

# Superconducting Nanowire Single Photon Detectors

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# Why Superconducting Detectors?

Superconducting detectors are the natural choice for very sensitive optical detection:

- 1- they have small energy gap
- 2- they work at cryogenic temperatures.

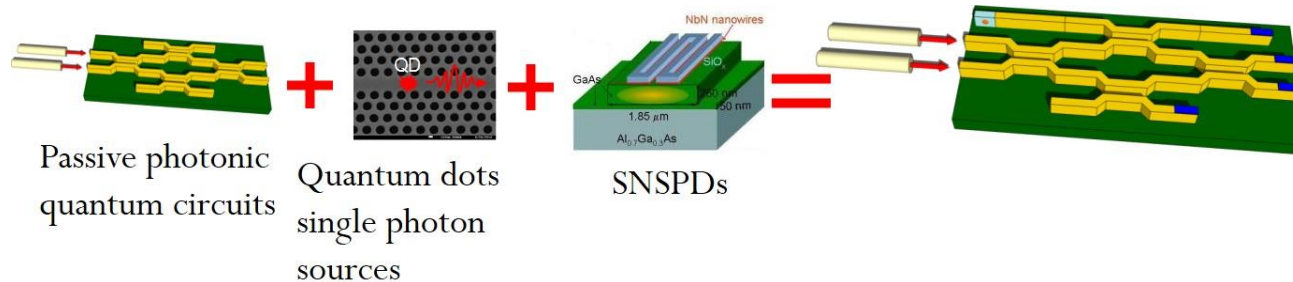
A small energy gap ( $\sim 1$  meV) as compared to semiconductors ( $\sim 1$  eV) implies an absorbed photon produces a much larger number of excitations (no needs to trigger an avalanche)

the inconvenience of operating at cryogenic temperatures ( $T \sim 4$  K) becomes a big advantage in terms of dark count as it is thermally activated

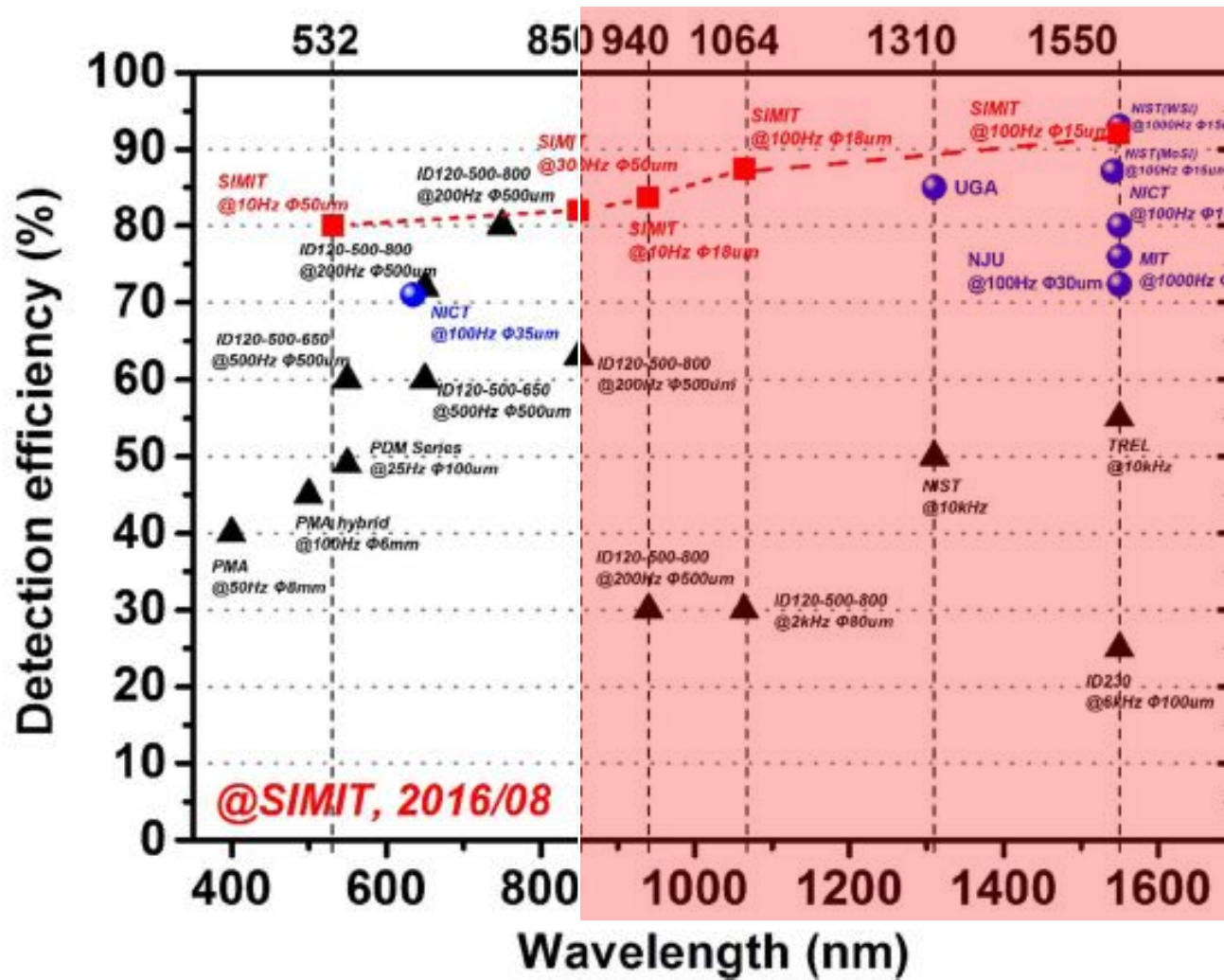
# Why Superconducting Nanowires Single Photon Detectors (SNSPD)?

## Why superconducting nanowire single photon detector?

- single photon counting from X-ray to MIR
- low dark count rate
- low jitter  $< 100$  ps (record 12 ps),
- fast count rates  $\sim$ GHz;
- Integration in photonic circuits (PICs)



# SPD technologies VIS-NIR



Lixing You et al., SUST (2017)

A. Gaggero, 01/10/2020, Genova

# SPD technologies @1550nm

Detector	DE	Maximum count rate	Dark count rate	FWHM Jitter	Operating temp.
PMT	2%	10 MHz	200 kHz	300 ps	200 K
InGaAs APD	10%	100 MHz	16 kHz	55 ps	250 K
TES	95%	100 kHz	< 1Hz	100 ns	0.1K
<b>SNSPD</b>	<b>93%</b>	<b>1GHz (potential)</b>	<b>&lt; 10 Hz</b>	<b>&lt; 20 ps</b>	<b>2.5 K</b>

$$\text{DE} = \frac{\text{\# detected photons}}{\text{\# incident photons}}$$

(detection efficiency)

H. Terai, et al." in *Optical Fiber Communication Conference*, paper M3G.4 (2018);

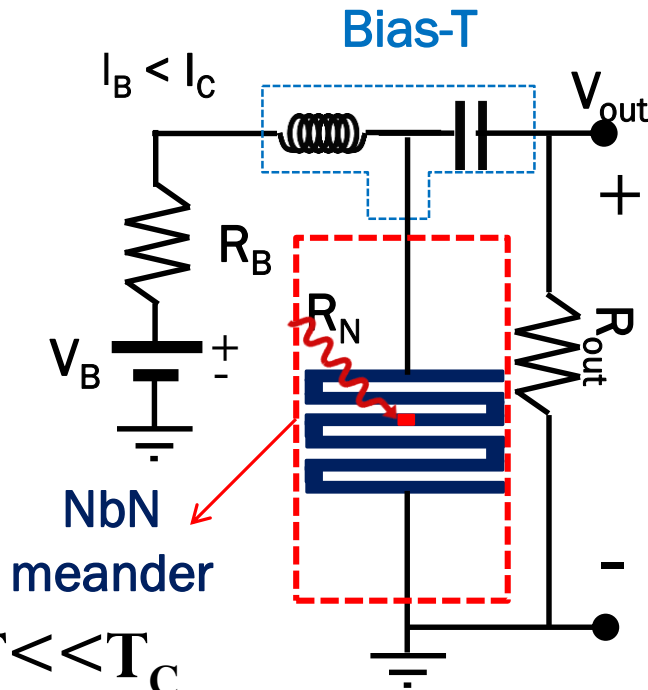
# SNSPD working principle

2 states:  $R_N = 0;$   
 $R_N \sim 1\text{k}\Omega;$

$$\tau_r = \frac{L_k}{50\ \Omega + R_n}$$

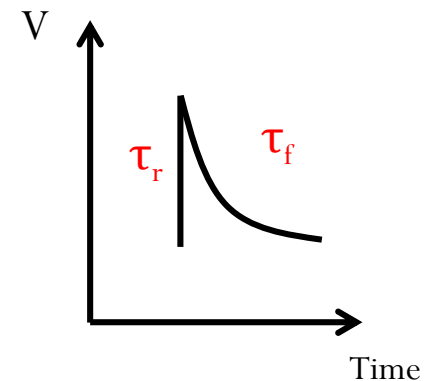
$$\tau_r = \frac{L_k}{50\ \Omega}$$

$T \ll T_C$



$$V_{out} \approx I_B \times R_{out}$$

$$R_{out} = 50\ \Omega$$



# Summary

- Active materials;
- Detection mechanism models;  
(counts vs Darkcounts)
- Detection efficiency;
- Single photon absorption in thin films, DE & SDE;
- Maximum Count rate;
- Timing resolution;
- Integration in photonics circuits (PICS);
- Photon number resolving functionality;
- Multiplexing;

# Active materials

Superconductors that have demonstrated capability of single-photon detection are films of compounds or alloys (classified as Type II superconductors):

Polycrystalline films: NbN (niobium nitride), NbTiN (niobium titanium nitride), NbSi, TaN...

Amorphous films: WSi (tungsten silicide) MoSi (Molibdenum Silicide), MoGe (Molybdenum Germanium) etc



# Polycrystalline films

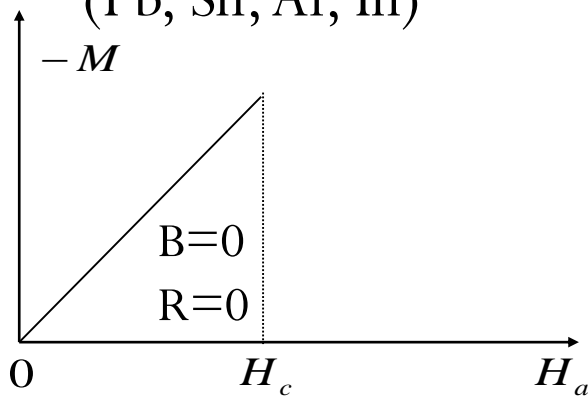
NbN, NbTiN Type II superconductors have short  $\xi$ .

They can be grown as ultra thin films (with thickness  $\sim \xi = 3-10$  (nm))

$$\xi_0 = \hbar v_F / \pi \Delta \quad \text{Coherence length} \sim \text{Cooper pair size}$$

Type I superconductors ( $\lambda < \xi$ )

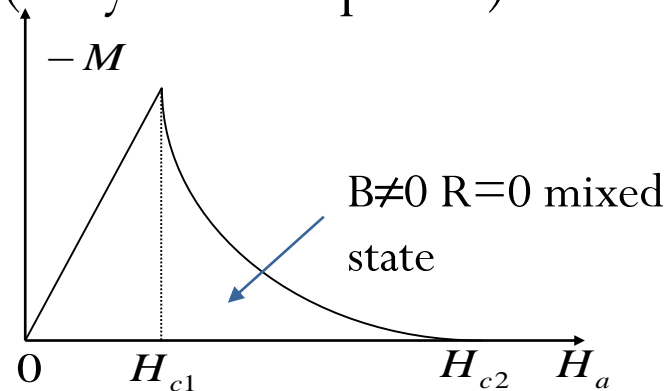
(Pb, Sn, Al, In)



Type I materials: at  $H_c$ , abrupt breakdown of the superconductivity

Type II superconductors ( $\lambda > \xi$ )

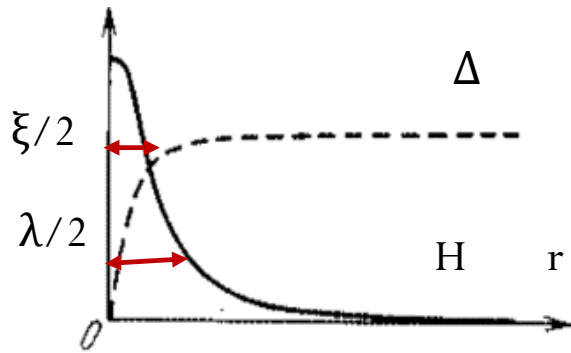
(alloy and compound)



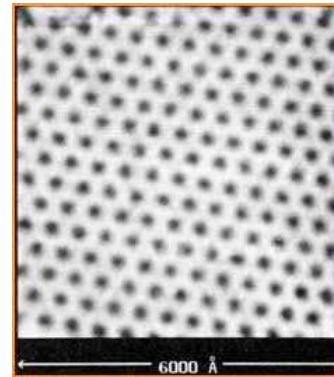
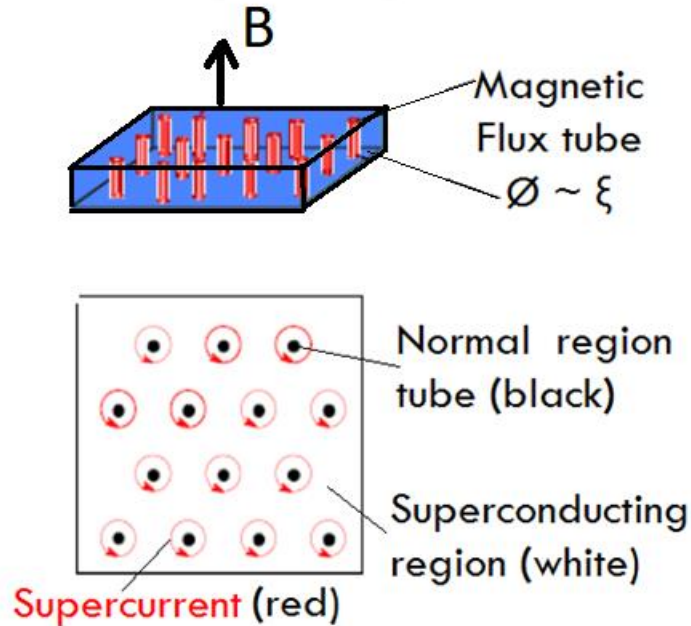
Type II materials: at  $H_{c1}$  B begins to penetrate; at  $H_{c2}$  total penetration of B

# Magnetic Vortices in Type II mixed state

Abrikosov (1957) Nobel Prize 2003

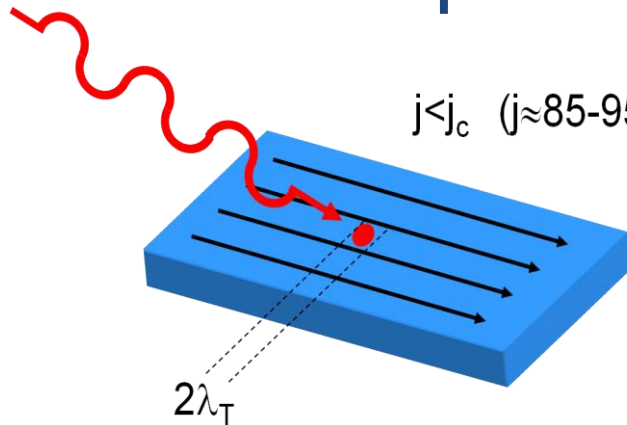


A magnetic vortex has a normal-conducting cylindrical core of radius  $\sim \xi$ , where a magnetic field persists enclosed by a circular supercurrent surrounded of the superconductive region over a length  $\lambda_L$ .



Abrikosov lattice on the surface of NbSe<sub>2</sub> film, imaged using STM. In the mixed state the density of vortices increases with  $H_a$

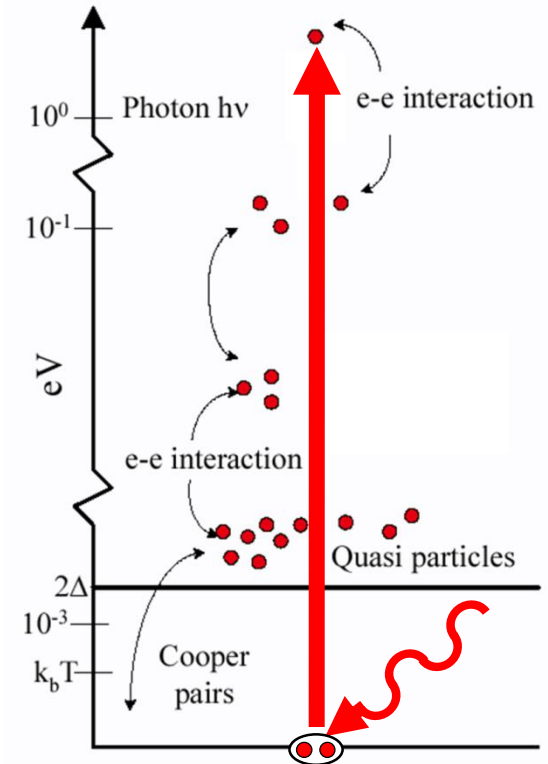
# Absorption and Quasi Particle Cloud



$w \sim 100\text{nm}$  wide,  
 $t \sim 4\text{nm}$  thick NbN  
Nanowire @  $T_b \sim 3\text{K}$

A photon with energy  $E_{\text{ph}} \sim 1\text{eV}$  gets absorbed by breaking a Cooper pair ( $E_{\text{ph}} \gg \Delta$ ), creating an excited electron

