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# The MINER $\nu$ A Flux Prediction

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*On behalf of the MINER $\nu$ A Collaboration*

Seoul National University, Seoul, Korea

October 25<sup>th</sup>, 2022

**NuINT 2022**

The 13th International Workshop on Neutrino-Nucleus Interactions  
in the Few GeV Regions

# Flux @ MINERvA



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*Main INjector ExpeRiment for  $\nu$ -A scattering*



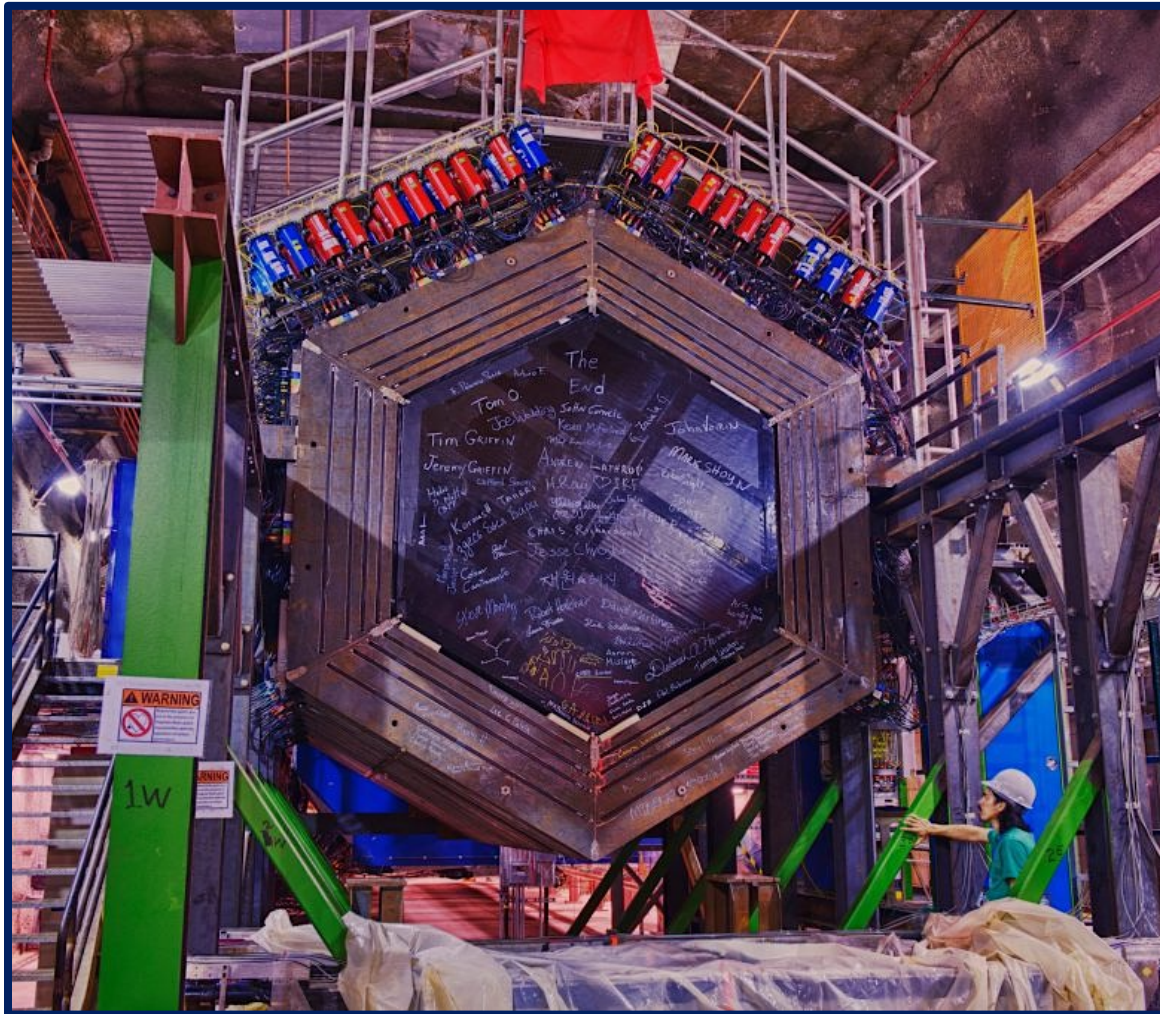
- The only currently active **neutrino cross-section experiment with high-statistics**, controlled systematics, different nuclear targets, and access to the DIS region
- 2009-2019 on axis in the **NuMI beamline** at Fermilab in 2 flux periods with 3.5 and 6 GeV flux peak, both in  $\nu/\bar{\nu}$

# Flux @ MINERvA

*Main INjector ExpeRiment for  $\nu$ -A scattering*



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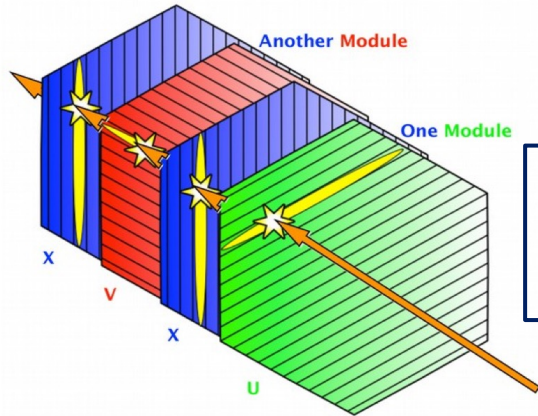


- **Dedicated flux campaign** with corrections to a-priori flux and in-situ measurements
  - Neutrino-nucleus scattering with low hadronic recoil
    - [A. Bashyal et al. JINST 16 P08068 \(2021\)](#)
  - Neutrino-electron elastic scattering
    - [E. Valencia et al. Phys. Rev. D 100, 092001 \(2019\)](#)
  - Inverse muon decay (IMD)
    - [D. Ruterbories et al. Phys. Rev. D 104, 092010 \(2021\)](#)
  - Combined constraint using  $\nu/\bar{\nu}$ -electron scattering and IMD
    - [L. Zazueta et al. Submitted for publication, \[hep-ex\]:2209.05540 \(2022\)](#)

# MINERvA Detector

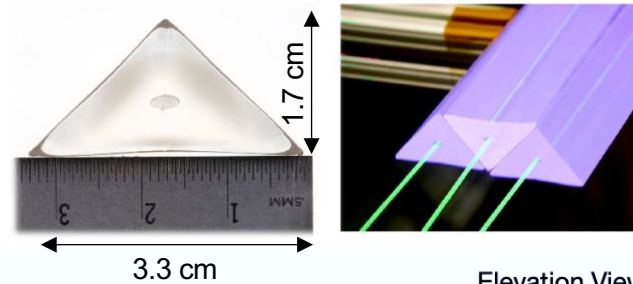


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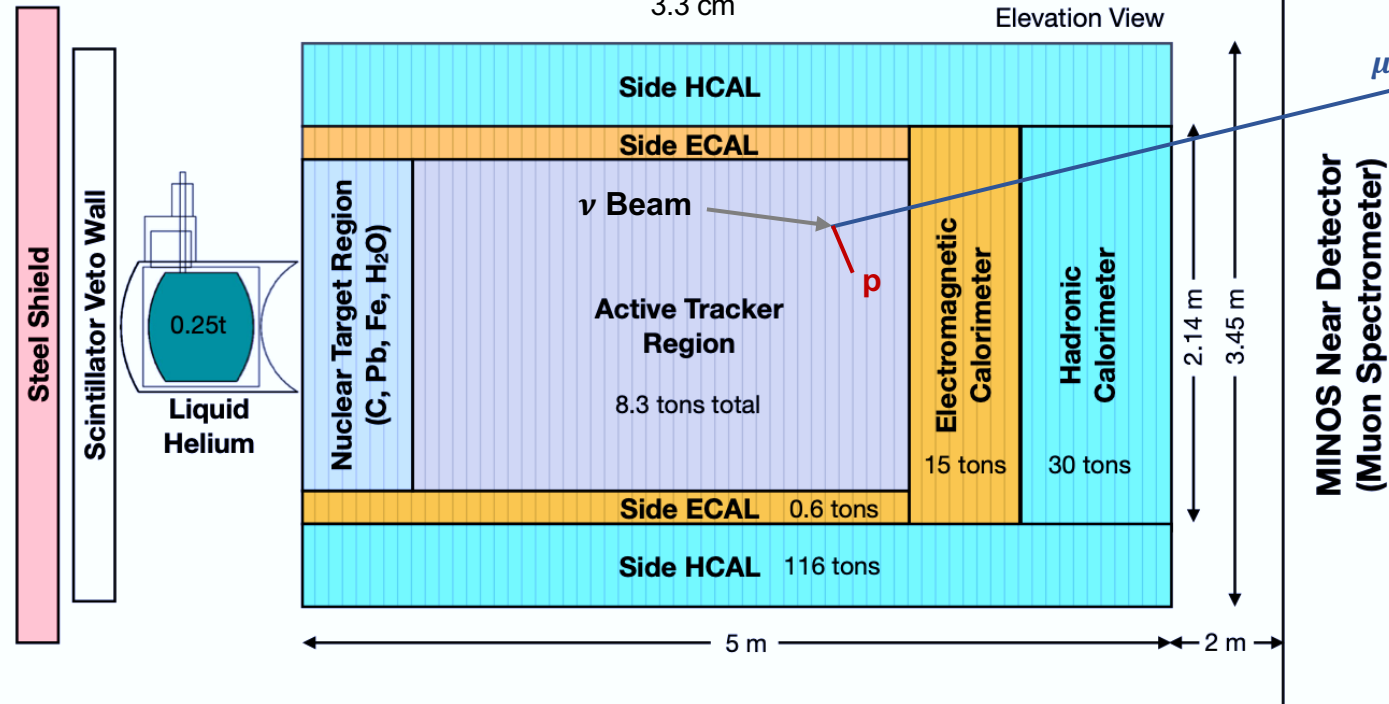
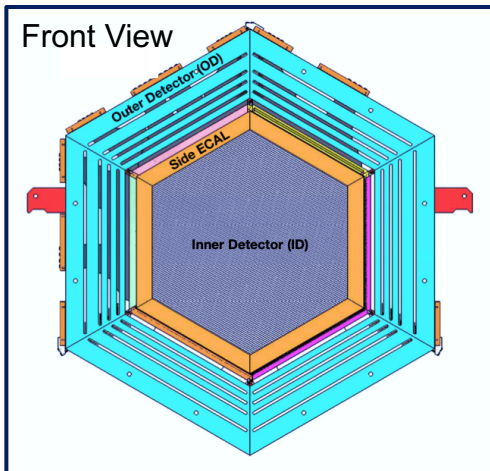


3 orientations of scintillator planes give unambiguous 3D track reconstruction.

Triangular strips arranged to give a better position resolution.



Read out using wavelength-shifting (WLS) fibres and photomultiplier tubes (PMTs): timing resolution better than  $\sim 5$  ns to distinguish overlapping events within a single spill ( $< 10 \mu\text{s}$ ).

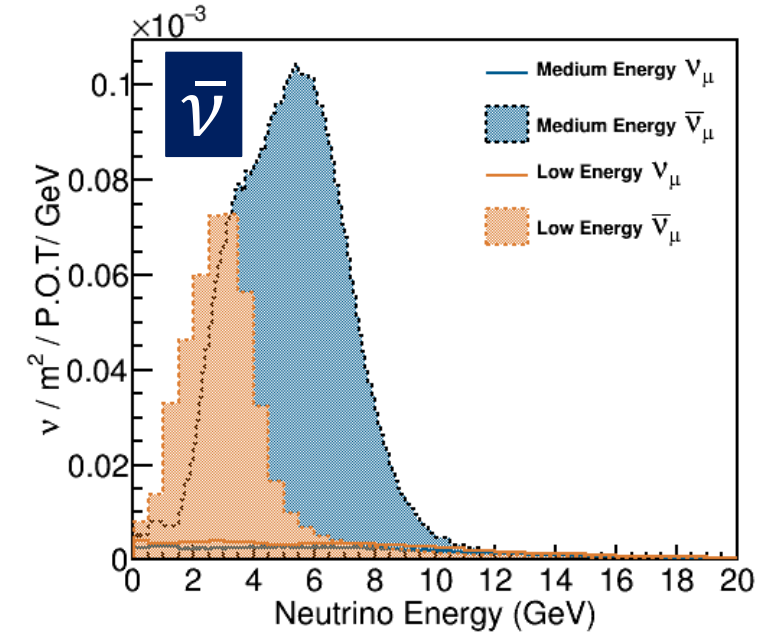
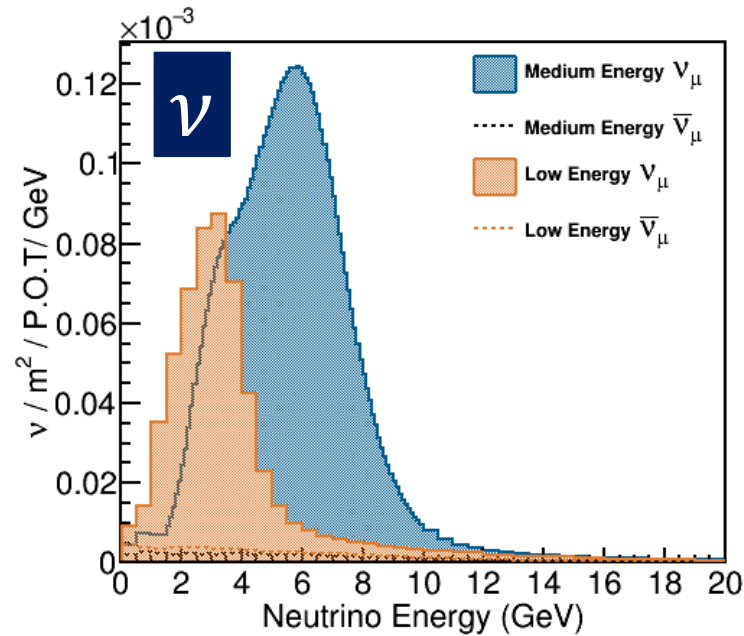


MINOS spectrometer: muon momentum and charge.

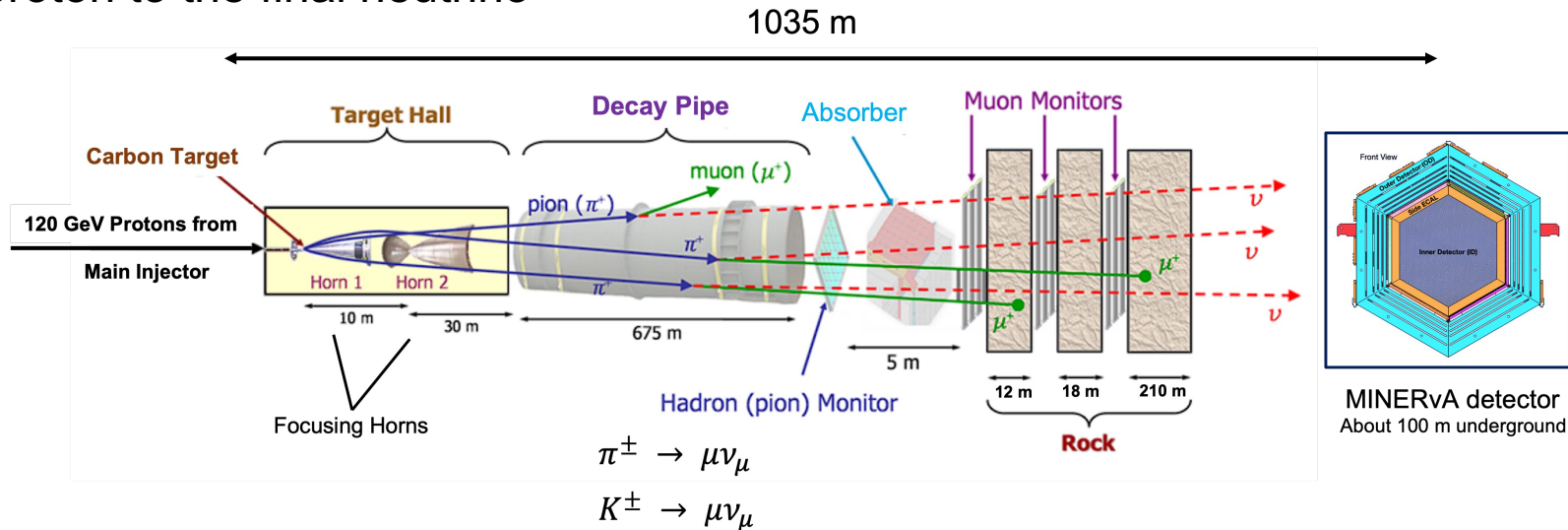
# NuMI Flux

- 2 flux periods with 3.5 and 6 GeV flux peak, both in  $\nu/\bar{\nu}$

Regime \ Mode	$\nu$ (POT)	$\bar{\nu}$ (POT)
Low (LE) ~ 3.5 GeV	$4 \times 10^{20}$	$1.7 \times 10^{20}$
Medium (ME) ~ 6 GeV	$12.1 \times 10^{20}$	$12.4 \times 10^{20}$

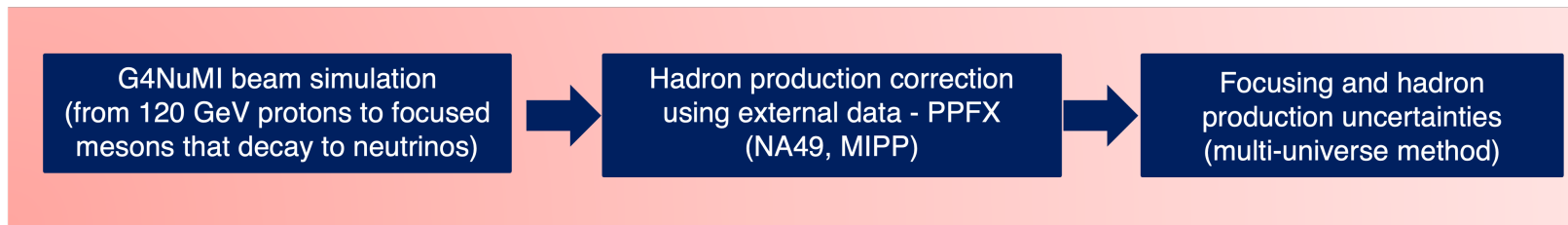


- Need to understand each step from the primary proton to the final neutrino

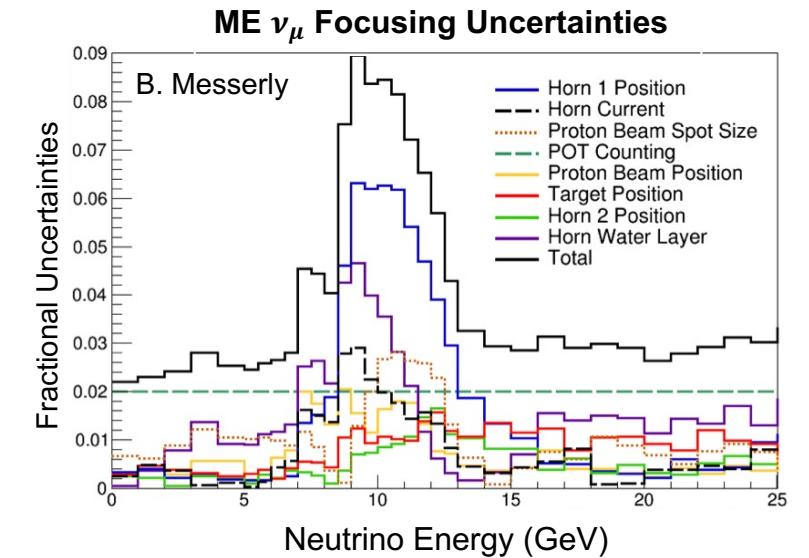
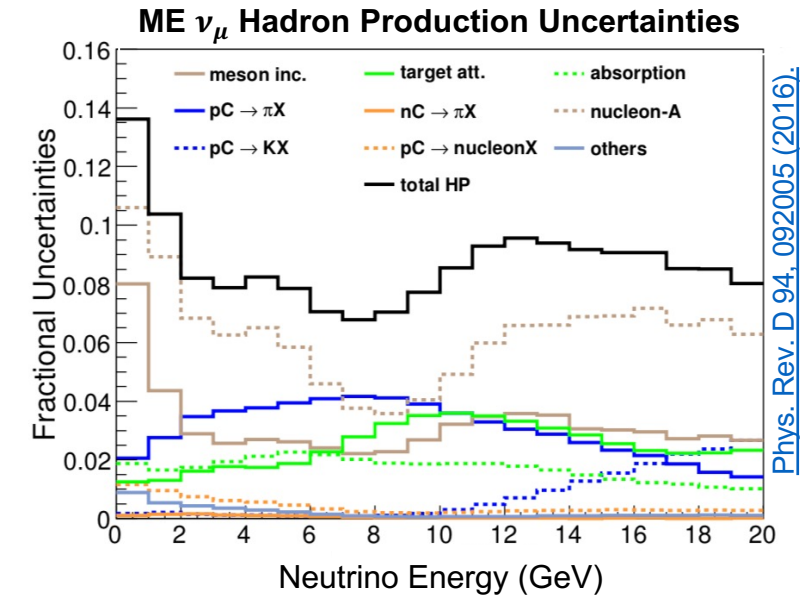
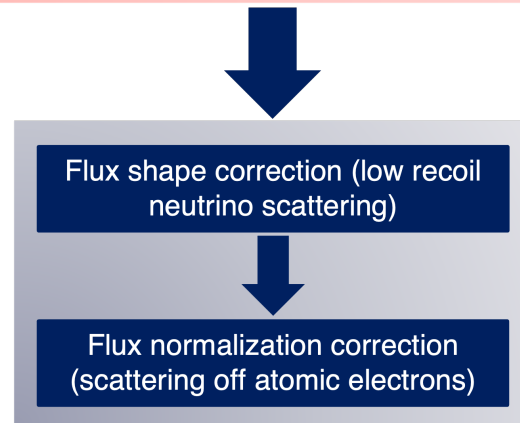


# Simulation & Uncertainties

## 1. Calculate and correct the a-priori flux



## 2. Use in-situ measurements



Small simulation inaccuracies have a big impact around the focusing peak!

