

Null test BSM searches with rare charm baryon decays

Marcel Golz

based on

JHEP 09 (2021) 208; [[arxiv:2107.13010](https://arxiv.org/abs/2107.13010)] MG, G. Hiller, T. Magorsch

11th International Workshop on the CKM Unitarity Triangle

24th November 2021



- ▶ Part I - Introduction to rare charm decays
 - ▶ Effective field theory framework
 - ▶ Null test overview
 - ▶ Baryon modes
- ▶ Part II - Null tests with baryons
 - ▶ Forward-backward asymmetry
 - ▶ F_L
 - ▶ LU ratios
 - ▶ CP-violation
- ▶ Outlook

A soft-focus photograph of the Melbourne city skyline, featuring the Eureka Tower and other modern skyscrapers reflected in the Yarra River. In the foreground, palm trees and a bridge are visible.

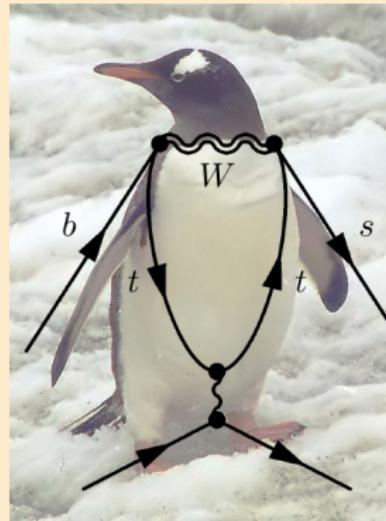
Part I - Introduction rare charm decays



EFT at the charm scale

de Boer, (2017), PhD thesis, TU Dortmund

What is the difference between $b \rightarrow s$ and $c \rightarrow u$ penguins?

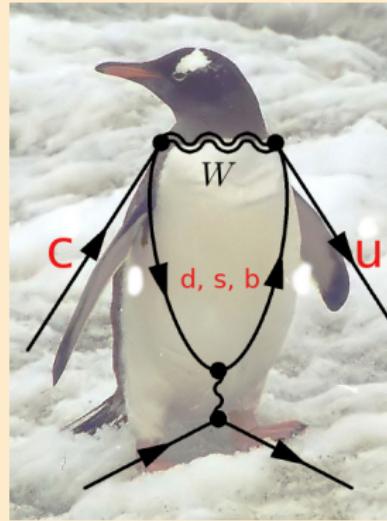




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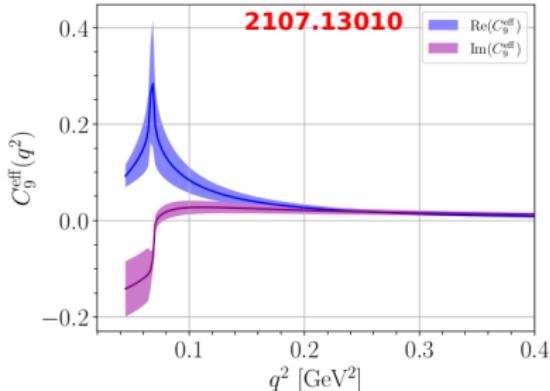
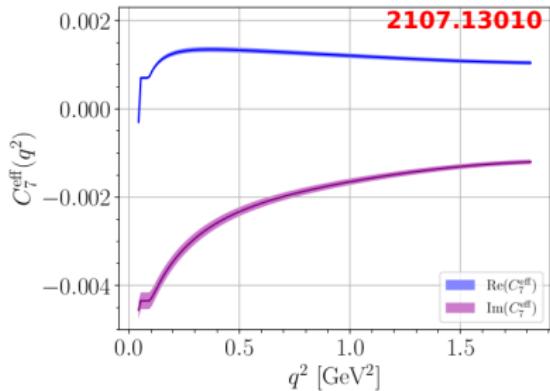


EFT at the charm scale

de Boer, (2017), PhD thesis, TU Dortmund

What is the difference between $b \rightarrow s$ and $c \rightarrow u$ penguins?

- ▶ Light quark masses need to be set to zero at μ_W
- ▶ Effective GIM-mechanism kills $C_{7,9,10}$ at μ_W
- ▶ $C_{7,9}^{\text{eff}}$ are induced by RG running to μ_c
- ▶ $C_{10}(\mu_c) = 0$



$$\mathcal{H}_{\text{eff}} \supset -\frac{4G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \left[\sum_{i=7,9,10,S,P} (c_i o_i + c'_i o'_i) + \sum_{i=T,T5} c_i o_i \right],$$

$$O_7 = \frac{m_c}{e} (\bar{u}_L \sigma_{\mu\nu} c_R) F^{\mu\nu},$$

$$O_9 = (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \ell), \quad O_{10} = (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$$