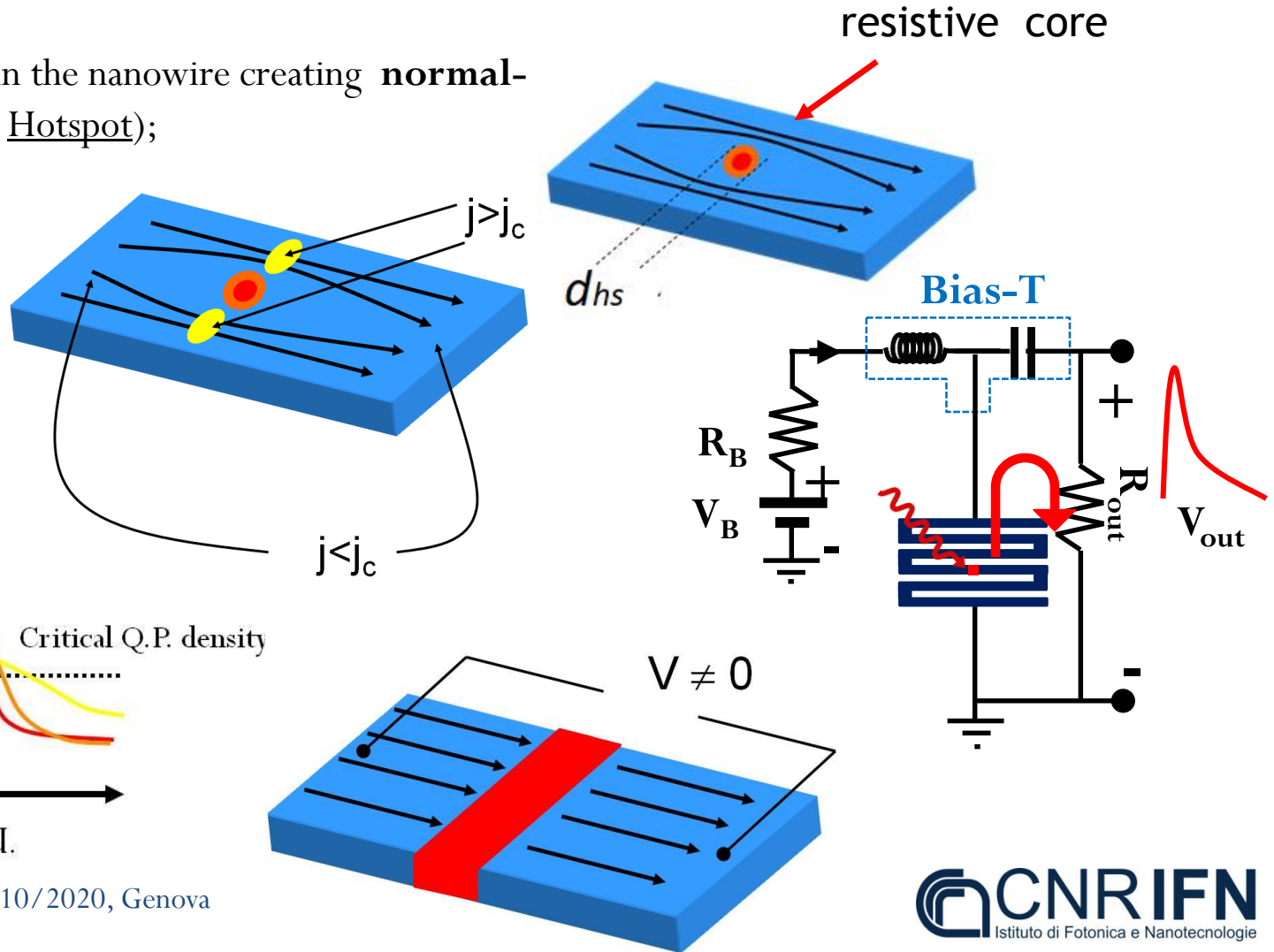
by Goltsman et al., APL (2001)



the hot (excited) electron relaxes, giving rise to a cascading process where several Cooper pairs are broken into excited electrons, creating a cloud of Quasi-Particles (QPs)

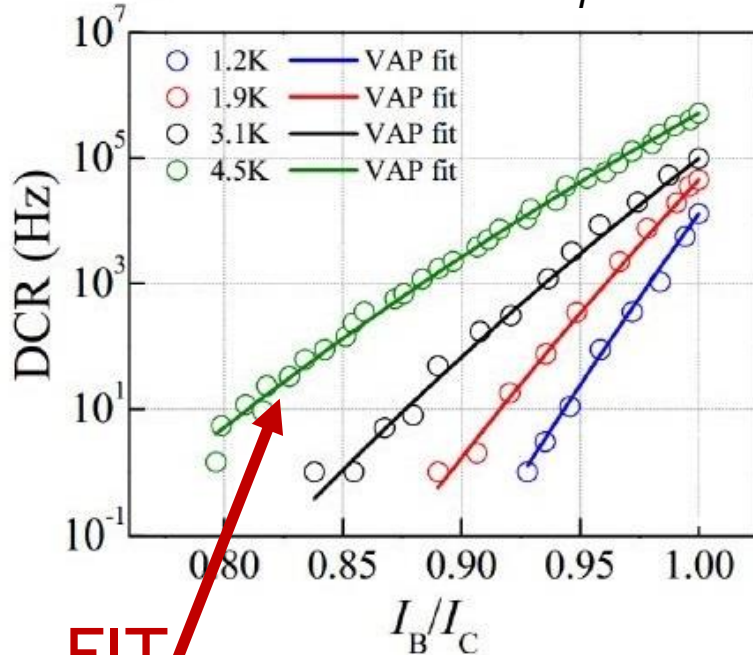
# Normal-Core Hotspot Model

The QPs cloud diffuses in the nanowire creating **normal-conducting core** (the Hotspot);



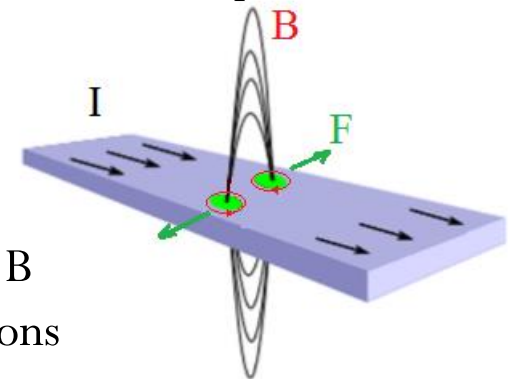
# Origin of Dark Counts in SNSPDs

Z. Zhou PhD thesis 2014



Kosterlitz–Thouless (KT) transition, Nobel Prize 2016

- NbN nanowire (thickness  $\sim \xi$ , width  $\gg \xi$ ) behaves like a 2-D Superconductor.
- **Vortex- antivortex pairs** (VAP) are pinned in the film (net  $B=0$ ) below critical temperature  $T_{KT}$



VAP unbinding due to:

- Lorentz force  $F = I \times B$
- Temperature fluctuations

Crossing of an unbound vortex (that has a normal core) creates decoherence due to dissipation and then triggers a resistive transition (false pulse => DCR)

$$P_{VAP} = \Gamma_{VAP} e^{-\frac{U_{VAP}}{k_B T}}$$

$$U_{VAP} \propto \Delta$$

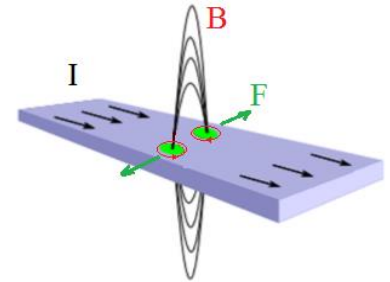
Binding VAP potential

A. Gaggero, 01/10/2020, Genova

# Limits of the Normal-Core Hotspot Model

1) The model does not explain origin of dark counts

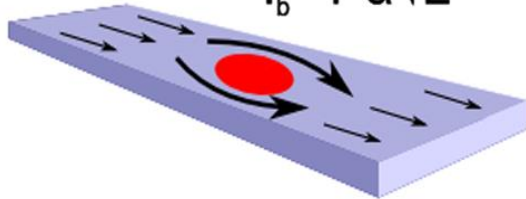
dark counts due to vortex crossing



*Yamashita APL (2011)*

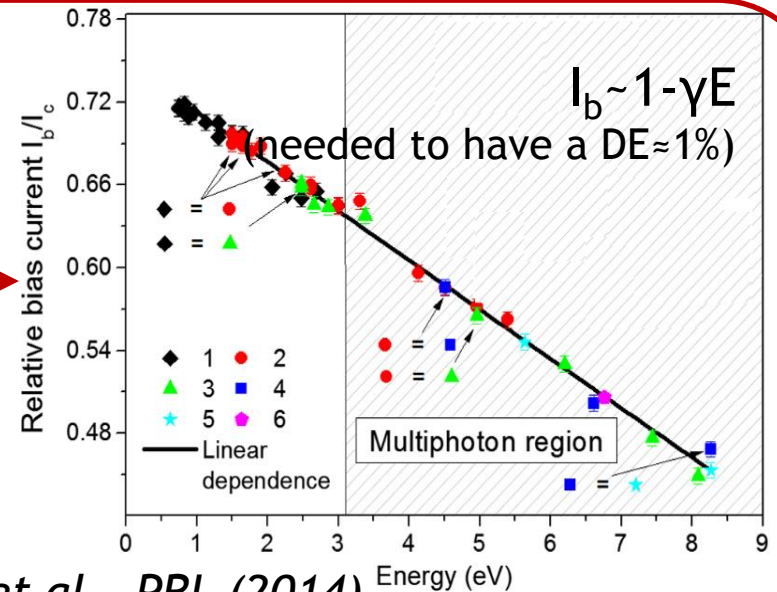
2) The model predicts:

$$I_b \sim 1 - \alpha \sqrt{E}$$



instead

A detection event need  $J > J_C$  (close the hotspot), i.e.  $I_b/I_c > 1 - d_{hs}/w$ .  
 $d_{hs} \sim E^{1/2}$  the hotspot diameter



*Renema et al., PRL (2014)*



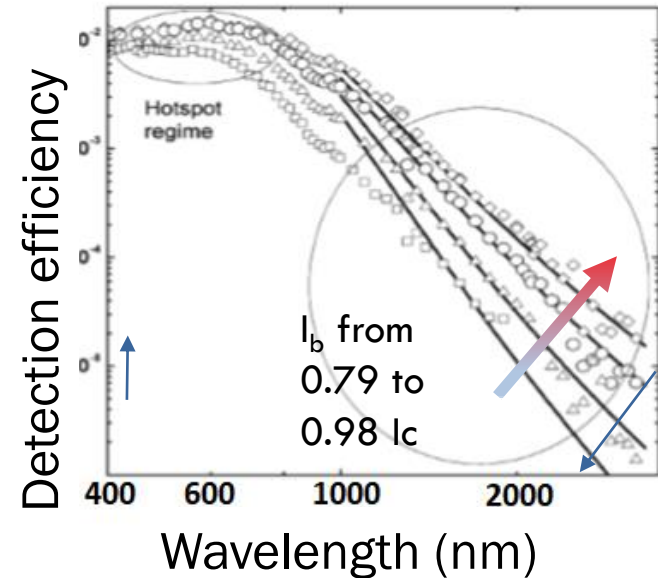
# Limits of the Normal-Core Hotspot Model

3) The model predicts a sharp spectral cut-off of the DE with the photon energy.

instead



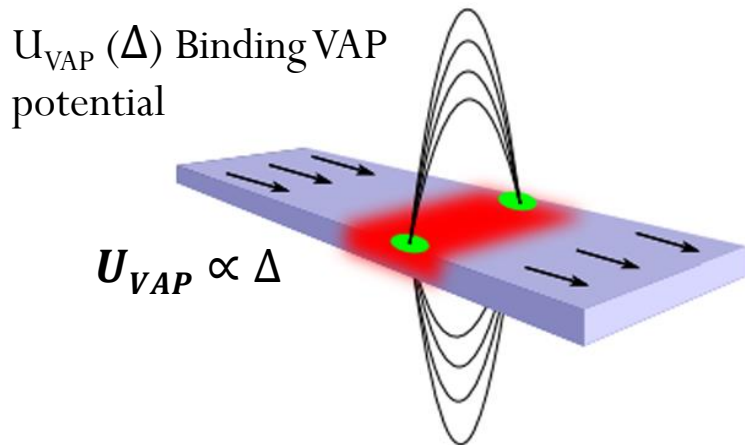
**Reason:** At low energies the hotspot size is too small to trigger the resistive transition



A. Semenov et al 2008

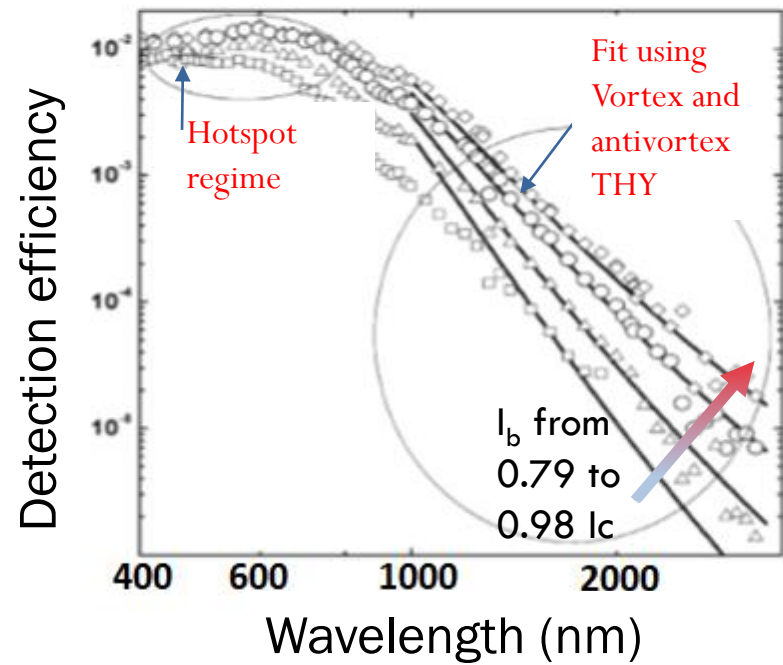
# Vortex-crossing model

The cloud of QPs ( $n_{qp}$ ) diffuse outward from the point of absorption, creating a (red) band of depleted superconductivity with a lower energy gap  $\Delta$ . This effect stimulates VAP unbinding.



- A lower  $\Delta$  decreases  $U_{VAP}$  allowing VAP unbinding
- Vortex crossing in the film triggers the resistive transition

A. Semenov et al 2008





In conclusion, Photon Detection results from the combination of Cooper pair breaking, QP diffusion and Vortex crossing.

- QP diffusion dominates at high energies
- Vortex crossing at low energies

# Detection Efficiency

The Detection efficiency (DE) is defined as:

$$DE = \frac{\# \text{ Counts} - \# \text{ Dark counts}}{\# \text{incident photons}}$$

DE is a function of the detector bias current  $DE(I_B)$ .

# Measuring DE: single photon regime

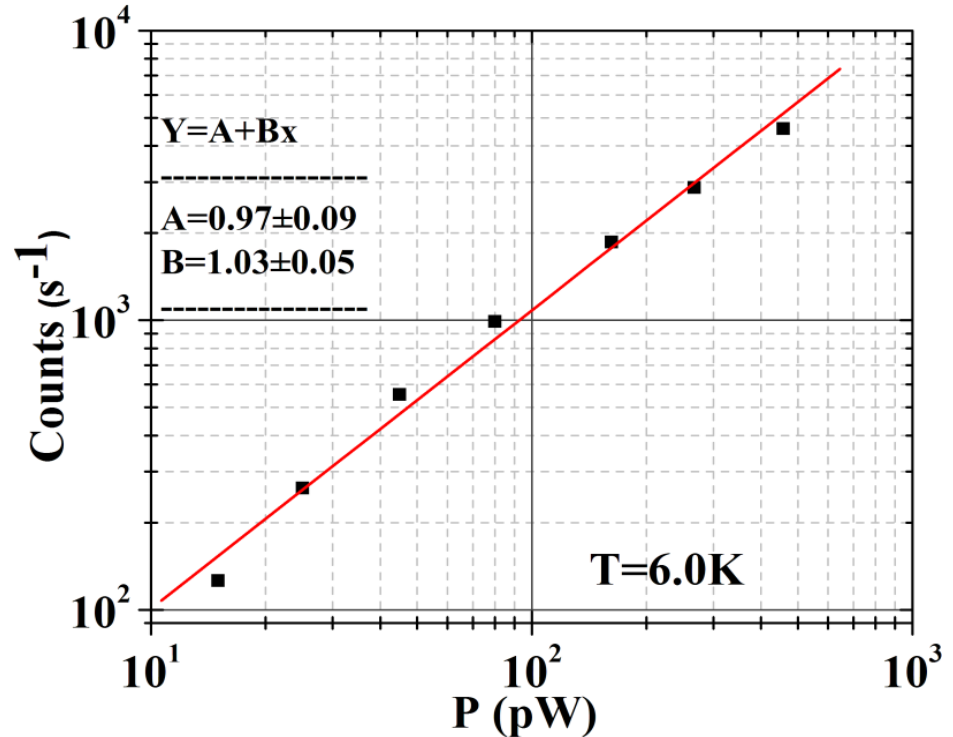
$\mu$  = average number of photons

$n$  = number of photons

$$P(n) = \frac{e^{-\mu} \mu^n}{n!}$$

If  $\mu \ll 1$ :

$$P(n) = \frac{\mu^n}{n!} \Rightarrow P(1) = \mu; P(2) \propto \mu^2; P(3) \propto \mu^3$$



# System detection efficiency SDE

$$DE = \eta_a \times \eta_i$$

$\eta_i$  = internal efficiency;

$\eta_a$  = probability of absorption

$$SDE = \eta_C \times \eta_a \times \eta_i$$

$\eta_C$  = optical losses in the cryostat;

$\eta_i$  improved by:

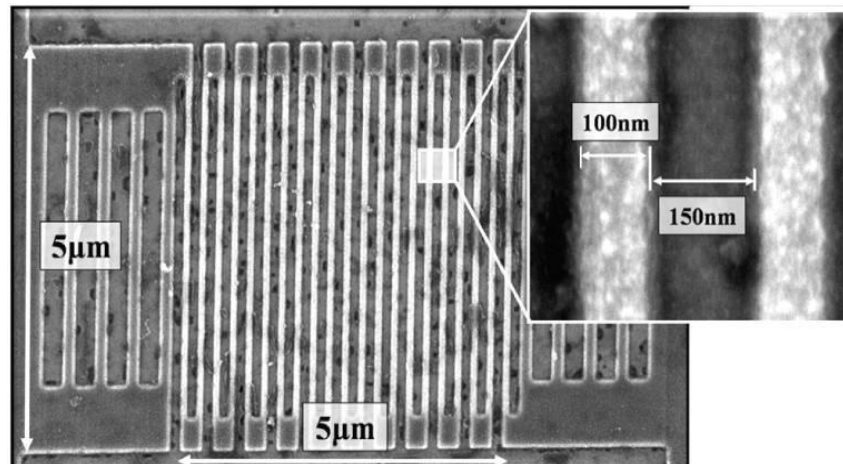
- Homogeneity and uniformity of the nanowire;
- Geometry (width, thickness);
- Fabrication parameters;

$\eta_a$  improved by

- Single pass cavity
- Integration on waveguide

$\eta_C$  improved by:

