

# Testing dark matter in galaxies with the Normalized Additional Velocity Distribution

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## Based on:

Alejandro Hernandez-Arboleda, Davi C. Rodrigues, Aneta Wojnar [[2204.03762](https://arxiv.org/abs/2204.03762)]

Code available at: <https://github.com/davi-rodrigues/NAVanalysis>



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**Cosmo22**

Rio de Janeiro, Brazil

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# Galaxy rotation curves: basics

Data from SPARC, plot from MAGMA  
[<https://github.com/davi-rodrigues/MAGMA>]

## Gas contribution:

Derived from the 21 cm radiation surface brightness.

Hydrogen density found from hyperfine transition.

Gas density  $\rho_{\text{gas}} = 1.33 \rho_{\text{H}}$ , from BBN.

$$V_{\text{gas}}^2 = r \partial_r \Phi_{\text{gas}}, \text{ with } \nabla^2 \Phi_{\text{gas}} = 4\pi G \rho_{\text{gas}}.$$

## Stellar contribution:

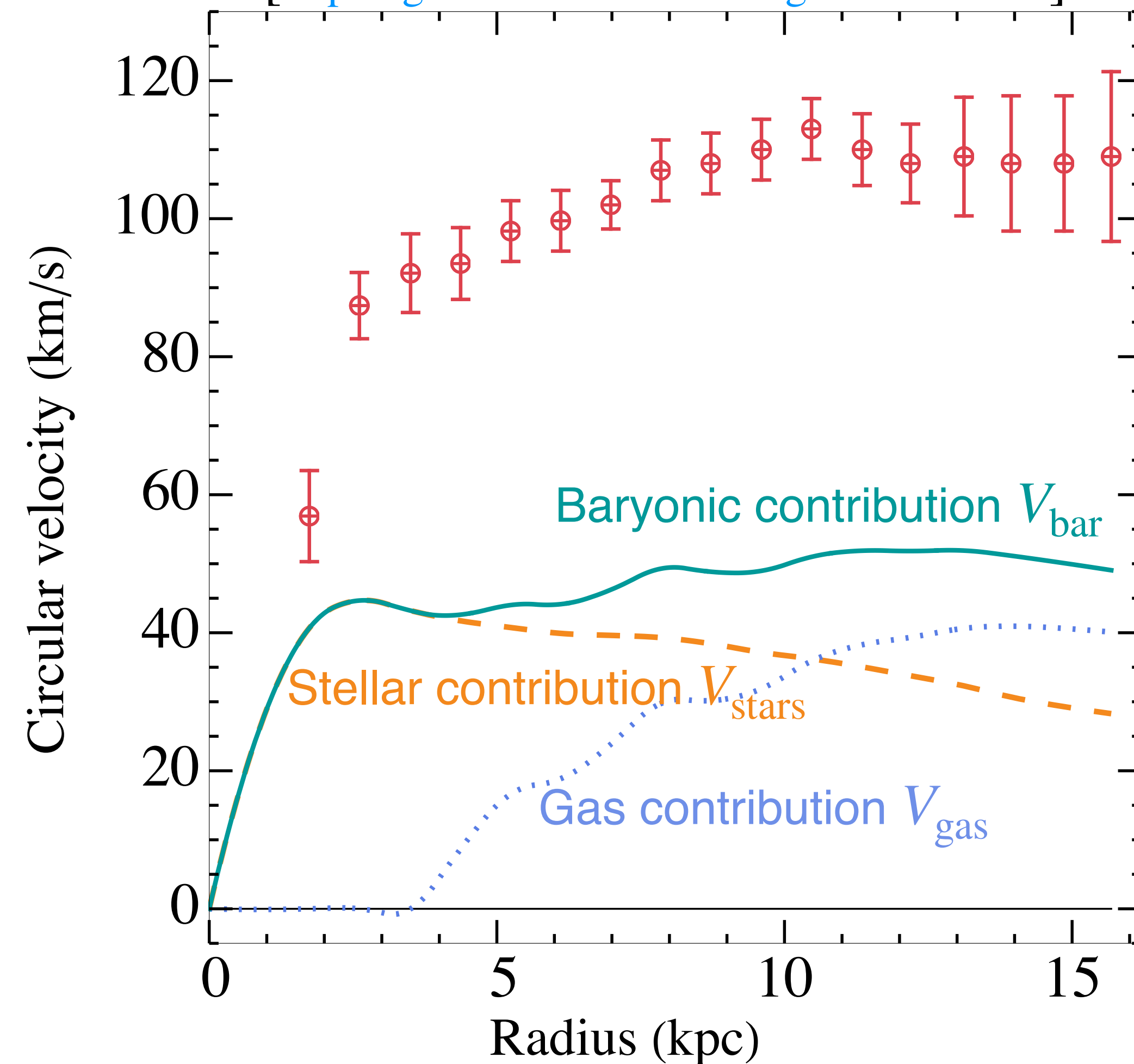
Derived from the stellar surface brightness (near infrared).

Stellar density depends on stellar population models.

For the Spitzer 3.6  $\mu\text{m}$  band (e.g., [Meidt et al ApJ 2014](#)):

$$Y_* = 0.50_{-0.10}^{+0.13} \text{ (dimensionless mass-to-light ratio, stellar disk)}$$

$$V_*^2 = r \partial_r \Phi_*, \text{ with } \nabla^2 \Phi_* = Y_* 4\pi G \rho_*|_{Y_*=1}.$$