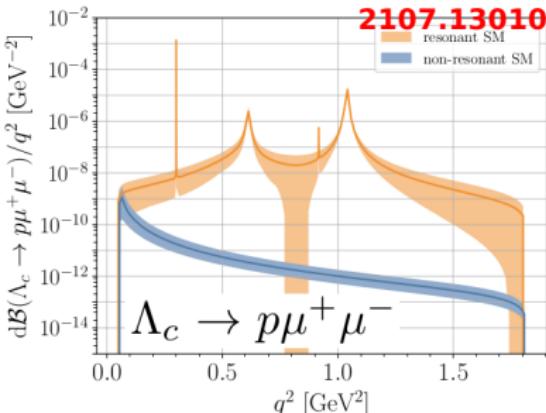
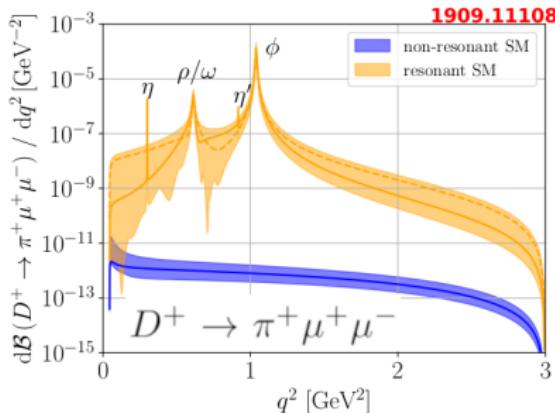
$$O_S = (\bar{u}_L c_R) (\bar{\ell} \ell), \quad O_P = (\bar{u}_L c_R) (\bar{\ell} \gamma_5 \ell),$$

$$O_T = \frac{1}{2} (\bar{u} \sigma_{\mu\nu} c) (\bar{\ell} \sigma^{\mu\nu} \ell), \quad O_{T5} = \frac{1}{2} (\bar{u} \sigma_{\mu\nu} c) (\bar{\ell} \sigma^{\mu\nu} \gamma_5 \ell).$$

- ▶ Primed operators obtained with $L \leftrightarrow R$
- ▶ $C_7^{\text{eff}} = \mathcal{O}(10^{-3})$, $C_9^{\text{eff}} = \mathcal{O}(10^{-2})$.
- ▶ $C_{10}^{(')} = C_S^{(')} = C_P^{(')} = 0$ and $C_T = C_{T5} = 0$



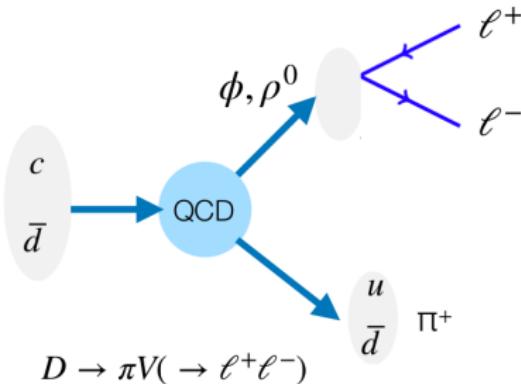
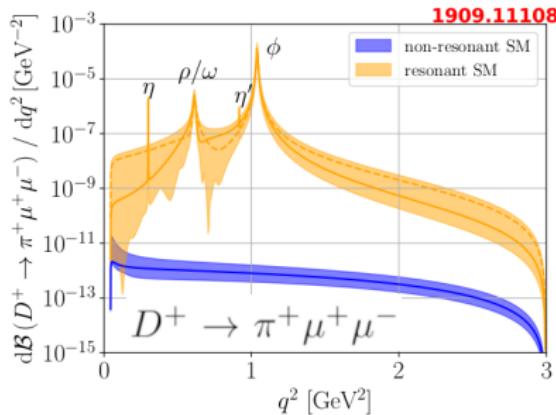
Introduction



- SM contributions dominated by long range dynamics
 $\mathcal{B}^{\text{SM}}(D \rightarrow \pi \ell^+ \ell^-) \approx \mathcal{B}(D \rightarrow \pi V(\rightarrow \ell^+ \ell^-))$
- Parametrized by a sum of Breit-Wigner contributions (fit from data)

$$C_9^R(q^2) = a_\omega e^{i\delta_\omega} \left(\frac{1}{q^2 - m_\omega^2 + i m_\omega \Gamma_\omega} - \frac{3}{q^2 - m_\rho^2 + i m_\rho \Gamma_\rho} \right) + \frac{a_\phi e^{i\delta_\phi}}{q^2 - m_\phi^2 + i m_\phi \Gamma_\phi}.$$

$$C_P^R(q^2) = \frac{a_\eta e^{i\delta_\eta}}{q^2 - m_\eta^2 + i m_\eta \Gamma_\eta} + \frac{a_{\eta'}}{q^2 - m_{\eta'}^2 + i m_{\eta'} \Gamma_{\eta'}}$$



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 $\mathcal{B}^{\text{SM}}(D \rightarrow \pi \ell^+ \ell^-) \approx \mathcal{B}(D \rightarrow \pi V(\rightarrow \ell^+ \ell^-))$
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- ▶ Parameters in C_9^R , C_P^R are main source of uncertainties
- ▶ Process dependent [1909.11108](#), [1805.08516](#)

	a_ρ / GeV^2	a_ϕ / GeV^2	a_η / GeV^2	$a_{\eta'} / \text{GeV}^2$
$D^+ \rightarrow \pi^+$	~ 0.2	~ 0.2	$\sim 6 \times 10^{-4}$	$\sim 8 \times 10^{-4}$
$D^0 \rightarrow \pi^0$	~ 0.9	~ 0.3	$\sim 5 \times 10^{-4}$	$\sim 8 \times 10^{-4}$
$D_s^+ \rightarrow K^+$	~ 0.5	~ 0.1	$\sim 6 \times 10^{-4}$	$\sim 7 \times 10^{-4}$
$D^0 \rightarrow \pi^+\pi^-$	~ 0.7	~ 0.3	$\sim 1 \times 10^{-3}$	$\sim 1 \times 10^{-3}$
$D^0 \rightarrow K^+K^-$	~ 0.7	—	$\sim 3 \times 10^{-4}$	—