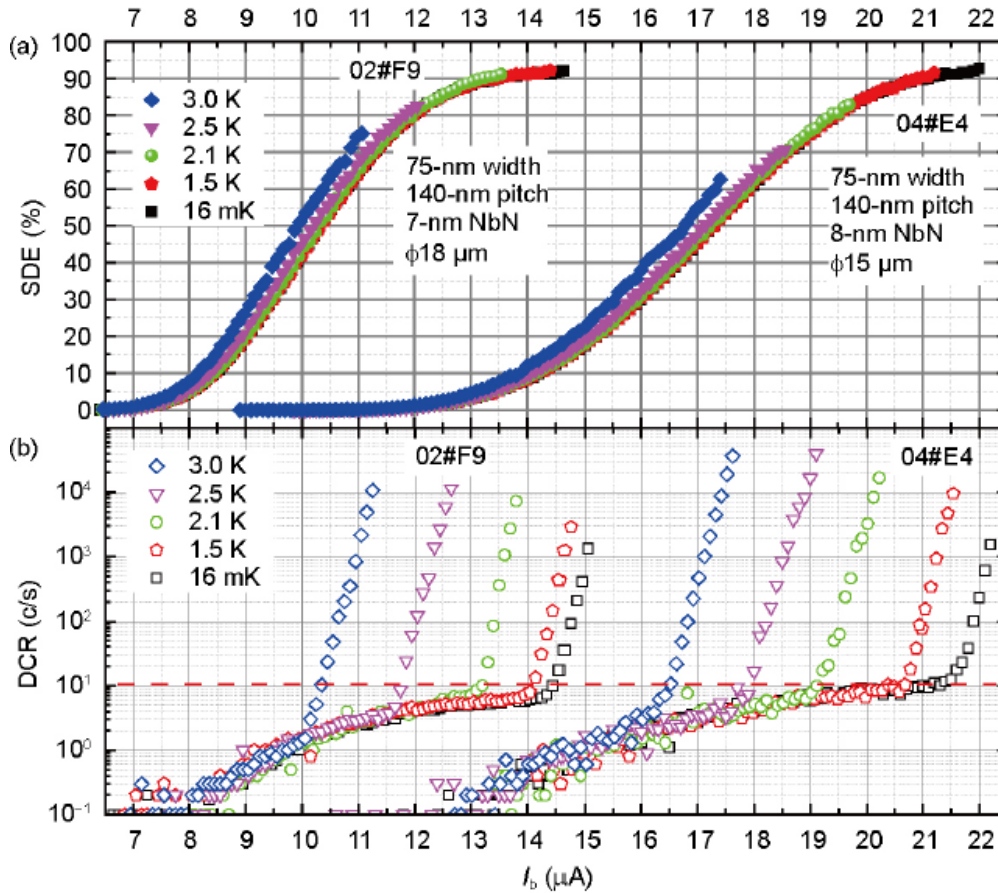
- Meander structuring
- Fiber alignment
- Grating couplers



# Internal efficiency, $\eta_i$

**Polycrystalline:** NbN, NbTiN;

high SNR, low jitter, high repetition rate, low yield

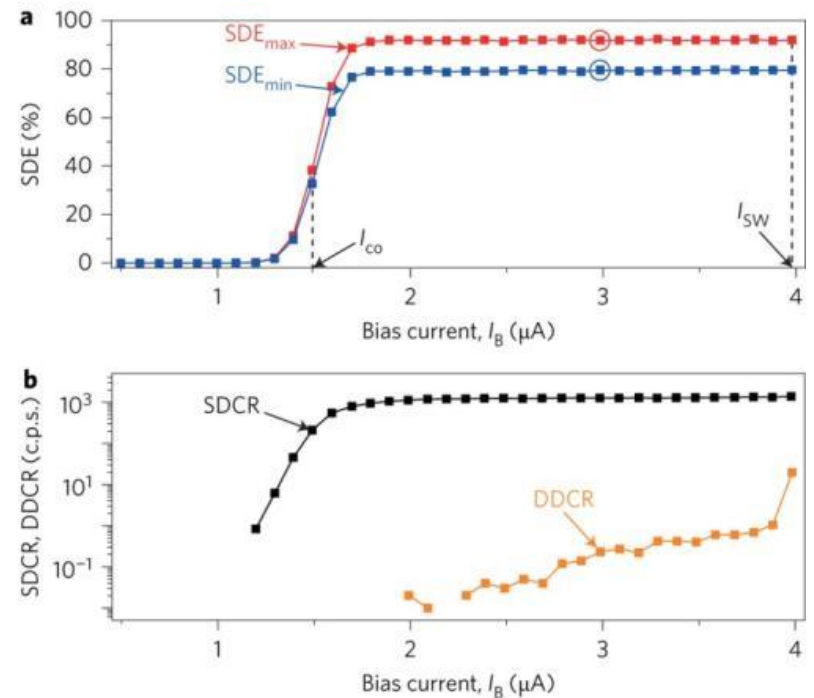


W. J. Zhang et al. Sci. China Phys. Mech. Astron. (2017)

A. Gaggero, 01/10/2020, Genova

**Amorphous:** WSi, MoSi;

high SQE, high yield, low SNR, high jitter.

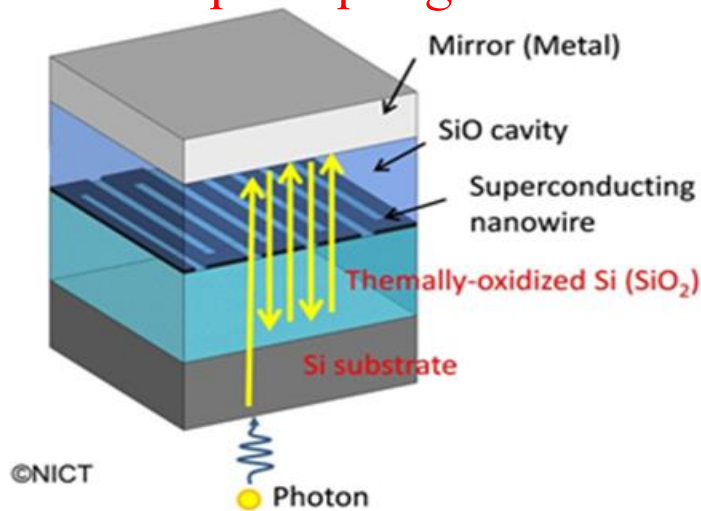


Marsili et al. Nat. Phot (2013);

# Single photon absorption in Nanowires, $\eta_a$

Thin superconducting film ( $3 \text{ nm} < d < 9 \text{ nm}$ ), low absorption!

## Top coupling



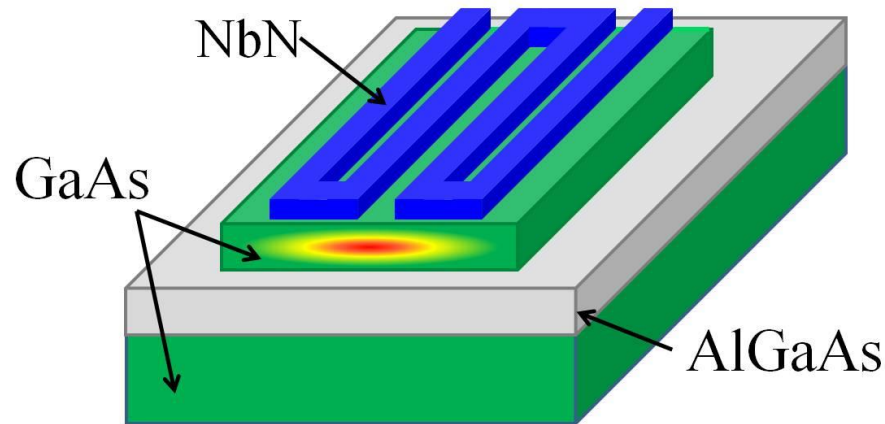
## Efficiently Fiber Coupled Detectors

Not Scalable, slower response.

High optical coupling, suitable fiber coupling with external experiments

A. Gaggero, 01/10/2020, Genova

## Travelling wave

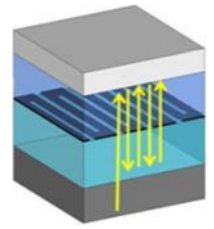


## Integration in photonic circuits

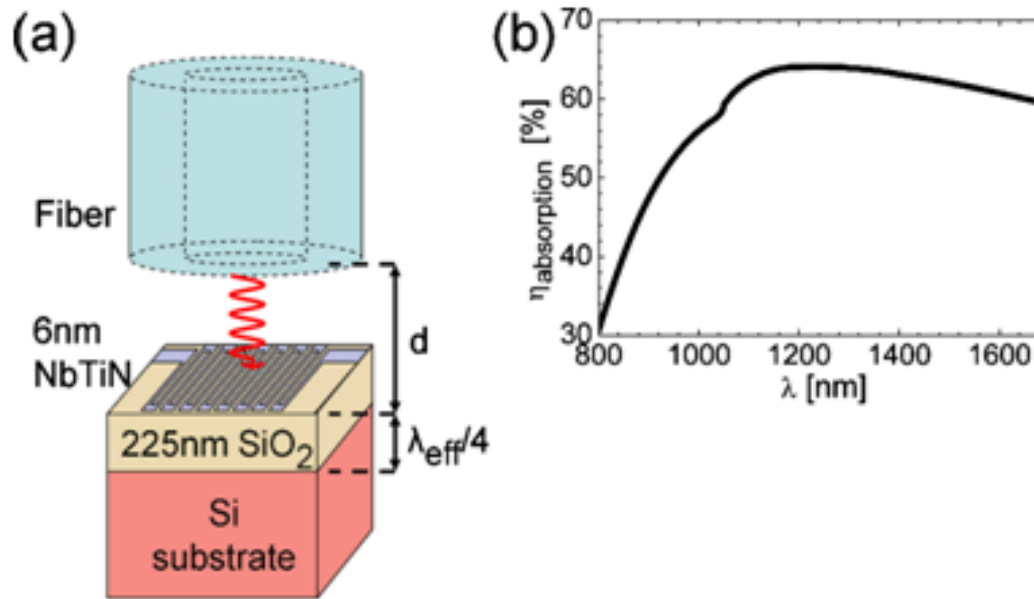
Scalable, faster response, better timing jitter.

High coupling losses, suitable for quantum optics experiments with integrated circuits.

# Efficiently Fiber Coupled Detectors: Absorption in Nanowires, $\eta_a$

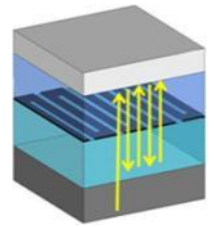


Broad optical cavity:  
quarter wavelength mirror

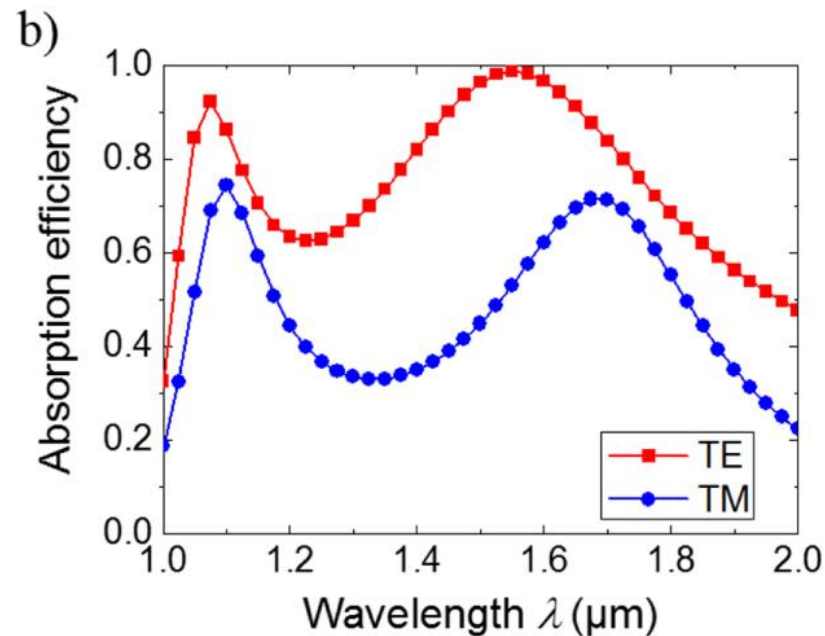
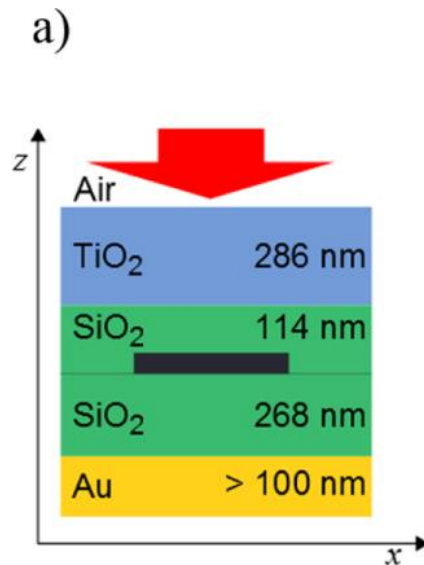


M. G. Tanner et al., *Appl. Phys. Lett.* (2010)

# Efficiently Fiber Coupled Detectors: Absorption in Nanowires, $\eta_a$



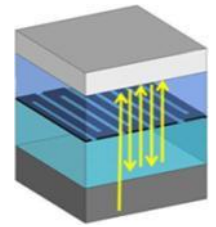
Broad optical cavity:  
quarter wavelength mirror



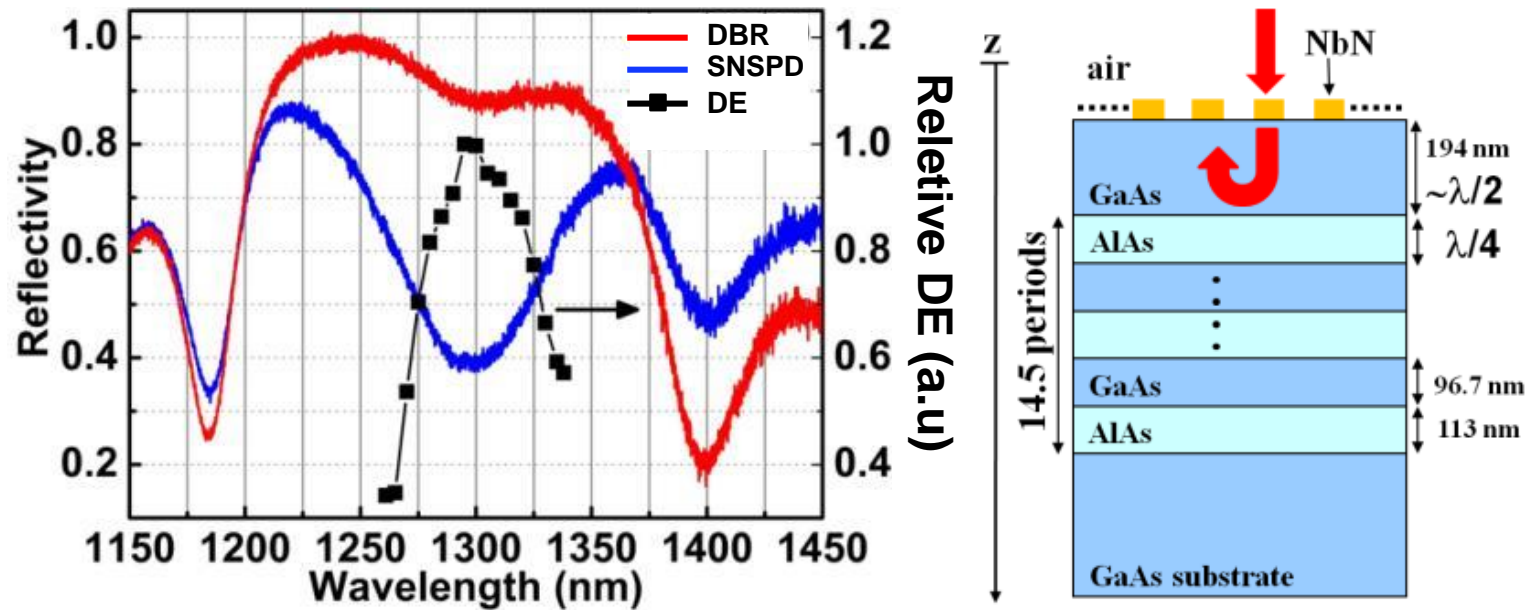
L Redaelli et al., *SUST* (2016)



# Efficiently Fiber Coupled Detectors: Absorption in Nanowires, $\eta_a$



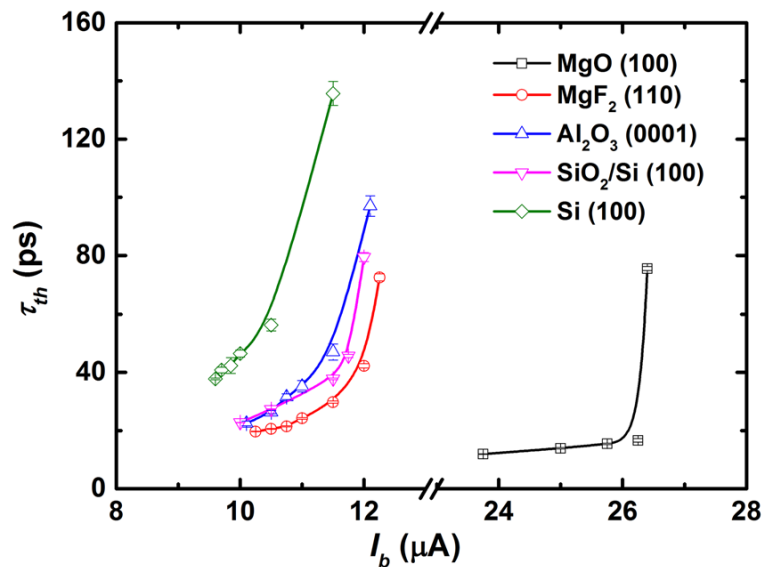
Narrow optical cavity:  
distributed bragg reflector



A. Gaggero et al. ,*Applied Physics Letters* (2010)

# Maximum Countrate: Hotspot relaxation time ( $\tau_{th}$ )

substrate	t (nm)	w (nm)	s (nm)	$I_{sc}$ ( $\mu A$ )	$J_c$ (MA/cm <sup>2</sup> )	$\tau_{th}$ (ps)
MgO (100)	5.5	90	110	33	6.7	11.6 $\pm$ 0.1
MgF <sub>2</sub> (110)	4.5	90	110	22.5	5.4	19.7 $\pm$ 0.1
Al <sub>2</sub> O <sub>3</sub> (0001)	7	130	70	21.5	2.4	22.5 $\pm$ 0.7
SiO <sub>2</sub> /Si (100)	7	90	110	21	3.3	22.7 $\pm$ 0.1
Si (100)	7.5	90	110	19	2.8	34.5 $\pm$ 0.3



A. Gaggero, 01/10/2020, Genova

$\tau_{th}$  (hotspot relaxation time) depends on film disorder.

