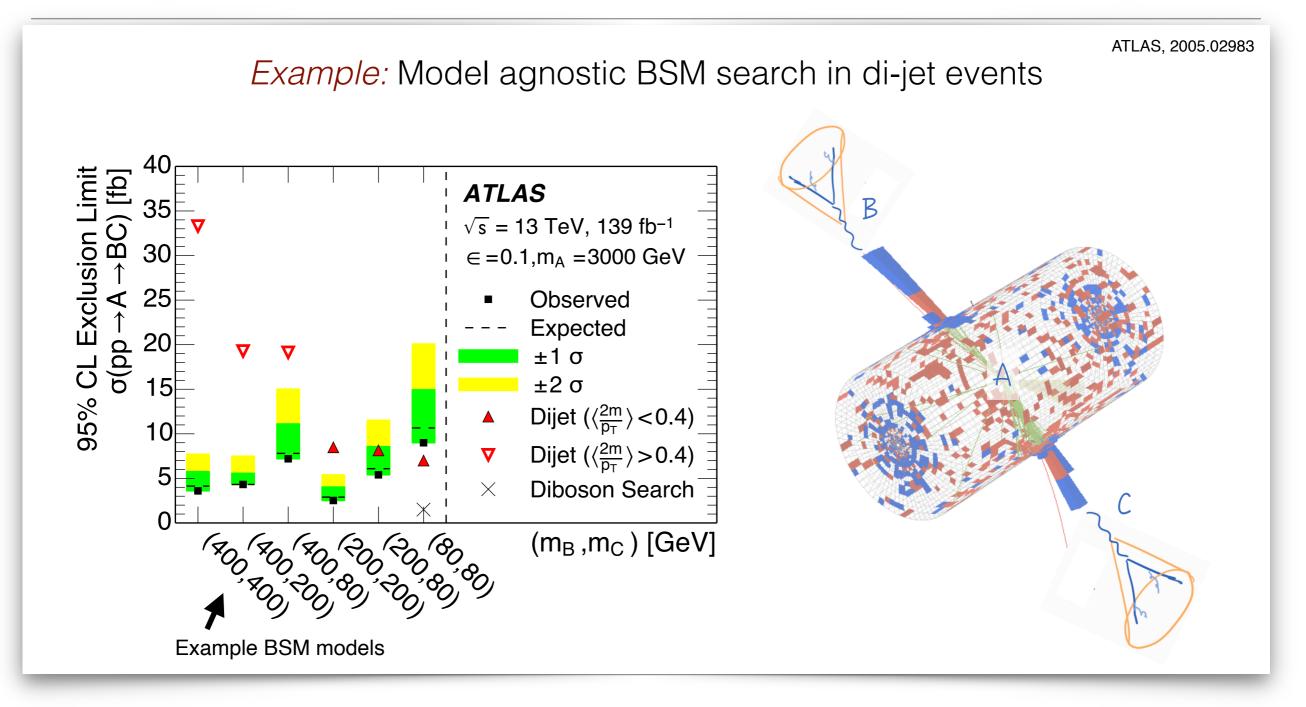
2.) Assume only $f_1 > f_2$ then use monotonicity of

$$\frac{p_{M_1}}{p_{M_2}} = \frac{f_1 \, p_S + (1 - f_1) \, p_B}{f_2 \, p_S + (1 - f_2) \, p_B}$$





Classifier Weakly-Supervised ML example



Challenges of (weakly supervised) ML for BSM

Scanning over possible signal-rich regions (M₁) can accumulate large trails factors (look-elsewhere effect).

see e.g. Bayer, Seljak & Robnik, 2108.06333

Crucial de-correlation of features $\{x_i\}$ and scanning variable (e.g. di-jet invariant mass M_{jj}) see e.g. Benkendorfer, Le Pottier & Nachman, 2009.02205

Assuming weakly supervised classifier *s* uncovers localized excess in data...

What is the physics contained in s(x)? see e.g. Bortolato et al., 2103.06595 Dillon et al., 1904.04200, 2005.12319

How is it sensitive to biases & systematics of $\{x_i\}$? See e.g. Nachman, 1909.03081 Gosh & Nachman, 2109.08159

How to quantify the significance of (lack of) detection ?