- ▶ Parameters in C_9^R , C_P^R are main source of uncertainties
- ▶ Process dependent [1909.11108](#), [1805.04025](#)

	$\Lambda_c \rightarrow p$	$\Xi_c^+ \rightarrow \Sigma^+$	$\Xi_c^0 \rightarrow \Sigma^0$	$\Xi_c^0 \rightarrow \Lambda^0$	$\Omega_c^0 \rightarrow \Xi^0$	
$D^+ \rightarrow \pi^+$	a_ω	0.062 ± 0.009	~ 0.06	~ 0.06	~ 0.06	~ 0.05
$D^0 \rightarrow \pi^0$	a_ω	0.110 ± 0.008	~ 0.1	~ 0.1	~ 0.1	~ 0.09
$D_s^+ \rightarrow K^+$	a_ϕ	0.110 ± 0.008	~ 0.1	$\sim 5 \times 10^{-4}$	$\sim 6 \times 10^{-4}$	$\sim 8 \times 10^{-4}$
$D^0 \rightarrow \pi^+\pi^-$	a_ϕ	0.110 ± 0.008	~ 0.3	$\sim 1 \times 10^{-3}$	$\sim 1 \times 10^{-3}$	$\sim 7 \times 10^{-4}$
$D^0 \rightarrow K^+K^-$		~ 0.7	—	$\sim 3 \times 10^{-4}$	—	$\sim 1 \times 10^{-3}$

$[r/\text{GeV}^2]$

[2107.13010](#)



- ▶ Parameters in C_9^R , C_P^R are main source of uncertainties
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$D^0 \rightarrow K^+K^-$		~ 0.7	—	$\sim 3 \times 10^{-4}$	—	$\sim 7 \times 10^{-4}$

2107.13010

- ▶ With more data model parameters (a_i , δ_i) can be constrained and the model can be improved.



- ▶ Rare charm decays observed only at the resonances, for the rest of the signal region U.L. are available at 90 % C.L. (see [2011.09478](#))
 - ▶ $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 6.2 \times 10^{-9}$
 - ▶ $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-) < 6.7 \times 10^{-8}$
 - ▶ $\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-) < 5.5 \times 10^{-7}$
 - ▶ $\mathcal{B}(\Lambda_c \rightarrow p \mu^+ \mu^-) < 7.7 \times 10^{-8}$
 - ▶ **New results from LHCb [2111.03327](#)**

Direct bounds on WC's from $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$, $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-)$ imply

- ▶ $C_{S,P} \lesssim \mathcal{O}(0.1) \quad C_{7,9,10,T,T5} \lesssim \mathcal{O}(1)$



NP searches in branching ratios are challenging.

Instead define null test observables where

Signal \leftrightarrow **NP**

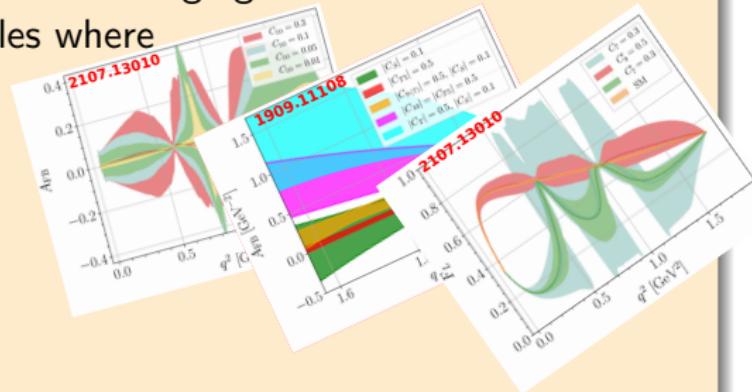


NP searches in branching ratios are challenging.

Instead define null test observables where

Signal \leftrightarrow NP

- ▶ Angular observables



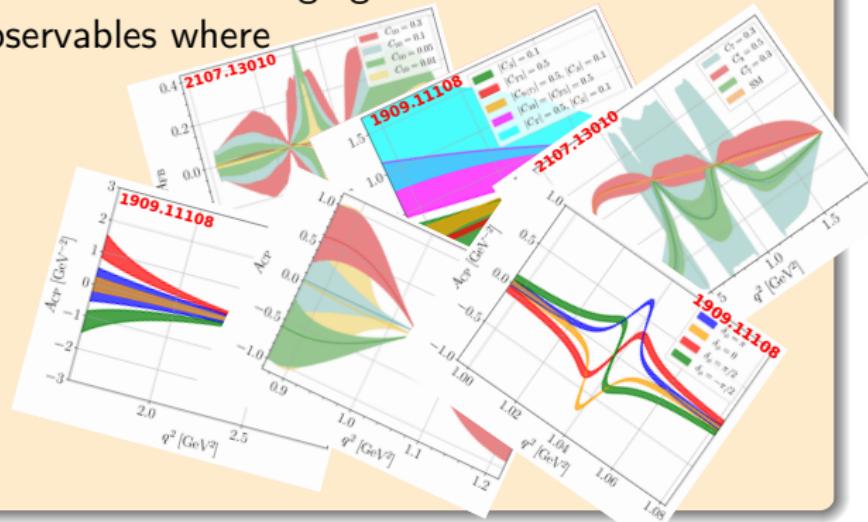


NP searches in branching ratios are challenging.