$$V_{\text{bar}}^2 = V_{\text{stars}}^2 + V_{\text{gas}}^2$$

# Testing a DM profile for a given galaxy

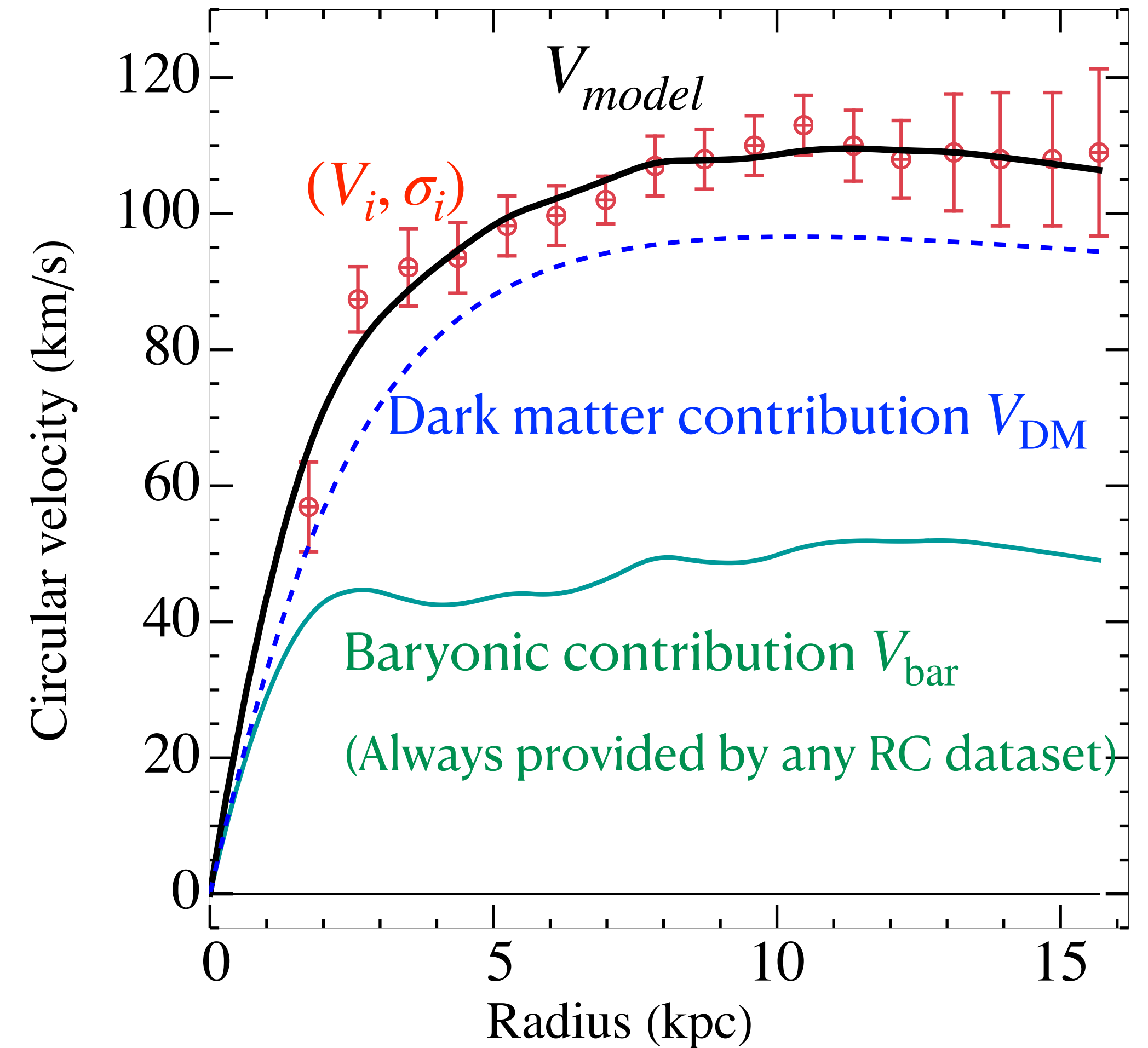
Typical procedure:

- One assumes a DM profile with free parameters (e.g., NFW, Einasto, Burkert, DC14...)
- For each galaxy RC data, the halo is fitted together with relevant baryonic uncertainties, if any (e.g.,  $Y_*$ ,  $\delta D$ ,  $\delta i$ ).

The maximization of the likelihood yields the best fit model parameters ( $p_a$ )

$$-\ln \mathcal{L}(p_a) \propto \chi^2(p_a) = \sum_i \left( \frac{V_{model}(p_a, R_i) - V_i}{\sigma_i} \right)^2$$

$$V_{model}^2 = V_{bar}^2 + V_{DM}^2$$



# Which model is better?

A simple and common approach: compute  $\chi_{\text{red}}^2$  for **each** galaxy.

- Models that yield the minimum average  $\langle |\chi_{\text{red}}^2 - 1| \rangle$  for a sample are the best.
- Variation: instead of the average, use the CDF distribution of  $\chi_{\text{red}}^2$  [[Katz et al, MNRAS 2016](#)]

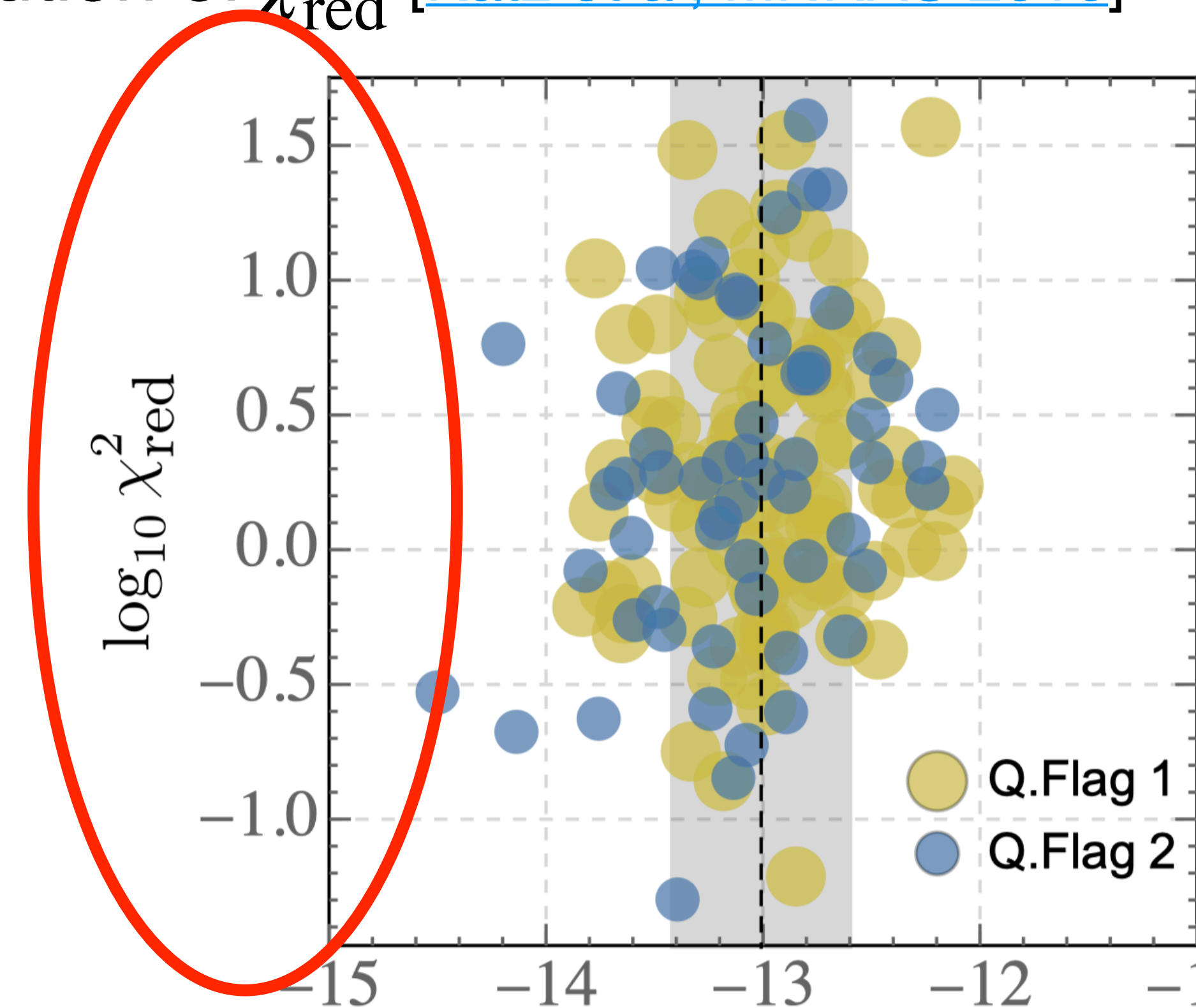
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**Problem:** DM halo profiles are nonlinear models, the rule  $\chi_{\text{red}}^2 \sim 1$  is not correct. [[Andrae et al 1012.3754](#)].