# In situ Measurements To Constrain Flux



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- 1. Neutrino-nucleus scattering with low hadronic recoil**
2. (Anti)Neutrino-electron elastic scattering
3. Inverse muon decay (IMD)
4. Combined constraint using  $\nu/\bar{\nu}$ -electron and IMD

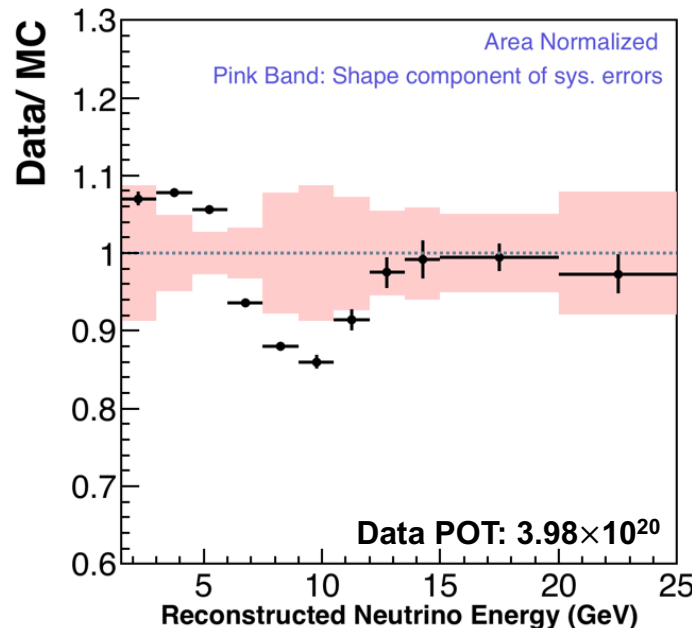
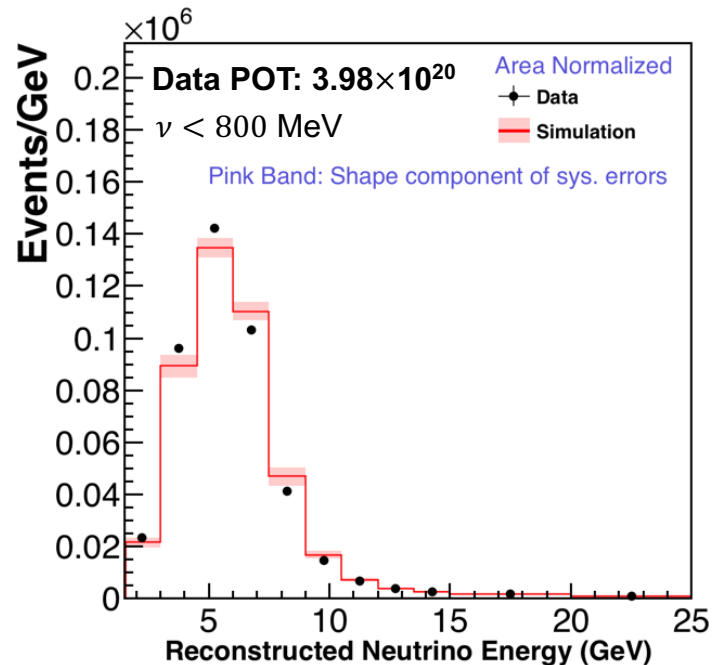
# Neutrino-Nucleus Scattering w/ Low Hadronic Recoil



- CC  $\nu_\mu$  inclusive cross-section if  $\nu/E_\nu$  small  $\propto$  const. and independent of energy

$$\frac{d\sigma}{d\nu} = \frac{G_F^2 M}{\pi} \int_0^1 \left( F_2 - \frac{\nu}{E_\nu} [F_2 + xF_3] + \frac{\nu}{2E_\nu^2} \left[ \frac{Mx(1-R_L)}{1+R_L} F_2 \right] + \frac{\nu^2}{2E_\nu^2} \left[ \frac{F_2}{1+R_L} + xF_3 \right] \right) dx$$

- Can measure **the shape of neutrino flux** by measuring the event rate( $E_\nu$ )



Discrepancies between data and MC predictions  $\rightarrow$  due to mismodeling of our **focusing parameters** or **instrumental**.



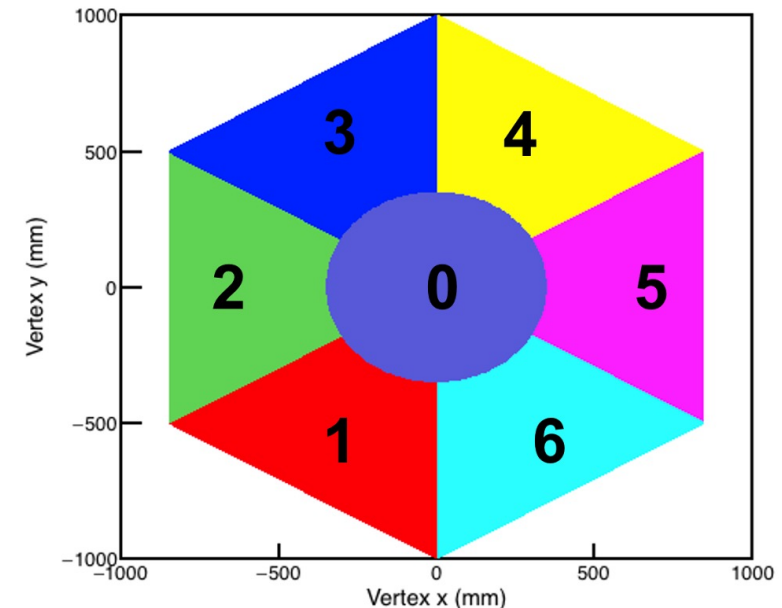
# Flux Fit w/ Focusing Parameters



- Multi-parameter fit with focusing parameters to investigate the discrepancy
- Shifts in focusing parameters not uniform across the face of the detector → fit in 7 bins (and merge later)
- Fit suggests **large shifts** in **longitudinal target position** and **horn current**
- NuMI experts are confident the parameters were within the tolerance

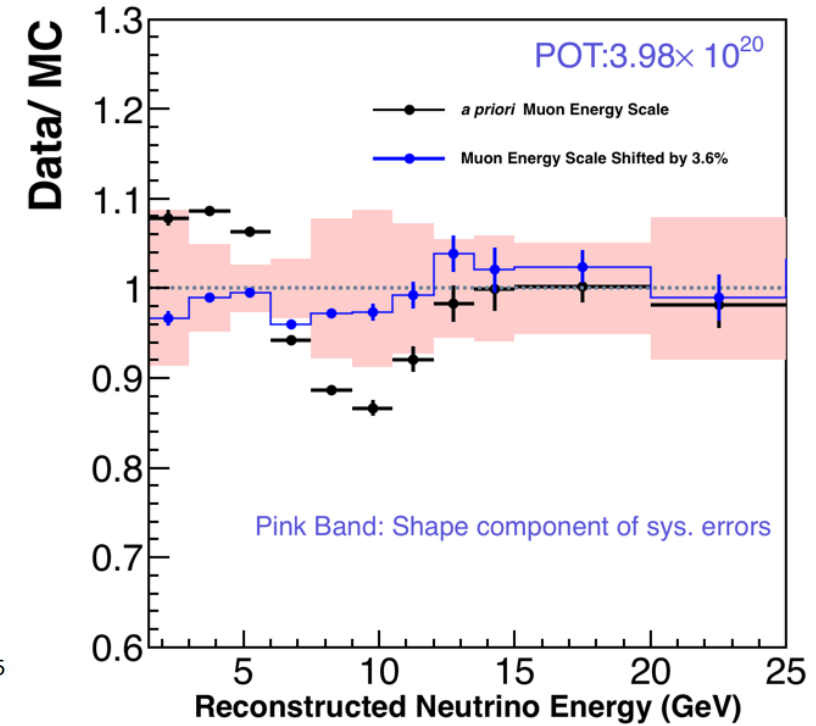
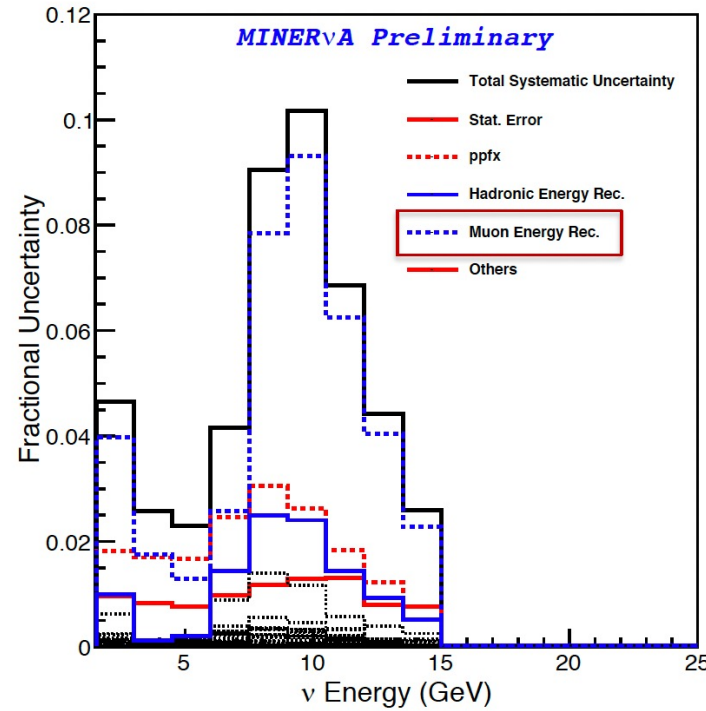
Parameter	Nominal Value	New Value
Beam Position (X)	0 mm	$-0.2 \pm 0.12$ mm
Beam Position (Y)	0 mm	$-0.53 \pm 0.14$
Beam Spot Size	1.5 mm	$1.22 \pm 0.14$ mm
Horn Water Layer	1 mm	$0.895 \pm 0.16$ mm
<b>2.6<math>\sigma</math></b> Horn Current	200 kA	$197.41 \pm 0.76$ kA
Horn 1 Position (X)	0 mm	$0. \pm 0.17$ mm
Horn 1 Position (Y)	0 mm	$-0.39 \pm 0.17$ mm
Target Position (X)	0 mm	$-0.32 \pm 0.17$ mm
Target Position (Y)	0 mm	$1.65 \pm 0.5$ mm
<b>&gt;10<math>\sigma</math></b> Target Position (Z)	-1433 mm	$-1419.44 \pm 1.83$ mm

**Note:** X horizontal, Y vertical, Z longitudinal (along the beam)



# An Instrumental Effect?

- Flux fit **sensitive to muon energy reconstruction**
- Added muon energy scale as a fitting parameter along with focusing parameters
- **Shift of  $1.8\sigma$  in muon energy scale resolves the data/MC discrepancy, other parameters within their standard deviations**
- **MINERvA analyses shift muon energy scale in data by  $1.8\sigma$  (3.6% of the nominal value)**
  - No shift to focusing parameters



Parameter	Nominal	Best Fit (No Prior)	Best Fit (Prior)
Beam Position (X)	0.0 mm	$-0.3 \pm 0.3 \pm 0.1$ mm	$-0.3 \pm 0.2 \pm 0.1$ mm
Beam Position (Y)	0.0 mm	$0.8 \pm 0.3 \pm 0.3$ mm	$0.7 \pm 0.2 \pm 0.2$ mm
Target Position (X)	0.0 mm	$-0.8 \pm 0.3 \pm 0.1$ mm	$-0.8 \pm 0.3 \pm 0.1$ mm
Target Position (Y)	0.0 mm	$2.3 \pm 0.7 \pm 1.2$ mm	$1.7 \pm 0.6 \pm 0.8$ mm
Target Position (Z)	-1433 mm	$-1432.4 \pm 2.4 \pm 0.3$ mm	$-1431 \pm 1.8 \pm 0.3$ mm
Horn 1 Position (X)	0.0 mm	$-0.3 \pm 0.4 \pm 0.5$ mm	$-0.1 \pm 0.3 \pm 0.1$ mm
Horn 1 Position (Y)	0.0 mm	$0.1 \pm 0.5 \pm 0.5$ mm	$0.0 \pm 0.3 \pm 0.3$ mm
Beam Spot Size	1.5 mm	$1.41 \pm 0.09 \pm 0.03$ mm	$1.32 \pm 0.09 \pm 0.03$ mm
Horn Water Layer	1.0 mm	$1.2 \pm 0.3 \pm 0.05$ mm	$1.3 \pm 0.25 \pm 0.1$ mm
Horn Current	200 kA	$198.0 \pm 1.4 \pm 1.4$ kA	$199.1 \pm 0.7 \pm 0.5$ kA
<b>Muon Energy Scale</b>	1.0	$1.032 \pm 0.004 \pm 0.008$	$1.036 \pm 0.004 \pm 0.006$

**$1.8\sigma$**

# In situ Measurements To Constrain Flux

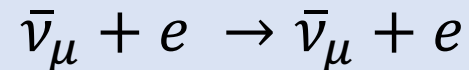
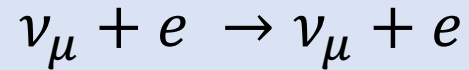


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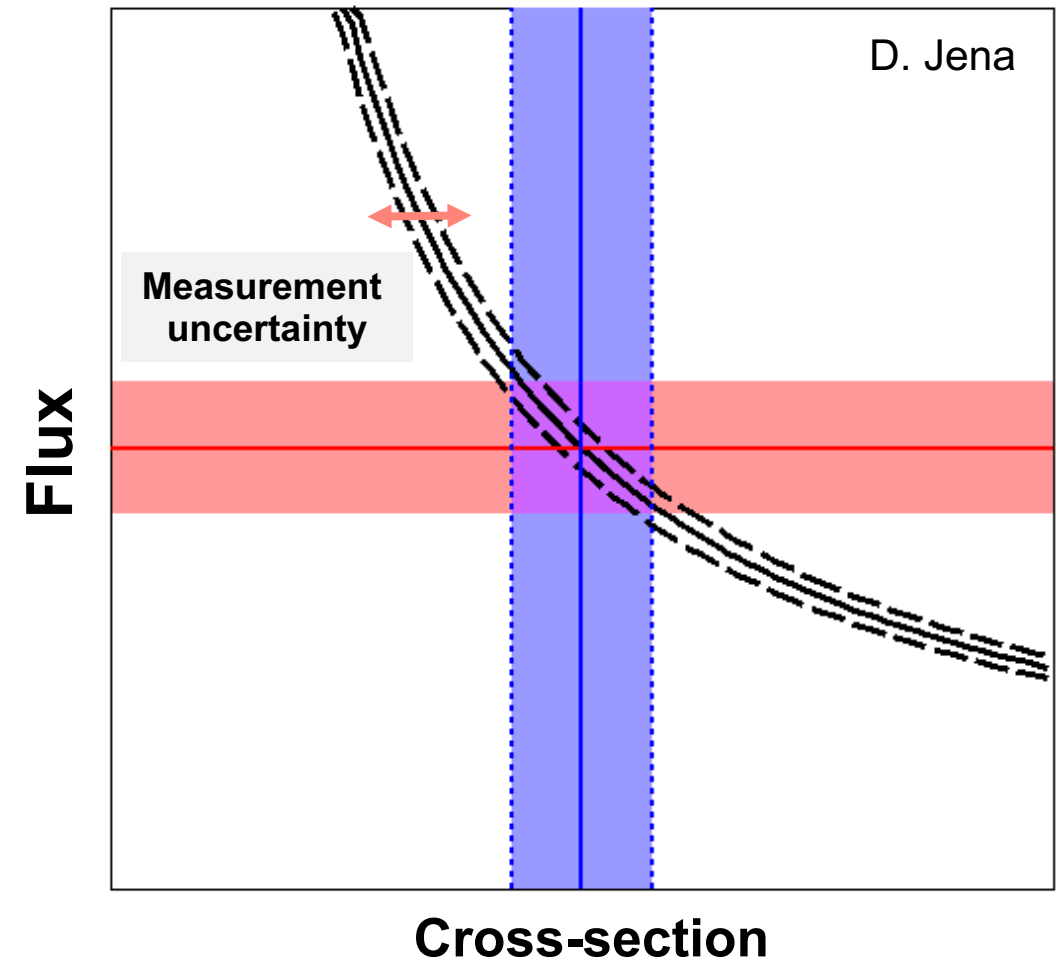
1. Neutrino-nucleus scattering with low hadronic recoil
- 2. (Anti)Neutrino-electron elastic scattering**
3. Inverse muon decay (IMD)
4. Combined constraint using  $\nu/\bar{\nu}$ -electron and IMD

# (Anti)Neutrino-Electron Elastic Scattering

- MINERvA uses the **standard candle for flux estimate** – (anti)neutrino-electron elastic scattering **BOTH in anti/neutrino beam in medium energy**



- Cross-section **precisely predicted** by the standard electroweak scattering theory
- **Limited statistics**: three orders of magnitude smaller than neutrino-nucleus cross-section
- Final state distribution of electron energies – **constraint on integrated flux** (improvement in normalization uncertainty)