Instead define null test observables where

Signal \leftrightarrow NP

- ▶ Angular observables
- ▶ CP-asymmetries



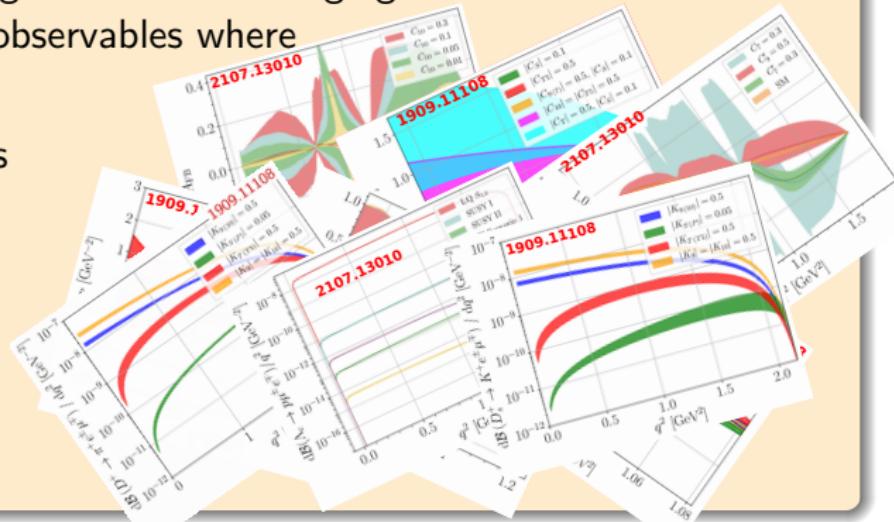


NP searches in branching ratios are challenging.

Instead define null test observables where

Signal \leftrightarrow NP

- ▶ Angular observables
- ▶ CP-asymmetries
- ▶ LFV



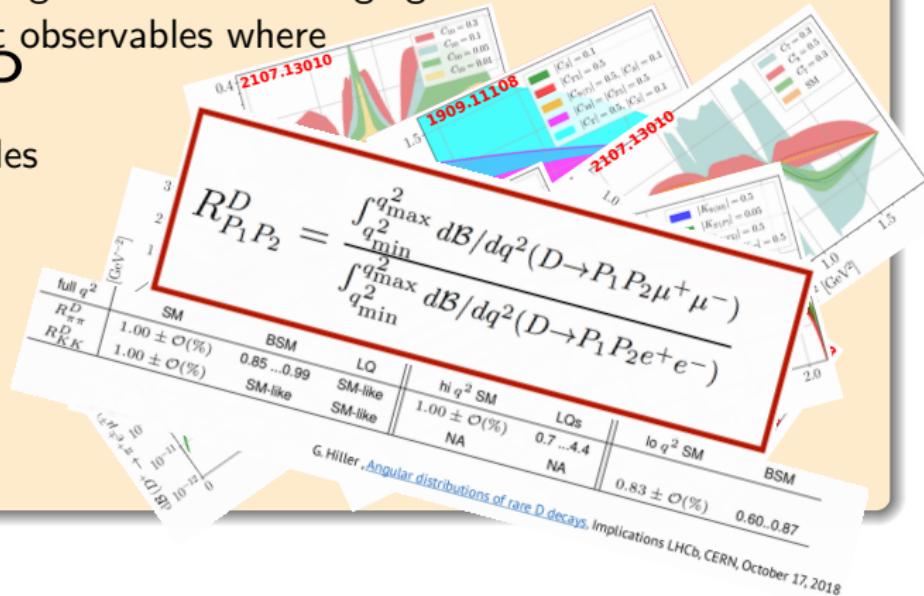


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Instead define null test observables where

