

Heavy-Ion Physics (I)



Yen-Jie Lee

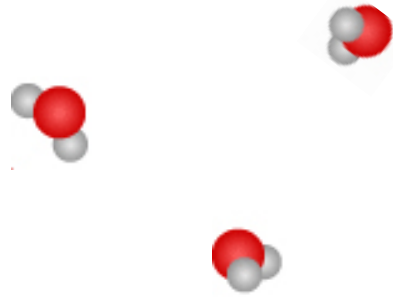
AEPSHEP 2022

Student Lecture
2022 Asia Europe Pacific School of High-Energy Physics
Pyeongchang, South Korea
5-18 October 2022

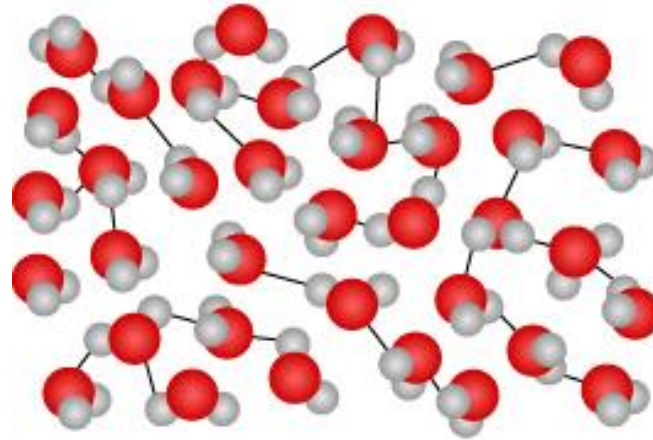


Phases of QED (Electrons and Nuclei) Matter

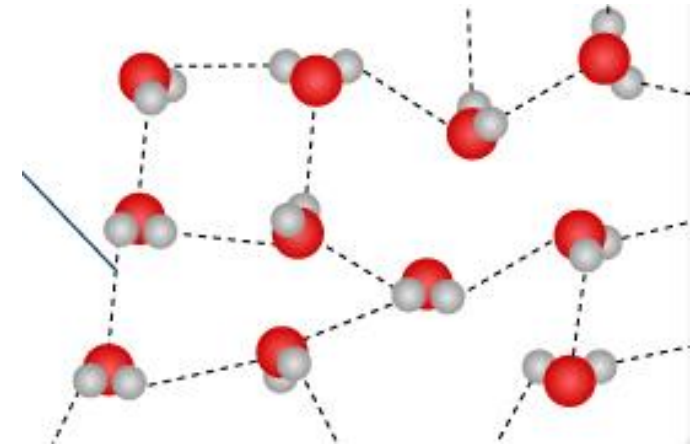
Vapor



Water



Ice



Quantum Chromodynamics

Structure of QCD driven by SU(3) color gauge symmetry

Gluon self-interaction

In principle, all is calculable from the QCD Lagrangian:

$$\mathcal{L}_{QCD} = \sum_{\text{flavours}} \bar{\psi}_a \left((i\gamma^\mu \partial_\mu - m) \delta_{ab} - g_s \gamma^\mu t_{ab}^C A_\mu^C \right) \psi_b - \frac{1}{4} F_{\mu\nu}^A F^{\mu\nu,A}$$

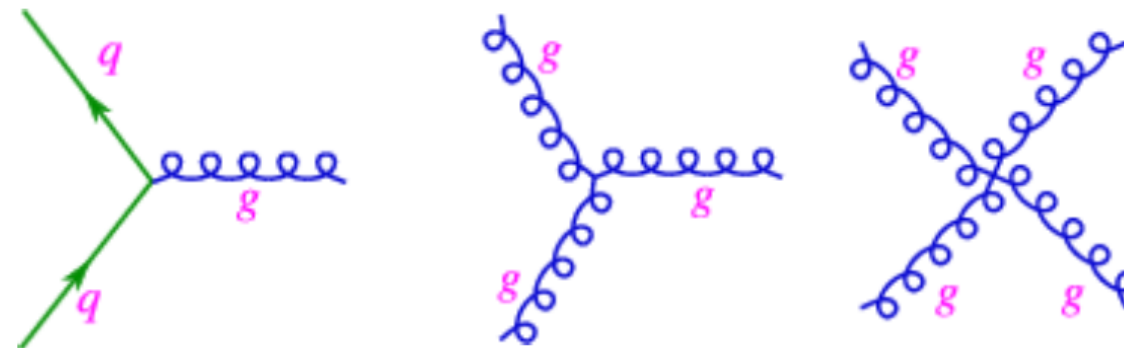
$$F_{\mu\nu}^A = \partial_\mu \mathcal{A}_\nu^A - \partial_\nu \mathcal{A}_\mu^A - g_s f_{ABC} \mathcal{A}_\mu^B \mathcal{A}_\nu^C$$

$$[t^A, t^B] = i f_{ABC} t^C$$

Quark propagator

Quark-gluon vertex

Field strength tensor



$$N_c^2 - 1 = 8 \text{ gluons}$$

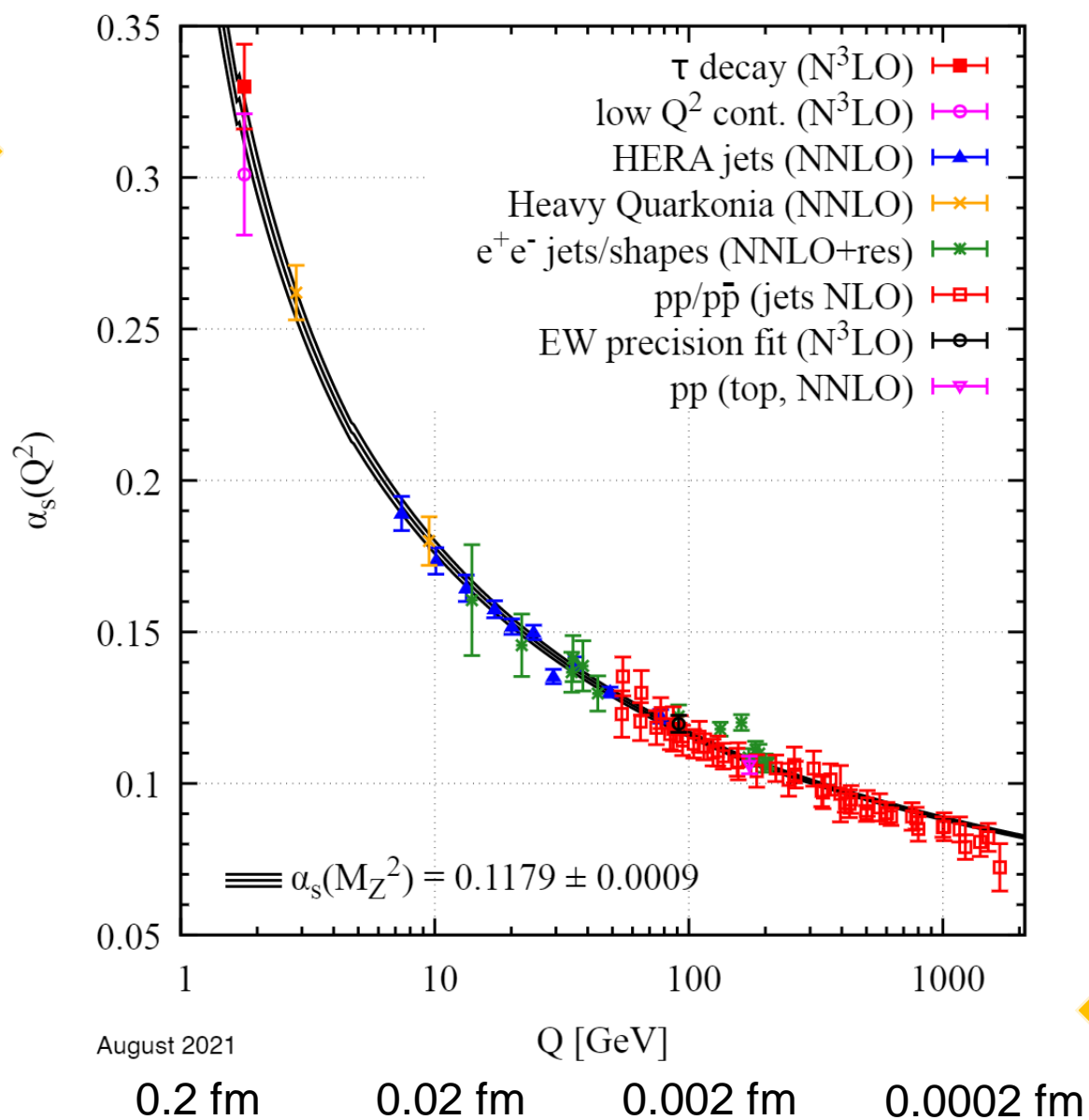
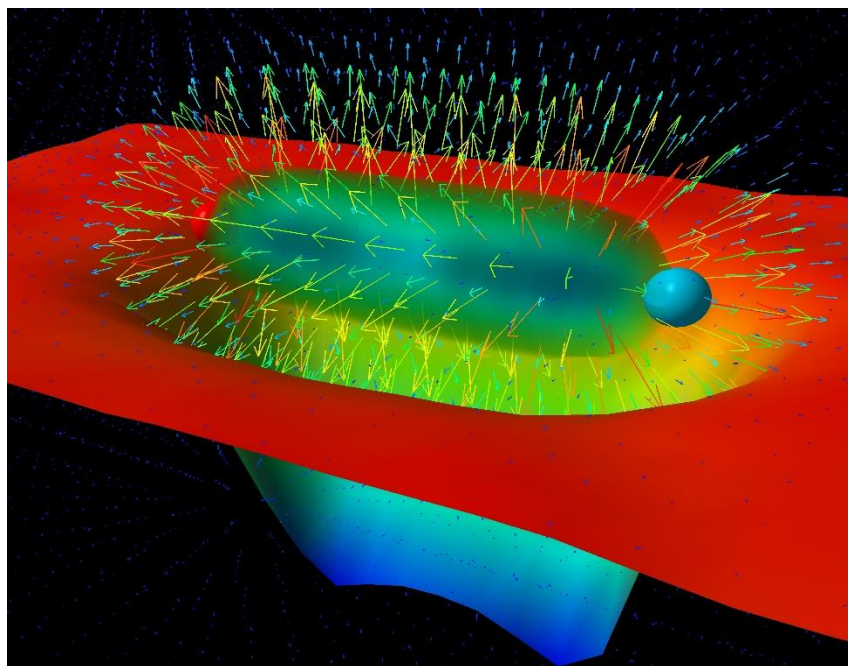
$$N_c * N_f \text{ quarks}$$

Quark masses

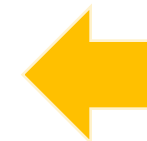
charge=+2/3	u (~5 MeV)	c (~1.5 GeV)	t (~175 GeV)
charge=-1/3	d (~10 MeV)	s (~100 MeV)	b (~5 GeV)

QCD Running Coupling α_s

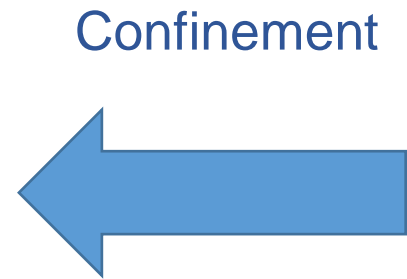
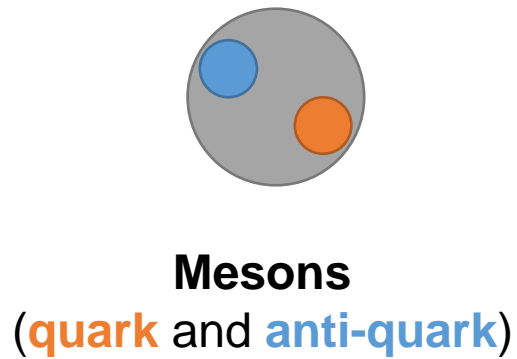
Strong coupling
Confinement
Infrared slavery
Non-perturbative



Weak coupling
Asymptotic freedom
Perturbative



Quarks and Hadrons



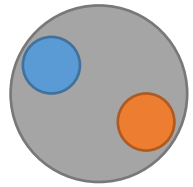
	I	II	III
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	u up	C charm	t top
	d down	S strange	b beauty
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$

QUARKS

When the quarks form a hadron, the total color charge needs to be neutral

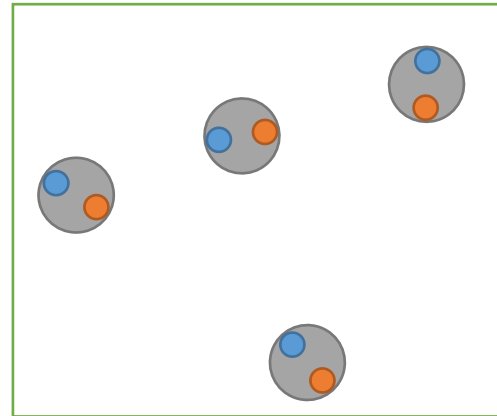
Ultra-dense QCD (Quarks and Gluons) Matter

Increase the Temperature (T)

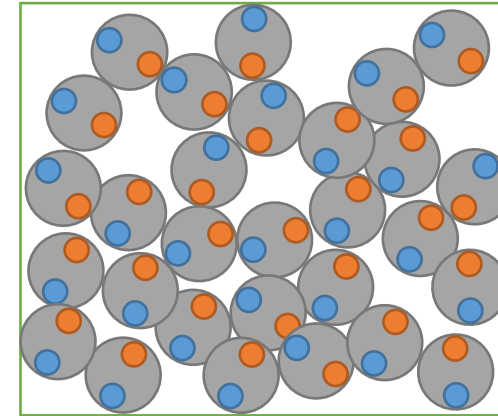


Mesons

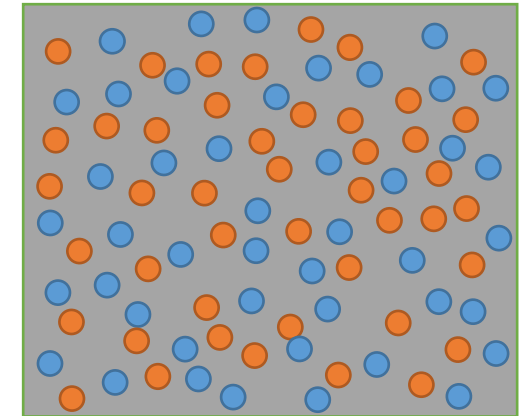
(**quark** and **anti-quark**)



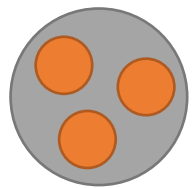
$T < T_c$



$T \sim T_c \sim 2$ trillion degrees



$T > T_c$



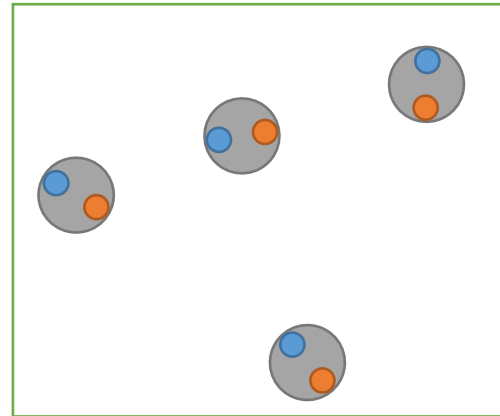
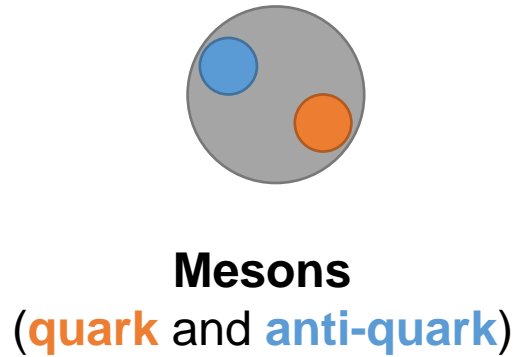
Baryons

(Three **quarks**)

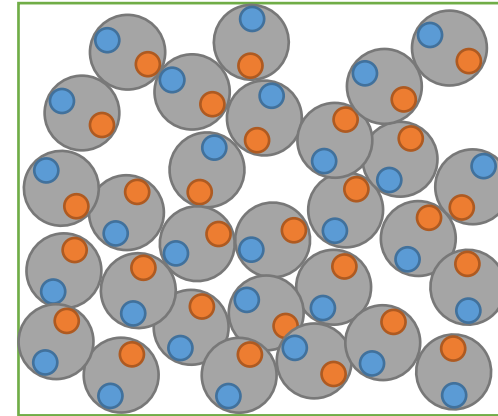
- Quark
- Anti-quark

Ultra-dense QCD (Quarks and Gluons) Matter

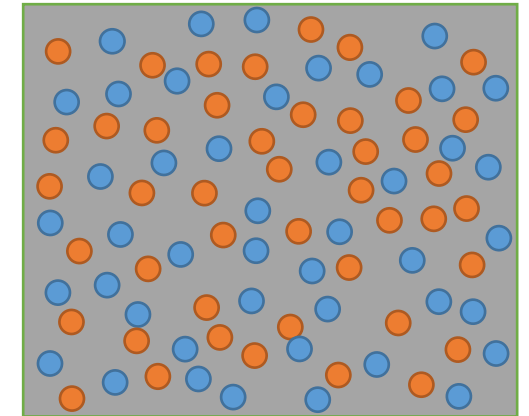
Increase the Temperature (T)



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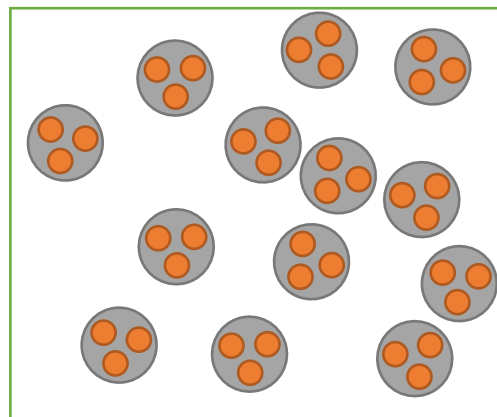
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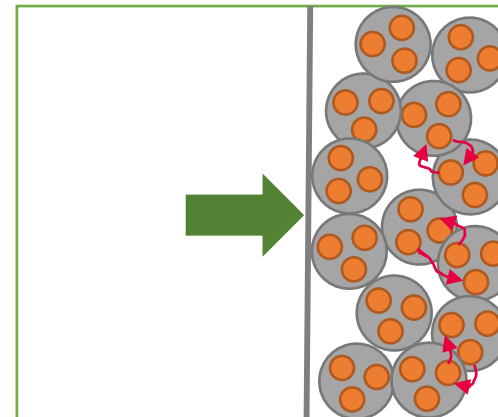
$T > T_c$

● Quark
● Anti-quark

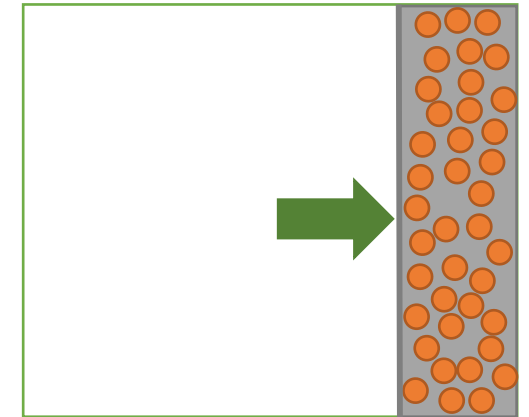
Increase the Density (ρ)



$\rho < \rho_c$



$\rho \sim \rho_c \sim (2 \text{ to } 12) \times$ nuclei density



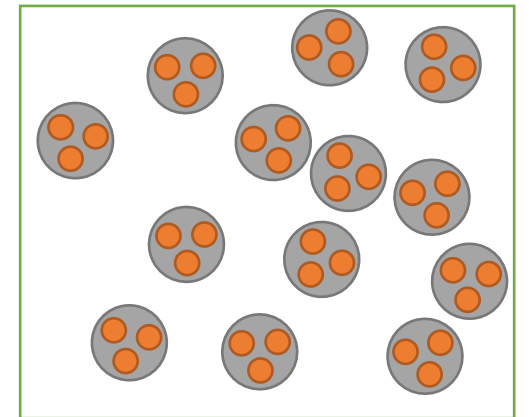
$\rho > \rho_c$

Rough Estimation of the Critical Density

- Normal nuclear matter
 - Baryon density

$$\rho_0 = \frac{A}{\frac{4}{3}\pi R^3} = \frac{1}{\frac{4}{3}\pi r_0^3} \approx 0.16/\text{fm}^3$$

$$r_0 \equiv \frac{R}{A^{1/3}} \approx 1.15 \text{ fm}$$



Proton Charge Radius: Nature volume 575, pages147–150 (2019)

Rough Estimation of the Critical Density

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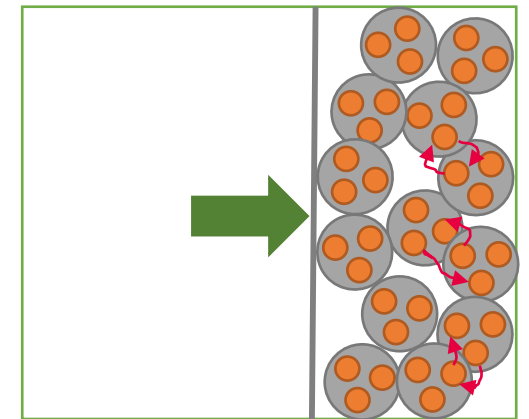
- Compressed nuclei: nucleons start to overlap!

$$r_p = 0.84 \text{ fm}$$

Rough estimation of critical density:

$$\rho_c = \frac{1}{\frac{4}{3}\pi r_p^3} \approx 0.4/\text{fm}^3$$

→ At least a few times of the normal nuclear matter density



Proton Charge Radius: Nature volume 575, pages147–150 (2019)

Reminder: Thermodynamics

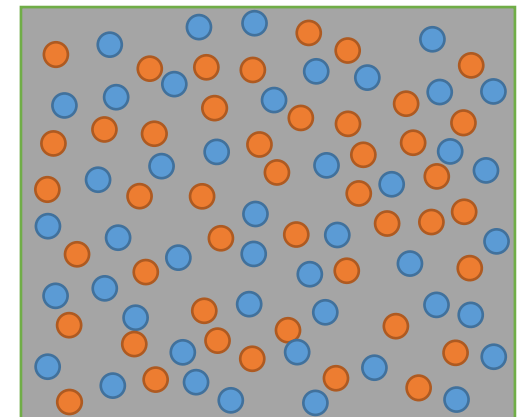
- **At high temperature limit:**

QGP as an ideal gas of non-interacting quarks and gluons

- Probability density:
$$N(E) = \frac{D}{(2\pi)^3} \frac{1}{e^{\frac{E-\mu}{T}} \pm 1}$$
 where $\begin{cases} + & \text{for Fermion} \\ - & \text{for Boson} \end{cases}$

With degeneracy D , chemical potential μ , energy E , and $\hbar = c = k_B = 1$

- Quark
- Anti-quark



Relativistic Bose Gas

- **At high temperature limit:**

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With degeneracy D , chemical potential μ , energy E , and $\hbar = c = k_B = 1$

- For a relativistic Bose gas, neglecting the chemical potential ($\mu=0$)

- Energy density:
$$\epsilon = \int N(E) p d^3 p = \frac{4\pi D}{(2\pi)^3} \int \frac{p^3 dp}{e^{\frac{p}{T}} - 1}$$

Relativistic Bose Gas

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With degeneracy D , chemical potential μ , energy E , and $\hbar = c = k_B = 1$

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- Energy density:
$$\epsilon = \int N(E) p d^3 p = \frac{4\pi D}{(2\pi)^3} \int \frac{p^3 dp}{e^{\frac{p}{T}} - 1}$$

$$\rightarrow \epsilon = \frac{3D}{\pi^2} T^4 \zeta(4) = \frac{\pi^2 D}{30} T^4$$

$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s} = \frac{1}{\Gamma(s)} \int_0^{\infty} \frac{x^{s-1}}{e^x - 1} dx,$$

where

$$\Gamma(s) = \int_0^{\infty} x^{s-1} e^{-x} dx$$

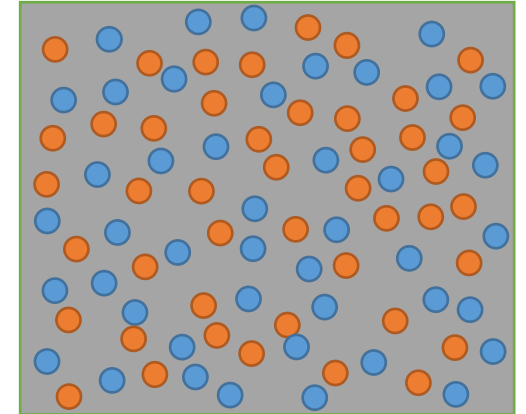
Relativistic Bose Gas

Bose gas energy density

$$\epsilon = \frac{\pi^2 D}{30} T^4$$

Pressure

$$P = \frac{1}{3} \epsilon = \frac{\pi^2 D}{90} T^4$$



Relativistic Bose Gas

Bose gas energy density

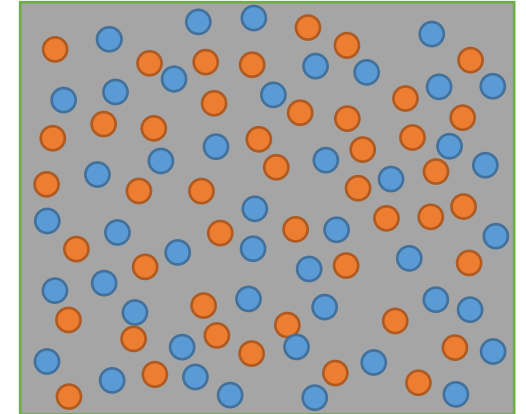
$$\epsilon = \frac{\pi^2 D}{30} T^4$$

Pressure

$$P = \frac{1}{3} \epsilon = \frac{\pi^2 D}{90} T^4$$

Entropy density

$$ds = \frac{d\epsilon}{T} = \frac{\pi^2 D}{30} \cdot \frac{4T^3 dT}{T} = \frac{4\pi^2 D}{30} \cdot T^2 dT$$



$$s = \int ds = \frac{4\pi^2 D}{30} \int T^2 dT \quad \rightarrow$$

$$s = \frac{4\pi^2 D}{90} T^3$$

$$s = \frac{4}{3} \frac{\epsilon}{T}$$

Relativistic Bose Gas

Bose gas energy density

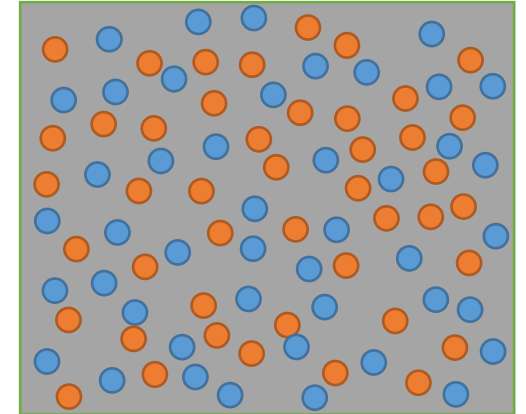
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$$s = \int ds = \frac{4\pi^2 D}{30} \int T^2 dT \rightarrow$$

$$s = \frac{4\pi^2 D}{90} T^3$$

$$s = \frac{4}{3} \frac{\epsilon}{T}$$

Number Density

$$\rho_N = \int N(E) d^3 p = \frac{D}{\pi^2} T^3 \zeta(3) \approx 0.12 D T^3$$

Exercise with Fermi Gas

$$\epsilon_f = \frac{7}{8} \epsilon_b$$

What Have We Learned So Far?