**Issue:** Computational time. Each galaxy needs to be carefully *individually* studied, even though the purpose is the overall sample result.



[[Rodrigues et al Nat.Ast. 2018](#)]

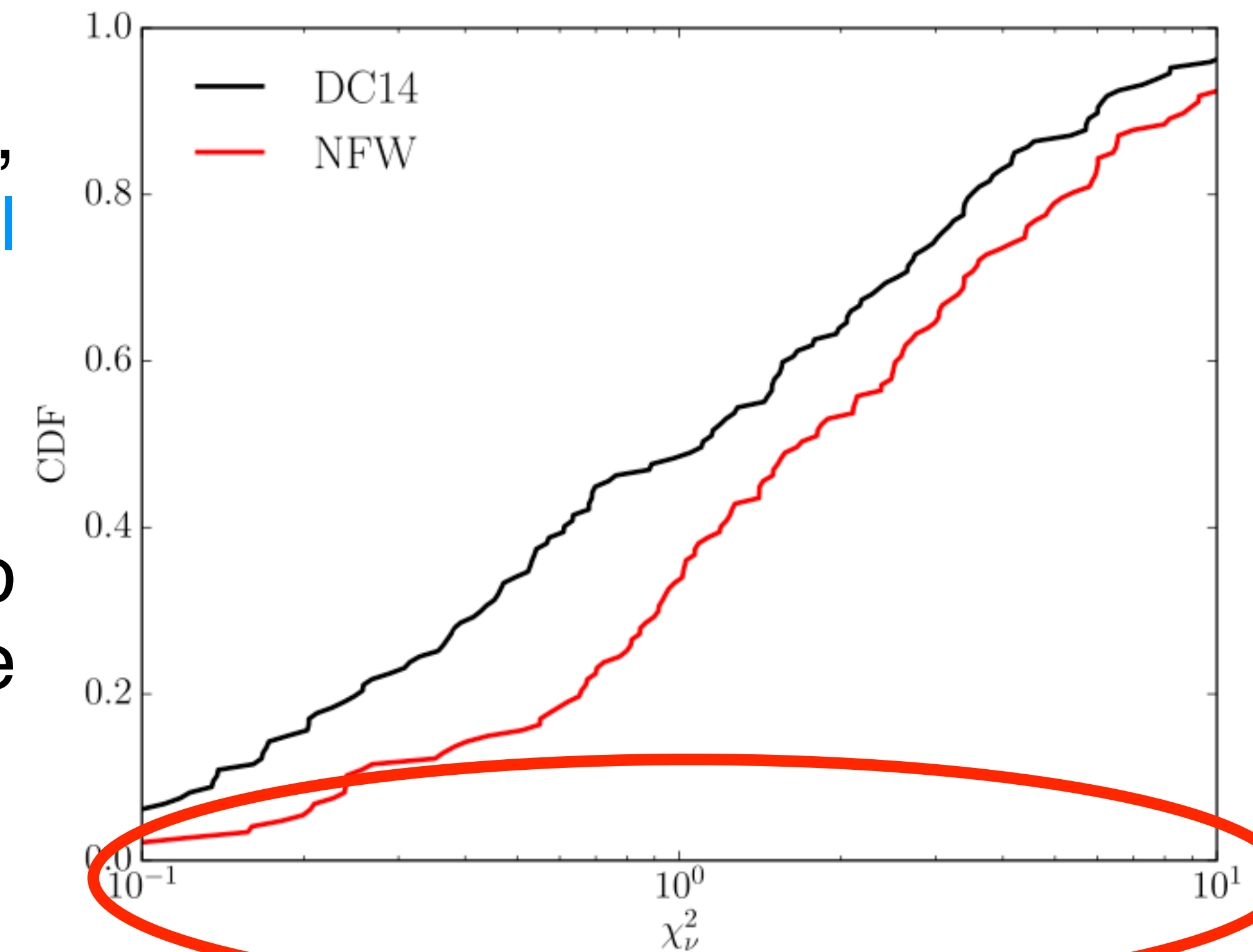
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- [[Katz et al, MNRAS 2016](#)]

# SPARC and modified gravity

- The SPARC galaxy sample [[Lelli et al AJ 2016](#)] is a well organized and well known galaxy RC sample. It includes 175 late-type galaxies with high quality data, with emphasis to the stellar component.
- From these, 153 are considered to be specially suitable for galaxy modeling (highly symmetric and with  $i \geq 30^\circ$ ).
- However, there is no public data on the complete  $3D$  baryonic distribution.
- [[Green, Moffat PDU 2019](#)] develop their own  $3D$  baryonic models in part based on the available SPARC data plus analytical approximations that can be found in the literature. This lead to systematical changes in the RC's.
- [[Naik et al MNRAS 2019](#)] use exponential profiles to mimic the stellar and the gaseous parts of each galaxy. The latter approximation is less suitable.

