



# **Amplitude Detuning from misaligned Triplets and IR multipolar Correctors**

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# Outline

- Setup
  - Motivation
  - Misaligning Correctors
  - Misaligning Triplets
  - Simulation and Measurement details
- Results
  - Corrector Misalignments
  - Triplet Misalignments
  - Conclusion

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# Motivation

With the advent of the HL-LHC, new **triplets** with larger aperture and new **corrector packages**<sup>1</sup>, for corrections of high-order non-linear magnetic field errors, will be installed in the low  $\beta$  Interaction Points (IP1 & IP5), which will require precise orbit control.

The goal of this study is, to investigate the influence of the **expected remaining orbit deviations**<sup>2</sup> in the **triplets** and the associated **non-linear corrector packages** on **Amplitude Detuning**.

A preliminary study showed large detuning, which turned out to be a bug, but triggered this more extensive study.

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<sup>1</sup>O. Brüning et al - *LHC Report 504: Dynamic aperture studies for the LHC separation dipoles*, 2004. <https://cds.cern.ch/record/742967>

<sup>2</sup>D. Gamba et al - *IP ORBIT CORRECTION UPDATE FOR HL-LHC*, IPAC, 2018.  
<http://cds.cern.ch/record/2648556>

# Misaligning Correctors

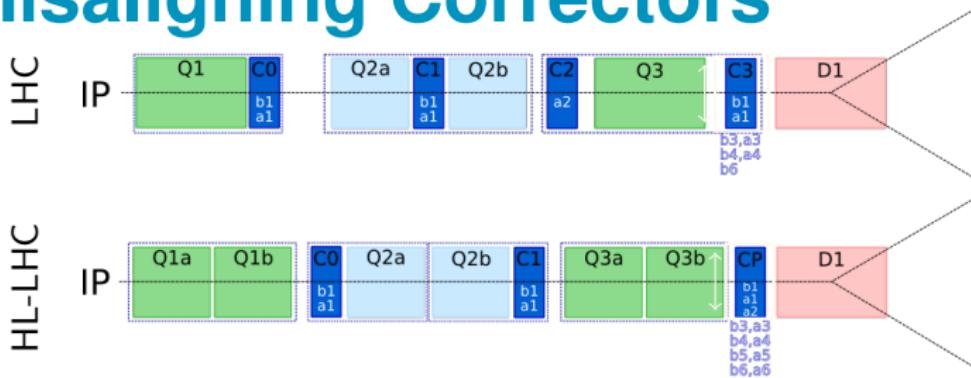


Figure: Schematic representation of half of the IR region in the accelerator.

- setup LHC/HL-LHC Sequence
- 60 WISE error realizations: octupole, (skew-)decapole and (skew-)dodecapole to MQX and MBX
- calculate triplet corrections for the MCX
- 50 misalignment realizations for **MCX**, **uniformly distributed**  $\in [-1 \text{ mm}, 1 \text{ mm}]$
- ⇒ check Amplitude Detuning

# Misaligning Correctors

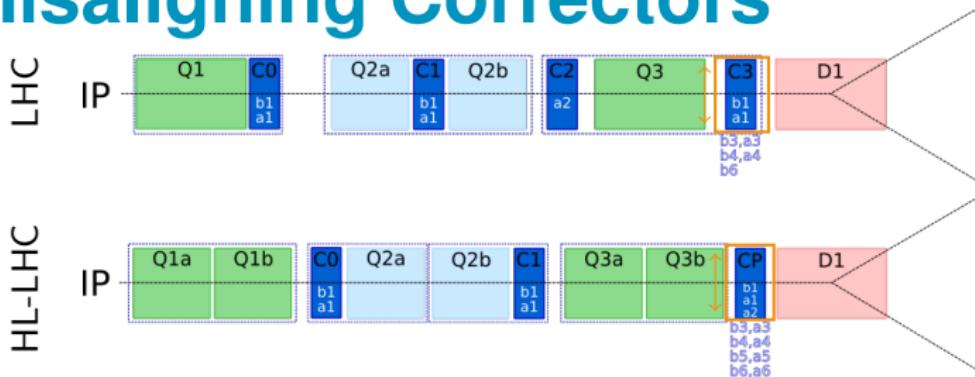


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# Misaligning Triplets

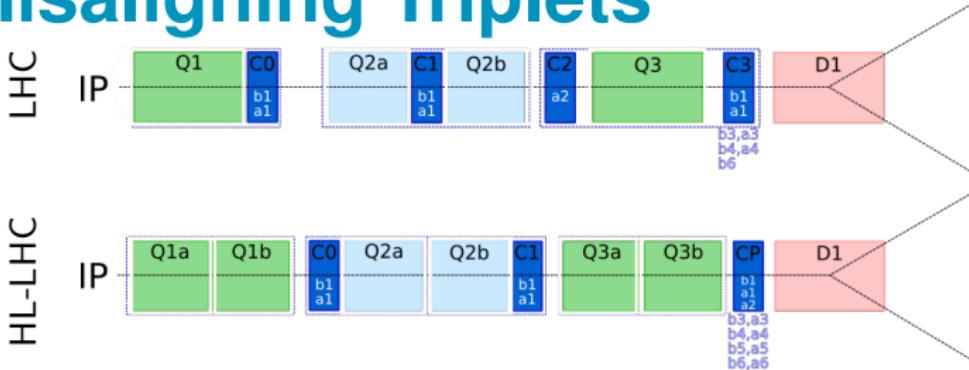


Figure: Schematic representation of half of the IR region in the accelerator.