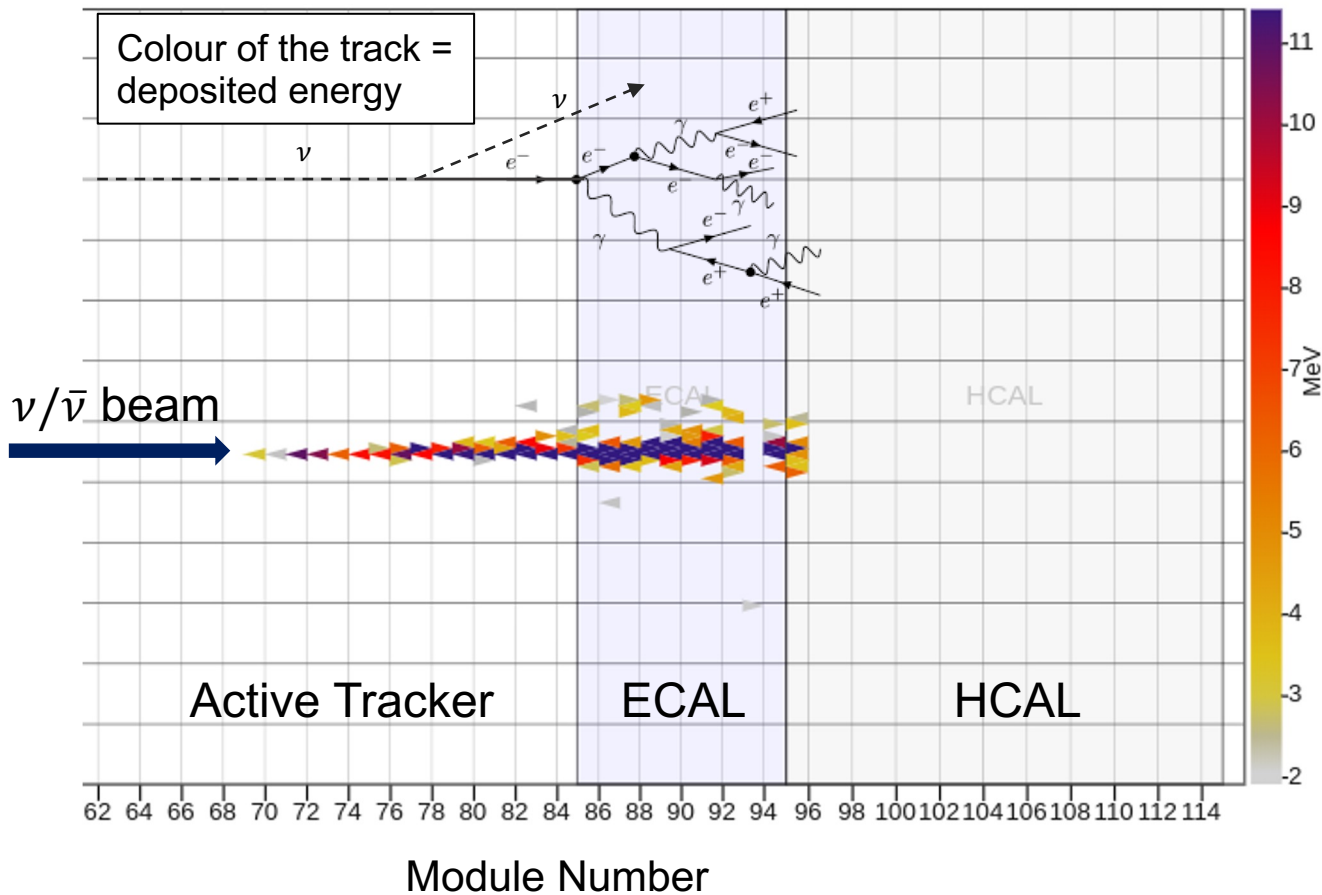


$$\text{Cross-section} = \frac{\text{\# of events}}{\text{Acceptance} \times \text{efficiency} \times \text{Flux}}$$

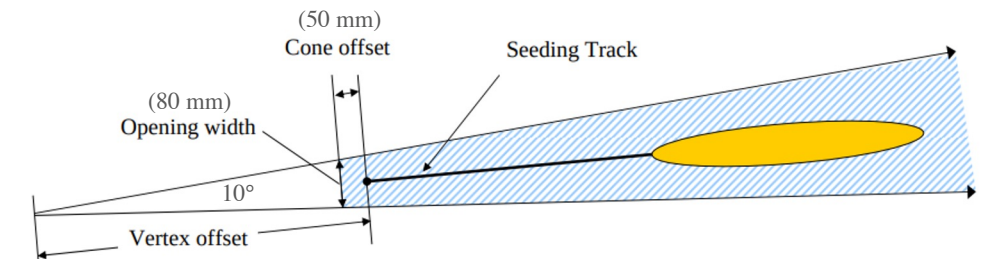
# Experimental Signature



- Very forward electromagnetic shower with vertex in the scintillator tracker and no other activity



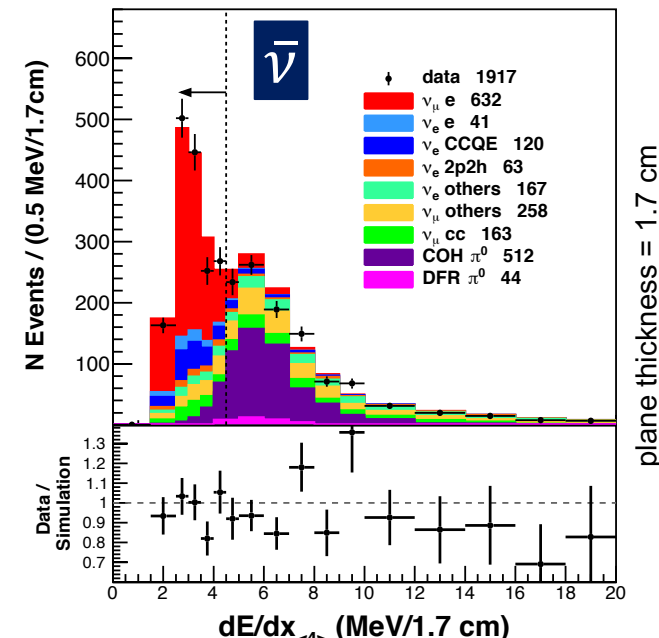
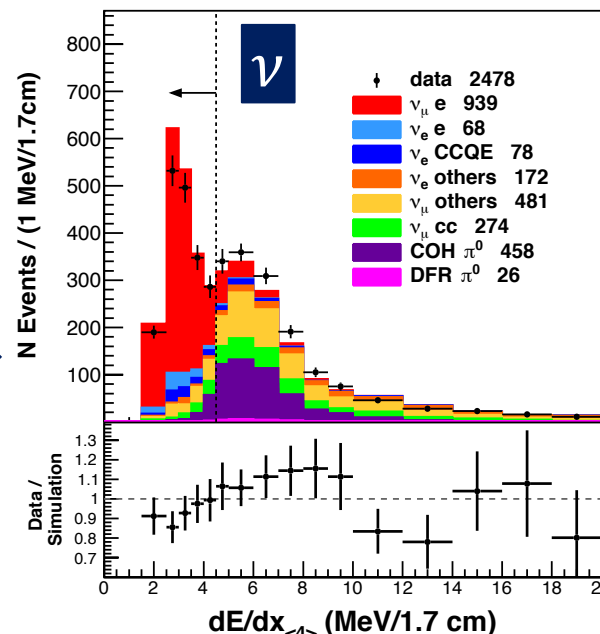
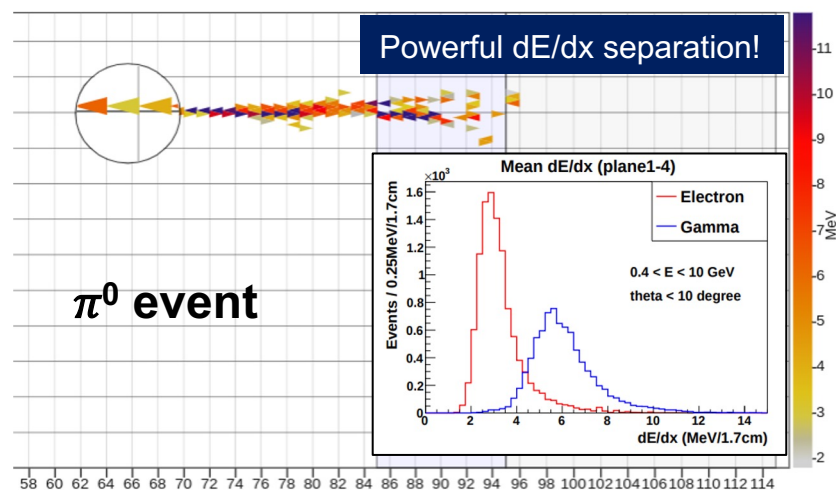
- Candidates reconstructed using cone algorithm



# Main Background Rejection

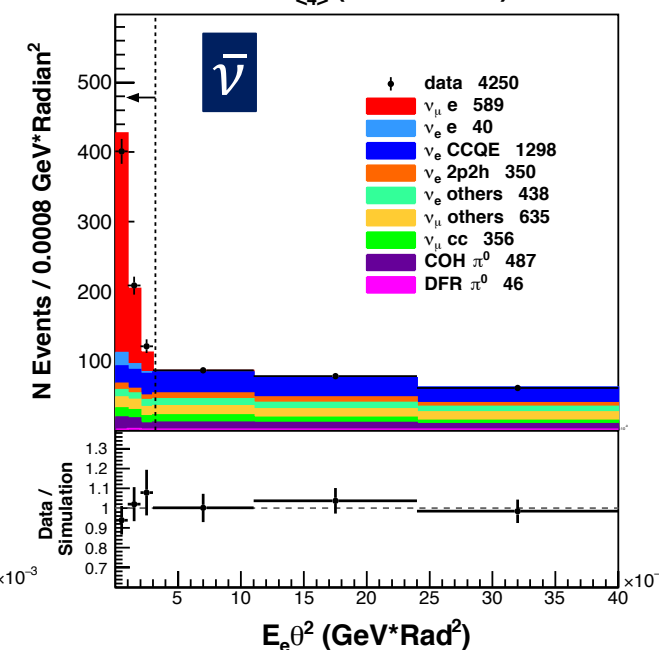
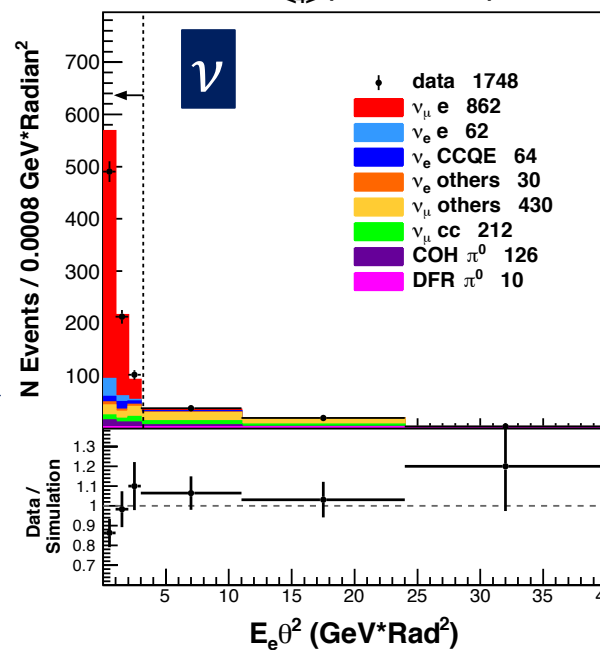
1. Photon background from  $\pi^0$  vs EM shower pair production (signal)

- Deposited energy per unit length  $dE/dx$



2. Kinematics of neutrino-electron elastic scattering

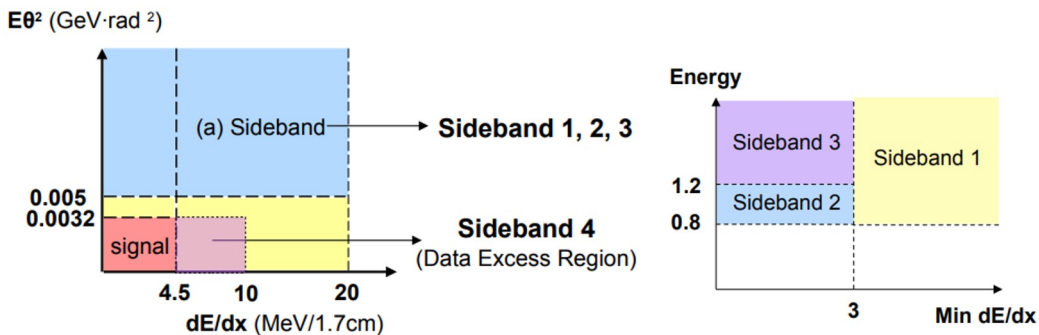
$$E_e \theta_e^2 < 2m_e$$



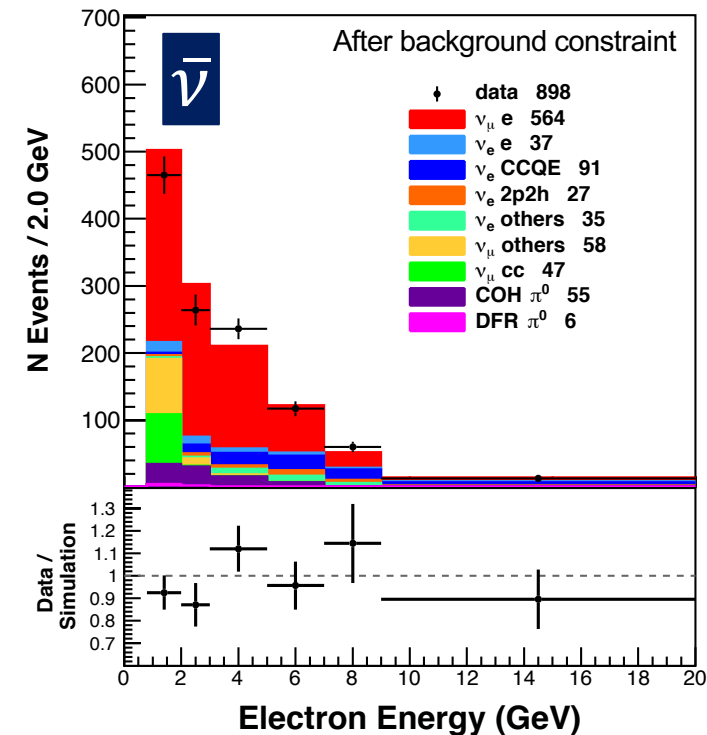
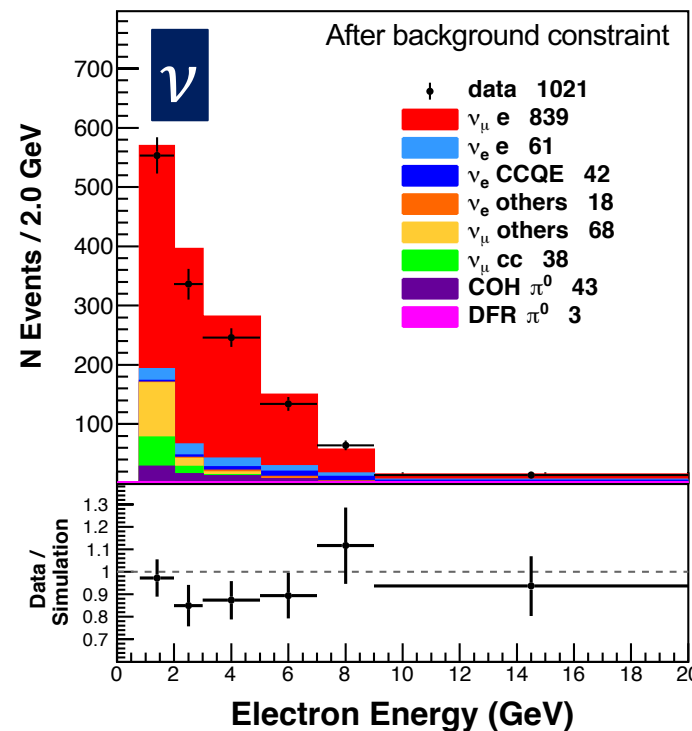
# Background Prediction & Selected Sample

- Background predicted by the simulation – main source of uncertainty
- Constrained by simultaneous fit to 4 kinematic sidebands
  - Single normalization factor for  $\nu_e$ ,  $\nu_\mu$  CC,  $\nu_\mu$  NC
  - Normalization of coherent  $\pi^0$  in 6 bins of electron energy

Background type	$\nu$ -mode	$\bar{\nu}$ -mode
$\nu_\mu$ neutral current coherent & diffractive $\pi^0$	~ 50%	/ ~ 50%
$\nu_\mu$ charged current	~ 20%	/ ~ 35%
$\nu_e$ interactions	~ 30%	/ ~ 15%



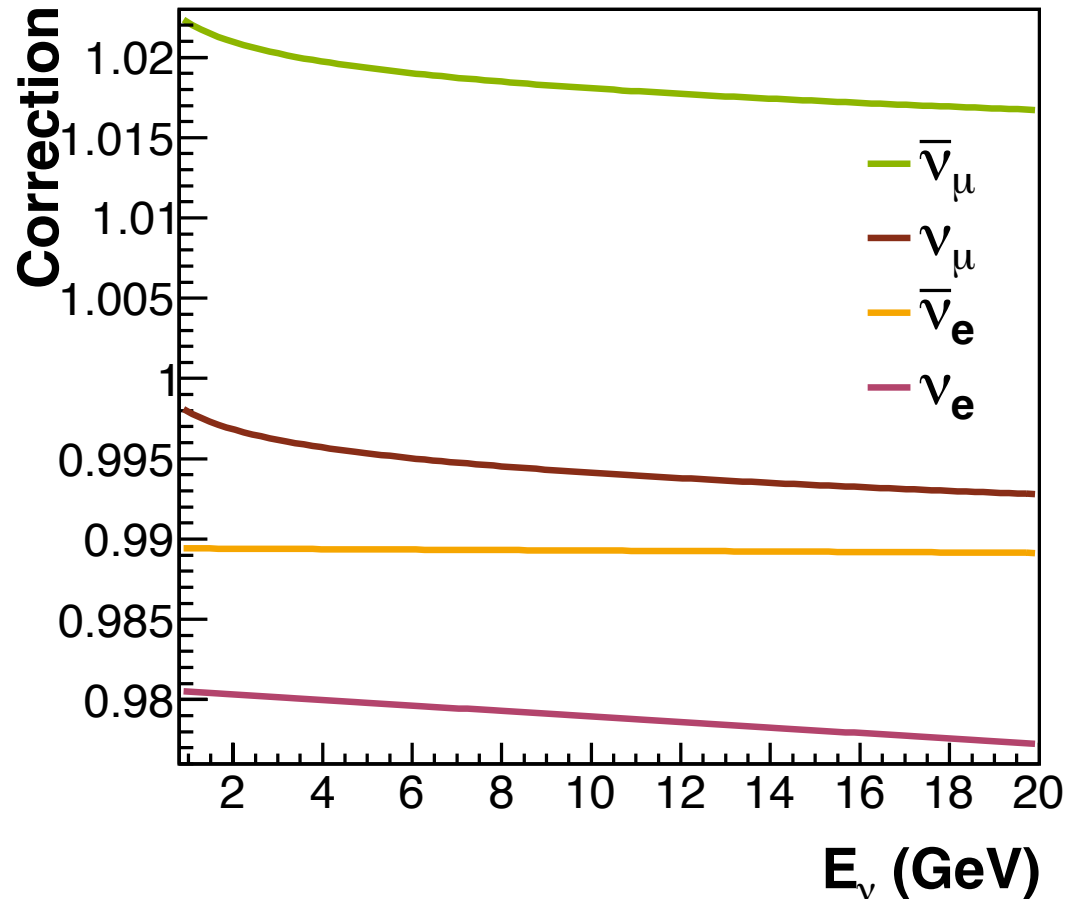
**Sideband 1:** shower + vertex activity; **Sideband 2:**  $\nu_\mu$  enriched  
**Sideband 3:**  $\nu_e$  enriched; **Sideband 4:**  $\pi^0$  enriched



# Radiative Corrections



Ratio between Phys. Rev. D 101, 033006 (2020)  
x-secs and GENIE 2.12.6.