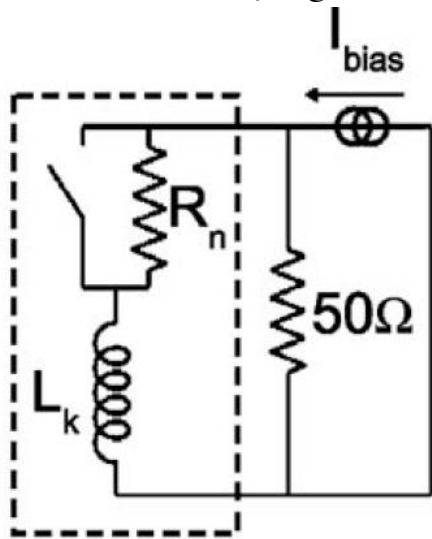
$\tau_{th}$  physical limit to the maximum countrate achievable

$\tau_{th} \rightarrow$  tens of ps  $R \rightarrow$  GHz

Zhang et al. Scientific reports 2018

# Maximum Countrate: Kinetic Inductance $L_K$

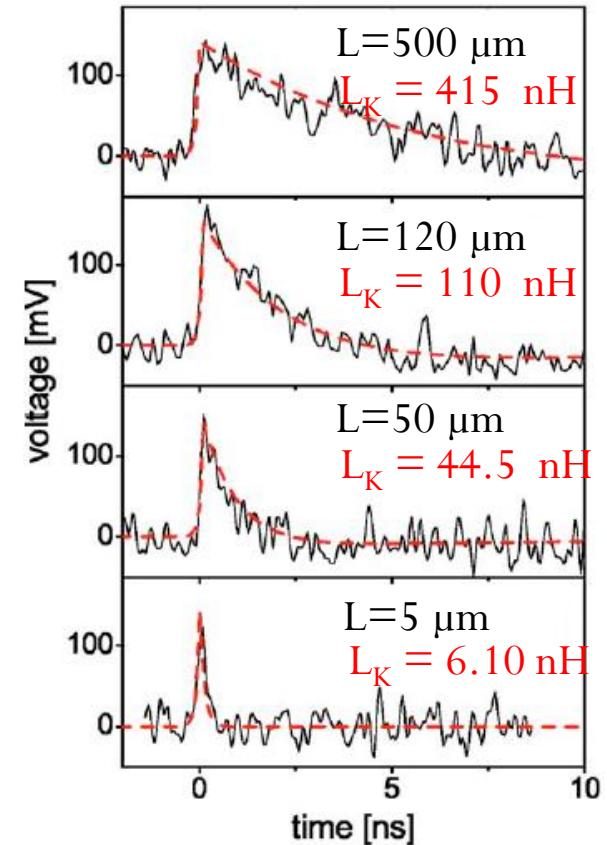
In a current-biased superconducting film, after the destruction of a certain number of Cooper pairs, the remaining pairs accelerate to carry the same bias current. Because the pairs are characterized by nonzero inertia, this process can be modelled as time-varying kinetic inductance  $L_K$



$$L_K = \frac{m}{2n_s e^2} \frac{L}{wd}$$

$$\tau_r = \frac{L_k}{50 \Omega + R_n} \quad \tau_f = \frac{L_k}{50 \Omega}$$

$\tau_f \rightarrow$  tens of ns  $R \rightarrow$  MHz



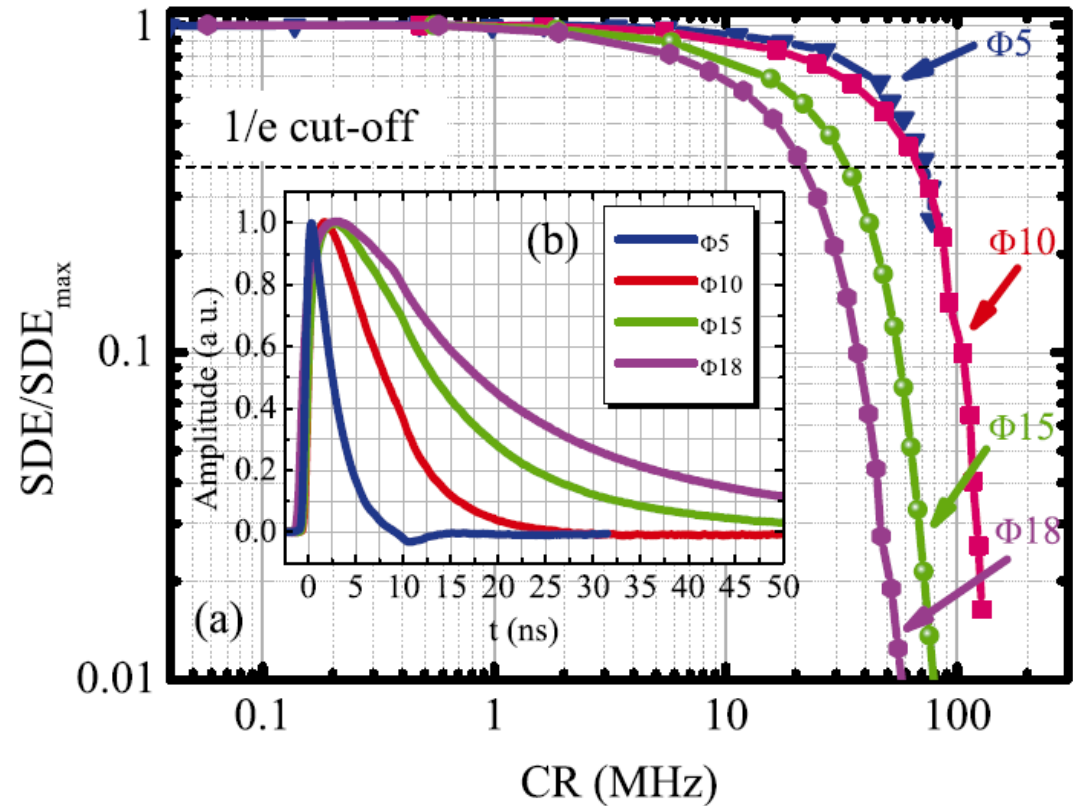
Kerman et al., app phys lett. 2006

# Maximum Countrate vs DE

Detector active area diameters  $\Phi = 5, 10, 15, \text{ and } 18 \mu\text{m}$

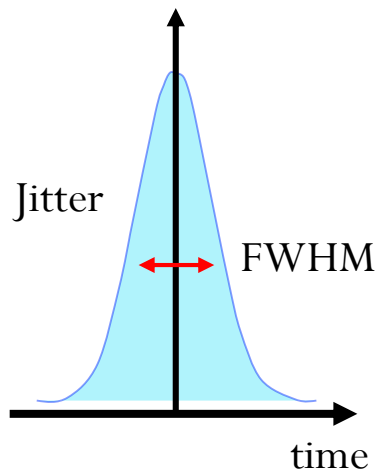
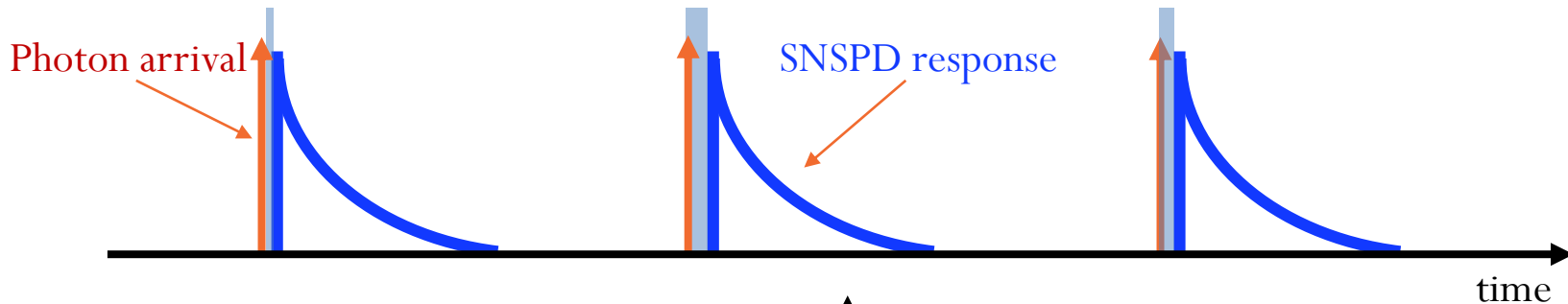
$\phi$ ( $\mu\text{m}$ )	$\tau_f$ (ns)	MCR (MHz)
5	4.8	208
10	11.9	84
15	26.2	38
18	44.4	23

Zhang et al. *AIP Advances* (2015)



# Timing resolution: Jitter

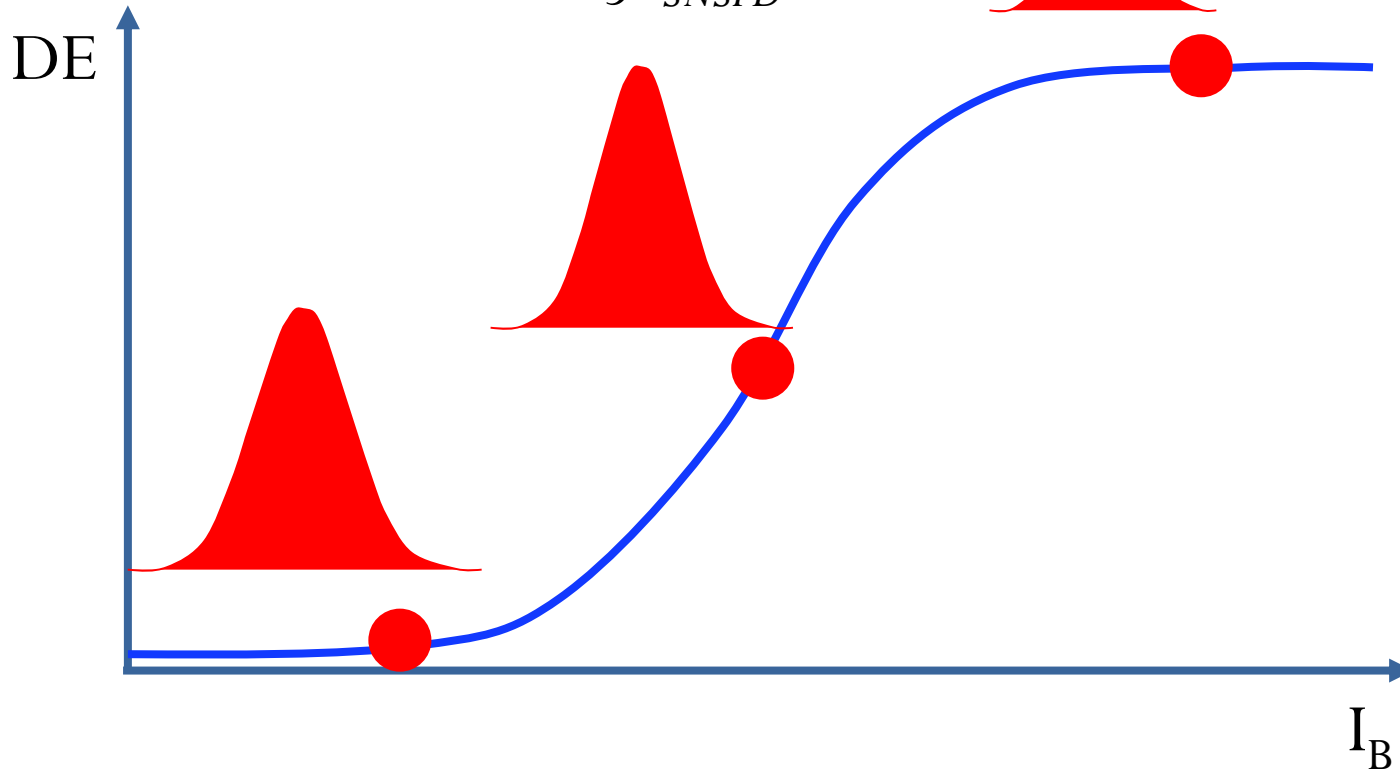
- Timing jitter characterizes the time **delay** between **the detection pulse** and the **the corresponding incident photon**. It is the detector **time resolution**.
- Gaussian distribution and the timing jitter is **FWHM**



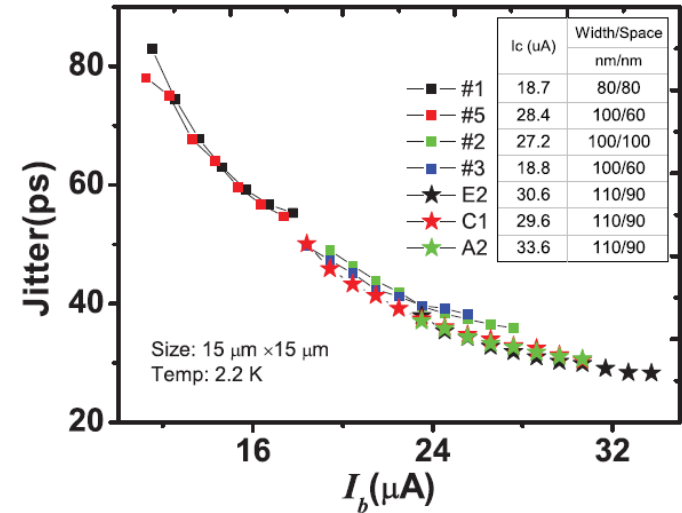
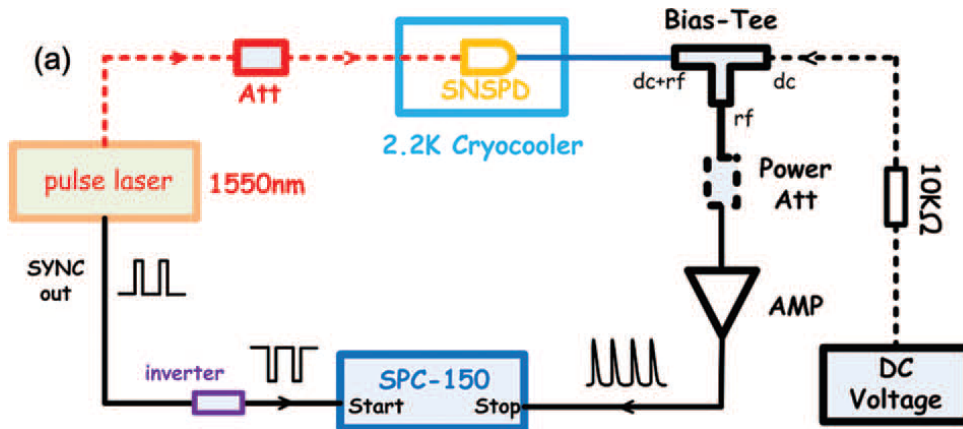
# Timing resolution: Jitter

$$J^2_{System} = J^2_{SNR} + \boxed{J^2_{geom} + J^2_{hp}} + J^2_{Setup}$$

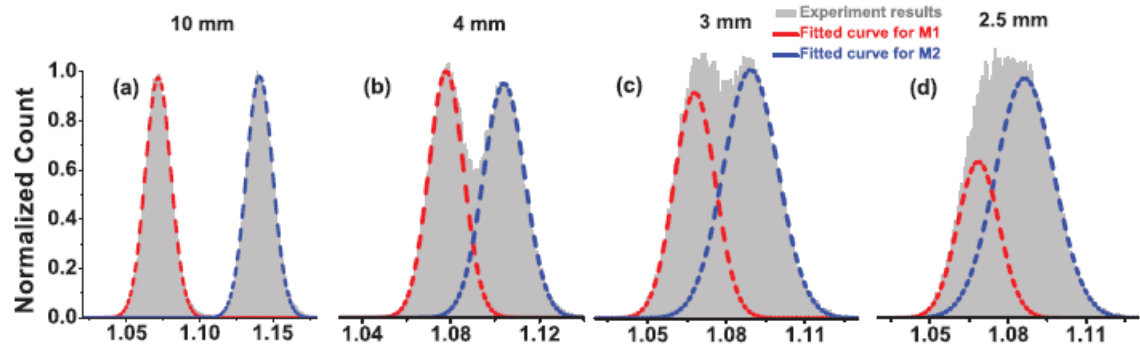
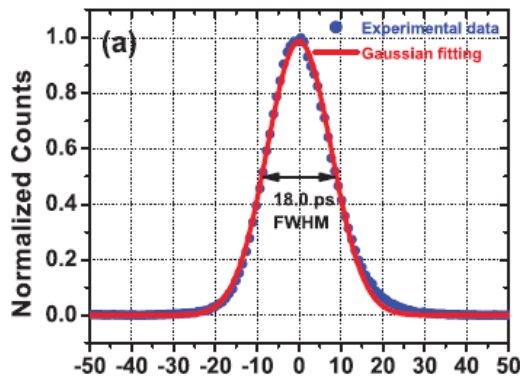
$J^2_{SNSPD}$



# Timing resolution: Jitter vs $I_B$



$$j_{\text{system}} = \sqrt{j_{\text{SNSPD}}^2 + j_{\text{laser}}^2 + j_{\text{SYNC}}^2 + j_{\text{SPC}}^2}$$

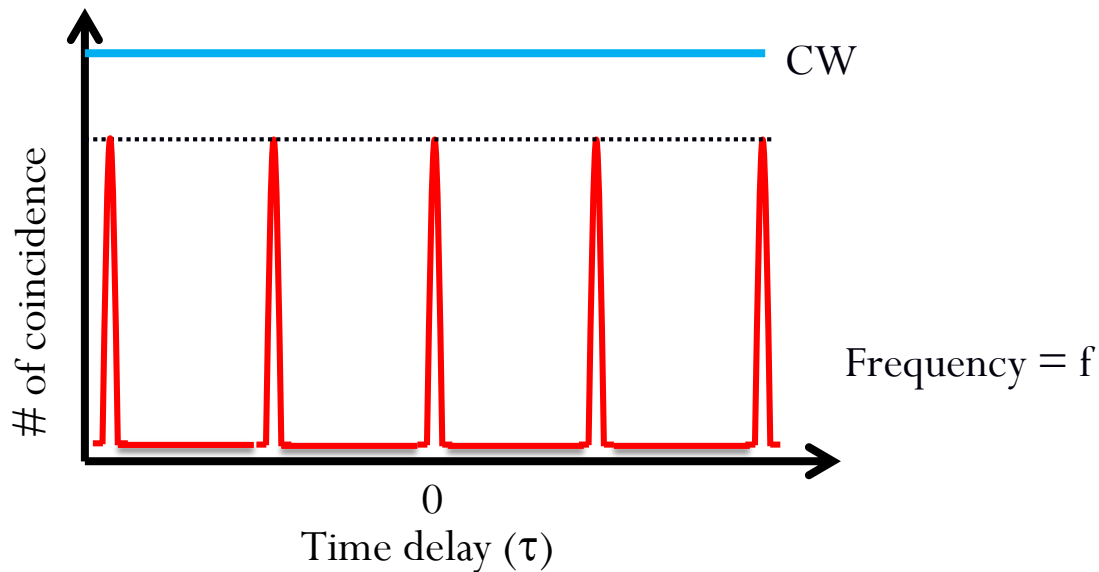
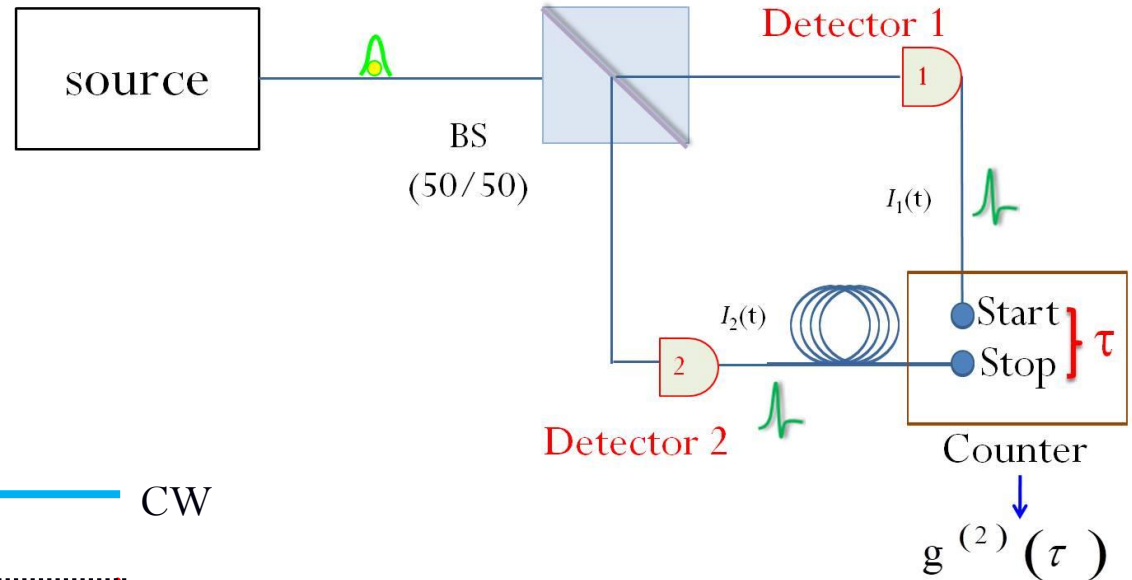


L. You et al., AIP Advances (2013)  
A. Gaggero, 01/10/2020, Genova

$\lambda = 1550 \text{ nm}$ , LiDAR, time of flight TOF WD  $\sim 115 \text{ m}$  with a depth resolution of 3 mm.