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- We focus on one relevant rotation curve feature: its shape

# Normalized Additional Velocity

- One can define the observational (model independent) additional velocity as

$$\Delta V_{\text{obs}}^2(r) \equiv V_{\text{obs}}^2(r) - V_{\text{bar}}^2(r) .$$

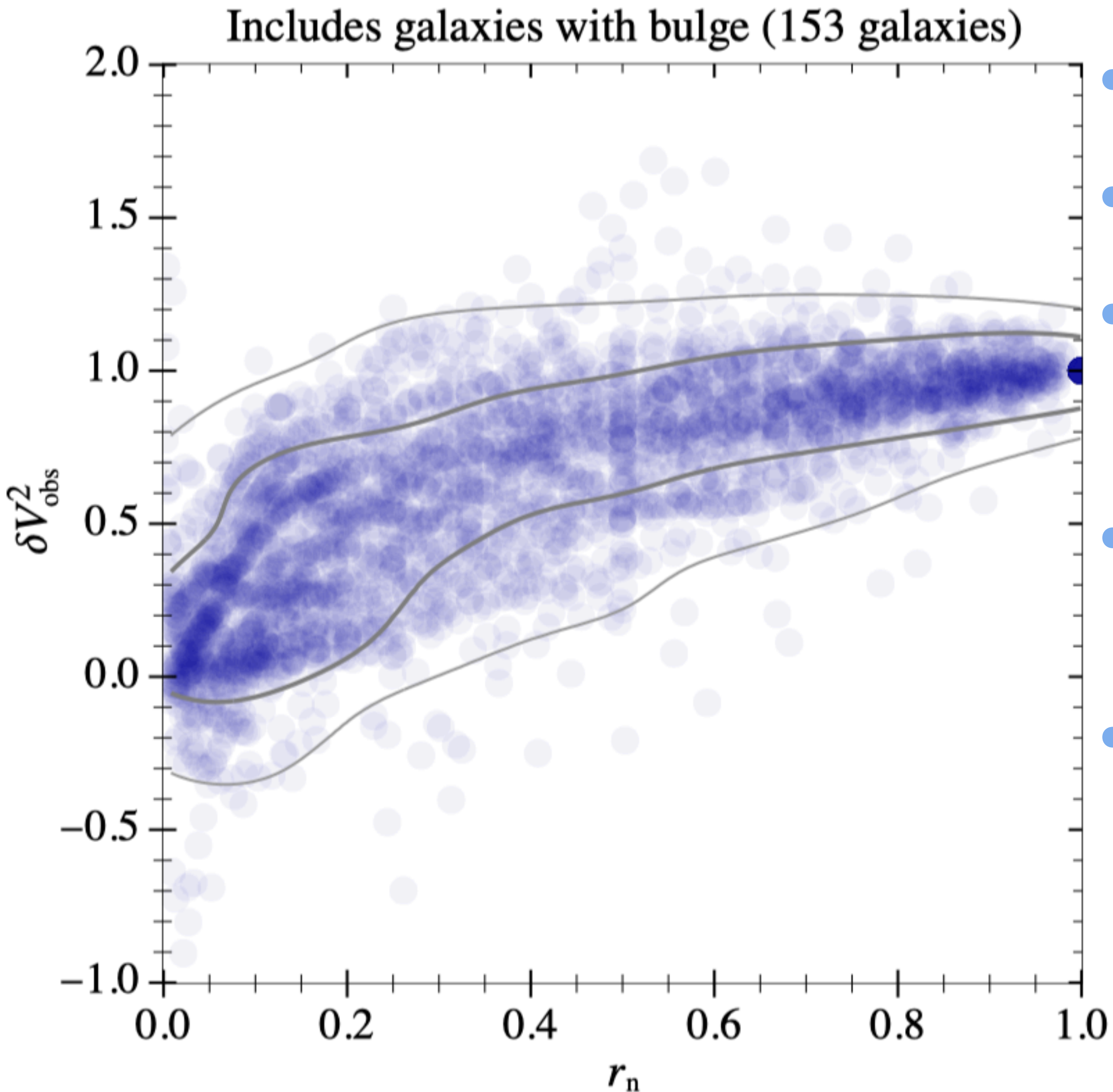
(Newtonian gravity without DM  $\implies \Delta V_{\text{obs}}^2 \sim 0$ , i.e., small oscillations about zero)

- And the *normalized additional velocity*, as function of  $r_n \equiv r/r_{\text{max}}$ , reads

$$\delta V_{\text{obs}}^2(r_n) \equiv \frac{\Delta V_{\text{obs}}^2(r_n r_{\text{max}})}{\Delta V_{\text{obs}}^2(r_{\text{max}})} .$$

(Newtonian gravity without DM  $\implies \delta V_{\text{obs}}^2(r_n)$  oscillate with arbitrary magnitude)

# The NAV distribution form the SPARC data



- This plot is model independent.
- Each blue circle is a data point from a galaxy.
- All the 153 galaxies have a point at  $(r_n, \delta V_{\text{obs}}^2) = (1,1)$ .
- The gray curves delimit the  $1\sigma$  and  $2\sigma$  highest density regions.
- If there was no dark matter, this plane should be randomly populated, without preference for  $\delta V_{\text{obs}}^2 > 0$ .

# First application: Burkert profile

$$\rho_{\text{Bur}}(r) = \frac{\rho_c}{(1 + r/r_c)(1 + r^2/r_c^2)} .$$

Two free parameters

In the above,  $r$  is the spherical radial coordinate, while  $r_c$  and  $\rho_c$  are constants that can change from galaxy to galaxy.

The internal mass of the Burkert profile reads,

$$\begin{aligned} M_{\text{Bur}}(r) &= 4\pi \int_0^r \rho_{\text{Bur}}(r) r^2 dr \\ &= 2\pi \rho_c r_c^3 \xi\left(\frac{r}{r_c}\right), \end{aligned} \quad (10)$$

where

$$\xi(x) \equiv \ln\left((1+x)\sqrt{1+x^2}\right) - \tan^{-1}(x). \quad (11)$$

It is convenient to introduce the normalized core radius

$$r_{\text{cn}} \equiv \frac{r_c}{r_{\text{max}}} .$$

Using that, for a spherical mass distribution,  $V^2(r)$ , we can now compute  $\Delta V_{\text{mod}}^2$  and  $\delta V_{\text{mod}}^2$  as

$$\Delta V_{\text{Bur}}^2(r_n) = 2\pi \frac{G\rho_c r_c^3}{r_{\text{max}}} \frac{1}{r_n} \xi\left(\frac{r_n}{r_{\text{cn}}}\right),$$

$$\delta V_{\text{Bur}}^2(r_n) = \frac{1}{r_n} \frac{\xi(r_n/r_{\text{cn}})}{\xi(1/r_{\text{cn}})} .$$