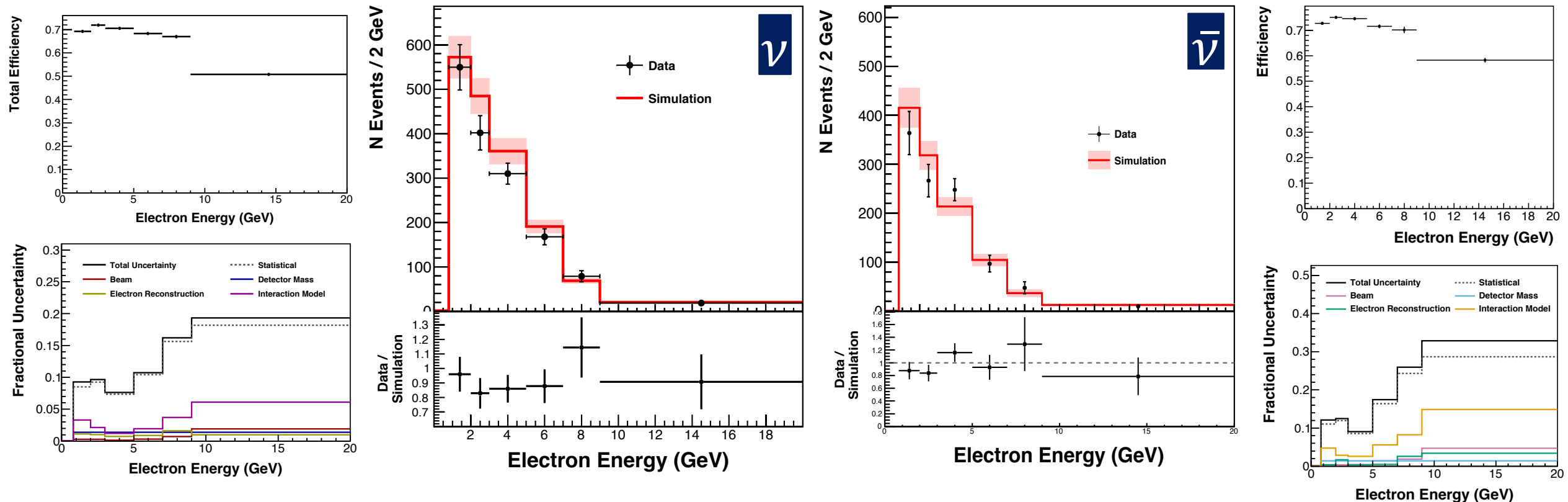
- GENIE tree-level cross-section reweighted to match the one calculated **including radiative corrections**
  - [O. Tomalak, R. J. Hill. Phys. Rev. D 101, 033006 \(2020\)](#)
  - Includes production of real photons in final state



# Final Electron Energy Spectra



- Subtracted tuned background and corrected by the efficiency  $\rightarrow$  dominated by statistical uncertainty



# Flux Constraint Procedure



- Using Bayes' theorem

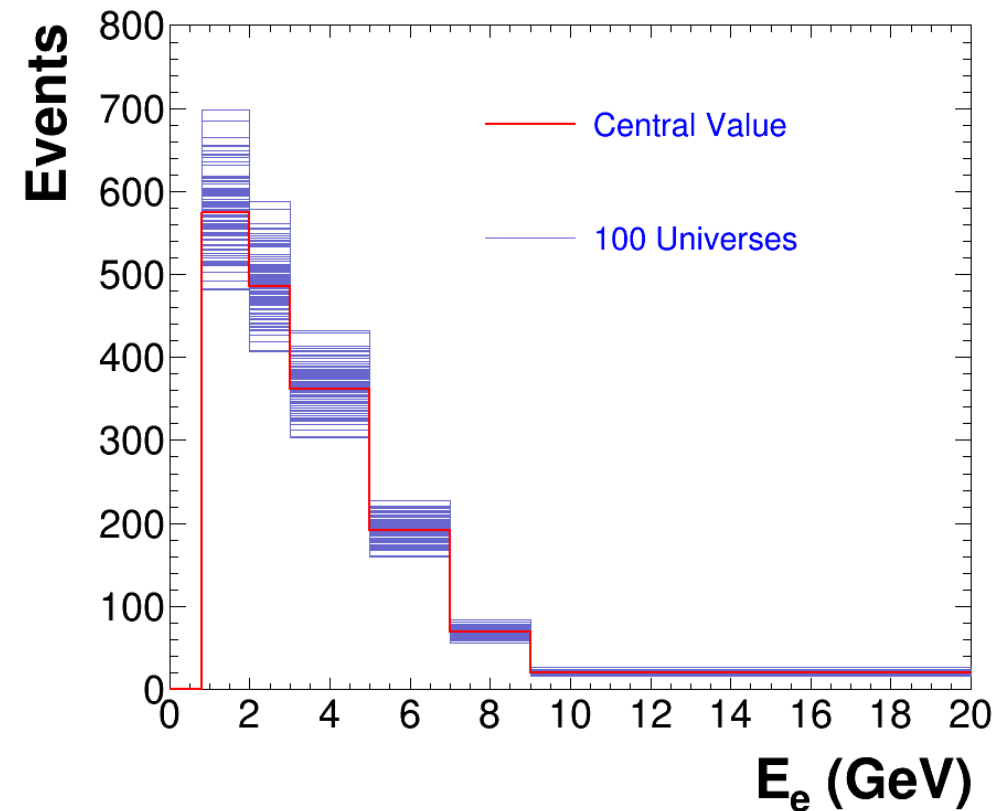
$$P(M|N_{\nu e \rightarrow \nu e}) \propto P(M) P(N_{\nu e \rightarrow \nu e}|M)$$

$P(M|N_{\nu e \rightarrow \nu e})$  new prediction (posterior) probability of the flux prediction given the electron spectra measurement)

$P(M)$  flux prediction in each universe/model (prior)

$P(N_{\nu e \rightarrow \nu e}|M)$  likelihood of the electron spectra measurement given the a-priori model

- A-priori flux uncertainty estimated using **multiverse method**
  - Ensemble of flux predictions by varying flux parameters within their uncertainties (hadron production, beam alignment)



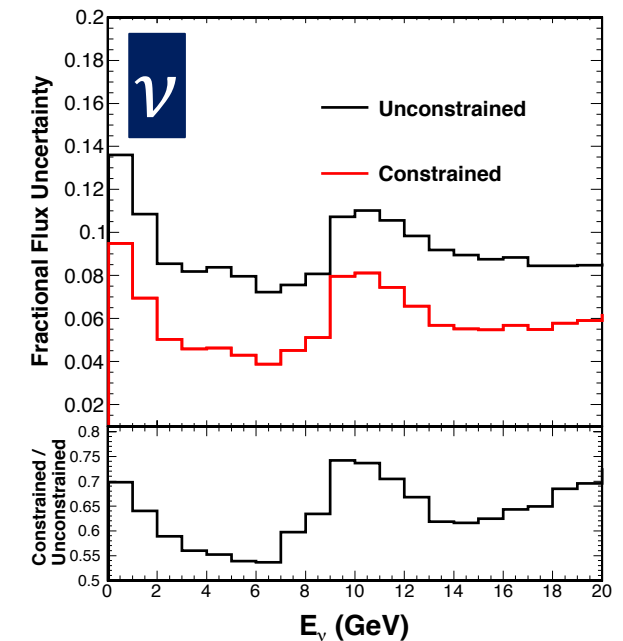
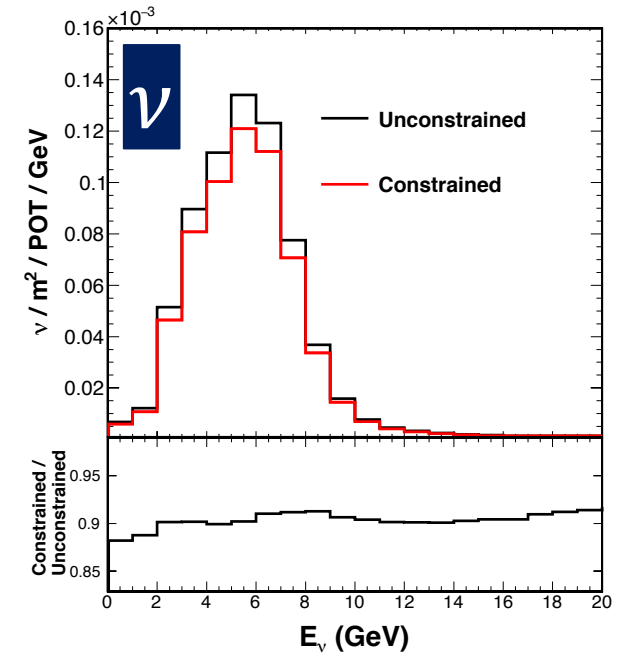
# Neutrino Flux Constraint

- Likelihood of the measurement for each universe

$$P(N_{\nu e \rightarrow \nu e} | M) = \frac{1}{(2\pi)^{K/2}} \frac{1}{|\Sigma_{\mathbf{N}}|^{1/2}} e^{-\frac{1}{2}(\mathbf{N}-\mathbf{M})^T \Sigma_{\mathbf{N}}^{-1} (\mathbf{N}-\mathbf{M})}$$

$N$	vector containing the bin content of the measured energy spectrum of given process
$M$	same as $N$ but for the MC prediction
$\Sigma_N$	covariance matrix of the uncertainties of $N$
$K$	number of the bins of the spectrum

- Predictions from universes with poor data agreement are weighted down → **reduces uncertainty** (spread of the universes)
- **In neutrino mode, the neutrino flux uncertainty is reduced from 7.6% to 3.9% (integrated flux over the energy range)**



Phys. Rev. D 100, 092001 (2019).

# In situ Measurements To Constrain Flux

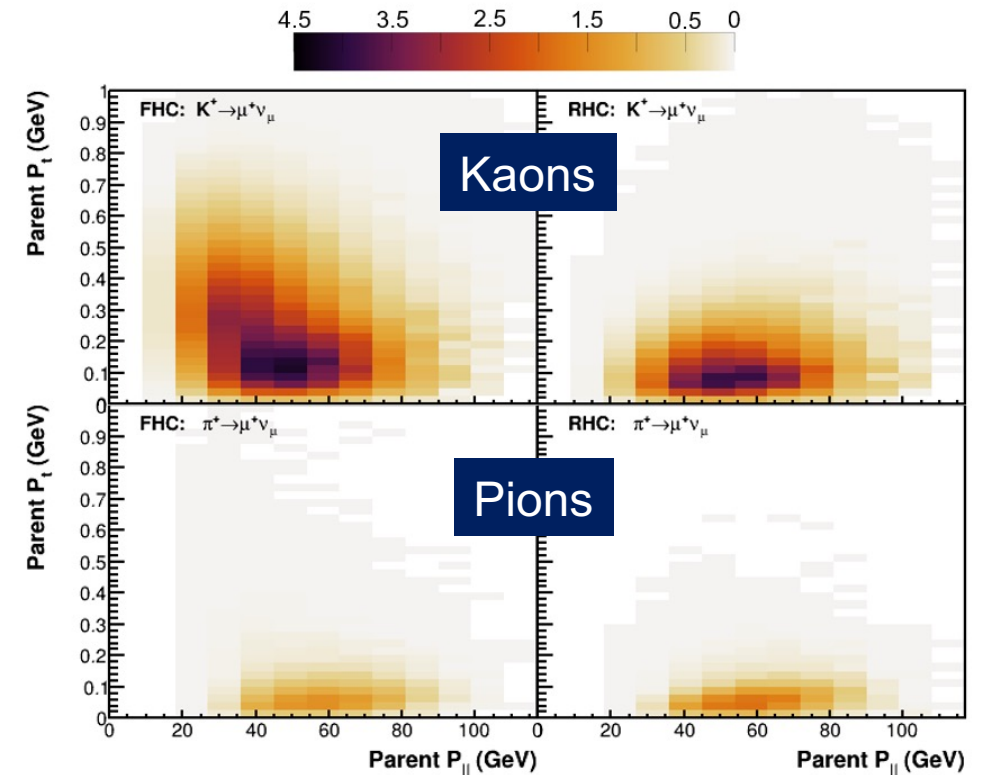
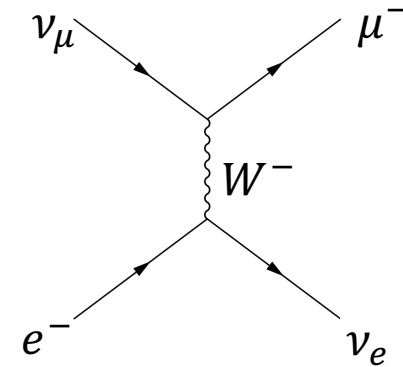


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# Inverse Muon Decay (IMD)

- Cross-section can be predicted with very small uncertainties
- **Threshold of  $\approx 11$  GeV with very forward going muon**
  - Indistinguishable process  $\bar{\nu}_e e^- \rightarrow \mu^- \bar{\nu}_\mu$  unimportant in MINERvA due to threshold
- Neutrinos from underfocused or unfocused  $K^+$  and  $\pi^+$
- Can **constrain the high-energy part of the flux** in the NuMI neutrino beam

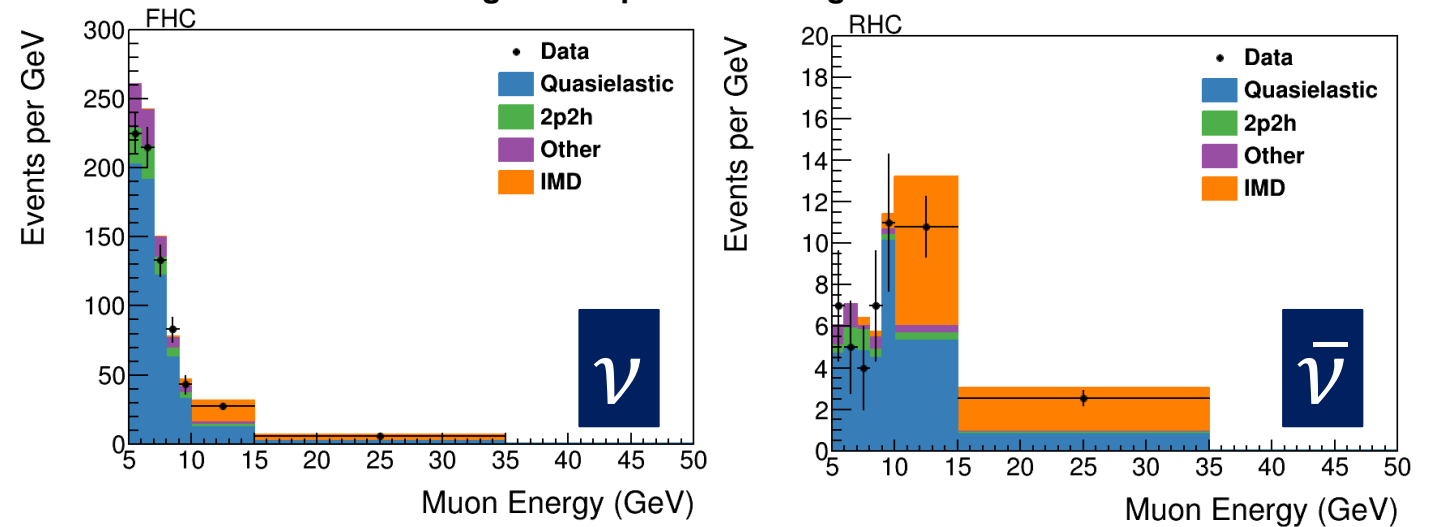


# IMD Sample & Flux Constraint

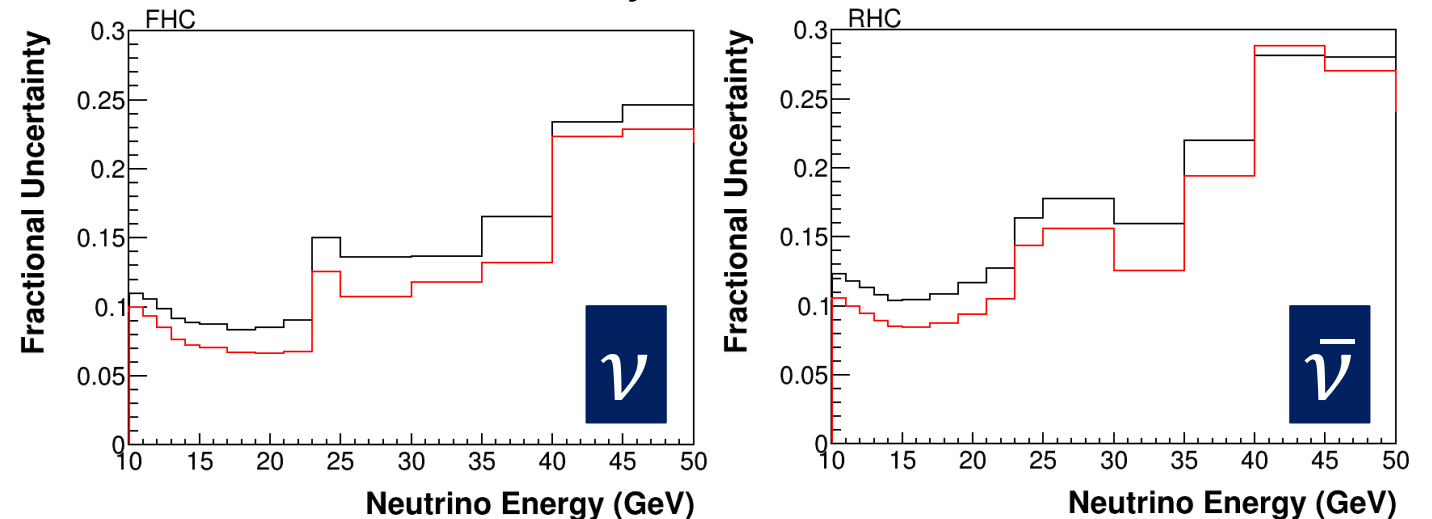
- Small sample  $\sim 0.006\%$  of the inclusive CC sample in tracker
- Threshold, angle + no visible recoil (muon only)
- Main background from CCQE, constraint using  $E_\mu, \theta_\mu$  sideband
- 127 (56) selected events in data for the neutrino (antineutrino) beam
- **Flux constraint extracted, reduced uncertainty in the high-energy tail of the flux**

Neutrino events in neutrino/antineutrino beam

Signal sample after background constraint



Flux uncertainty before and after the constraint



# In situ Measurements To Constrain Flux



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4. **Combined constraint using  $\nu/\bar{\nu}$ -electron and IMD**

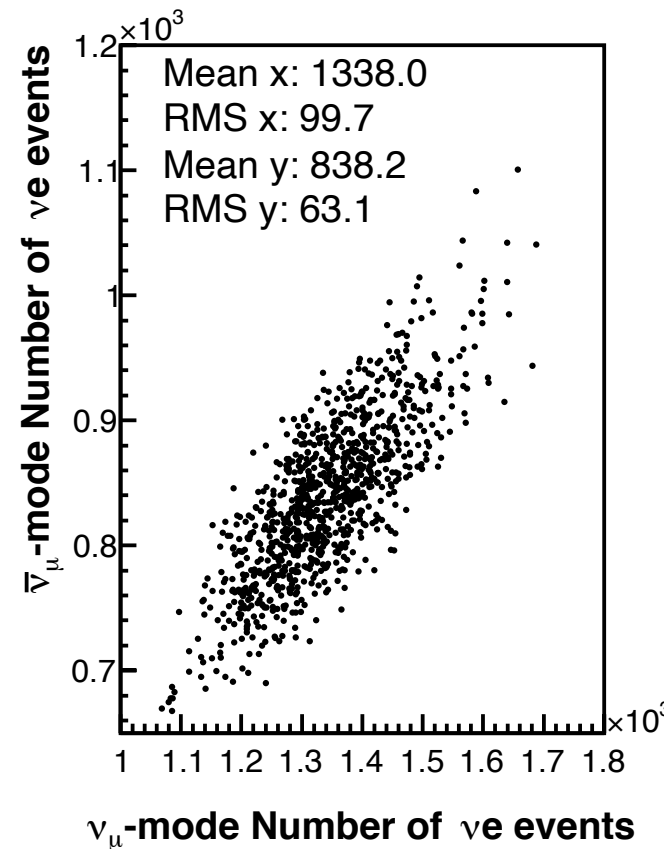
# Combined Flux Constraint



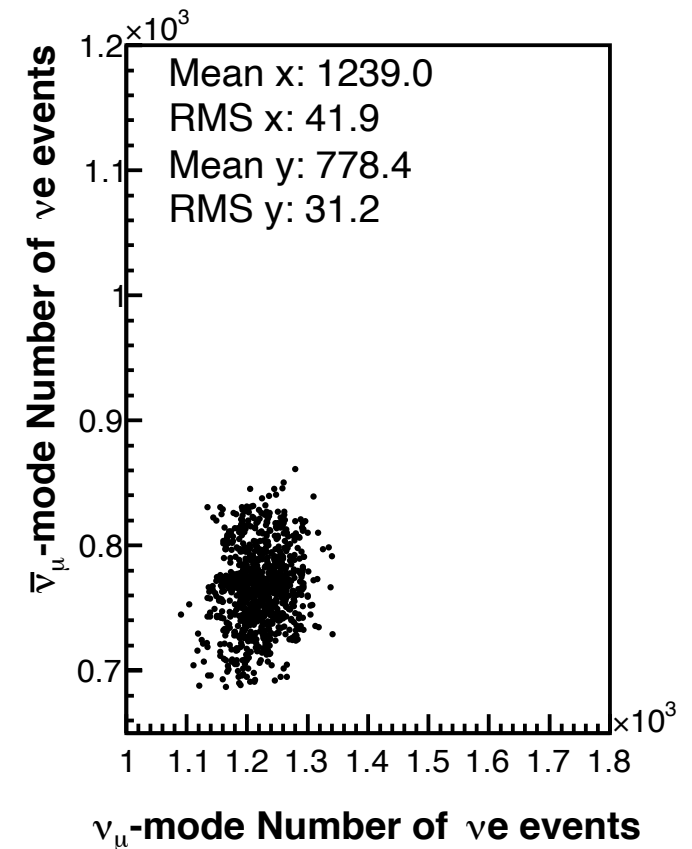
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- Extracted combined flux uncertainty using neutrino(antineutrino)-electron scattering result and IMD
- Uncertainties on  $\nu/\bar{\nu}$ -electron scattering correlated  $\rightarrow$  predictions of # events correlated
  - Hadron production constraints from the same experiments and data

A priori prediction



After constraint



Predicted number of neutrino(antineutrino)-  
electron scattering events by each flux universe.