- setup LHC/HL-LHC Sequence
- 60 WISE error realizations: octupole, (skew-)decapole and (skew-)dodecapole MQX and MBX
- calculate triplet corrections for the MCX
- 50 misalignment realizations for **Q1-Q3**, truncated-gaussian distributed  $\sigma = 0.4 \text{ mm}$  ( $0.8 \text{ mm}$  Q3), cut at  $2.5\sigma$
- ⇒ check Amplitude Detuning

# Misaligning Triplets

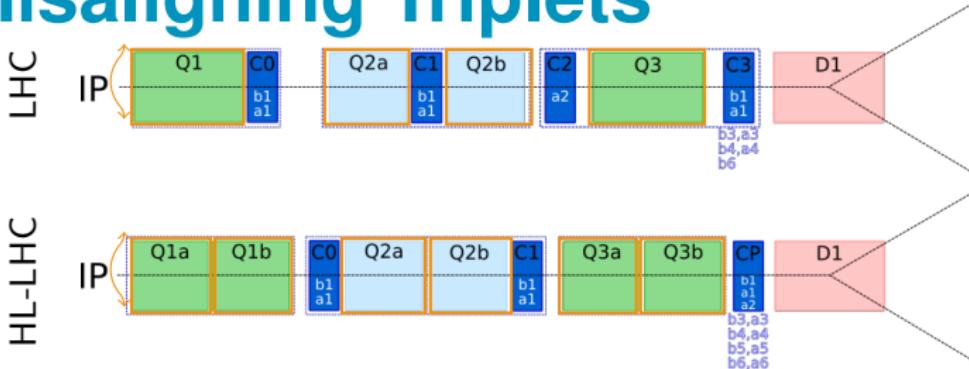


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- ⇒ check Amplitude Detuning

# Setup

	Simulation		Measurements <sup>1</sup> LHC
	LHC	HL-LHC (v1.3)	
Energy	6.5 TeV	7.0 TeV	6.5 TeV
$\beta^*$		30 cm round optics	
Orbit		flat orbit	
$Q_x, Q_y$		0.31, 0.32	
MO Power	off (see later)		off
$b_4$ corrected		yes	

<sup>1</sup>in MD3311 <http://cds.cern.ch/record/2692810>

# Calculate Detuning

Feeddown:

$$K_5 \rightarrow K_4 = dx \cdot K_5$$

$$K_5 S \rightarrow K_4 = -dy \cdot K_5 S$$

$$K_6 \rightarrow K_4 = \frac{1}{2} (dx^2 - dy^2) \cdot K_6$$

$$K_6 S \rightarrow K_4 = -dx \cdot dy \cdot K_6 S$$

Detuning:

$$\frac{\partial Q_x}{\partial 2J_x} = \frac{K_4}{32\pi} \beta_x^2$$

$$\frac{\partial Q_x}{\partial 2J_y} = -\frac{K_4}{16\pi} \beta_x \beta_y$$

$$\frac{\partial Q_y}{\partial 2J_y} = \frac{K_4}{32\pi} \beta_y^2$$

$K_n(S)$ : Integrated (skew) magnetic field strength,  
with  $n = 4 \Rightarrow$  octupole etc.

$dx, dy$ : Beam offset from element center

$J_{x,y}$ : Action

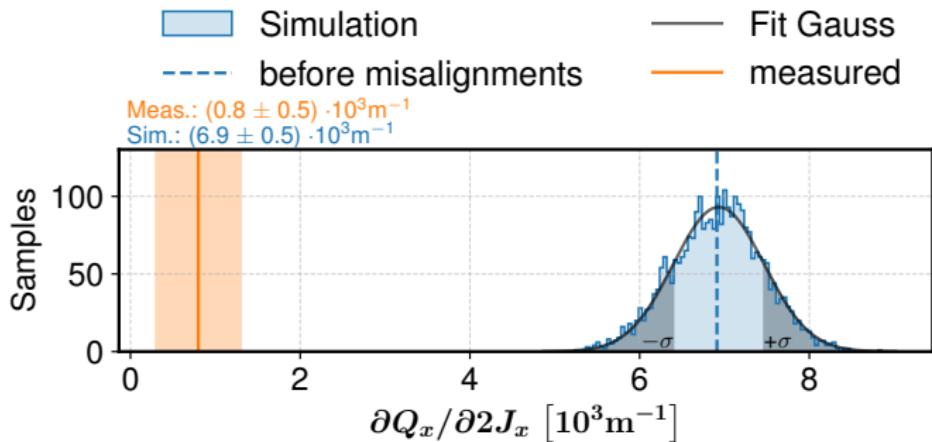
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## Subsection 1