Bose gas energy density: $\epsilon = \frac{\pi^2 D}{30} T^4$

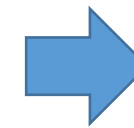
Bose gas pressure $P = \frac{\pi^2 D}{90} T^4$

Bose gas entropy density $s = \frac{4\pi^2 D}{90} T^3$

Fermi Gas $\epsilon_f = \frac{7}{8} \epsilon_b$

$$P = \frac{1}{3} \epsilon$$

$$s = \frac{4}{3} \frac{\epsilon}{T}$$



Speed of sound c_s

$$c_s^2 = \frac{dP}{d\rho} = \frac{dP}{d\epsilon} = \frac{1}{3}$$

$$c_s \approx 0.58$$

- Energy density and pressure increases very quickly with temperature! (T^4)
- Proportional to number of degrees of freedom (degeneracy D)
- Similar dependence between Bose and Fermi gas except for a scale factor (**7/8**)!
- Speed of sound is around 0.58 c

Number of Degree of Freedom (D) for Hadron Gas

Hadron Gas:

- Suppose we focus on $T < 400$ MeV, it is a gas of pions
- **D = 3** for π^+ , π^- and π^0 $\Rightarrow \epsilon = 3 \times \frac{\pi^2}{30} T^4$



Number of Degree of Freedom (D) for QGP

Hadron Gas:

- Suppose we focus on $T < 400$ MeV, it is a gas of pions

- **D = 3** for π^+ , π^- and π^0 $\rightarrow \epsilon = 3 \times \frac{\pi^2}{30} T^4$

Non-interacting **Quark and Gluon** gas:

- Number of Gluons (Boson): **D_g** = 2_(spin) × 8_(color) = 16

- Number of Quarks (Fermion):

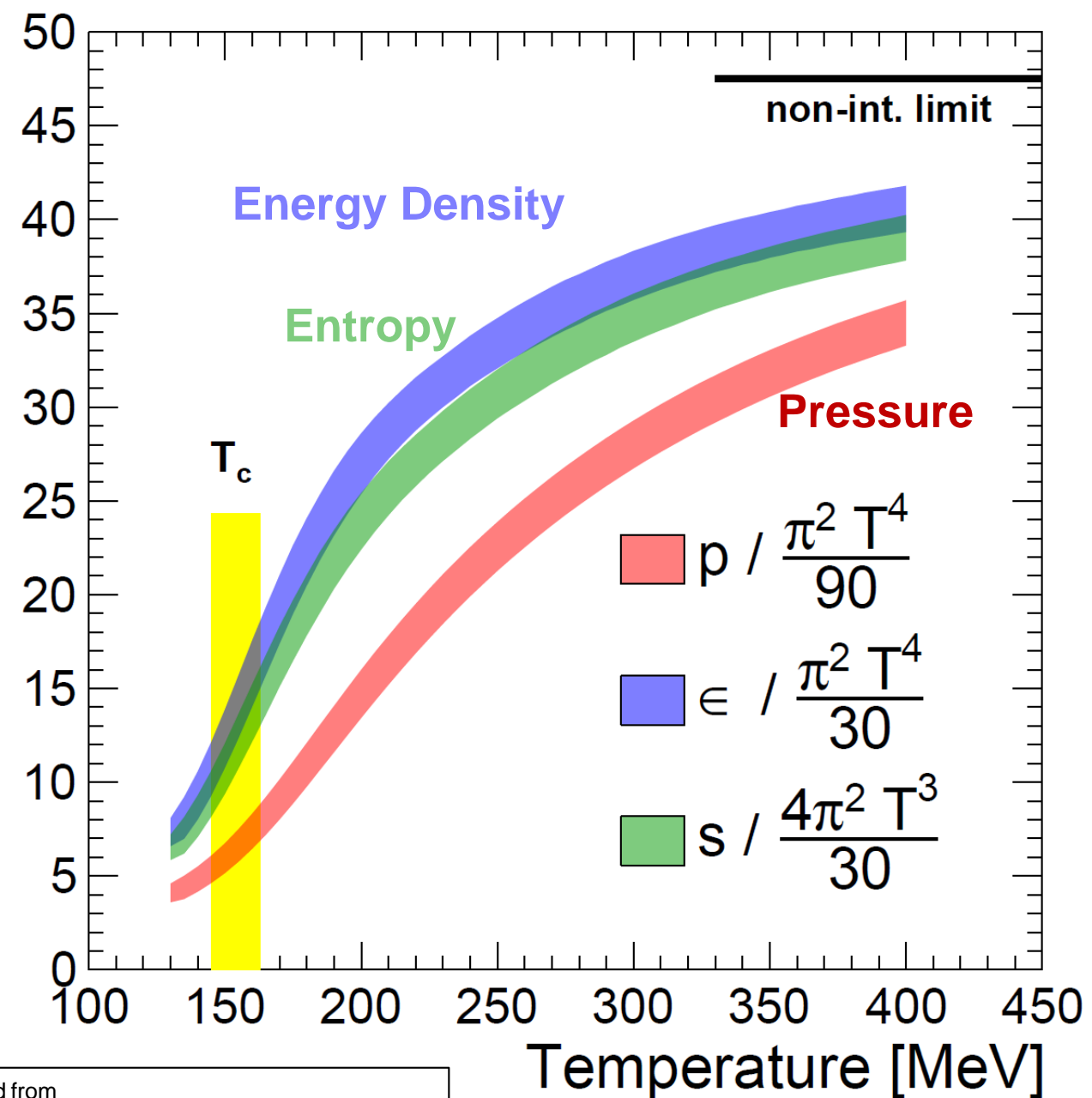
$$\mathbf{D}_q = 2_{(\text{spin})} \times 2_{(\text{particle/anti-particle})} \times 3_{(\text{color})} \times 3_{(\text{flavor } u,d,s)} = 36$$

$$\rightarrow \epsilon = \left(16 + \frac{7}{8} \times 36\right) \times \frac{\pi^2}{30} T^4 = 47.5 \times \frac{\pi^2}{30} T^4$$

16x jump in
energy density!!!

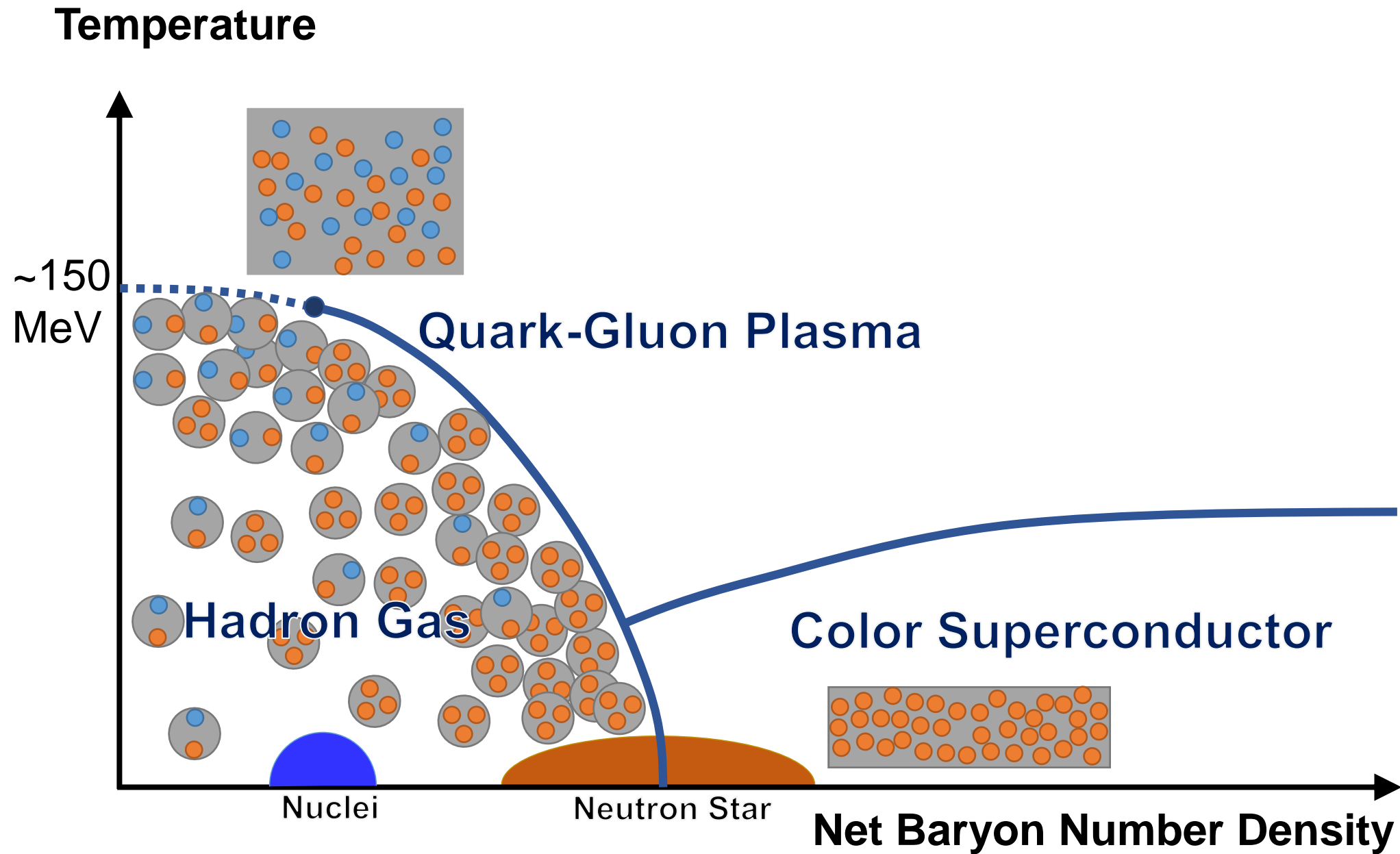
Lattice QCD Equation of State

- Solve the QCD equation of state on a discrete space-time lattice
- Reliable for zero net baryon density!
- Indeed, we see a rapid increase in the degrees of freedom!!!
- Predicts a speed of sound $c_s \approx 0.4 - 0.55$



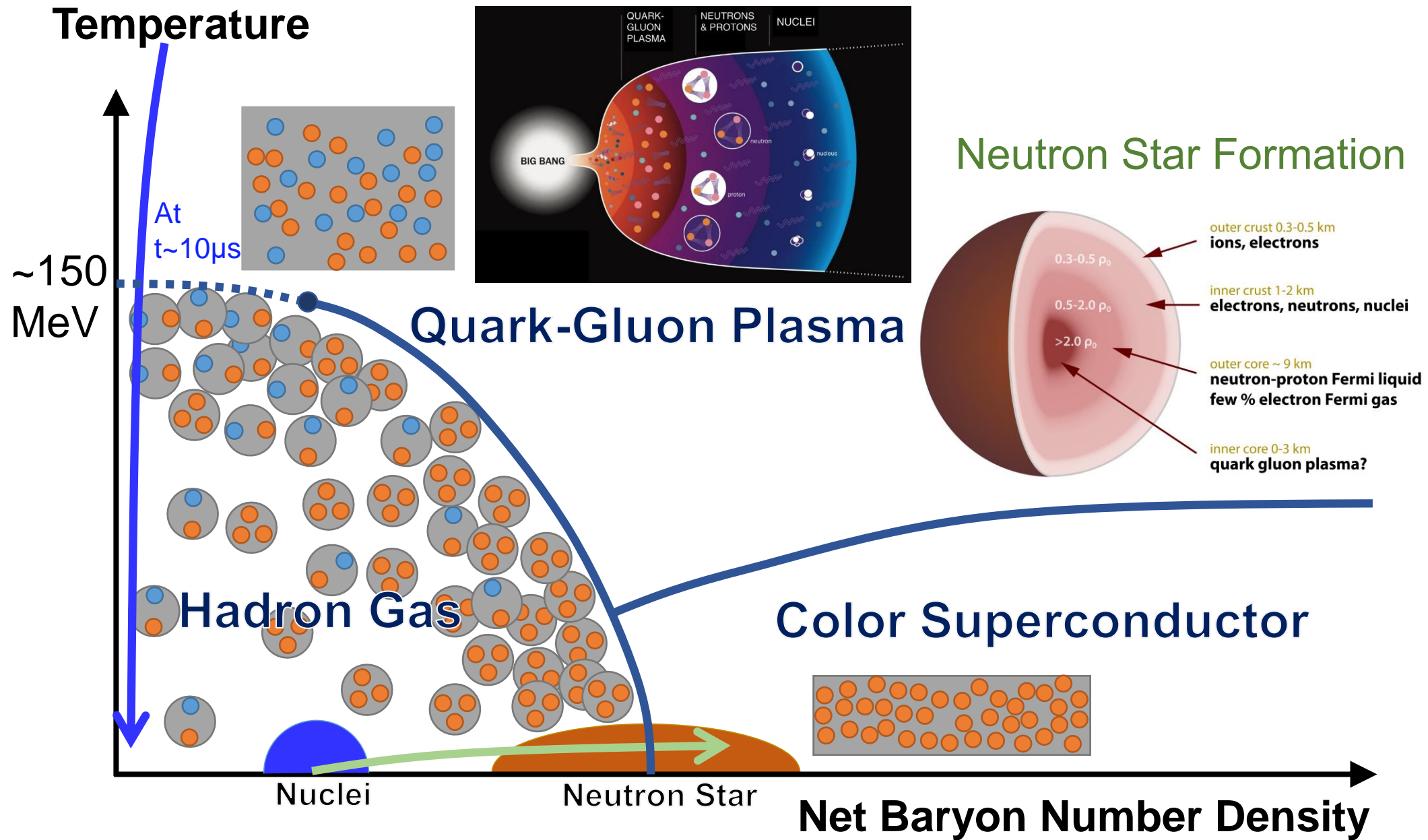
Replotted from
HotQCD Collaboration PRD90 (2014) 094503

QCD Phase Diagram

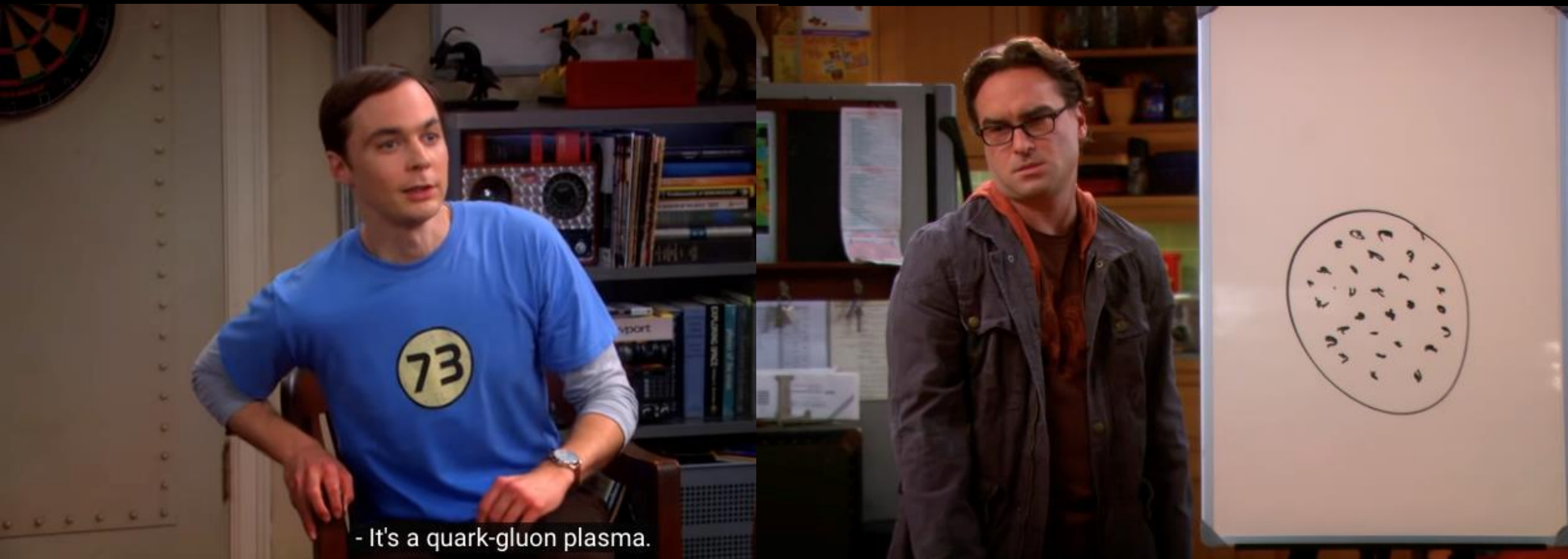


QCD Phase Diagram

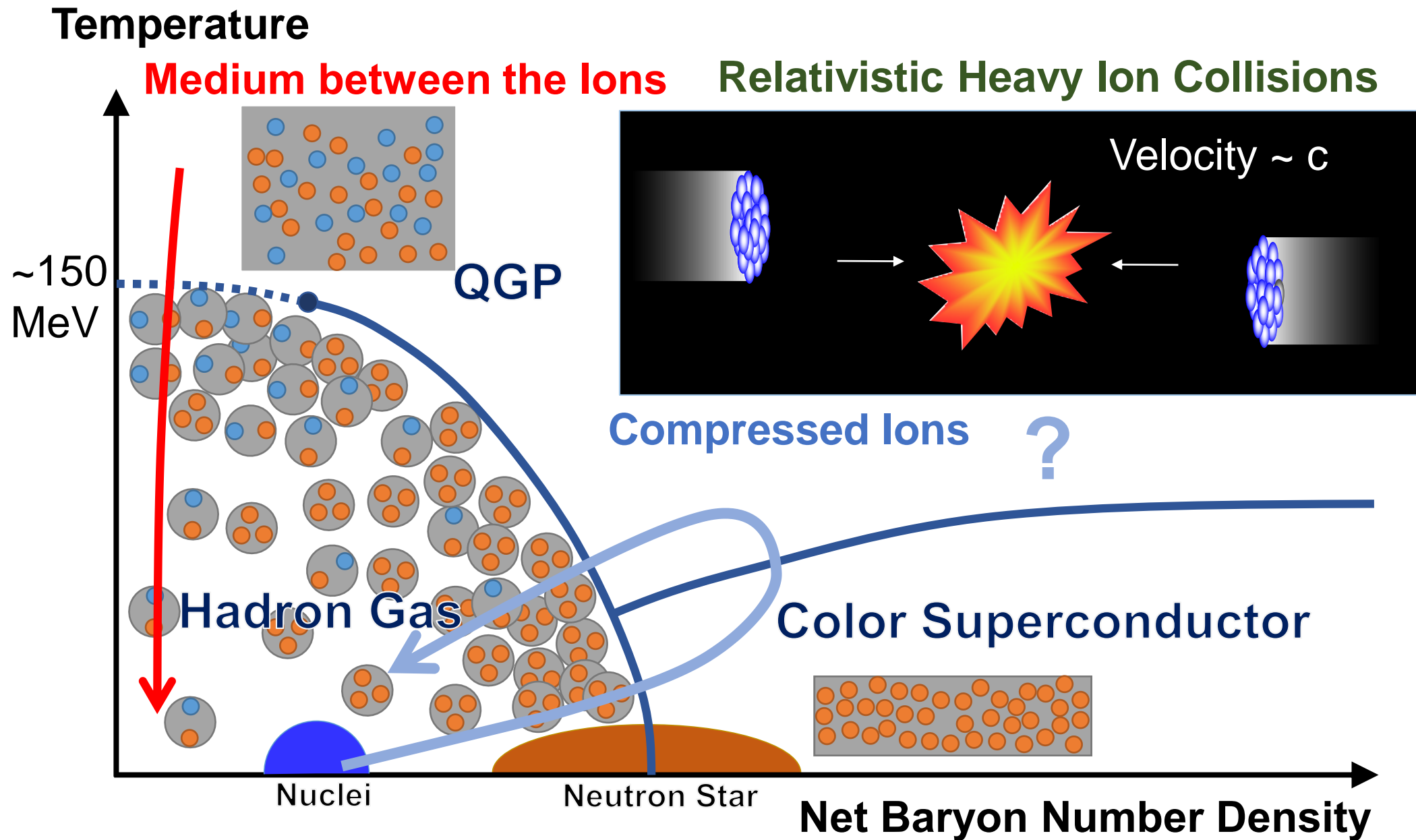
Expansion of Early Universe



How Do We Generate Quark-Gluon Plasma in a Lab?



QCD Phase Diagram



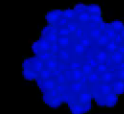
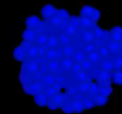
Relativistic Heavy Ion Collisions (Simulation)

MIT Heavy Ion Event Display: Pb+Pb 5.02 TeV

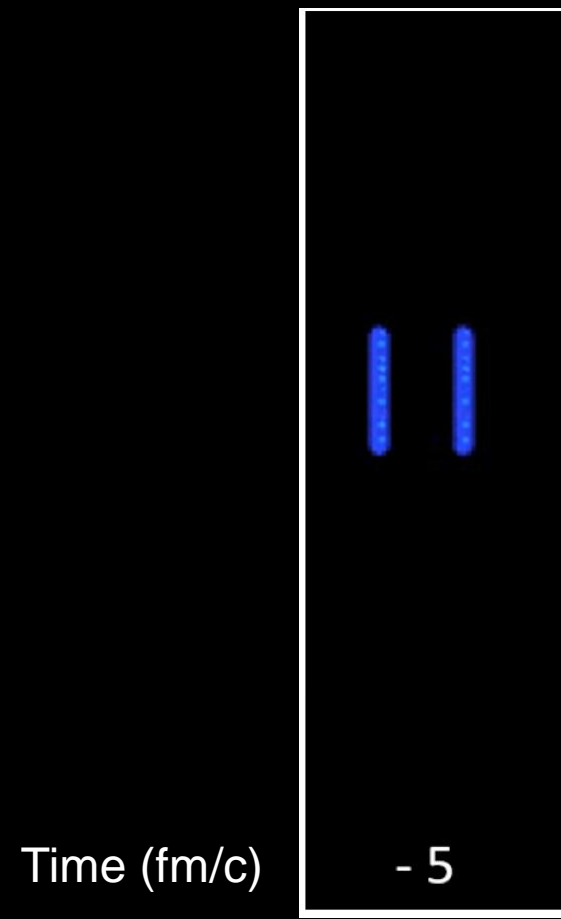
 **Quark Gluon Plasma**

 **Baryons** 

 **Mesons** 



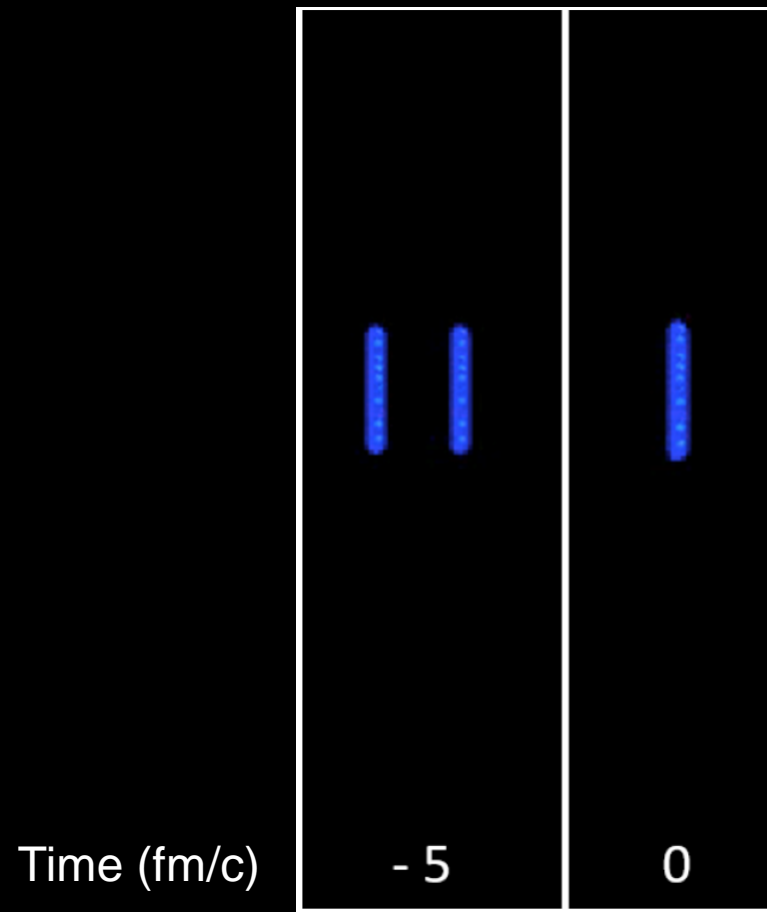
Relativistic Heavy Ion Collisions



Two discs of almost real quarks and gluons

Relativistic Heavy Ion Collisions

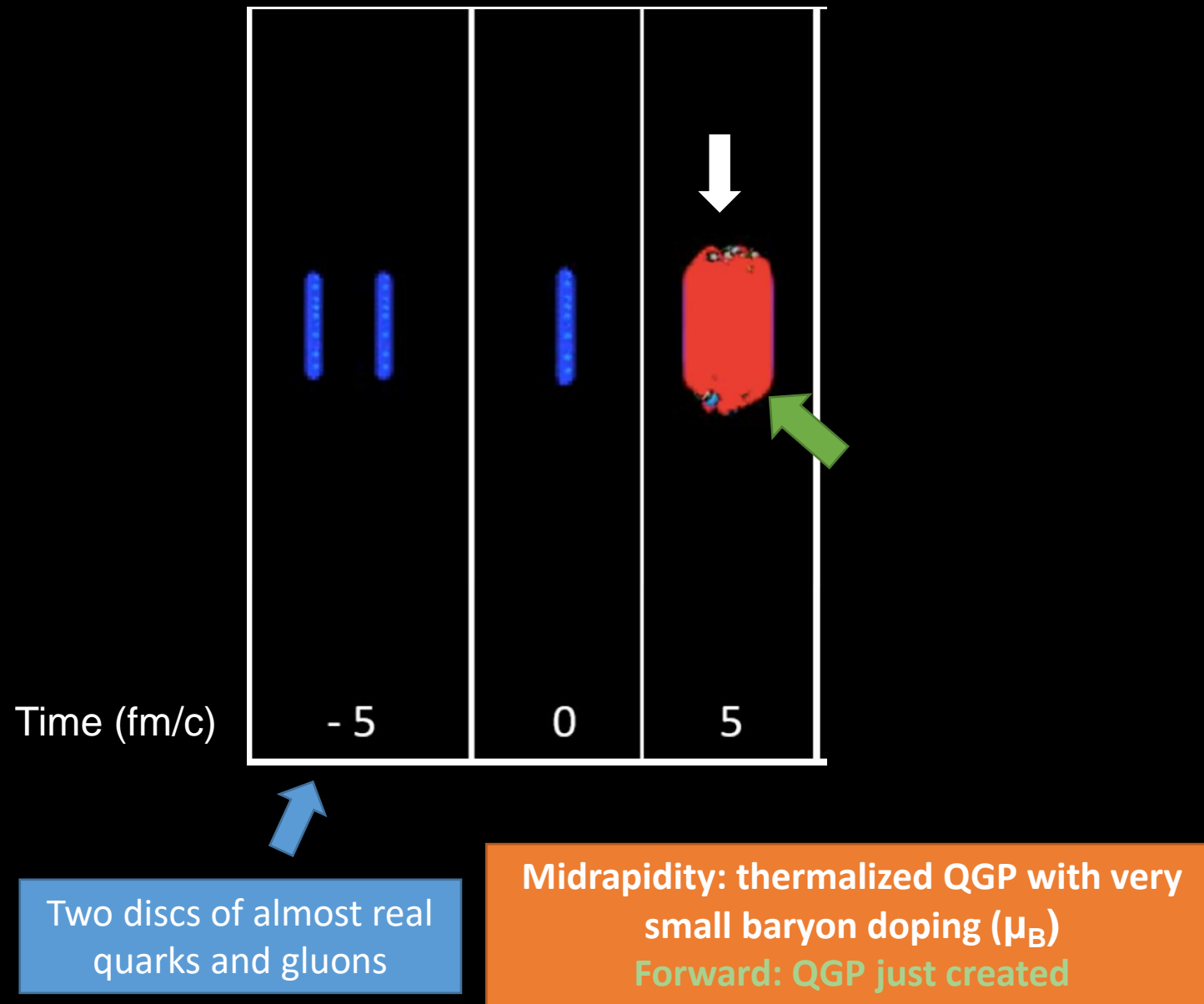
Collision! Highest energy density state. Huge amount of soft (low momentum transfer) scatterings.



Two discs of almost real quarks and gluons

Relativistic Heavy Ion Collisions

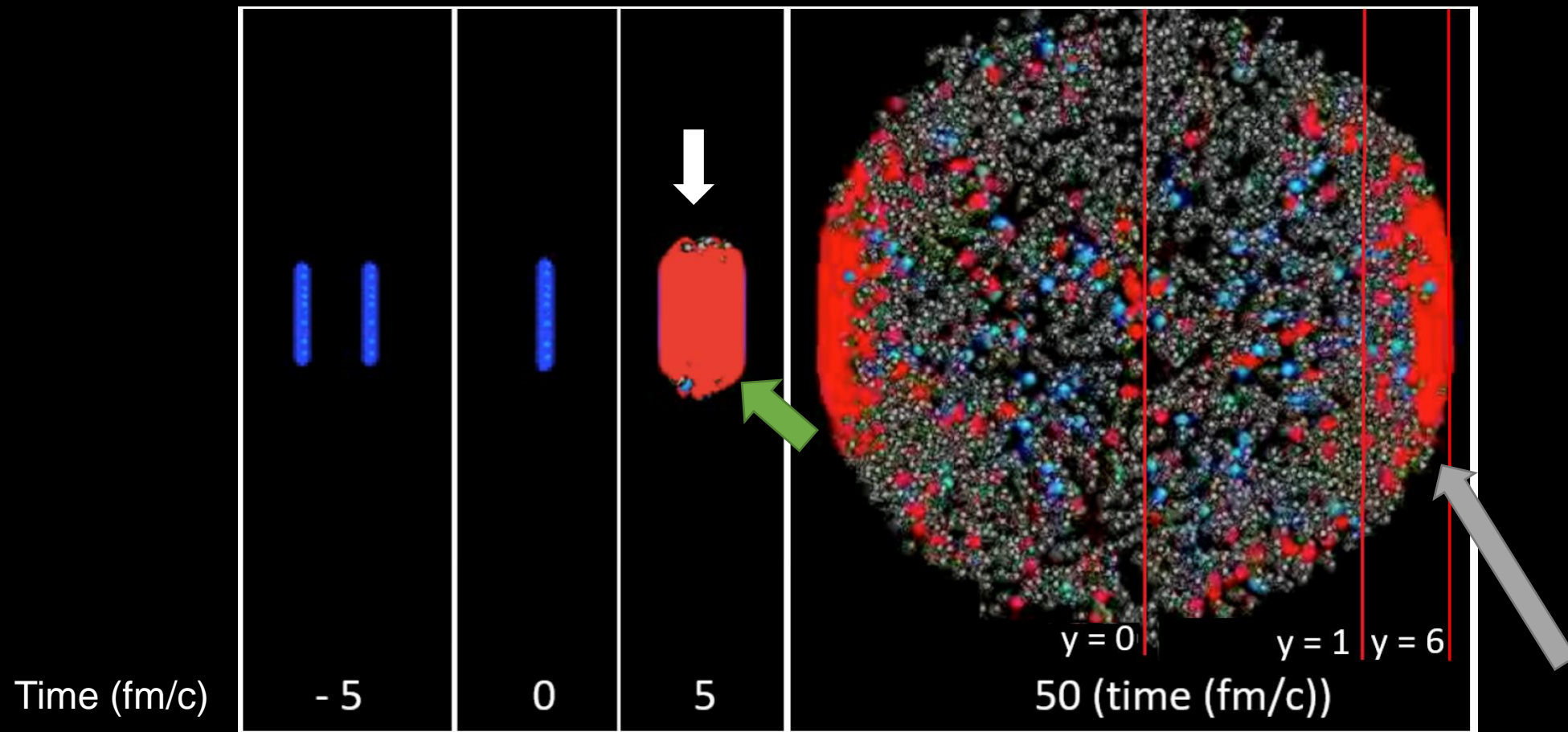
Collision! Highest energy density state. Huge amount of soft (low momentum transfer) scatterings.