[Submitted for publication, \[hep-ex\]:2209.05540.](#)



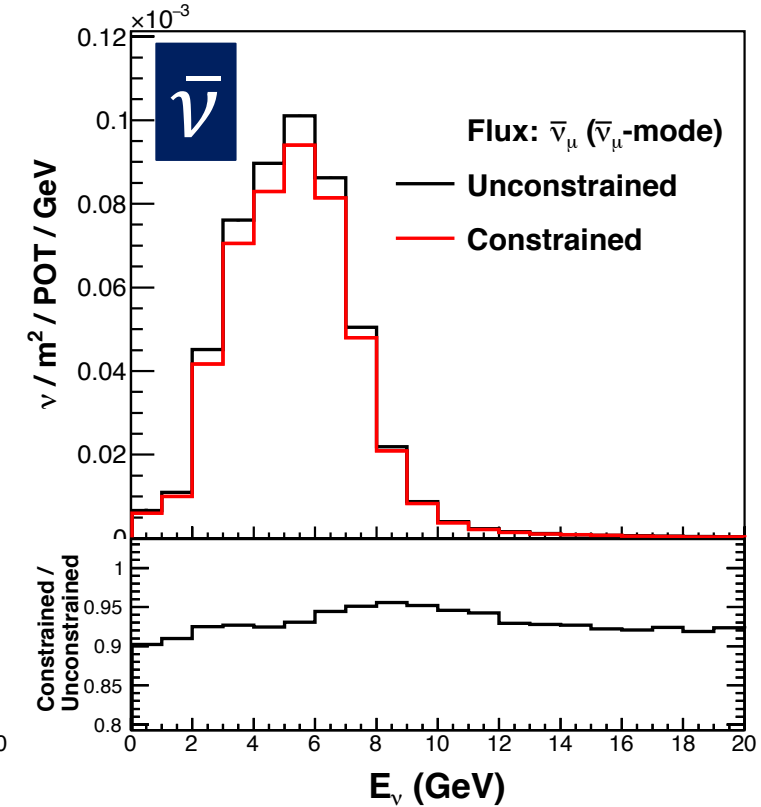
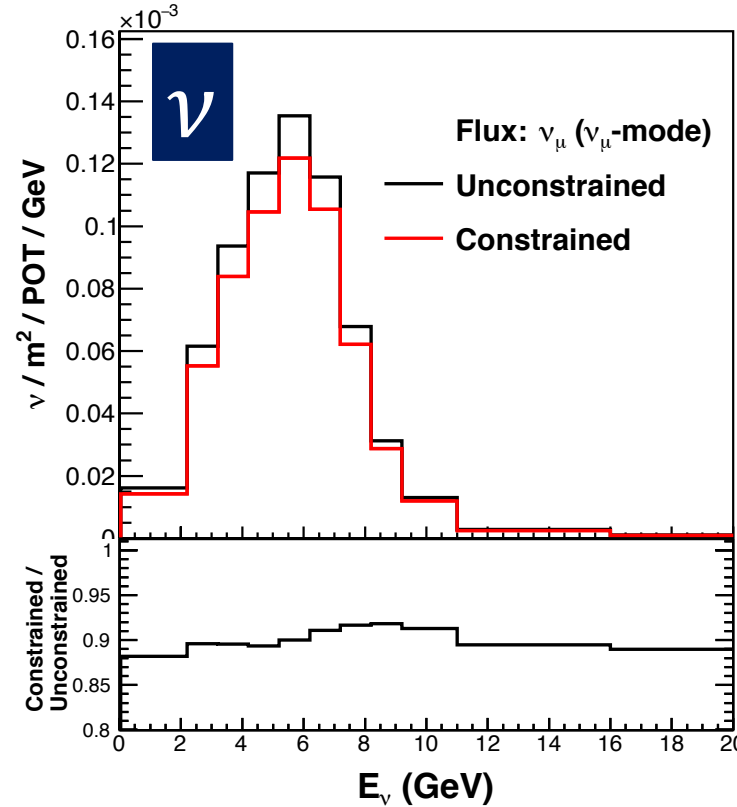
# Predicted Flux



- $\nu(\bar{\nu})$ -electron constraint the strongest in its respective mode
- IMD affects the high-energy tail

	$\bar{\nu}_\mu$ -mode				$\nu_\mu$ -mode			
	$\bar{\nu}_\mu$	$\bar{\nu}_e$	$\nu_\mu$	$\nu_e$	$\nu_\mu$	$\nu_e$	$\bar{\nu}_\mu$	$\bar{\nu}_e$
<i>a priori</i>	7.76	7.81	11.1	11.9	7.62	7.52	12.2	11.7
$\nu_\mu$ -mode $\nu e^-$	6.11	5.81	6.30	8.50	3.90	3.94	8.37	8.68
$\bar{\nu}_\mu$ -mode $\nu e^-$	4.92	4.98	8.07	9.19	5.88	5.68	8.36	8.64
combined $\nu e^-$	4.68	4.62	5.56	7.80	3.56	3.58	7.15	7.84
combined $\nu e^- + \text{IMD}$	4.66	4.56	5.20	6.08	3.27	3.22	6.98	7.54

(Energy range integrated flux uncertainty)



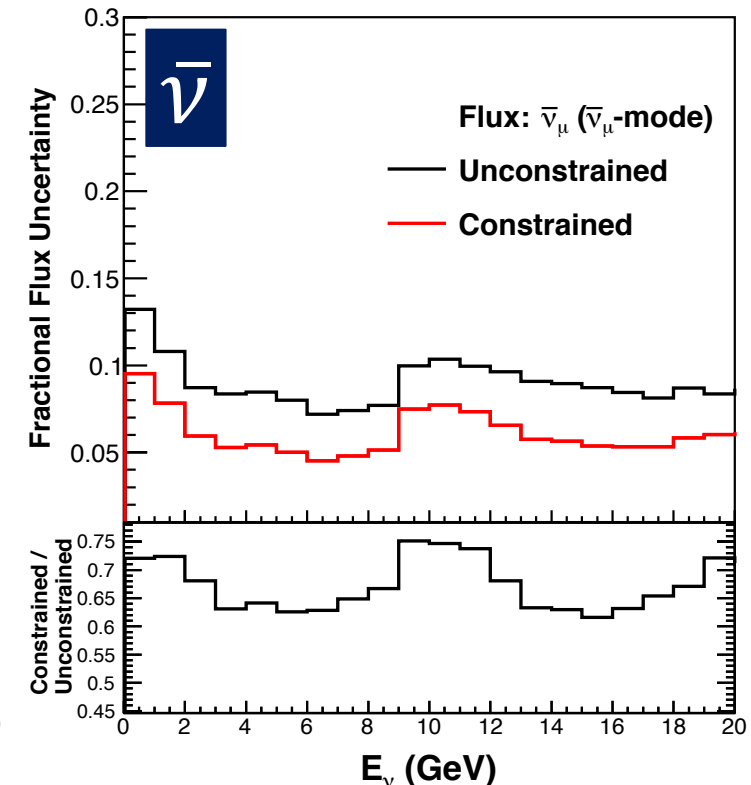
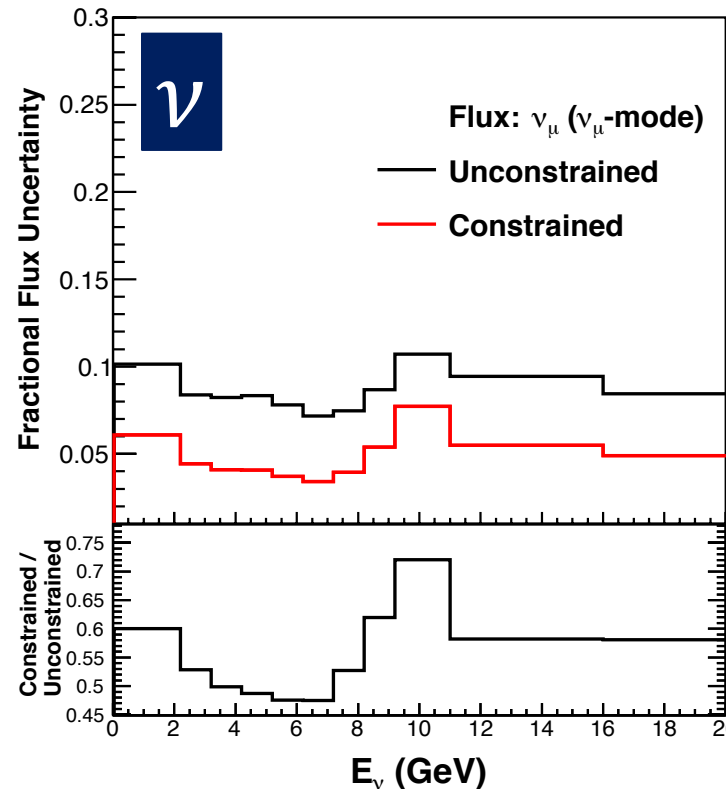
# Fractional Uncertainties



- Flux uncertainty in  $\nu$  mode reduced from 7.6% to 3.3%
- In  $\bar{\nu}$  mode from 7.8% to 4.7%
- Used in MINERvA analyses!

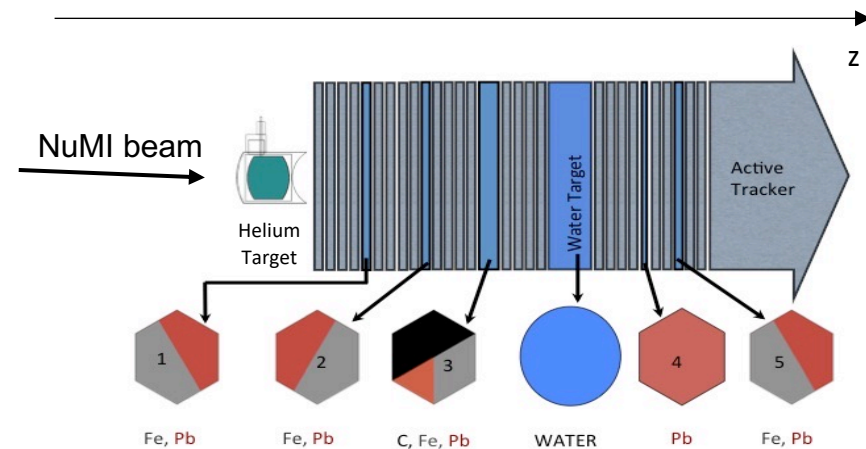
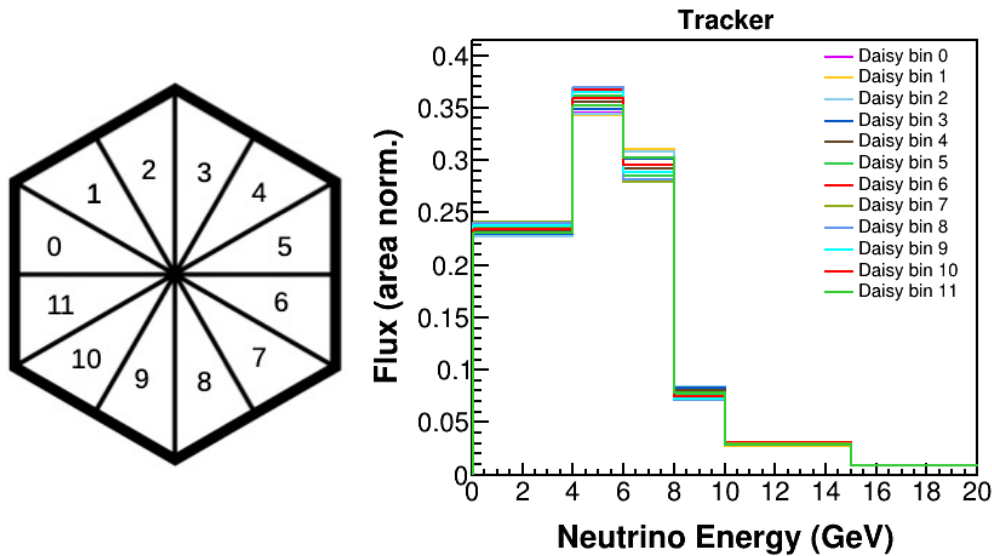
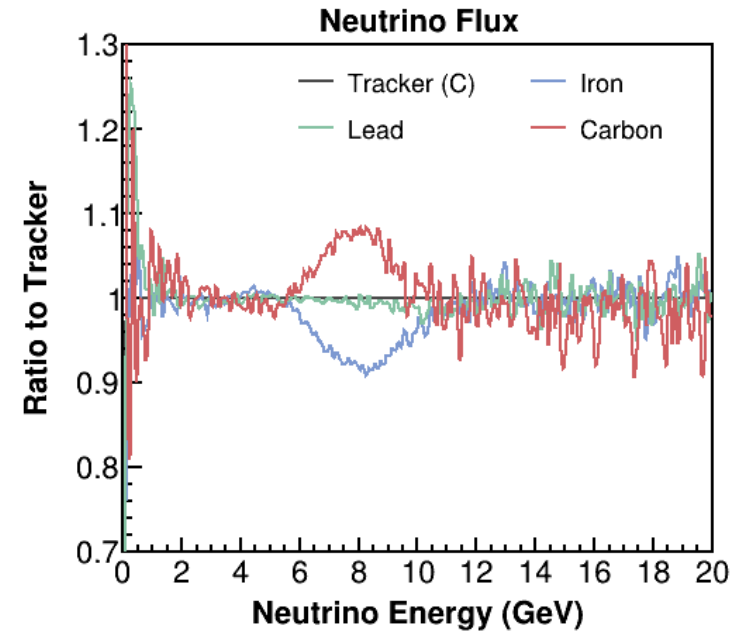
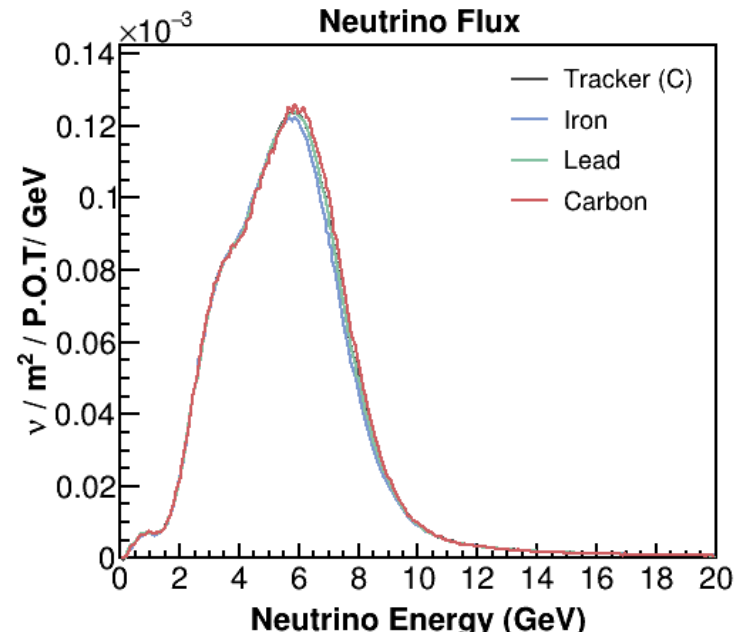
	$\bar{\nu}_\mu$ -mode				$\nu_\mu$ -mode			
	$\bar{\nu}_\mu$	$\bar{\nu}_e$	$\nu_\mu$	$\nu_e$	$\nu_\mu$	$\nu_e$	$\bar{\nu}_\mu$	$\bar{\nu}_e$
<i>a priori</i>	7.76	7.81	11.1	11.9	7.62	7.52	12.2	11.7
$\nu_\mu$ -mode $\nu e^-$	6.11	5.81	6.30	8.50	3.90	3.94	8.37	8.68
$\bar{\nu}_\mu$ -mode $\nu e^-$	4.92	4.98	8.07	9.19	5.88	5.68	8.36	8.64
combined $\nu e^-$	4.68	4.62	5.56	7.80	3.56	3.58	7.15	7.84
combined $\nu e^-$ + IMD	4.66	4.56	5.20	6.08	3.27	3.22	6.98	7.54

(Energy range integrated flux uncertainty)



# Flux for Cross-Section Ratios

- NuMI beam pointed downwards → transverse center of the beam changes as a function of the longitudinal position
- Difference in the flux shape + normalization in the nuclear targets compared to the tracker (problem for cross-section ratios)
- **“Daisy technique”** – take linear combination of tracker fluxes in 12 bins to match the target



# Conclusions



- MINERvA is a neutrino-nucleus experiment with a dedicated flux campaign – **in-situ measurements to constrain flux**
- Measured neutrino-nucleus scattering with low hadronic recoil to constrain flux shape
  - Discrepancy in data/MC resolved by shifting muon energy scale by  $1.8\sigma$
- Measured (anti)neutrino-electron elastic scattering to constrain flux normalization, and inverse muon decay to constrain the high-energy tail
- Combined flux constraint of these 3 measurements **reduces the flux uncertainty from 7.6% to 3.3% in  $\nu$  mode and 7.8% to 4.7% in  $\bar{\nu}$  mode**
- Can use similar techniques to constrain flux at other accelerator-based neutrino experiments (e.g., DUNE)



**Funding Acknowledgement:** Funded by an Imperial College London President's PhD Scholarship.

# Back-up



= Package to Predict the Flux

- Experiment independent NuMI reweighting package, external of MINERvA framework
- Applies all relevant data, removes the model spread and handles correlated uncertainties
- Accounts for the attenuation of particles passing through NuMI materials
- Multiverse method for handling the uncertainty propagation
- Used by other NuMI experiments, e.g., MINOS+, NOvA, MicroBooNE

# In situ Measurements To Constrain Flux



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- 1. Neutrino-nucleus scattering with low hadronic recoil**
2. (Anti)Neutrino-electron elastic scattering
3. Inverse muon decay (IMD)
4. Combined constraint using  $\nu/\bar{\nu}$ -electron and IMD