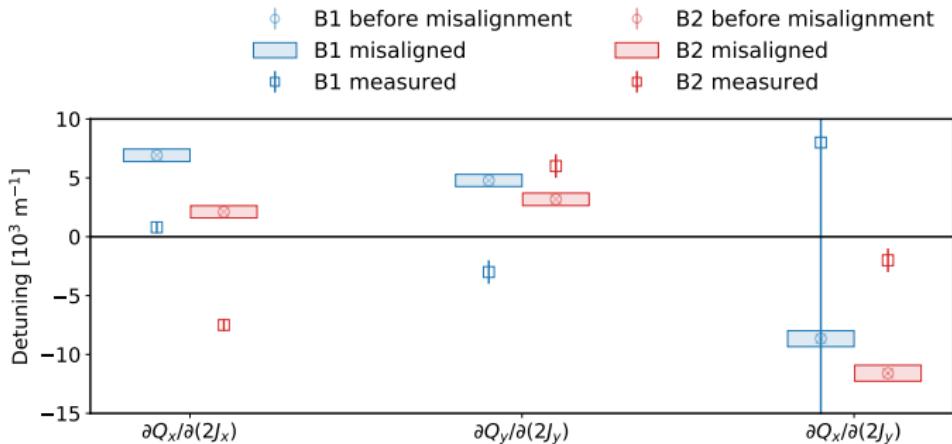
# Corrector Misalignments

# Misalign LHC Correctors



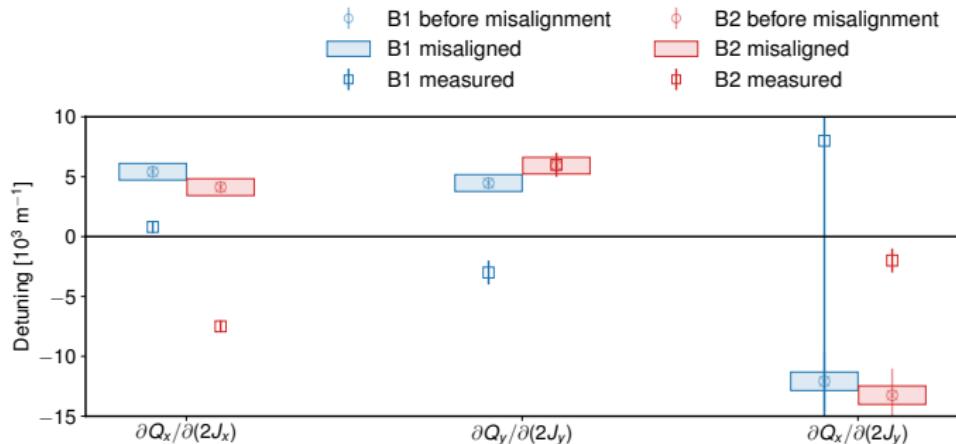
- Shown: result for Beam 1 direct horizontal term
- Simulation "offset" from zero due to amplitude detuning from arc-sextupoles
- Gaussian detuning distribution (from uniform misalignments)  
⇒ compare for both beams and all detuning components

# Misalign LHC Correctors



- amplitude detuning spread from misalignments is small compared to expected detuning without misalignments
- also smaller or of similar order as measured amplitude detuning
- contribution only from feeddown from  $b_6$  as, this is the only corrector

# Misalign HL-LHC Correctors

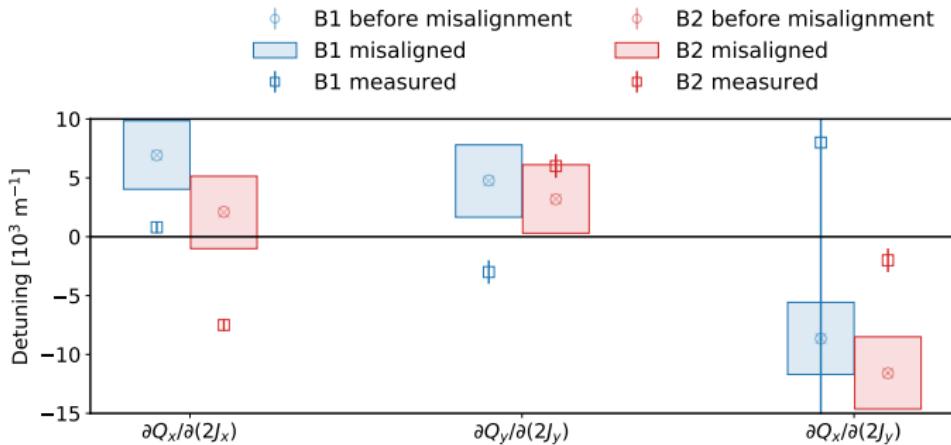


- amplitude detuning spread from misalignments is small compared to expected detuning without misalignments
- also smaller or of similar order as measured amplitude detuning
- contribution from feeddown from  $b_5$ ,  $a_5$ ,  $b_6$ , and  $a_6$  (see appendix)

## Subsection 2

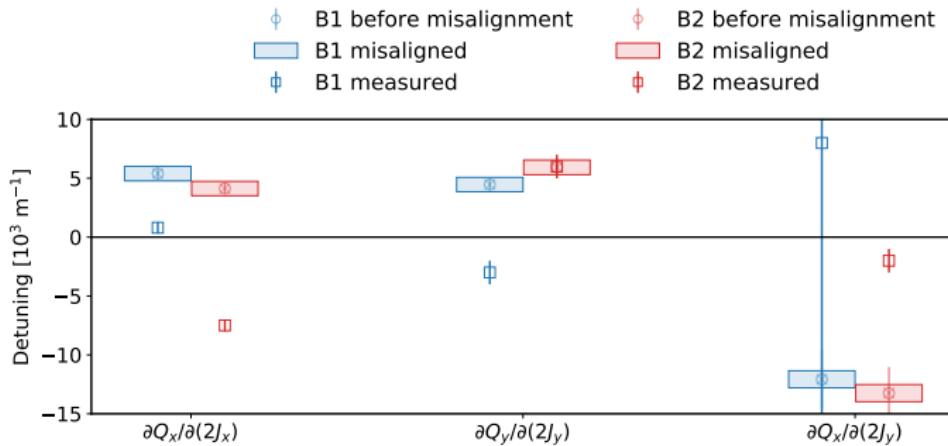
### **Triplet Misalignments**

# Misalign LHC Triplets



- amplitude detuning **spread from misalignments is of equal order** compared to expected detuning without misalignments, but not problematic
- large spread** compared to HL-LHC; reasons under investigation (possibly: cancellation due to shorter magnets / independent misalignments, differences in error-tables)

# Misalign HL-LHC Triplets

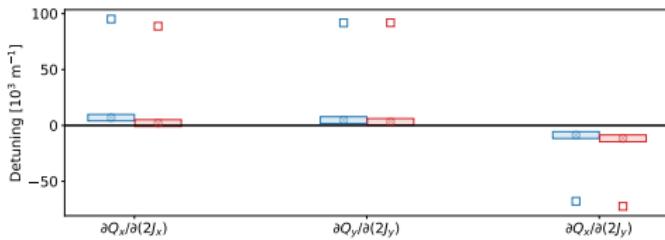


- amplitude detuning spread from misalignments is small compared to expected detuning without misalignments
- also spread smaller or of similar order as measured amplitude detuning

# Misalign Triplets

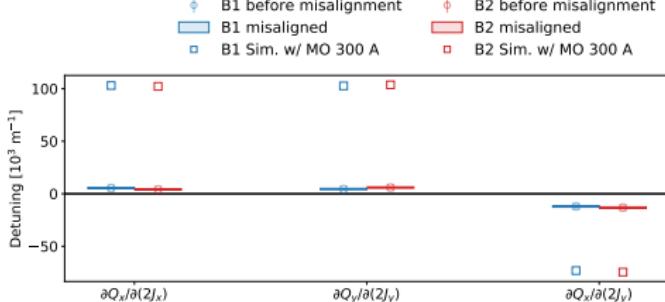
... and compare to powered MO's

LHC



- MO powering of 300 A causes amplitude detuning to increase from  $\sim 5 \cdot 10^3 \text{ m}^{-1}$  up to  $\sim 100 \cdot 10^3 \text{ m}^{-1}$  in the direct terms.

