

Charged Higgs production and decay for  
signature of Inert Dark model (old title)

$\Rightarrow$   
**Simple method for measuring of  
properties of Dark Matter particles  
at ILC for different models of DM**

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# Dark matter. Candidates

About 25% of the Universe is made from Dark Matter (DM).

Different candidates for particles of DM have common property: They **conserve specific discrete quantum number**, we name it ***D*-parity**..

Usually particles with new value of *D*-parity form some family — *D*-family, the lightest from them is DM particle.

***MSSM***: DM is lightest superparticle, often – fermion,  $D \rightarrow R$ -parity

***Inert Dark Model, IDM***: DM – Higgs-like scalar,  $D \equiv D$ -parity .....

We consider first models in which lightest *D*-particles are – **neutral  $D^0$  – properly DM particle** and **charged  $D^\pm$**  with identical spin so that main their interaction with ordinary matter is  $D^\pm D^0 W^\mp$ .

In the estimates we have in mind  $M_{D^\pm} \gtrsim 100$  GeV (LEP data)

and  $M_{D^0} < M_{D^\pm} < E \equiv \sqrt{s}/2$  – electron beam energy of ILC

# Production. Decay. Signature

Main production channel  $e^+e^- \rightarrow D^+D^-$

Cross section is  $\sim \sigma(e^+e^- \rightarrow \mu\mu)$  – huge for ILC.

Then — decay  $D^+ \rightarrow W^+D$  with branching close to 1.

Observable final state (**signature**)

Two dijets, representing  $W^+$  and  $W^-$

$(2/3)^2 \approx 0.44$  total cross section;

One dijet +  $e$  or  $\mu$ , representing  $W^+$  and  $W^-$

–  $2 \times (2/3) \times 2[1/9(1 + 0.17)] \approx 0.35$  total cross section

(0.17 is fraction of  $\mu$  or  $e$  from decay of  $\tau$ )

**AND** large missing  $p_{\perp}$  and energy

Cross sections of SM processes with the same observable final state is typically 2 orders of value ( $\sim \alpha$ ) less, since they include radiation of  $\nu$ 's or somewhat else.

$$M_{D^\pm} > M_{D^0} + M_W$$

**Additional signature:** effective mass of dijet close to  $M_W$ .

We denote  $\Delta(s; s_1, s_2) = \sqrt{s^2 + s_1^2 + s_2^2 - 2ss_1 - 2ss_2 - 2s_1s_2}$ .

In the **rest frame of  $D^+$**  the energy and momentum of  $W^\pm$  from decay  $D^+ \rightarrow DW^+$  are

$$E_W^r = \frac{M_{D^+}^2 + M_W^2 - M_{d^0}^2}{2M_{D^+}}, \quad p^r = \frac{\Delta(M_{D^+}^2, M_W^2, M_{D^0}^2)}{2M_{D^+}}.$$

In the **lab system** energy of  $D^\pm$  is equal to beam energy  $E$  and velocity of  $D^\pm$  is  $v = \sqrt{1 - M_{D^\pm}^2/E^2}$ ,  $\gamma = E/M_{D^\pm}$ .

Denoting  $W$  escape angle in  $D^+$  rest frame relative to direction of  $D^+$  motion in the lab system by  $\theta$  and  $c = \cos \theta$  we have energy of  $W^+$  in the lab system  $E_W^L = \gamma(E_W^r + cvp^r)$ .  $W$ 's are distributed within interval  $E(-) = \gamma(E_W^r - vp^r), E(+)= \gamma(E_W^r + vp^r)$ .

The end point values  $E(\pm)$  give two equations for determination of masses  $D^\pm$  and  $D^0$ .

The distribution of these dijets in energy is uniform.  $dN(E) \propto dE$  since there is no correlation between escape angle of  $W$  in the rest frame of  $D^\pm$  and production angle of  $D^\pm$ .