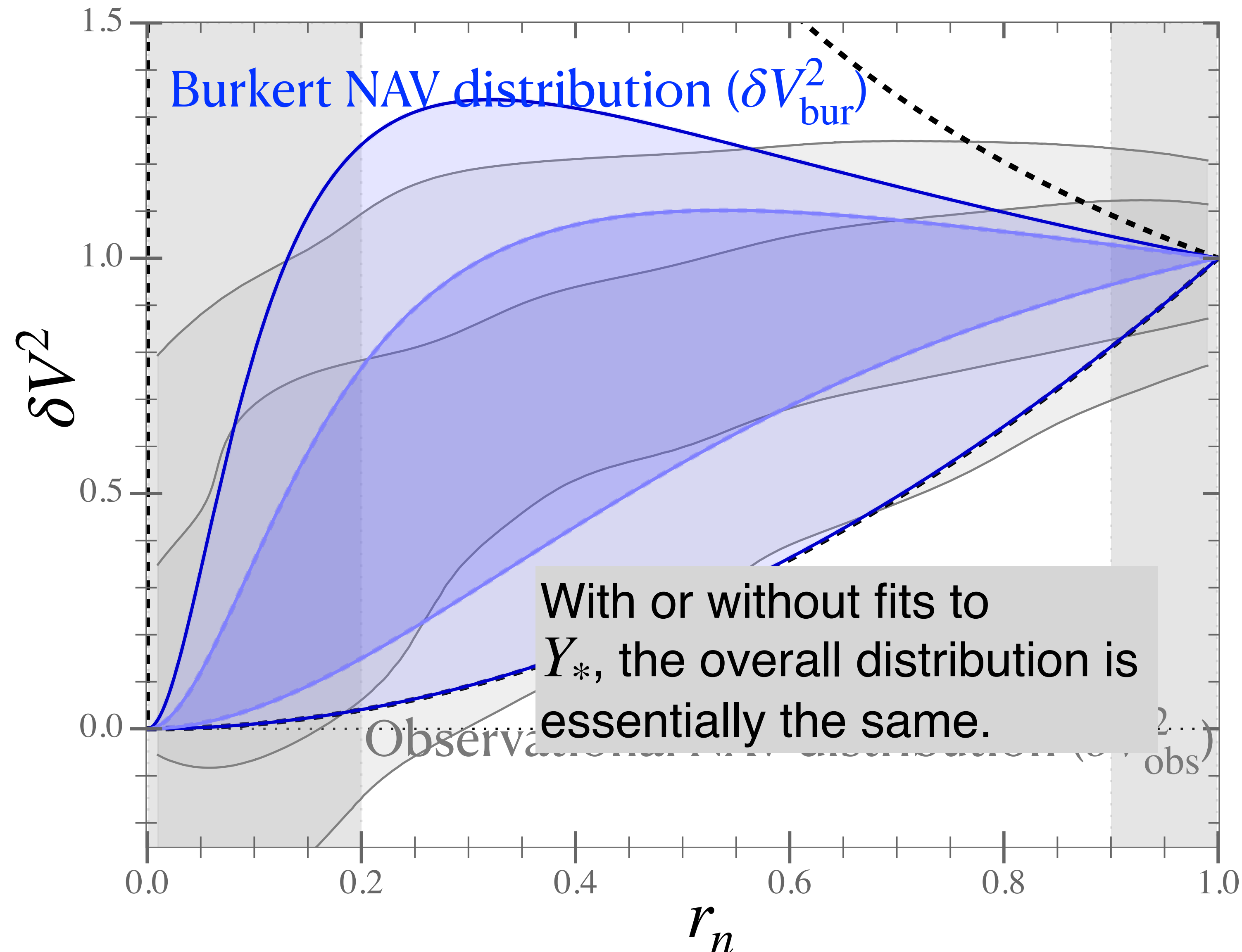
One free parameter

Model NAV: it will be compared with  $\delta V_{\text{obs}}^2$

# Burkert profile's NAV

Results valid for any  $\rho_c$

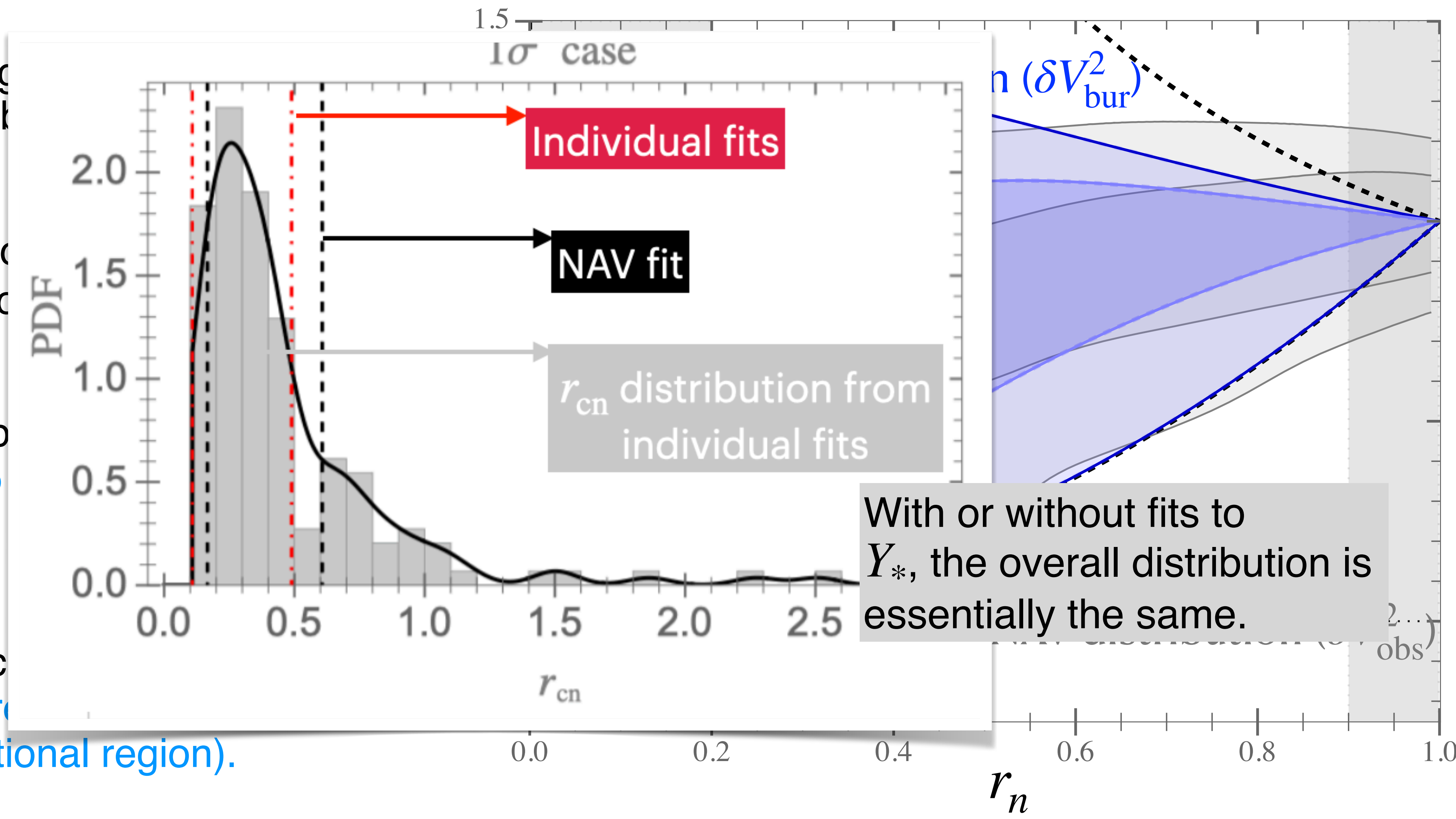
- ▶ Instead of fitting individual galaxies, one fits the distribution.
- ▶  $r_{cn}$  is fitted to mimic the  $\delta V_{obs}^2$  distribution as close as possible.
- ▶ The most probable values of  $r_{cn}$  :  
 $0.2 < r_{cn} < 0.6$  ( $1\sigma$  region, NAV).  
 $0.1 < r_{cn} < 0.5$  ( $1\sigma$  region, individual)
- ▶ Efficiency coefficient:  $0.74$   
 $\propto$  (Intersection region – Model region beyond observational region).