HL-LHC



# Conclusion

- Expected amplitude detuning spread is **larger** from investigated **triplet misalignment** than from corrector misalignments in the **LHC**.
- Expected amplitude detuning spread is **marginally larger** from investigated **corrector misalignments** than from triplet misalignments in the **HL-LHC**.
- The investigated misalignments, with spreads of  $\pm 1$  mm in the MCX and  $\pm 0.4$  mm(0.8 mm) in the MQX **do not cause problematic amplitude detuning** in either machine.
- Amplitude detuning is **negligible** when comparing to **expected detuning from MO powering**.
- Expected detuning from triplet-misalignments is smaller for **HL-LHC** than for **LHC** for the same  $\beta^* = 30$  cm.

# Thank you for your attention!

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# Amp. Det. References

Table: Reference Values Summary

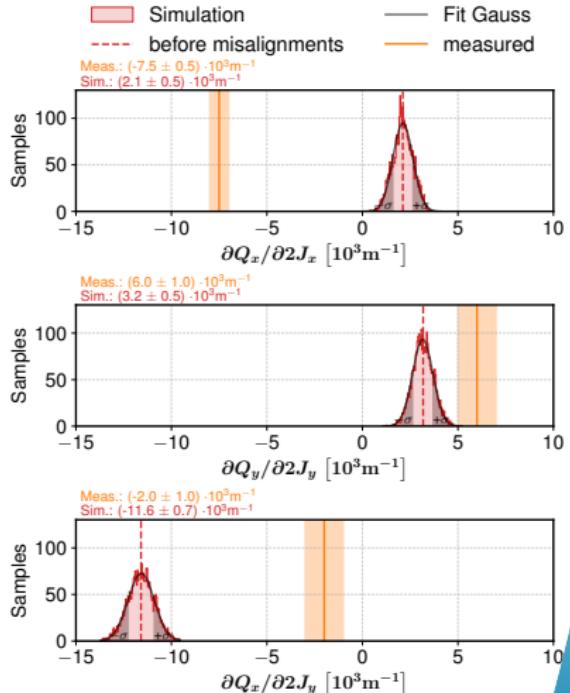
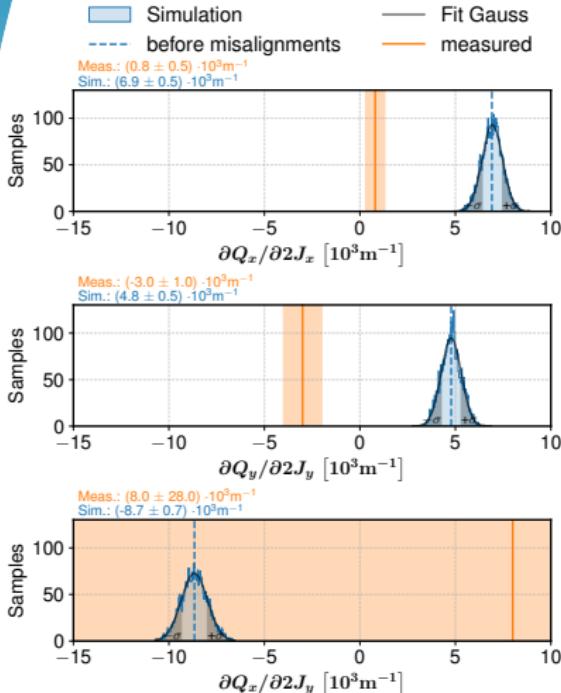
	[ $10^3 \text{ m}^{-1}$ ]	MD3311	w/ Errors	MO-Powering	0 A	300 A	570 A	0 A w/o Sextupoles
Beam 1	$\partial Q_x / \partial 2J_x$ LHC HL-LHC	$0.8 \pm 0.5$	$6.9 \pm 0.0$		<b>6.6</b>	<b>95.2</b>	<b>174.8</b>	<b>0.1</b>
		–	$5.4 \pm 0.4$		<b>5.3</b>	<b>103.0</b>	<b>191.0</b>	<b>0.2</b>
	$\partial Q_y / \partial 2J_y$ LHC HL-LHC	$8 \pm 28$	$4.8 \pm 0.0$		<b>4.</b>	<b>91.7</b>	<b>170.2</b>	<b>0.1</b>
Beam 2		–	$4.5 \pm 0.4$		<b>4.6</b>	<b>102.7</b>	<b>191.0</b>	<b>0.2</b>
	$\partial Q_x / \partial 2J_y$ LHC HL-LHC	$-3 \pm 1$	$-8.7 \pm 0.1$		<b>-7.9</b>	<b>-67.9</b>	<b>-121.8</b>	<b>0.0</b>
		–	$-12 \pm 2.5$		<b>-12.4</b>	<b>-73.2</b>	<b>-127.9</b>	<b>0.1</b>
	$\partial Q_x / \partial 2J_x$ LHC HL-LHC	$-7.5 \pm 0.5$	$2.1 \pm 0.0$		<b>1.9</b>	<b>88.8</b>	<b>166.9</b>	<b>0.1</b>
		–	$4.1 \pm 0.4$		<b>4.2</b>	<b>102.2</b>	<b>190.4</b>	<b>0.2</b>
	$\partial Q_y / \partial 2J_y$ LHC HL-LHC	$-2 \pm 1$	$3.2 \pm 0.0$		<b>3.0</b>	<b>91.8</b>	<b>171.8</b>	<b>0.1</b>
		–	$5.9 \pm 0.4$		<b>5.9</b>	<b>103.7</b>	<b>191.8</b>	<b>0.2</b>
	$\partial Q_x / \partial 2J_y$ LHC HL-LHC	$6 \pm 1$	$-11.6 \pm 0.1$		<b>-12.5</b>	<b>-72.4</b>	<b>-126.3</b>	<b>0.0</b>
		–	$-13.3 \pm 2.2$		<b>-13.7</b>	<b>-74.6</b>	<b>-129.4</b>	<b>0.1</b>