# Single photon emitter characterization

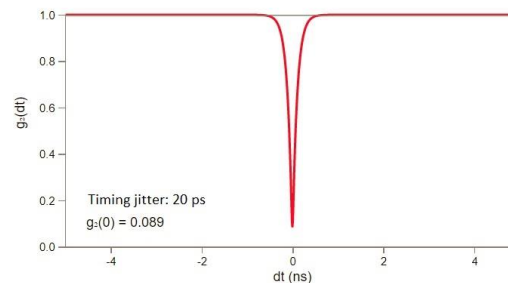
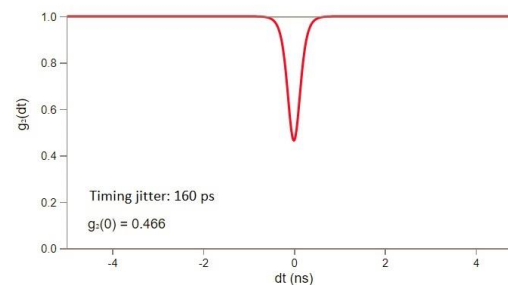
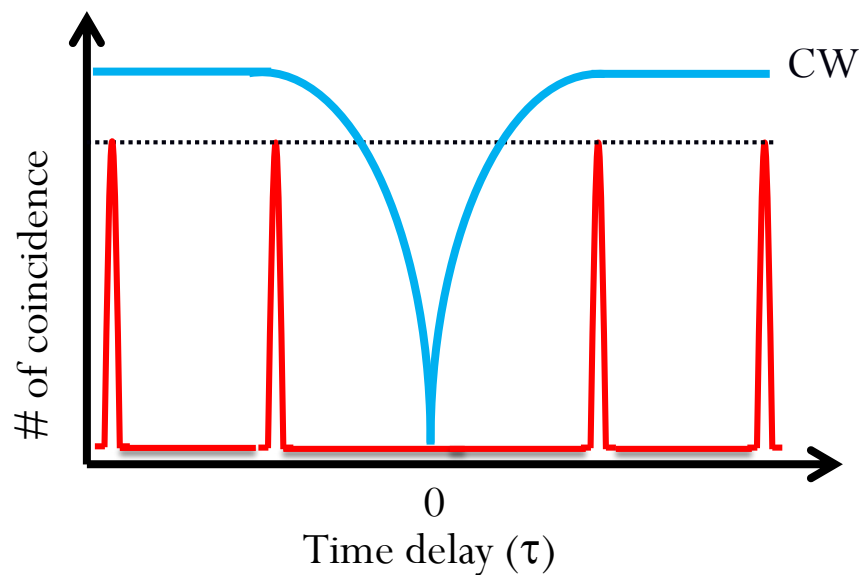
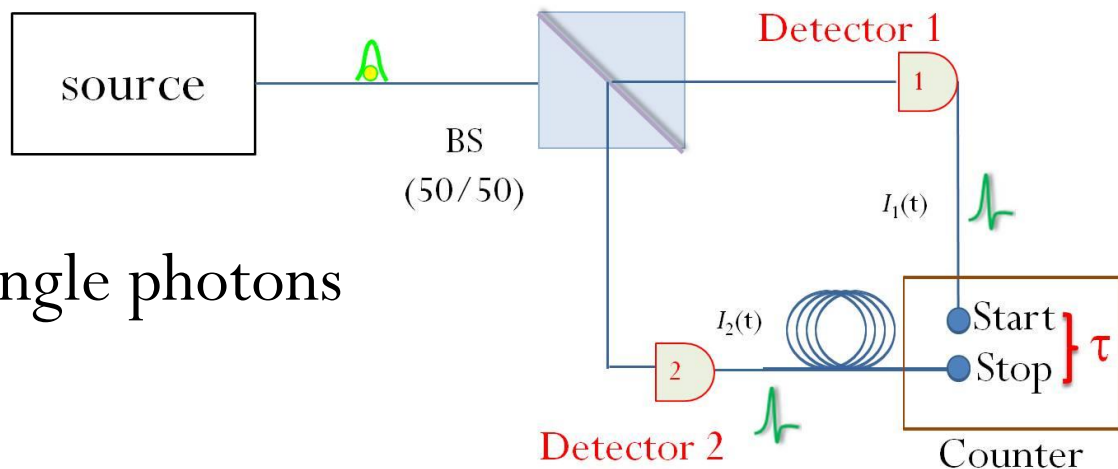
Source 1:  
CW or Pulsed Laser





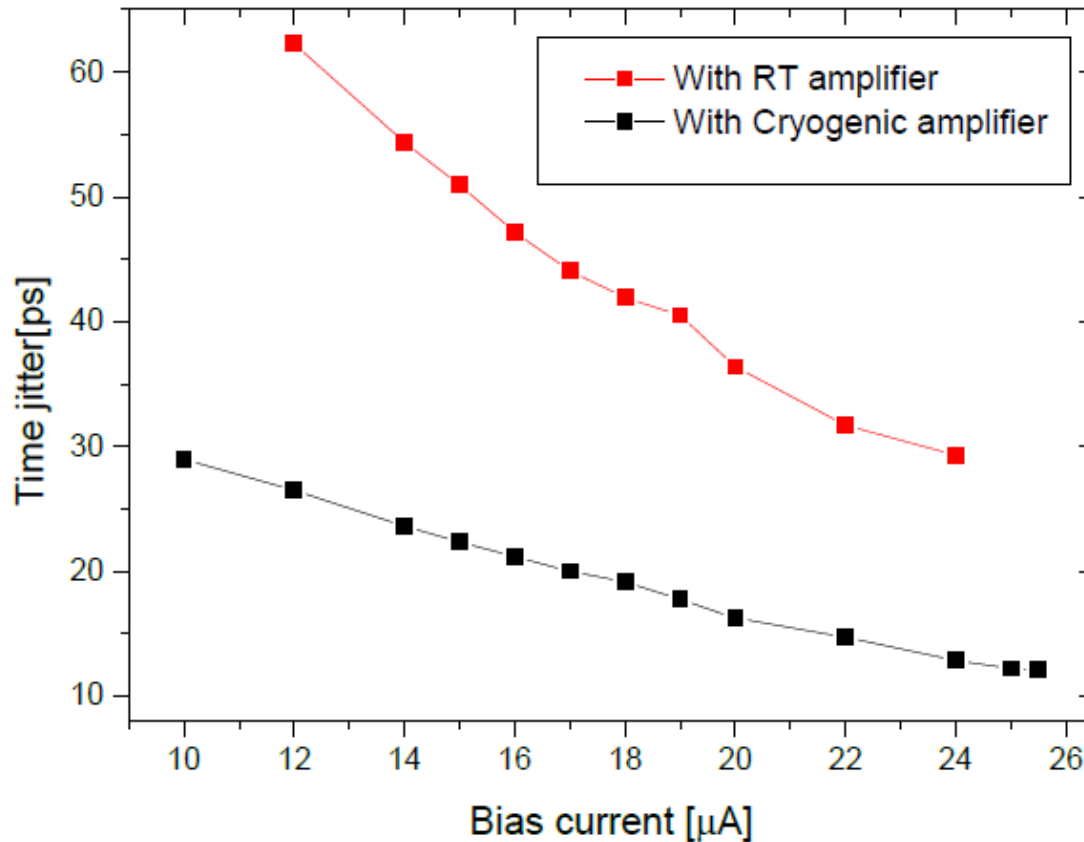
# Single photon emitter characterization

Source 2:  
Quantum emitter of single photons



$g^{(2)}(\tau)$

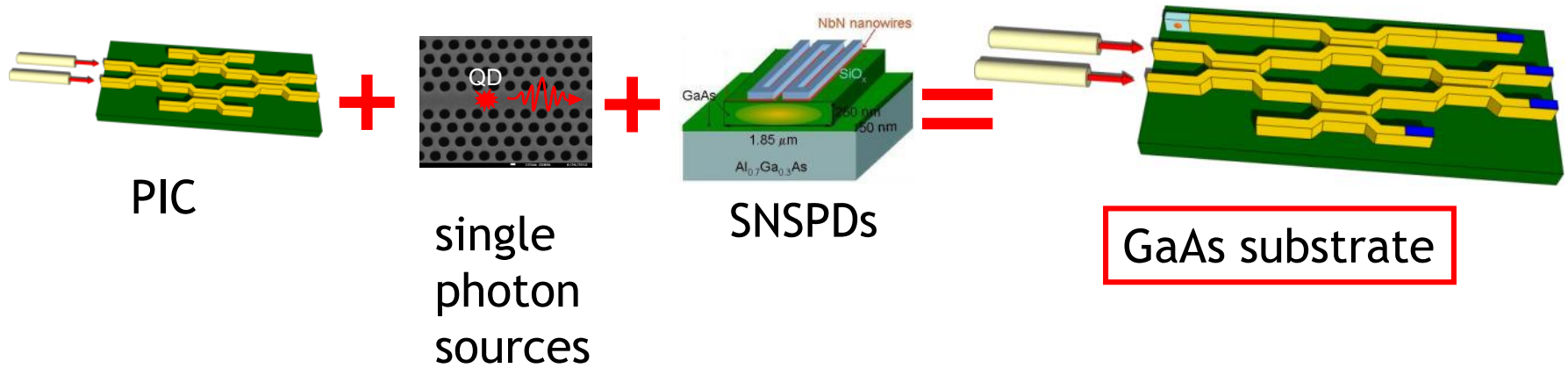
# Timing resolution: Jitter



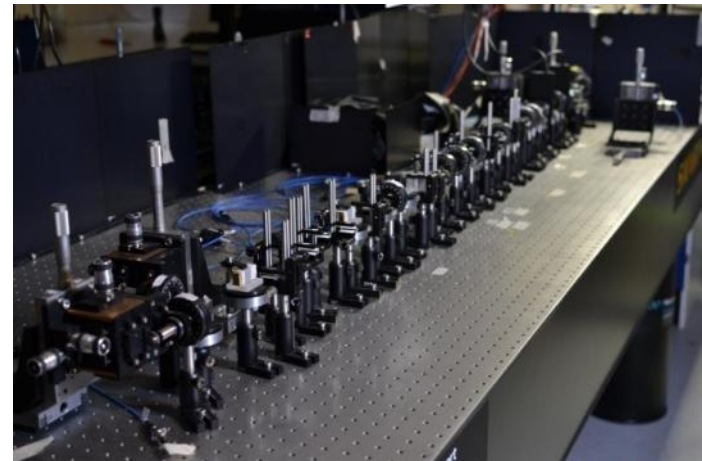
I. Zadeh et al., arXiv (2018)

A. Gaggero, 01/10/2020, Genova

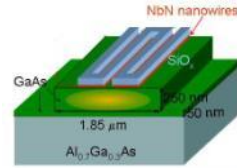
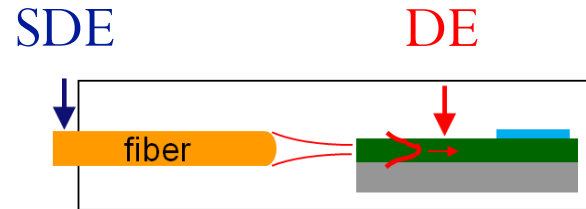
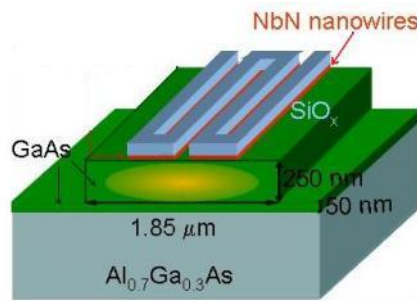
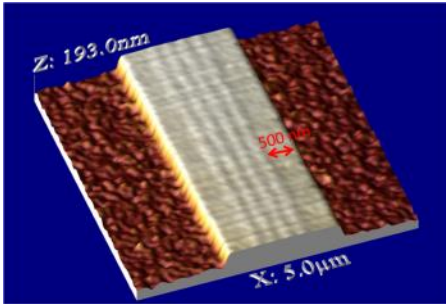
# Adding Detection Functionality to PICs



Conventional approach

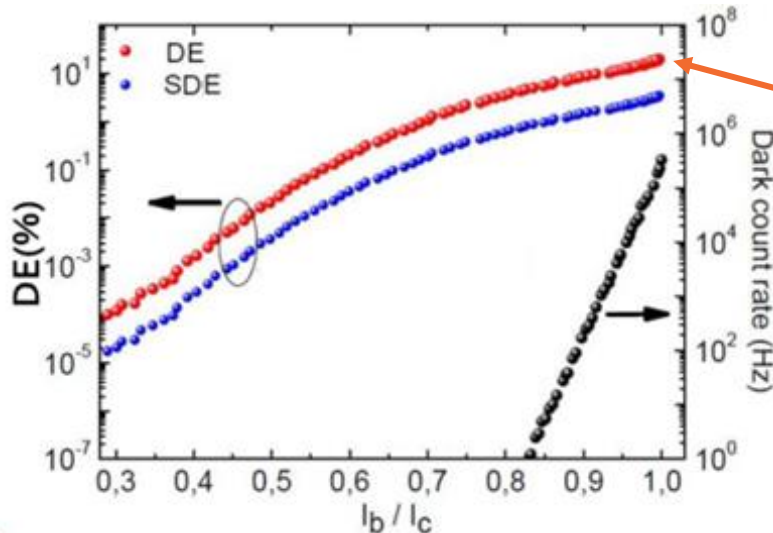


# Waveguide Single Photon Detectors: GaAs



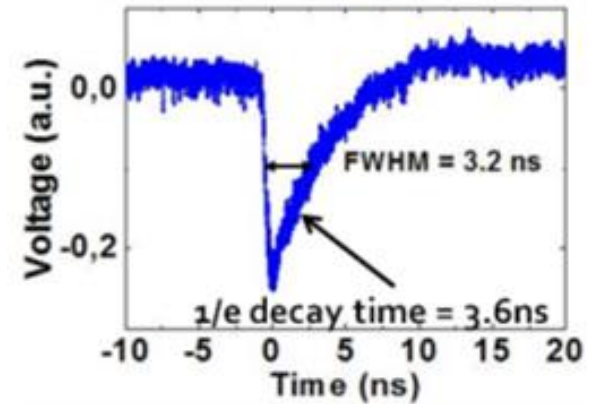
End fire coupling

*J. P. Sprengers, Gaggero et al APL (2011)*



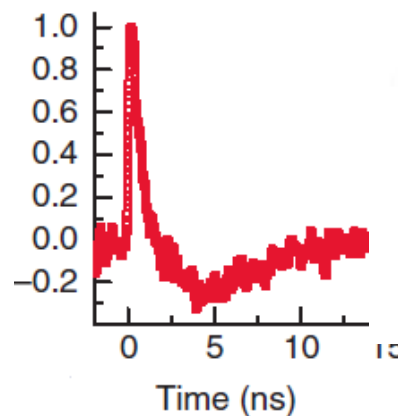
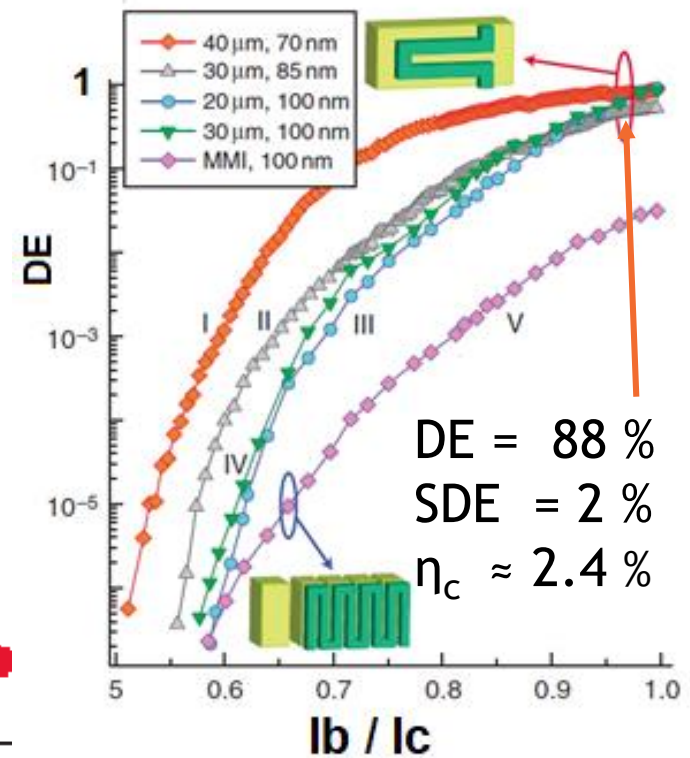
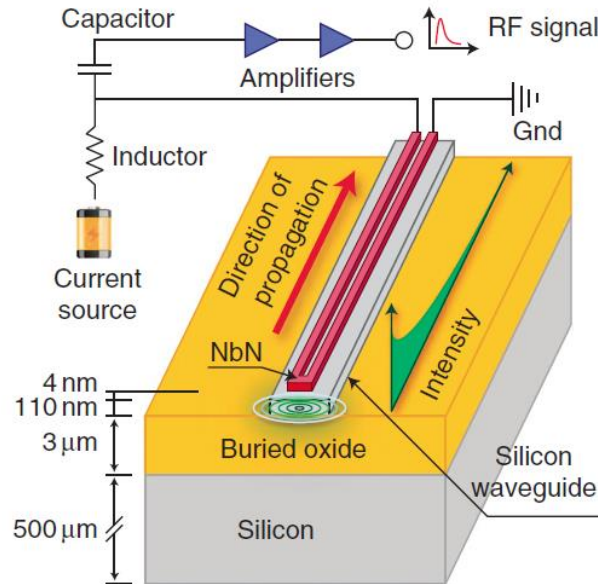
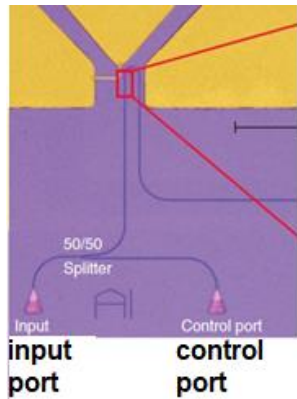
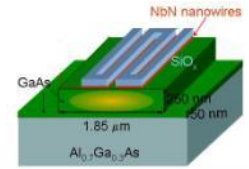
DE = 20 %  
SDE = 3.4 %  
 $\eta_c = 17 %$