Signal \leftrightarrow NP

- ▶ Angular observables
- ▶ CP-asymmetries
- ▶ LFV
- ▶ LU ratios



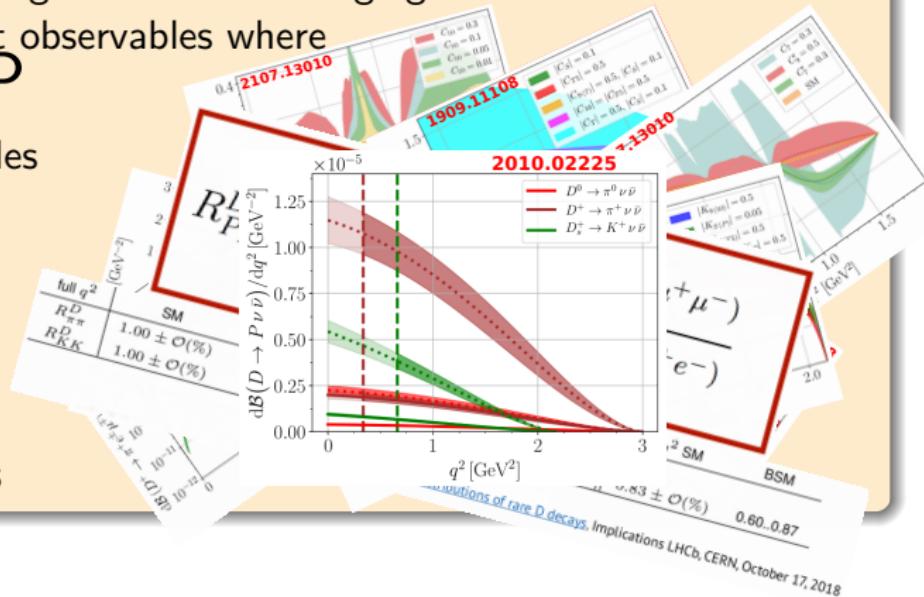


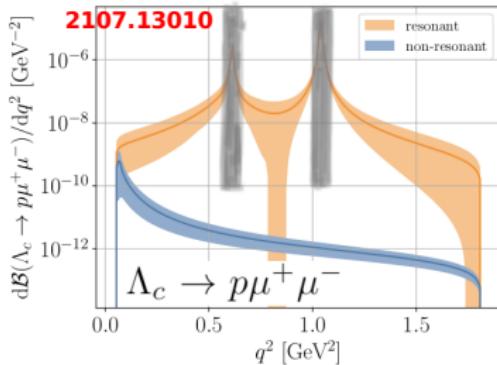
NP searches in branching ratios are challenging.

Instead define null test observables where

Signal \leftrightarrow NP

- ▶ Angular observables
- ▶ CP-asymmetries
- ▶ LFV
- ▶ LU ratios
- ▶ Dineutrino modes





- LHCb upper limit at 90 % C.L. with ± 40 MeV cuts around known resonance masses, then extrapolated to full q^2 region

$$\mathcal{B}_{\text{LHCb}}(\Lambda_c \rightarrow p\mu^+\mu^-) < 7.7 \times 10^{-8}$$

- Including form factor and resonance uncertainties and integrating the LHCb search region

$$\mathcal{B}^{\text{SM}}(\Lambda_c \rightarrow p\mu^+\mu^-) = (1.9^{+1.8}_{-1.5}) \times 10^{-8}$$

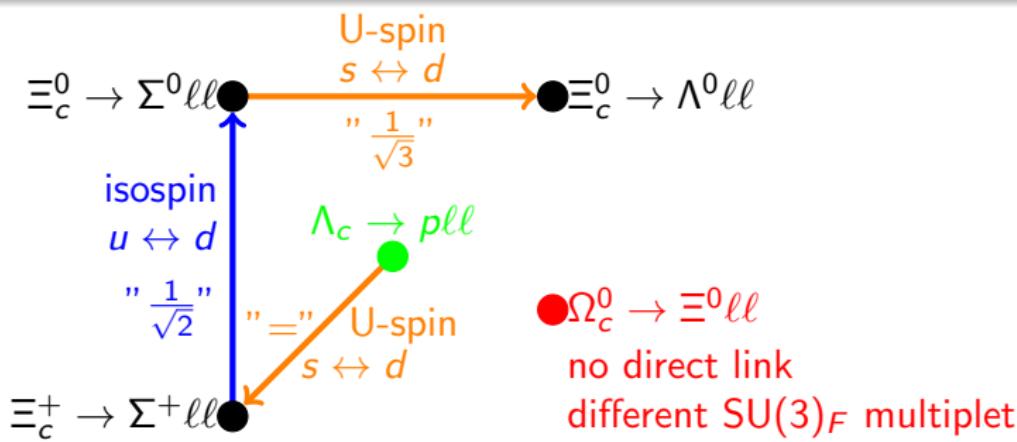
$$\mathcal{B}^{\text{SM}}(\Xi_c^+ \rightarrow \Sigma^+ \mu^+\mu^-) \sim 1.8 \times \mathcal{B}^{\text{SM}}(\Lambda_c \rightarrow p\mu^+\mu^-)$$

$$\mathcal{B}^{\text{SM}}(\Xi_c^0 \rightarrow \Sigma^0 \mu^+\mu^-) \sim 0.4 \times \mathcal{B}^{\text{SM}}(\Lambda_c \rightarrow p\mu^+\mu^-)$$

$$\mathcal{B}^{\text{SM}}(\Omega_c^0 \rightarrow \Xi^0 \mu^+\mu^-) \sim 1.3 \times \mathcal{B}^{\text{SM}}(\Lambda_c \rightarrow p\mu^+\mu^-)$$



- ▶ Form factors are available for $\Lambda_c \rightarrow p\mu^+\mu^-$ from Lattice QCD (see 1712.05783)
- ▶ No results for other decay modes (from the lattice) available yet.
- ▶ Use $SU(3)_F$ flavor symmetries to relate modes



The background of the slide features a soft-focus photograph of a city skyline, likely Melbourne, Australia. It includes several prominent skyscrapers, a bridge spanning a river in the foreground, and palm trees along the waterfront.