Relativistic Heavy Ion Collisions

Collision! Highest energy density state. Huge amount of soft (low momentum transfer) scatterings.

Hadronization of QGP, different from elementary collisions like e^+e^- or pp collisions



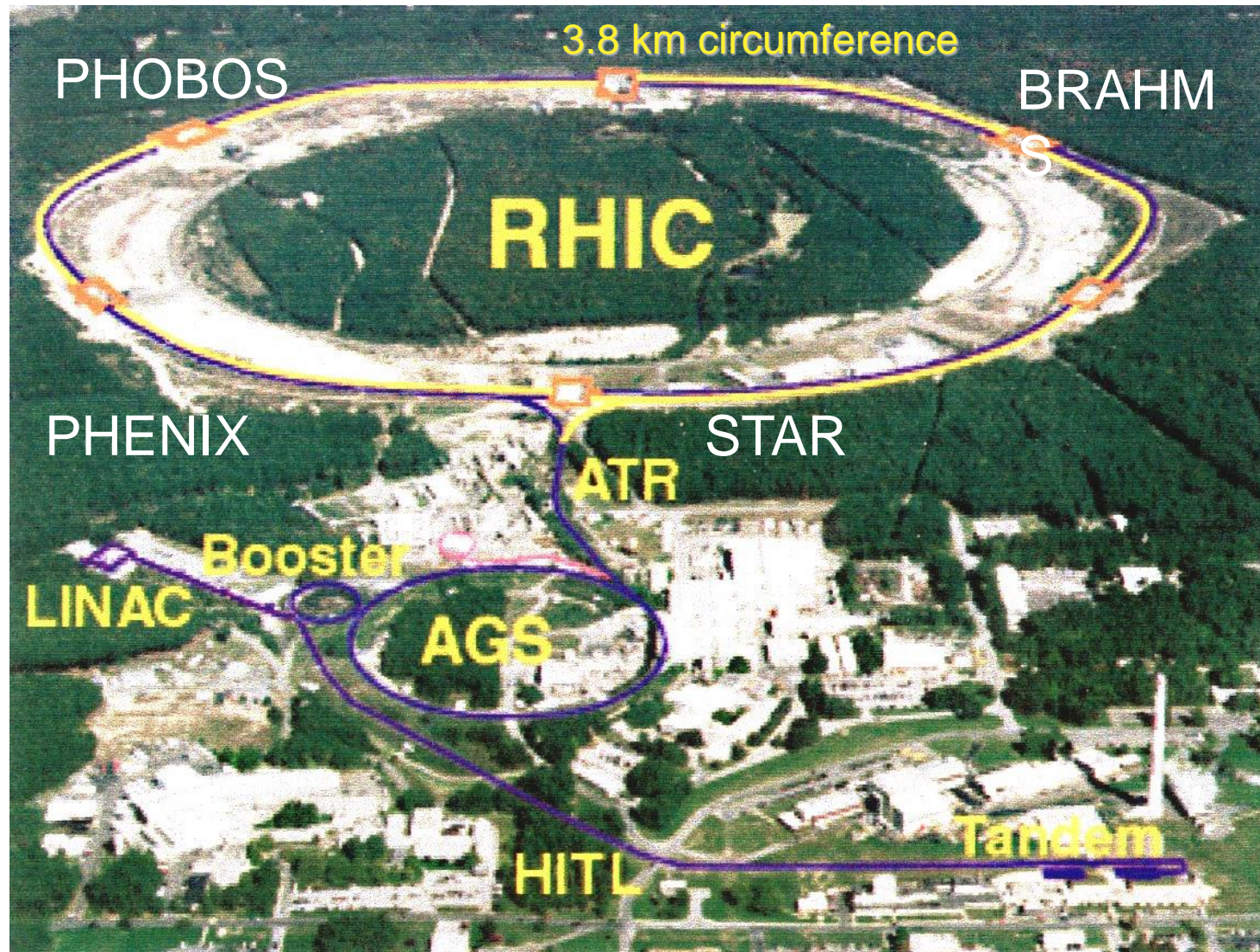
Two discs of almost real quarks and gluons

Midrapidity: thermalized QGP with very small baryon doping (μ_B)
Forward: QGP just created

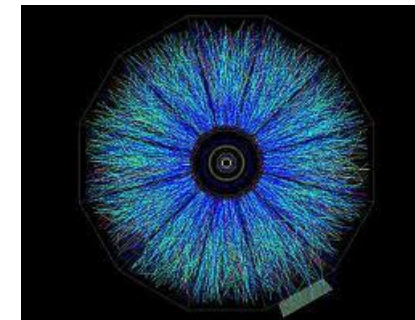
The ions lose $\sim 85\%$ of the momentum and form a compressed baryon-rich QGP (high μ_B) at large rapidity

The First Dedicated Heavy Ion Collider

Relativistic Heavy Ion Collider



Au+Au
7.7 - 200 GeV

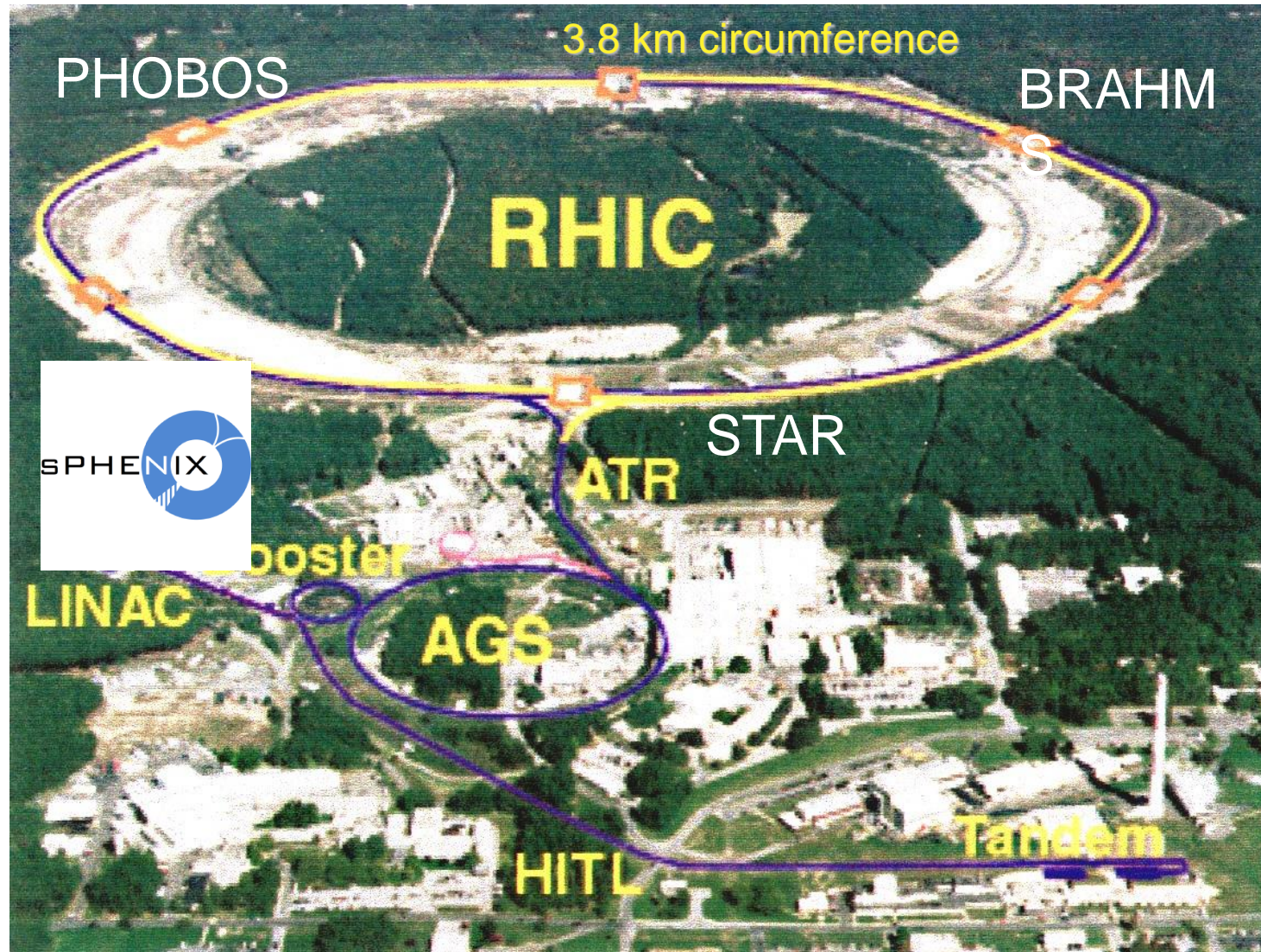


Since 2000~

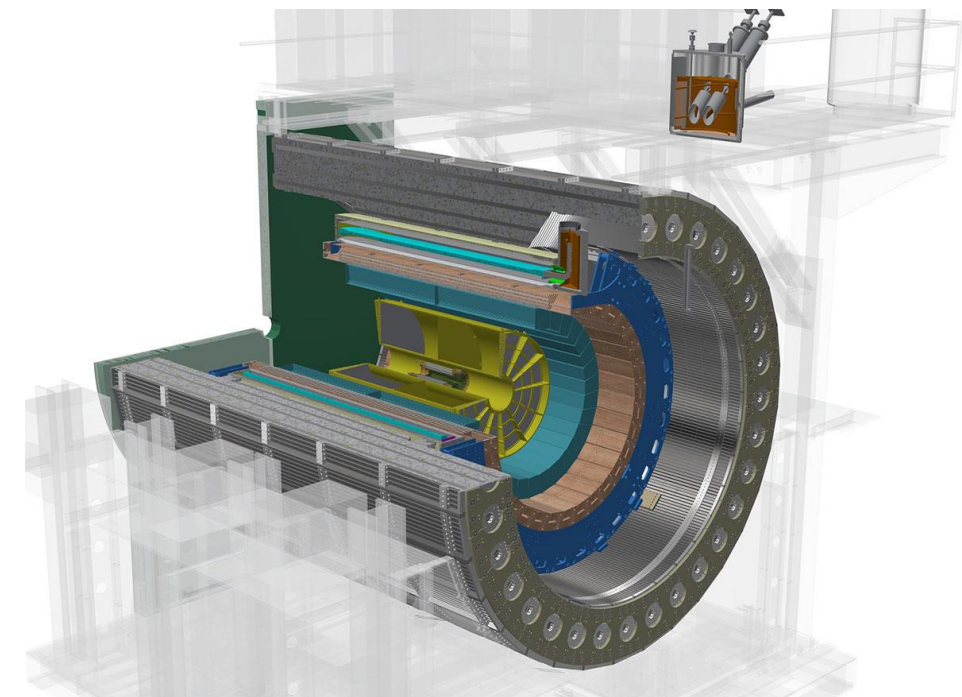


sPHENIX Data-Taking in 2023

Relativistic Heavy Ion Collider

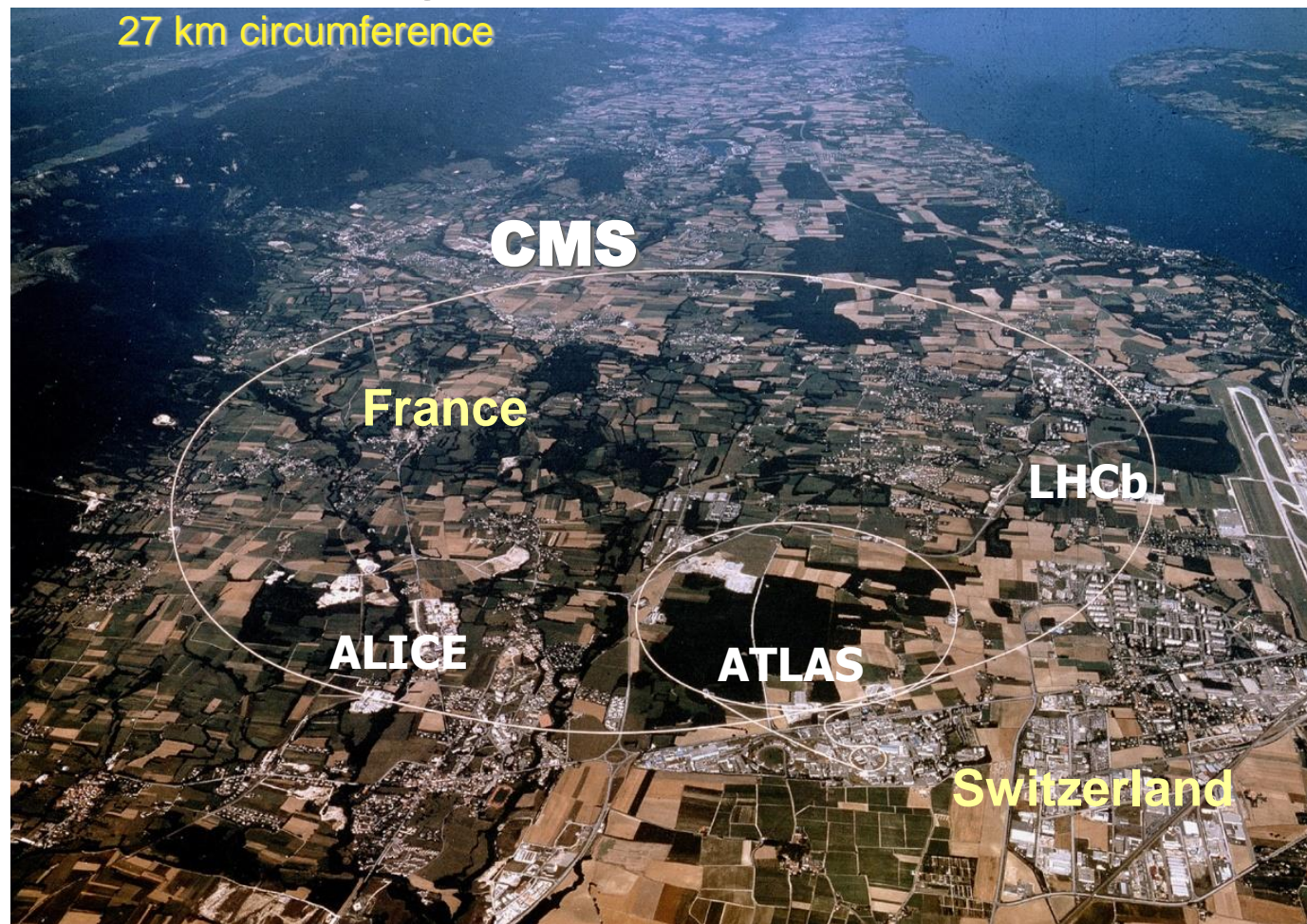


Au+Au
200 GeV



High Energy (Temperature) Frontier

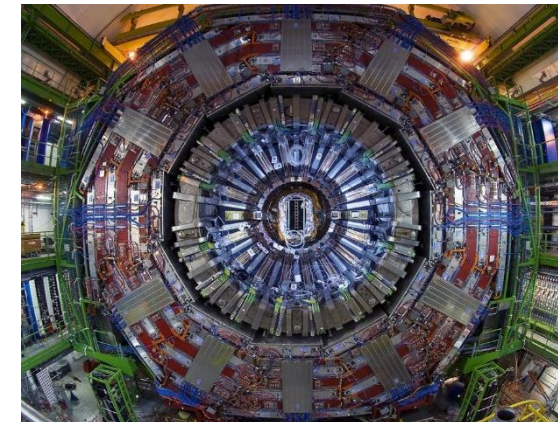
Large Hadron Collider



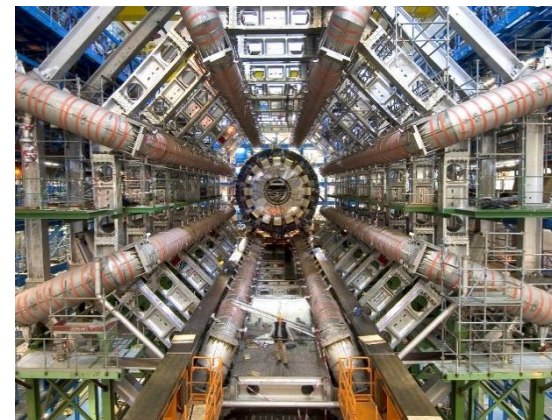
ALICE



CMS



ATLAS



LHCb



Lead+Lead (PbPb) collisions

2010-11: **2.76 TeV** **0.16/nb**

2015-18: **5.02 TeV** **1.7/nb**

Also smaller system data:

Proton-lead (pPb) at 5.02 & 8.16 TeV

Xenon-Xenon (XeXe) at 5.44 TeV

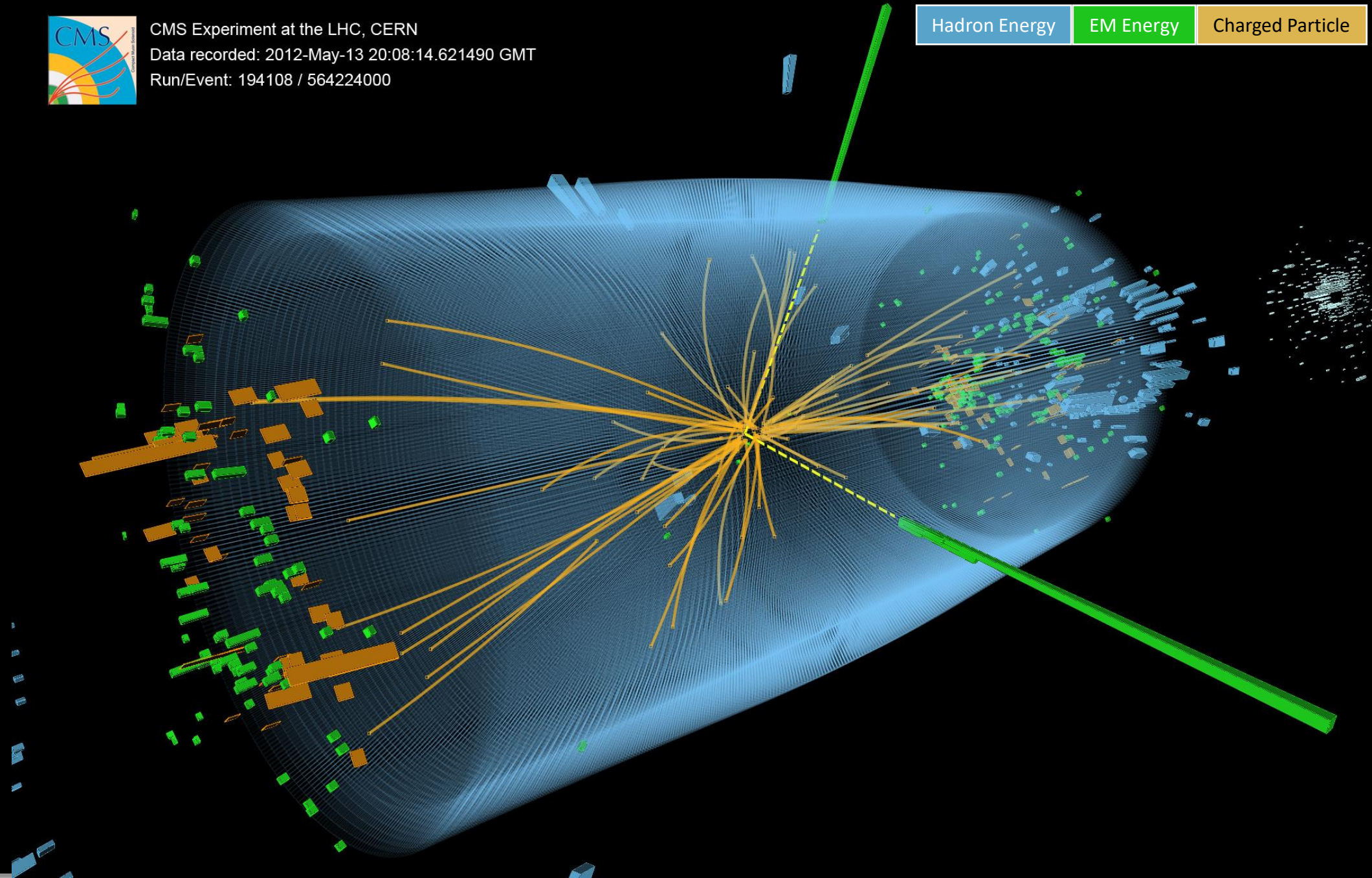
A flying mosquito has about 4 trillion electronvolts (**4TeV**) of energy

Proton-Proton Collision Recorded by CMS



CMS Experiment at the LHC, CERN
Data recorded: 2012-May-13 20:08:14.621490 GMT
Run/Event: 194108 / 564224000

Hadron Energy EM Energy Charged Particle



Lead-Lead Collision Recorded by CMS (2018)



CMS Experiment at the LHC, CERN

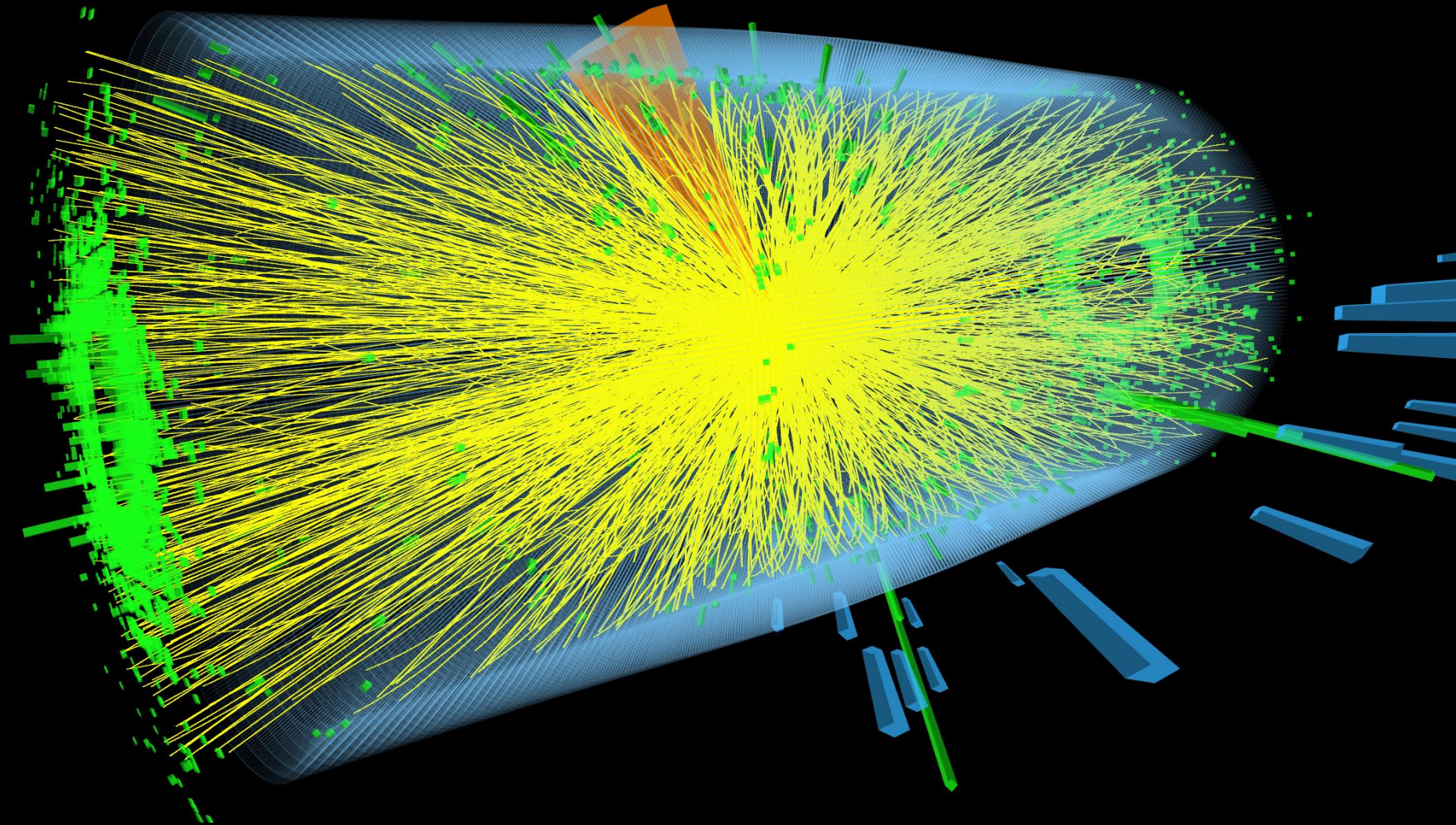
Data recorded: 2018-Nov-12 08:36:52.866176 GMT

Run / Event / LS: 326586 / 2491137 / 6

Hadron Energy

EM Energy

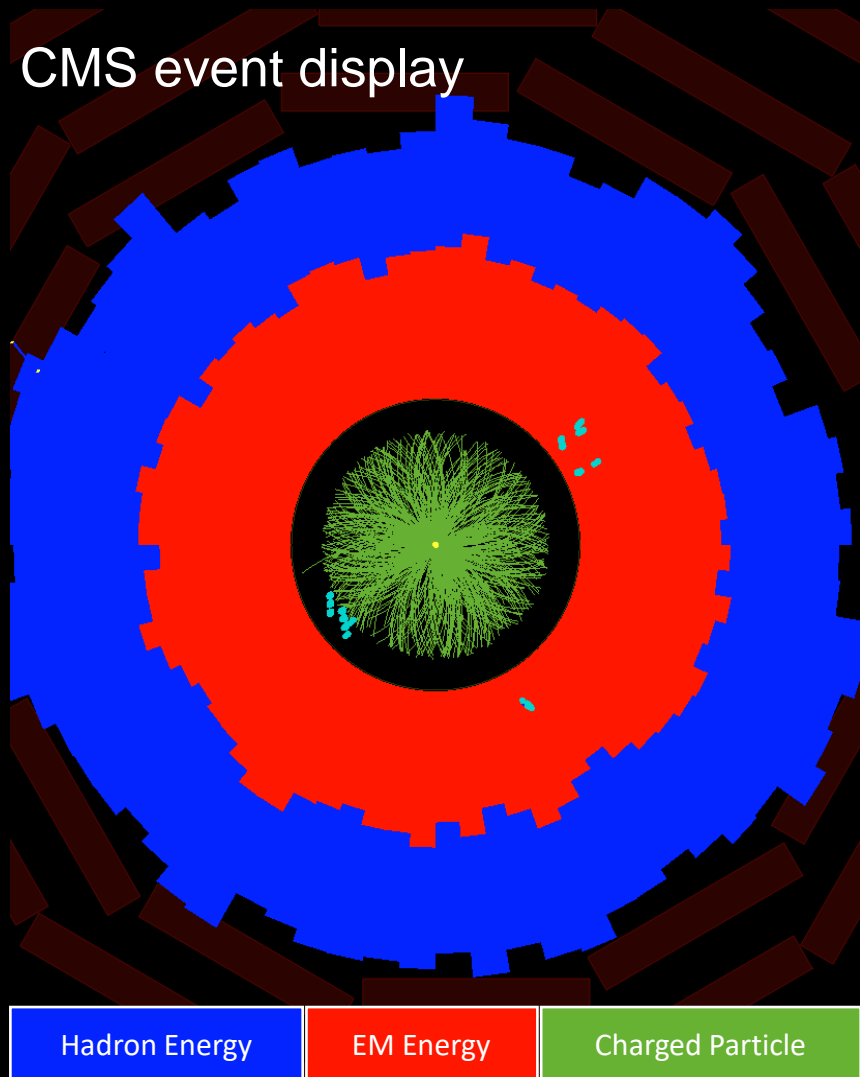
Charged Particle



Data-Taking

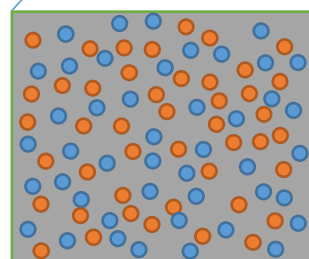
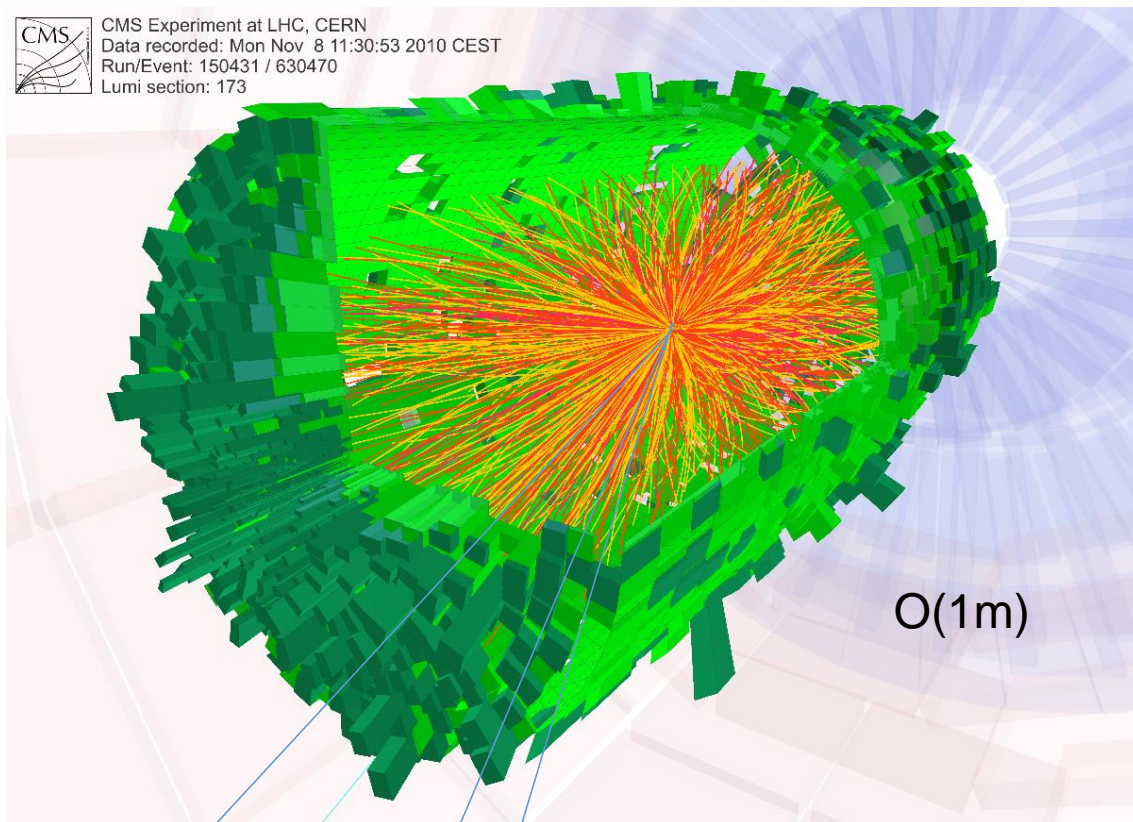
- LHC delivers heavy ion collisions for around **one month per year**
- 2018: PbPb collision data rate up 50 kHz; CMS peak data throughput 9 GB/s
- We are actively preparing for the first data-taking in Run 3!