Photoresponse of a 4x50 µm WSPD



$\eta_c$  is low, but the goal is to integrate either sources and detectors in the PICs

# Waveguide Single Photon Detectors: SOI



SOI vs GaAs

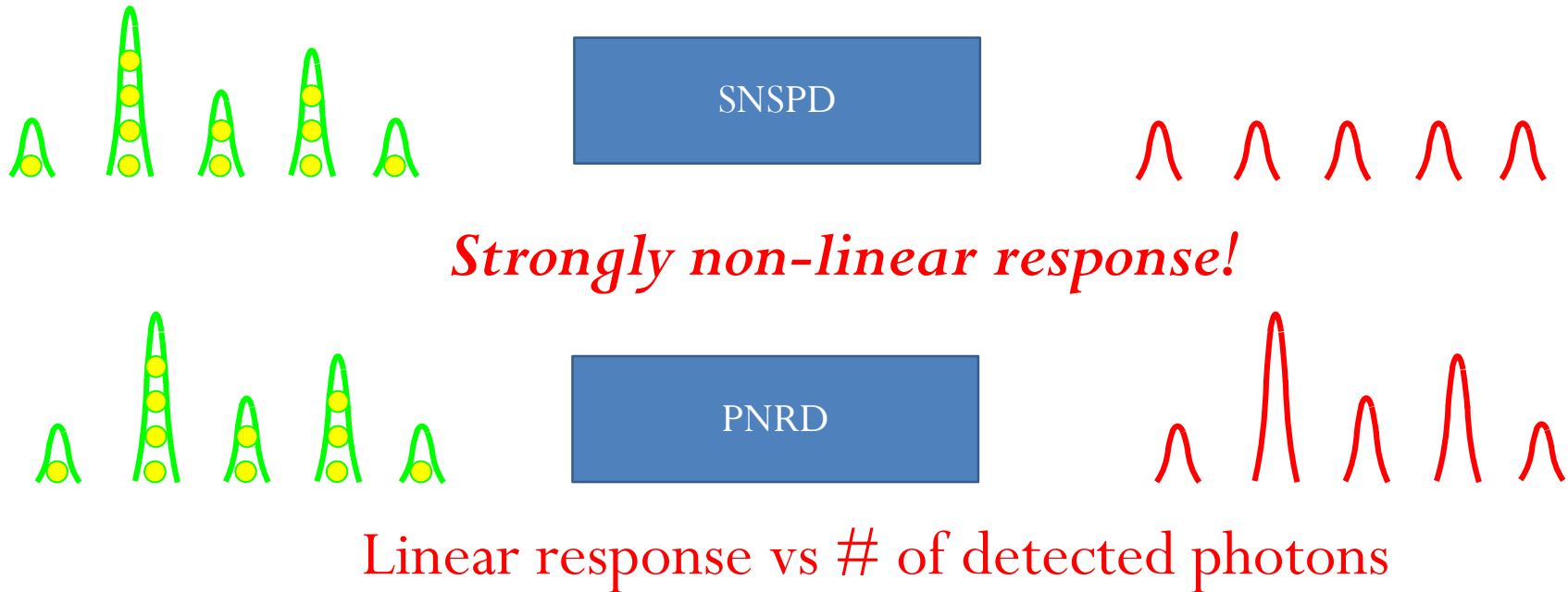
- Higher index contrast
- Higher NbN deposition temperature

*Pernice et al., Nat Comm (2012)*

A. Gaggero, 01/10/2020, Genova

After these first successful integrations of WSPDs on GaAs and SOI platforms, this approach has been followed also on SiN, Diamond and (work is in progress) on AlN and SiC and other materials suitable for integrated photonics.

# Photon Number Resolution

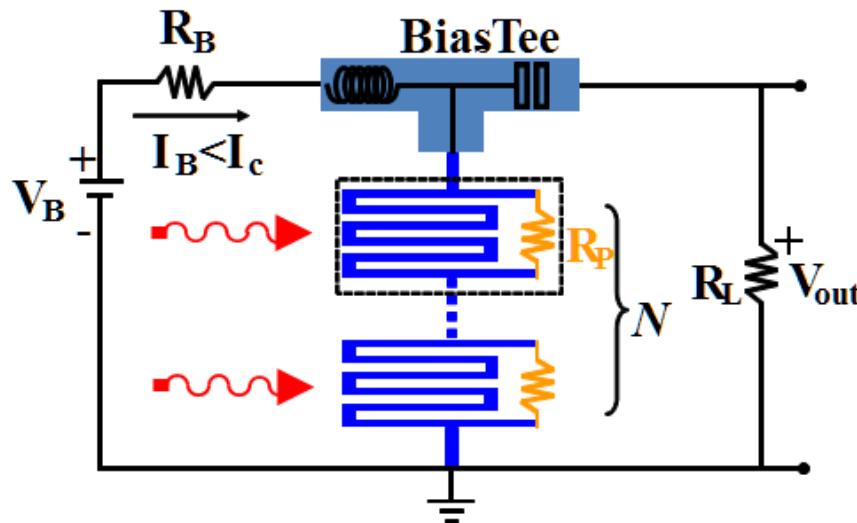


photon number resolving detectors (PNRDs):

- have the sensitivity at level of single photon
- Have an output proportional to the # of incident photons.

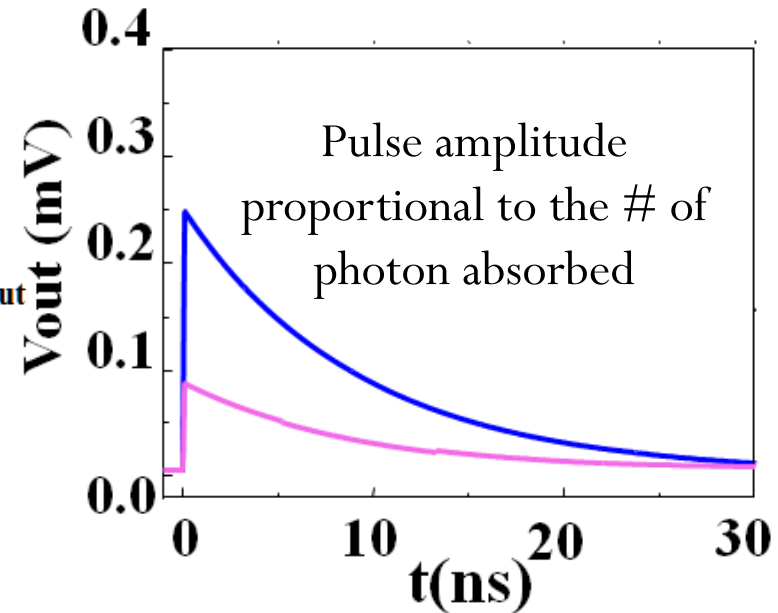
# Photon Number Resolving detectors

- Photon number resolution achieved using the concept of spatial multiplexing.
- The area of the detector is divided in pixels, i.e. smaller meanders with equal resistors in parallel.
- Pixels are connected in series



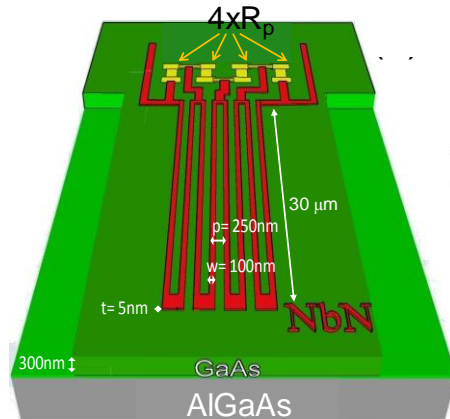
## Series nanowire detector

*Jahanmirinejad et al Opt. Exp. (2012)*

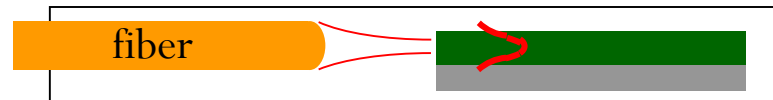




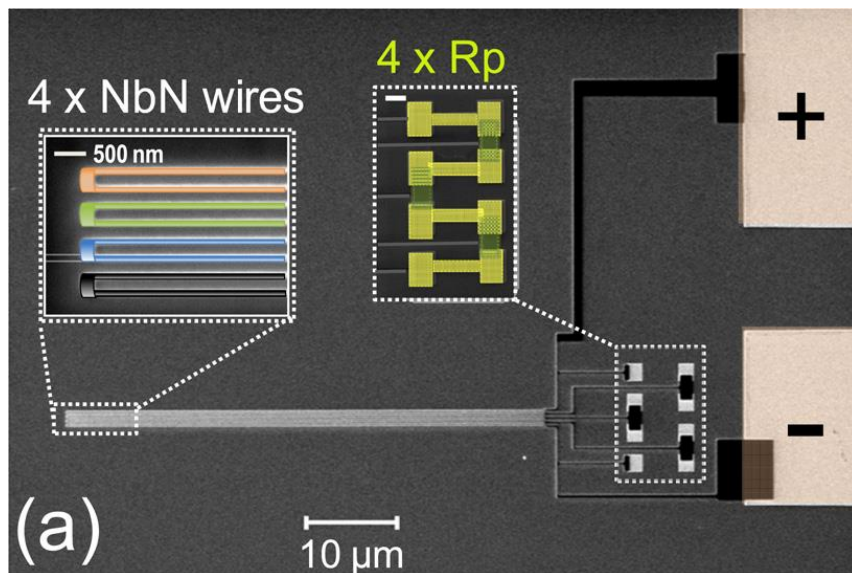
# 4-Pixels Waveguide PNRD: GaAs



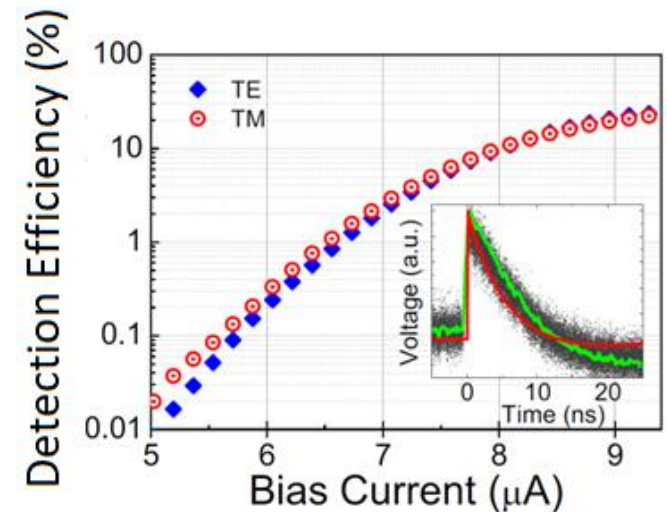
Sahin, Gaggero et al APL (2013)



The nanowires are distinct detecting elements sensing different parts of the same waveguide mode



A. Gaggero, 01/10/2020, Genova



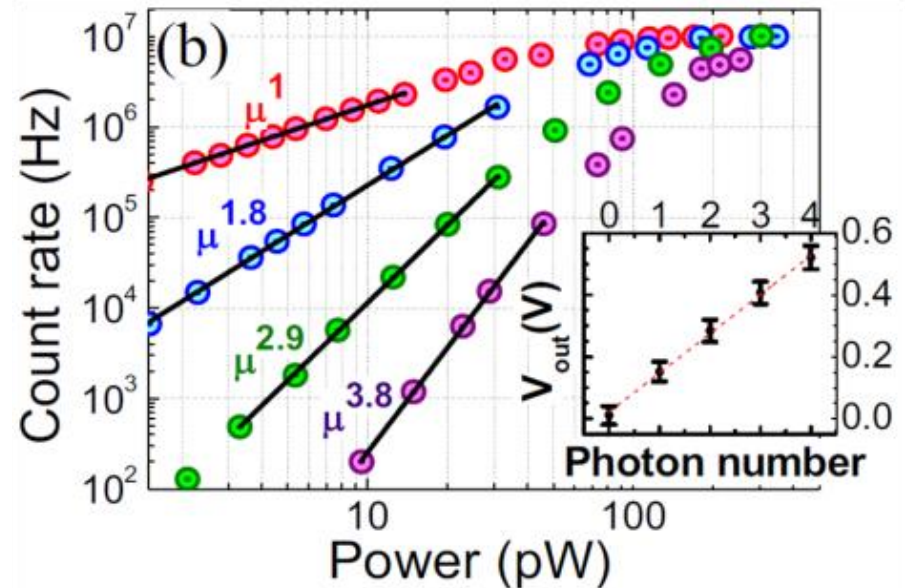
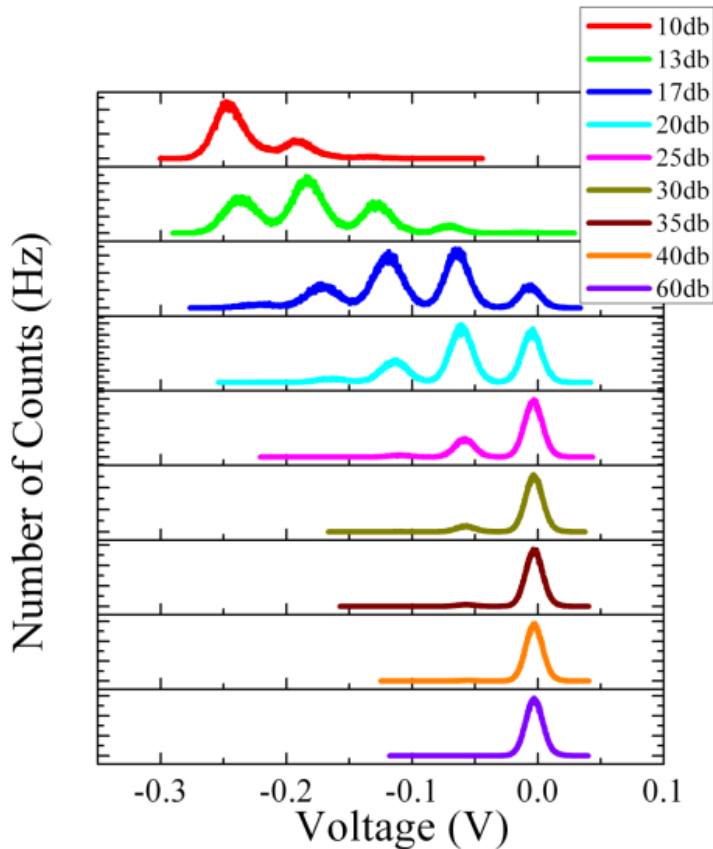
$$DE_{(TM)} = 22\%$$

$$DE_{(TE)} = 24\%$$

$$\lambda = 1300\text{nm};$$

$$T < 4\text{ K}$$

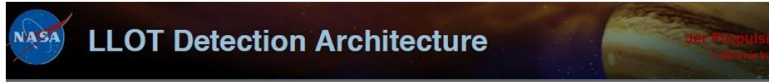
# 4-Pixels Waveguide PNRD: GaAs



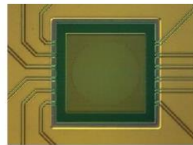
$P(n, \mu) \propto \mu^n$ , for a Poissonian source in the regime, where detected average photon number  $\mu \ll 1$ , as shown by the fits.