Part II - Null tests with baryons

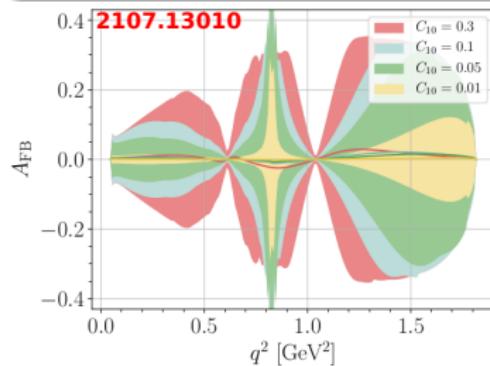


$\Lambda_c \rightarrow p\mu^+\mu^-$ decay distribution:

$$\frac{d\Gamma}{dq^2 d \cos \theta_\ell} = \frac{3}{2} (K_{1ss} \sin^2 \theta_\ell + K_{1cc} \cos^2 \theta_\ell + K_{1c} \cos \theta_\ell),$$

$$A_{FB} = \frac{1}{d\Gamma/dq^2} \left[\int_0^1 - \int_{-1}^0 \right] \frac{d\Gamma}{dq^2 d \cos \theta_\ell} d \cos \theta_\ell = \frac{3}{2} \frac{K_{1c}}{2K_{1ss} + K_{1cc}}.$$

$K_{1c} \sim C_9 C_{10}$, $C'_9 C'_{10}$ and $C_7^{(\prime)} C_{10}^{(\prime)}$ interference terms \Rightarrow no SM.





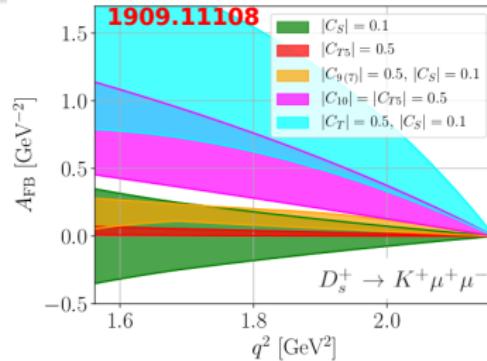
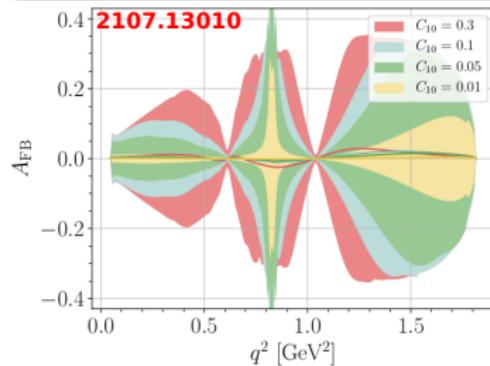
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$K_{1c} \sim C_9 C_{10}$, $C'_9 C'_{10}$ and $C_7^{(i)} C_{10}^{(i)}$ interference terms \Rightarrow no SM.

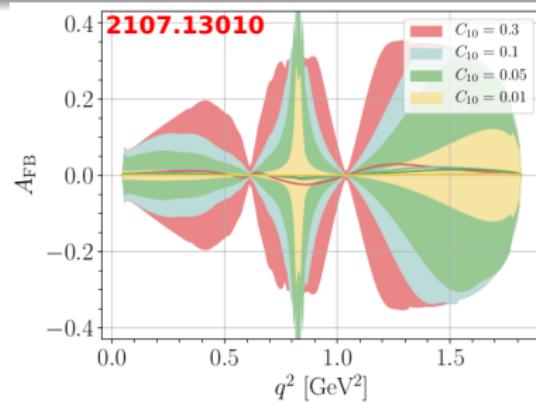
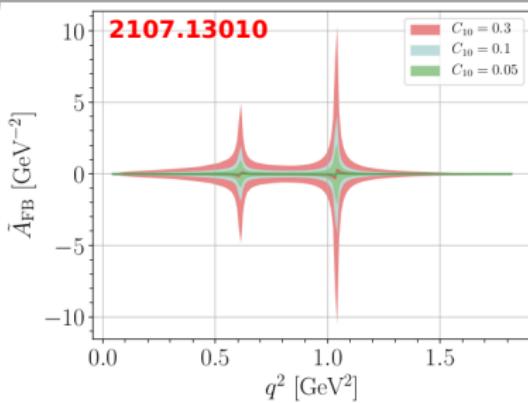
Complementary results in $D \rightarrow P\mu^+\mu^-$ (Normalized to integrated rate)





Normalization matters

- ▶ $\tilde{A}_{FB} = \frac{3}{2} \frac{K_{1c}}{\Gamma}$ with $\Gamma = \int_{q^2_{\min}}^{q^2_{\max}} (2 K_{1ss} + K_{1cc})$
- ▶ $A_{FB} = \frac{3}{2} \frac{K_{1c}}{d\Gamma/dq^2}$ with $d\Gamma/dq^2 = 2 K_{1ss} + K_{1cc}$
- ▶ Resonance enhancement