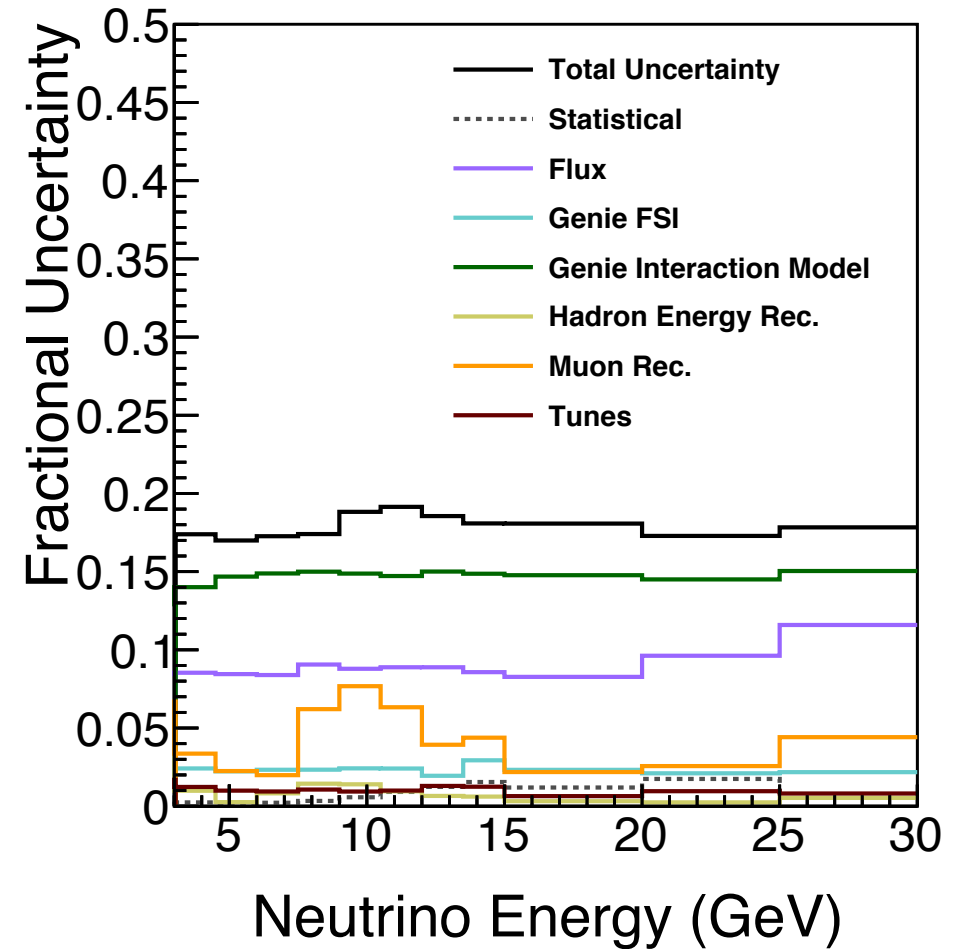
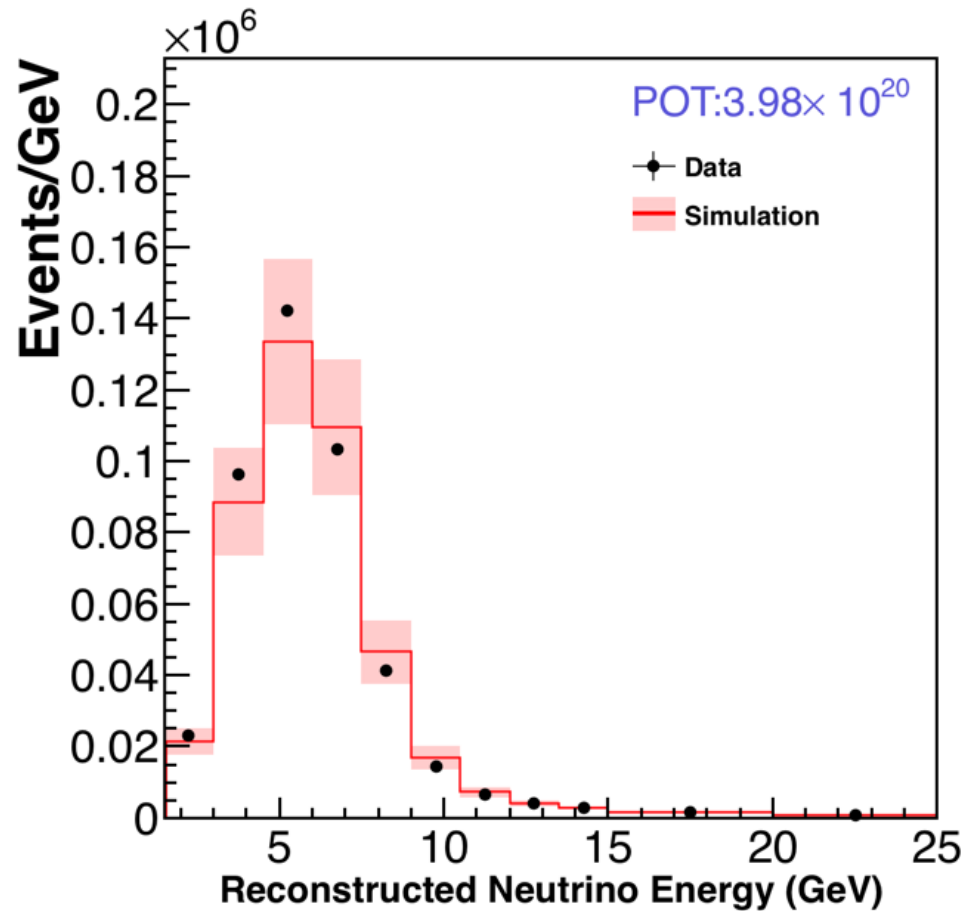


# 1 $\sigma$ Tolerances On Beam Parameters

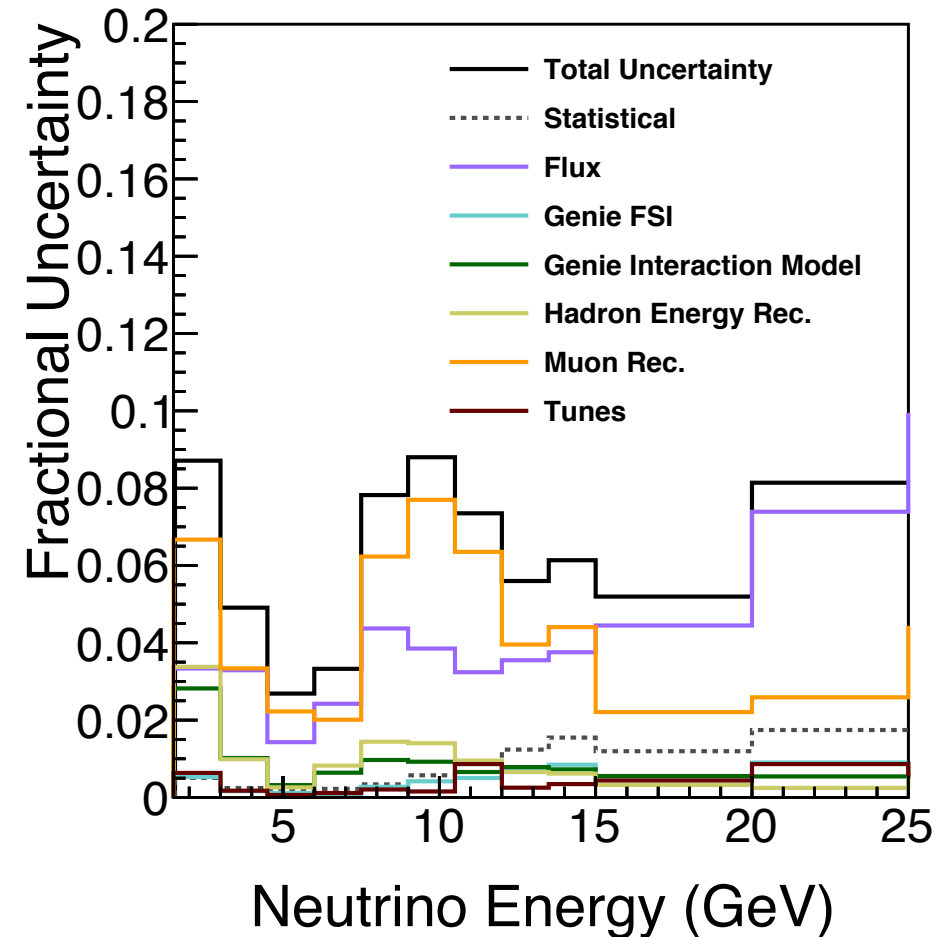
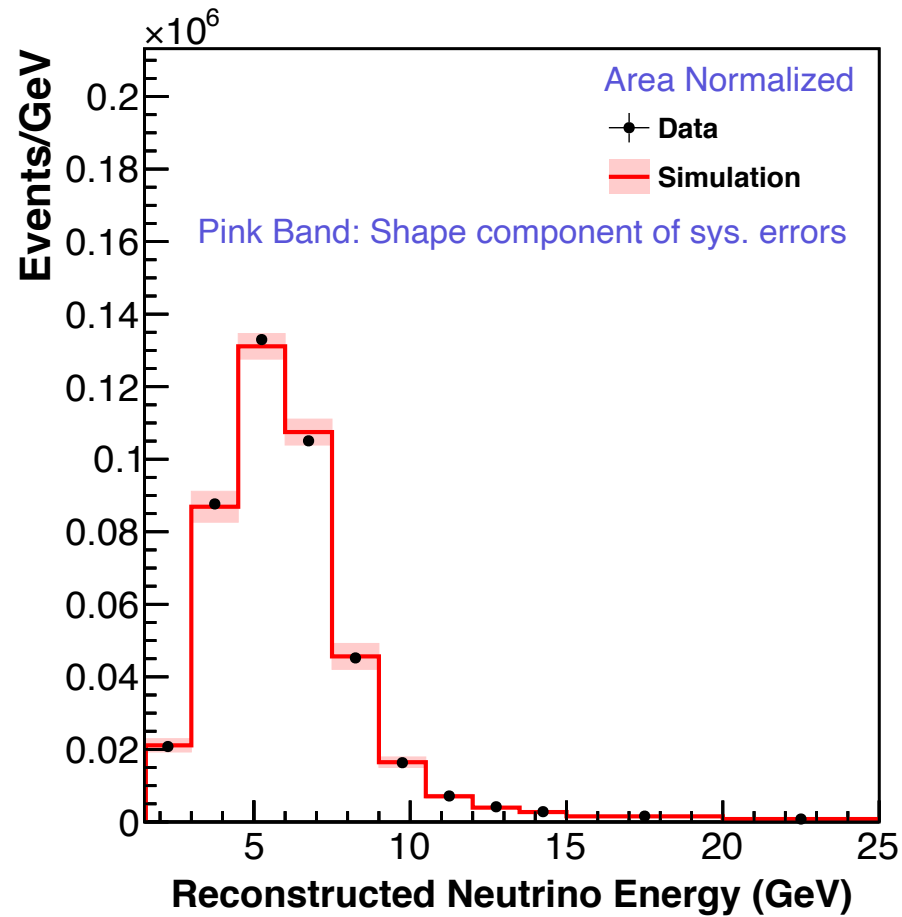


Parameter	Nominal Value	Final 1 $\sigma$ shifts used in MINERvA analyses	Preliminary 1 $\sigma$ shifts used in this work
Beam Position (X)	0 mm	0.4 mm	1 mm
Beam Position (Y)	0 mm	0.4 mm	1 mm
Beam Spot Size	1.5 mm	0.3 mm	0.3 mm
Horn Water Layer	1.0 mm	0.5 mm	0.5 mm
Horn Current	200 kA	1 kA	1 kA
Horn 1 Position (X)	0 mm	1 mm	1 mm
Horn 1 Position (Y)	0 mm	1 mm	1 mm
Horn 1 Position (Z)	30 mm	2 mm	-
Horn 2 Position (X)	0 mm	1 mm	1 mm
Horn 2 Position (Y)	0 mm	1 mm	1 mm
Target Position (X)	0 mm	1 mm	1 mm
Target Position (Y)	0 mm	1 mm	1 mm
Target Position (Z)	-1433 mm	1 mm	3 mm
POT Counting	0	2% of Total POT	-
Baffle Scraping	0	0.25% of POT	-

# Systematic Uncertainties For The Simulated Neutrino Energy Distribution



# Systematic Uncertainties For The Simulated Neutrino Energy Distribution



# Fitting Procedure



- Chi2 minimization: 
$$\chi_{prior}^2 = \sum_{ij} \frac{(Data'_{ij} - MC'_{ij})^2}{\sigma_{ij}^2} + \sum_k (\alpha_k)^2$$

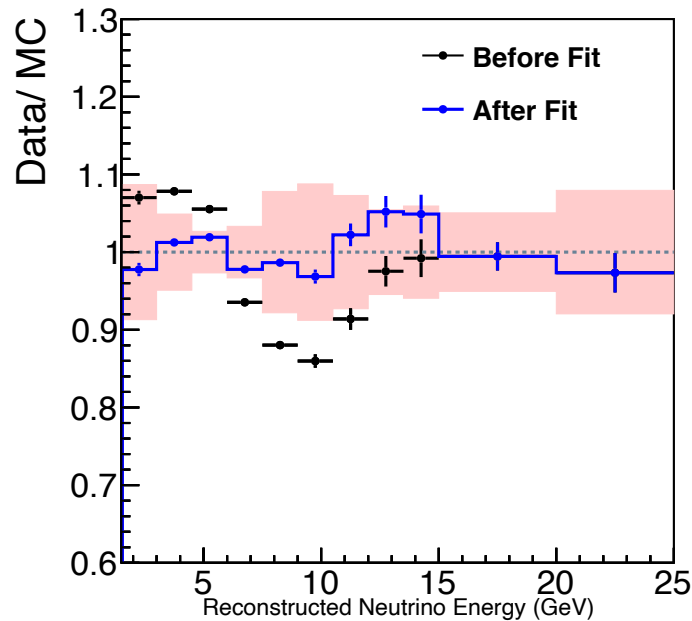
penalty term – number of standard deviations that the parameter  $k$  has been shifted from the nominal value

- Uncertainty: 
$$\sigma_{ij} = \sqrt{\sigma_{Data',ij}^2 + \sigma_{MC',ij}^2}$$

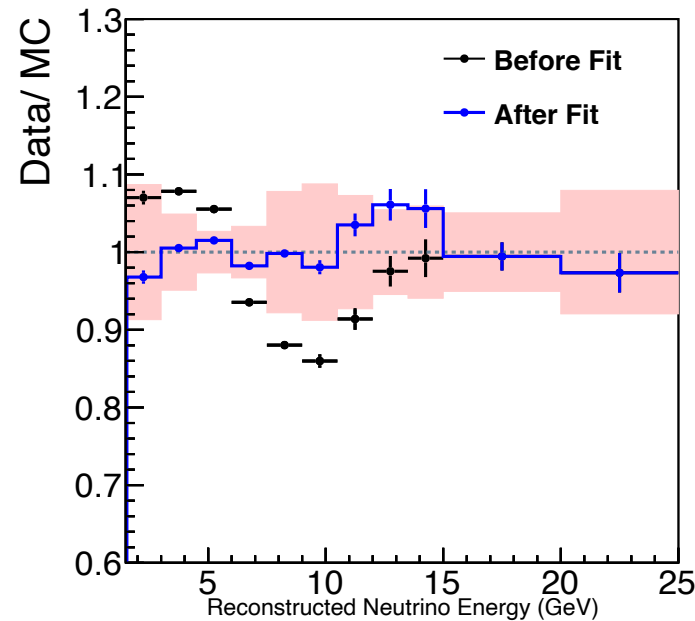
# Fits w/ & w/o Priors For All Parameters vs Muon Energy Scale Fit Only



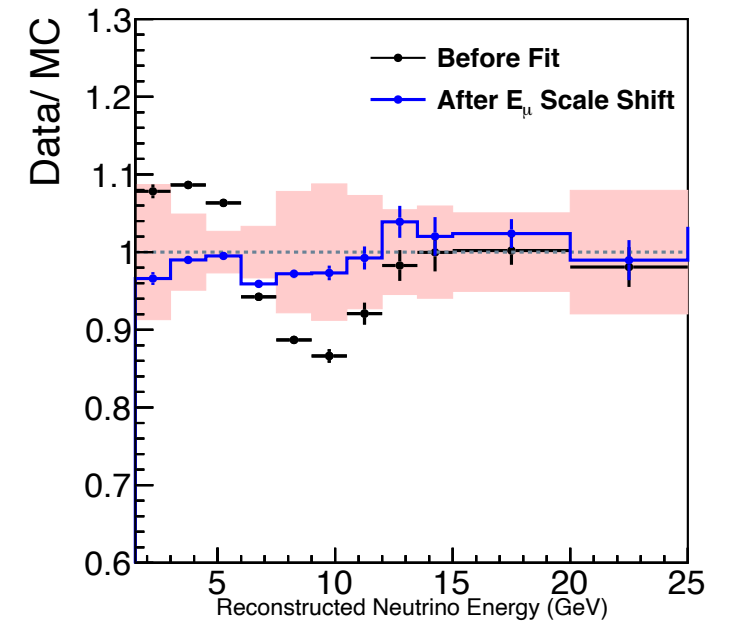
Fit without prior



Fit with prior



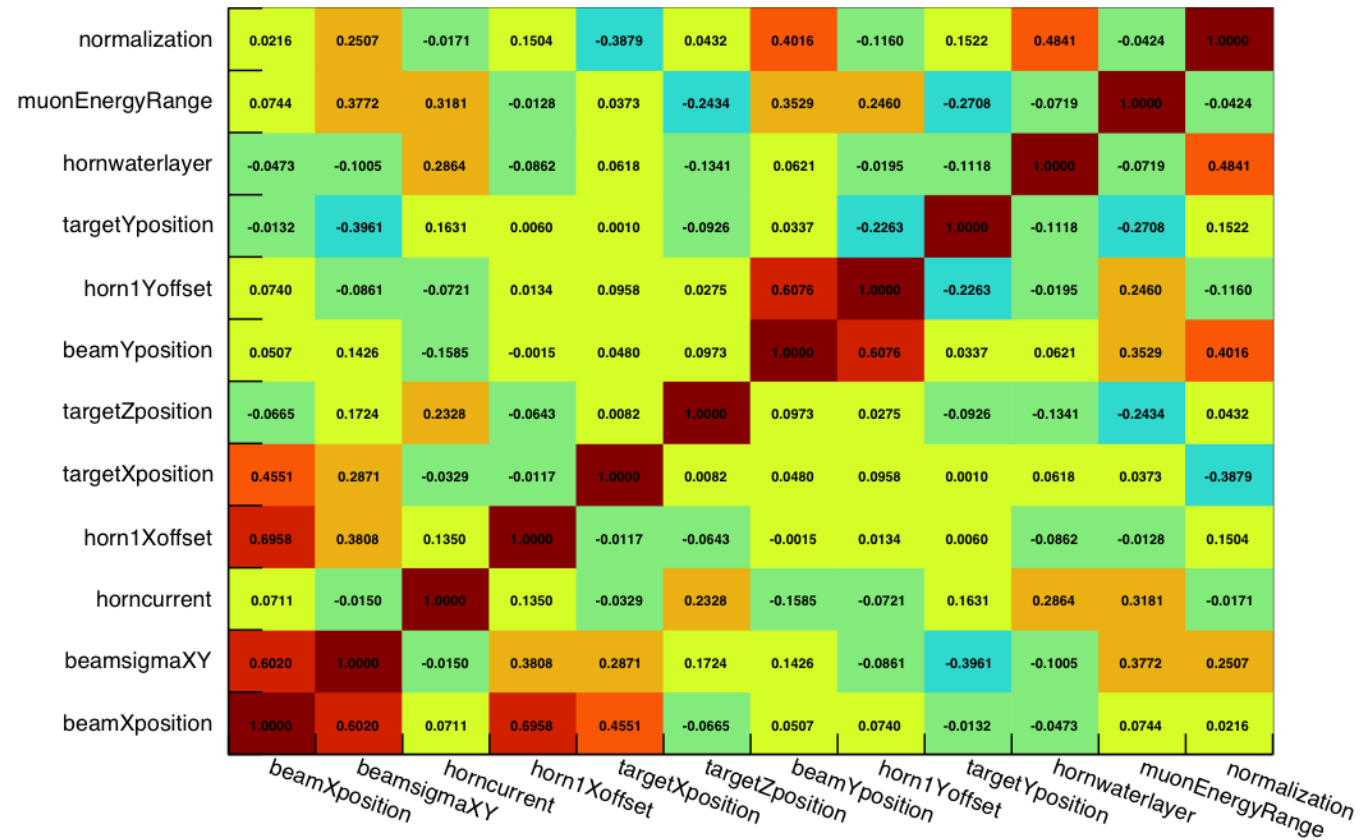
Muon energy scale shift only



# Best-Fit Parameters Correlation Matrix



With priors



# In situ Measurements To Constrain Flux



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# Selection Cuts



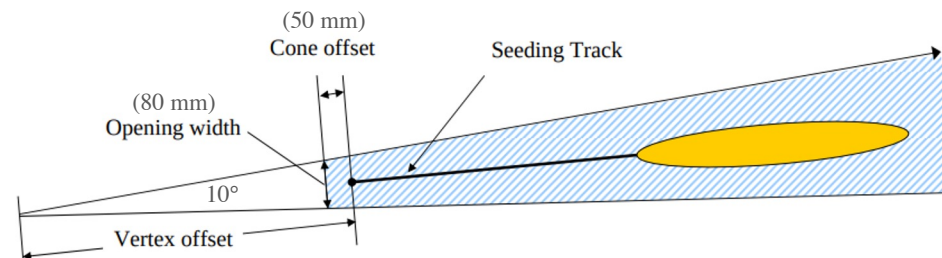
- Clean detector
  - Upstream energy  $< 300$  MeV
  - Neighbouring energy  $< 120$  MeV
- Other shower quality cuts
  - Energy balance between views
  - Not too wide transverse spread near the vertex
  - Straight tracks
- $\nu_\mu$  rejection
  - $E_e > 800$  MeV
  - Reject tracks going out
- $\nu_\mu$  rejection
  - Mean  $dE/dx$  in the first 4 planes  $< 4.5$  MeV/1.7cm
  - Check for single photon consistency
- $\nu_e$  CC rejection
  - $E\theta^2 < 0.0032$  GeV Rad<sup>2</sup>
  - QE  $Q^2 < 0.02$  GeV