In essence classification from mixed samples

$$p_{M_1}(\vec{x}) = f_1 \, p_S(\vec{x}) + (1 - f_1) \, p_B(\vec{x}),$$
$$p_{M_2}(\vec{x}) = f_2 \, p_S(\vec{x}) + (1 - f_2) \, p_B(\vec{x}),$$

defines a mixture model assuming conditional independence: $p(s(\vec{x}), y|\pi) = (1 - \pi) p(s(\vec{x})|B)p(y|B) + \pi p(s(\vec{x})|S)p(y|S)$ $\uparrow \qquad \uparrow \qquad \uparrow$ Classifier output = anomaly score $\sim S/B$ scanning variable defining $M_{1,2}$

 \Rightarrow Null-hypothesis test = statistical independence of s & y

$$p(s(\vec{x}), y | \pi = 0) \qquad I(s, y | z) = \int ds \, dy \, p(s, y | z) \log \frac{p(s, y | z)}{p(s | z) p(y | z)} = 0$$

 \Rightarrow Clear statement on the presence of signal (p-value)

 \Rightarrow No fixed anomaly score cuts or *B* extrapolations!

Conclusions

Machine learning methods have long history of applications in particle physics

Today part of standard toolbox of HEP data analysis

Example: Higgs boson discovery and characterization

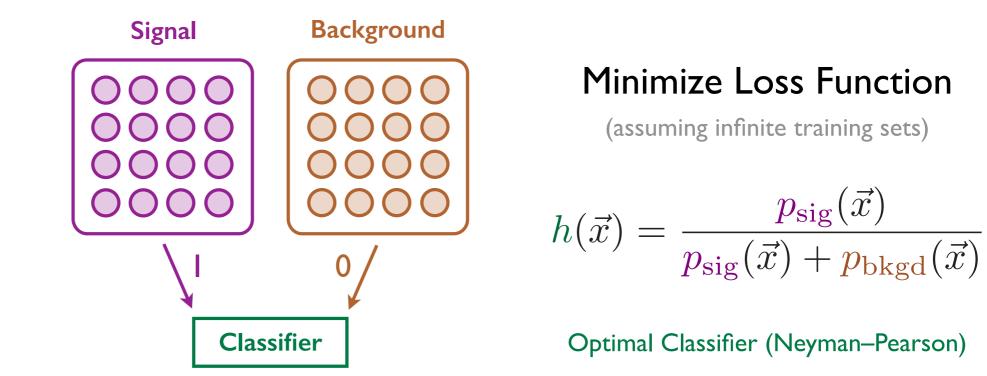
Open-ended nature of BSM physics searches presents novel challenges \Rightarrow opportunities for ML see e.g. Shanahan et al., 2209.07559 Carleo et al., 1903.10563

Recent exciting progress in weakly- and un-supervised ML approaches to BSM physics (only one direction covered today)

Extras

 $\boldsymbol{\mathsf{x}}$ list of observables useful for distinguishing $\boldsymbol{\mathsf{S}}$ from $\boldsymbol{\mathsf{B}}$

ps(x) and p_B(x) - probability distributions of x for S and B classifier h(x) close to $f(x) = \frac{1}{2} \int_{and}^{b} (h(x) = 1)^2 (h(x) = 1)^2 \int_{and}^{b} (h(x) = 1)^2 (h(x)$



 $\boldsymbol{\mathsf{x}}$ list of observables useful for distinguishing $\boldsymbol{\mathsf{S}}$ from $\boldsymbol{\mathsf{B}}$

 $p_{S}(x)$ and $p_{B}(x)$ - probability distributions of x for S and B

classifier h(x) close to 1 for S and close to 0 for $B_{\ell_{MSE}} = \langle (h(\vec{x}) - 1)^2 \rangle_{signal} + \langle (h(\vec{x}) - 1)^2 \rangle_{si$