# Corrector Misalignment Feeddown

**Table:** Corrector misalignment summary - feeddown from field components to first order amplitude detuning

	[ $10^3 \text{ m}^{-1}$ ]	Sum	Decapole	Skew Decapole	Dodecapole	Skew Dodecapole
Beam 1	$\partial Q_x / \partial 2J_x$ LHC HL-LHC	$0.00 \pm 0.53$ $0.01 \pm 0.69$	$0.00 \pm 0.43$	$0.01 \pm 0.55$	$0.00 \pm 0.53$ $0.00 \pm 0.05$	$0.00 \pm 0.02$
	$\partial Q_y / \partial 2J_y$ LHC HL-LHC	$0.00 \pm 0.52$ $0.00 \pm 0.70$	$0.00 \pm 0.48$	$0.00 \pm 0.52$	$0.00 \pm 0.52$ $0.00 \pm 0.05$	$0.00 \pm 0.02$
	$\partial Q_x / \partial 2J_y$ LHC HL-LHC	$0.00 \pm 0.68$ $-0.01 \pm 0.77$	$0.00 \pm 0.51$	$0.00 \pm 0.59$	$0.00 \pm 0.68$ $0.00 \pm 0.05$	$0.00 \pm 0.02$
Beam 2	$\partial Q_x / \partial 2J_x$ LHC HL-LHC	$0.00 \pm 0.52$ $0.00 \pm 0.70$	$0.00 \pm 0.48$	$0.00 \pm 0.52$	$0.00 \pm 0.52$ $0.00 \pm 0.05$	$0.00 \pm 0.02$
	$\partial Q_y / \partial 2J_y$ LHC HL-LHC	$0.00 \pm 0.53$ $-0.01 \pm 0.69$	$0.00 \pm 0.43$	$-0.01 \pm 0.55$	$0.00 \pm 0.53$ $0.00 \pm 0.05$	$0.00 \pm 0.02$
	$\partial Q_x / \partial 2J_y$ LHC HL-LHC	$0.00 \pm 0.68$ $0.01 \pm 0.77$	$0.00 \pm 0.51$	$0.01 \pm 0.59$	$0.00 \pm 0.68$ $0.00 \pm 0.05$	$0.00 \pm 0.02$