CMS event display



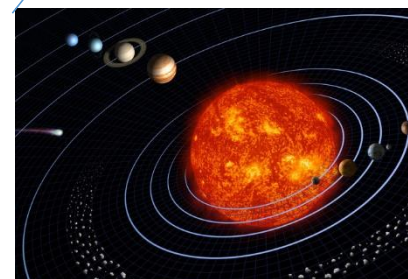
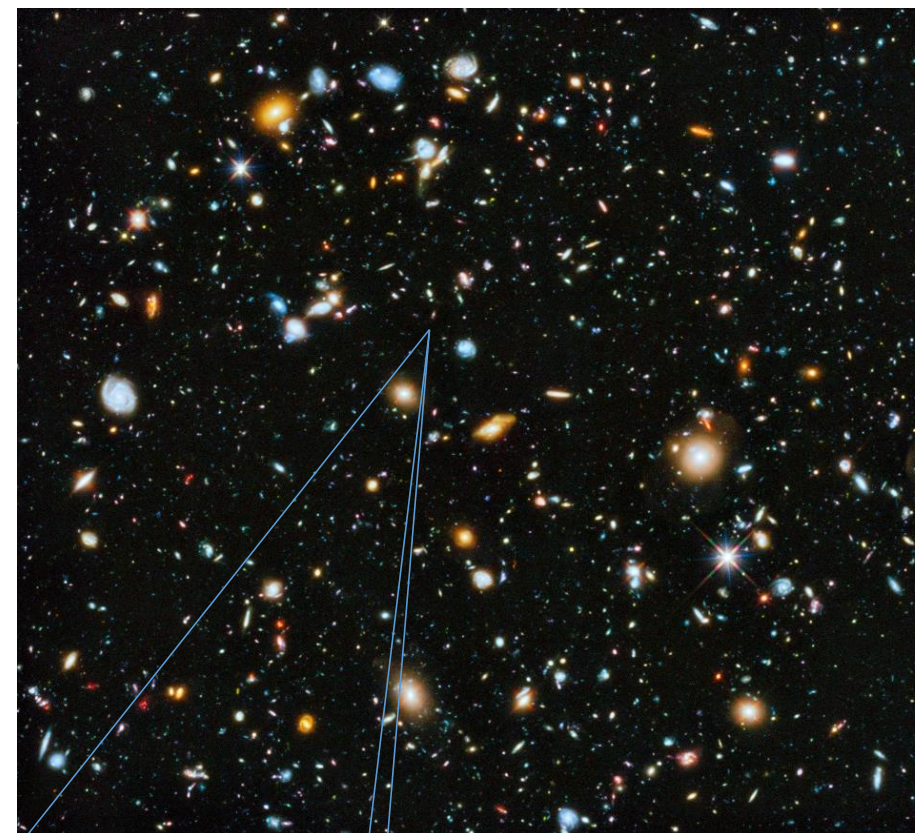
Reconstruct the Quark Soup with CMS

Size of the CMS detector



Inner Structure of QGP

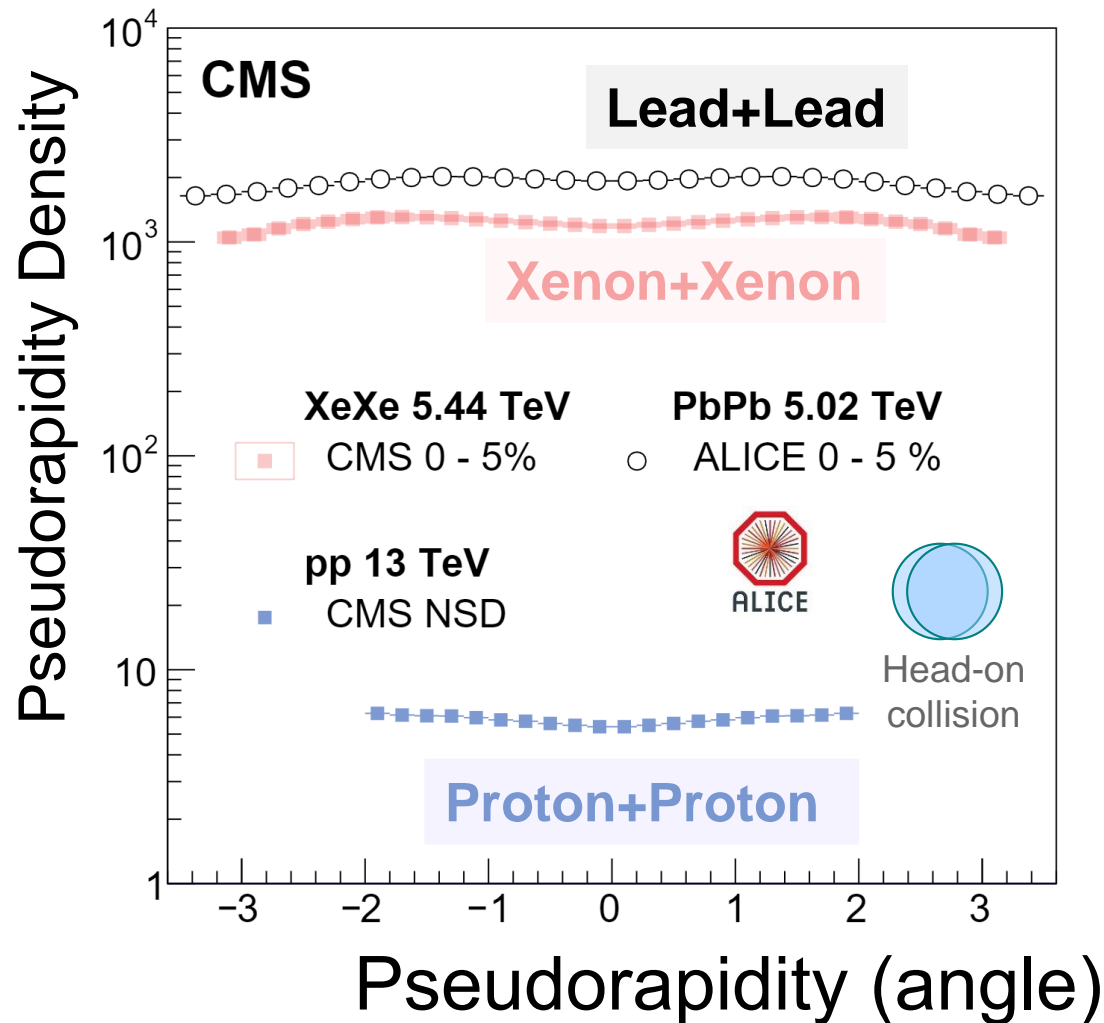
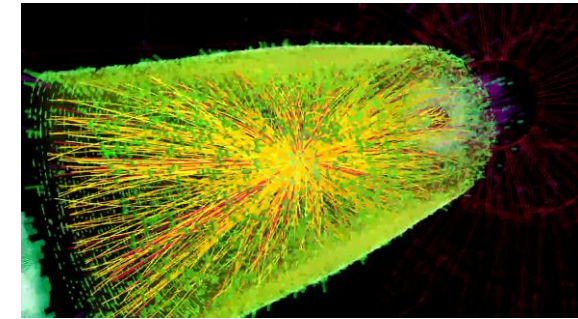
Size of the Universe



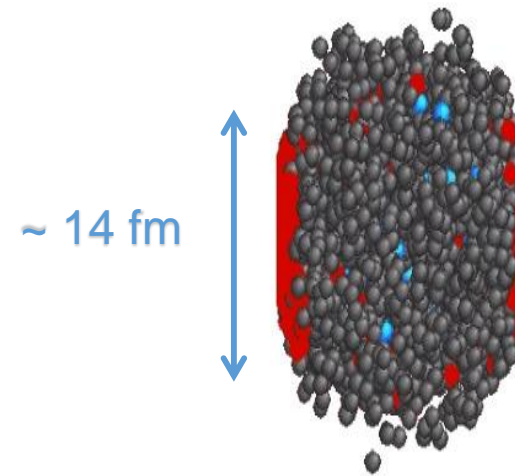
Inner Structure of Our Solar System

Density of the Quark Soup

Count the number of particles produced in **head-on** collisions.
 Particle density in **Lead+Lead** ~ **400x** of that in **Proton+Proton**



At $\tau_0 \sim 0.2$ fm/c:



$$\epsilon = \frac{1}{A \cdot \tau_0} \left. \frac{dE_T}{dy} \right|_{y=0}$$

Energy density of the medium based on CMS $dE/d\eta \sim 2$ TeV: ~ 65 GeV/fm³

> 100x denser than the proton!

At **early time** of the collision, the system can not be described by hadrons

Rough Estimation of QGP Temperature

At $\tau_0 \sim 0.2 \text{ fm}/c$:

$$\epsilon = \frac{1}{A \cdot \tau_0} \left. \frac{dE_T}{dy} \right|_{y=0} \approx 65 \text{ GeV}/\text{fm}^3$$

$$\approx 0.5 \text{ GeV}^4 = 47.5 \times \frac{\pi^2}{30} T^4$$

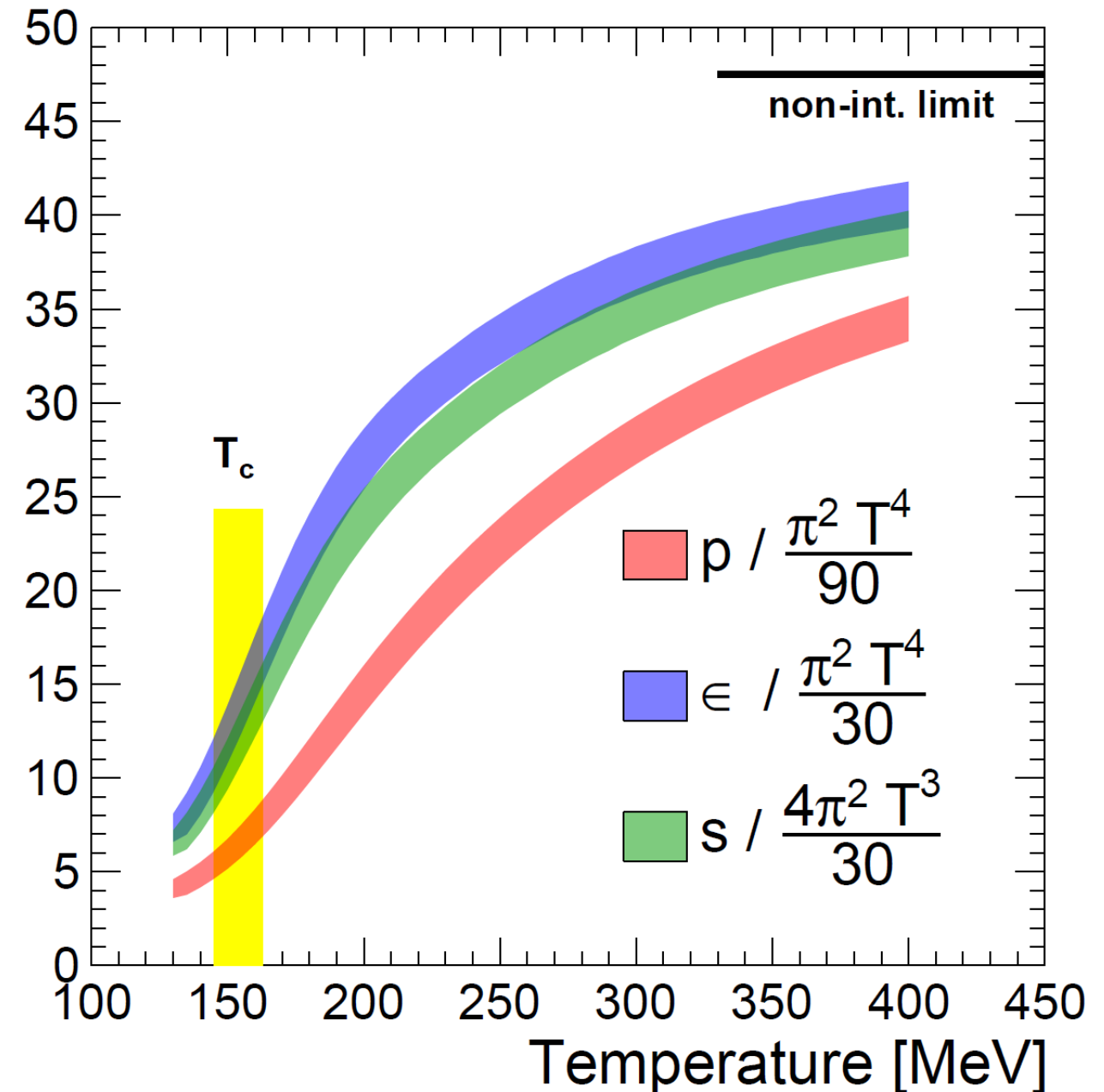
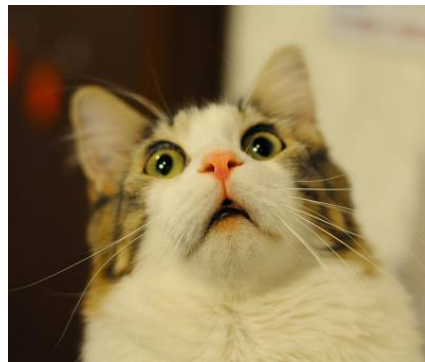
$$1 \text{ fm}^{-1} = 0.1973 \text{ GeV}$$

$$T \approx 0.423 \text{ GeV} = 423 \text{ MeV}$$

$$\approx 5 \times 10^{12} \text{ K}$$

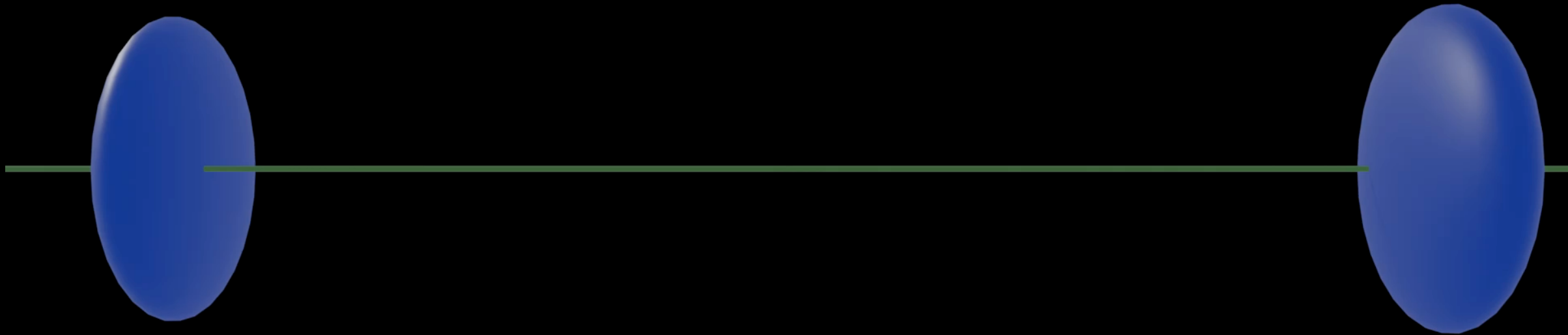
$$1 \text{ GeV} = 1.16 \times 10^{13} \text{ K}$$

!!!



Collision with Finite Impact Parameter

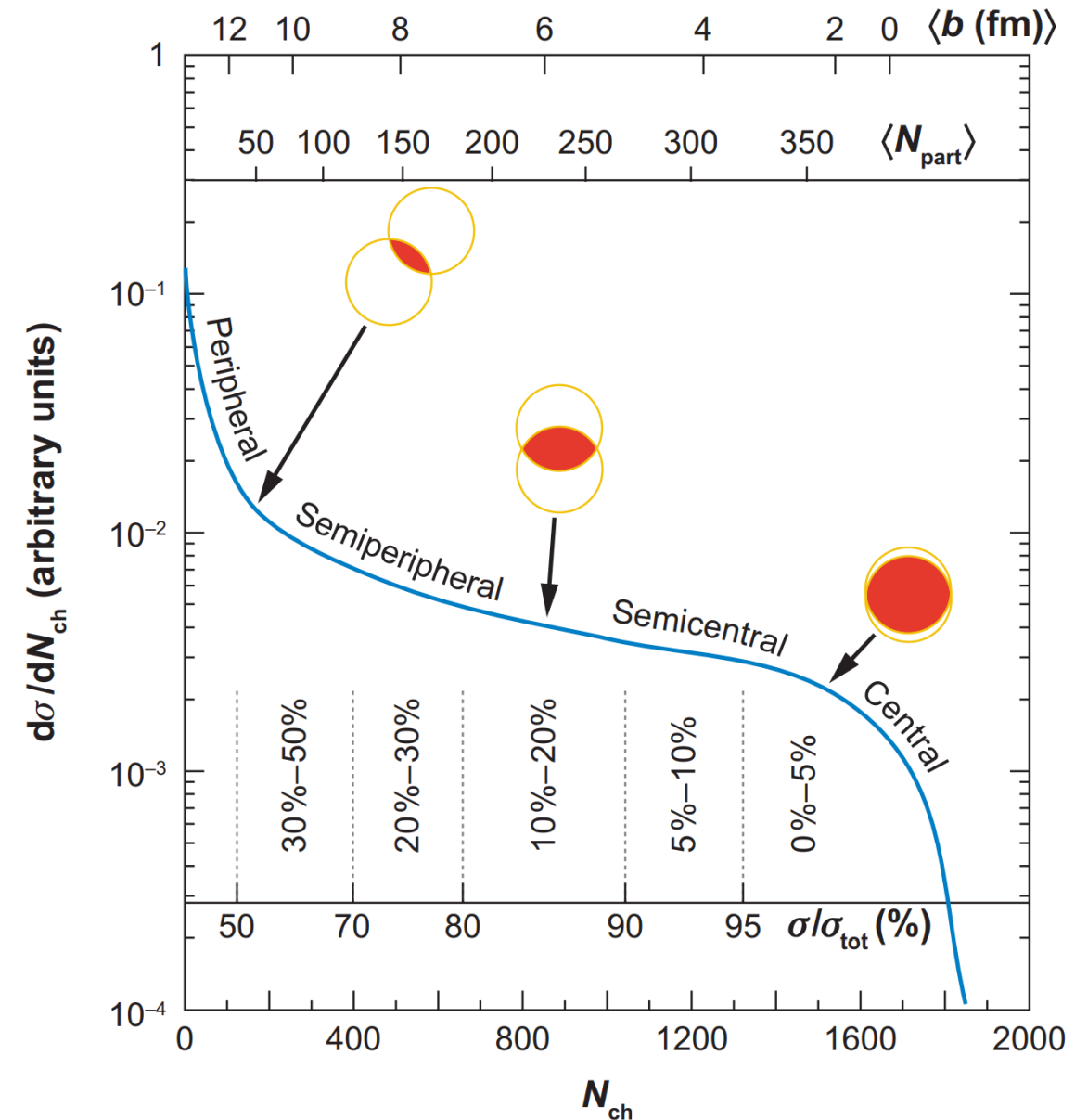
Initial azimuthal anisotropic shape



Animation from Jing Wang (MIT)

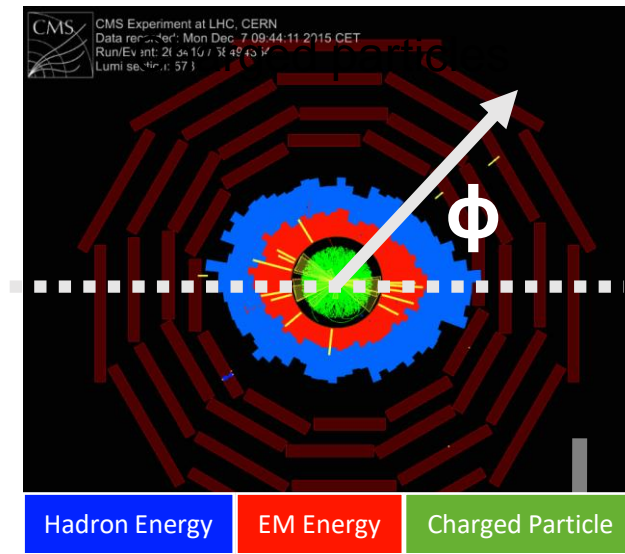
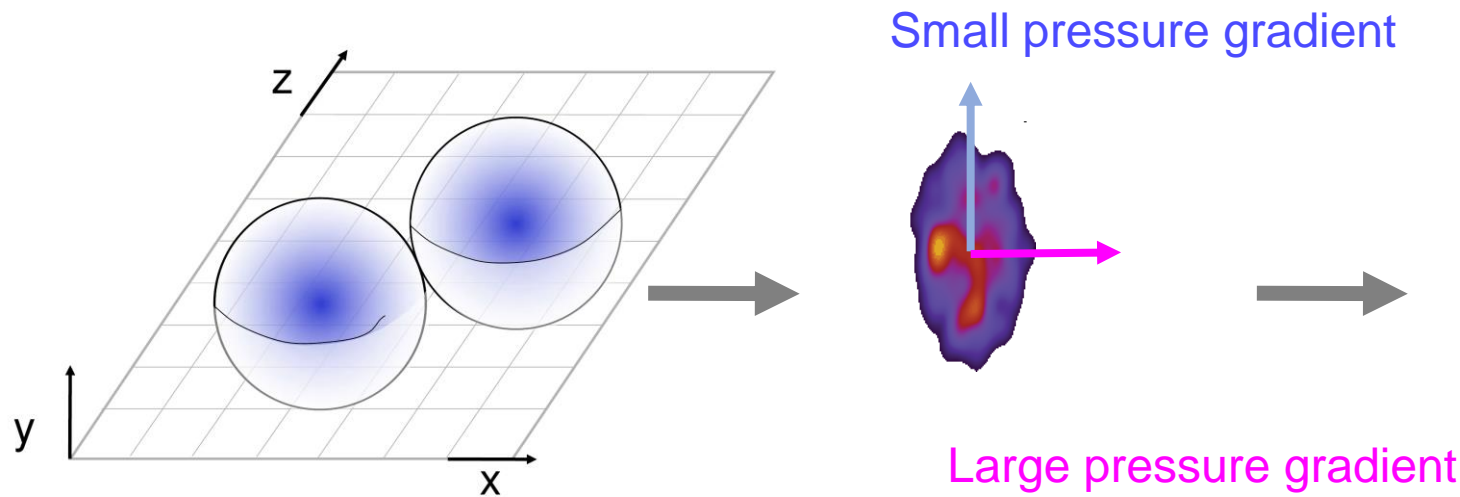
Centrality

- Need experimental access to the impact parameter \mathbf{b} of the collision
- Idea: use an observable which change **monotonically with \mathbf{b}** , such as:
 - Forward calorimeter energy
 - Charged particle multiplicity (N_{ch}).
- Centrality classes: percentiles (fraction of total integral) of centrality distribution
- Convention:
 - 0% = “most central” (head-on!), $b \sim 0$ (high N_{ch})
 - 100% = most peripheral (low N_{ch})

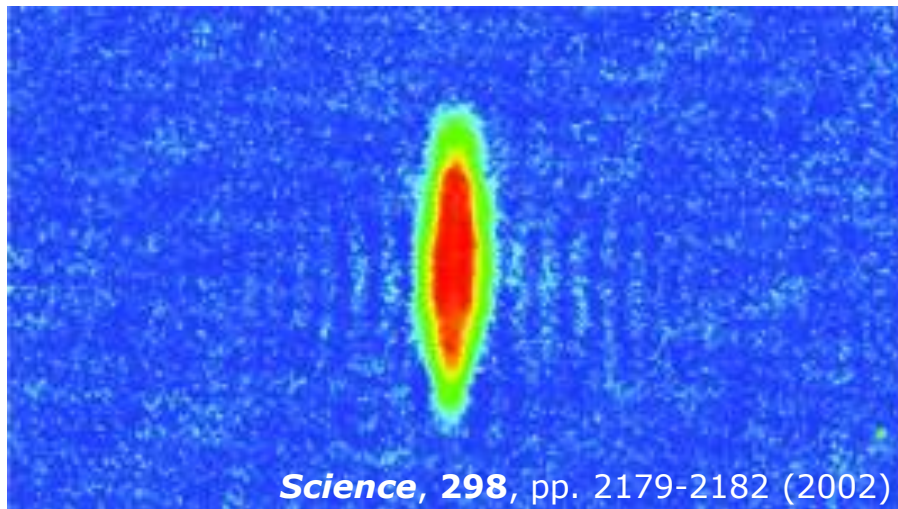


Annual Review of Nuclear and Particle Science, 57:205-243 (2007)