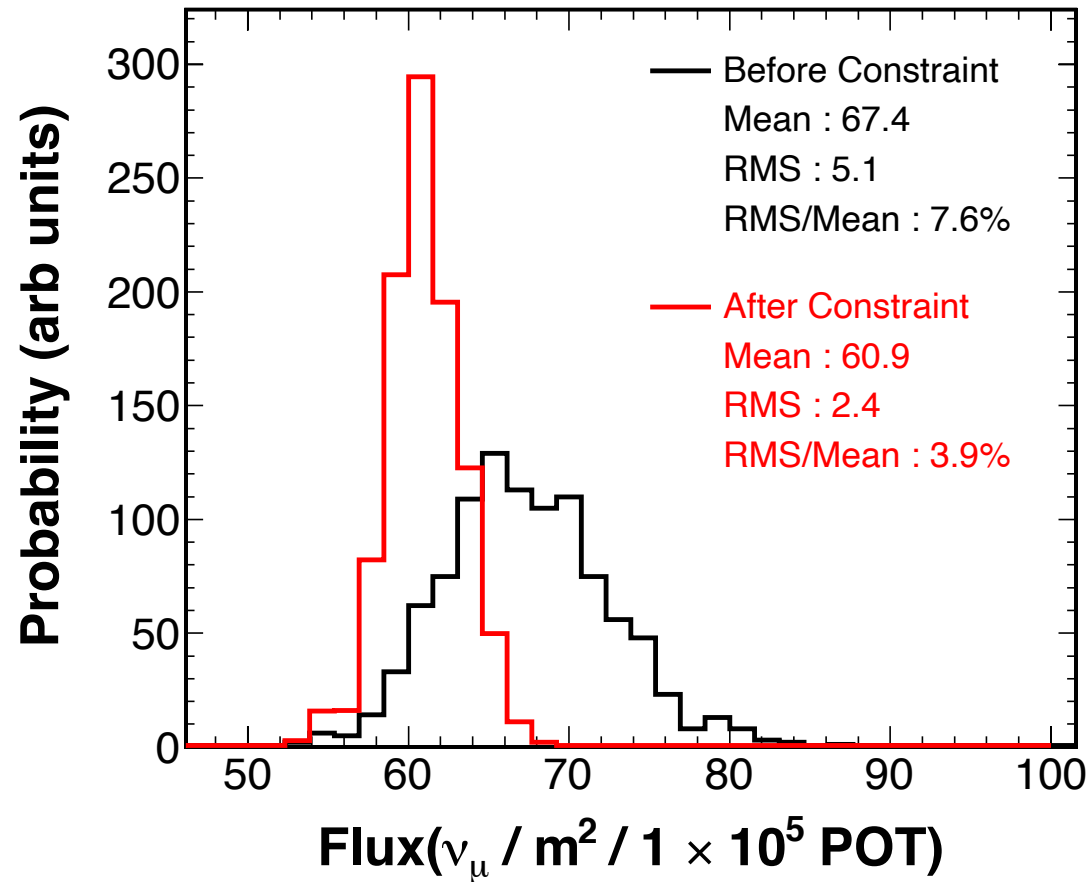
# Cone Algorithm



- Seeded by either tracks or group of clusters
- Usually, clusters formed to tracks and fit using Kalman filter – start vertex and track direction
- Formed cone begins upstream of the vertex and extends downstream until no minimum-ionizing-level energy depositions are found within the cone volume
- Parameters chosen to maximize efficiency and containment for the signal in the simulation



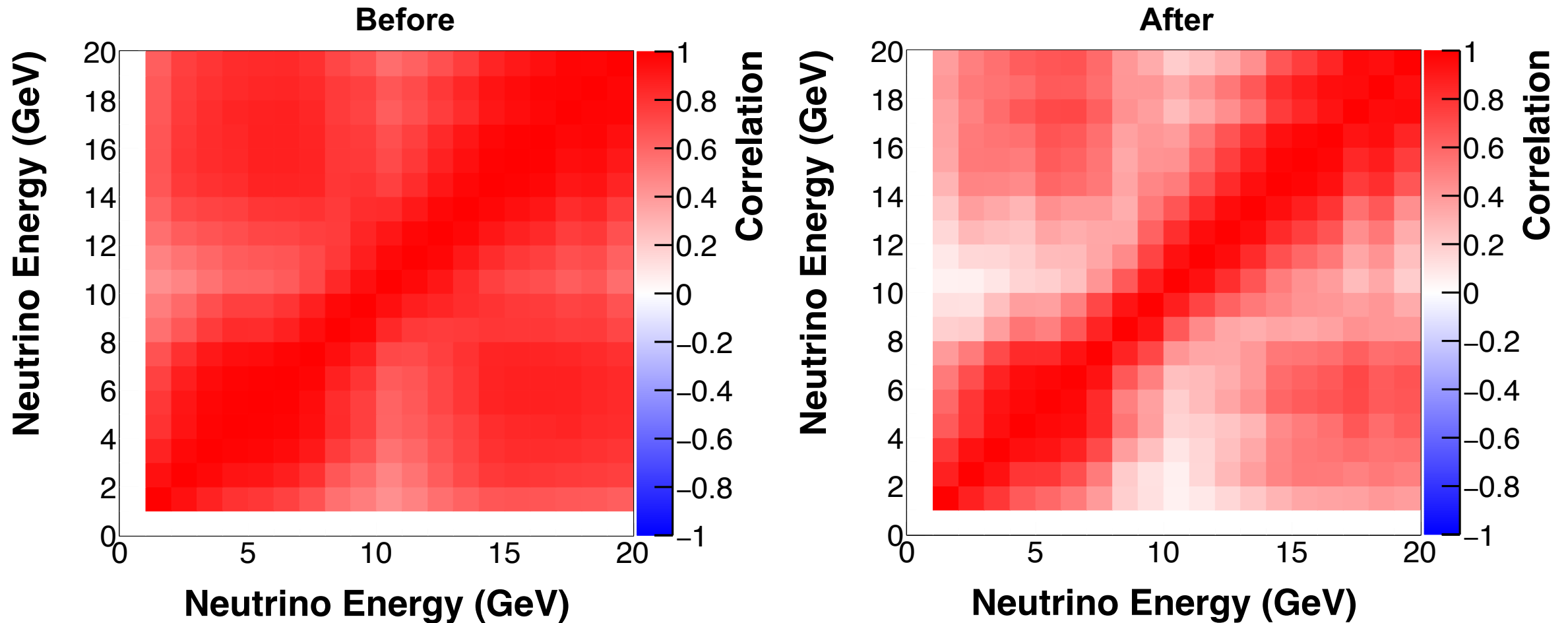
# Neutrino-Electron Scattering: Neutrino Flux Probability Distribution



# Neutrino-Electron Scattering: Correlations Of Unconstrained And Constrained Flux Uncertainties



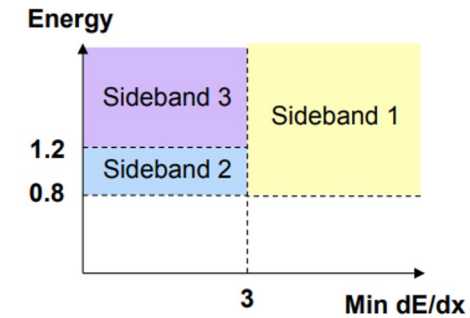
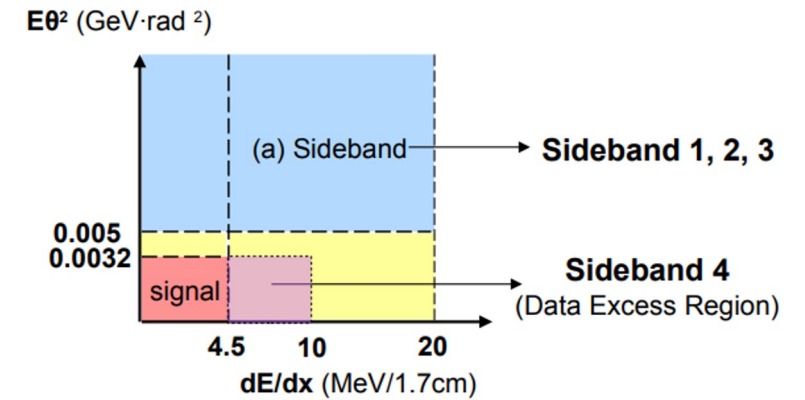
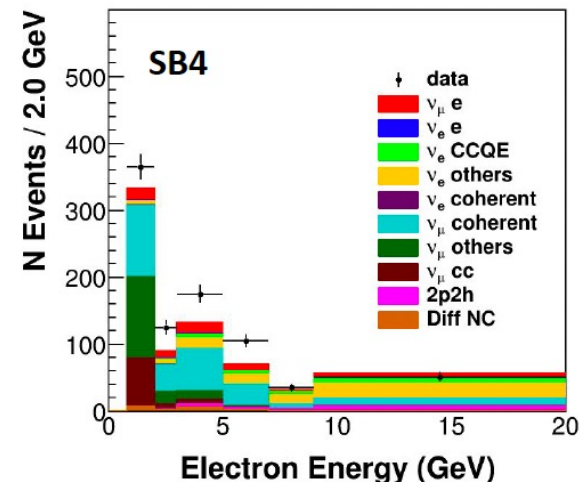
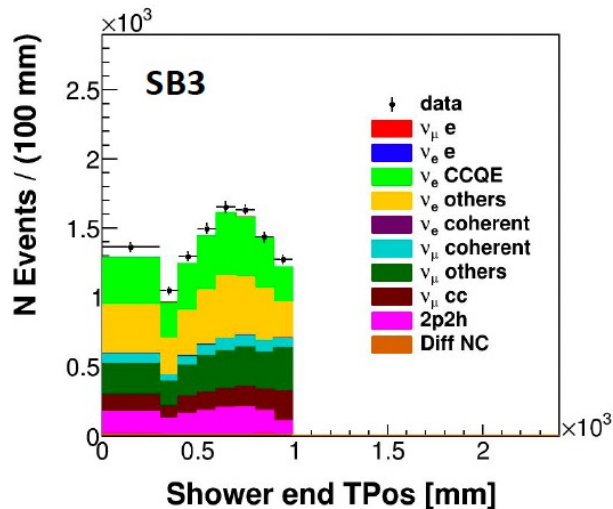
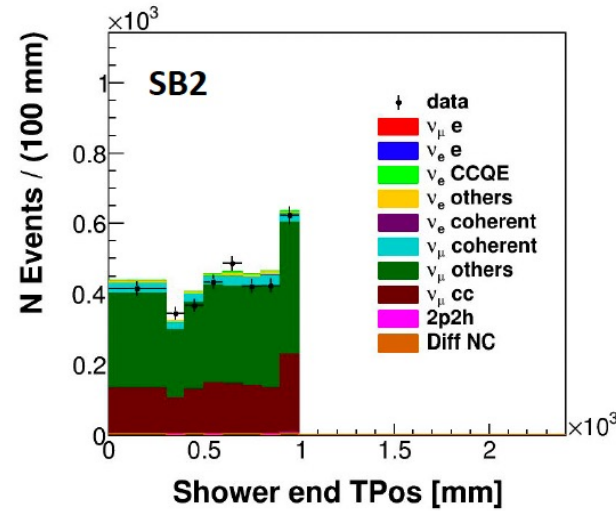
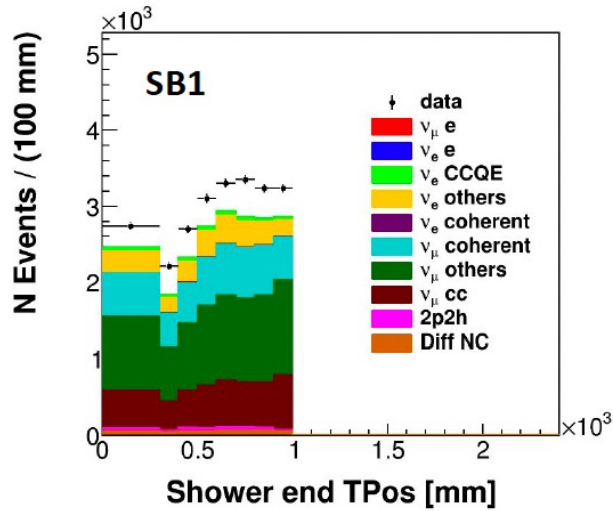
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# Antineutrino-Electron Scattering: Sideband Fit



Before

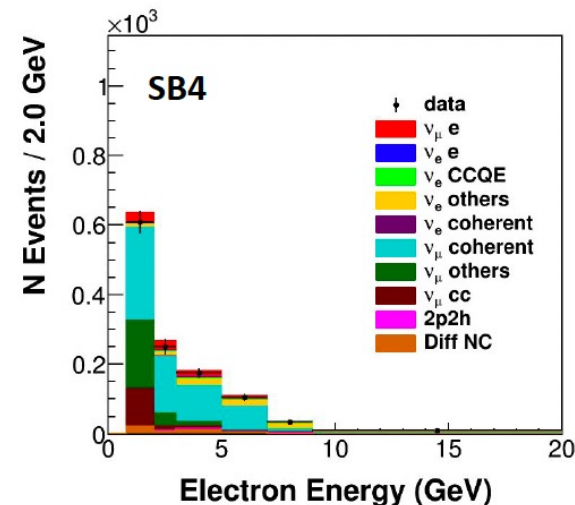
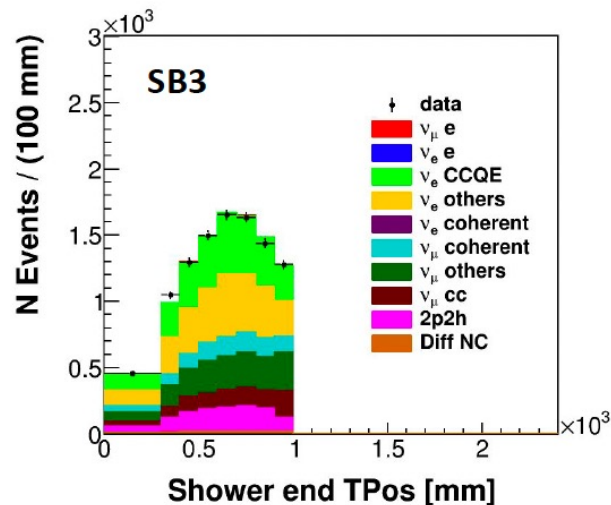
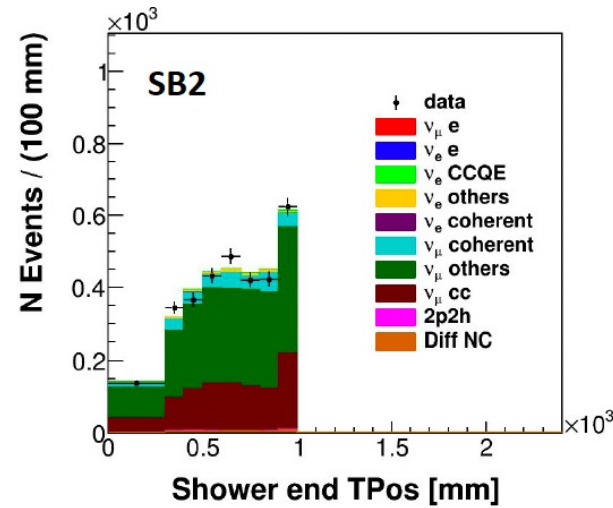
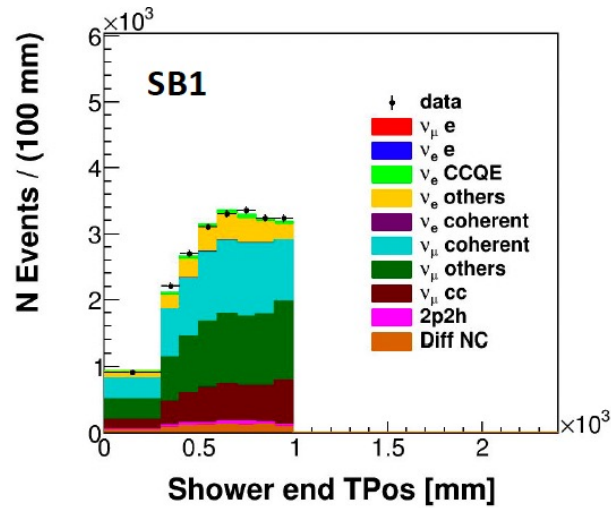


Sideband 1: shower + vertex activity; Sideband 2:  $\nu_\mu$  enriched  
Sideband 3:  $\nu_e$  enriched; Sideband 4:  $\pi^0$  enriched

# Antineutrino-Electron Scattering: Sideband Fit



After



Process	$\bar{\nu}_\mu$ -mode	$\nu_\mu$ -mode
$\nu_e$	$1.02 \pm 0.02$	$0.87 \pm 0.03$
$\nu_\mu$ CC	$0.93 \pm 0.03$	$1.08 \pm 0.04$
$\nu_\mu$ NC	$0.93 \pm 0.03$	$0.86 \pm 0.04$
NC COH $0.8 < E_e < 2.0$ GeV	$1.6 \pm 0.2$	$0.9 \pm 0.2$
NC COH $2.0 < E_e < 3.0$ GeV	$2.1 \pm 0.3$	$1.0 \pm 0.3$
NC COH $3.0 < E_e < 5.0$ GeV	$1.8 \pm 0.2$	$1.3 \pm 0.2$
NC COH $5.0 < E_e < 7.0$ GeV	$2.1 \pm 0.4$	$1.5 \pm 0.3$
NC COH $7.0 < E_e < 9.0$ GeV	$1.2 \pm 0.7$	$1.7 \pm 0.8$
NC COH $9.0 < E_e$	$0.8 \pm 0.6$	$3.0 \pm 0.9$