For scalars it is evident, for fermions there is dependence on the  $D^\pm$  spin direction. It results in correlations like those in  $Z$ -peak

After determining of  $M_{D^\pm}$ , cross section of  $e^+e^- \rightarrow D^+D^-$  process is calculated precisely with QED for each D-particle spin value. It allows to determine spin of  $D$  particles via measuring of cross sections (typically  $\sigma(e^+e^- \rightarrow D^+D^-)/\sigma(e^+e^- \rightarrow \mu^+\mu^-)$  is about 1/4 if  $D^\pm$  – scalar, it is about 1 if  $D^\pm$  – fermion)

Observation of process  $e^+e^- \rightarrow D^+D^- \rightarrow D^0D^0jj\ell + \nu$ 's allow to determine **sign of charge of 2-jets  $W = q\bar{q}$**  in each separate case. It allows to study charge and polarization asymmetries (like at  $Z$ -peak) for checking on more detail properties of  $D$ -particles.



**If  $M_{D^\pm} < M_{D^0} + M_W$ ,**

single decay channel is  $D^+ \rightarrow D^0 W^*$ , where  $W^*$  means dijet ( $q\bar{q}$ ) or  $\ell\nu$  system having effective mass  $M^* < M_W$ . ( $M^* < M_{D^+} - M_{D^0}$ ). All above results are valid for each separate value  $M^*$  with the change in all equations  $M_W \rightarrow M^*$ .

The energy and  $M^*$  distributions for each pair of dijets are independent from each other.

If  $M_{D^\pm} \gg M_{D^0} + M_W$ ,

proper width of  $D^\pm$  is large enough (for scalars

$$\frac{\Gamma(D^+ \rightarrow D^0 W^+)}{M_{D^+}} = \frac{\alpha}{2 \sin^2 \theta_W} \frac{(p^r)^3}{M_W^2 M_{D^\pm}}.$$

(This ratio  $> 0.1$  at  $M_{D^\pm} \gtrsim 500$  GeV). In this case the energy and  $M^*$  distribution of dijets will be convolution of uniform distribution for narrow  $D^\pm$  with Breit-Wigner mass distribution. One can hope that the measuring of violation of the observed energy distribution from uniform will allow to determine both mass of  $D^\pm$  and its width.

## Axial $D$ -particle $D^A$

For scalar  $D$ -particles, the pseudoscalar  $D^A$  also exists, it has interaction  $ZD^AD^0$ .

Therefore the process  $e^+e^- \rightarrow Z \rightarrow D^0D^A \rightarrow D^0D^0Z$  has only cross section of the same order as  $e^+e^- \rightarrow \mu^+\mu^-$  and observable either dilepton ( $e^+e^-$  or  $\mu^+\mu^-$ ) or dijet with effective mass equal to  $M_Z$  (with accuracy to  $Z$  width).

Almost entire above discussion is valid in this case.

The observation of these dilepton or dijet with large missed energy and  $p_\perp$  gives good signature of DM.

$$\text{If } M_{D^\pm} > M_{D^A} + M_W$$

cascade processes like

$$e^+e^- \rightarrow D^+D^- \rightarrow D^A W^+ D^0 W^- \rightarrow D^0 Z W^+ D^0 W^-$$

become possible. In this case the energy distribution for W-produced di-jets will be sum of distributions of the first case types and additional signature in the form of dilepton pair also exist.

# SUMMARY

In many models of DM the process  $e^+e^- \rightarrow D^+D^-$  must be studied.

The signature:

2 di-jets, representing  $W$  or 1 di-jet +lepton plus large missing  $p_\perp$  and energy with cross section close to main cross section of  $e^+e^-$  annihilation

**Masses of  $D^\pm$  and DM candidate  $D^0$**

will be determined via end points of energy distribution of  $W$  representing di-jets either at  $M^* \approx M_W$  or at  $M^* < M_W$ .

**Spin**

will be determined via (even rough) measuring of total cross section

# SUMMARY (continuation)

If particle  $D^A$  having parity opposite to that of  $D^0$  exists,  
the process  $e^+e^- \rightarrow D^0D^A \rightarrow D^0D^0Z$  must be studied.

The signature:

di-jet or dilepton, representing  $Z$  plus large missing  $p_\perp$  and energy with cross section close to main cross section of  $e^+e^-$  annihilation

**Masses of  $D^A$  and DM candidate  $D^0$**

will be determined via end points of energy distribution of  $Z$  representing di-jet or dilepton.

**Spin**

will be determined via (even rough) measuring of total cross section