Pressure Driven Expansion of the Quark Soup

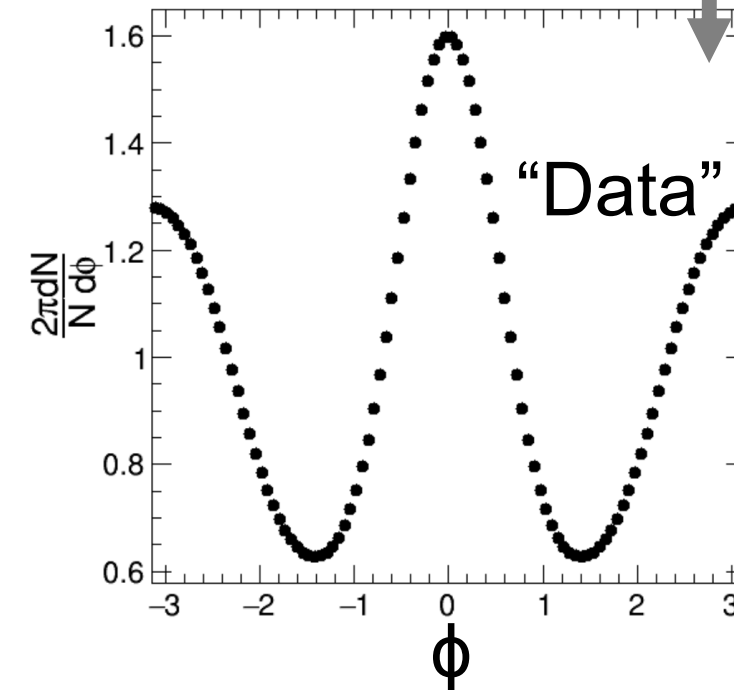


Expansion of **Ultra-cold atoms (Li-6)** released from laser trap



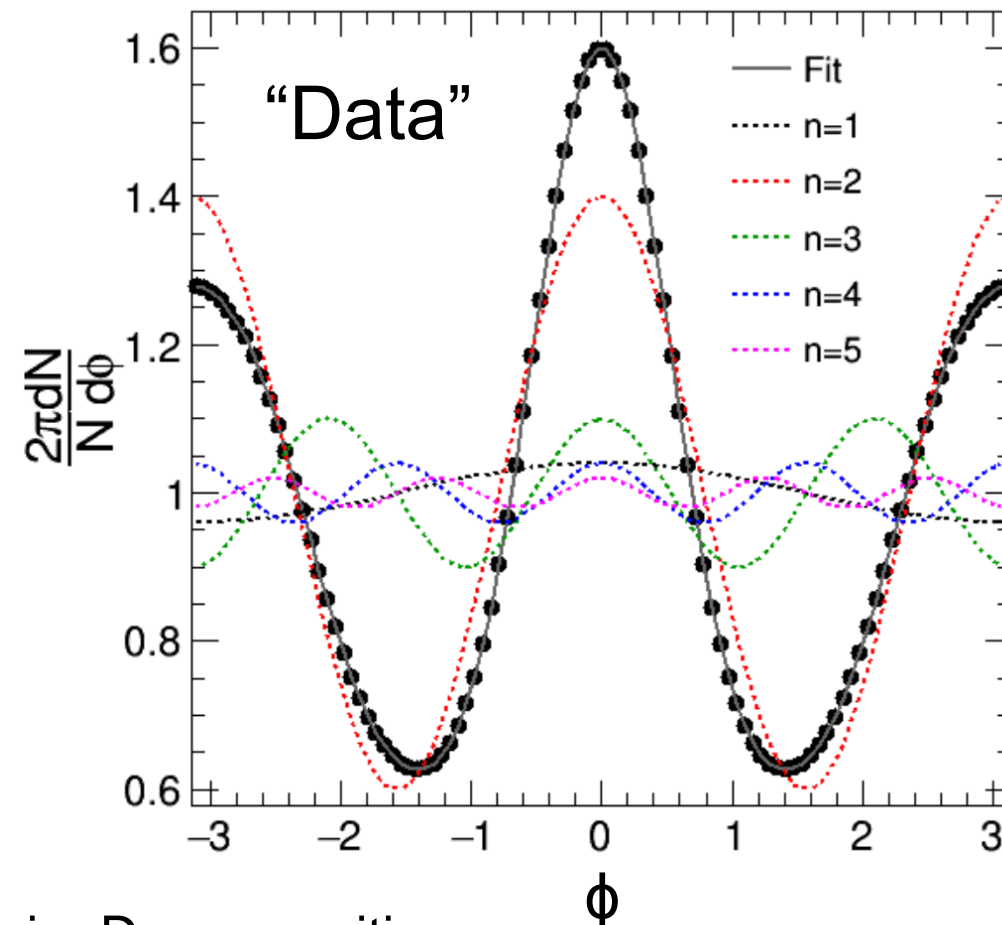
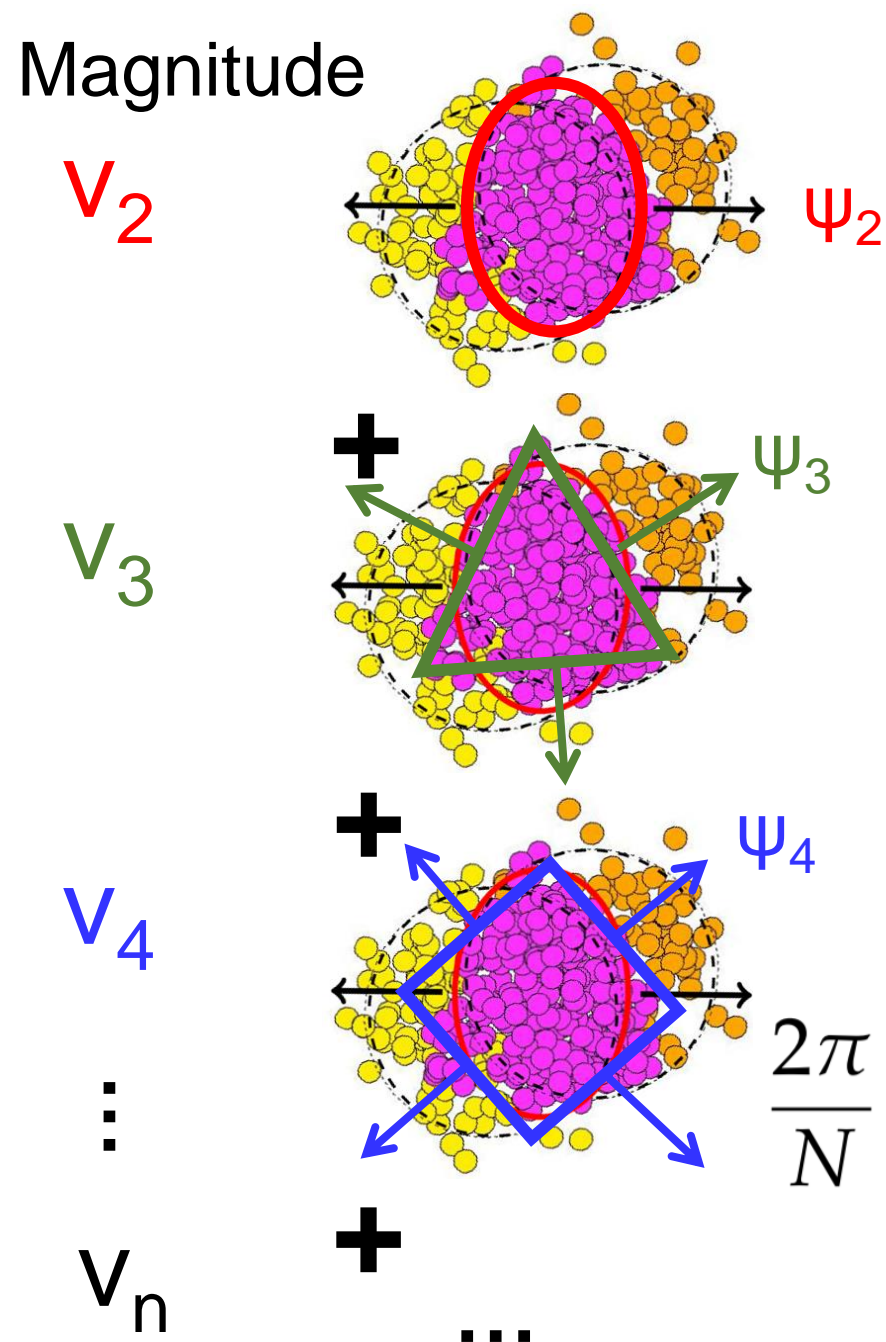
100 μ s

Collective motion is observed
→ **Early hydrodynamization!**



Particle Azimuth Angle Distribution

Particle Azimuthal Anisotropy



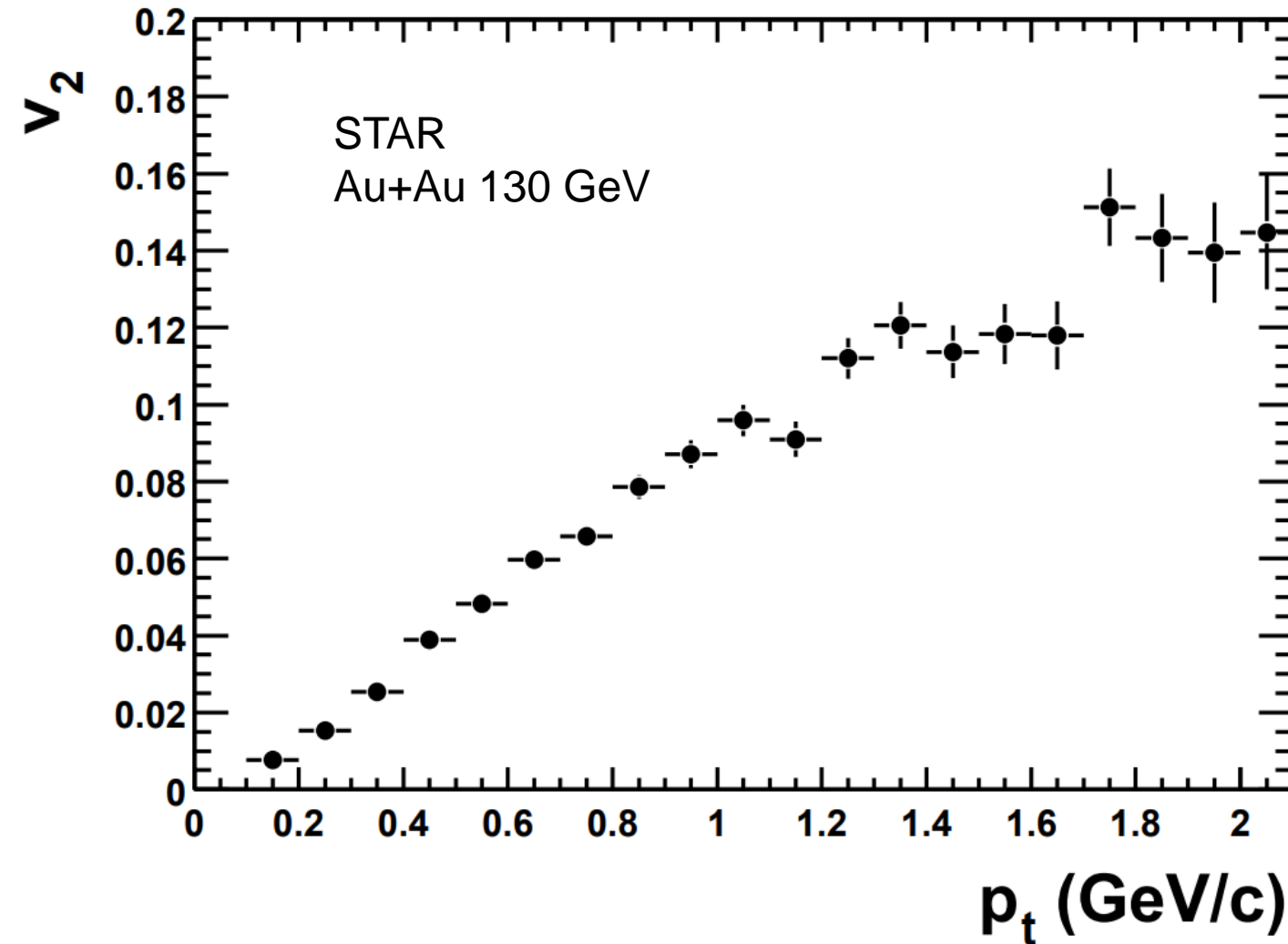
Fourier Decomposition:

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_n)]$$

Alver and Roland (MITHIG)
 “Collision geometry fluctuation”
 PRC82 (2010) 039903

Elliptic Flow

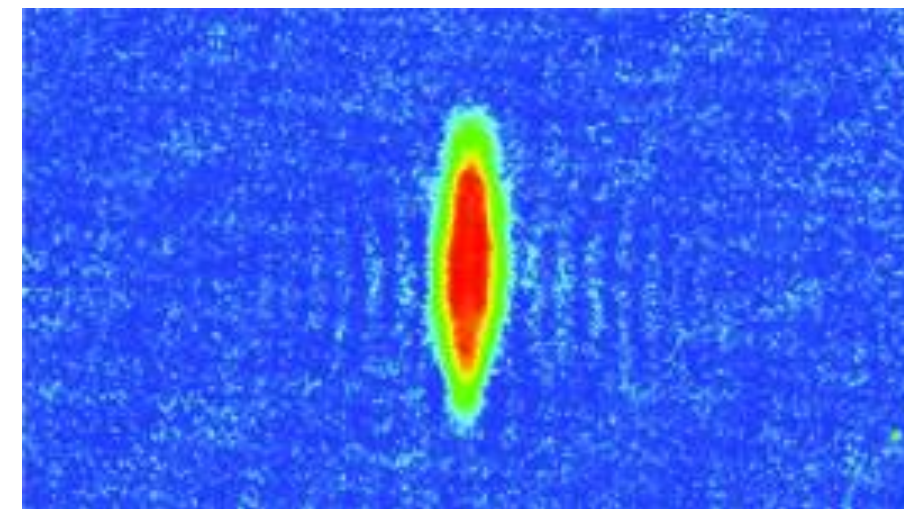
- The first result from STAR at RHIC
- The extracted v_2 increases with transverse momentum



PRL 86 (2001) 402

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_n)]$$

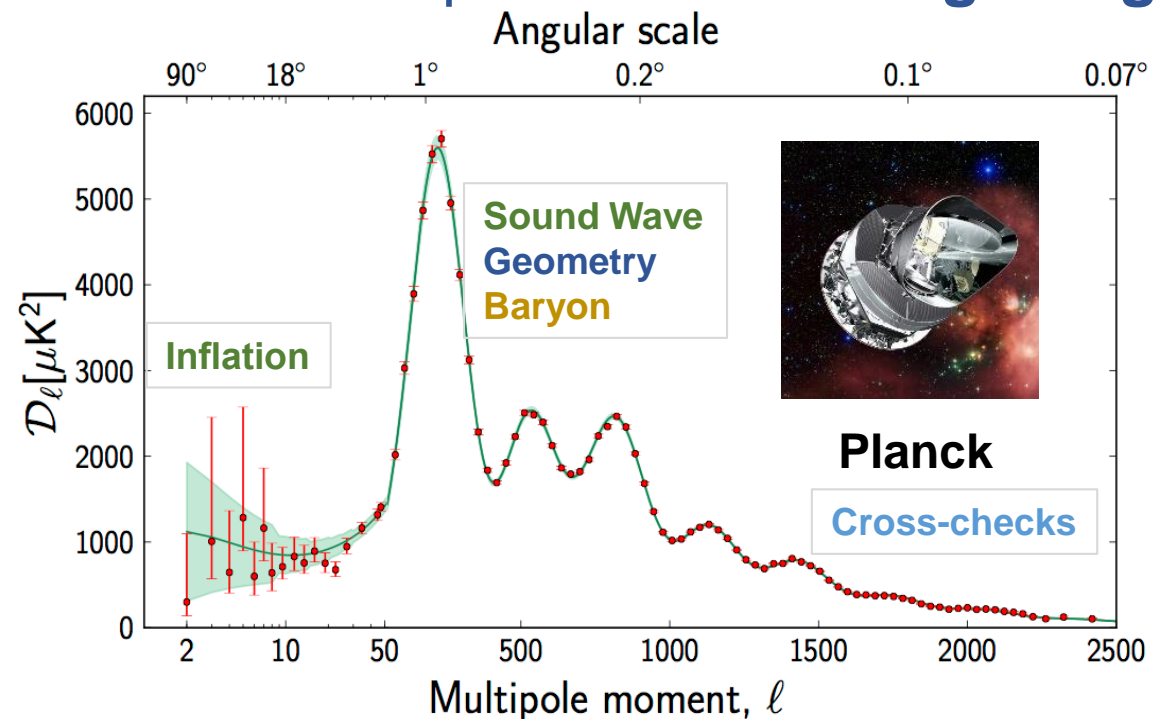
Expansion of **Ultra-cold atoms (Li-6)** released from laser trap



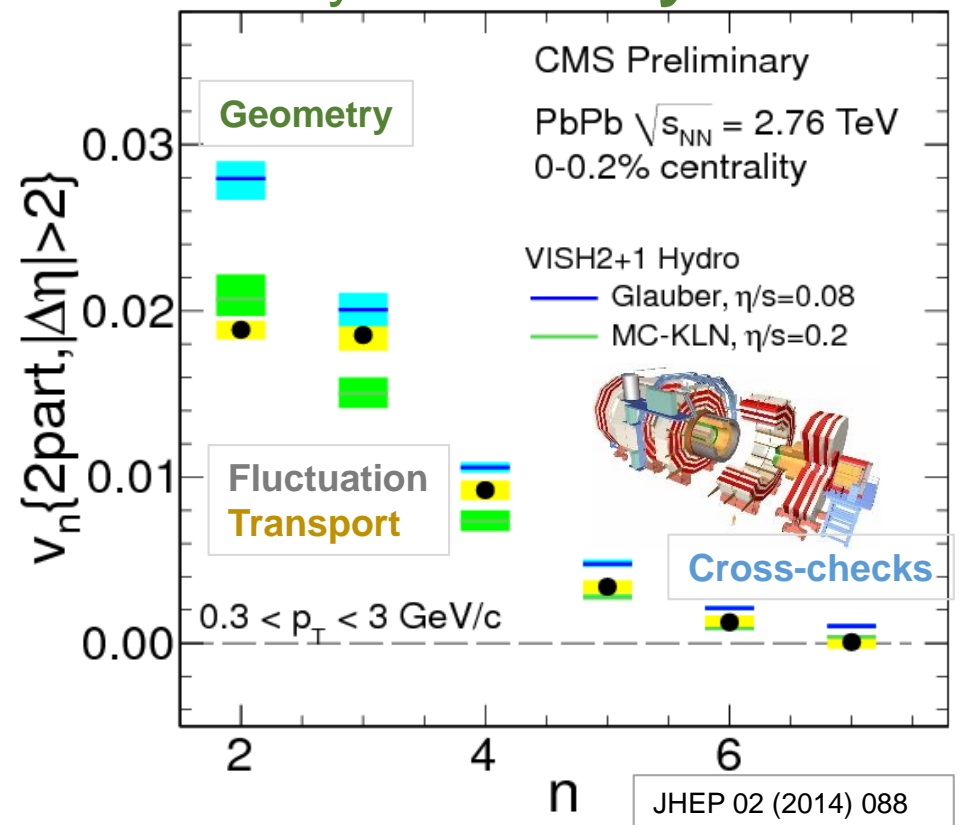
100 μ s

Density Fluctuation

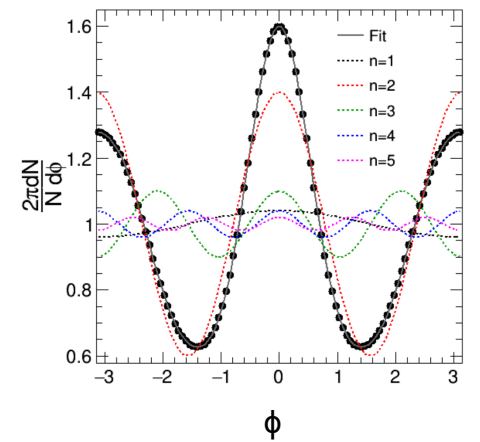
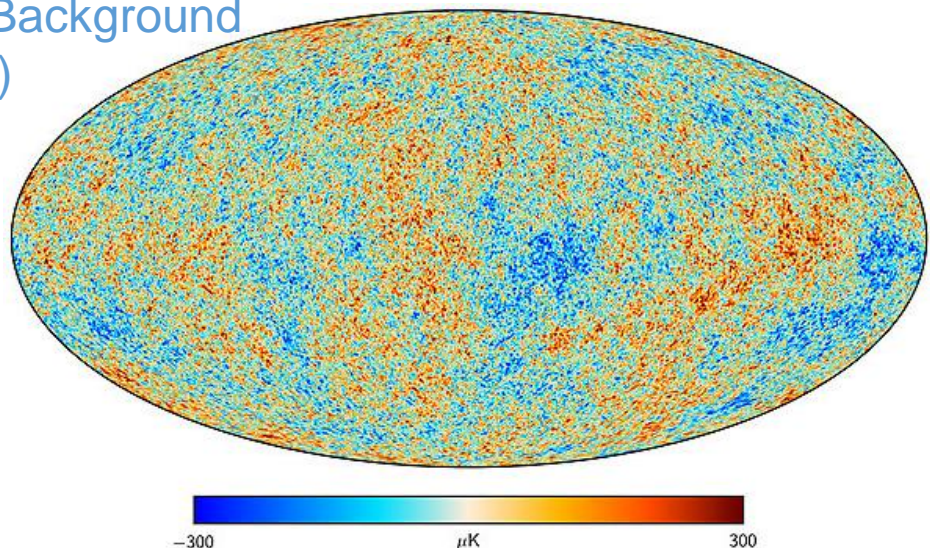
Power spectrum of the Big Bang



Fourier analysis of many little bangs

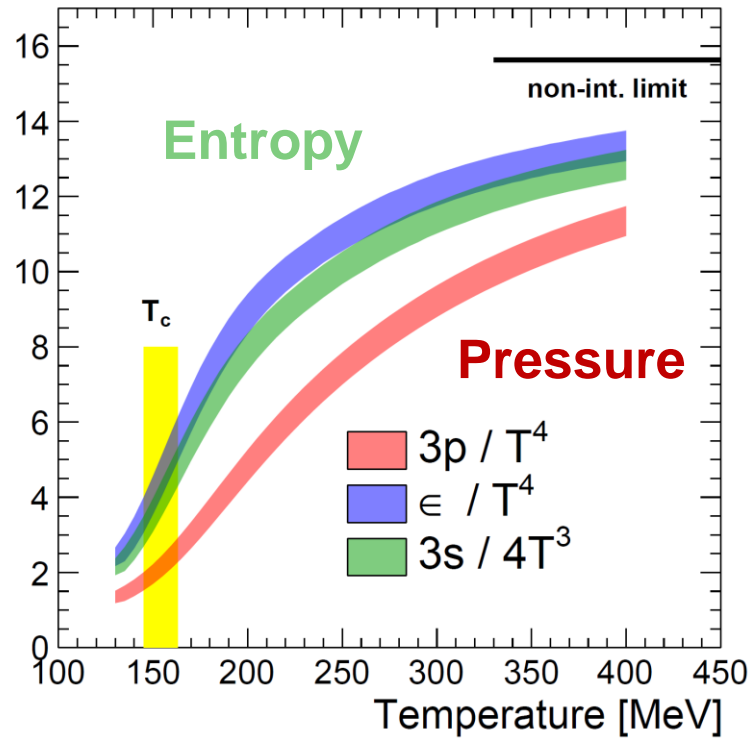


Cosmic Microwave Background (CMB)

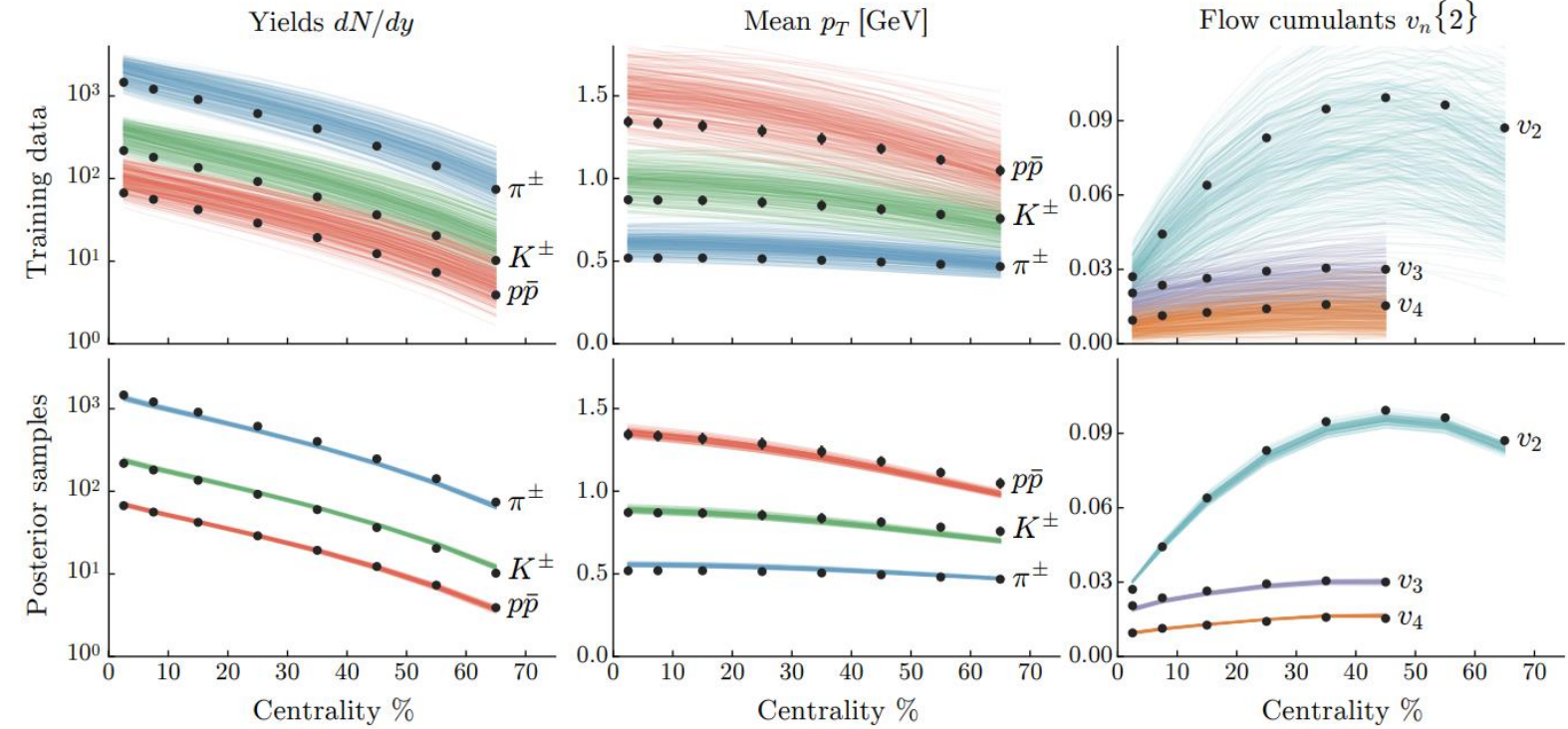


Quark Gluon Plasma (QGP)

Relativistic Hydrodynamics Calculations



Lattice QCD based
Equation of State



Output (from Global fit)
Medium Properties

$$T_{\mu\nu} = \varepsilon u_\mu u_\nu + p[\varepsilon] \Delta_{\mu\nu} - \eta[\varepsilon] \sigma_{\mu\nu} - \zeta[\varepsilon] \Delta_{\mu\nu} \nabla_\mu u^\mu + \mathcal{O}(\partial^2),$$

$$\sigma_{\mu\nu} = \Delta_{\mu\alpha} \Delta_{\nu\beta} (\nabla^\alpha u^\beta + \nabla^\beta u^\alpha) - \frac{2}{3} \Delta_{\mu\nu} \Delta_{\alpha\beta} \nabla^\alpha u^\beta,$$

$$\Delta_{\mu\nu} = g_{\mu\nu} + u_\mu u_\nu,$$

hydrodynamic evolution equations, $\nabla_\mu T^{\mu\nu} = 0$



ALICE

Example:
PRC 94 (2016) 2, 024907

Shear Viscosity

Viscosity η in the kinetic theory:^[1] $\eta = k\rho \langle p \rangle \lambda_f$

$\mathbf{p} \rightarrow$ momentum

$\rho \rightarrow$ the density of medium constituents (quarks and gluons)

$\sigma \rightarrow$ Cross-section

$\lambda_f \rightarrow$ mean free path

$$\lambda_f = \frac{1}{\rho\sigma}$$

$k \rightarrow$ a constant $\sim \frac{1}{3}$ from kinetic theory calculation

Therefore, $\eta = \frac{\langle p \rangle}{3\sigma}$

\rightarrow **Large transport cross-section** leads to **small shear viscosity**

[1] F. Reif, Fundamentals of Statistical and Thermal Physics (McGraw-Hill, New York, 1965)

Shear Viscosity to Entropy Ratio

The motivation of $\frac{\eta}{s}$: Normalize by system size

Relativistic Version of $F = ma$ results in $\frac{\eta}{\epsilon + P} \sim \frac{\text{force}}{\text{mass}}$

At zero chemical potential: $\epsilon + P = Ts$

Therefore $\frac{\eta}{\epsilon + P} = \frac{\eta}{s} \times \frac{1}{T}$

Where $\frac{\eta}{s}$ is a dimensionless number and $\frac{1}{T}$ is the natural thermal time