# Burkert profile's NAV

Results valid for any  $\rho_c$

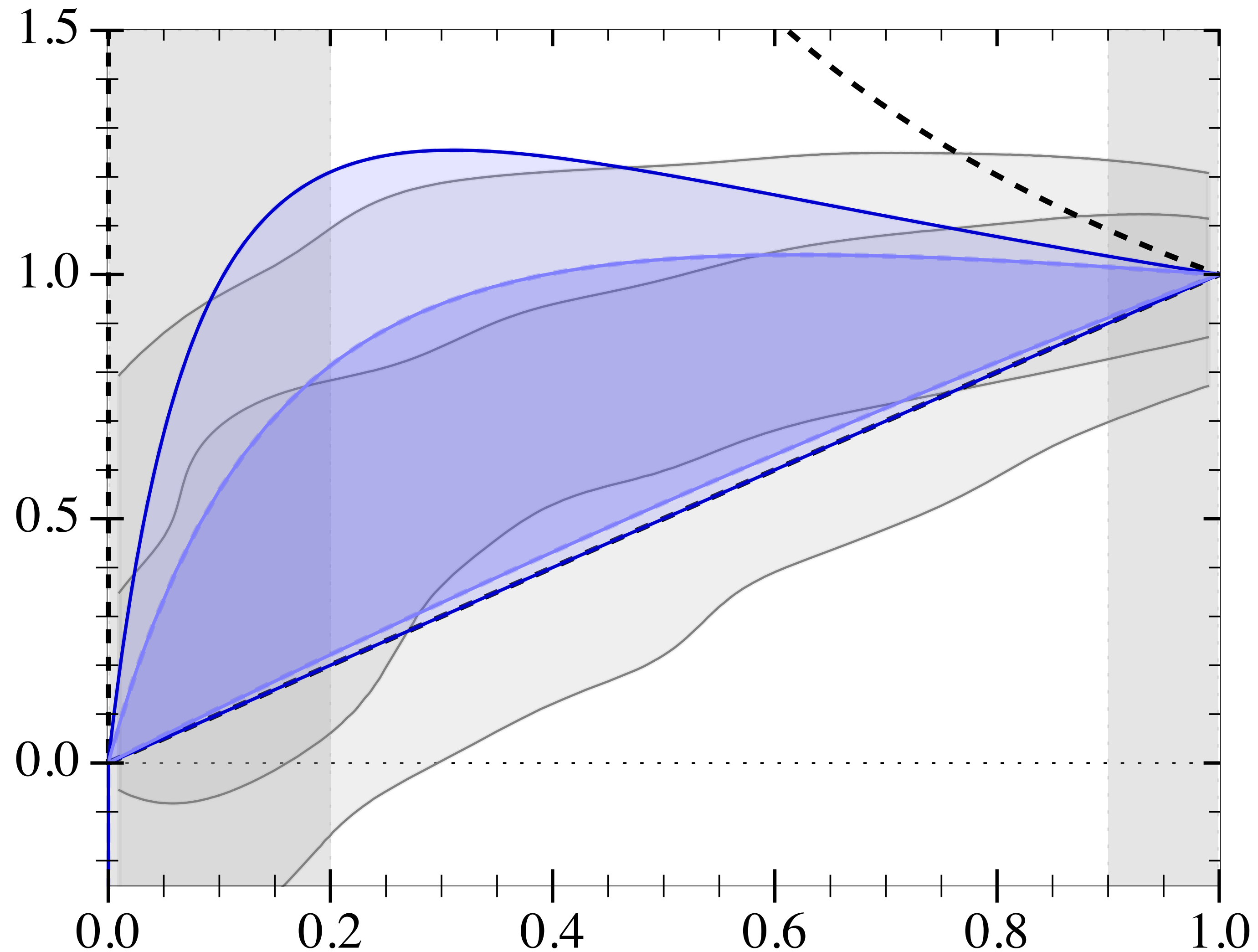
- ▶ Instead of fitting one fits the distribution
- ▶  $r_{cn}$  is fitted to distribution as close
- ▶ The most probable  $0.2 < r_{cn} < 0.6$   
 $0.1 < r_{cn} < 0.5$
- ▶ Efficiency coefficient  $\propto$  (Intersection ratio beyond observational region).