# Readout

## DEEP SPACE COMMUNICATIONS



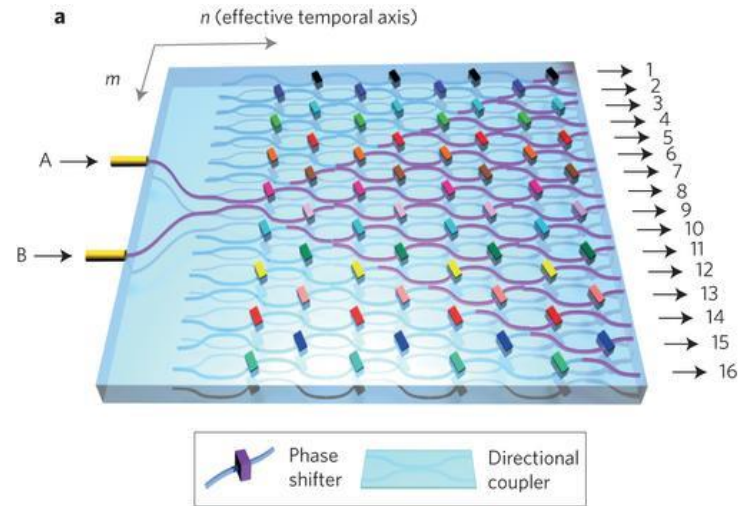
- LLOT (Table Mountain, CA) is a backup ground OCTL terminal for the LLCDC (Lunar Laser Commun. Demonstration)



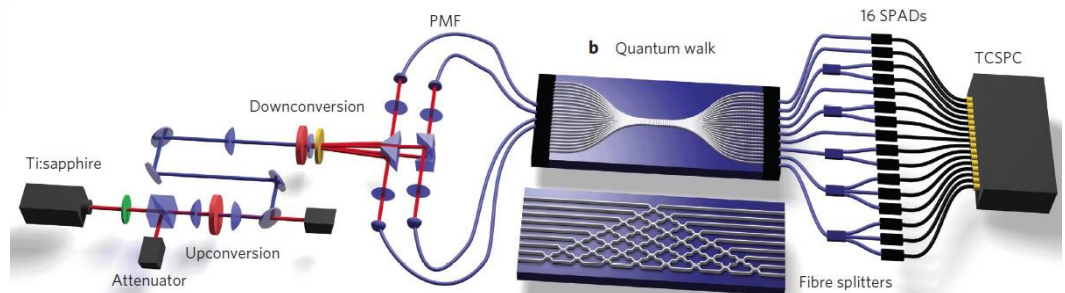
- 12-pixel WSi SNSPD array
- 64- $\mu\text{m}$  diameter active area
- ~40% system detection efficiency
- All channels combined electronically
- signal coupled to GIF-625 multimode)
- Receiver implemented in software

*Proc. SPIE 8971, (2014);  
doi:10.1117/12.2044087*

## INTEGRATED PHOTONIC CIRCUITS.



Crespi et al., Nature Photonics 7, 322 (2013)



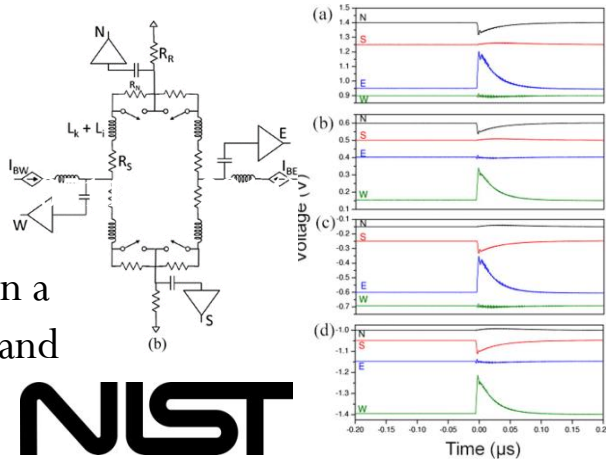
Carolan et al., Nature Photonics 8, 612 (2014)

# Readout

Verma et al.; *Appl. Phys. Lett.*, 104 (2014)

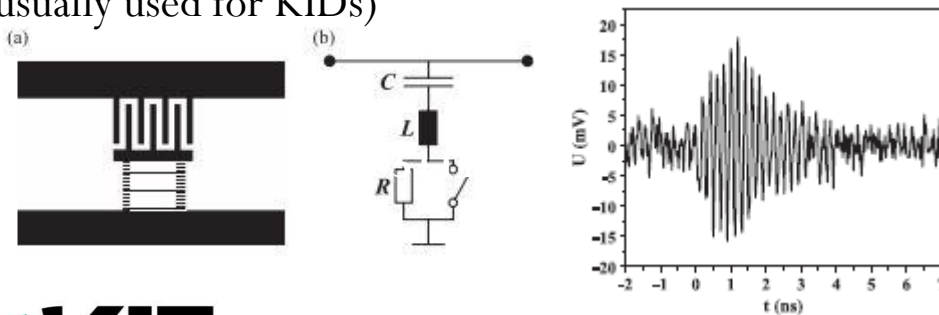
Readout circuit:  
NxN detectors  
2N coaxial cables

Position is encoded in a  
combination of row and  
column pulses



**NIST**

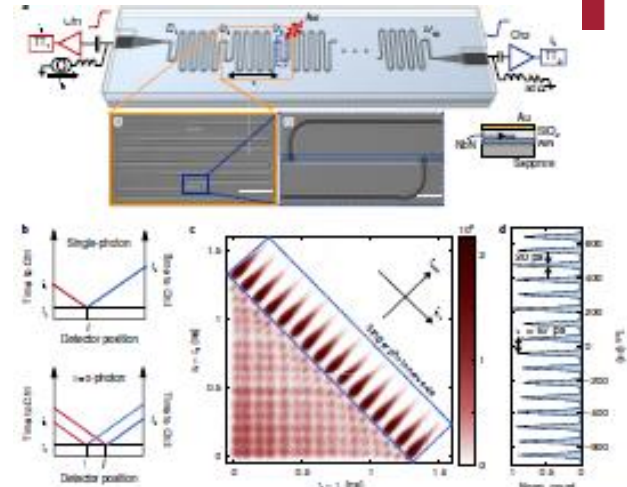
2 coaxial cables: frequency division multiplexing scheme  
(usually used for KIDs)



**KIT**  
Karlsruher Institut für Technologie

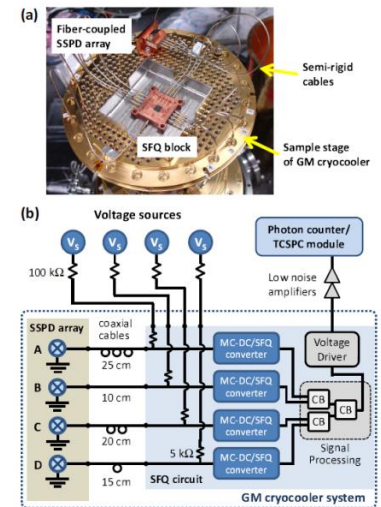
Doerner et al., *Ieee Trans. App. Super.*, 26, (2016)

Zhu et al., *nat. Nanotech.*, 13, 596, (2018)



Low temperature SFQ  
readout electronic

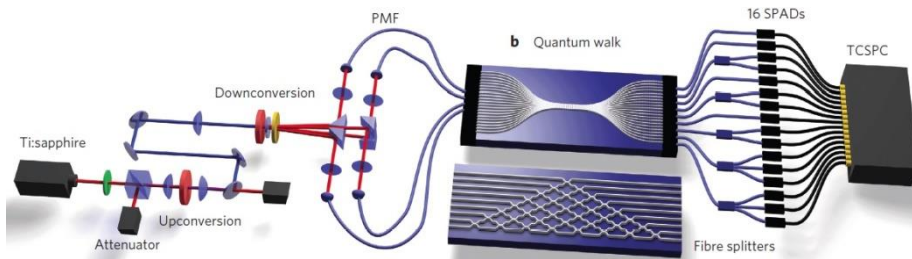
**NICT**



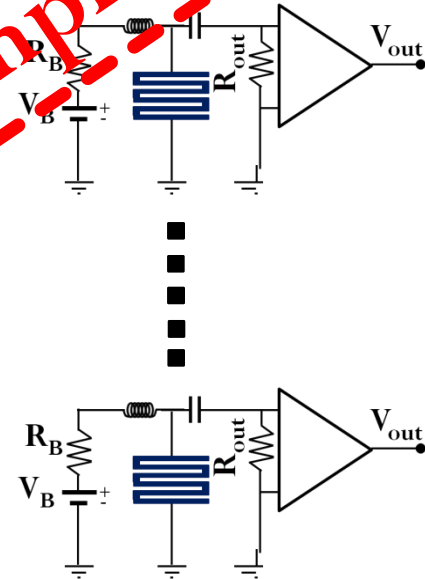
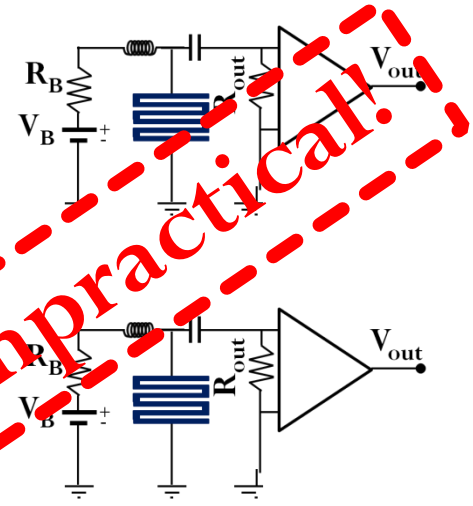
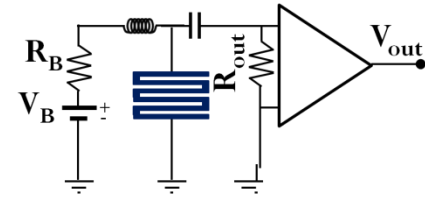
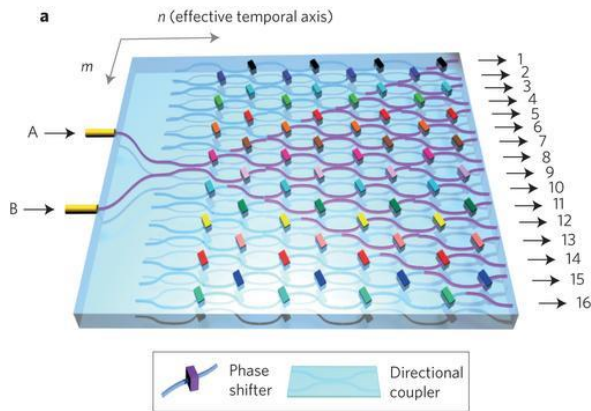
Yamashita et al., *Opt. Lett.*, 37, 2982 (2012)



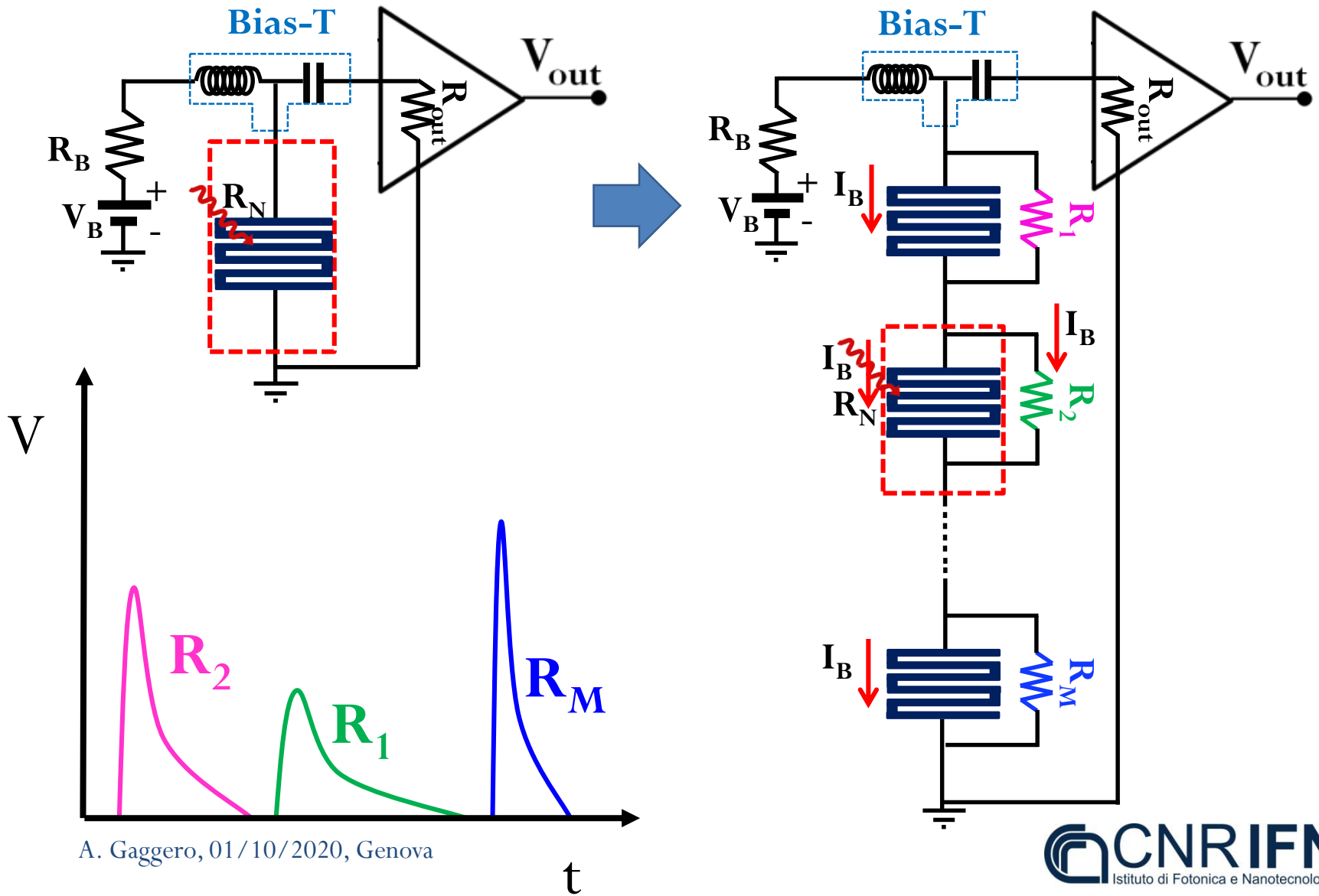
# Readout



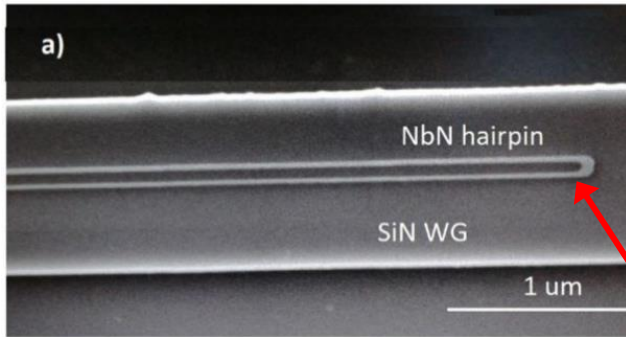
## INTEGRATED PHOTONIC CIRCUITS.



# Amplitude Multiplexing

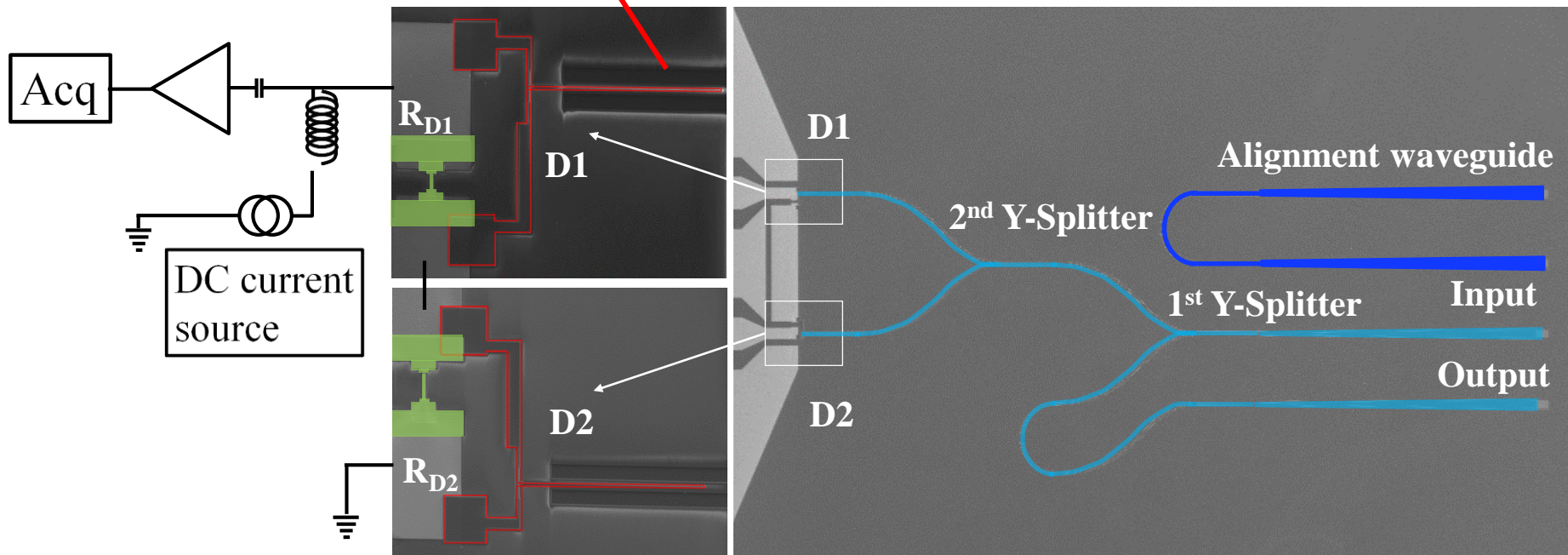


# Integrated array



6 nm thick, 80nm wide NbN nwrs  
350 nm thick and 1.9  $\mu$ m wide  $S_3N_4$  ridge Wg

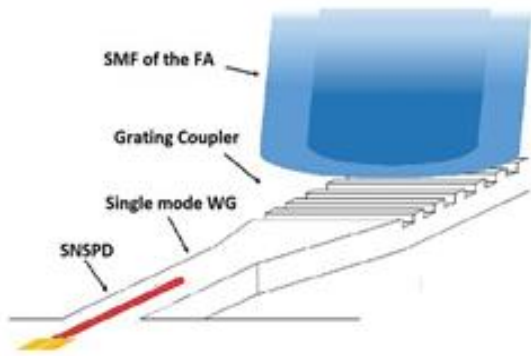
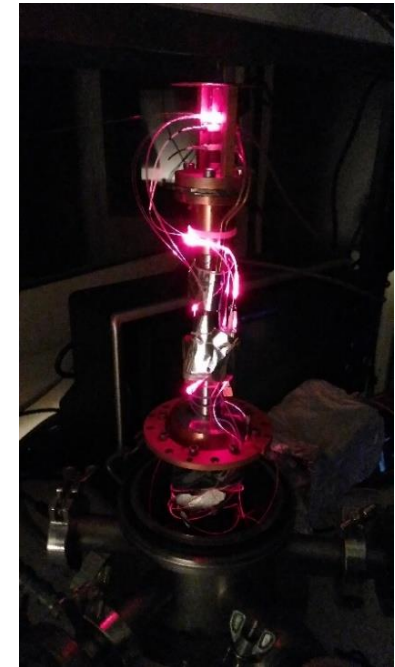
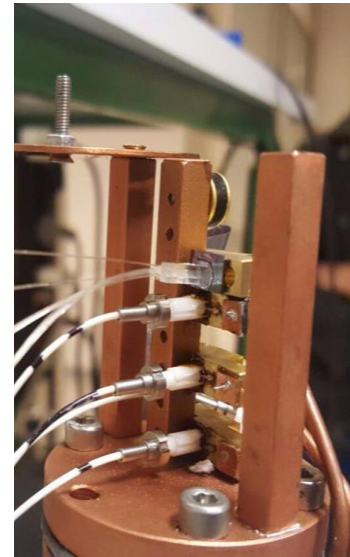
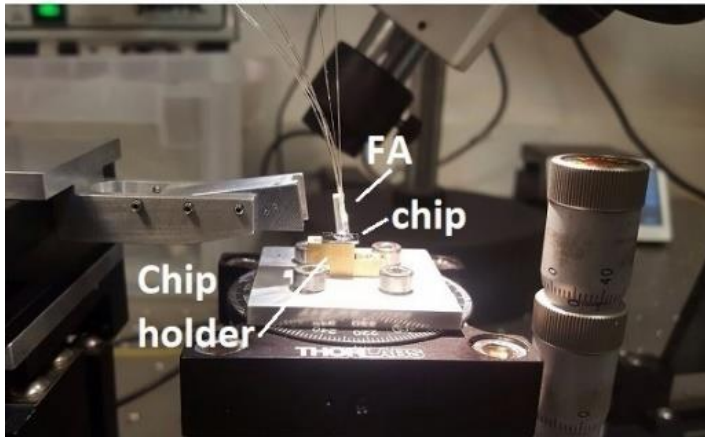
Grating Simulated CE=35% @1530nm @ 300K  
measured CE=10% @1550nm @ 300K