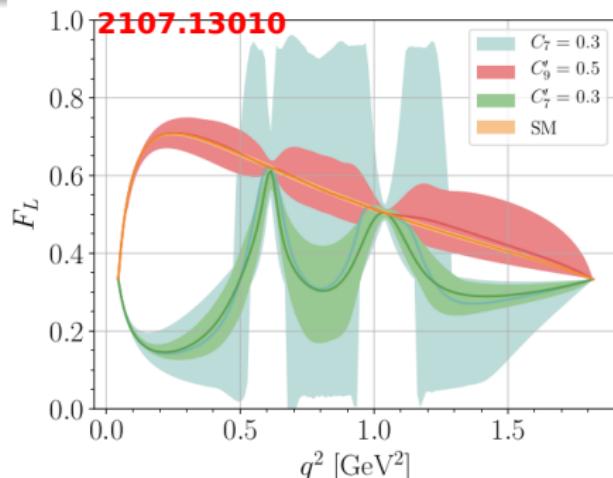
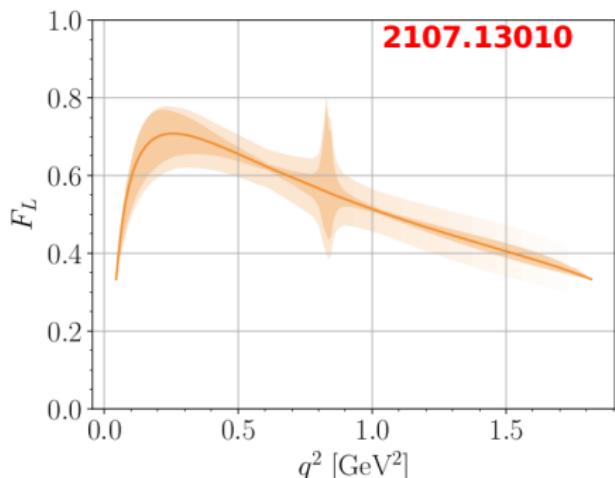




Fraction of longitudinally polarized dimuons

$$F_L = \frac{2K_{1ss} - K_{1cc}}{2K_{1ss} + K_{1cc}}$$

No null test, but cancellation of hadronic uncertainties in the SM and highly sensitive to $C_7^{(\prime)}$.





$$R_\pi^D = \left. \int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(D \rightarrow \pi \mu^+ \mu^-)}{dq^2} dq^2 \right/ \int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(D \rightarrow \pi e^+ e^-)}{dq^2} dq^2$$

R_π^D	SM	$ C_9 = 0.5$	$ C_{10} = 0.5$	$ C_9 = \pm C_{10} = 0.5$
full q^2	$1.00 \pm \mathcal{O}(\%)$	SM-like	SM-like	SM-like
low q^2	$0.95 \pm \mathcal{O}(\%)$	$\mathcal{O}(100)$	$\mathcal{O}(100)$	$\mathcal{O}(100)$
high q^2	$1.00 \pm \mathcal{O}(\%)$	$0.2 \dots 11$	$3 \dots 7$	$2 \dots 17$

1909.11108



	R_π^D	$R_p^{\Lambda_c}$
SM	$\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(D \rightarrow \pi \mu^+ \mu^-)}{dq^2} dq^2 / \int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(\Lambda_c \rightarrow p e^+ e^-)}{dq^2} dq^2$	$\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(\Lambda_c \rightarrow p \mu^+ \mu^-)}{dq^2} dq^2 / \int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(\Lambda_c \rightarrow p e^+ e^-)}{dq^2} dq^2$
full q^2	$1.00 \pm \mathcal{O}(\%)$	$ C_9^\mu = 0.5 C_{10}^\mu = 0.5$
low q^2	$0.94 \pm \mathcal{O}(\%)$	SM-like
high q^2	$1.00 \pm \mathcal{O}(\%)$	$7.5 \dots 20$

2107.13010



$$R_{\pi}^D = \int_{q_{\min}^2}^{q_{\max}^2} \frac{d\sigma^2}{dq^2} d\mathcal{B}(\Lambda_c \rightarrow p e^+ e^-) dq^2$$

$$R_{P_1 P_2}^D = \frac{\int_{q_{\min}^2}^{q_{\max}^2} dB/dq^2 (D \rightarrow P_1 P_2 \mu^+ \mu^-)}{\int_{q_{\min}^2}^{q_{\max}^2} dB/dq^2 (D \rightarrow P_1 P_2 e^+ e^-)}$$

$\leq |C_9^{\prime\mu}| = |C_{10}^{\prime\mu}| = 0.5$
SM-like
8.2 ... 26
 $\mathcal{O}(100)$

full q^2	SM	BSM	LQ	hi q^2 SM	LQs	lo q^2 SM	BSM
$R_{\pi\pi}^D$	$1.00 \pm \mathcal{O}(\%)$	0.85 ... 0.99	SM-like	$1.00 \pm \mathcal{O}(\%)$	NA	0.83 $\pm \mathcal{O}(\%)$	0.60 ... 0.87
R_{KK}^D	$1.00 \pm \mathcal{O}(\%)$	SM-like	SM-like	NA	0.7 ... 4.4	NA	
full q^2	SM						
low q^2	$1.00 \pm \mathcal{O}(\%)$	7.5 ... 20	$\mathcal{O}(100)$				
high q^2	$0.94 \pm \mathcal{O}(\%)$						