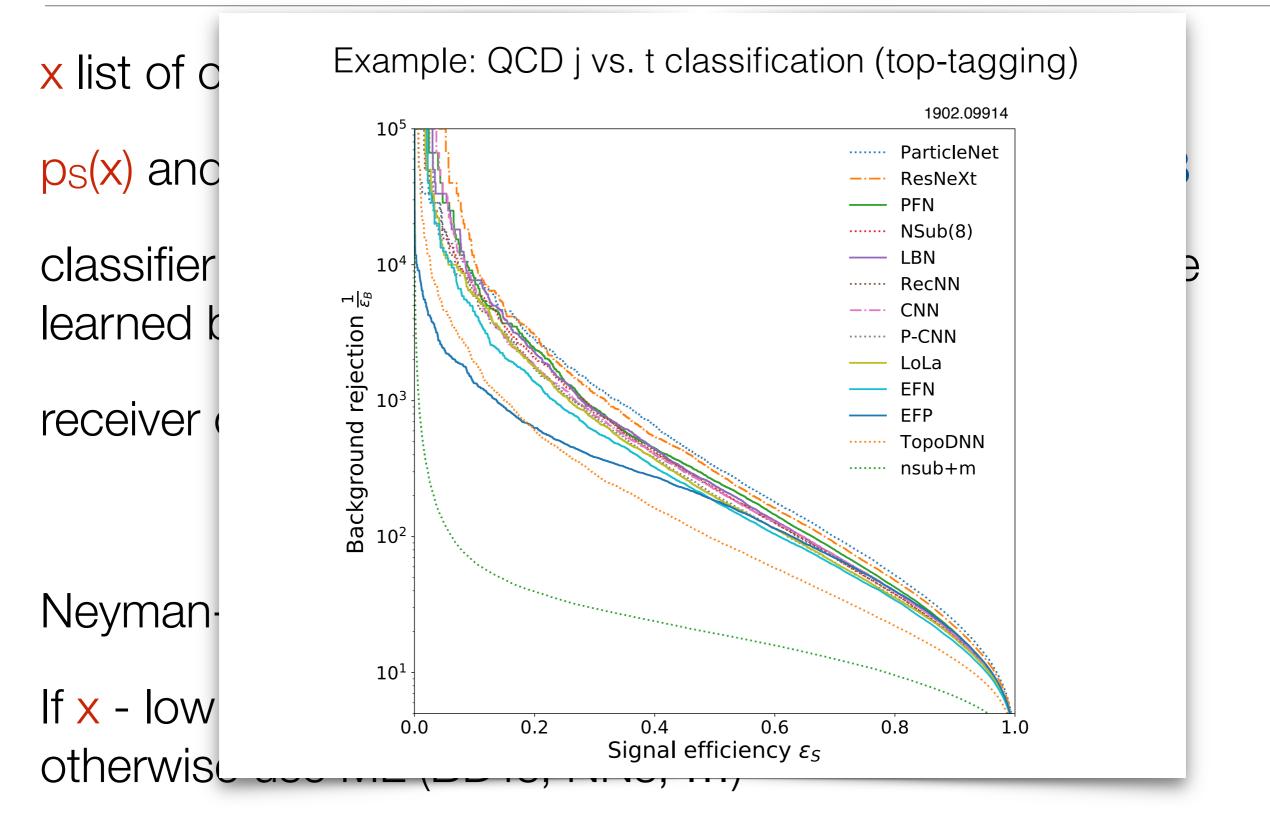
receiver operating characteristic (ROC) curve

 $\epsilon_S = \int d\vec{x} \, p_S(\vec{x}) \,\Theta(h(\vec{x}) - c)$ $\epsilon_B = \int d\vec{x} \, p_B(\vec{x}) \,\Theta(h(\vec{x}) - c)$

Neyman-Pearson lemma: $h_{\text{optimal}}(\vec{x}) = p_S(\vec{x})/p_B(\vec{x})$ (likelihood ratio)

If x - low dimensional, can use histograms directly, otherwise use supervised ML (BDTs, NNs, ...)

Jet classification: basics



Classifier Jet classification: mixed samples

Classification from mixed samples: pure samples not $\int_{\text{Mixed A}}^{p_{\text{mixed}}(\vec{x}) = f_q p_{\text{quark}}(\vec{x}) + (1 - M_{\text{Mixed A}}) = \int_{\text{Mixed B}}^{p_{\text{mixed}}(\vec{x}) + (1 - M_{\text{Mixed A}}) = \int_{\text{Mixed B}}^{p_{\text{mixed}}(\vec{x}) + (1 - M_{\text{Mixed B}}) = \int_{\text{Mixed B}}^{p_{\text{mixed}}(\vec{x}) + (1 - M_{\text{$

$$p_{M_1}(\vec{x}) = f_1 \, p_S(\vec{x}) + (1 - f_1) \, p_B(\vec{x}),$$
$$p_{M_2}(\vec{x}) = f_2 \, p_S(\vec{x}) + (1 - f_2) \, p_B(\vec{x}),$$

 $h_{\text{mixed}}(\vec{x}) = \frac{1}{2}$ $h_{\text{mixed}}(\vec{x}) = \frac{1}{2}$ $h_{\text{pure}}(\vec{x}) = \frac{1}{2}$ $h_{\text{pure}}(\vec{x}) = \frac{1}{2}$

Blanchard, Flaska, Handy, Pozzi, Scott, 2016; Dery, Nachman, Rubb

1.) Assume f₁, f₂ known (e.g. from MC), then simply

 $h_{\text{optimal}}^{M_1/M_2}(\vec{x}) = p_{M_1}(\vec{x})/p_{M_2}(\vec{x})$

2.) Assume only $f_1 > f_2$ then use monotonicity of

 $\frac{p_{M_1}}{p_{M_2}} = \frac{f_1 \, p_S + (1 - f_1) \, p_B}{f_2 \, p_S + (1 - f_2) \, p_B}$

(Classification Without Labels)

0000

 \mathbf{OOOO}

Metodiev, Nachman & Thaler, 1708.02949