# In situ Measurements To Constrain Flux



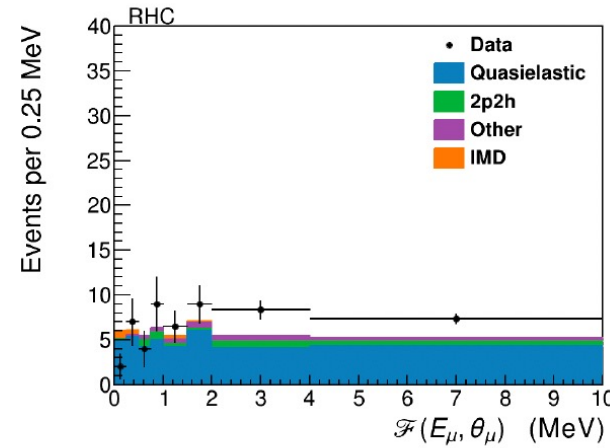
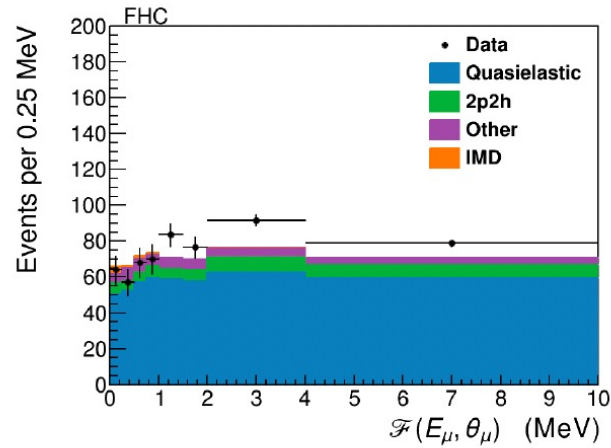
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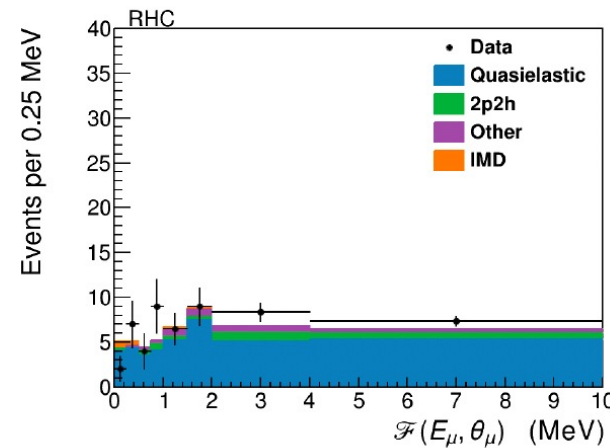
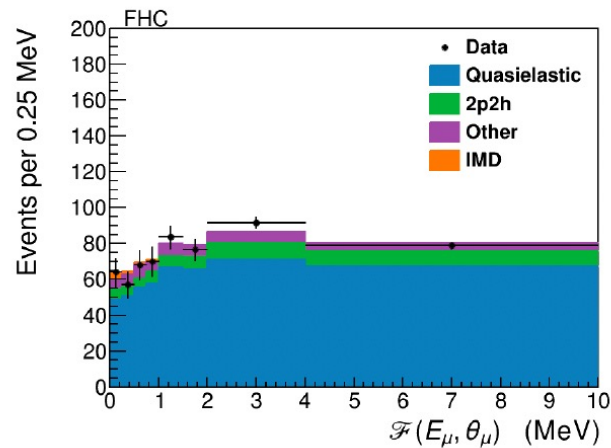
# Sideband Fit



Before



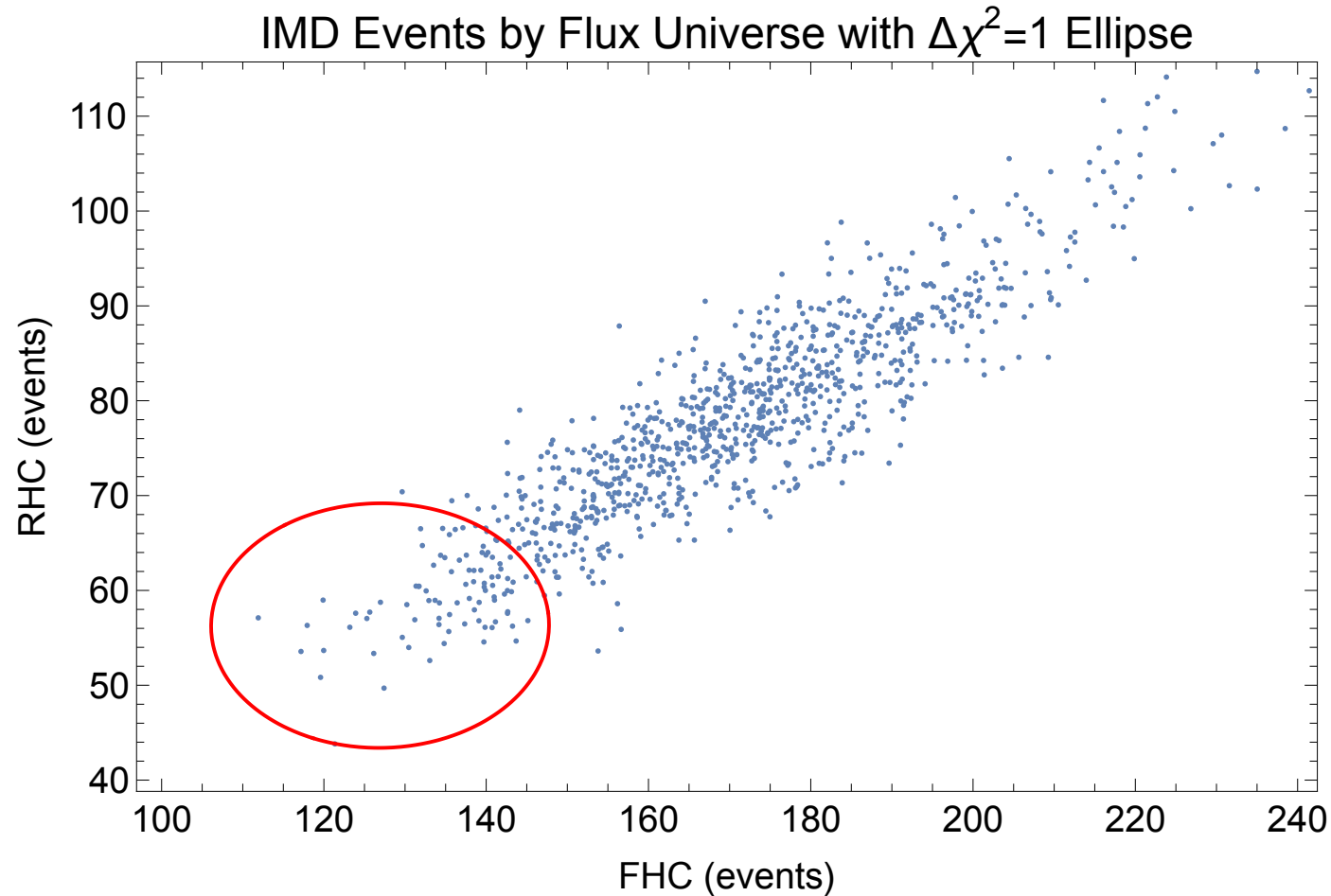
After



Note:

$$\mathcal{F}(E_\mu, \theta_\mu) \equiv \frac{E_\mu \frac{\theta_\mu^2}{1 \text{radian}^2}}{1 - \frac{E_\mu}{E_\nu^{\text{max}}}}$$

# Neutrino/antineutrino flux IMD events correlations





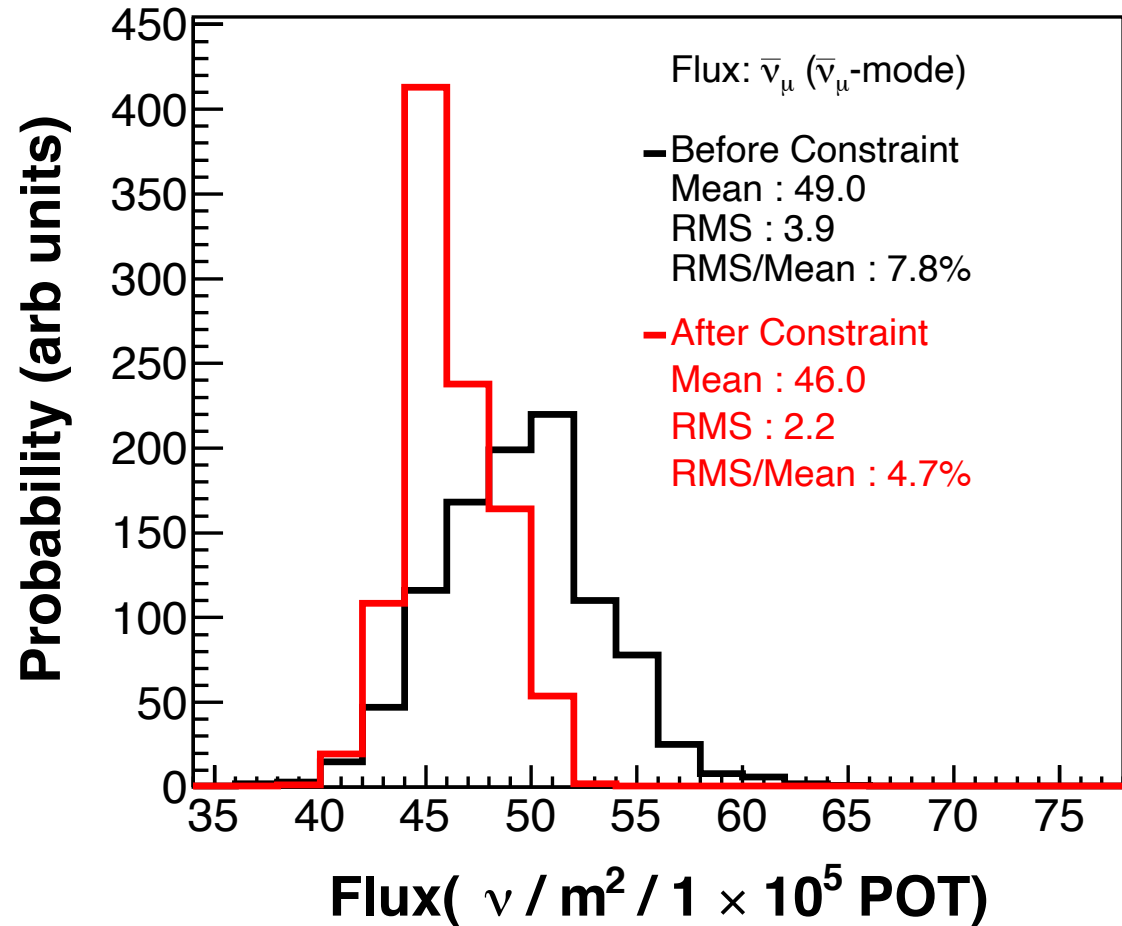
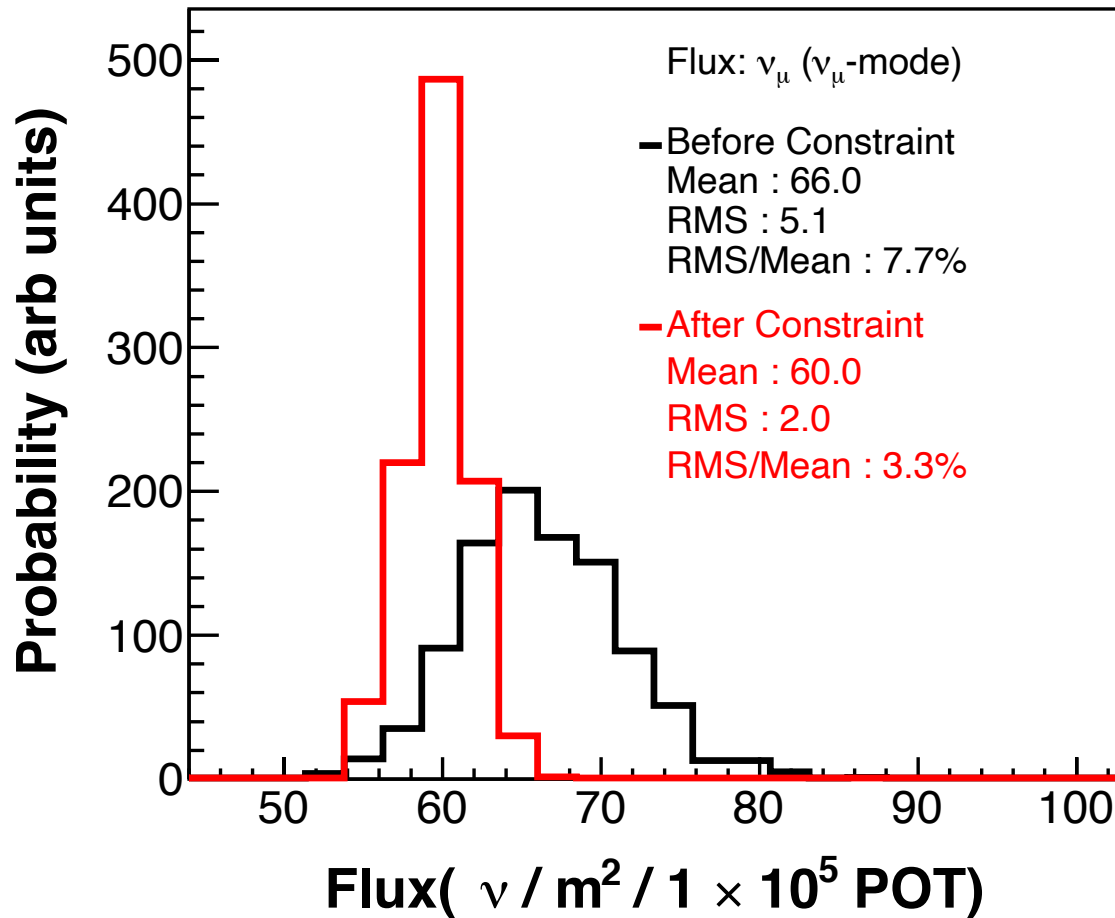
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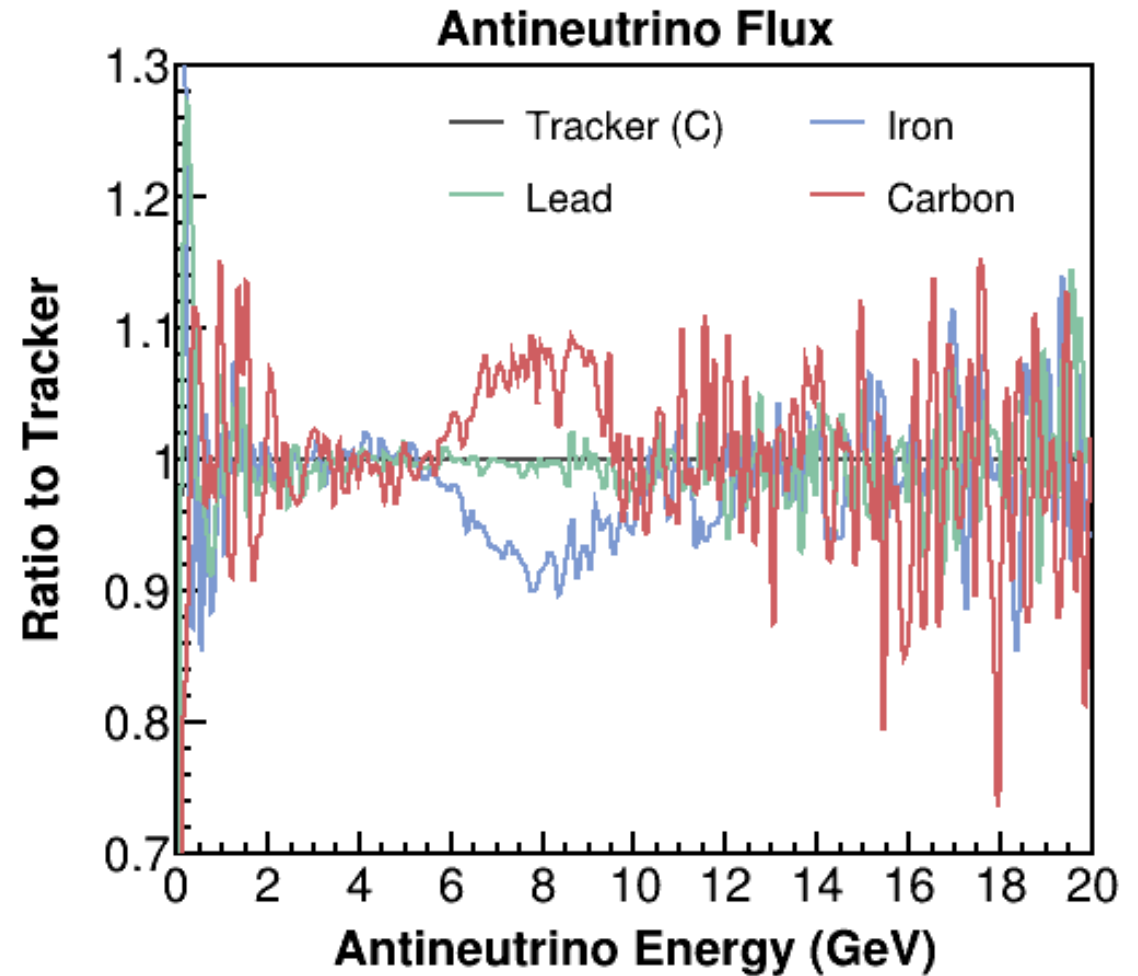
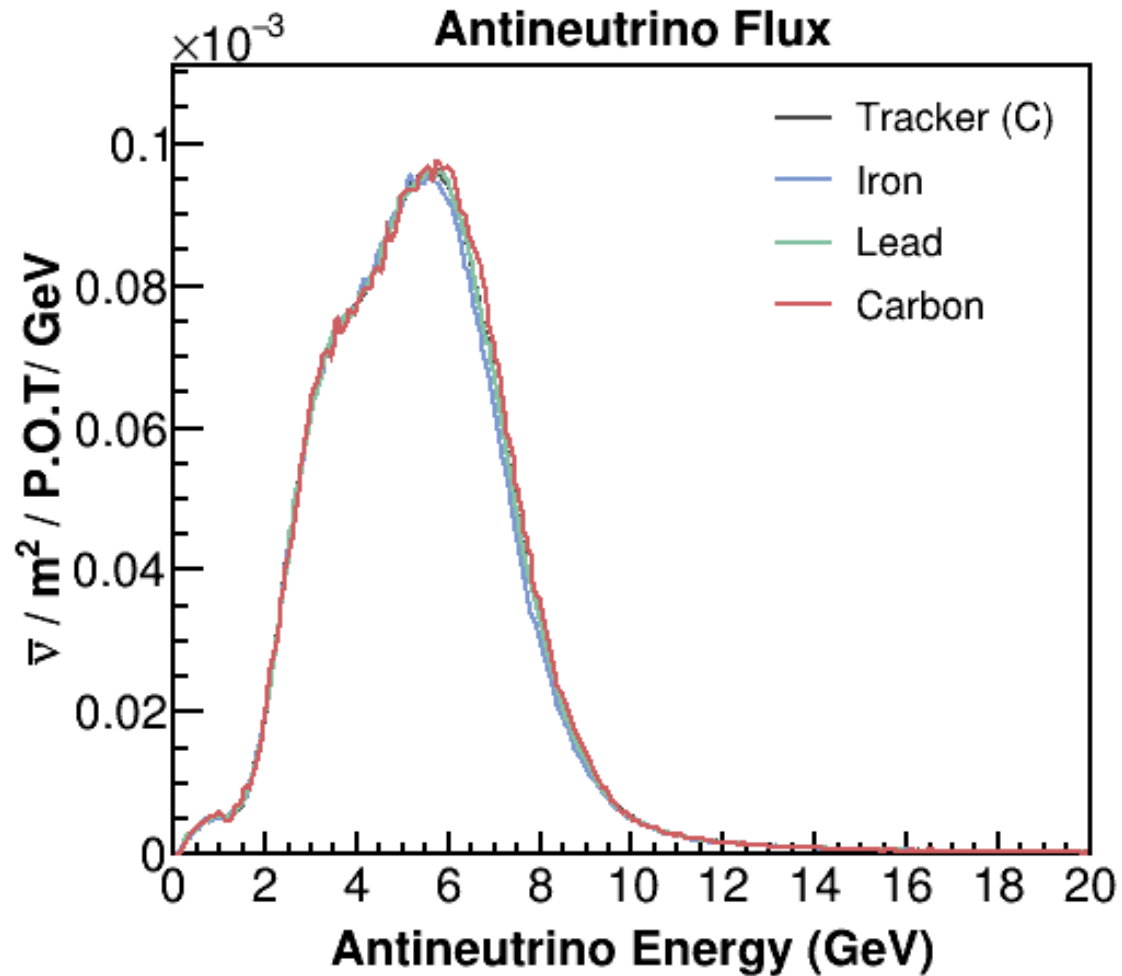
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# Combined Flux Constraint: Flux Probability Distributions



# Antineutrino Flux in Targets



# Simulation and Uncertainties



## 1. Calculate and correct the a-priori flux

G4NuMI beam simulation  
(from 120 GeV protons to focused  
mesons that decay to neutrinos)

Hadron production correction  
using external data - PPFX  
(NA49, MIPP)

Focusing and hadron  
production uncertainties  
(multi-universe method)

## 2. Use in-situ measurements

Flux shape correction (low recoil  
neutrino scattering)

Flux normalization correction  
(scattering off atomic electrons)