Gaggero et al. Optica (2019)

A. Gaggero, 01/10/2020, Genova

# Set-up



$\lambda = 1.55 \mu\text{m}$   
Cw/pulsed  
laser



Power  
meter

99 %



1 %

variable  
attenuator



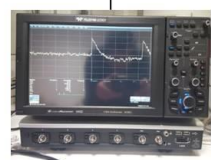
Bias source

DC

Bias T

Rf

DC + Rf



4GHz oscilloscope

Rf Amplifiers



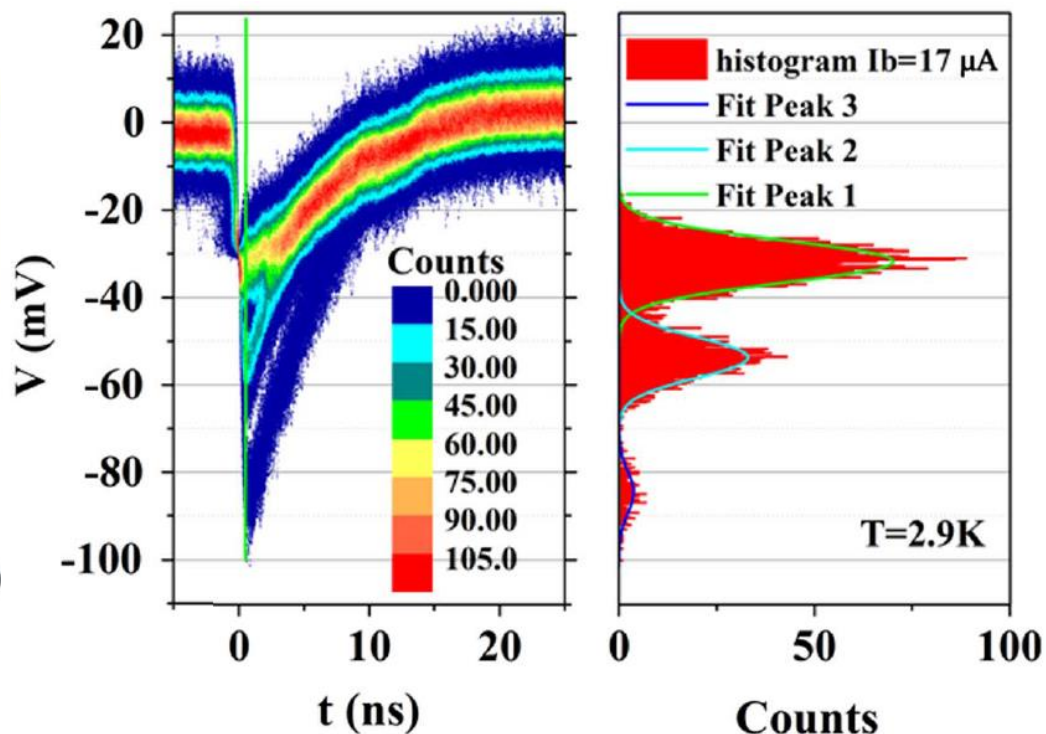
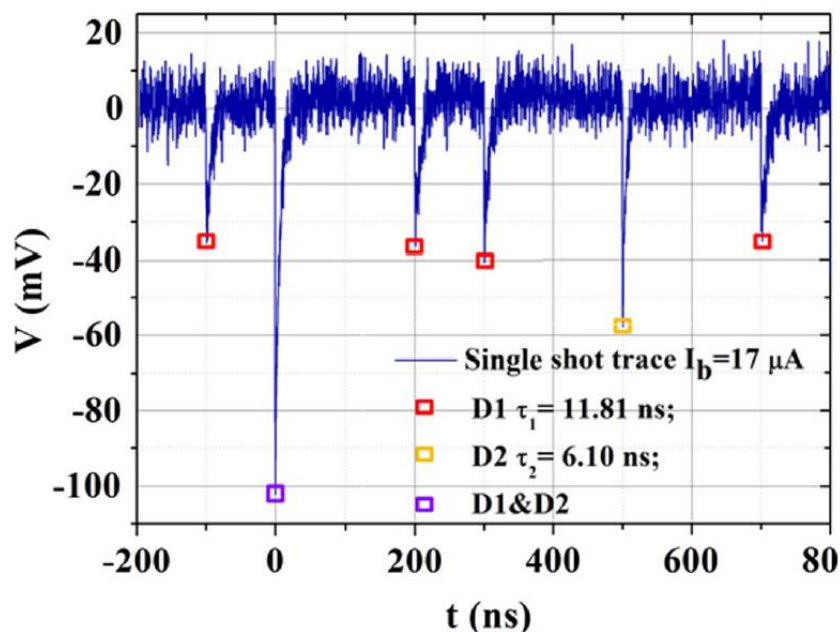
counter 350 MHz



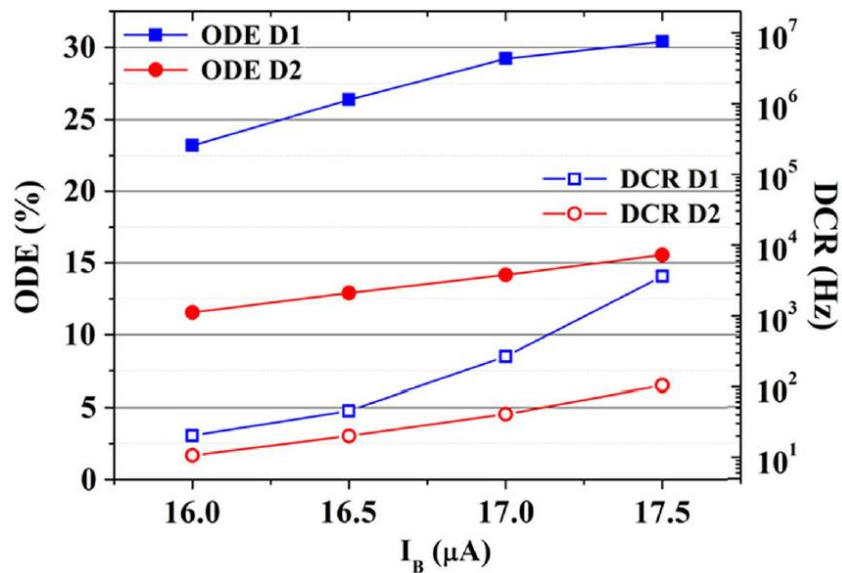
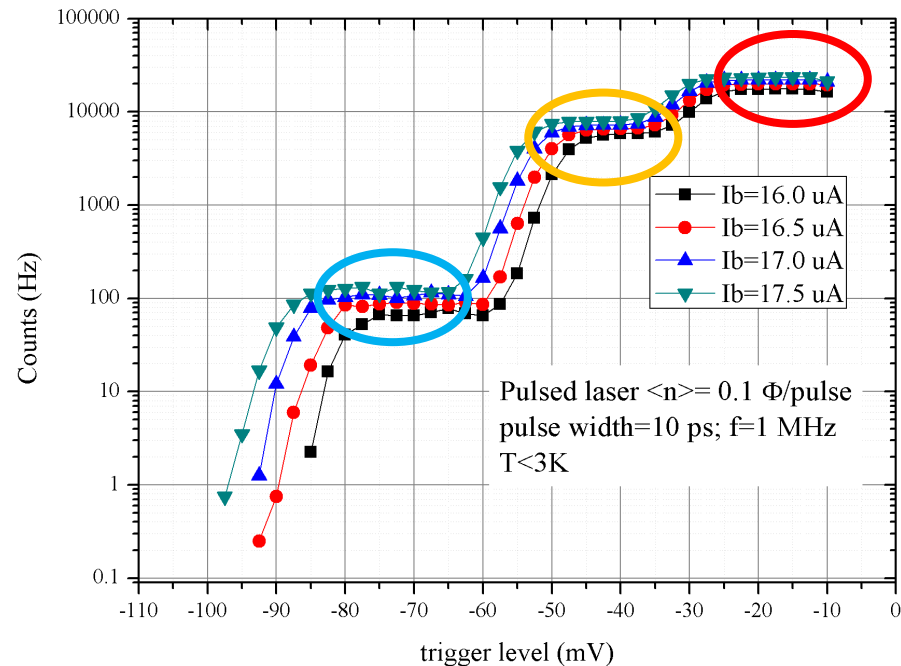
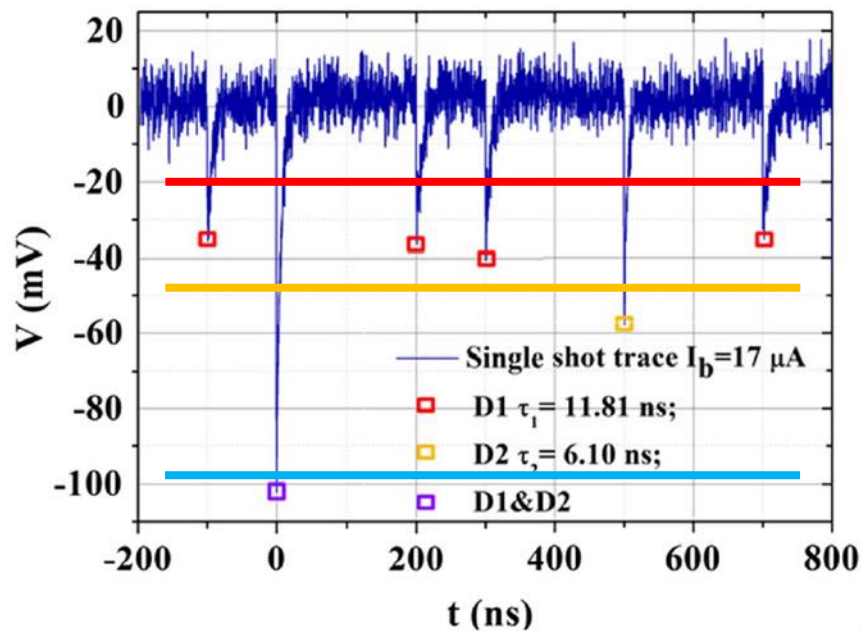


# Optical Characterization @ $T < 3\text{K}$

$\lambda = 1550\text{ nm}$ ,  $f = 1\text{ MHz}$ ,  $\langle n \rangle = 0.1$   
Pulse width 10 ps



# Optical Characterization @ $T < 3K$



$\lambda = 1550 \text{ nm}$ ,  $f = 1 \text{ MHz}$ ,  $\langle n \rangle = 0.1$   
Pulse width 10 ps

$\text{ODE}_{d1} = 30.4 \% @ 4 \text{ kHz DCR}$

$\text{ODE}_{d2} = 15.6 \% @ 100 \text{ Hz DCR}$

# Scalability

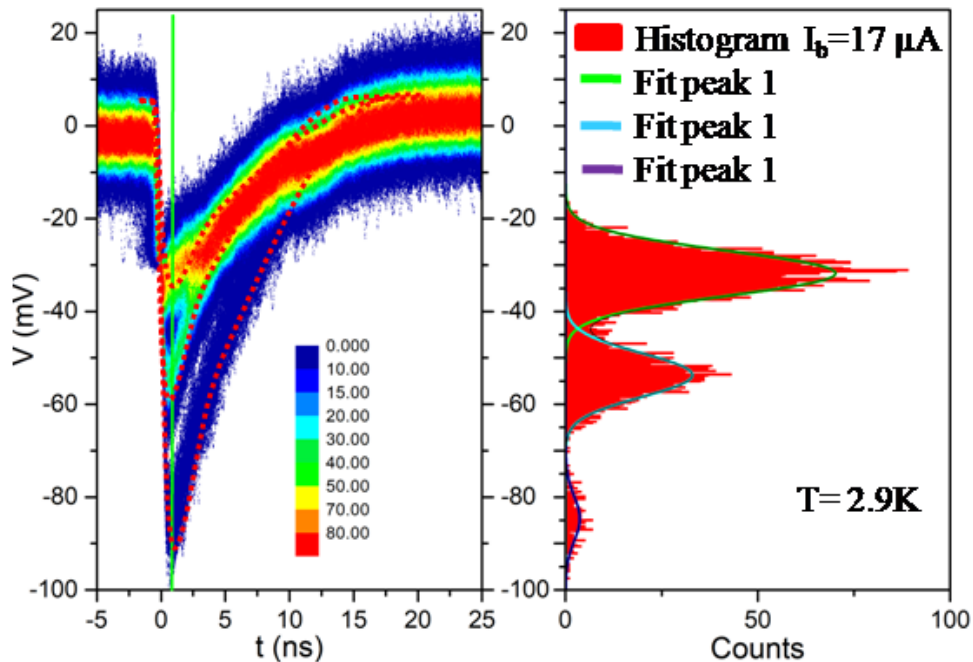
Gain  $\sim$  49 dB @ 500MHz

$V_{\sigma} = 3.7$  mV

$$I_B = 17.0 \mu\text{A} \Rightarrow \Delta R_{2\sigma} = V_{2\sigma} / I_B = 1.6 \Omega$$

$$\Delta R_{6\sigma} = V_{6\sigma} / I_B = 4.7 \Omega$$

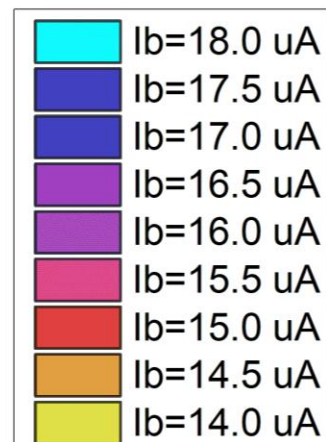
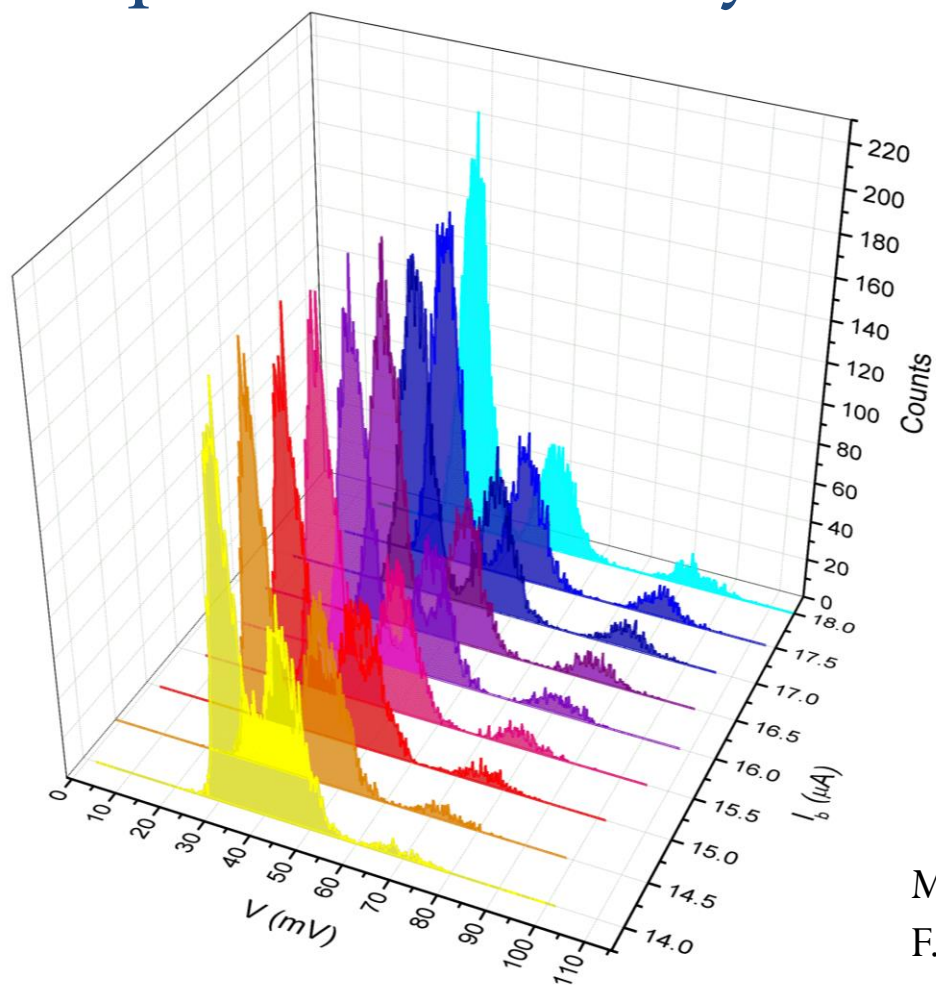
$$V_{th} = (4k_B B T 50 \Omega)^{1/2} = 20.3 \mu\text{V} \Rightarrow \Delta R_{th} = 1.2 \Omega$$



$$Ch_i = R_M / \Delta R_i$$

$R_{in}$ (Ohm)	T (K)	B (MHz)	$\Delta R_{th}$ (Ohm)	$\Delta R_{2\sigma}$ (Ohm)	$\Delta R_{6\sigma}$ (Ohm)	$R_M$ (Ohm)	$Ch_{2\sigma}$	$Ch_{6\sigma}$
50	300	0.1-500	1.2	1.6	4.7	50	30	10

# Prospects: Scalability



Gain  $\sim 49$  dB @ 500MHz

$$V_{\text{th}} = (4k_B T 50\Omega)^{1/2}$$

M Ejrnaes et al. *Appl. Phys. Lett.*, 91 (2007)

F. Marsili et al., *Nano Lett.* 11 (2011)

# Prospects: Cryogenic Amplifier



$$V_{th} = (4k_B B T R_{in})^{1/2}$$

NF @ 20 K: < 0.11 dB, from .0001 to 1.5 GHz

NF @ 300K < 1.5 dB from .0001 to 1.5 GHz

[www.cosmicmicrowavetechnology.com/citlf1](http://www.cosmicmicrowavetechnology.com/citlf1)

$R_{in}$ (Ohm)	T (K)	B (MHz)	$R_{th}$ (Ohm)	$\Delta R_{2\sigma}$ (Ohm)	$\Delta R_{6\sigma}$ (Ohm)	$R_M$ (Ohm)	$Ch_{2\sigma}$	$Ch_{6\sigma}$
50	300	0.1-500	1.2	1.6	4.7	50	30	10
50	20	0.1-500	0.31	0.4	1.2	50	121	41

Thank you for the attention!