# NFW profile's NAV

$$\rho_{\text{NFW}} = \frac{\rho_s}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

- ▶ Are there  $r_{\text{sn}}$  values that can cover a large part of the  $\delta V_{\text{obs}}^2$  region? **ANS: Yes, but problems in the lower part of the plot.**
- ▶ The most probable values of  $r_{\text{cn}}$   
 **$0.29 < r_{\text{sn}} < 9.9$**
- ▶ Efficiency coefficient: **0.67**



Results valid for any  $\rho_s$



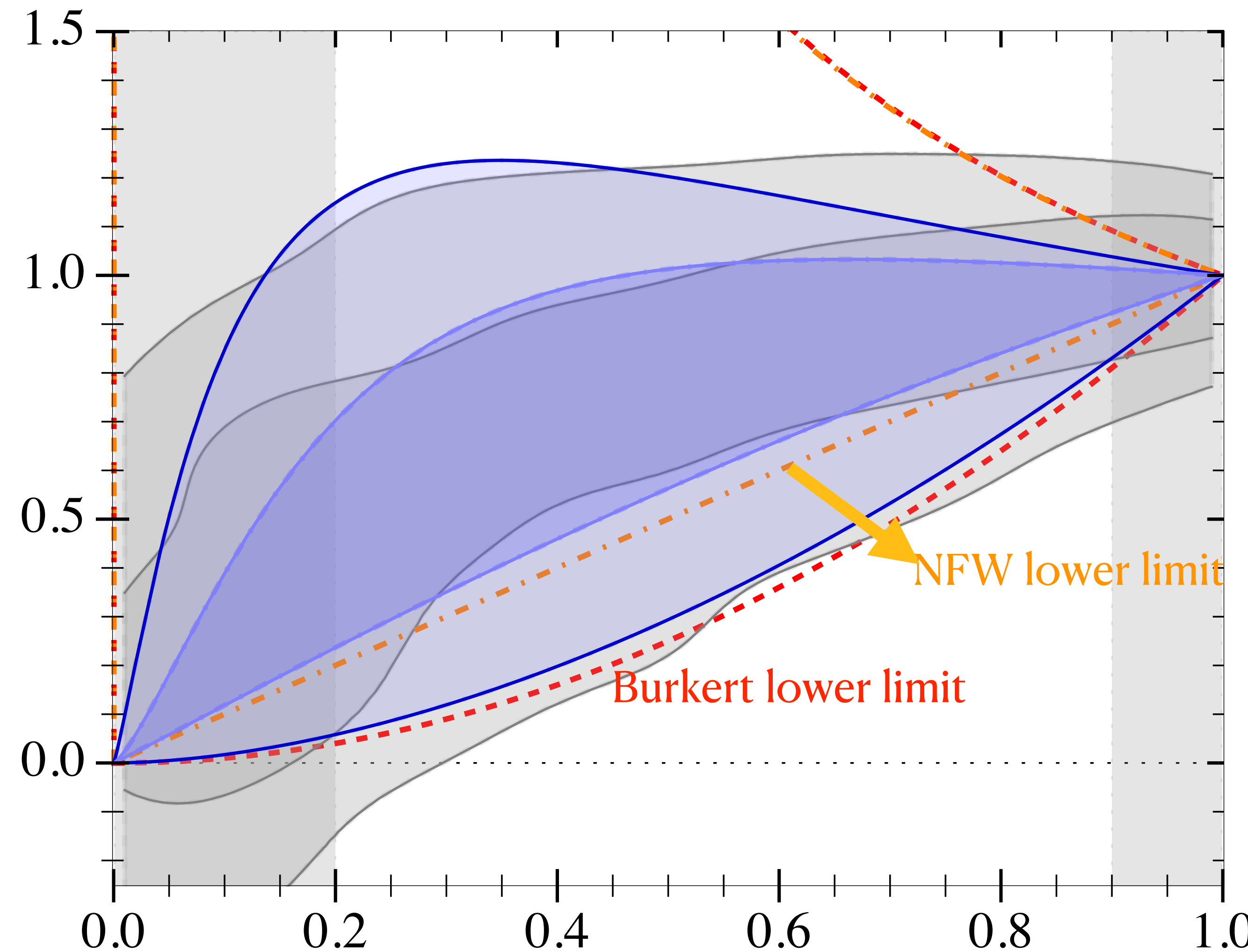
# DC14 profile NAV

[Di Cintio et al MNRAS 2014]

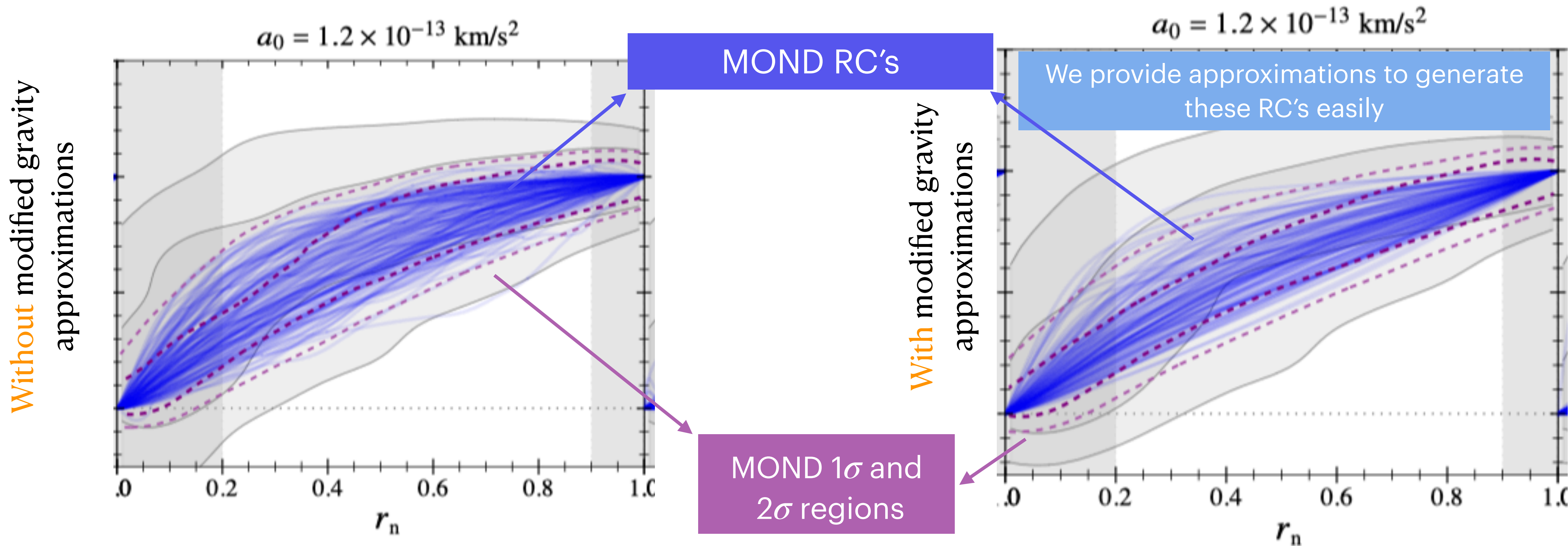
$$\rho_{\text{DC14}} = \frac{\rho_s}{\frac{r^\gamma}{r_s^\gamma} \left( 1 + \frac{r^\alpha}{r_s^\alpha} \right)^{(\beta-\gamma)/\alpha}}$$

Where  $\alpha, \beta, \gamma$  depend on a quantity  $X$ , which depends on the stellar mass of the galaxy.