# Misalign LHC Correctors



# Misalign LHC Correctors

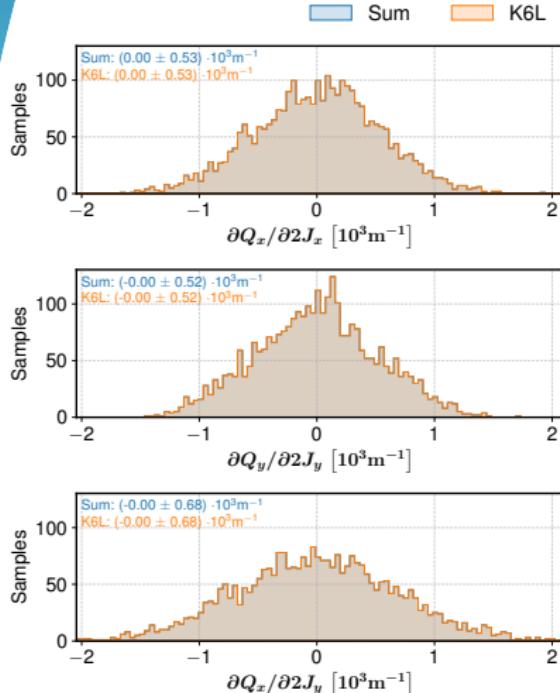


Figure: Beam 1

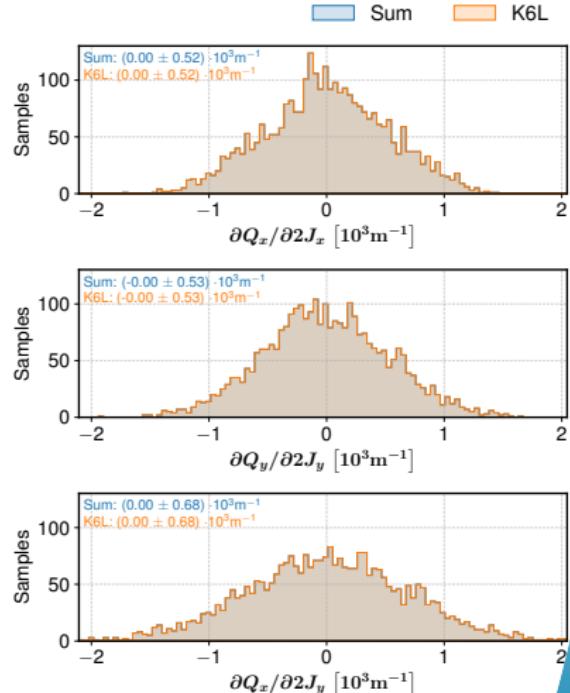


Figure: Beam 2

# Misalign HL-LHC Correctors

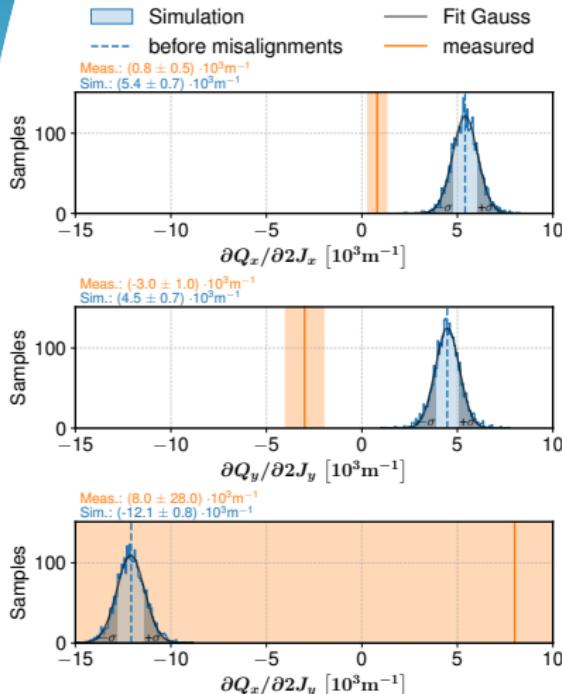


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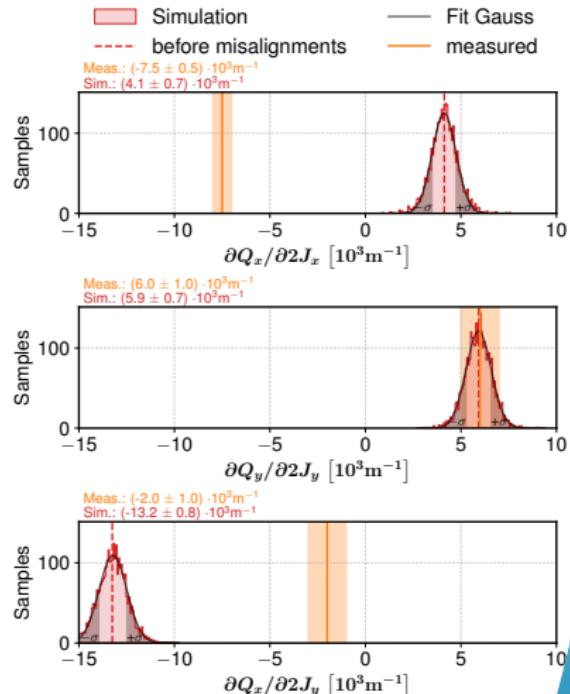


Figure: Beam 2

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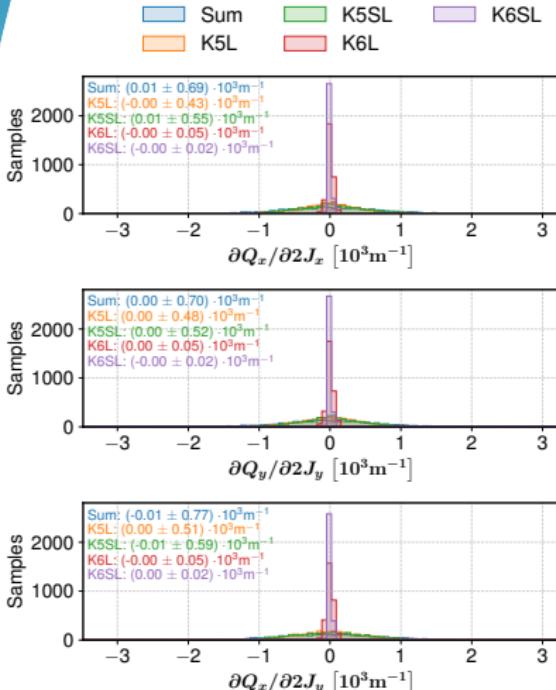


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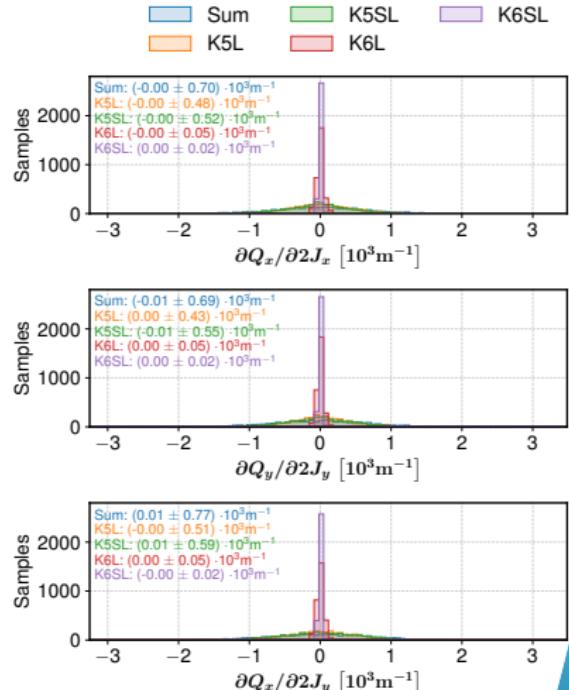