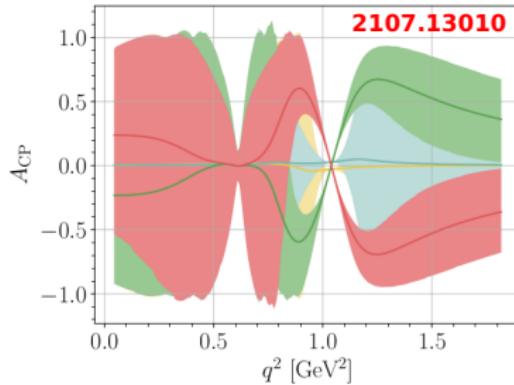
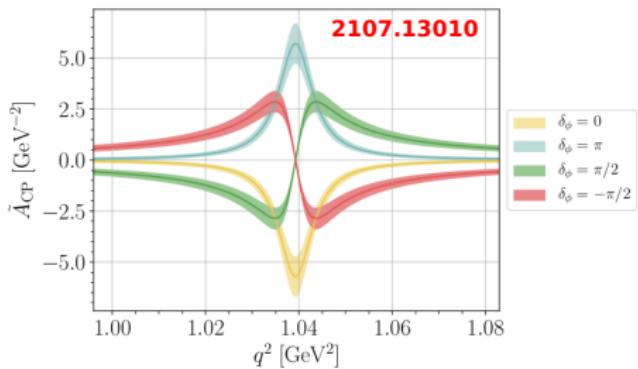
G. Hiller, *Angular distributions of rare D decays, Implications LHCb, CERN, October 17, 2018*

1805.08516



$$\tilde{A}_{\text{CP}}(q^2) = \frac{1}{\Gamma + \bar{\Gamma}} \left(\frac{d\Gamma}{dq^2} - \frac{d\bar{\Gamma}}{dq^2} \right) \quad \text{with} \quad \Gamma = \int_{q^2_{\min}}^{q^2_{\max}} \frac{d\Gamma}{dq^2} dq^2 \quad \text{Or} \quad A_{\text{CP}}(q^2) = \frac{\frac{d\Gamma}{dq^2} - \frac{d\bar{\Gamma}}{dq^2}}{\frac{d\Gamma}{dq^2} + \frac{d\bar{\Gamma}}{dq^2}}$$

- ▶ Strong phase from resonances needed → measurement around the ϕ resonance. S. Fajfer and N. Kosnik [1208.0759](#)
- ▶ NP weak phase needed. → benchmark $C_9 = 0.5 \exp(i\pi/4)$.
- ▶ Binning necessary.

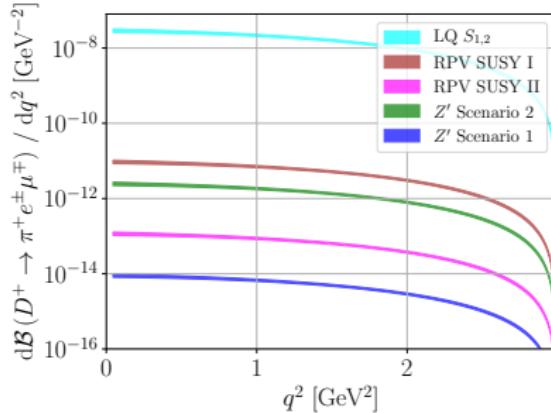
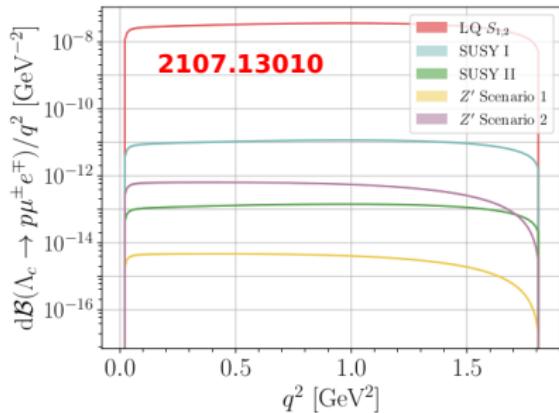




- ▶ Rare charm decays are dominated by long-distance resonance contributions
- ▶ NP can be probed in **clean null test** observables
- ▶ Plenty of opportunities with baryon modes
- ▶ Resonance enhancement turns the bug into a feature
- ▶ Different observables test different Wilson coefficients → complementarity

A soft-focus photograph of the Melbourne city skyline during the day. The Yarra River is in the foreground, with a bridge spanning it. Several prominent skyscrapers, including the Eureka Tower and the Rialto Towers, are visible against a bright sky.

BACKUP



LQ's ($K'_9 = K'_{10} = 0.5$),
 SUSY + R-parity violation ($K_9 = -K_{10} = 0.009$),
 SUSY no R-parity violation ($K_9 = -K_{10} = 0.001$),
 Z' 1 ($K_9 = K'_9 = -K_{10} = -K'_{10} = 1.4 \cdot 10^{-4}$),
 Z' 2 ($K_9 = K'_9 = -K_{10} = -K'_{10} = 2.3 \cdot 10^{-4}$).