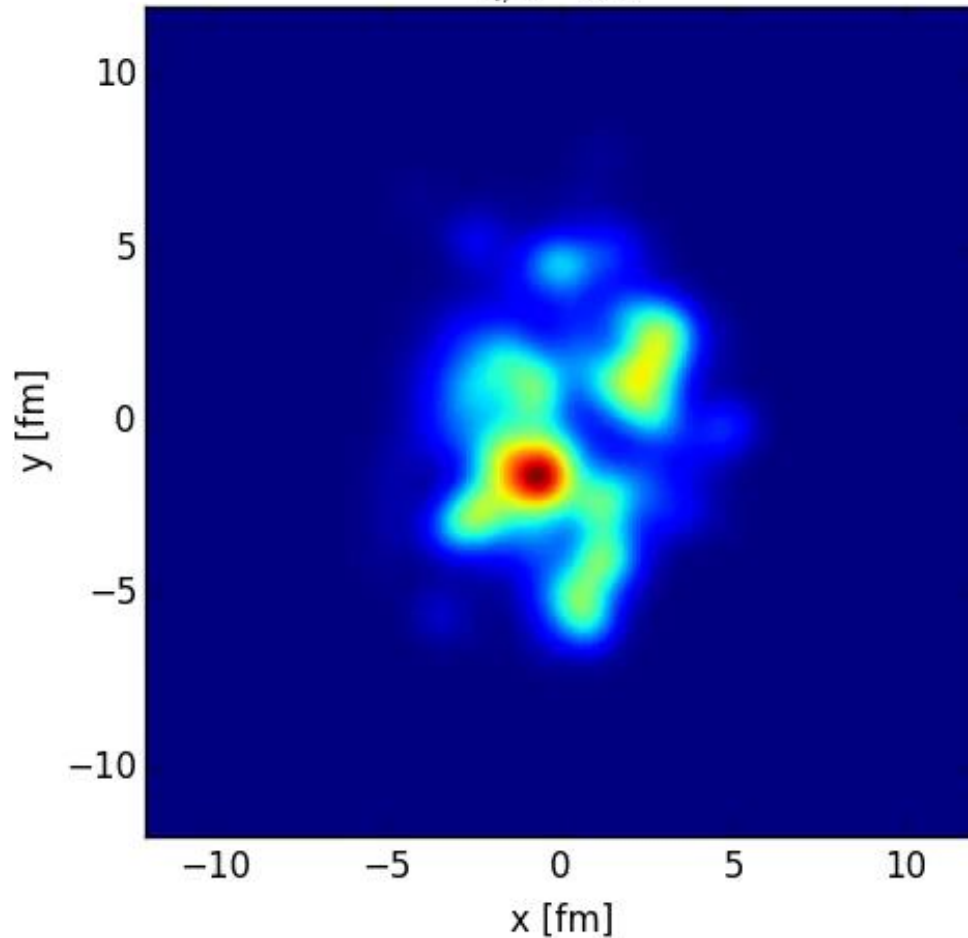
Small specific shear viscosity ~ very small force per inertial mass

Effect of Specific Shear Viscosity in Simulation

Ideal hydrodynamics

$$\eta/s = 0$$

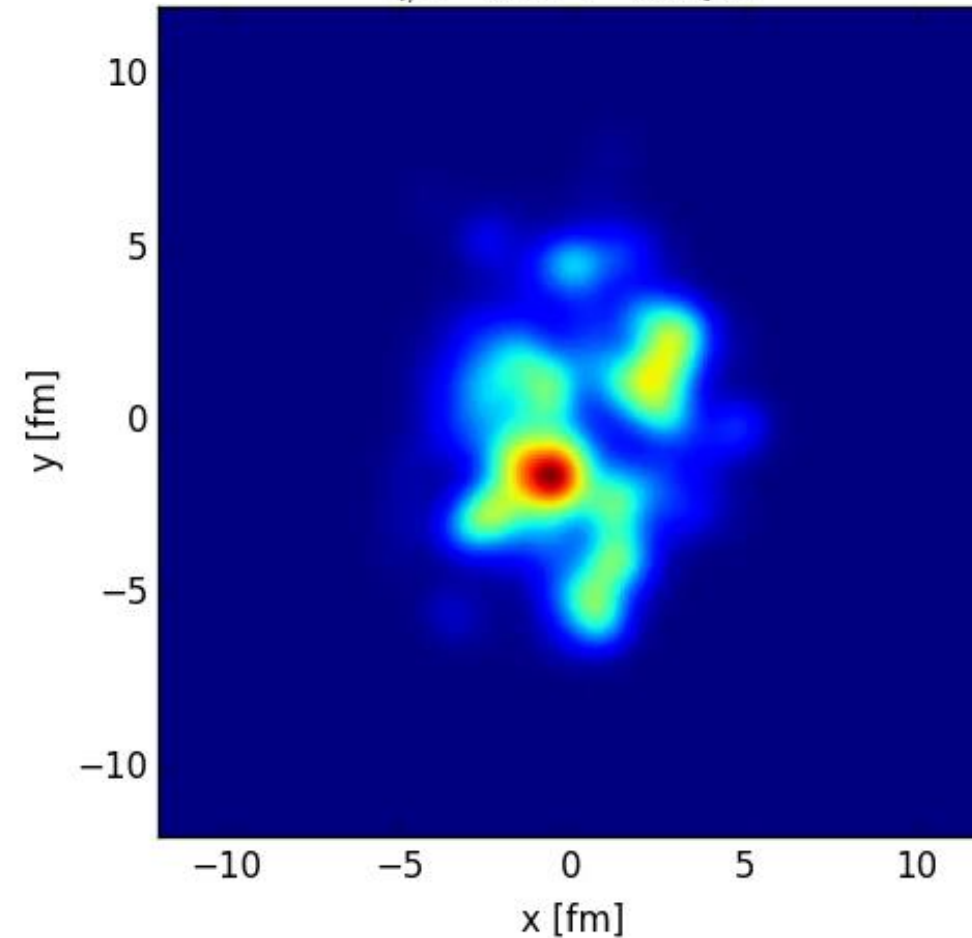
$$\eta/s = 0.0$$



Viscous hydrodynamics

$$\eta/s = 0.08$$

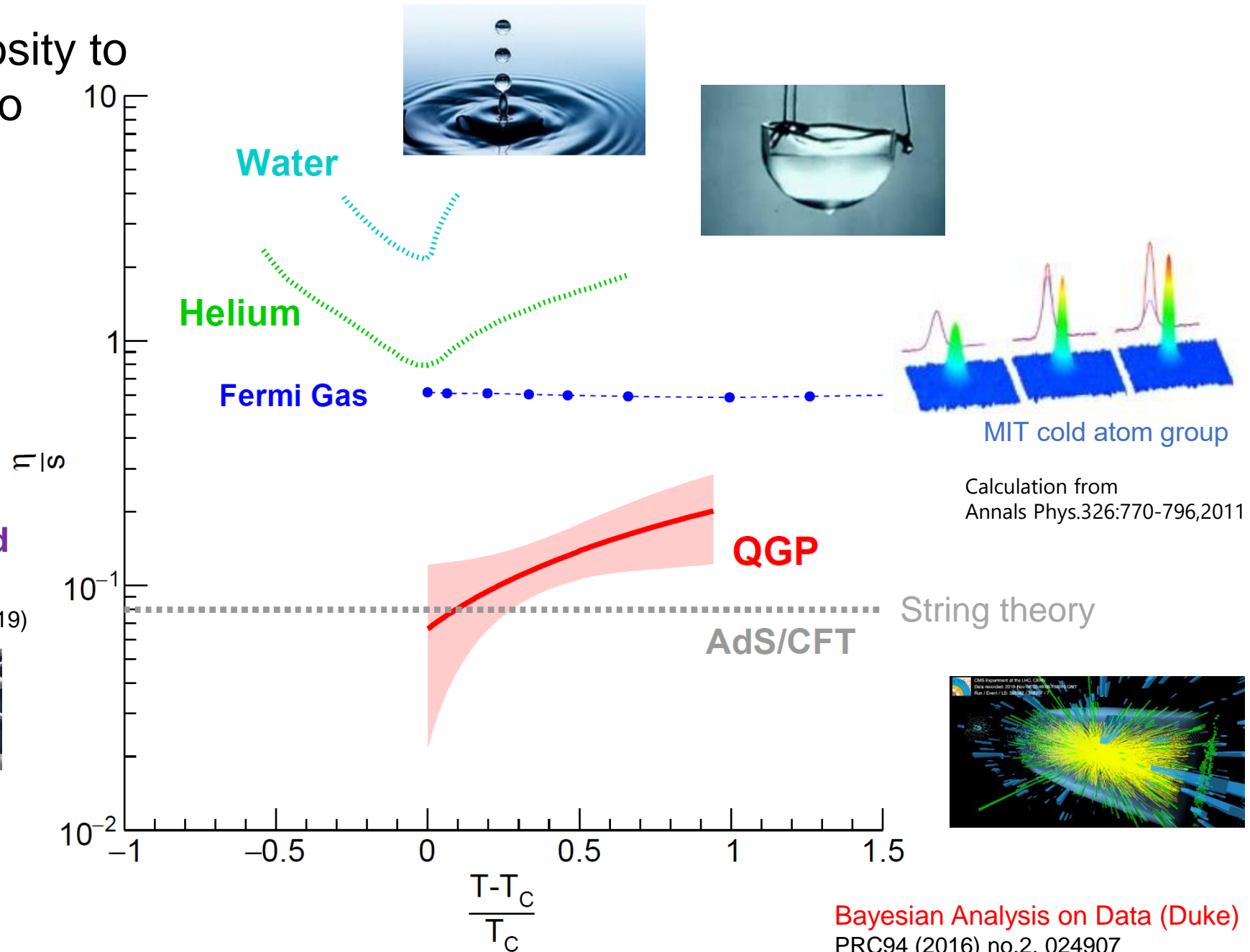
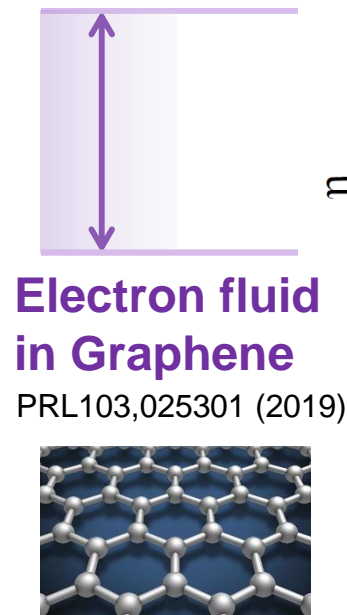
$$\eta/s = 0.08 \quad \tau = 0.2 \text{ fm}$$



Animation from L. G. Peng

Near Perfect Fluid

Shear viscosity to entropy ratio



Shear Viscosity of the QGP

Shear viscosity of the QGP is very large

$$\eta \approx 0.1\hbar s \approx 10^{12} \text{ erg s/cm}^3$$
$$\approx 10^{14} \text{ centipoise}$$

Almost as large as the **glass** ($>10^{15}$ cp)

However, due to the large QGP entropy s ,
QGP specific viscosity η/s is very small

* Note that the physics picture of QGP is not like slow-moving Honey or stationary glass! The strong force acting on QGP is also way bigger (a dynamic system)

Table 8.4.1. Viscosities η for some common materials in units of centipoise (10^{-2} erg s/cm³).

Substance	Temperature	Viscosity (cp)
Air	18°C	0.018
Water	0°C	1.8
Water	20°C	1
Water	100°C	0.28
Glycerin	20°C	1500
Mercury	20°C	1.6
<i>n</i> -Pentane	20°C	0.23
Argon	85K	0.28
He ⁴	4.2K	0.033
Superfluid He ⁴	< 2.1K	0
Glass		> 10 ¹⁵

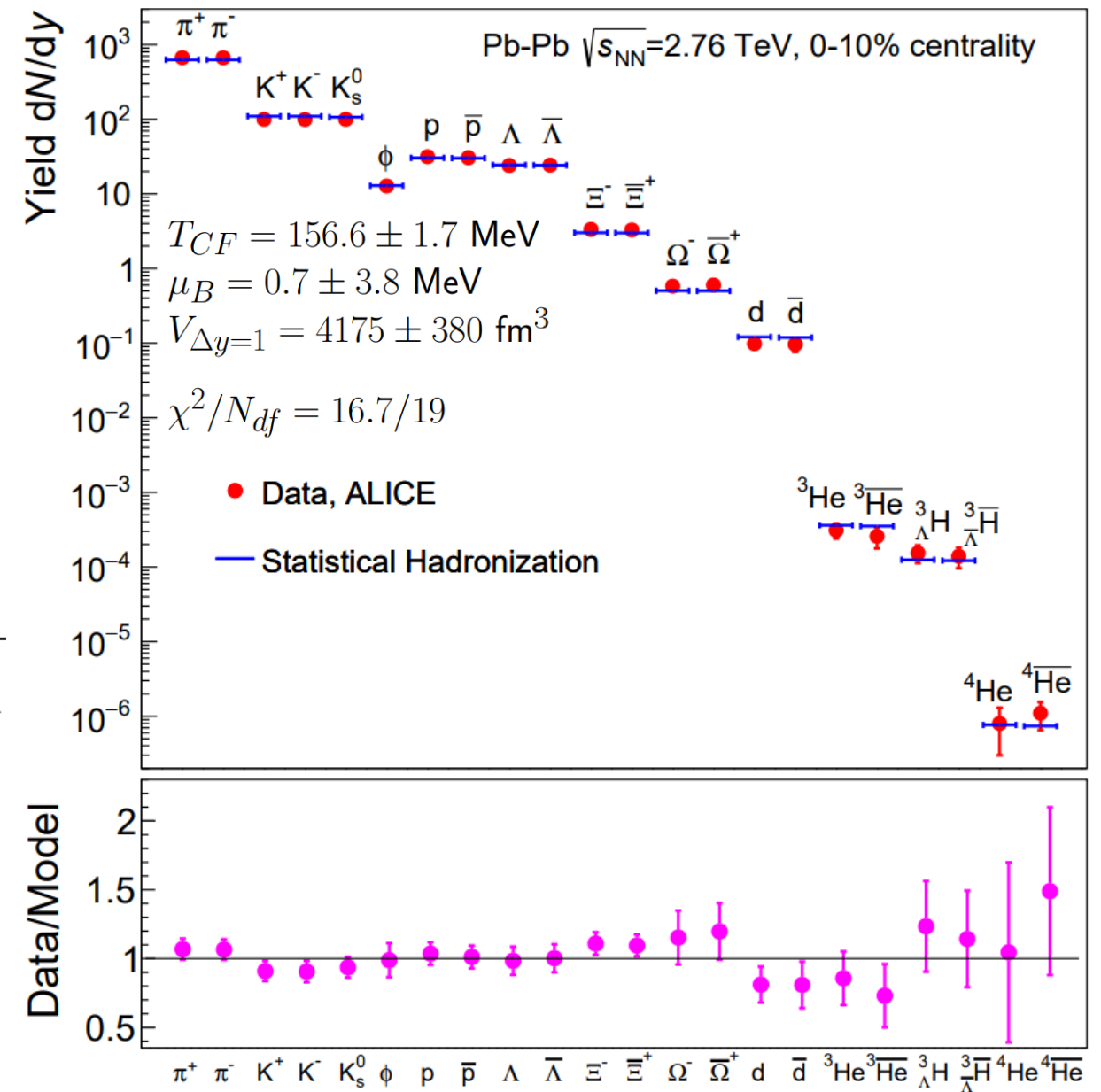
Note that, by popular convention, the designation “glass” is applied to any disordered material once its viscosity exceeds 10¹⁵cp.



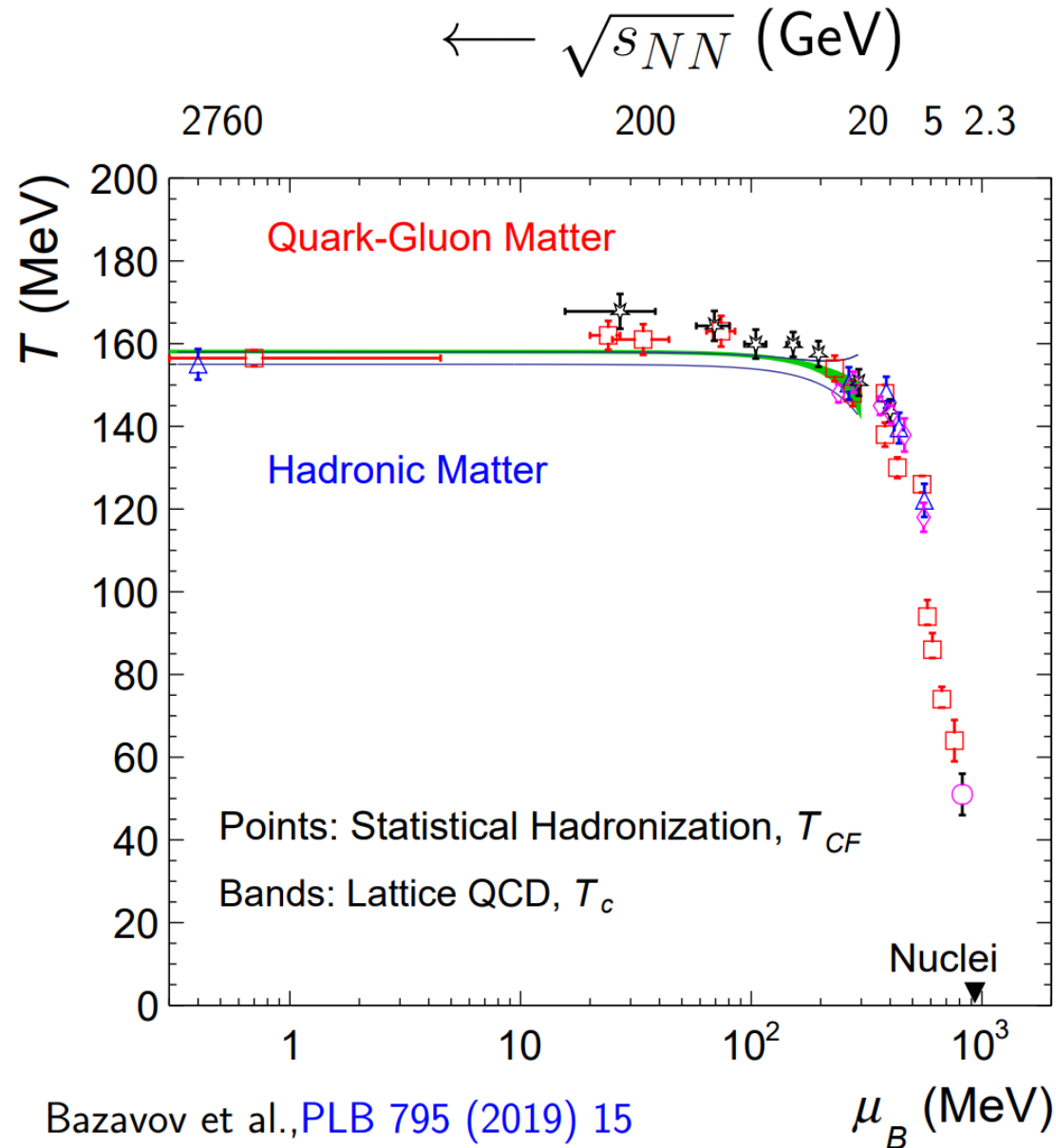
Statistical Hadronization

- Hadronization process: non-perturbative
- In **ee** and **pp**: string fragmentation, cluster
- Postulate: QGP cools into an equilibrated gas of hadrons
- Particle abundance produced in QGP could be described by calculation with partition function

$$n = \int N(E) d^3p \quad \text{and} \quad N(E) = \frac{D}{(2\pi)^3} \frac{1}{e^{\frac{E-\mu}{T}} \pm 1}$$
- Conserved quantum number, such as baryon number gives a chemical potential μ_B
- Temperature at the chemical freeze-out could be extracted



QGP Phase Diagram from Stat Hadronization Model



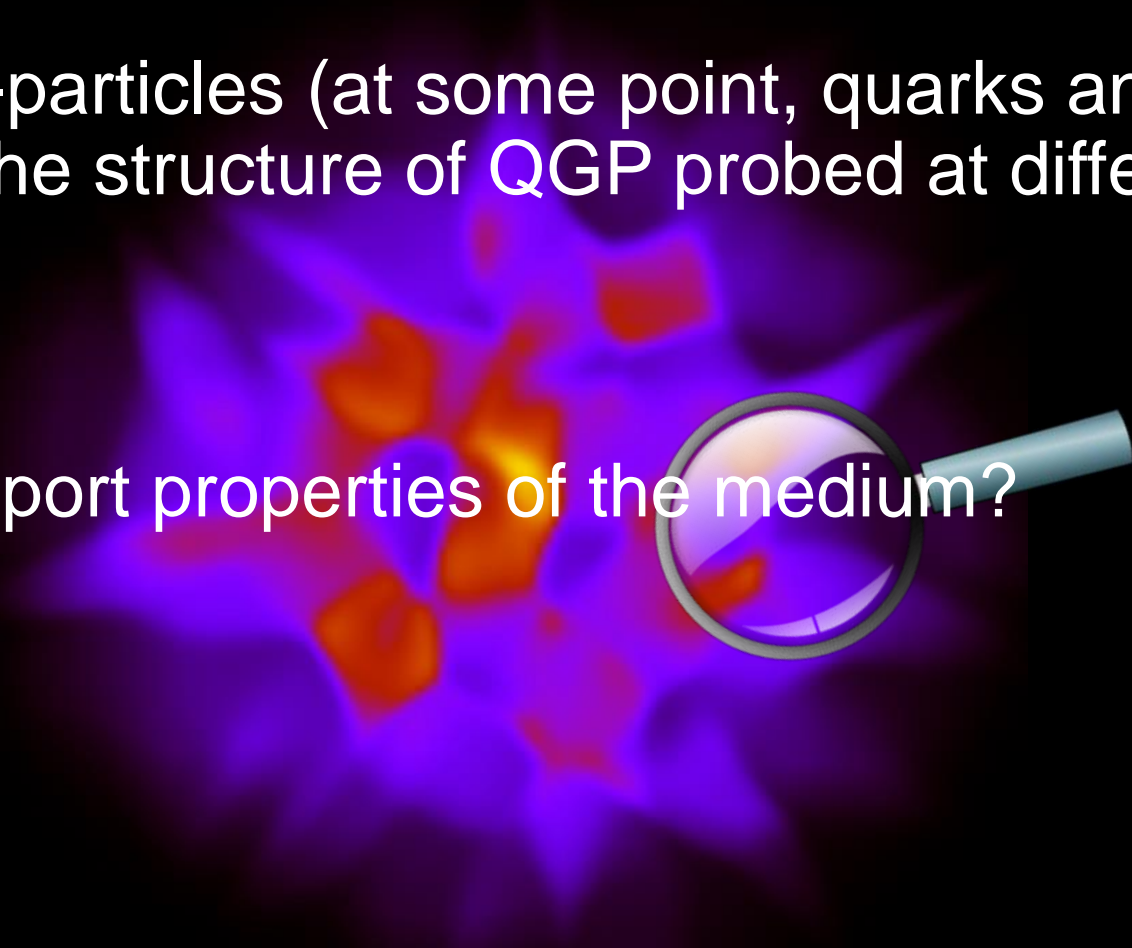
Bazavov et al., [PLB 795 \(2019\) 15](#)

Borsanyi et al., [PLB 370 \(2014\) 99](#)

- Extracted result from LHC: remarkable coincidence with Lattice QCD results
- At LHC, baryon chemical potential $\mu_B \sim 0$: produced matter and anti-matter as in the Early Universe
- At lower collision energy: more matter from beam remnants of the colliding nuclei, larger μ_B
- Critical point still to be located (RHIC Beam Energy Scan, FAIR)

Unanswered Questions

- How does the strongly interacting medium emerge from an asymptotic free theory?
- Can we see quasi-particles (at some point, quarks and gluons) in the Quark-Gluon Plasma? What is the structure of QGP probed at different length scales?
- What are the transport properties of the medium?



Probe the Quark Soup!

- How does the strongly interacting medium emerge from an asymptotic free theory?

Start from “un-thermalized” objects and see how they are thermalized in the Quark Soup

- Can we see quasi-particles (at some point, quarks and gluons) in the Quark-Gluon Plasma? What is the structure of QGP probed at different length scales?

“QGP Rutherford Experiment”

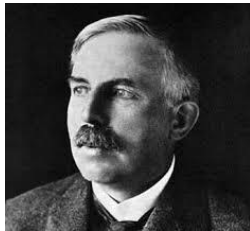
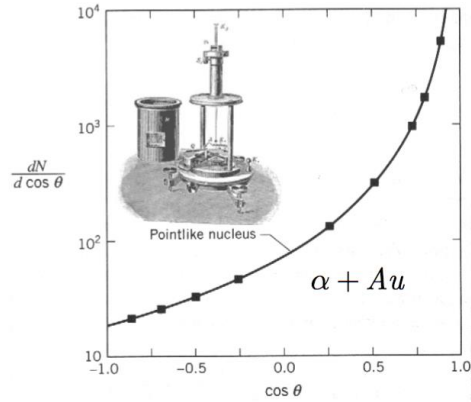
- What are the transport properties of the medium?

Study how Colored Probes are modified by QGP
Study how QGP respond to Colored Probes

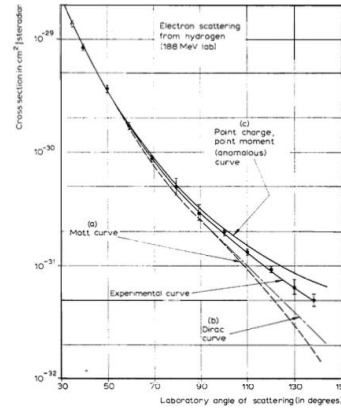


Hard Probes

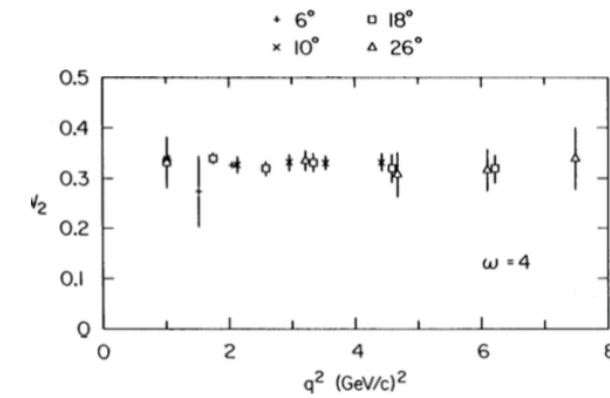
Atoms → Nuclei



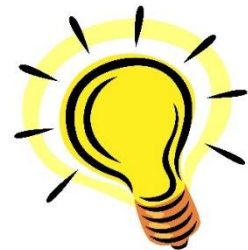
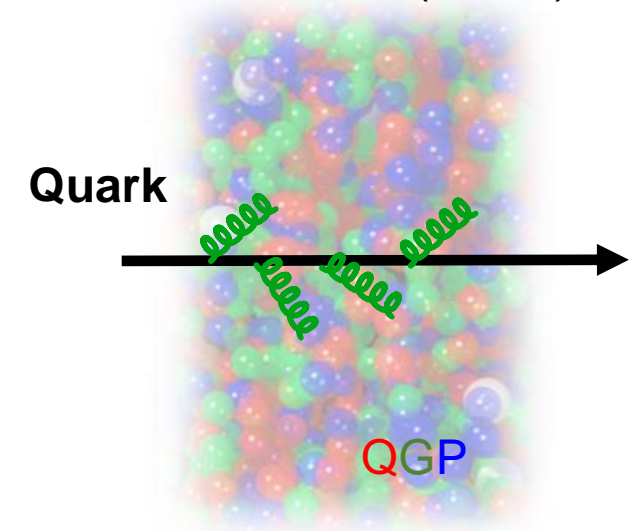
Nuclei → Nucleons



Nucleons → Quarks



Lifetime $O(10^{-24}s)$



James Bjorken (1982)