- ▶ Is there  $r_{\text{sn}}$  values that can cover a large part of the  $\delta V_{\text{obs}}^2$  region? **ANS: Yes.**
- ▶ Efficiency: **0.80**



# MOND's NAV



- MOND's result is excessively concentrated: much less diversity. **Efficiency: 0.53**. ( $\chi^2$  values of MOND are much larger than those of DM).
- With or without approximations, the results are the same.

# f(R) Palatini NAV (identical results for EiBI)

$$S[g, \Gamma, \Psi] = \frac{1}{2\kappa} \int f(R(\Gamma, g)) \sqrt{-g} d^4x + S_{\text{matter}}[g, \Psi],$$

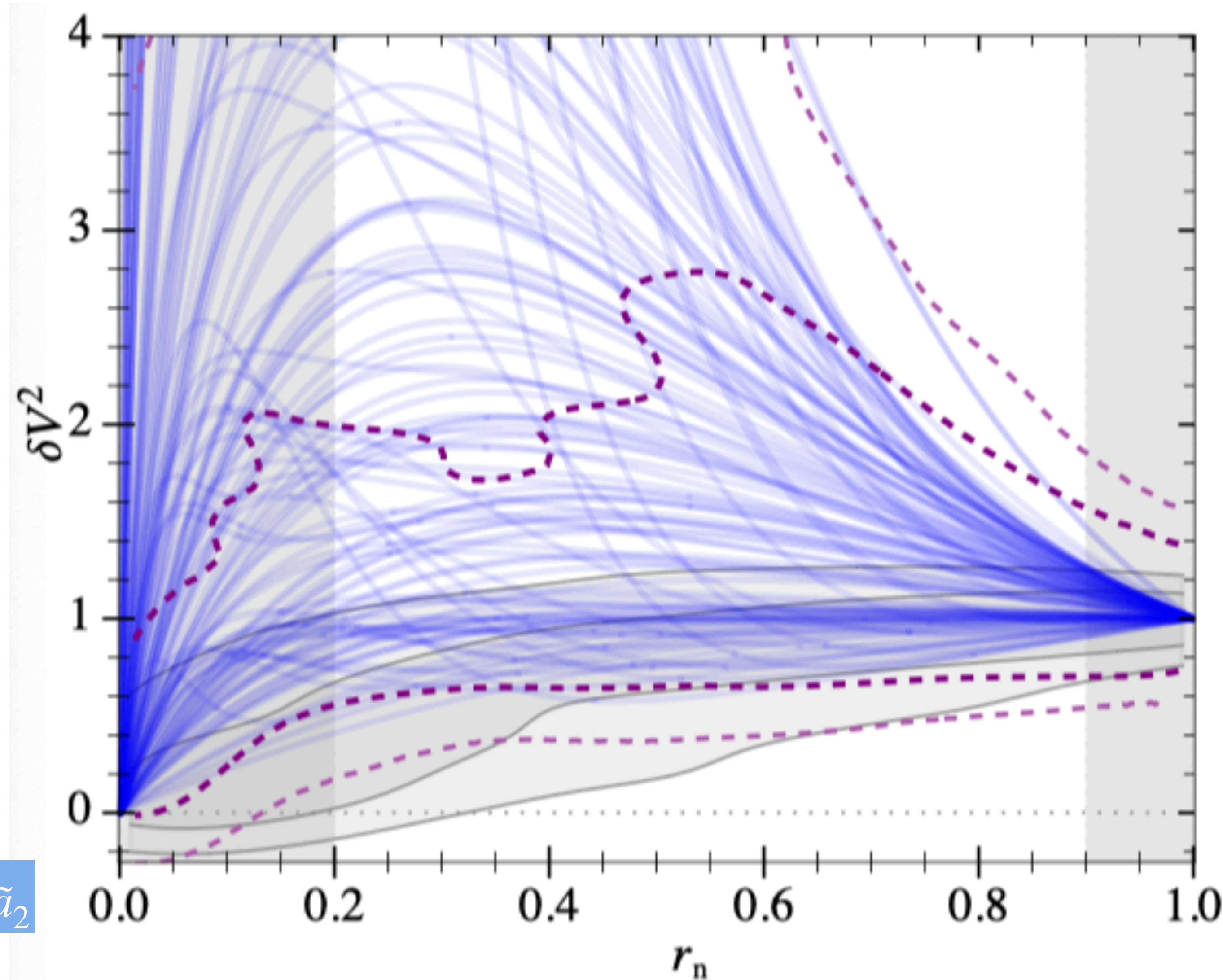
$$\frac{V_c^2}{r} = \partial_r U + \tilde{a}_2 \partial_r \rho$$

$$\Delta V_c^2 = r \tilde{a}_2 \partial_r \rho$$

$$\delta V_{\text{Palatini}}^2(r_n) = r_n \frac{\rho'(r_n)}{\rho'(1)}$$

Efficiency:  $< -2.0$

Independent from  $\tilde{a}_2$



# Conclusions

- For large surveys, efficient ways to compare DM and MG models are relevant.
- It is particularly difficult to study MG in individual galaxies: Time consuming and data availability are issues.
- The NAV method provides fast results for an important RC feature: its shape.
- Some results:
  - Most NAV efficient DM models: DC14 > Burkert > NFW  
Besides cusp/core, it is relevant to consider the intermediate radial dependence.
  - MOND RC's lack diversity. For stronger issues: [Rodrigues et al Nat.Ast. 2018]
  - Palatini  $f(R)$  and EiBI gravity: they cannot be used to replace DM in galaxies.
- Further details in [Hernandez-Arboleda, Rodrigues, Wojnar 2204.03762].  
The code can be found here: <https://github.com/davi-rodrigues/NAVanalysis>