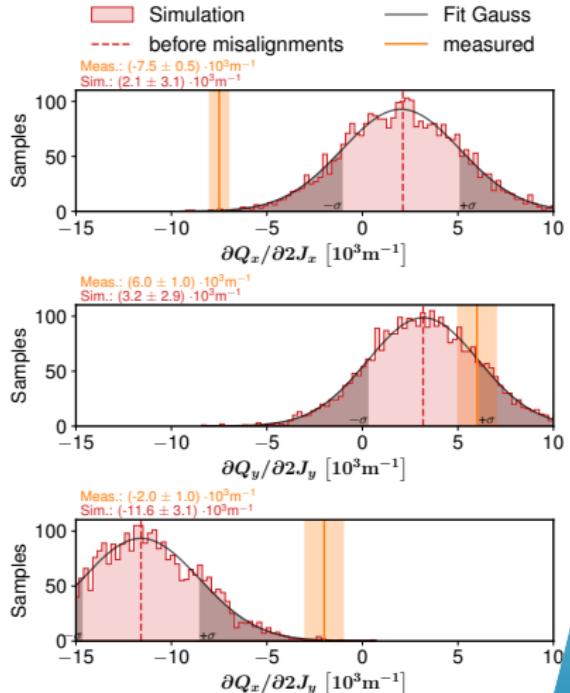
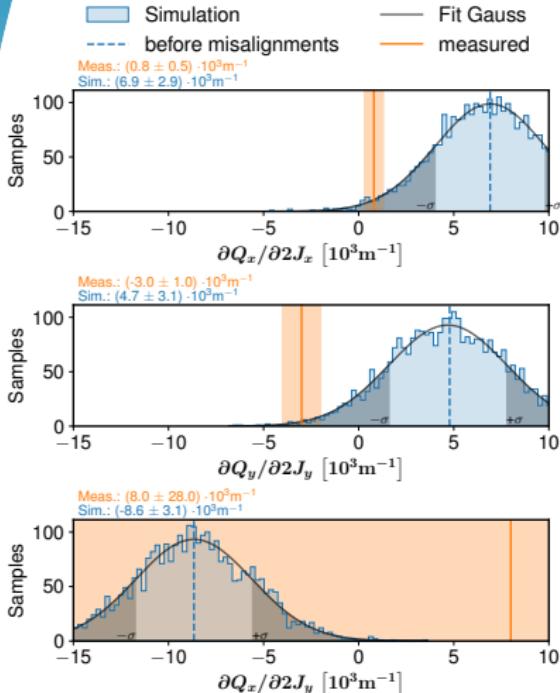
Figure: Beam 2

# Triplet Misalignment Feeddown

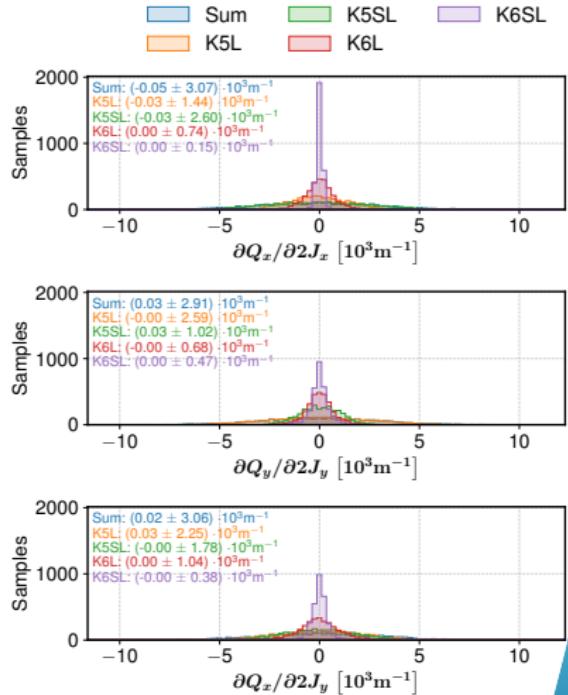
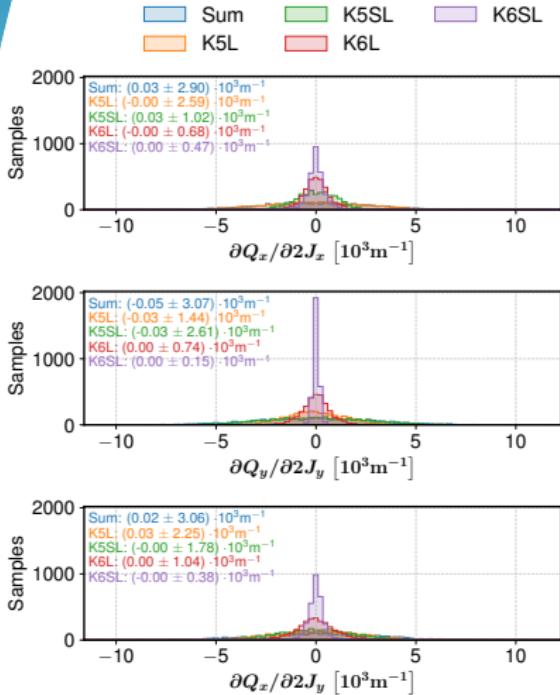
**Table:** Triplet misalignment summary - feeddown from field components to first order amplitude detuning

	[ $10^3 \text{ m}^{-1}$ ]	Sum	Decapole	Skew Decapole	Dodecapole	Skew Dodecapole
Beam 1	$\partial Q_x / \partial 2J_x$	LHC HL-LHC	$0.03 \pm 2.90$ $-0.01 \pm 0.62$	$0.00 \pm 2.59$ $0.00 \pm 0.42$	$0.03 \pm 1.02$ $-0.01 \pm 0.44$	$0.00 \pm 0.68$ $0.00 \pm 0.07$
	$\partial Q_y / \partial 2J_y$	LHC HL-LHC	$-0.05 \pm 3.07$ $0.00 \pm 0.61$	$-0.03 \pm 1.44$ $0.00 \pm 0.42$	$-0.03 \pm 2.61$ $-0.01 \pm 0.44$	$0.00 \pm 0.74$ $0.00 \pm 0.07$
	$\partial Q_x / \partial 2J_y$	LHC HL-LHC	$0.02 \pm 3.06$ $0.00 \pm 0.73$	$0.03 \pm 2.25$ $0.00 \pm 0.50$	$0.00 \pm 1.78$ $0.01 \pm 0.51$	$0.00 \pm 1.04$ $0.00 \pm 0.09$
	$\partial Q_x / \partial 2J_x$	LHC HL-LHC	$-0.05 \pm 3.07$ $0.00 \pm 0.61$	$-0.03 \pm 1.44$ $0.00 \pm 0.42$	$-0.03 \pm 2.60$ $-0.01 \pm 0.44$	$0.00 \pm 0.74$ $0.00 \pm 0.07$
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# Misalign LHC Triplets