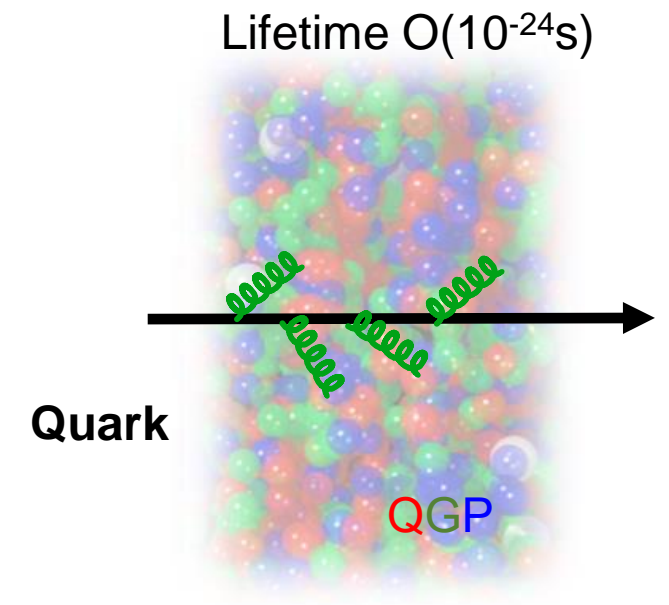
FERMILAB-PUB-82-059-T

Jet Quenching

Use **Energetic Quarks** to reveal QGP structure at various length scales

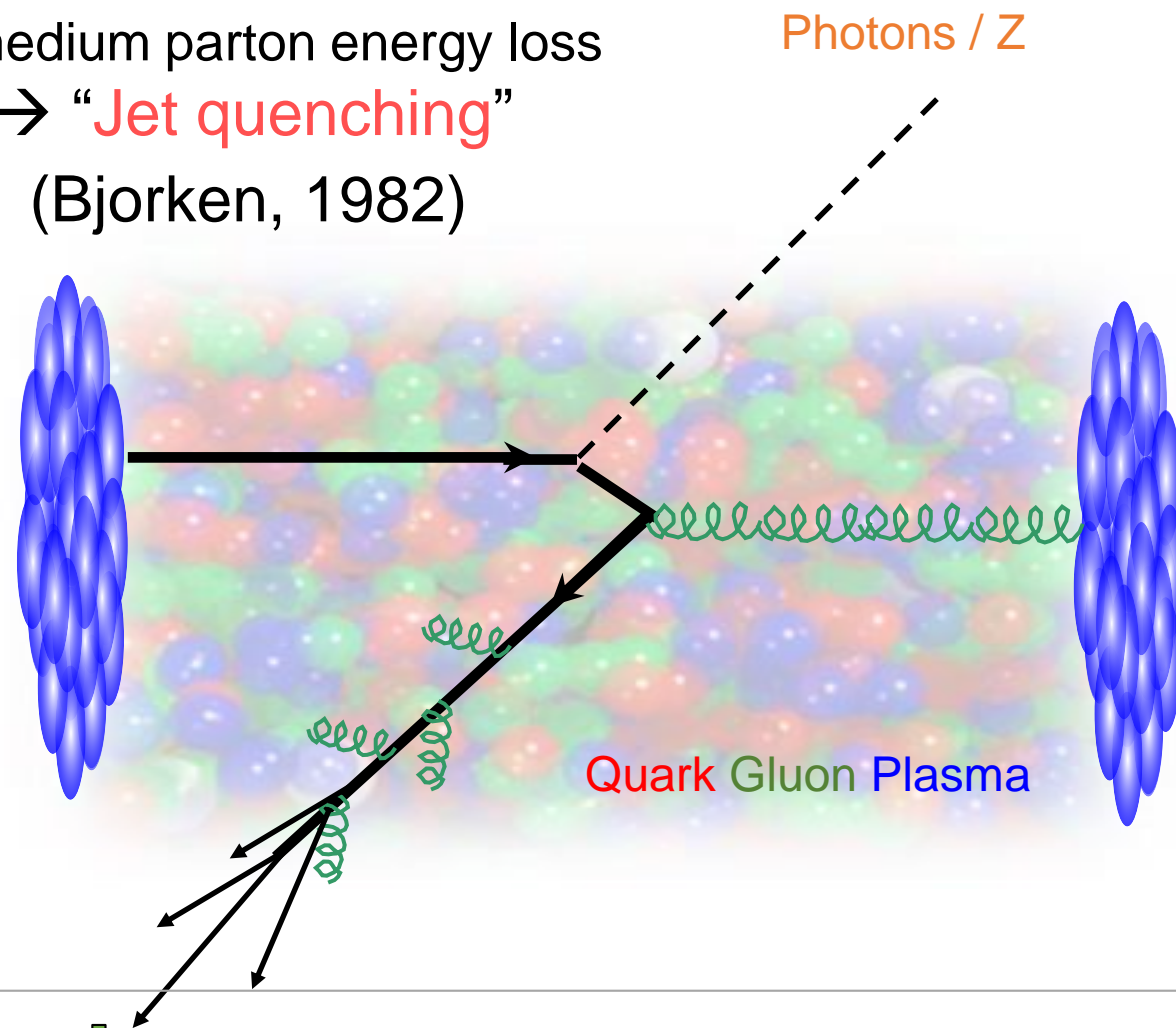
The Advantage of Hard Probes

- Momentum scale is well above QCD scale $\Lambda_{\text{QCD}} \sim 200 \text{ MeV}$
 - Described by perturbative methods (pQCD), calculations can be tested with pp scattering
- They are produced early: sensitive to full evolution of QGP
- Sensitive to short wave-length behavior of the medium
 - Transverse resolution of a radiated quanta: $\lambda \sim \frac{1}{Q} \ll 1 \text{ fm}$
 - Example: $Q=100 \text{ GeV} \rightarrow \lambda=0.05 \text{ fm}$
- Long relaxation time: “memory” of their initial conditions at production



Colorless and Colored Hard Probes

In medium parton energy loss
→ “**Jet quenching**”
(Bjorken, 1982)



Colorless Probes
Photons, electroweak bosons
Validation
Tag the initial state

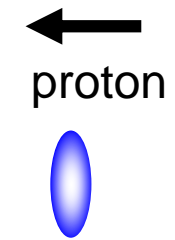
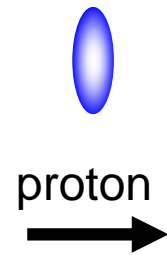
Transport coefficient \hat{q} , stopping power dE/dx ,
gluon density $\frac{dN_g}{dy}$, temperature T ...

Colored Probes:

Fast-moving high energy quarks and gluons,
Heavy quarks

Studies of the medium properties

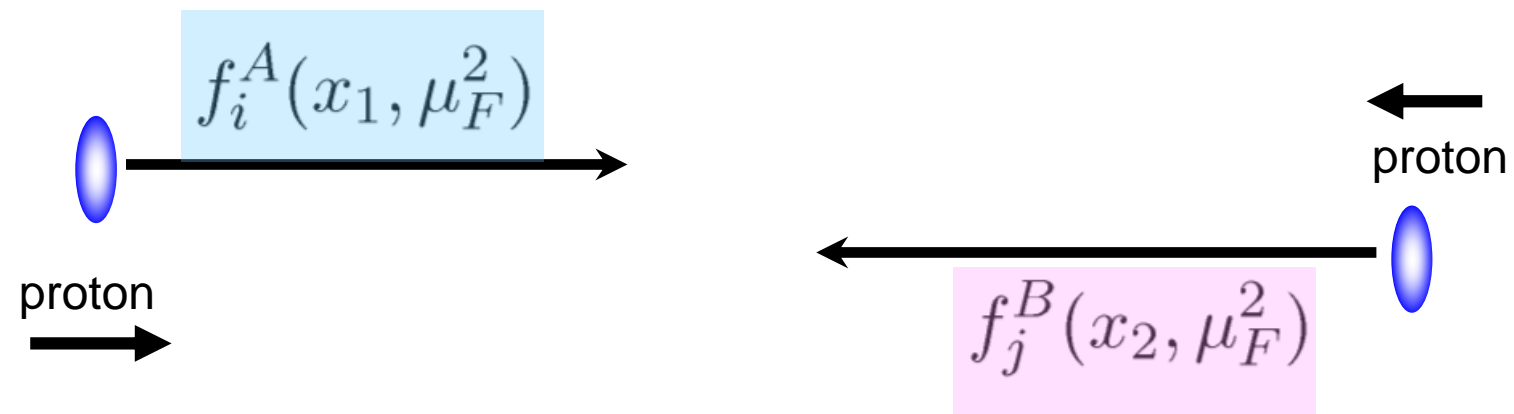
Factorization



Factorization

$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, \mu_F^2) \otimes f_j^B(x_2, \mu_F^2) \otimes \hat{\sigma}^{ij \rightarrow kl}$$

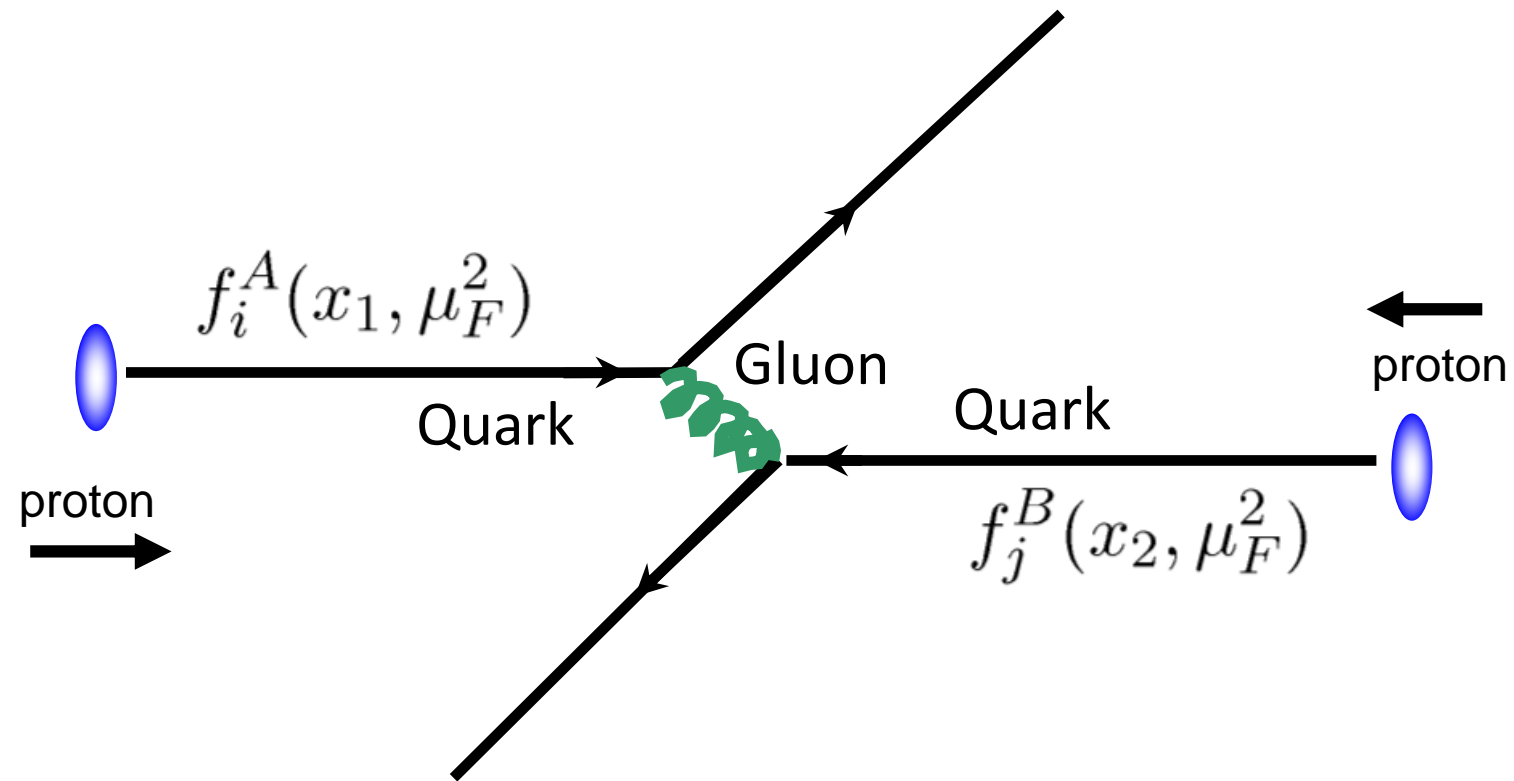
Parton Distribution Function (PDF)



Factorization

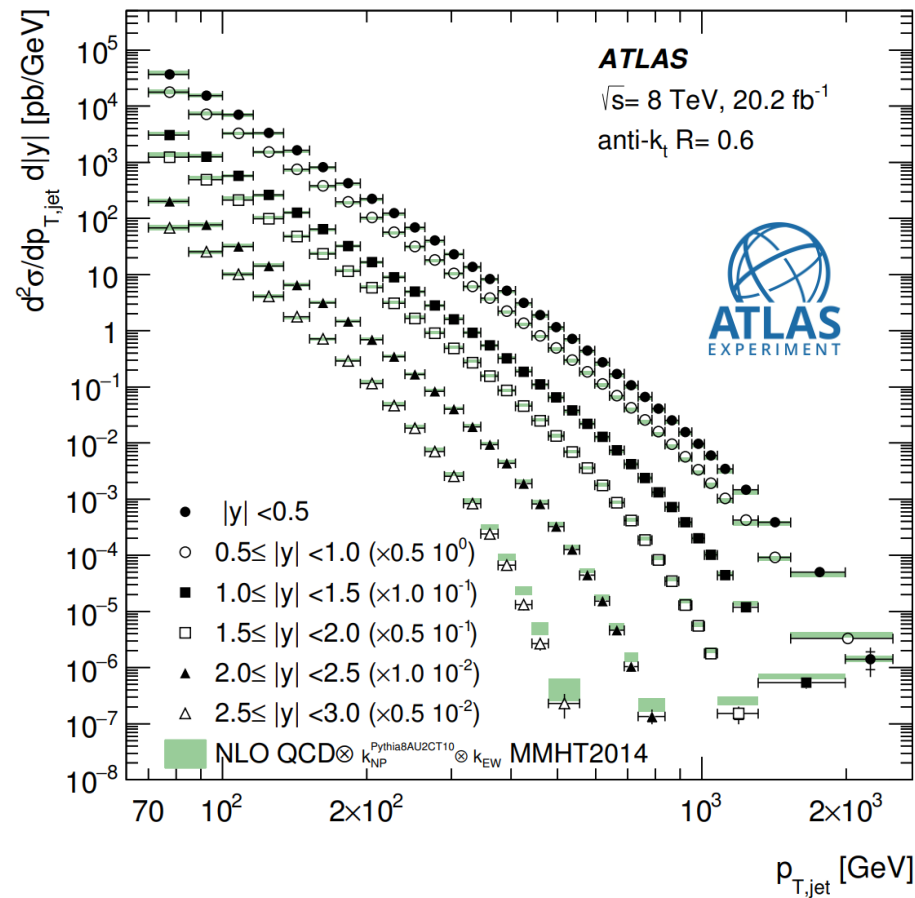
$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, \mu_F^2) \otimes f_j^B(x_2, \mu_F^2) \otimes \hat{\sigma}^{ij \rightarrow kl}$$

Parton Distribution Function (PDF) Cross-section of 2→2 process

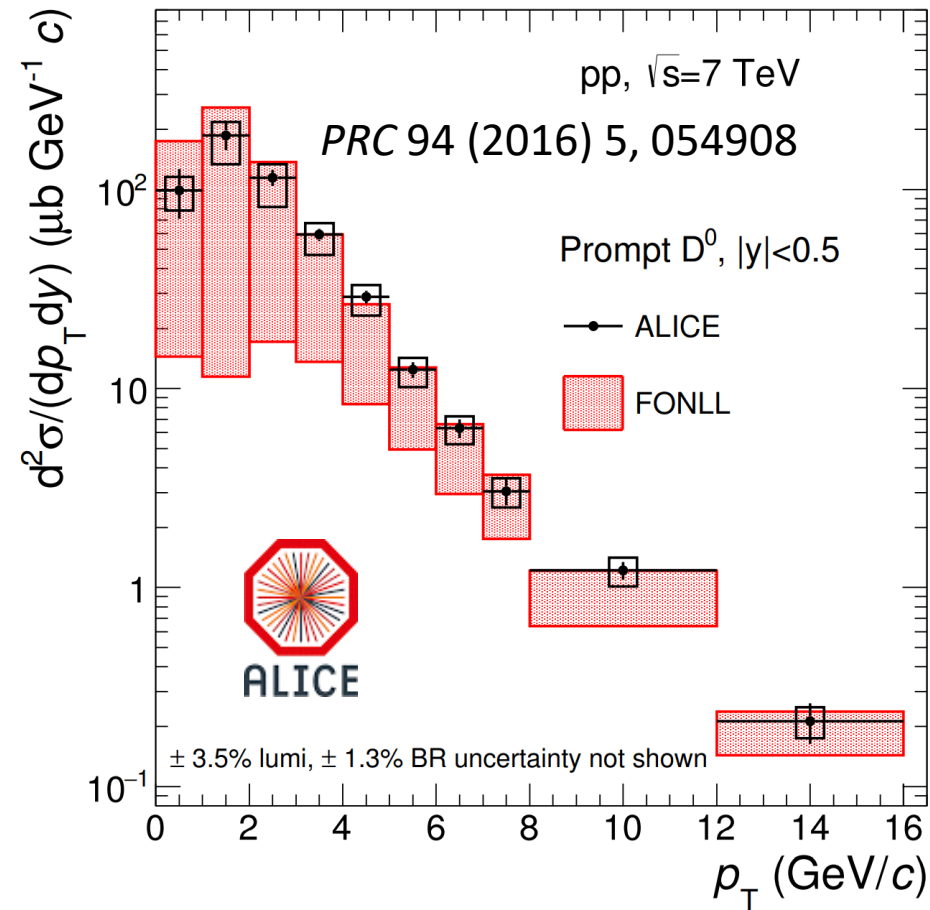


Jet and Heavy Flavor Meson Production in PP

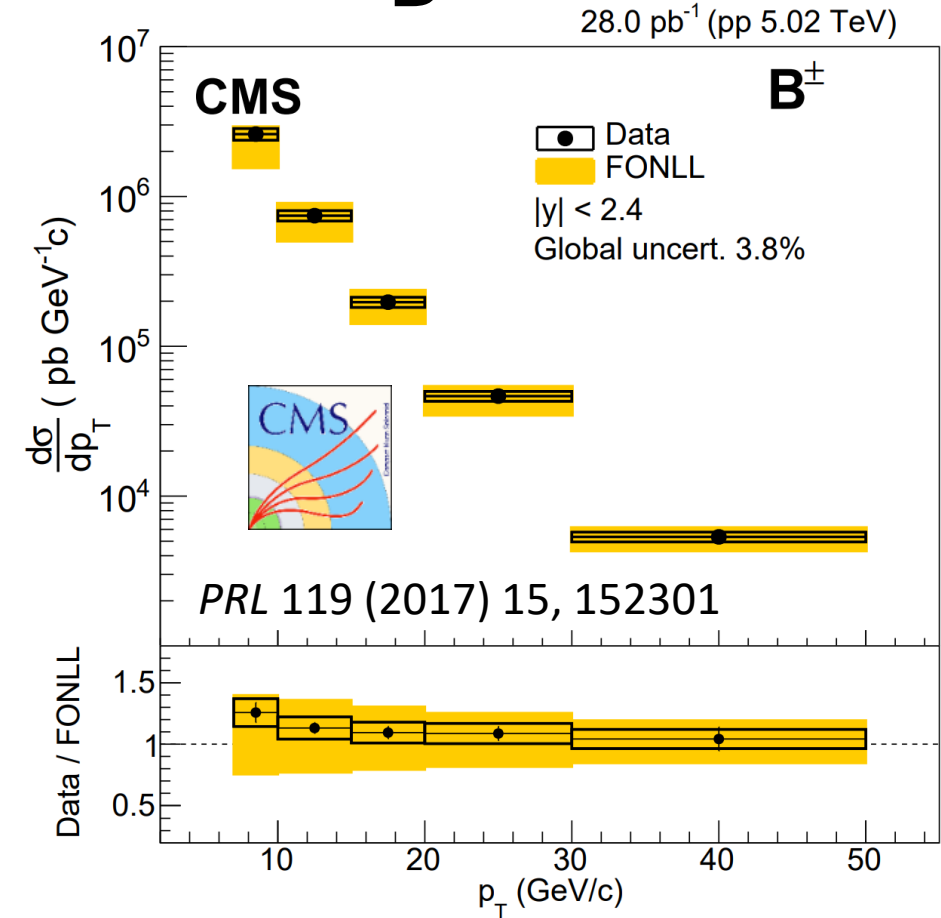
Jet



D^0



B^+

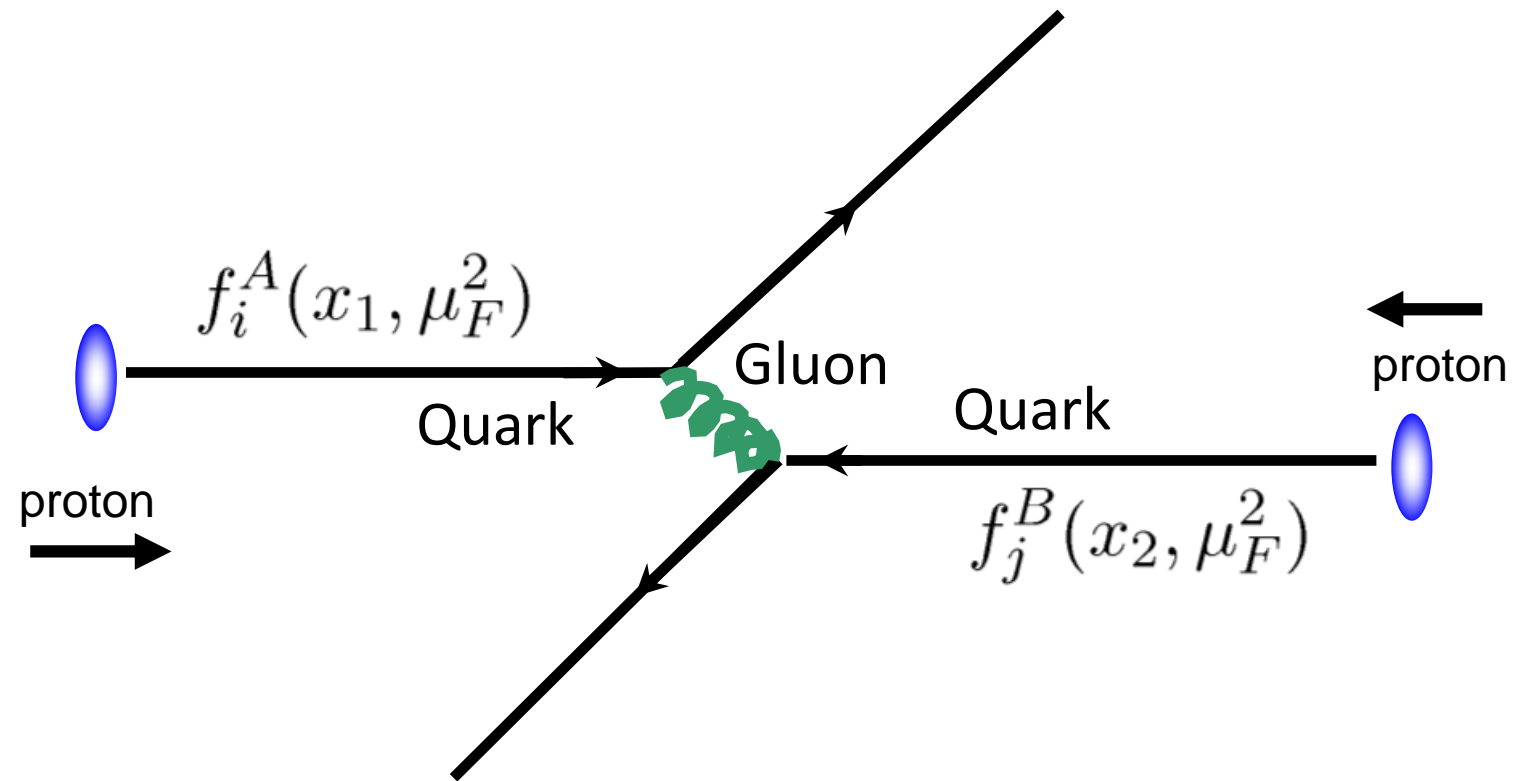


Jets and heavy flavor meson p_T spectra can be described by pQCD calculations

Factorization

$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, \mu_F^2) \otimes f_j^B(x_2, \mu_F^2) \otimes \hat{\sigma}^{ij \rightarrow kl}$$

Parton Distribution Function (PDF) Cross-section of 2→2 process

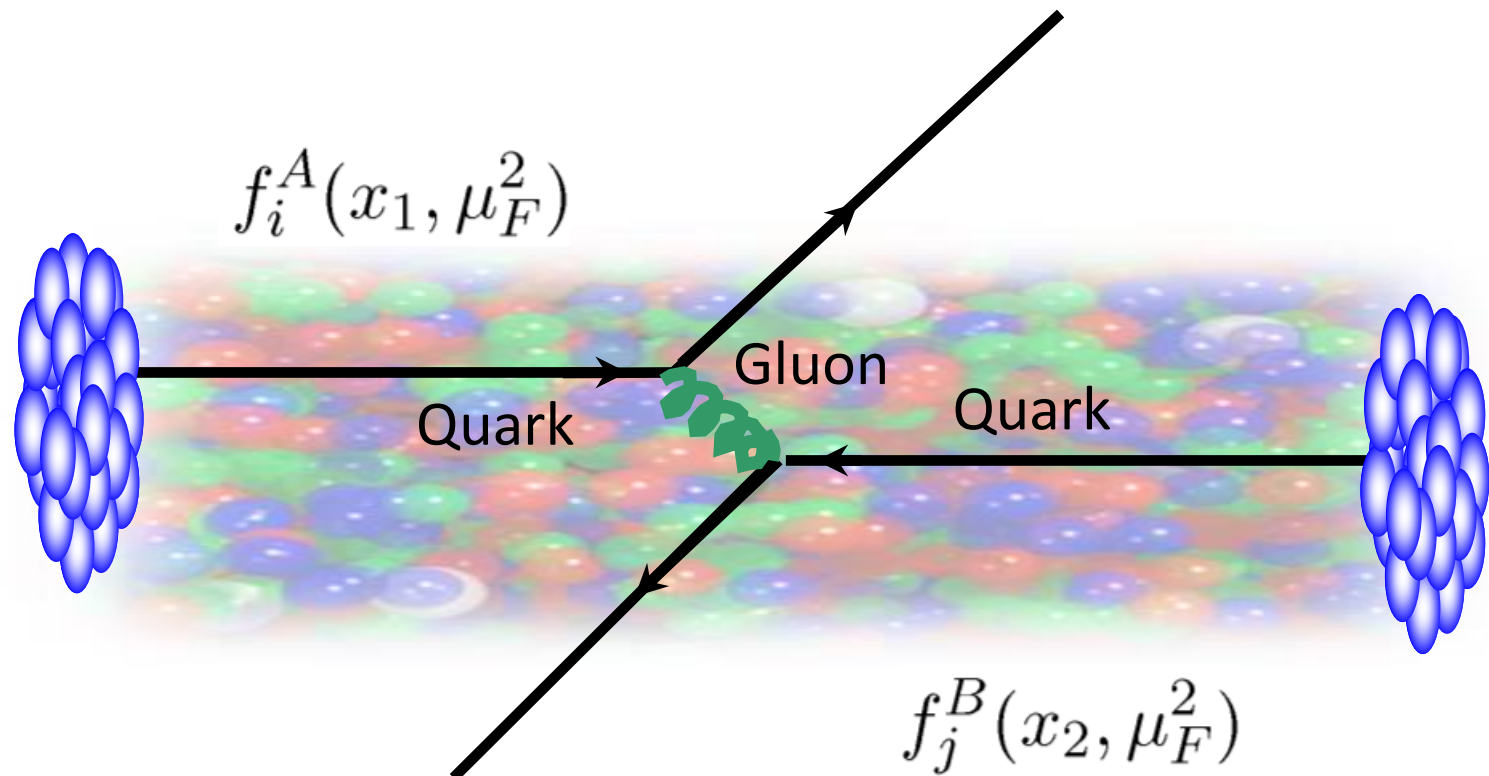
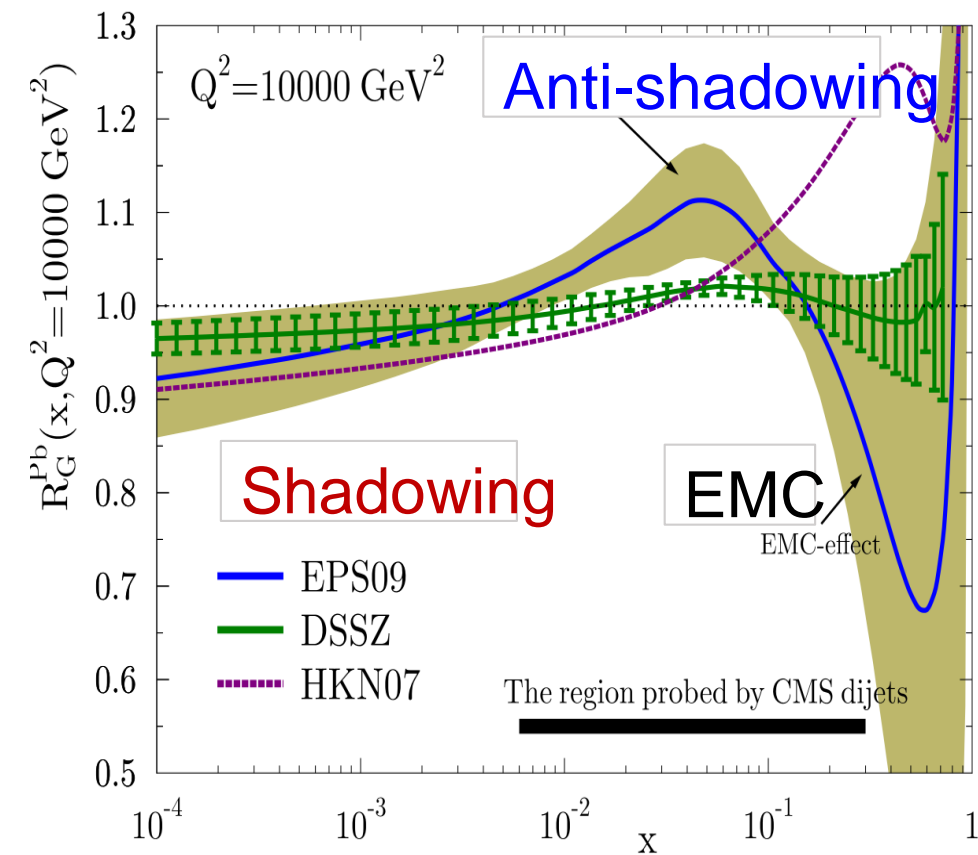


Factorization in AA collisions

$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, \mu_F^2) \otimes f_j^B(x_2, \mu_F^2) \otimes \hat{\sigma}^{ij \rightarrow kl}$$

Nuclear Parton Distribution Function (nPDF) Cross-section of 2→2 process

$$R = \frac{nPDF}{PDF}$$



Summary

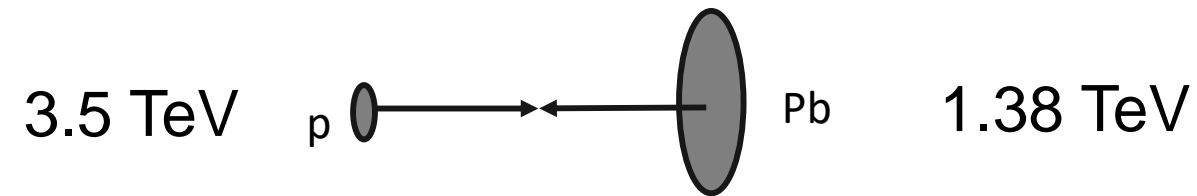
- Heavy-Ion Collisions: experiments that give access to Quark Gluon Plasma
- The medium produced in HI collisions is very dense, strongly interacting, flows like a perfect fluid.
- The abundance of the final state baryons and mesons can be described by a statistical hadronization model
- Next: Hard Probes of QGP

Bonus Material



Nuclear Parton Distribution Function

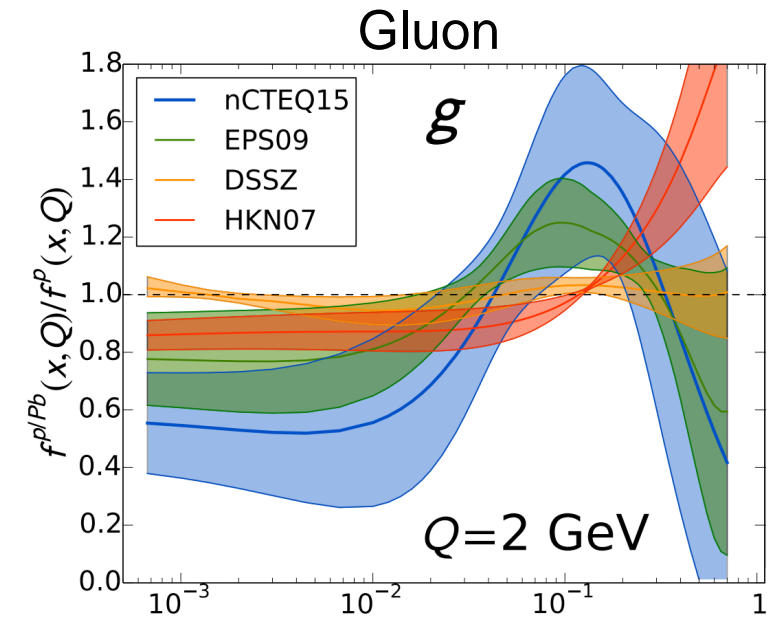
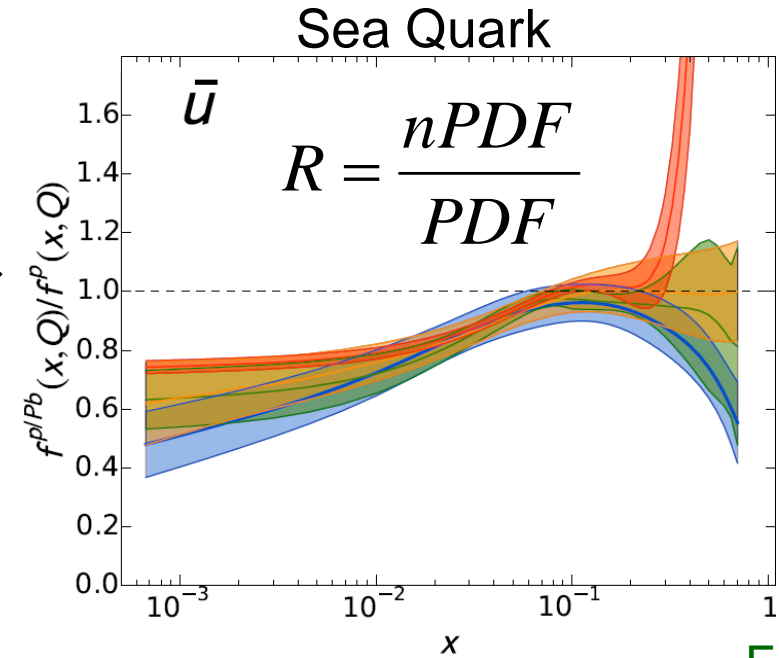
Jet for constraining the nuclear parton distribution function



Parton Distribution Function

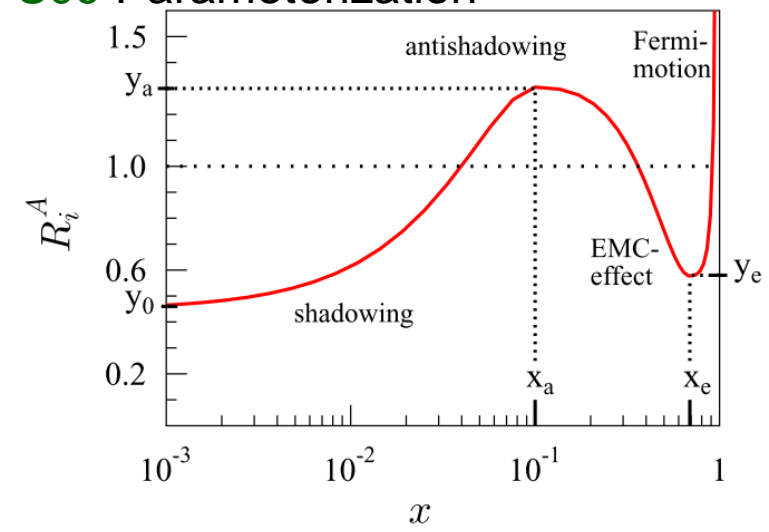
Nuclear Parton Distribution Functions (nPDF)

- Deep Inelastic Scattering Data
- Drell-Yan Data
- RHIC Pion Data



EPS09 Parameterization

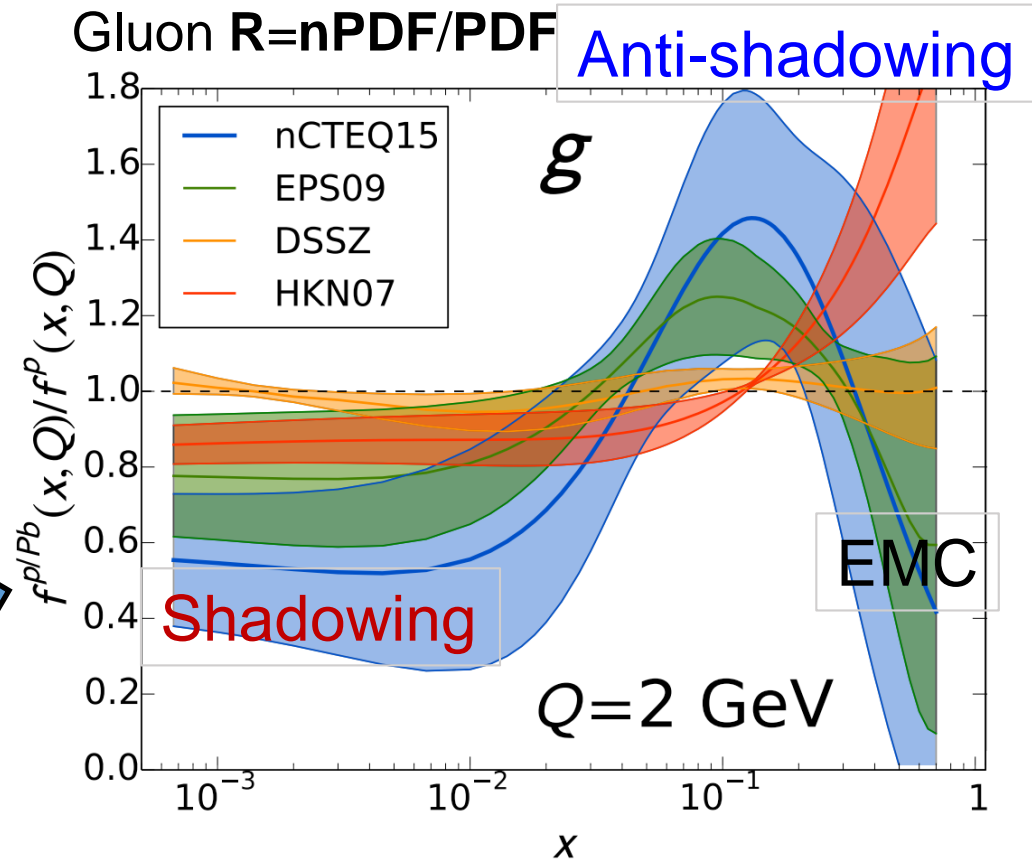
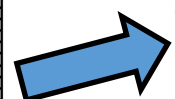
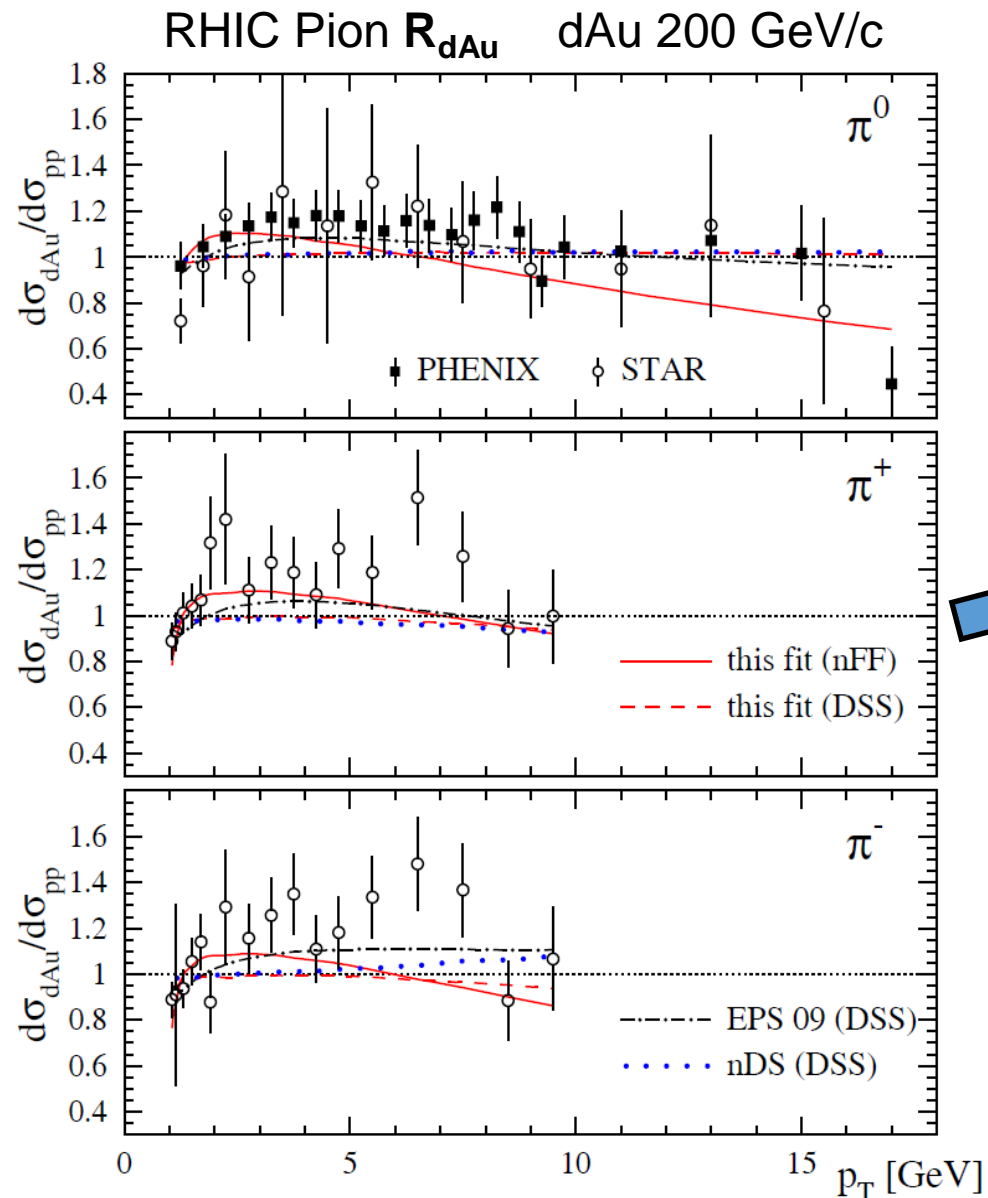
	Q^2 cutoff	DIS	DY	PHENIX Pion	STAR Pion
HKN07	1	V	V		
EPS09	1.69	V	V	V	
DSSZ	1	V	V	V	V
nCTEQ15	4	V	V	V	V



EPPS16: with LHC pPb data (W,Z, jets)

Different interpretation of the pion data

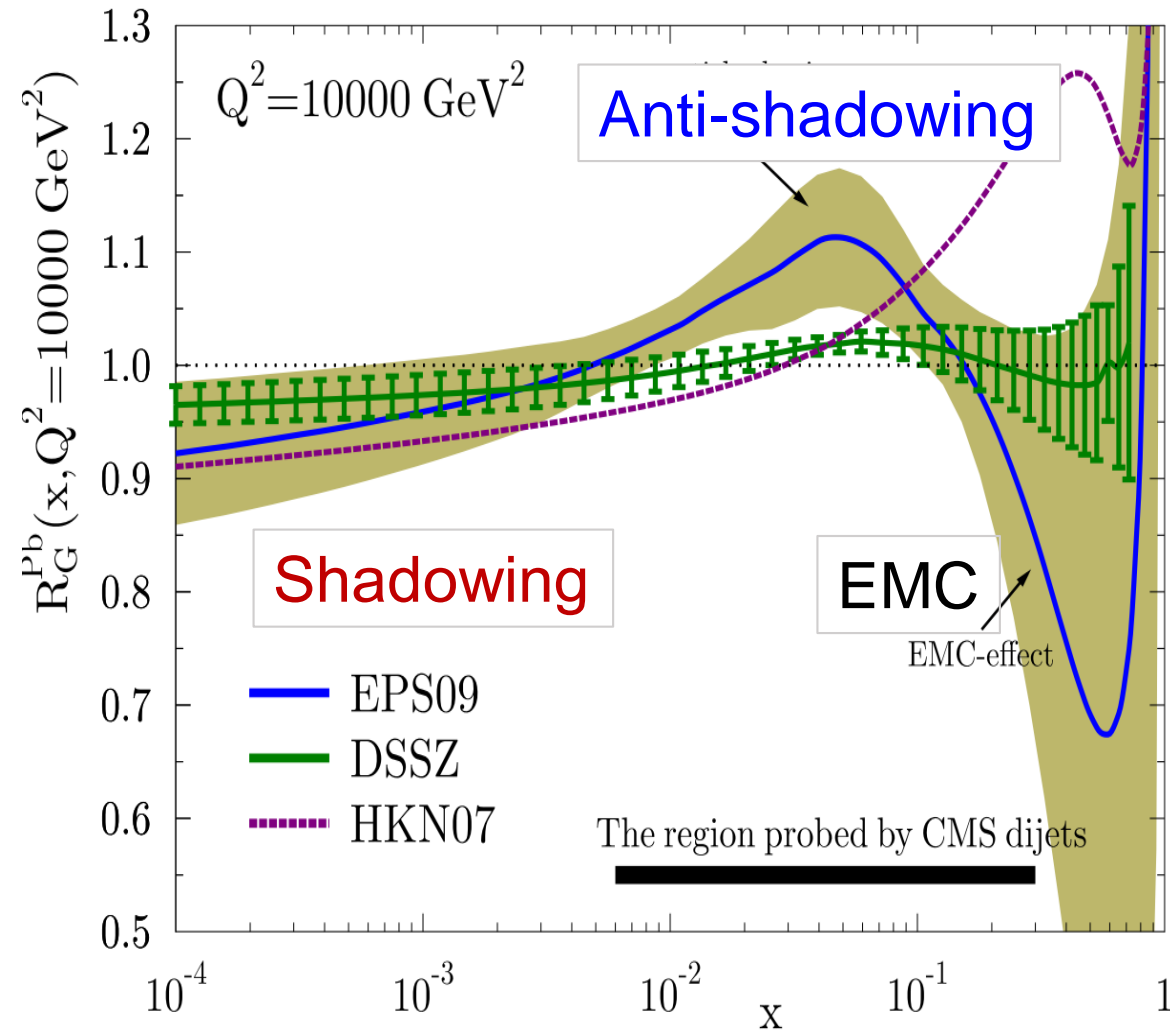
Hadron observables: sensitive to possible modifications of **fragmentation function** and **hadronization** → **Different interpretation of the data!**



- **EPS09** & **nCTEQ15**: hint of **anti-shadowing** and **EMC effect** of gluon nPDF
- **DSSZ**: modification of parton-to-pion fragmentation function in heavy ion collisions and no gluon anti-shadowing

nPDF modification at large Q^2

$$R = \frac{nPDF}{PDF}$$

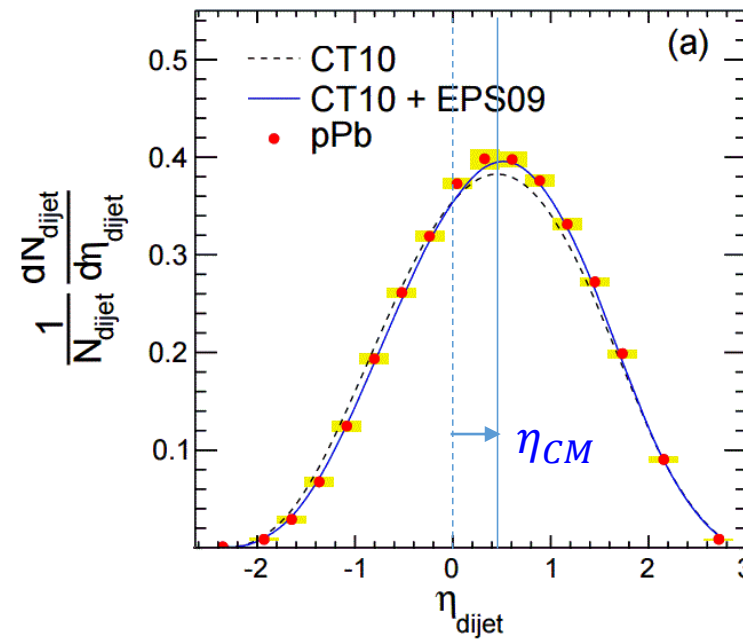


Nuclear modification of hard scattering involving large momentum transfer due to PDF is small (at the order of 10%)

Dijet pseudorapidity in the LAB Frame

Idea: Angular distributions of high p_T dijets

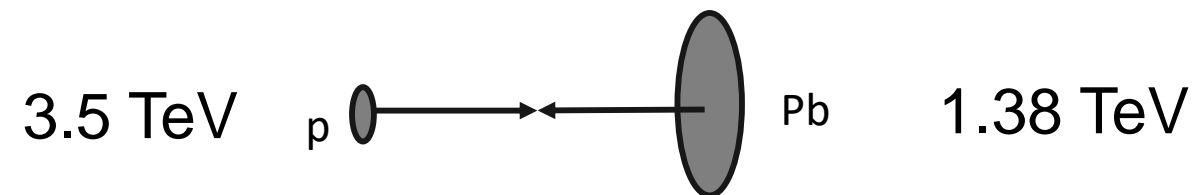
CMS pPb 35 nb⁻¹
 $\sqrt{s_{NN}} = 5.02$ TeV
 $p_{T,1} > 120$ GeV/c
 $p_{T,2} > 30$ GeV/c
 $\Delta\phi_{1,2} > 2\pi/3$
 All $E_T^{4 < |\eta| < 5.2}$



$$\eta_{dijet} = \frac{\eta_1 + \eta_2}{2}$$

$$\propto 0.5 \log\left(\frac{x_p}{x_{Pb}}\right) + \eta_{CM}$$

- Jets: Less sensitive to fragmentation functions and hadronization effects
- Can be calculated with pQCD with small theoretical uncertainties
- Normalized distribution: lead to smaller theoretical and experimental uncertainties



Distribution shift to positive value due to asymmetric proton and lead ion beam energy

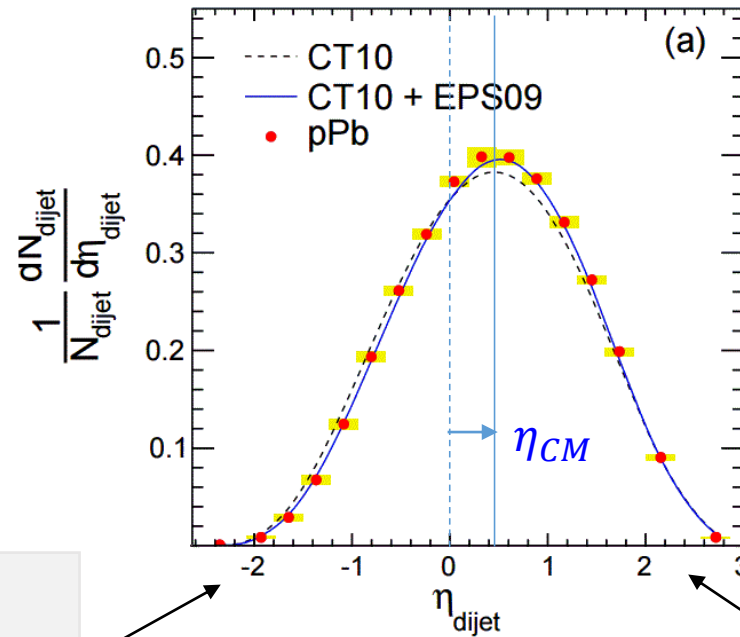
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Dijet pseudorapidity in the LAB Frame



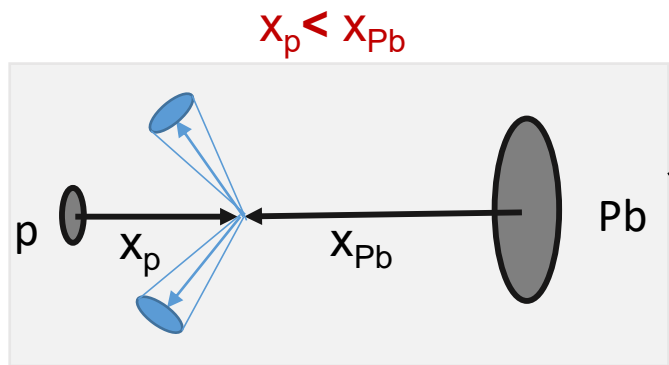
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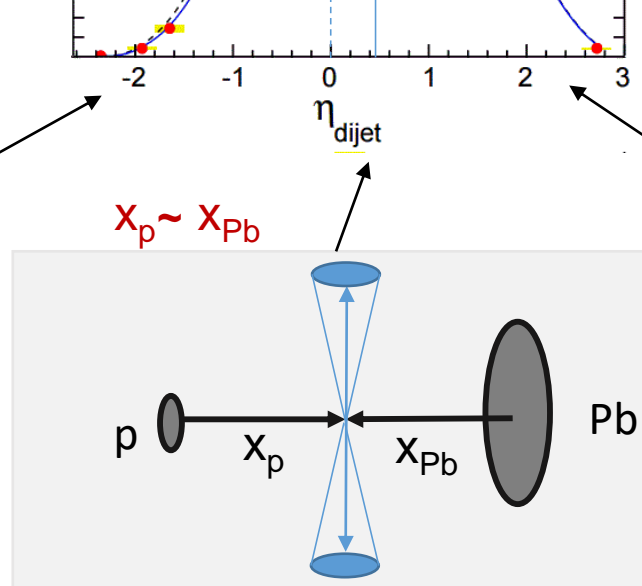


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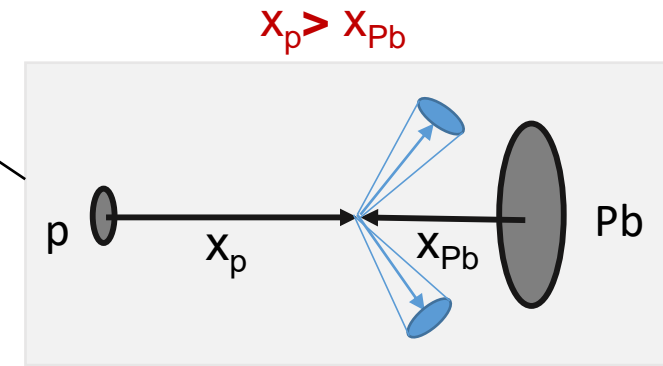
$$\propto 0.5 \log\left(\frac{x_p}{x_{Pb}}\right) + \eta_{CM}$$



Sensitive to EMC effect



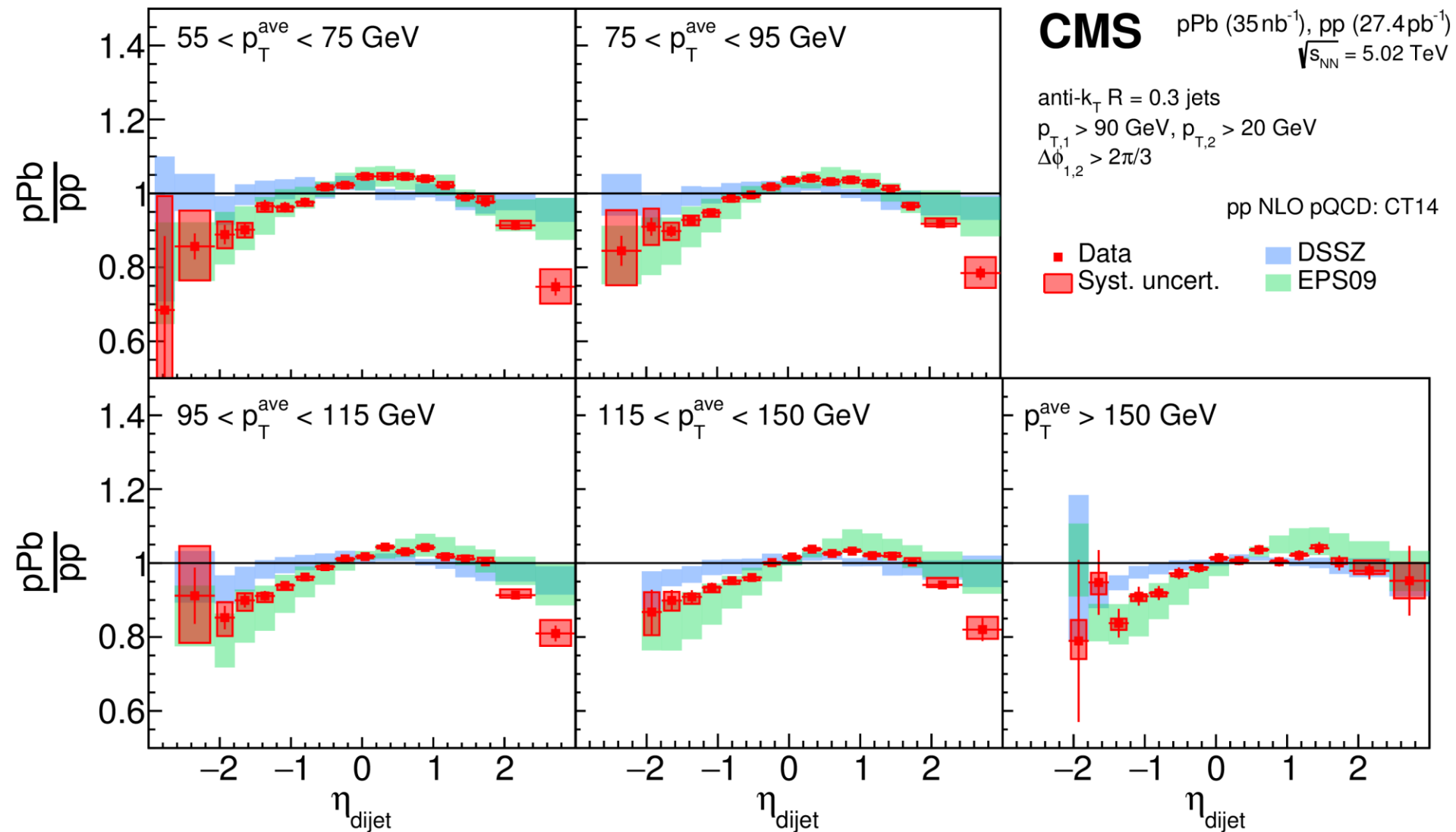
Sensitive to anti-shadowing



Sensitive to shadowing

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Observation of nPDF effect



- **EPS09**: hint of **anti-shadowing** and **EMC effect** of gluon nPDF
- **DSSZ**: modification of parton-to-pion fragmentation function in heavy ion collisions and no gluon anti-shadowing