# Misalign LHC Triplets



# Misalign HL-LHC Triplets

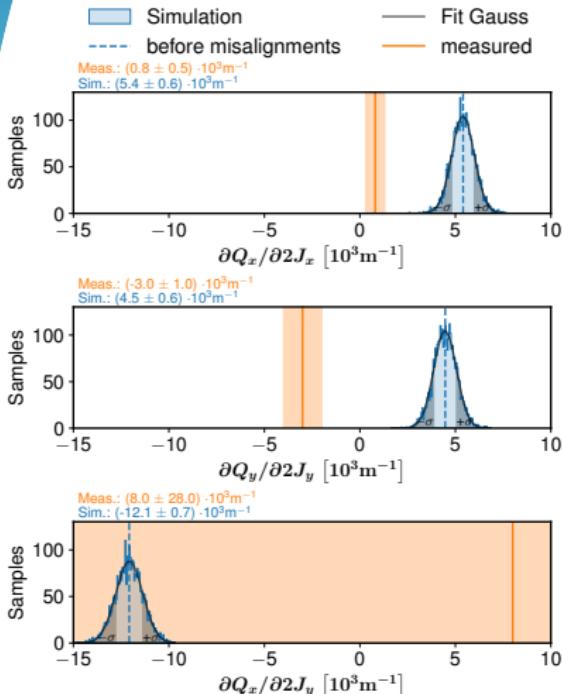


Figure: Beam 1

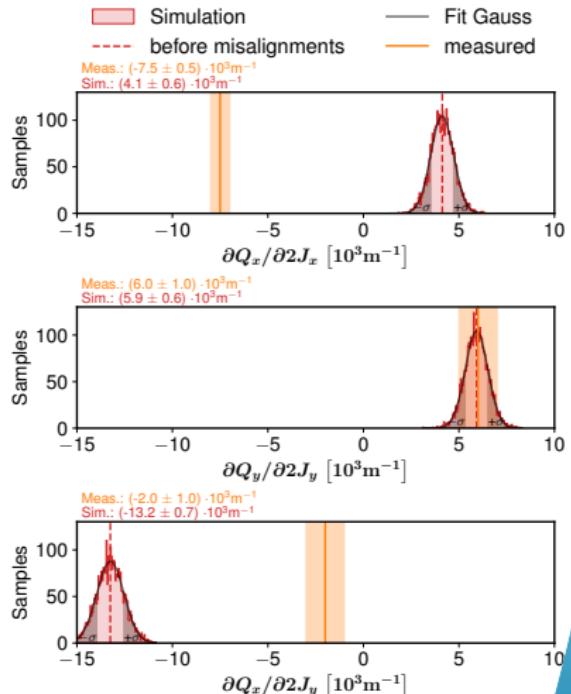
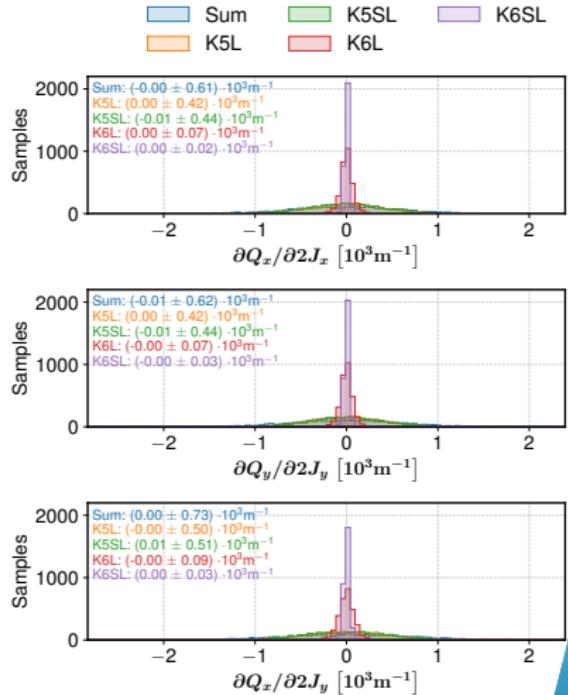
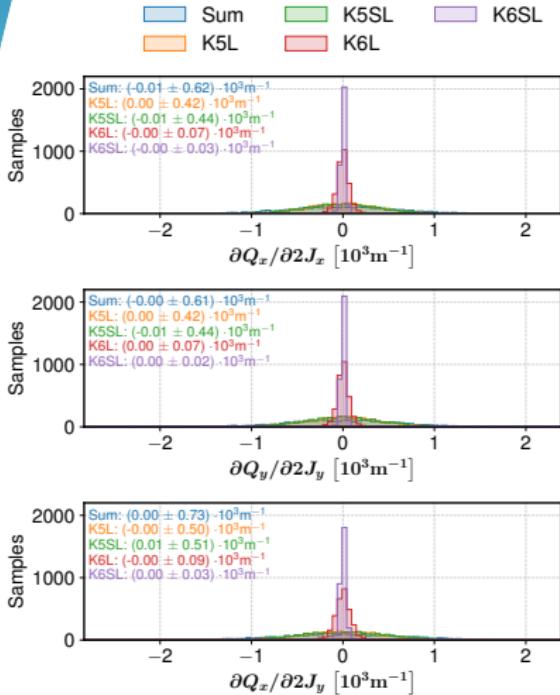


Figure: Beam 2

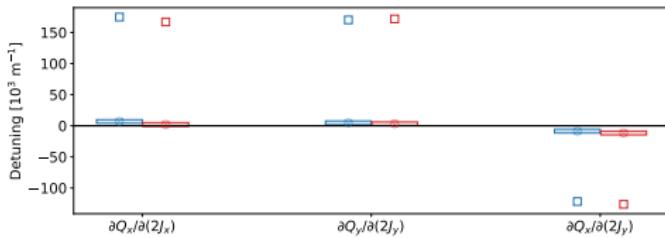
# Misalign HL-LHC Triplets



# Misalign Triplets

... and compare to highly powered MO's

LHC



- MO powering of 570 A causes amplitude detuning to increase from  $\sim 5 \cdot 10^3 \text{ m}^{-1}$  up to  $\sim 170 \cdot 10^3 \text{ m}^{-1}$  in the direct terms.

HL-LHC

